



# Article High Frequency Analysis and Optimization of Planar Spiral Inductors Used in Microelectronic Circuits

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**Copyright:** © 2021 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). **Abstract:** This paper deals with high frequency analysis of spiral inductors, used in microelectronics circuits, to optimize their configuration. Software developed, designed, and implemented by the authors for nano and micrometre spiral inductor high frequency analysis, named ABSIF, is presented in this paper. ABSIF determines the inductance, quality factor, and electrical parameters for square, hexagonal, octagonal, and circular spiral inductor design optimization optimization for energy efficiency. ABSIF is a good tool for spiral inductor design optimization in high frequency applications and takes into account the imposed technological limits and/or the designers' constraints. A set of spiral inductors are considered and analysed for high frequency values using ABSIF, and the results are presented in the paper. The validation of ABSIF was completed by comparing the results with those obtained using a similar commercial software, Sonnet Lite<sup>TM</sup>, which is dedicated to high frequency electromagnetic analysis.

**Keywords:** planar spiral inductors; microelectronic circuits; high frequency; analysis; optimal design; inductance; quality factor; energy efficiency; electrical and electronic parameters

## 1. Introduction

Spiral inductors are the main pawns in microelectronic circuits, thanks to the possibility of reducing their dimensions at the micro and nanometre order and increasing their frequency at the GHz order. For high performance microelectronic circuits, it is necessary to improve the performance of their essential components, such as spiral inductors [1-3]. Spiral inductors have a crucial role in integrated circuits that work at very high frequencies. Spiral inductors are especially used in the design of miniature wireless power supply devices such as mobile or smartwatch chargers, wireless routers, wireless control and monitoring devices, wireless communication devices, radiofrequency amplifiers and converters, filters, antennas, and others [4–11]. Most of the next generation devices, apparatus, and equipment are based on radiofrequency micrometric integrated circuits. To improve their performance and to better understand them, the analysis of each constructive element of the integrated circuit, specifically of the spiral inductors integrated into radiofrequency microelectronic circuits [12,13], using proper tools and software, is of great interest to the designers and engineers of these circuits. The accurate calculation and extraction of spiral inductor electronic and electrical parameters, using adequate methods that do not require long computation time, excessive computational resources, or high effort, are necessary. The integrated circuits must be modelled and simulated to understand, study, and analyse their behaviour as well as highlight the phenomena and effects that occur at high frequency at micrometric geometries [14-18]. To achieve these, the following specific research objectives were met in this article: the extraction of inductance, quality

factor, and electrical parameters for square, hexagonal, octagonal, and circular spiral inductors; the analysis of frequency and geometrical parameters influences on inductance and quality factor; planar spiral inductors configuration's optimization for energy efficiency. For this reason, a software program that was developed, designed, and implemented by the authors and dedicated to spiral inductors high frequency analysis, named ABSIF, is presented in this article. The ABSIF software program allows inductance, quality factor, and electrical parameters extraction for square, hexagonal, octagonal, and circular spiral inductors and their configuration optimization for energetic efficiency. It is dedicated to high frequency application.

## 2. High Frequency Analysis of Spiral Inductors by Means of ABSIF Software

Compact software programs are needed for the analysis, design, and optimization of spiral inductors because the available software (i.e., Sonnet Lite<sup>TM</sup> [19]) typically does not allow analysis and optimization of spiral inductors in high frequency applications. The ABSIF software developed, implemented, and designed by the authors is a compact software program that can be used for high frequency spiral inductor analysis, optimization, and to determine the electronic and electrical parameters, inductance, and quality factor, optimizing their configuration for high performance applications. ABSIF allows the implementation of square, hexagonal, octagonal, and circular spiral inductors for high frequency analysis; these spiral inductor shapes are frequently used in radiofrequency microelectronic circuits [20]. The ABSIF software program has four modules: two modules for inductance, quality factor, and electronic/electrical parameters computation and two modules for spiral inductor optimization in high frequency applications. The first module of the program, CPEPDC, is dedicated to inductance, quality factor, and electronic/electrical parameter extraction for constant descriptive parameters. The second module, CPEPDV, extracts the inductance, quality factor, and electronic/electrical parameters for variable descriptive parameters. The third module, OCBSIM, optimizes the spiral inductor configuration for maximum inductance, and the fourth one, OCBSFCM, optimizes the spiral inductor configuration and maximizes the quality factor, aiming at their energy efficiency.

