

Substrate Integrated Waveguide (SIW) with Koch Fractal Electromagnetic Bandgap Structures (KFEBG) for Bandpass Filter Design

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Abstract—High-performance bandpass filters (BPFs) based on substrate integrated waveguide (SIW) and half mode SIW (HMSIW) with Koch fractal electromagnetic bandgap (KFEBG) patterns etched on the waveguide surface are proposed. These BPFs are designed using a new methodology. The BPF responses are improved by applying a chirped and tapered technique to the KFEBG patterns, which exhibit a radius-to-period ratio $r/a \geq 0.5$. Simulation results and experimental verification are presented. Low insertion loss and high rejection are achieved.

Index Terms—Bandpass filters, electromagnetic bandgap (EBG), Koch fractal, substrate integrated waveguide (SIW).

I. INTRODUCTION

SUBSTRATE integrated waveguide (SIW) and half mode SIW (HMSIW) have been used to develop bandpass filters (BPFs) with electromagnetic bandgap (EBG) patterns [1], [2]. SIW (HMSIW) performances, such as insertion loss, quality factor and power handling capability, are better than those of filters based on conventional microstrip and coplanar waveguides. SIW technology is low cost and has easy integration with other planar circuits. Bandpass responses are obtained by combining the high-pass characteristics of the SIW (HMSIW) [3], [4] and the stopband behavior of EBG patterns. These BPFs present an excellent rejection level due to the periodic EBG patterns, but as a drawback they exhibit reduced width of the stopband, large size, and ripple in the passband. To improve these features, as required by modern microwave systems, we have applied a chirping and tapering technique to Koch fractal EBG (KFEBG) patterns with a radius-to-period ratio $r/a \geq 0.5$ [5], [6]. Fig. 1 shows the layouts of the proposed bandpass filters. They are made of a SIW (HMSIW) waveguide with KFEBG patterns etched on the top plane of the SIW (or on the bottom plane of the HMSIW) and a transition to a 50Ω microstrip. These SIW (HMSIW)-KFEBG BPFs have been designed by using an original procedure. Remarkable performances have been obtained.

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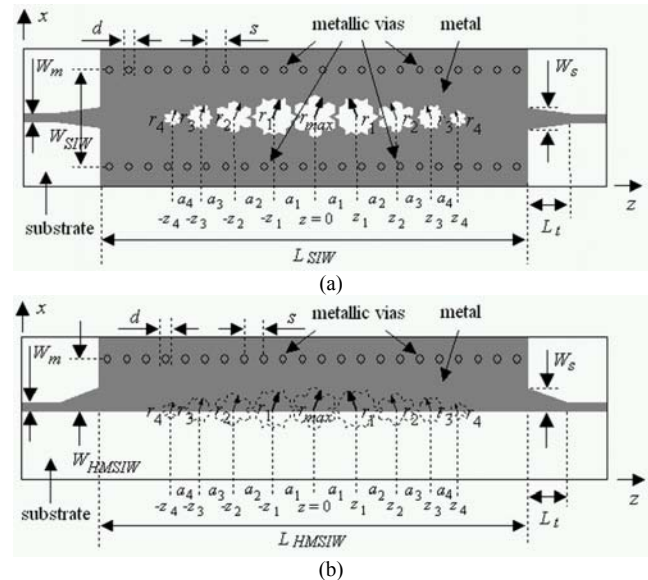


Fig. 1. Layouts of the proposed chirped and tapered (a) SIW-KFEBG and (b) HMSIW-KFEBG bandpass filters.

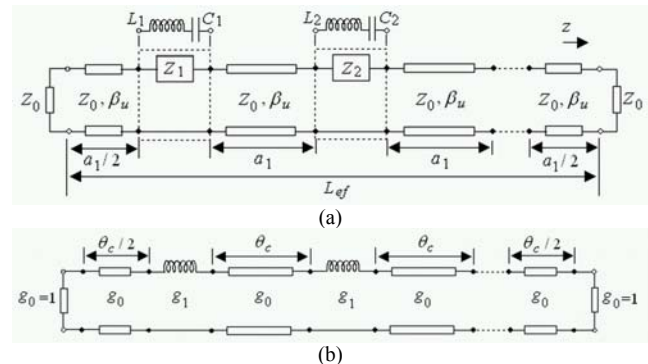


Fig. 2. (a) Equivalent circuit of a generalized bandpass periodic structure. (b) Generalized low-pass filter (LPF) prototype for periodic structures with lumped-distributed network.

