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Title: Heat exchanger performance modelling using ice slurry as secondary refrigerant.

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Keywords: Ice slurry; Pressure drop; Heat transfer; Heat exchanger.

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Abstract: Ice slurry is well known as a biphasic secondary refrigerant that presents several potential advantages compared to single phase secondary refrigerants. These potential advantages can be summarized in the ability to use the thermal storage and the high cooling capacity given by the latent heat. Theoretically, these features should allow important energy savings in secondary refrigerant distribution loop. However, an accurate evaluation of these energy savings requires the knowledge of the thermal and rheological performance of the refrigerant studied.

Based on the experimental model developed by the authors for brine based ice slurry, a theoretical analysis of heat exchangers performance is presented in this work in order to calculate the potential energy savings associated to its use. The influence of ice concentration, mass flow rate, heat exchanger length and cooled fluid temperature over pumping power and heat transfer rate is studied. The ratio between heat transfer rate and pumping power is used as the evaluation parameter, which allows us to find the most favourable operation conditions for ice slurry flow.

In order to assess the improvement obtained using ice slurry, results for ice slurry are compared to those obtained for carrier fluid at same inlet temperature.

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Departamento de Ingeniería Térmica y de Fluidos

Cartagena, 20th of July, 2011

Dear Editor,

Attached we are sending the paper titled:

“Heat exchanger performance modelling using ice slurry as secondary refrigerant”

Authors: F. Illán and A. Viedma,

We would like to submit this paper to publication in the International Journal of Refrigeration. The paper has been written in manuscript format according to the “guide for authors” found at Elsevier homepage.

This paper is an improvement of the paper “Assessment of improvement in heat exchangers behaviour using ice slurry as secondary refrigerant” published in the 3rd IIR Conference on Thermophysical Properties and Transfer Processes of Refrigerants, Boulder, CO, 2009.

We hope that the original will fulfil all the requirements. We accept all the conditions included in the journal web about transfer of copyright and originality.

Please send all the correspondence related to this paper to the address below:

Yours faithfully,

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1) Abstract should be provided within 150 words. In this article, the word count is 196. Please revise.

Abstract has been reduced to 150 words.

2) Style for the unit should be kg h⁻¹ and not kg/h.

Style has been corrected.

3) Type the whole manuscript with uniform double line spacing.

Uniform double line spacing has been used for the whole manuscript.

4) Figures, figure captions and tables should be provided in this order at the end of the article.

The order has been corrected but the upload page changes automatically the order and puts the tables before the figures when I click the "Upload File Order" button and, according to the "Attach Files Order" page "The order in which the attached items appear is the order established by this publication".

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All pages have been numbered.

6) The tel/fax numbers (with area and country code) of the corresponding author should be provided on the first page of the manuscript.

Telephone and fax numbers have been included.

Highlights

Assessment of the improvement obtained using ice slurry in heat exchangers.

Chilled carrier fluid compared to ice slurry.

The influence of ice concentration, mass flow rate, heat exchanger length and cooled fluid temperature over pumping power and heat transfer rate is studied.

The optimal ice concentration depends on specific operation conditions and the heat exchanger type.

As a general rule, the optimal ice concentration increases as the heat exchanger length increases.

Heat exchanger performance modelling using ice slurry as secondary refrigerant.

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Abstract.

Ice slurry is a biphasic secondary refrigerant that theoretically allows important energy savings in secondary refrigerant distribution loop compared to single phase refrigerants. However, an accurate evaluation of these energy savings requires the knowledge of the thermal and rheological performance of the refrigerant.

Based on the experimental model developed by the authors, a theoretical analysis of heat exchangers performance is presented in this work in order to calculate the potential energy savings associated to its use. The influence of ice concentration, mass flow rate, heat exchanger length and cooled fluid temperature over pumping power and heat transfer rate is studied. The ratio between heat transfer rate and pumping power is used as the evaluation parameter, which allows us to find the most favourable operation conditions for ice slurry flow.

Results for ice slurry are compared to those obtained for carrier fluid at same inlet temperature to assess the improvement obtained.

Keywords: Ice slurry; Pressure drop; Heat transfer; Heat exchanger.

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Nomenclature

1		
2	A	heat transfer area (m^2)
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4	c_p	specific heat ($\text{J kg}^{-1} \text{K}^{-1}$)
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7	D	pipe diameter (m)
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9		
10	h	convective heat transfer coefficient ($\text{W m}^{-2} \text{K}^{-1}$)
11		
12	H_f	specific latent heat of fusion of ice (J kg^{-1})
13		
14		
15	HTR	heat transfer ratio ($HTR = \dot{q}_{is}/\dot{q}_{cf}$)
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17		
18	IR	improvement ratio ($IR = PR_{is}/PR_{cf}$)
19		
20	k	thermal conductivity ($\text{W m}^{-1} \text{K}^{-1}$)
21		
22		
23	L	tube length (m)
24		
25	\dot{m}	mass flow rate (kg s^{-1})
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28	P	pumping power (W)
29		
30	PPR	pumping power ratio ($PPR = P_{is}/P_{cf}$)
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33	PR	power ratio ($PR = \dot{q}/P$)
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36	\dot{q}	heat transfer rate (W)
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38	T	temperature (K)
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40	ΔT_m	effective mean temperature difference (K)
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43	U	overall heat transfer coefficient ($\text{W m}^{-2} \text{K}^{-1}$)
44		
45	v	flow velocity (m s^{-1})
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Greek symbols

50		
51		
52	ϕ	ice mass fraction (-)
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55	λ	Darcy friction factor (-)
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Subscripts

1 *c* corrugated tube

2 *cf* carrier fluid

3
4
5 *in* tube inner wall

6
7 *is* ice slurry

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10 *out* tube outer wall

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12 *pg* propylene glycol

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15 *s* smooth tube

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22 **1. - Introduction.**

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25 Ice slurry is considered as a very promising secondary refrigerant that, besides the
26
27 reduction on the charge of primary refrigerant associated to any secondary refrigerant,
28
29 allows a reduction in energy consumption compared to single phase secondary
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31 refrigeration systems as well as the possibility of thermal storage. This reduction in
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33 energy consumption has been extensively treated previously and is only outlined here. It
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35 is obtained in two different ways: firstly, the energy efficiency of an ice slurry plant is
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37 greater than that of a plant using a single phase secondary refrigerant (Rivet, 2007;
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39 Stamatiou, 2005); secondly, the energy consumption on the pumps used in the
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41 secondary refrigerant distribution system can be reduced compared to the energy
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43 consumption necessary to pump the traditional single phase secondary refrigerant
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45 (Kauffeld, 2005).
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52 The attention of this paper is focused on the energy savings obtained in the secondary
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54 refrigerant distribution system. An accurate assessment of these savings requires the
55
56 knowledge of ice slurry thermal and rheological performance. The authors of this work
57
58 have experimentally developed a thermal and rheological model for the ice slurry
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1 produced using 9 wt% sodium chloride brine as base solution (Illán and Viedma, 2009a;
2 2009b), which has been experimentally validated in a commercial corrugated tube heat
3 exchanger (Illán and Viedma, 2009c). According to that model, the Darcy friction factor
4 and the Nusselt number for ice slurry flowing through horizontal pipe can be obtained
5 as a function of Reynolds number, ice content and ice particle-pipe diameter ratio:
6 $\lambda = f(Re, \phi, d/D); Nu = f(Re, \phi, d/D)$. Based on this model, a theoretical analysis of
7 smooth and corrugated tube heat exchangers performance is developed in this work in
8 order to analyze the potential energy savings associated to the use of ice slurry.
9 Pumping power and heat transfer rate have been numerically obtained for tube lengths
10 between 0 and 10 meters. Influence of ice content, mass flow rate and cooled fluid
11 temperature have been analyzed for each tube length; the variation range of all these
12 variables analyzed is given in Table 1.
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29 According to Kozawa (Kozawa et al., 2005), one way of categorizing ice slurry thermal
30 storage systems is to distinguish between stores with heterogeneous and homogeneous
31 compositions of ice particles. When heterogeneous storage is employed, the ice slurry
32 can be used in an indirect way. The chilled carrier fluid with no ice particles can be
33 extracted from the bottom of the storage tank and used as conventional single phase
34 secondary refrigerant, maintaining the high thermal storage capacity of ice slurry
35 systems. On the other hand, when homogeneous storage is employed, ice slurry can be
36 extracted from the storage tank and used in a direct way. In this case, some benefits of
37 saving in pipe dimensions are expected.
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51 A power ratio, defined as the ratio between heat transfer rate and pumping power
52 ($PR = \dot{q}/P$), has been used as comparison parameter. The ice slurry power ratio (PR_{IS})
53 has been calculated for the case when ice slurry flows through the heat exchanger.
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1 Similarly, carrier fluid power ratio (PR_{cf}), has been calculated for the case when a
2 heterogeneous storage is used and only carrier fluid flows through the heat exchanger.
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4
5 In order to assess the improvement obtained using ice slurry, an improvement ratio has
6 been defined as the ratio between ice slurry and carrier fluid power ratios ($IR =$
7 PR_{is}/PR_{cf}). Values of improvement ratio higher than 1 will represent those situations
8 where the use of ice slurry improves heat exchanger performance; alternatively, values
9 of improvement ratio lower than 1 imply that the use of ice slurry will not be
10 recommended.
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21 Heat transfer ratio ($HTR = \dot{q}_{is}/\dot{q}_{cf}$) and pumping power ratio ($PPR = P_{is}/P_{cf}$) have
22 also been calculated and plotted in order to obtain additional information about ice
23 slurry performance.
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31 **2. - Procedure.**