The ABSIF software is based on: analytical expressions for low frequency inductance calculations, based on the current sheet method [21–27]; analytical expressions for electrical parameters and for high frequency were set up by the authors using the  $\pi$  equivalent electrical circuit method. This method implies the use of  $\pi$  models with concentrated parameters for each side of the spiral inductor [28–34]. For example, a square inductor with N turns has 4N sides; each turn is formed of four lines and a  $\pi$  equivalent circuit with concentrated parameters, such as the one represented in Figure 1.



Figure 1. The equivalent circuit for one side of the spiral inductor.

The model includes the following: the spiral series inductance, L; the series resistance, R; the capacitance between the spiral and the underpass, C; the capacitance between the spiral and the oxide layer,  $C_{ox}$ ; the substrate capacitance,  $C_{sub}$ ; the substrate resistance,  $R_{sub}$ .

The resistances and capacitances of the equivalent circuit have simple, intuitive, physical analytical expressions; only the inductance of the entire inductor implemented on the integrated circuit has no exact expression in high frequency and is determined by using the other parameters and frequency, based on the equivalent circuit reported in Figure 1. There is a difference between the spiral inductance, L, and the inductor high frequency inductance, L<sub>f</sub> [35–39]. For high frequency applications, it is not enough to calculate the inductance of the spiral, as it is being placed in the air, so all the electrical parameters that appear (Figure 1) and, obviously, the frequency value must be considered. The high frequency inductor is characterized by its inductance, L<sub>f</sub>, given by:

$$L_{f} = \frac{\Im m(1/\underline{Y}_{11})}{\omega} = \frac{\Im m(1/\underline{Y}_{11})}{2\pi f},$$
(1)

and its quality factor, Q, determined by:

$$Q = \frac{\Im m(1/\underline{Y}_{11})}{\Re e(1/\underline{Y}_{11})},$$
(2)

where  $\omega$  is the pulsation, f is the frequency, and  $\underline{Y}_{11}$  is the input admittance:

$$\underline{\mathbf{Y}}_{11} = \left. \frac{\underline{\mathbf{I}}_1}{\underline{\mathbf{U}}_1} \right|_{\underline{\mathbf{U}}_2 = 0},\tag{3}$$

when the port 2 is short circuited; then, due to the symmetry of the oxide layer and substrate geometries,  $\underline{Y}_{11} = Y_s + Y_1$  and  $\underline{Y}_{22} = Y_s + Y_2$ . The admittances of the element represented in Figure 1 are  $\underline{Y}_1$ ,  $\underline{Y}_2$ , and  $\underline{Y}_s$ .

The spiral admittance,  $\underline{Y}_s$ , refers to the series admittances of the spiral inductor, composed of the inductors' inductances and resistances in the series connection, and the capacitance between the spiral and underpass in parallel connection. The following expression is utilized for this admittance:

$$\underline{Y}_{s} = \frac{\mathbf{R} + \mathbf{j}\omega \left[ \mathbf{R}^{2}\mathbf{C} - \mathbf{L}(1 - \omega^{2}\mathbf{L}\mathbf{C}) \right]}{\mathbf{R}^{2} + \omega^{2}\mathbf{L}^{2}},$$
(4)

