Two Gallium data sets, spin flavour precession and KamLAND

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Abstract

We reexamine the possibility of a time modulation of the low energy solar neutrino flux which is hinted by the average decrease of the Ga data in line with our previous arguments. We perform two separate fits to solar neutrino data, one corresponding to 'high' and the other to 'low' Ga data, associated with low and high solar activity respectively. We therefore consider an alternative to the conventional solar+KamLAND fitting, which allows one to explore the much wider range of the θ_{12} angle permitted by the KamLAND fitting alone. We propose a solution with parameters $\Delta m_{21}^2 = 8.4 \times 10^{-5} eV^2$, $tan^2 \theta = 0.27$ in which the 'high' and the 'low' Ga rates lie far apart and are close to their central values, in contrast to the global best fit solution where these rates lie close to each other. This is an indication that the best fit in which all solar and KamLAND data are used is not a good measure of the separation of the two Ga data, as the information from the low energy neutrino modulation is dissimulated in the wealth of data. Furthermore for the parameter set proposed one obtains an equally good fit to the KamLAND energy spectrum and an even better fit than the 'conventional' LMA one for the reactor antineutrino survival probability as measured by KamLAND.

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1 Introduction

After having been asserted that the solar neutrino problem was essentially a particle physics one and neutrinos oscillate $[1, 2]$, the next step is to search for a possible time dependence of the active solar neutrino flux and to investigate its low energy sector $(E < 1 - 2 \; MeV)$ which accounts for more than 99% of the total flux. These two issues in association with each other may lead to further surprises in neutrino physics, possibly the hint of a sizable magnetic moment. Although a lot of effort has been devoted to examine the possible time modulation of the neutrino flux $[3]$ - $[8]$, this question remains largely unsettled. The claim made in the early days [9, 10] of a possible anticorrelation of the Homestake event rate [11] with sunspot activity remained unproven, as no sufficient evidence was found in its support. More recently the Stanford Group has been claiming the existence of two peaks [6] in the Gallium data at 55-70 SNU and 105-115 SNU. Moreover, Gallium experiments [12] - [15], which have been running since 1990-91 and whose event rates are mainly due to pp and ${}^{7}Be$ neutrinos (55% and 25% respectively), also show a flux decrease from their start until 2003 [16]. These data are hardly consistent with a constant value and exhibit a discrepancy of 2.4 σ between the averages of the 1991-97 and 1998-03 periods (see table I). No other experiment sees such variations and none is sensitive to low energy neutrinos with the exception of Homestake whose rate contains only 14% of $7Be$. Hence this fact opens the possibility that low energy neutrinos may undergo a time modulation partially hidden in the Gallium data which may be directly connected in some non obvious way to solar activity [17]-[19]. Hence also the prime importance of the low energy sector investigation. To this end, in the near future, two experiments, Borexino [20] and KamLAND [21], will be monitoring the 7Be neutrinos.

Period	1991-97 (I)	1998-03 (II)
$SAGE+Ga/GNO$	77.8 ± 5.0	63.3 ± 3.6
Ga/GNO only	$77.5 + 7.7$	62.9 ± 6.0
SAGE only	$79.2 + 8.6$	63.9 ± 5.0

Table 1 - Average rates for Ga experiments in SNU (see ref. $[16]$).

In our former work [17, 18] we developed a model where active neutrinos are partially converted to light sterile ones in addition to LMA conversion at times of strong magnetic field, thus leading to the lower Gallium event rate (II). When the field is weaker, LMA oscillations act alone and the higher rate (I) is obtained. The resonant conversion from active to sterile neutrinos is originated from the interaction between the magnetic moment

and the solar magnetic field. Its location is determined by the order of magnitude of the corresponding mass squared difference Δm_{10}^2 and is expected to occur in the tachocline, where a strong time varying field is assumed. This implies $\Delta m_{10}^2 = O(10^{-8})eV^2$ so that the LMA resonance and the active \rightarrow sterile one do not interfere ¹. It was shown [17, 18] that the high Gallium data as in table 1 can be fitted assuming a 'quiet sun' with a weak field while the low data are fitted with a strong field ('active sun'). On the other hand the bimodal character of the data as claimed by the Stanford Group [6] cannot be explained in the context of this model.