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33 Figure 1 shows a sketch of the type of heat exchangers analyzed in this work. It is a
34 tube-in-tube heat exchanger consisting of a single ice slurry tube (outer diameter 20
35 mm, inner diameter 18 mm) mounted inside an outer shell (outer diameter 31 mm, inner
36 diameter 28 mm). The ice slurry stream flows inside the tube, cooling the product (10
37 wt% propylene glycol solution) which flows around it.
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46 The model used in this work is based on the basic correlations obtained by the authors
47 for Nusselt number and Darcy friction factor for ice slurry flow through horizontal
48 smooth and corrugated pipes (Illán and Viedma, 2009a; 2009b). Pumping power and
49 heat transfer rate can be obtained from these basic correlations as shown below.
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55 According to the conclusions obtained in those works, the parameters which have more
56 influence over the heat transfer and pressure drop processes are the Reynolds number
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1 (Re), the ice concentration (ϕ) and the ice particle-pipe diameter ratio (d/D). All the
2 results obtained in this work have been calculated assuming that the ice particle mean
3 diameter remain constant at 500 μm ($d/D = 36^{-1}$), whereas ice concentration has been
4 varied between 5 wt% and 25 wt% and the outlet temperature for propylene glycol
5 solution has been varied between 0 °C and 50 °C.
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11 Since there are no existing recommendations for ice slurry flow through heat
12 exchangers, in order to establish the tube-side velocity for ice slurry, general
13 recommendations for water have been taken into account. According to Kuppan
14 (Kuppan, 2000), the tube-side velocity for water and similar fluids must be maintained
15 between 0.9 to 2.4 $\text{m}\cdot\text{s}^{-1}$; the lower velocity limit corresponds to limiting the fouling,
16 and the upper velocity limit corresponds to limiting the rate of erosion. Other authors
17 (Taborek, 1983) state that, based on overall cost optimization between pumping power
18 cost and cost of fouling, the optimal tube-side flow velocity for cooling water is around
19 2 $\text{m}\cdot\text{s}^{-1}$. Since ice slurry can be used as a cleaning agent (Quarini, 2002), ice slurry mass
20 flow has been initially fixed at 1500 $\text{kg}\cdot\text{h}^{-1}$ to obtain a flow velocity around 1.5 $\text{m}\cdot\text{s}^{-1}$
21 and then reduce pumping power cost without increasing the cost of fouling. In order to
22 obtain similar values for the shell-side and tube-side heat transfer coefficients, mass
23 flow for propylene glycol solution has been initially fixed at 1250 $\text{kg}\cdot\text{h}^{-1}$, leading to a
24 flow velocity of around 1.1 $\text{m}\cdot\text{s}^{-1}$, which falls within the range of 0.6 to 1.5 $\text{m}\cdot\text{s}^{-1}$
25 recommended by Kuppan (Kuppan, 2000) for the shell-side velocity.
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29 In a later analysis, the influence of the ice slurry Reynolds number and the shell-side
30 heat transfer coefficient has also been studied by varying the ice slurry mass flow
31 between 825 $\text{kg}\cdot\text{h}^{-1}$ and 2425 $\text{kg}\cdot\text{h}^{-1}$ (0.85-2.55 $\text{m}\cdot\text{s}^{-1}$ approx.) and the propylene glycol
32 mass flow between 650 $\text{kg}\cdot\text{h}^{-1}$ and 1650 $\text{kg}\cdot\text{h}^{-1}$ (0.6-1.5 $\text{m}\cdot\text{s}^{-1}$ approx.).
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2 *2.1.- Pumping power.*
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4 When the Darcy friction factor, λ , is known, the pressure drop through a straight stretch
5 of tube can easily be obtained by applying the Darcy-Weisbach equation. Therefore, the
6
7 pumping power can be obtained as:
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$$10 \quad P = \lambda \frac{\dot{m}Lv^2}{2D} \quad (1)$$

11
12 where \dot{m} is the mass flow rate in $\text{kg}\cdot\text{s}^{-1}$, L is the pipe length in m, v is the flow velocity
13 in $\text{m}\cdot\text{s}^{-1}$ and D is the pipe diameter in m.
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16 Due to the ice melting, the friction factor value varies along the tube length and its value
17 depends on the heat transfer rate. Therefore the friction factor has been obtained
18 simultaneously to the heat transfer rate, using the correlations proposed by the authors
19 (Illán and Viedma, 2009a, 2009b).
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22
23 *2.2.- Heat transfer rate.*
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26 To obtain the heat transfer rate, the whole heat exchanger was divided into 1 mm length
27 elements. In each element, the differences between inlet and outlet properties are nearly
28 imperceptible and therefore the heat transfer rate can be obtained from the following
29 equation system:
30
31

$$32 \quad \dot{q} = AU\Delta T_m = A \left[\frac{1}{A_{in}h_{in}} + \frac{\ln(D_{out}/D_{in})}{2\pi kL} + \frac{1}{A_{out}h_{out}} \right]^{-1} (\overline{T}_{pg} - \overline{T}_{is}) \quad (2)$$

$$33 \quad \dot{q} = \dot{m}_{is} [(\phi_{inlet} - \phi_{outlet})H_f + (1 - \bar{\phi})\overline{c_{p,cf}}(T_{is,outlet} - T_{is,inlet})] \quad (3)$$

$$34 \quad \dot{q} = \dot{m}_{pg}\overline{c_{p,pg}}(T_{pg,in} - T_{pg,out}) \quad (4)$$

35
36 where the only unknown variables are the heat transfer rate, \dot{q} , the ice slurry outlet
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1 temperature, $T_{is,out}$ and the propylene glycol inlet temperature, $T_{pg,in}$. In these
2 expressions, the mean values for the ice slurry temperature, $\overline{T_{is}}$, the propylene glycol
3 temperature, $\overline{T_{pg}}$, the ice concentration, $\overline{\phi}$, the propylene glycol specific heat, $\overline{c_{p,pg}}$,
4 and the carrier fluid specific heat, $\overline{c_{p,cf}}$, have been obtained as the average between
5 inlet and outlet values.
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11 The heat transfer coefficient in the tube inner wall, h_{in} , has been obtained as a function
12 of the ice slurry mean temperature using the correlations proposed by the authors (Illán
13 and Viedma, 2009a, 2009b).
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21 The heat transfer coefficient in the tube outer wall, h_{out} , has been obtained as a function
22 of the propylene glycol mean temperature, using the correction factors given by
23 Petukhov and Roizen (Petukhov and Roizen, 1964) for turbulent flow in concentric
24 annular ducts. Assuming that the outer wall is insulated, the heat transfer at the inner
25 wall in concentric annuli may be calculated as:
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$$32 \frac{Nu_i}{Nu_{tube}} = 0.86 \left(\frac{D_i}{D_o} \right)^{-0.16} \quad (5)$$

33 where D_i is the diameter of the inner wall of the duct and D_o is the diameter of the outer
34 wall.
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45 **3. – Results and discussion.**

46 Equations (1) to (5) have been used to obtain the improvement ratio for smooth (IR_s)
47 and corrugated (IR_c) heat exchangers, as well as heat transfer and pumping power ratios.
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53 Results are shown below.
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58 *3.1.- Smooth tube heat exchanger results.*

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Fig.2 shows results for the ice slurry improvement ratio (a), the heat transfer ratio (b) and the pumping power ratio (c) for an ice slurry mass flow rate of $1500 \text{ kg}\cdot\text{h}^{-1}$, and a propylene glycol mass flow rate of $1250 \text{ kg}\cdot\text{h}^{-1}$ at an outlet temperature of $0 \text{ }^\circ\text{C}$. As can be seen in Fig. 2.a the improvement ratio increases as heat exchanger length increases, although a critical length exists, around 1.5 m., below which the improvement ratio is lower than 1. According to Fig.2.b, the heat transfer ratio is greater than 1 in almost all cases, except for heat exchangers shorter than 1 meter at very low ice concentrations. This mean that the direct use of ice slurry increases in almost all cases the heat transfer rate. On the other hand, as Fig.2.c shows, the pumping power ratio is always greater than 1, which means that the direct use of ice slurry raises in all cases the pumping power consumption. In those cases where the increase in heat transfer rate compensates for the increase in pumping power consumption, the improvement ratio will be greater than 1 and therefore the direct use of ice slurry improves the performance of the heat exchanger. On the other hand, in those cases where the increase in heat transfer rate does not compensate for the increase in pumping power consumption the indirect use of ice slurry will be recommended over its direct use.