II. FILTER DESIGN APPROACH

Using a previous work [6], the design approach starts by applying a Cauchy tapering function T_i to the radii r_i of each Koch fractal (KF), and a chirping period a_i to the separation between Koch fractals (Fig. 1)

$$r_i = r_{max} T_i \quad i = 0, 1, \dots \quad (1)$$

$$T_i = \left[1 + (i/2)^2 \right]^{-1} \quad i = 0, 1, \dots \quad (2)$$

TABLE I
GEOMETRIC PARAMETERS OF THE SIW-KFEBG AND HMSIW-KFEBG

Parameter	Value (mm)	Parameter	Value (mm)	Parameter	Value (mm)	Parameter	Value (mm)	Parameter	Value (mm)		
W_{SIW}	20	s	2	W_m	0.594	r_{max}	5.551	r_3	1.708	a_2	9.771
W_{HMSIW}	10	L_{SIW}	65	W_s	2.2	r_1	4.441	r_4	1.110	a_3	6.107
d	1	L_{HMSIW}	65	L_t	11	r_2	2.776	a_1	11.103	a_4	3.838

$$a_i = r_{i-1} / C \quad i=1, 2, \dots \quad (3)$$

where r_i and r_{max} are the i -th and maximum Koch fractal radii, respectively. a_i preserves a constant r/a ratio (denoted C) between the centers of adjacent Koch fractals along the structure. In (3), r_i is computed from (1), r_0 is equal to r_{max} , and C is a constant ≥ 0.5 in order to achieve a wide stop-band behavior [5], [6].

The proposed BPFs (Fig. 1) can be modeled by a transmission line of effective length L_{ef} periodically loaded with N_{eq} equivalent lumped impedances Z_i as in Fig. 2(a) [7] using the transformation [8]

$$L_{ef} = L \cdot \int_{-0.5}^{0.5} T(z/L) d(z/L) = L \cdot A_{eq} \quad \text{and} \quad N_{eq} = L_{ef} / a_1 \quad (4)$$

where $L = \sum_{i=1}^{(N+1)/2} 2 \cdot a_i$ and $A_{eq} = 0.57$ for the Cauchy tapering function (2). Note that, due to the tapering applied, the BPFs of Fig. 1 behave as BPFs of reduced order $N_{eq} < N$. The BPF equivalent circuit of Fig. 2(a) is assumed lossless and the coupling effects between resonators are neglected. Z_0 and β_u are, respectively, the characteristic impedance and the phase constant of the unperturbed structure (without KFEBG). a_1 is the period defined in (3) for $i = 1$ and a defined value C . Between two possible options for Z_i , we have chosen the simplest, which consists in considering the same series $L_1 C_1$ resonant circuit for all the KFEBG patterns. In this way, we can introduce a design procedure based on the LPF prototype shown in Fig. 2(b) [9], with the characteristic impedance of all transmission lines scaled to the same value as the source impedance $g_0 = 1$. Due to the periodicity of the structure, each KFEBG pattern with $L_1 C_1$ resonant circuit has the same g_1 and each transmission line section of length a_1 has the same phase shift θ_c . The element values from lowpass to bandpass transformation are as follows:

$$L_1 = Z_0 \left(\frac{1}{FBW \omega_0} \right) g_1, \quad C_1 = \frac{1}{(\omega_0)^2 L_1} \quad \text{and} \quad a_1 = \frac{\theta_c}{\beta_u} \Big|_{f_2} \quad (5)$$

with $FBW = (f_2 - f_1) / f_0$ and $f_0 = \sqrt{f_1 f_2}$ (f_1 and f_2 are the passband-edge frequencies). While f_2 depends on a_1 , f_1 (lower cutoff frequency of the passband) is linked to the cutoff frequency f_c of the SIW (HMSIW) which will be optimized during the design procedure ($f_c < f_1$). The constant $C = r/a$

and the number N of KFEBG patterns are respectively related with the width and the rejection level of the stopband [5].