The purpose of this paper is to aim at oscillation and oscillation + spin flavour precession (SFP) fits to the data, taking Δm_{21}^2 , θ_{12} as free parameters. Two separate global fits for Gallium sets (I) and (II) are performed with the solar data which were available in the corresponding periods (see table 2).

Experiment	Data	Theory	Reference
Homestake	$2.56 \pm 0.16 \pm 0.15$	$8.09\pm^{1.9}_{1.9}$	$\left[11\right]$
SAGE	see table I	$125.9\pm_{12.1}^{12.2}$	$\left[14\right]$
$Gallex + GNO$	see table I	$125.9\pm_{12.1}^{12.2}$	$\left[13\right]$
Kamiokande	$2.80 \pm 0.19 \pm 0.33$	5.69 ± 1.41	[24]
SuperK	$2.35 \pm 0.02 \pm 0.08$	5.69 ± 1.41	[25]
SNO CC	$1.68 \pm 0.06 \pm 0.08$	5.69 ± 1.41	[26]
SNO ES	$2.35 \pm 0.22 \pm 0.15$	5.69 ± 1.41	[26]
SNO NC	$4.94 \pm^{0.21}_{0.21} \pm^{0.38}_{0.34}$	5.69 ± 1.41	$\left[26\right]$

Table 2 - Data from the solar neutrino experiments except Ga which is given in Table 1. Units are SNU for Homestake and 10^6 cm⁻²s⁻¹ for Kamiokande, SuperKamiokande and SNO. We use the $BS05(OP)$ solar standard model [22].

Hence for data set (I) we consider a rate fit to Gallium, Chlorine and Kamiokande data, the only ones existing at the time, together with the KamLAND fit, as these data are obviouly independent from solar activity. For set (II) we consider a global fit (rates $+$ spectrum) with the exclusion of the Chlorine one, the replacement Kamiokande \rightarrow SuperKamiokande and the inclusion of the SNO data. We consider a solar field profile peaked at the bottom of the convective zone. We hence determine the parameter values that lead to the best solar+KamLAND fit for data set (I). Using these, we establish the best solar fit for set (II) on the grounds of its order parameter values Δm_{10}^2 , which situates the SFP resonance, and

¹For mathematical details we refer the reader to [17, 18].

 B_0 , the field strength at the peak. This is also the best solar+KamLAND fit for data set (II). The Ga (I) and (II) rate predictions lie quite close to each other in this fit, both almost 2σ away from their central values. This is not totally surprising, as their relative weight is small within the wealth of solar+KamLAND data. It tells us instead that the global fit analysis is not adequate for the investigation of the possible Ga flux variability. To this end we present a choice of a slightly different value of Δm_{21}^2 , θ_{12} whose fit to data is almost as good as the best fit and in which the Ga (I) and (II) rate predictions lie much further apart. We use throughout the BS05 (OP) solar model [22].

Since our solar fit is independent from the conventional solar one, our only a priori parameter constraints come from the KamLAND fit for which the mixing angle θ_{12} bears a considerable uncertainty (fig.4 of ref.[21]). In this way we scan the range $\tan^2\theta_{12} \in$ [0.1, 10]. Moreover in the new scenario the prediction for the KamLAND antineutrino survival probability is consistent with the measured one [23]. A clear distinction between our scenario and the conventional LMA one is expected to be provided by the forthcoming KamLAND data if and when new reactors start and others cease operation, thus changing the effective source-detector distance travelled by the antineutrinos.

2 Global Fits and Survival Probability

We start this section by introducing the following solar field profile

$$
B = \frac{B_0}{ch[6(x - x_c)]} \quad 0 < x < x_c \tag{1}
$$

$$
B = \frac{B_0}{ch[15(x - x_c)]} \quad x_c < x < 1 \tag{2}
$$

whose peak value B_0 is situated at $x_c = 0.71$, x denoting the fraction of the solar radius.