Finally, the ice content has only a slight influence on the heat exchanger performance. As the ice content increases, the heat transfer ratio and the pumping power ratio increase. Due to these two opposite effects, the improvement ratio remains nearly independent of ice content for ice concentrations below 10 %, increasing slightly as ice concentration increases for ice content over 10 %.

Fig. 3 is similar to Fig.2 although in this case the values for improvement, heat transfer and pumping power ratios have been obtained for a propylene glycol outlet temperature of $50 \text{ }^\circ\text{C}$. In this case the ice concentration has a stronger influence over the heat exchanger performance although its influence depends on the heat exchanger's length.

1 For low lengths the heat exchanger's performance improves as ice content increases
2 whereas for medium lengths the tendency is reversed and finally, for high lengths, the
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4 influence is reversed again and beyond a length of 7.88 meters, the heat exchanger's
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6 performance clearly improves as ice content increases. Additionally, the critical length
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8 value varies in this case between 3.61 m. (for 5 % ice content) and 6.01 m. (for 25 % ice
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10 content). The values obtained for intermediate propylene glycol outlet temperatures
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12 vary progressively between the two extreme situations plotted in Fig. 2 and Fig. 3.
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17 Fig.4 shows the evolution of all the parameters that influence the heat exchanger
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19 performance. Results correspond to an ice slurry mass flow rate of $1500 \text{ kg}\cdot\text{h}^{-1}$ and 25%
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21 of ice content and a propylene glycol mass flow rate of $1250 \text{ kg}\cdot\text{h}^{-1}$ and an outlet
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23 temperature of $50 \text{ }^\circ\text{C}$. Although as can be seen in Fig.4.a, the convective coefficient for
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25 ice slurry direct application is in many cases lower than that obtained using indirect
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27 application, Fig.4.c shows that the heat transfer rate for ice slurry direct application is
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29 always greater than that obtained using indirect application, mainly due to the greater
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31 temperature difference obtained thanks to the high thermal capacity of ice slurry. As a
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33 result, Fig.3.b shows how the heat transfer ratio initially increases slightly while the ice
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35 is melting and the convective coefficient decreases for direct application but, once the
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37 ice is completely melted (the vertical dotted line in Figs.3.a,b&c marks the end of the
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39 melting process), the increase in the convective coefficient together with the high
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41 temperature difference improves the heat transfer rate for direct application and
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43 therefore increases the slope for the heat transfer ratio. On another note, as Fig.4.b
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45 shows, due to its lower density, fluid velocity for direct application is initially greater
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47 but, as ice melts, ice slurry density increases and finally, when all ice is melted, density
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49 for direct application is greater than for indirect application and hence velocity for direct
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51 application is lower. Something similar occurs with the friction factor and as a result,
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1 initially the pumping power consumption is greater for direct application but, as the
2 length increases, this tendency is reversed and finally, for high lengths, pumping power
3 consumption is greater using indirect application. This effect can be seen in Fig.3.c
4 which shows an increase in the pumping power ratio for low heat exchanger lengths and
5 a decrease for high lengths. Nevertheless, when comparing Fig.3 and Fig.4 it is
6 necessary to take into account that the ratios plotted in Fig.3 have been obtained for
7 accumulated values of heat transfer and pumping power whereas the data plotted in
8 Fig.4 are instantaneous values.

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20 Fig. 5 shows the influence that ice slurry mass flow rate and propylene glycol mass flow
21 rate have over the improvement ratio. Two extreme situations are plotted in Fig.5.a. In a
22 minimum mass flow rate situation ice slurry and propylene glycol mass flow rates were
23 fixed to 825 and 650 $\text{kg}\cdot\text{h}^{-1}$ respectively whereas in a maximum mass flow rate
24 situation propylene glycol and ice slurry mass flow rates were fixed at 2425 and 1650
25 $\text{kg}\cdot\text{h}^{-1}$. As can be seen, in both cases the improvement obtained using ice slurry is lower
26 than that obtained for the base case (1500 and 1250 $\text{kg}\cdot\text{h}^{-1}$). According to Fig.5.b, for a
27 constant ice slurry mass flow rate of 1500 $\text{kg}\cdot\text{h}^{-1}$, the improvement ratio increases as the
28 propylene glycol mass flow rate increases although the increase obtained is less
29 important as mass flow rate increases. Fig.5.c shows, for a constant propylene glycol
30 mass flow rate of 1250 $\text{kg}\cdot\text{h}^{-1}$, the influence of the ice slurry mass flow rate over the
31 improvement ratio. According to this figure, in almost all cases, the improvement
32 obtained by the direct use of ice slurry increases as ice slurry mass flow decreases. The
33 exception is the ice slurry mass flow rate of 825 $\text{kg}\cdot\text{h}^{-1}$. In this case, due to the low
34 velocity, the fluid flows under laminar flow conditions and pumping power increases
35 due to the high increase in the friction factor.

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Fig.6 helps to better understand the results plotted in Fig.5. According to Fig.6.a, for low propylene glycol mass flow rates, \dot{m}_{pg} , the overall heat transfer coefficient based on the inside tube area, U_{in} , is mainly dominated by the shell-side convective heat transfer coefficient, h_{pg} . As \dot{m}_{pg} increases, the increase of h_{pg} is less important and simultaneously, the influence that a variation of h_{pg} has over U_{in} values become less important (the influence of h_{pg} is similar to the influence of h_{is}) but, in any case, an increase in \dot{m}_{pg} improves the heat exchanger's performance. On the other hand, according to Fig.6.b, an increase in the ice slurry mass flow rate, \dot{m}_{is} , has very low influence over U_{in} because it is mainly dominated by h_{pg} . Although the friction factor, λ_{is} , decreases as \dot{m}_{is} increases, in general terms this decrease in λ_{is} is not enough to compensate for the effect that the increase in flow velocity has over pumping power consumption. Therefore as \dot{m}_{is} increases, the pumping power increases whereas the heat transfer rate remains nearly constant and so heat exchanger's performance worsens. Only at low \dot{m}_{is} values (laminar flow) the heat exchanger's performance improves as \dot{m}_{is} increases. In this case, thanks to the strong decrease in λ_{is} as \dot{m}_{is} increases, the increase in the heat transfer rate is stronger than the increase in the pumping power consumption and therefore the improvement ratio increases.

As a conclusion, in general terms the improvement obtained using ice slurry is higher for the lower ice slurry mass flow rate, the higher ice concentration, the lower outlet temperature for the cooled fluid, the higher cooled fluid mass flow rate and the higher heat exchanger length. Nevertheless, as the outlet temperature for the cooled fluid increases, the influence of the length varies slightly and an initial decrease of the improvement ratio can be observed for low heat exchanger lengths until an inflection point is reached where IR value again increases with heat exchanger length.

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Table 2 shows the absolute values of pressure drop and heat transfer rate obtained for direct and indirect application of ice slurry in cooling propylene glycol until 0 °C, 25 °C and 50 °C. According to these values, 1500 kg·h⁻¹ of ice slurry directly used in a 10 meter long heat exchanger allow a reduction in the temperature of 1250 kg·h⁻¹ of propylene glycol from 6 to 0 °C ($\dot{q} = 8.67 \text{ kW}$), from 65.3 to 25 °C ($\dot{q} = 58.07 \text{ kW}$), or from 126 to 50 °C ($\dot{q} = 111.84 \text{ kW}$), whereas if only the liquid phase is used as refrigerant fluid, the temperature of the propylene glycol flow only can be reduced from 4.5 to 0 °C ($\dot{q} = 6.5 \text{ kW}$), from 56 to 25 °C ($\dot{q} = 44.5 \text{ kW}$), or from 114 to 50 °C ($\dot{q} = 94 \text{ kW}$).