 $\underline{Y}_1$  and  $\underline{Y}_2$  are the admittances equivalent to the elements of the oxide layer and substrate. The admittance  $\underline{Y}_1$  is:

$$\underline{Y}_{1} = \frac{\omega^{2} R_{sub} C_{ox}^{2} + j \omega C_{ox} \left[ 1 + \omega^{2} C_{sub} R_{sub}^{2} (C_{sub} + C_{ox}) \right]}{1 + \omega^{2} R_{sub}^{2} (C_{sub} + C_{ox})^{2}},$$
(5)

We calculate  $\underline{Y}_2$  in a similar manner. The admittance  $\underline{Y}_{11}$  is:

$$\underline{Y}_{11} = \frac{R + j\omega \Big[ R^2 C - L(1 - \omega^2 L C) \Big]}{R^2 + \omega^2 L^2} + \frac{\omega^2 R_{sub} C_{ox}^2 + j\omega C_{ox} \Big[ 1 + \omega^2 C_{sub} R_{sub}^2 (C_{sub} + C_{ox}) \Big]}{1 + \omega^2 R_{sub}^2 (C_{sub} + C_{ox})^2},$$
(6)

The optimal design procedure is formulated as an objective problem, which allows us to find the electrical parameters of the spiral inductors, the inductance, and quality factor. The objective is to find the optimal configuration of the spiral inductor, at maximum inductance L and quality factor Q, by satisfying the proper objective functions.

The objective function for the first optimization module is:

$$f(N, f, w, s, t, t_C, t_o, t_s) = L_{f_{max}}$$
(7)

and for the second optimization module is:

$$f(N, f, w, s, t, t_C, t_o, t_s) = Q_{max},$$
(8)

where  $L_{f max}$  and  $Q_{max}$  are calculated using the above expressions.

#### 2.1. CPEPDC Module

The module for the computation of the electrical parameters of spiral inductors, utilized in microelectronic circuits for constant descriptive parameters, the CPEPDC module, allows us to determine, for a high frequency analysis, the following parameters: spiral inductance, L; resistance, R; capacitance, C; oxide capacitance,  $C_{ox}$ ; substrate resistance,  $R_{sub}$ ; capacitance,  $C_{sub}$ ; spiral inductor high frequency inductance, L<sub>f</sub>; quality factor, Q.

The following are used as input data for the geometrical definition of the inductor in the module: the spiral shape; the number of turns, N; the turn's width, w; the distance between turns, s; the external diameter,  $d_e$ ; the internal diameter,  $d_i$ ; the turn's thickness, t; the via thickness,  $t_c$ ; the oxide thickness,  $t_o$ ; the substrate thickness,  $t_s$ . The frequency and the materials for each component of the spiral inductor must be properly set. The computed values of the electrical parameters, the inductance, and the quality factor are displayed in a window with the equivalent circuit, on which the parameter that is selected to be displayed is automatically highlighted.

A set of designed spiral inductors was analysed for high frequency values using our ABSIF software. All the spiral inductors were designed to be utilized on microelectronic circuits on the same area of  $0.25 \text{ mm}^2$ . The geometrical parameters are the same for all the designed spiral inductors: the external diameter is 500 µm, the distance between the turns is 5 µm, the turn width is 10 µm, the turn thickness is 2 µm, the oxide layer thickness is 6 µm, the substrate thickness is 380 µm, the via thickness is 2 µm, and the underpasses thickness is 2 µm. We considered turn numbers from one to sixteen and frequencies from one to ten GHz for all the analyses. We assumed the use of copper for the spiral, silicon dioxide for the oxide layer, and silicon for the substrate. The CPEPDC module was implemented to compute the values of the electrical parameters of the spiral inductors, the inductance, and the quality factor for constant descriptive parameters, frequency, and number of turns. Table 1 shows the results obtained for the analysis of the set of designed square spiral inductors analysed at 4 GHz.