For the solar statistical analysis we use the standard χ^2 function

$$
\chi_{\odot}^{2} = \sum_{j_{1},j_{2}} (R_{j_{1}}^{th} - R_{j_{1}}^{exp}) \left[\sigma^{2}(tot) \right]_{j_{1}j_{2}}^{-1} (R_{j_{2}}^{th} - R_{j_{2}}^{exp}) \tag{3}
$$

where indices j_1, j_2 run over all solar neutrino experiments and the error matrix includes the cross section, astrophysical and experimental uncertainties ² . For the KamLAND analysis we compute the prompt energy spectrum of the positron according to

$$
S(E) = N \int \sigma(E_{\bar{\nu}}) R(E, E') \frac{d\phi}{dE_{\bar{\nu}}} dE'.
$$
 (4)

²For mathematical details see e.g.[27].

Here E' , E denote the physical and measured prompt event energy, so that E' includes the e^+e^- annihilation energy and the positron kinetic energy, $E' = 2m_e + T'_{e^+}$. From the well known relation

$$
E_{\bar{\nu}} = m_N - m_P + m_e + T'_{e^+} = 1.804 MeV + T'_{e^+},\tag{5}
$$

(for zero neutron recoil) one gets $E_{\bar{\nu}} = 0.782 MeV + E'$. Hence eq.(4) is also an integral over antineutrino energy. The quantity N is a normalization constant obtained from the total number of events in the absence of antineutrino disappearance above the energy cut at 2.6MeV [21]

$$
\int S(E)dE = 365.2.\tag{6}
$$

The quantity $\sigma(E_{\bar{\nu}})$ is the total cross section for the reaction $\nu p \to n e^+$ with zero neutron recoil energy [28] and $R(E, E')$ is the energy resolution function

$$
R(E, E') = \frac{1}{\sigma\sqrt{2\pi}} exp\left[-\frac{(E - E')^2}{2\sigma^2}\right]
$$
\n(7)

with $\sigma = 0.062\sqrt{E}$. The KamLAND energy spectrum comprises 13 bins of size 0.425 MeV in the range from 2.6 to 8.125 MeV . For convenience we integrate eq.(4) in antineutrino energy, so that in order to take into account the important low energy tail of the spectrum we run the integration from $E_{\bar{\nu}_{min}} = 1.804 MeV$ up to $E_{\bar{\nu}_{max}} = (8.125 + 0.782) MeV$. In contrast, in eq.(6) the integral extends over all 13 energy bins. The information on the flux and spectra of the 20 power reactors is contained in the time averaged differential neutrino flux $\frac{d\phi}{dE_{\nu}}$ which denotes the number of neutrinos per unit energy, area and time. We have used the approximation (see e.g.[29]):

$$
\frac{d\phi}{dE_{\bar{\nu}}} \simeq \sum_{j=1}^{20} P_{osc}(E_{\bar{\nu}}, L_j) \phi_j \sum_{f=1}^{4} \frac{q_f}{E_f} \frac{dN_f}{dE_{\bar{\nu}}}.
$$
\n(8)

In this expression

$$
P_{osc}(E_{\bar{\nu}}, L_j) = 1 - \sin^2 2\theta \sin^2 \left(\frac{\Delta m_{21}^2 L_j}{4E_{\bar{\nu}}}\right)
$$
 (9)

is the well known oscillation survival probability formula for antineutrinos from the jth reactor at distance L_j , ϕ_j is the reactor flux at the KamLAND detector [30], q_f and E_f are the relative fission yields and fission energies [21, 29]. Following [29], we take

$$
\frac{dN_f}{dE_{\bar{\nu}}} = exp(a_f^0 + a_f^1 E_{\bar{\nu}} + a_f^2 E_{\bar{\nu}}^2)
$$
\n(10)

with the coefficients given in [31].

We have used Poisson statistics for the 13 KamLAND energy bins. Our χ^2 function therefore is [1]

$$
\chi_{KL}^2 = \sum_{i=1}^{13} \left[2(\alpha R_i^{th} - R_i^{exp}) + 2R_i^{exp} \ln \left(\frac{R_i^{exp}}{\alpha R_i^{th}} \right) \right] + \frac{(\alpha - 1)}{\sigma_{sys}^2}
$$
(11)

with α being an absolute normalization constant and $\sigma_{sys} = 6.5\%$ the total systematic uncertainty. The binned spectrum calculated in the basis of eq.(4) added to the background spectrum [32] is thus inserted in (11) as R_i^{th} .