3.2.- Corrugated tube heat exchanger results.

Results of the improvement ratio obtained in corrugated tube heat exchangers are shown in Fig. 7 and Fig. 8 for a propylene glycol outlet temperature of 0 °C and 50 °C respectively. According to Fig. 7.c the pumping power ratio increases as ice content increases whereas, according to Fig. 7.b, for heat exchanger length below 8 meters the heat transfer ratio increases as ice content decreases. Therefore, as Fig. 7.a shows, for heat exchanger lengths below 8 meters the improvement ratio clearly increases as the ice content decreases. Finally, whereas for 5 % ice content the improvement ratio remains over 1 for any heat exchanger length, for 25 % ice content the improvement ratio is below 1 for heat exchanger lengths below 2.4 meters. Fig. 8 shows results for a propylene glycol outlet temperature of 50 °C. Results are qualitatively similar to those shown in Fig. 7, although the inflection point observed in Fig. 7 for 5 % ice content and 8 meters length heat exchanger appears in this case for all ice contents and therefore, for heat exchanger lengths over 6.16 meters, the improvement ratio increases as ice content increases.

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2 Similarly to Table 2, Table 3 summarizes the absolute values of pressure drop and heat
3 transfer rate obtained for direct and indirect application of ice slurry in a corrugated tube
4 heat exchanger of length between 1 and 10 meters.
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7 Fig. 9 shows the influence that ice slurry mass flow rate and propylene glycol mass flow
8 rate have over the improvement ratio. In this case, the influence is similar to that
9 observed in Fig. 5 for smooth tube and the same conclusions are valid for corrugated
10 tube.
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17 18 19 **4. - Conclusions.** 20

21 A theoretical analysis of heat exchanger performance has been presented which allows
22 us to find out those situations where the use of ice slurry as a secondary refrigerant, in
23 substitution of single phase refrigerants, can lead to important energy savings.
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27 The optimal ice concentration depends on specific operation conditions and the heat
28 exchanger type (smooth or corrugated tube). As a general rule, the optimal ice
29 concentration increases as the heat exchanger length increases. Although in most cases
30 the direct use of ice slurry improves the heat exchanger's performance, there are some
31 cases, especially for low heat exchanger length, where the direct use of ice slurry is
32 inadvisable. A careful analysis is strongly recommended before deciding about the use
33 of ice slurry.
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47 48 **Acknowledgements.** 49

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Tube type	Tube length (m)	Ice concentration (wt%)	Ice slurry mass flow rate (kg·s⁻¹)	Propylene glycol outlet temperature (°C)	Propylene glycol mass flow rate (kg·s⁻¹)
Smooth	0 ÷ 10 (ΔL=1 mm)	5, 10, 15, 20 & 25	825, 1225, 1625, 2025 & 2425	0, 25 & 50	650, 900, 1150, 1400 & 1650
Corrugated	0 ÷ 10 (ΔL=1 mm)	5, 10, 15, 20 & 25	825, 1225, 1625, 2025 & 2425	0, 25 & 50	650, 900, 1150, 1400 & 1650

Table 1. Variation range of all variables analyzed.

<i>L</i> (m)	$T_{pg,out} = 0\text{ }^{\circ}\text{C}$				$T_{pg,out} = 25\text{ }^{\circ}\text{C}$				$T_{pg,out} = 50\text{ }^{\circ}\text{C}$			
	\dot{q}_{is}	Δp_{is}	\dot{q}_{cf}	Δp_{cf}	\dot{q}_{is}	Δp_{is}	\dot{q}_{cf}	Δp_{cf}	\dot{q}_{is}	Δp_{is}	\dot{q}_{cf}	Δp_{cf}
	(kW)	(kPa)	(kW)	(kPa)	(kW)	(kPa)	(kW)	(kPa)	(kW)	(kPa)	(kW)	(kPa)
1	0.64	2.20	0.60	2.13	3.89	2.19	3.62	2.11	7.75	2.19	7.27	2.09
2	1.32	4.39	1.22	4.25	8.11	4.37	7.40	4.18	16.08	4.35	15.04	4.10
3	2.04	6.59	1.84	6.36	12.69	6.54	11.36	6.21	25.01	6.50	23.32	6.04
4	2.82	8.78	2.47	8.47	17.66	8.70	15.50	8.20	34.60	8.62	32.10	7.90
5	3.64	10.97	3.11	10.57	23.05	10.84	19.83	10.15	45.28	10.68	41.35	9.70
6	4.51	13.15	3.77	12.66	28.88	12.97	24.36	12.06	56.92	12.64	51.06	11.44
7	5.45	15.34	4.43	14.74	35.23	15.09	29.09	13.93	69.43	14.50	61.19	13.13
8	6.45	17.52	5.11	16.82	42.31	17.17	34.02	15.76	82.81	16.27	71.72	14.77
9	7.52	19.70	5.80	18.89	49.95	19.17	39.15	17.56	97.01	17.95	82.67	16.37
10	8.67	21.87	6.50	20.95	58.07	21.11	44.50	19.33	111.84	19.58	94.03	17.93

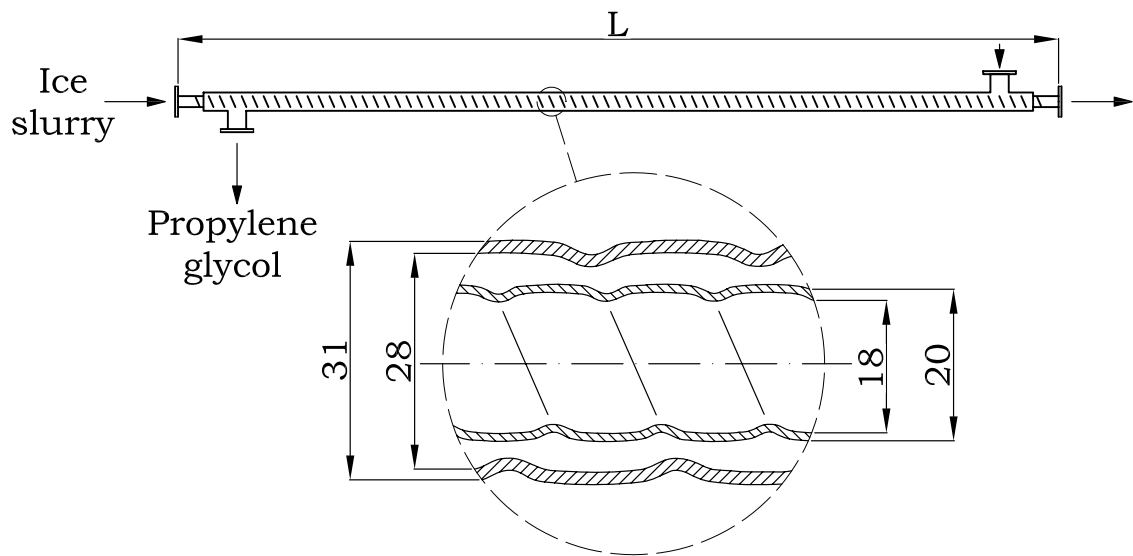
Table 2. Absolute values of heat transfer rate and pressure drop for 25 % ice content ice slurry

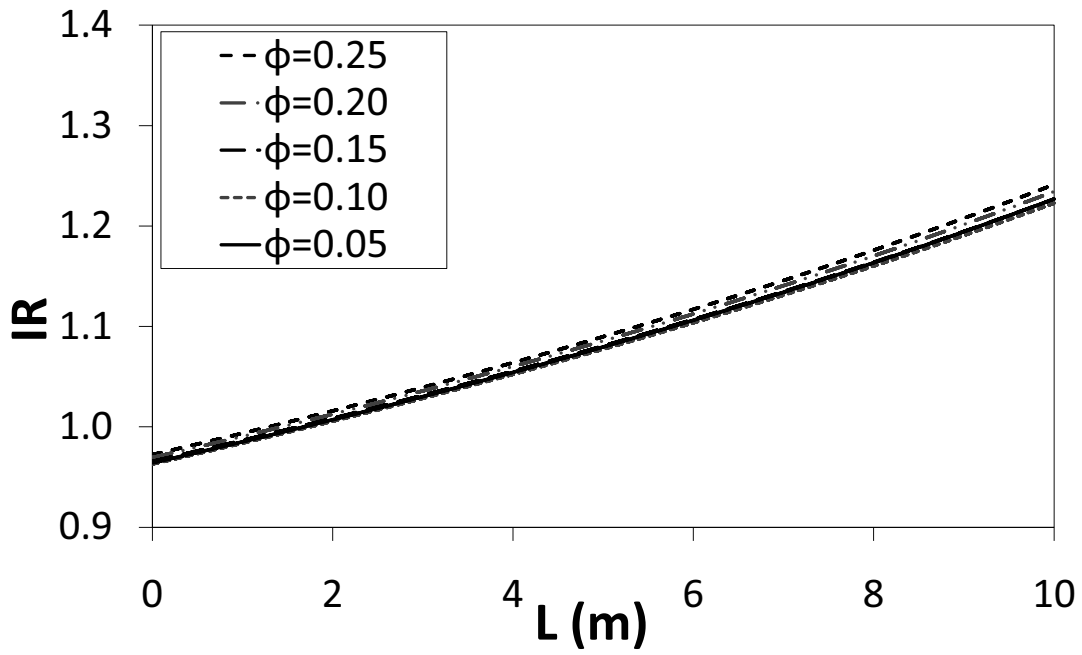
direct and indirect application in smooth tube heat exchangers.