<b>T</b>	Electrical Parameters									
lurns	L, nH	R, Ω	C, fF	Cox, fF	$R_{sub}$ , M $\Omega$	C <sub>sub</sub> , fF	L <sub>f</sub> , nH	Q		
1	1.807	3.793	1.726	135.362	88.126	2.717	1.816	11.915		
2	5.5820	6.092	3.453	217.410	54.868	4.364	5.738	22.395		
3	10.526	8.588	5.179	306.447	38.926	6.151	11.373	28.501		
4	16.149	10.964	6.906	391.241	30.490	7.853	18.974	31.483		
6	28.080	15.227	10.359	543.353	21.954	10.907	44.795	28.990		
8	39.347	18.788	13.812	670.412	17.793	13.458	119.398	17.244		
12	55.314	23.747	20.718	847.379	14.077	17.010	179.706	17.868		
16	60.063	25.802	27.625	920.677	12.956	18.481	81.589	42.778		

Table 1. Results of analysed square spiral inductors at 4 GHz.

The ABSIF gives the results, immediately, for all the interest inductor's parameters for the desired frequency. The spiral inductance increases with the number of inductor's turns, but not with the inductor's inductance, which depends on frequency and reaches its maximal value at its resonance frequency. In high frequency, there is not a linear increment of the inductance with the number of turns because of the different frequency resonance of each inductor. All the layers on which the spiral is constructed have an influence on the planar inductor parameters in high frequency, and all of these must be properly calculated and considered in their design and optimization. Table 2 shows the results obtained for the analysis of the set of designed square spiral inductors analysed at 10 GHz. In this way, using our program, the inductor's parameters can be properly found for a wide range of frequencies.

T	Electrical Parameters									
Iurns	L, nH	<b>R</b> , Ω	C, fF	Cox, fF	$R_{sub}, M\Omega$	C <sub>sub</sub> , fF	L <sub>f</sub> , nH	Q		
1	1.807	5.374	1.726	135.362	88.126	2.717	1.865	20.469		
2	5.5820	8.631	3.453	217.410	54.868	4.364	6.727	33.697		
3	10.526	12.166	5.179	306.447	38.926	6.151	19.697	29.002		
4	16.179	15.532	6.906	391.241	30.490	7.853	224.300	4.471		
6	28.080	21.572	10.359	543.353	21.954	10.907	21.0488	108.437		
8	39.347	26.616	13.812	670.412	17.793	14.458	12.3147	293.174		
12	55.314	33.642	20.718	847.379	14.077	17.010	7.718	722.663		
16	60.063	36.552	27.625	920.677	12.956	18.481	6.099	988.178		

Table 2. Results of analysed square spiral inductors at 10 GHz.

## 2.2. CPEPDV Module

The CPEPDV module of ABSIF for electrical parameters, inductance, and quality factor computation for variable descriptive parameters is similar to the CPEPDC module, and it also analyses the electrical parameters, the inductance, and the quality factor variations in terms of variable frequency, number of turns, and other descriptive geometrical parameters for the same shapes of the spiral inductor. This module of the program computes and displays, in a table, the inductance value and the quality factor value with reference to the parameter selected as variable. By using this module, it is possible to obtain the inductance and quality factor variations at high frequency without the necessity of a separate implementation and analysis of each inductor, and then, it is possible to directly collect the results and plot the desired variations. The designed spiral inductors are also analysed in this module to plot the inductance and the quality factor variations, directly, in the graphical representation module, with it not being necessary to use other programs to plot the results. The inductance is plotted in terms of frequency for the square spiral inductor with 3 turns in Figure 2a and for the one with 8 turns in Figure 2b.



Figure 2. The inductance variation vs. frequency for: (a) 5 and (b) 8 turns spiral inductors.

At a frequency variation between 1 and 10 GHz, as can be seen in Figure 2, the inductors each reach at a single or multiple resonance frequency, where the higher value of the inductance is found. If high-performance inductors are desired, they must also be properly analysed in terms of frequency. In ABSIF, these types of analyses are possible, for

the all the inductors that were analysed in our research activities, we consider the frequency variation between 1 and 10 GHz, with the step 0.025 GHz. If it is desired, the step can be also smaller or higher than this. Each researcher can choose it in terms of the accuracy he wants for the results.