We are now in a position to obtain the result of the best fits which we show in table 3. For sets (I) and (II) we take $f_B = 1.0$. We found for set (I)

$$
\Delta m_{21}^2 = 8.2 \times 10^{-5} eV^2, \tan^2 \theta = 0.31, \ \alpha = 1.01 \tag{12}
$$

We include for comparison the 'KamLAND only' LMA best fit [21] with all Gallium data replaced by their average [16]

$$
R_{Ga} = 68.3 \pm 2.9 \; SNU \tag{13}
$$

and with parameters ³

$$
\Delta m_{21}^2 = 7.9 \times 10^{-5} eV^2, \tan^2 \theta = 0.46, \ B_0 = 0, \ f_B = 0.9, \ \alpha = 1.01. \tag{14}
$$

		Cl K (SK) SNO _{NC} SNO _{CC} SNO _{ES} χ^2_{rates} $\chi^2_{SK_{sp}}$ $\chi^2_{SNO_{gl}}$ χ^2_{KL}							
Set (I) 71.7 2.66		2.29				3.09			15.3
Set (II) 69.6		2.18	5.53	1.54	2.16	2.28	44.6	45.8	15.3
LMA	64.8 2.74	2.30	5.10	1.75	2.28		0.95 45.7	43.1 14.5	

Table 3 - Best fits to data sets (I), (II) and LMA best fit. For data set (I) only Ga, Cl and Kamiokande data were available and for set (II) all SuperKamiokande and SNO data were available but not Cl, hence the blank spaces. In set (II) only the Ga rate contributes to χ^2_{rates} . Units are SNU for Ga and Cl and $10^6 cm^{-2}s^{-1}$ for SK and SNO.

Using Δm_{21}^2 , $tan^2\theta$ from (12), we get the best fit for set (II) with

$$
\Delta m_{10}^2 = -6.5 \times 10^{-8} eV^2, \ 300kG. \tag{15}
$$

³The 'LMA parameter values' we consider are the ones fixed from the best fit analysis to KamLAND data only, since the conventional solar fits are not taken into account in the present work.

Table 3 $\chi^2_{SK_{sp}}$ contains the contribution from electron scattering in SuperKamiokande (44) data points) and χ^2 $^{2}_{SNO_{gl}}$ contains the whole SNO data consisting of 38 data points (34 CC, 2 NC and 2 ES day-night rates). We have

$$
\chi_{gl}^2 = \chi_{\odot}^2 + \chi_{KL}^2 \tag{16}
$$

with

$$
\chi_{\odot}^2 = \chi_{rates}^2 + \chi_{SK_{sp}}^2 + \chi_{SNO_{gl}}^2.
$$
 (17)

For sets (I), (II) and LMA we have therefore $\chi^2_{gl} = 18.4, 107.9, 104.3$ for 13, 94 and 93 degrees of freedom (d.o.f.) respectively. We thus see that for the best global fit the parameter Δm_{10}^2 is well above $O[10^{-8}eV^2]$. This implies that the resonances of the low energy neutrinos lie too deep inside the sun for the possible time variation of the field to significantly modulate their flux. This is particularly true for the pp sector. In fact the resonances of these neutrinos lie around $x = 0.45$, where the field is 40% of its maximum and the matter density is much higher than near the peak. Hence for the best global fit only a small difference is expected between the two Gallium values (see table 3).

It should be noted however that the global best fit presented here refers to 97 different experiments and the Gallium data account for only one of them, so their relevance is smeared by all other data. For a global solar fit the situation is much the same, as the number of experiments is reduced to 84 or 16 with the information on the low energy neutrinos included only in one of them. The global fit is therefore not a good measure for the investigation of time variability of low energy neutrinos: the information on them is nearly hidden within the wealth of solar and KamLAND data.