<i>L</i> (m)	$T_{pg,out} = 0\text{ }^{\circ}\text{C}$				$T_{pg,out} = 25\text{ }^{\circ}\text{C}$				$T_{pg,out} = 50\text{ }^{\circ}\text{C}$			
	\dot{q}_{is}	Δp_{is}	\dot{q}_{cf}	Δp_{cf}	\dot{q}_{is}	Δp_{is}	\dot{q}_{cf}	Δp_{cf}	\dot{q}_{is}	Δp_{is}	\dot{q}_{cf}	Δp_{cf}
	(kW)	(kPa)	(kW)	(kPa)	(kW)	(kPa)	(kW)	(kPa)	(kW)	(kPa)	(kW)	(kPa)
1	0.98	4.12	1.00	4.08	5.44	4.11	5.56	4.05	10.57	4.09	10.87	4.02
2	2.06	8.23	2.02	8.15	11.68	8.18	11.43	8.03	22.81	8.13	22.54	7.90
3	3.24	12.34	3.06	12.21	18.82	12.22	17.60	11.93	36.91	12.10	34.97	11.65
4	4.55	16.44	4.12	16.25	27.00	16.23	24.10	15.77	53.07	16.05	48.10	15.29
5	5.99	20.53	5.21	20.28	36.43	20.18	30.91	19.53	70.55	19.81	61.86	18.83
6	7.59	24.62	6.33	24.29	47.19	24.16	38.05	23.22	89.23	23.42	76.22	22.29
7	9.36	28.69	7.47	28.29	58.75	28.02	45.51	26.86	108.97	26.90	91.16	25.68
8	11.32	32.76	8.63	32.27	71.04	31.76	53.29	30.44	129.58	30.29	106.66	29.01
9	13.52	36.81	9.82	36.24	84.00	35.38	61.37	33.97	150.99	33.60	122.67	32.28
10	15.97	40.86	11.04	40.19	97.57	38.91	69.73	37.45	173.12	36.82	139.16	35.50

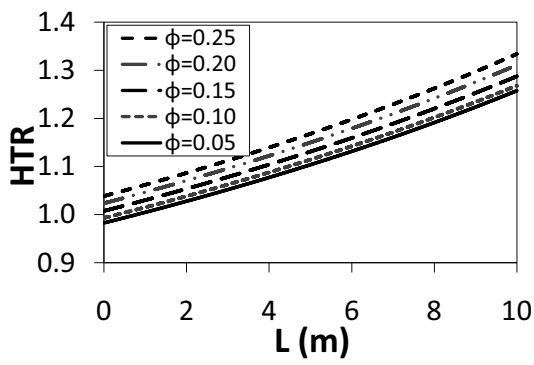
Table 3. Absolute values of heat transfer rate and pressure drop for 25 % ice content ice slurry direct and indirect application in corrugated tube heat exchangers.

Figure 01

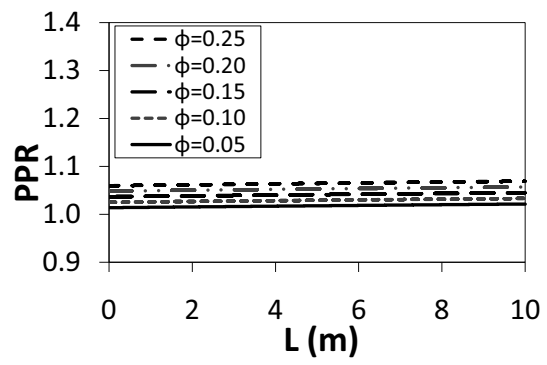




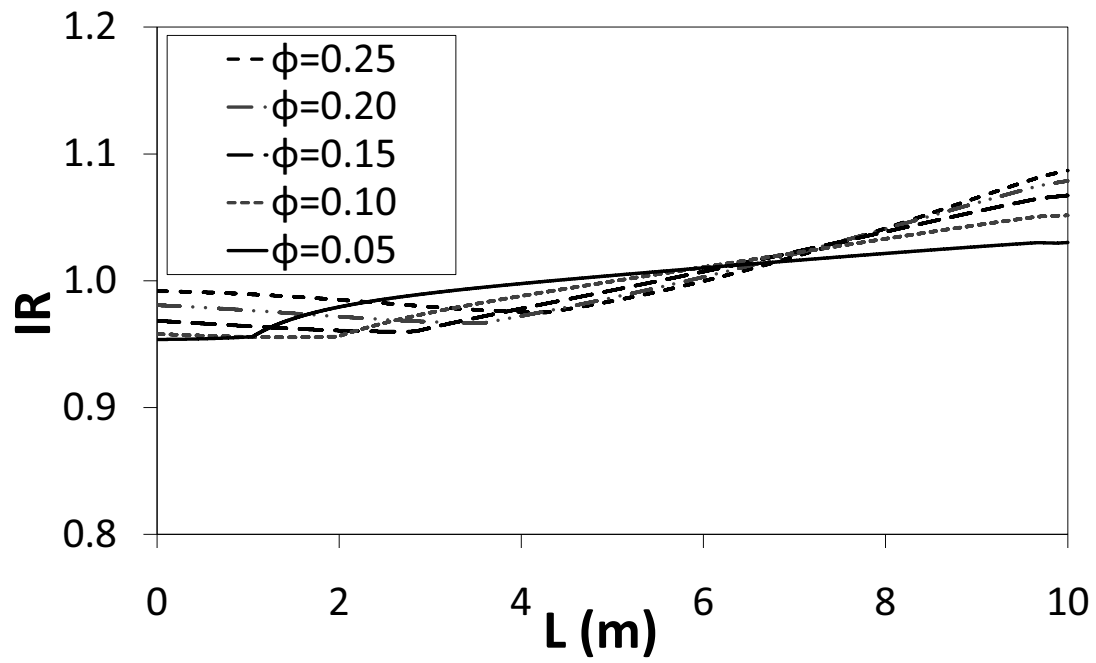
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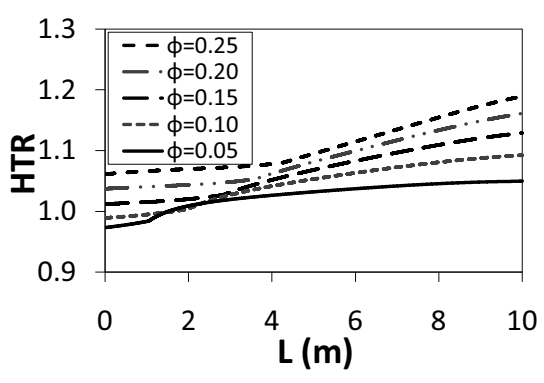
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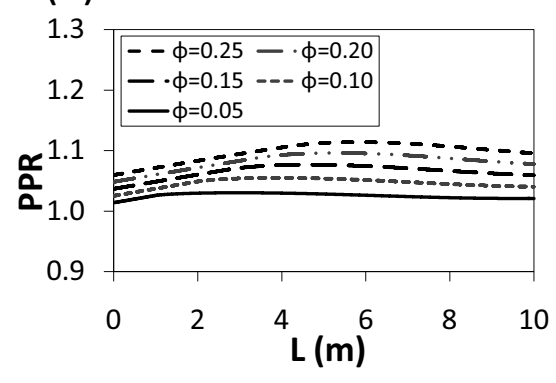
(c)