According to given design specifications (bandwidth, rejection level, etc.) and a selected substrate, the design procedure of the proposed BPFs (Fig. 1) is as follows.

- Step 1) Simulate the LPF prototype (Fig. 2(b)) and increase N to get the desired stopband rejection. Obtain g_1 and θ_c by optimizing the LPF according to 3-dB cutoff at the normalized angular frequency ($\omega = 1$ rad/s) and for a desired stopband frequency (ω_s).
- Step 2) Extract the geometric parameters of the SIW (HMSIW) waveguide using the analytical relationships in references [3], [4] for $f_c < f_1$.
- Step 3) Optimize the transition microstrip to SIW (HMSIW) for $Z_0 = 50 \Omega$ using a full-wave simulator (HFSS). Extract transition dimensions, β_u (effective permittivity ϵ_{ref}) and compute L_1 , C_1 and a_1 from Step 1) and equation (5).
- Step 4) Extract the geometric parameters of the chirped and tapered SIW (HMSIW)-KFEBG BPF using (1)-(4) and the previous data. Simulate the BPF circuit (Fig. 2(a)) with the obtained N_{eq} . If the desired stopband rejection and bandwidth are achieved then go to Step 5). If not, vary f_c of the SIW (HMSIW) and then go back to Step 2).
- Step 5) Simulate the chirped and tapered BPF using a full-wave simulator and the previous data.
- Step 6) Final design: optimize basic dimensions of the previous BPF using a full-wave simulator to improve performance. Extract the final geometric parameters.

III. EXPERIMENTAL RESULTS

The proposed BPFs (Fig. 1) were designed with the above design procedure with $C = r/a = 0.5$, an Arlon AD1000 substrate ($\epsilon_r = 10.2$, $\text{tg} \delta = 0.0023$ at 10 GHz and substrate thickness $h = 0.635$ mm) and the following specifications: ripple < 1 dB, insertion loss $IL < 2$ dB, return loss $RL > 10$ dB, stopband rejection level $SRL > 35$ dB at $f_s = 5$ GHz, a central frequency $f_0 = 3.4$ GHz and 3 dB cutoff bandwidth of $BW = 0.65$ GHz and $BW = 0.85$ GHz for the SIW-KFEBG and HMSIW-KFEBG, respectively. Intermediate data obtained from the design procedure for both filters were: $g_1 = 1$, $N = 9$, $\theta_c = 114.74^\circ$, $\epsilon_{ref} = 6.3$ and $N_{eq} = 4$. Their geometric parameters, after the final optimization, are provided in Table I. These structures were fabricated using the PCB process and measured with a Rohde & Schwarz ZVA network analyzer.

TABLE II
COMPARISON BETWEEN THE PROPOSED FILTERS AND THE REFERENCES

	3-D size	FBW (%)	Ripple (dB)	IL (dB)	RL (dB)	Stopband bandwidth (GHz)	SRL
Fig. 3(a)	$0.24\lambda_0 \times 0.008\lambda_0 \times 0.73\lambda_0$	18.9	0.43	1.3	12.3	2.4	42dB@5.6GHz
Fig. 3(b)	$0.15\lambda_0 \times 0.008\lambda_0 \times 0.73\lambda_0$	25.2	0.67	1.7	11.4	2.3	39dB@5.57GHz
Fig. 22 [1]	$0.52\lambda_0 \times 0.02\lambda_0 \times 1.24\lambda_0$	61.2	1.5	1.3	10	–	50dB@20GHz
Fig. 12 [2]	$0.33\lambda_0 \times 0.009\lambda_0 \times 0.75\lambda_0$	55	1.4	0.6	9	0.45	53dB@3.38Hz
Fig. 16 [2]	$0.29\lambda_0 \times 0.009\lambda_0 \times 0.75\lambda_0$	74	1.4	0.5	9	0.45	50dB@4GHz
Fig. 5 [10]	$0.31\lambda_0 \times 0.035\lambda_0 \times 1.22\lambda_0$	19.5	0.05	3.2	15	4	42dB@5.6GHz

where λ_0 is free-space wavelength. The sizes of [1] and [10] have been calculated for 9 cells. Any size includes the microstrip feeding.