A small change in the parameters provides a considerable difference: in table 4 we present the fits for $\Delta m_{21}^2 = 8.4 \times 10^{-5} eV^2$, $tan^2\theta = 0.27$ which lead to a much larger separation between high and low Ga rates in better accordance with table 1 at the price of a slightly higher χ_{gl}^2 . Here $\Delta m_{10}^2 = -1.7 \times 10^{-8} eV^2$, $f_B = 1.03$, $\alpha = 0.99$ and $B_0 = 280kG$ for set (II). From table 4 we obtain $\chi^2_{gl} = 18.7, 121.1$ for sets (I) and (II) with 13 and 94 d.o.f. respectively.

		Ga Cl K (SK) SNO _{NC} SNO _{CC} SNO _{ES} χ^2_{rates} $\chi^2_{SK_{sp}}$ χ^2_{SNO} χ^2_{KL}						
Set (I) 74.7 2.63 2.28						2.14		16.5
Set (II) 60.5		2.28	5.82	1.53	2.24 0.495 50.6 53.5 16.5			

Table 4 - Same as table 3 with $\Delta m_{21}^2 = 8.4 \times 10^{-5} eV^2$, $tan^2 \theta = 0.27$.

In fig.1 we plot the 'KamLAND only' fit on which we superimpose our own fit (see table

3) in the plane Δm_{21}^2 , $tan^2\theta$. The contour lines correspond to the 95%, 99%, 99.73% CL. We also show our choice of parameters (table 4) in this figure whose goodness of fit is seen to lie well within the 95% CL. On the other hand a comparison with fig.4 (a) of ref. [21] shows that it clearly lies outside the 99.73% CL (3σ) of the conventional solar fit which we neglected in the present paper. The best fit for the 'low' Ga rate in the plane Δm_{10}^2 , B_0 together with the 90%, 95% and 99% CL contours is plotted in fig.2 where we also show the parameter choice of table 4 lying well within the 90% CL.

The binned KamLAND spectrum obtained from eq.(4) is plotted in fig. 3 for nonoscillating neutrinos together with the data points, the LMA spectrum and the LMA+SFP one for $\Delta m_{21}^2 = 8.4 \times 10^{-5} eV^2$, $tan^2 \theta = 0.27$ (table 4). A close inspection shows that the latter exhibits a considerable discrepancy in the first bin which is similar to the one exhibited by the LMA one in the $6th$ bin. Moreover the LMA+SFP spectrum is otherwise slightly more accurate than the LMA one. Altogether their quality is similar $(\chi^2_{KL} = 16.5$ and 14.5 respectively) and close to the best LMA+SFP fit with $\chi^2_{KL} = 15.1$ (table 3), so that its prediction is equivalent to the LMA one.

We next describe a crucial consistency test for the present scenario, namely the survival probability prediction for reactor antineutrinos as measured by KamLAND [21]. Our results are depicted in fig.4 for the best fit LMA+SFP prediction with $\Delta m_{21}^2 = 8.2 \times$ $10^{-5} eV^2$, $tan^2\theta = 0.31$ (middle curve), for the set $\Delta m_{21}^2 = 8.4 \times 10^{-5} eV^2$, $tan^2\theta = 0.27$ (upper curve) and for the LMA best fit, $\Delta m_{21}^2 = 7.9 \times 10^{-5} eV^2$, $tan^2 \theta = 0.46$ (lower curve). For the average source-detector distance of 180 km, as reported by KamLAND, we get from $fig.4,$

$$
P = 0.576 \text{ (LMA)}, 0.623 \text{ (Best fit SFP)}, 0.651 \text{(Table 4 fit)} \tag{18}
$$

to be compared with the data, $P = 0.658 \pm 0.064$ [23]. Interestingly enough it is seen that the best of the three fits lies in this case for the parameter choice as in table 4, namely the one leading to the Gallium data sets which lie the furthest apart: 74.7 and 60.5 SNU. The LMA solution provides the poorest of all fits, at 1.28σ away from the central value. The present data may only allow us to expect a clear distinction between the fit of table 4 and the LMA one for average distances below 110-120 km (see fig.4), which will happen only if new reactors come into operation or others cease. However the accumulation of more data from KamLAND will no doubt turn the situation clearer. Besides this, we also need more data from the low energy solar sector to tell us whether its time modulation is a true or just an apparent effect.