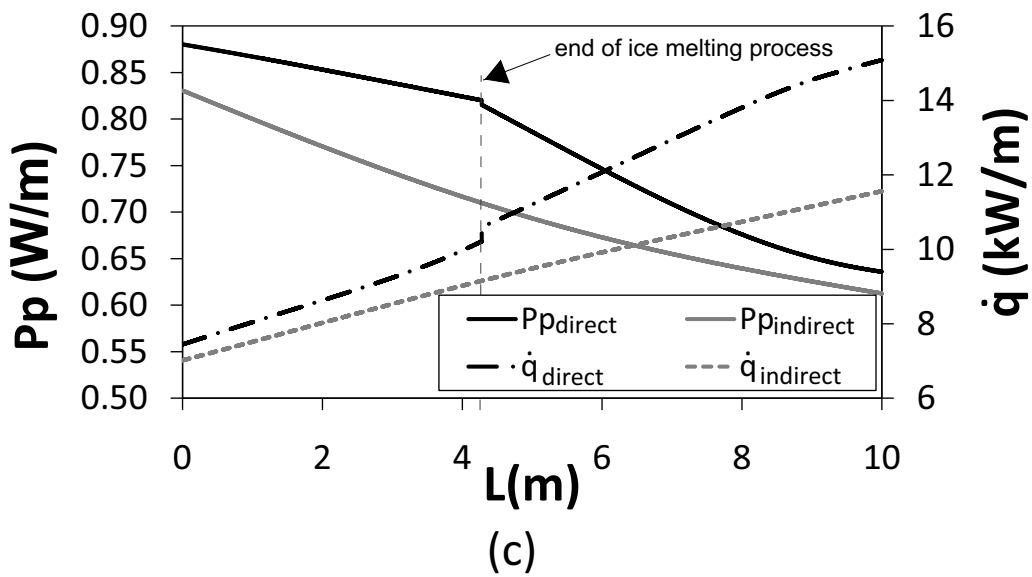
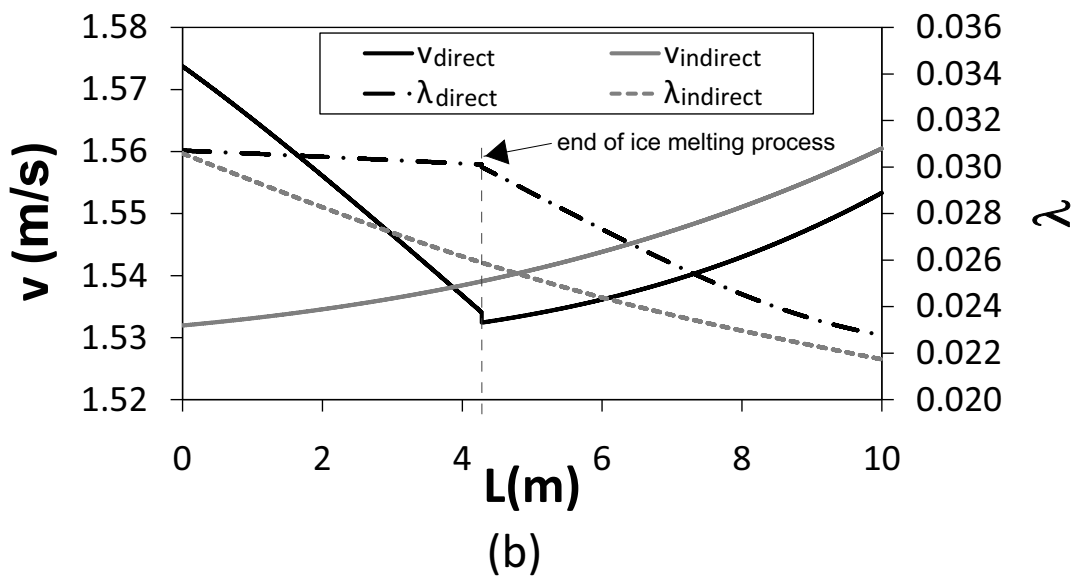
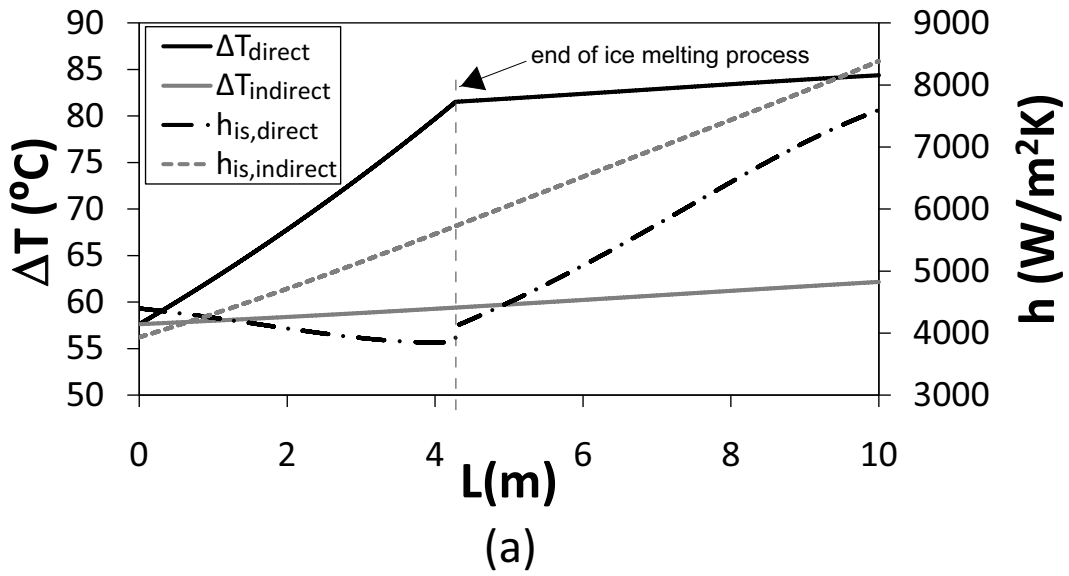
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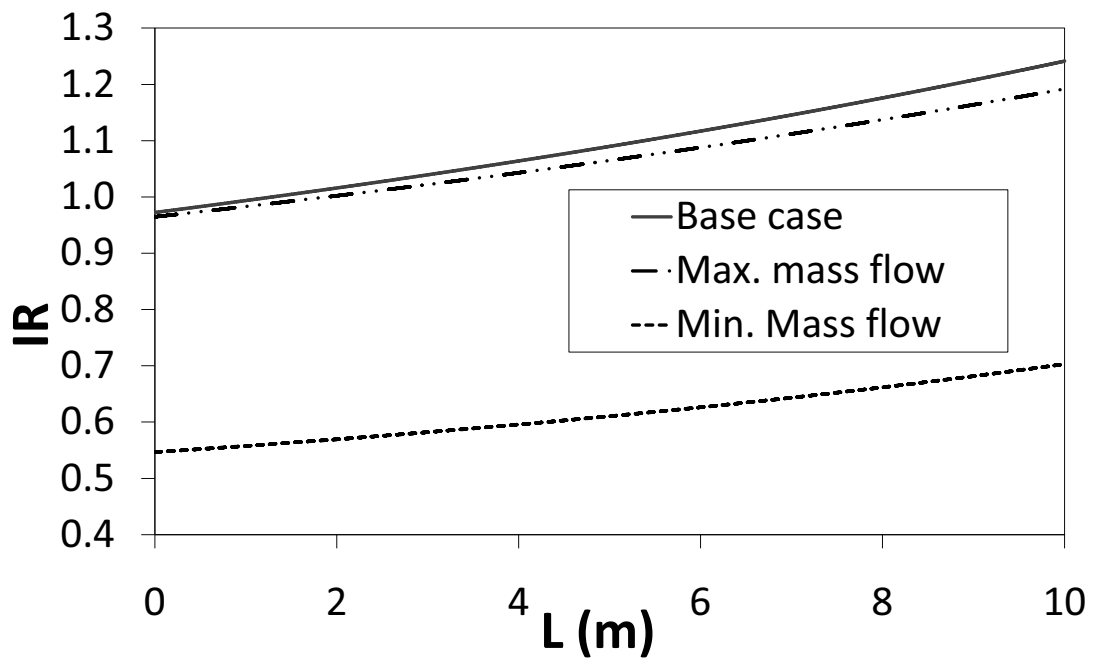


(b)

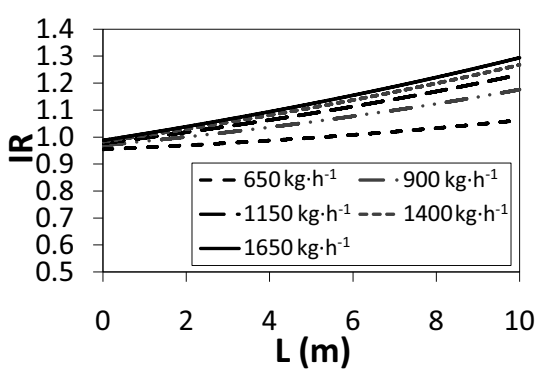


(c)