Fig. 3 shows a good agreement between the EM simulation (HFSS) and measurement results for the proposed BPFs. The measured central frequency of the stopband $f_s = 5.6$ GHz is slightly higher than the initial design specifications (5 GHz), since the phase constant was considered constant and unperturbed (β_u) in the equivalent circuit. The number of reflection zeroes must be equal to $N_{eq} = 4$. However, the number of reflection zeroes in the frequency axis shown in Fig. 3(a) for the SIW-KFEBG does not match this value. This is because 2 reflection zeroes become complex due to weak couplings between resonators in the SIW-KFEBG. These couplings are stronger in the HMSIW-KFEBG (Fig. 3(b)) because the resonators are crossed by fringing fields. The central frequency is around $f_0 = 3.4$ GHz for both BPFs. The measured insertion losses for the SIW-KFEBG and HMSIW-KFEBG are 1.3 dB and 1.7 dB, respectively, which include the extra loss from the SMA connectors. The measured return losses are better than 11.4 dB for both BPFs. The stopband rejection is better than 20 dB up to the spurious band, which appears at a frequency higher than 6 GHz. Table II provides a performance comparison between the proposed BPFs and other SIW-EBG designs [1], [2], and also for a classical SIW-Chebyshev BPF [10]. The proposed BPFs have better performance than the other SIW-EBGs in size, ripple, return loss and stopband bandwidth, and in size and insertion loss with respect to the classical SIW-Chebyshev BPF.

IV. CONCLUSION

A new design approach is applied to SIW and HMSIW BPFs implemented with KFEBG patterns etched on the waveguide surface, allowing a radius-to-period ratio $r/a \geq 0.5$. A chirped and tapered technique based on a Cauchy function is applied to the KFEBG patterns to improve the BPF responses. Performance of both BPFs are good as demonstrated by their measured insertion ($IL < 1.7$ dB) and return ($RL > 11.4$ dB) losses. A good stopband rejection ($SRL > 39$ dB) is obtained with nine chirped and tapered Koch fractal patterns.

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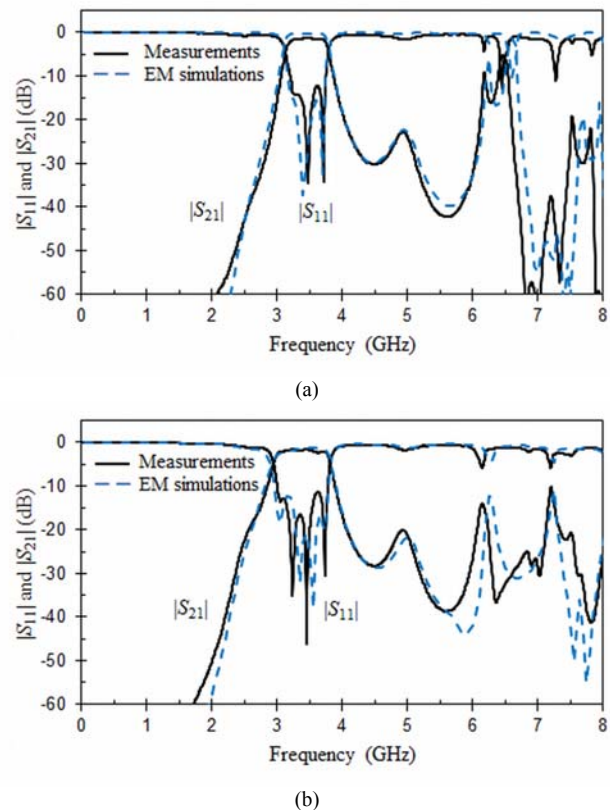


Fig. 3. EM simulation (dashed lines) and measured (solid lines) results for the (a) SIW-KFEBG and (b) HMSIW-KFEBG bandpass filters.

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