3 Summary and Concluding Remarks

We have considered an alternative to the conventional solar neutrino data fit which takes into account the possible time dependence of the Gallium flux in the form of two data sets corresponding to two different periods and separated by 2.4σ (table 1). This is interpreted as an indication of a possible time variability in the low energy neutrinos, mainly pp , which, though constituting more than 99% of the solar flux, only contribute with 55% of the Gallium flux.

The simplest mechanism that explains the discrepancy of the two data sets is based on the partial conversion of active to sterile neutrinos through the spin flavour precession originated from a varying magnetic field in addition to the LMA oscillation. In the global best fit that takes into account all solar data including KamLAND, the two Gallium rate predictions for each period lie much closer to each other than what the data seem to indicate. Low energy neutrinos however contribute to only part of the Gallium rate which in turn amounts to one single experiment within the wealth of solar+ KamLAND data. It is therefore quite natural to expect that the minimum χ^2_{gl} is not obtained for a Gallium rate prediction close to its central value. For this reason the global fit analysis is not a good measure for the investigation of the time variability of the low energy neutrinos. We have presented a slightly different parameter choice $\Delta m_{21}^2 = 8.4 \times 10^{-5} eV^2$, $tan^2\theta_{12} = 0.27$ (see fig.1) and $\Delta m_{10}^2 = -1.7 \times 10^{-8} eV^2$, $B_0 = 280 kG$ (see fig.2) for which the two Gallium rates are much separated from each other (see table 4). It can be seen from figs.1 and 2 that this parameter choice lies well within 1.5σ of the best fit.

The KamLAND spectrum prediction associated to the choice of parameters of table 4 is plotted in fig.3 and compared to the LMA one. It is seen that their fits to the data are practically as equal in quality.

We also tested the antineutrino survival probability as a function of the source-detector distance. It was found that the parameter choice leading to the two clearly separate Gallium rates (table 4) provides the survival probability prediction which is best in agreement with the data (fig.4).

A close inspection of fig.4 tells us that with the presently existing data, one can only hope for a distinction between the two scenarios (LMA nad LMA+RSFP) if the effective sourcedetector distance is reduced to less than 110-120km. The Shika2 reactor, which started operation in late 2005 and gradually increased the operation time at the nominal power (4GW thermal power) from last November, will reduce this effective distance from 160- 190km to 140-170km [33]. Although this cannot provide a definitive answer, it is expected that the situation will continue to evolve as new reactors come into operation and others cease. The accumulation of more data from KamLAND and especially on the low energy solar neutrino sector is essential to disentangle the prevailing misteries of solar neutrinos.

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Figure 1: Our best fit $\Delta m_{21}^2 = 8.2 \times 10^{-5} eV^2$, $tan^2 \theta = 0.31$ (table 3) is superimposed on the neutrino oscillation parameter allowed region from KamLAND [21]. The contour lines are the 95%, 99%, 99.73% CL. The fit of table 4, $\Delta m_{21}^2 = 8.4 \times 10^{-5} eV^2$, $tan^2 \theta = 0.27$ is also shown.

Figure 2: The best fit (table 3) in the plane Δm_{10}^2 , B_0 and the fit of table 4. The contour lines are the 90%, 95%, 99% CL.

Figure 3: The non-oscillation neutrino spectrum, the LMA one $(\Delta m_{21}^2$ = 7.9 \times $10^{-5} eV^2$, $tan^2\theta = 0.46$), the one for parameters $\Delta m_{21}^2 = 8.4 \times 10^{-5} eV^2$, $tan^2\theta = 0.27$ (labeled $LMA+SFP$) corresponding to the fit in table 4, the KamLAND data points and the background. The quality of the two fits for oscillating neutrinos is comparable: $\chi^2/d.o.f.$ 14.5/11, $\chi^2/d.o.f. = 16.5/11$ respectively.

Figure 4: The antineutrino survival probability for all three fits considered: LMA best fit, $LMA+SFP$ best fit (table 3) and $LMA+SFP$ 'favoured' fit (table 4). The circle denotes the central data point: $P=0.658$ for $d=180$ km. Dashed lines refer to the 1 σ range [23].