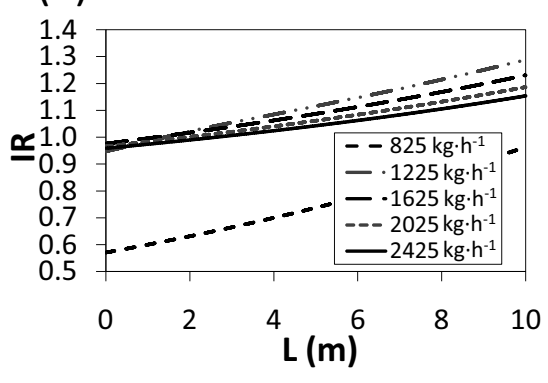




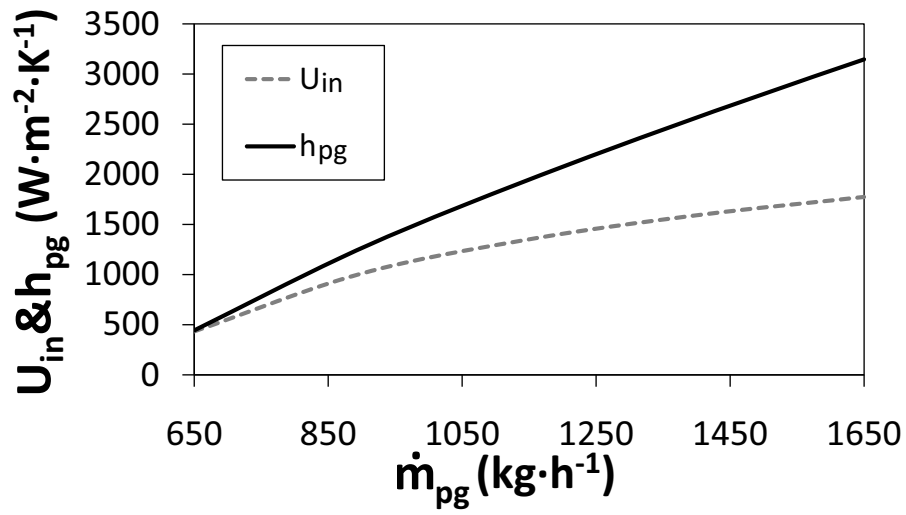
(a)



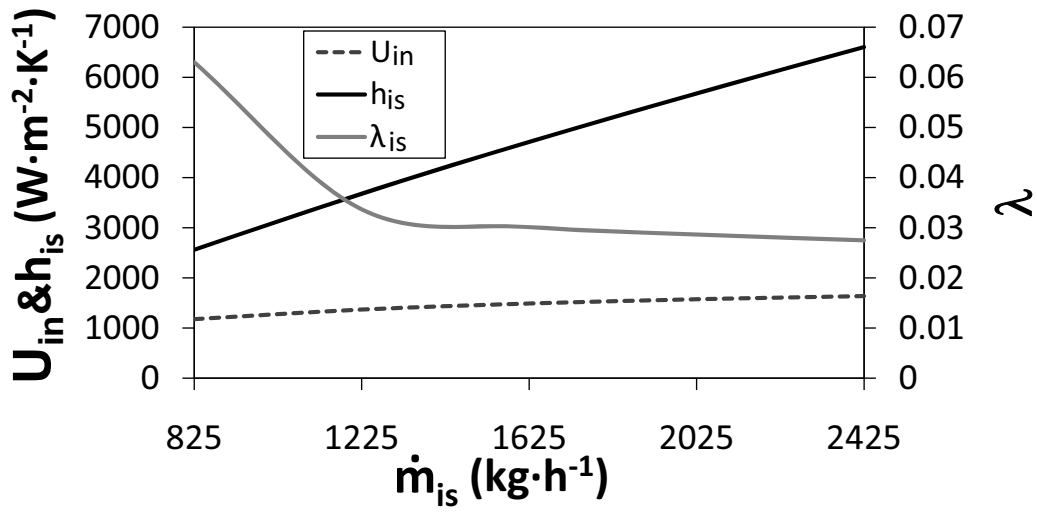
(b)



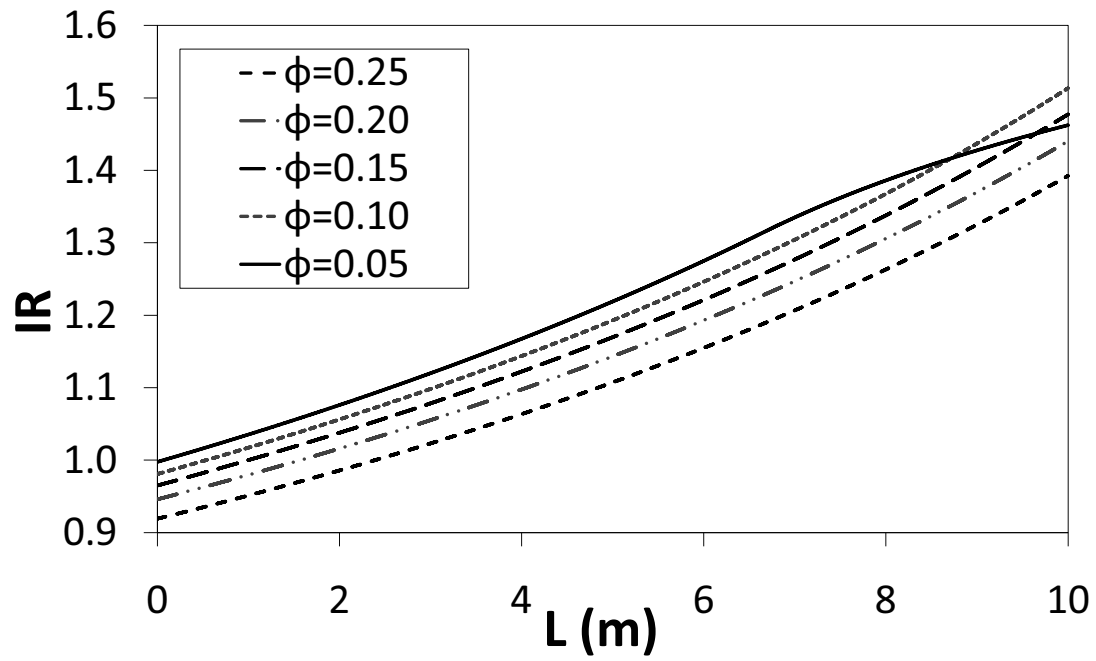
(c)



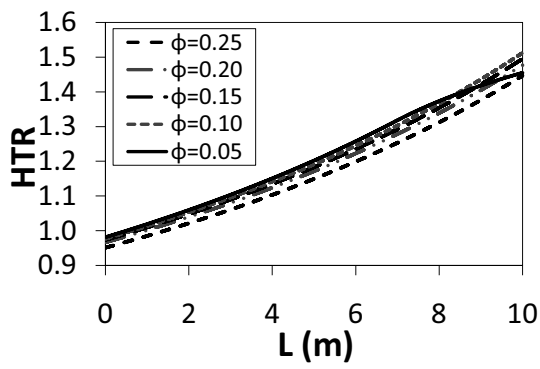
(a)