The quality factor variation, in terms of frequency, can also be plotted, directly, in this module of the software. For example, the quality factor is plotted, in terms of frequency, for the square spiral inductor, with 2 turns in Figure 3. The frequency varies between 1 and 10 GHz, with step 0.5. The frequency at which the quality factor is maximal can be found for inductor's energy efficiency.



Q = f(f) min = 1, max=10, pas=0.5GHz

Figure 3. The quality factor variation vs. frequency for 3 turns spiral inductors.

## 2.3. OCBSIM Module

The module for the optimization of the spiral inductor configuration for maximal inductance, the OCBSIM module, is dedicated to finding the optimal configuration of spiral inductors for the maximum inductance, given a particular area of implementation, on the microelectronic circuit.

The input data in this module are the spiral inductor shape (square, hexagonal, octagonal, or circular), the type of material, and the exterior diameter, d<sub>e</sub>. This module of the program enables the use of additional optimization options. The software displays the value of maximal inductance, the frequency, and details about the optimal configuration that is found for the maximum inductance. The module automatically draws the cross section and top view of the optimal configuration.

The optimization module of the ABSIF program is a useful tool for spiral inductor design and optimization; it has a very friendly interface that facilitates the implementation, and the optimization process is easy to use. It also has short running time compared to similar programs.

Square spiral inductors with an exterior diameter of  $10 \ \mu\text{m}$ ,  $50 \ \mu\text{m}$ ,  $100 \ \mu\text{m}$ ,  $200 \ \mu\text{m}$ ,  $300 \ \mu\text{m}$ ,  $500 \ \mu\text{m}$ ,  $700 \ \mu\text{m}$ , and  $800 \ \mu\text{m}$  were optimized, and the optimal solution was found for each one to achieve the maximum inductance for a frequency range 1–10 GHz. Keeping the same shape of spiral inductors and the above detailed materials, the optimal configuration of these spiral inductors was found. The results are given for the analysed inductors in Table 3.

For these optimization processes, additional optimization options were considered. The program automatically draws the optimal configuration found for each implementation, so the designer can obtain the optimal configuration of the spiral inductor.

1	T II	( CH	<b>Optimal Configuration of Spiral Inductors</b>							
a <sub>e</sub> , μm	L <sub>max</sub> , nH	f, GHZ	w, μm	s, µm	d <sub>i</sub> , μm	N, turns	t, μm	tc, μm	t <sub>o</sub> , μm	t <sub>s</sub> , μm
10	0.037	9	1	1	4	2	1	1	1	1
50	4.606	9	1	1	4	12	1	1	1	1
100	133.753	9	1	1	38	16	1	1	7	5
200	317.771	3	1	1	138	16	1	1	5	9
300	377.834	3	1	1	254	12	1	1	9	9
500	712.4	1	1	1	438	1	1	1	9	9
700	582.067	1	1	1	654	12	1	1	9	9
800	494.63	1	1	1	762	10	1	1	9	9

Table 3. The optimal configuration for maximal inductance in 1–10 GHz frequency domain.

#### 2.4. OCBSFCM Module

OCBSFCM is the module dedicated to the optimization of spiral inductor configuration for the maximum quality factor and energy efficiency. Given the area on which the spiral inductor will be implemented on the microelectronic circuit, this module of ABSIF helps obtain the optimal configuration of the inductor that has the maximum quality factor with high energy efficiency and high performance.

With the OCBFCM module of ABSIF, by using the same input data, the optimal solution for each spiral inductor in terms of high energy efficiency is obtained. For exterior diameters of 10  $\mu$ m, 50  $\mu$ m, 100  $\mu$ m, 200  $\mu$ m, 300  $\mu$ m, 500  $\mu$ m, 600  $\mu$ m, and 800  $\mu$ m, the optimal configuration for the maximum quality factor was obtained. The results for analysed inductors are shown in Table 4.

Table 4. The optimal configuration for maximal quality factor in 1–10 GHz frequency domain.

1	0	f, GHz	<b>Optimal Configuration of Spiral Inductors</b>							
a <sub>e</sub> , μm	Q		w, μm	s, μm	d <sub>i</sub> , μm	N, turns	t, μm	tc, μm	t <sub>o</sub> , μm	t <sub>s</sub> , μm
10	1.842	9	1	1	4	2	5	1	1	1
50	5.932	9	1	1	4	12	5	1	1	1
100	1.026	9	1	1	38	16	5	3	9	1
200	0.971	3	1	1	138	16	5	9	9	1
300	1.192	3	1	1	254	12	5	1	9	9
500	1.124	1	1	1	438	16	5	1	9	5
600	1.149	1	1	1	546	14	5	1	9	7
800	1.009	1	1	1	762	12	5	1	5	9

## 3. Results and Discussion

The ABSIF software was validated by comparing the results with those obtained by using a similar commercial software, Sonnet Lite<sup>TM</sup> [19], for high frequency electromagnetic analysis. Different types of spiral inductors were implemented by using these software programs [21,22]. We intend, in the near future, to also validate our program with experimental measurements. We constructed some of the inductors analysed in our research activities and presented in this article, and we want to measure their Q and L by using a Network Analizer GHz.

This section presents the analysis for the designed set of square spiral inductors, with the dimensions and material properties given above. The inductance and the quality factor variations are analysed in the frequency domain 1–10 GHz. In Table 5, the results obtained by means of ABSIF are shown and compared to those obtained by Sonnet Lite<sup>TM</sup> for the set of square spiral inductors with 1–16 turns at 4 GHz frequency.

The frequency analysis for the square spiral inductor with 2 turns was initially compared. The results obtained by using the two similar software programs, for inductance and quality factor variation is terms of frequency, are reported in Table 6.

Square Spiral Inductor	L <sub>ABSIF</sub> , nH	L <sub>Sonnet</sub> , nH	QABSIF	Q <sub>Sonnet</sub>
1 turn	1.81667	1.605376	11.9152	11.78124
2 turns	5.7382	4.866895	22.39523	16.64678
3 turns	11.37367	10.49286	28.50145	17.15152
4 turns	18.97421	19.43089	31.48352	16.41239
5 turns	29.43674	38.00863	31.57406	12.47133
6 turns	44.79571	83.67156	28.99092	7.485075
8 turns	119.39874	-234.313	17.24493	3.512818
12 turns	-179.706	-66.5797	17.8686	19.48071
16 turns	-81.5899	-58.8932	42.7782	33.70341

Table 5. Comparison of the results obtained by ABSIF and Sonnet at 4 GHz.

**Table 6.** L and Q vs. f for 2 turns spiral inductor at 4 GHz: comparison of the results obtained by ABSIF and Sonnet.

Frequency, GHz	L <sub>ABSIF</sub> , nH	L <sub>Sonnet</sub> , nH	Q <sub>ABSIF</sub>	Q <sub>Sonnet</sub>
1	5.591	4.582481	8.3	7.835281
2	5.620	4.623863	14.07	12.5581
3	5.669	4.716134	18.64	15.30015
4	5.738	4.866895	22.4	16.64678
5	5.830	5.088538	25.51	17.00251
6	5.946	5.401603	28.07	16.66686
7	6.090	5.840430	30.14	15.85112
8	6.265	6.464510	31.75	14.68275
9	6.475	7.384216	32.93	13.21468
10	6.727	8.82726	33.7	11.43541

It is also very important to make the next comparison for a more complex spiral inductor and give the results for the square spiral inductor with 16 turns in the analysis of the inductance, and the quality factor variation in terms of frequency, in Table 7.

**Table 7.** L and Q vs. f for 16 turns spiral inductor: comparison of the results obtained by ABSIF and Sonnet.

Frequency, GHz	L <sub>ABSIF</sub> , nH	L <sub>Sonnet</sub> , nH	QABSIF	QSonnet
1	67.350	56.40525	18.83	15.61315
2	105.983	88.47989	20.32	17.14319
2.975	1184.864	1220.688	1.89	0.782397
3	1430.291	-230.072	1.12	0.091579
3.025	880.472	-1274.88	0.34	0.986546
3.05	-1101.464	-1057.03	0.46	1.901337
3.075	-1423.381	-809.371	1.27	2.834652
4	-81.590	-58.8932	42.78	33.70341
5	-35.083	-24.4080	34.83	35.44694
6	-20.676	-13.1851	21.8	26.36955
7	-13.920	-8.25221	13.84	13.10635
8	-10.108	-4.50733	10.56	9.586369
9	-7.714	-1.63675	3.11	2.369961
10	-6.1	1.922089	1.18	1.153401

For a better visualization of the good agreements of the results, the results for the square spiral inductor with 16 turns were plotted separately in Figure 4, those obtained with ABSIF in Figure 4a, and those with Sonnet in Figure 4b for the same frequency variation between 1 and 10 GHz.



**Figure 4.** Inductance variation, in terms of frequency for the square spiral inductor with 16 turns obtained by: (**a**) ABSIF software program; (**b**) Sonnet Lite<sup>TM</sup>.

The results for inductance and quality factor, for the square spiral inductor with 16 turns, were compared and plotted in Figure 5. By overlaying the results, their good agreements are obvious.



Figure 5. Comparison of the results for 16 turns square spiral inductor: (a) inductance; (b) quality factor.

The ABSIF implementation immediately yielded the L and Q variations; each inductor was not analysed separately, as was necessary in the Sonnet software program, so the running times for ABSIF are much shorter than for similar programs.

The ABSIF program can be used with confidence for high frequencies analysis, modelling, simulation, design, and optimization of microelectronic planar spiral inductors of millimetre, micrometre and nanometre dimensions that operate at gigahertz order frequencies. The software is dedicated, exclusively, to spiral inductor high frequency analysis, so it can be used for parameter extraction for parametric inductor's analysis (inductance variation in terms of frequency, in terms of some of the geometrical parameter, and so on) and for optimal design of the planar spiral inductor configuration with square, hexagonal, octagonal, and circular shapes.

## 4. Conclusions

The design of a spiral inductor requires a preliminary analysis for a proper high frequency to achieve high performance and to avoid errors. It is very important to have a software tool able to conduct this analysis as simply, easily, and quickly as possible while maintaining high accuracy.

In the present paper, ABSIF software was proposed, which is a well-assembled and well-structured software. Each module of the software is set for a specific computation or optimization to provide opportunities for all the studies that spiral inductor designers must conduct before, during, and after the construction of the spiral inductors. The geometrical parameters and materials used for the other components of the microelectronic circuits can affect the inductance and the quality factor values of spiral inductors and must be properly analysed to achieve inductors with high performances. Using the ABSIF software the planar spiral inductor can be very deeply analysed, their electrical parameters (resistances, capacitances, inductances) can be extracted easy and fast with high accuracy for a wide range of planar inductor types of millimetre, micrometre, and nanometre dimensions and in a wide range of high frequencies. The software allows us to directly analyse the inductor's parameters variations in terms of frequency and/or in terms of geometrical parameters by plotting their variation in real time, as was exemplified in Figures 2–4 and detailed in Tables 6 and 7. A set of spiral inductors were designed to be analysed in high frequency to validate our ABSIF software and the obtained results, presented in Figure 5, show their accuracy.

The software program enables the analysis and optimization of a board range of spiral inductors. It is very good for spiral inductor design because it allows to compute its inductance, quality factor, and electrical parameters for high frequency applications with very good accuracy and to optimize the spiral inductor configuration for the imposed technological limits and/or for the designers' needs.

In the present paper, we demonstrated that, by comparing the results obtained with other commercial software, the proposed software is of much help in the design, optimization, and verification of spiral inductors.

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