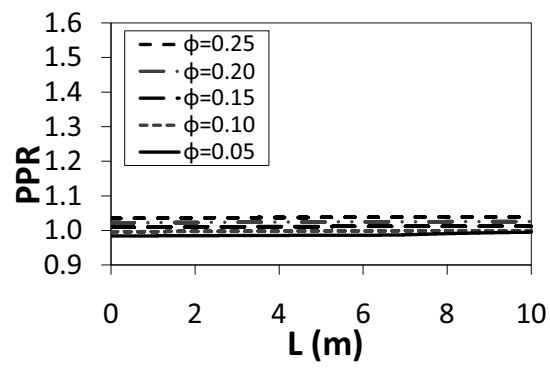
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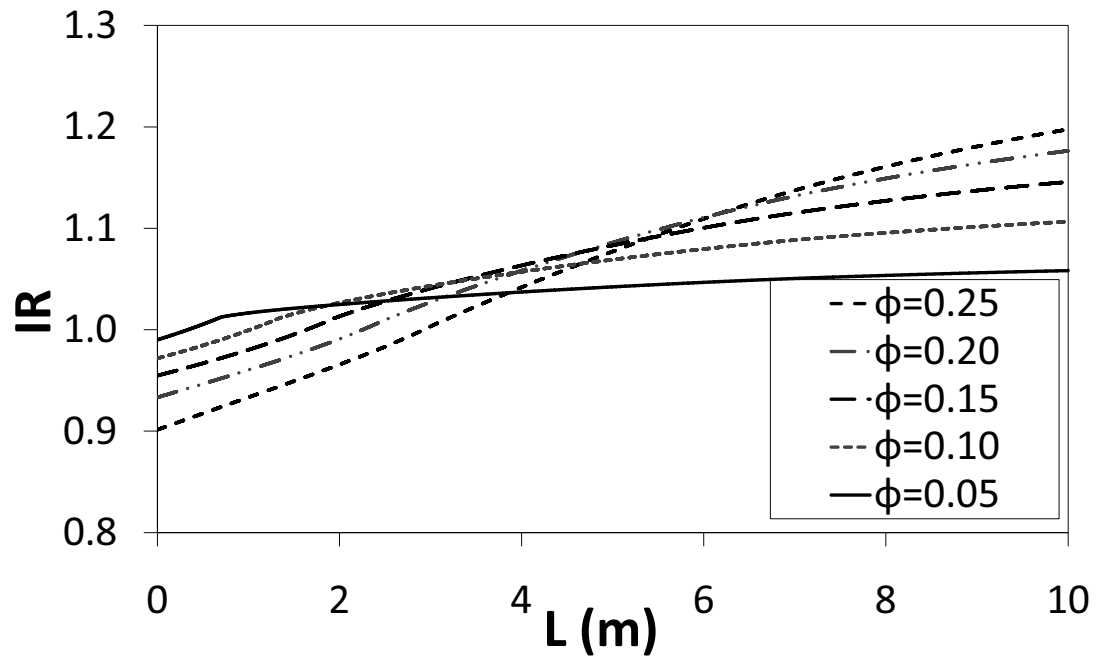
(a)



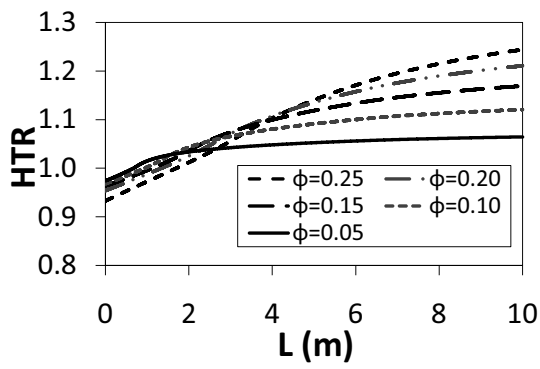
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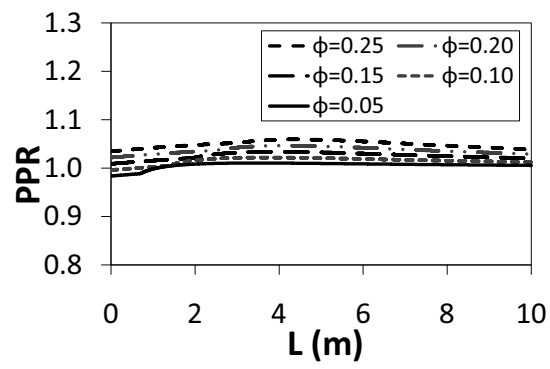
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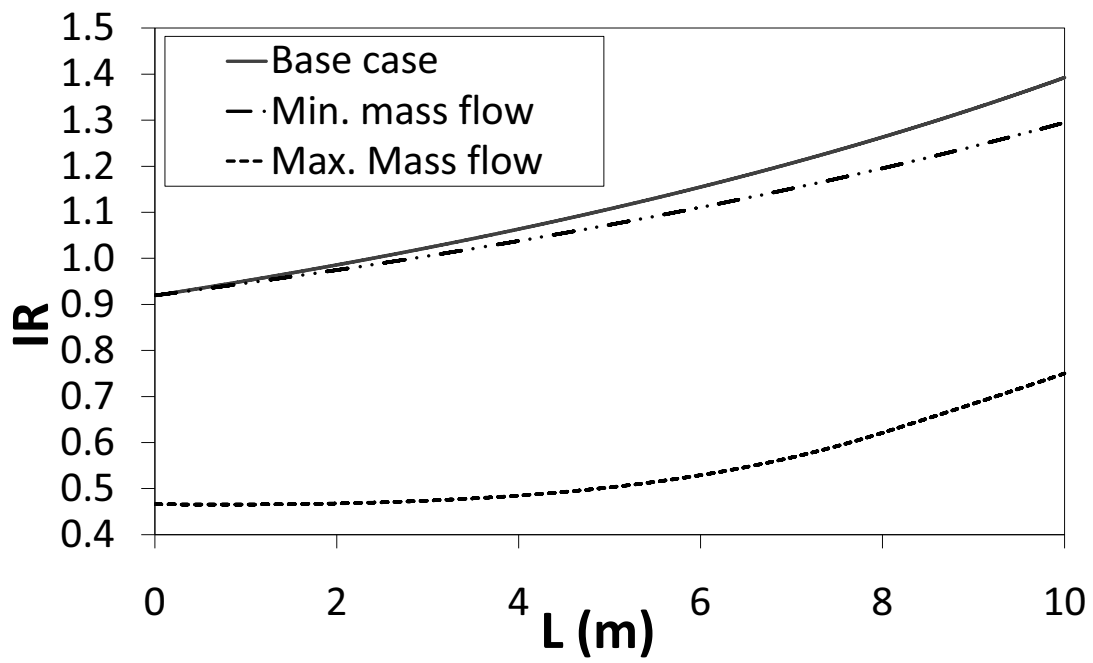
(a)



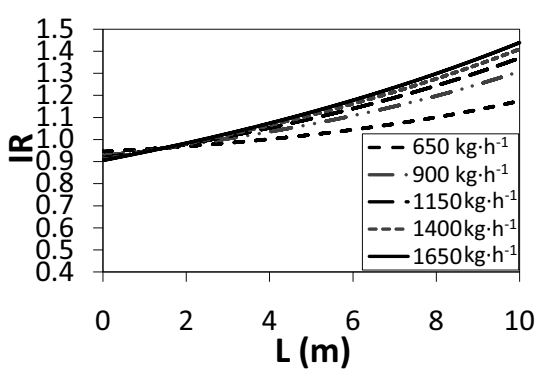
(b)



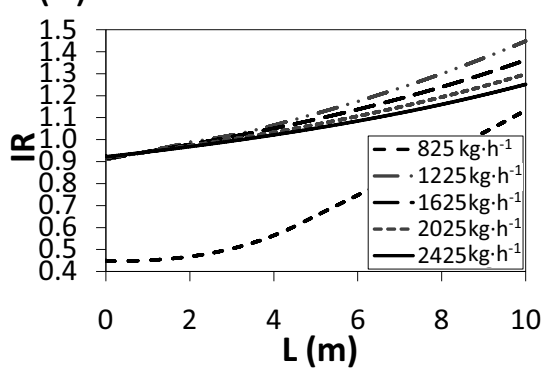
(c)



(a)



(b)



(c)

Figure 1. Sketch of the heat exchanger analyzed.

Figure 2. Improvement ratio (a), heat transfer ratio (b) and pumping power ratio (c) for smooth tube heat exchangers with an ice slurry mass flow rate of $1500 \text{ kg}\cdot\text{h}^{-1}$ and a propylene glycol mass flow rate of $1250 \text{ kg}\cdot\text{h}^{-1}$ and outlet temperature of 0°C .

Figure 3. Improvement ratio (a), heat transfer ratio (b) and pumping power ratio (c) for smooth tube heat exchangers with an ice slurry mass flow rate of $1500 \text{ kg}\cdot\text{h}^{-1}$ and a propylene glycol mass flow rate of $1250 \text{ kg}\cdot\text{h}^{-1}$ and outlet temperature of 50°C .

Figure 4. Convective coefficient and temperature difference (a), flow velocity and Darcy friction factor (b) and pumping power and heat flow per unit length (c) for smooth tube heat exchangers with an ice slurry mass flow rate of $1500 \text{ kg}\cdot\text{h}^{-1}$ and 25 % ice content and a propylene glycol mass flow rate of $1250 \text{ kg}\cdot\text{h}^{-1}$ and outlet temperature of 50°C .

Figure 5. Improvement ratio for maximum, minimum and standard mass flow rate conditions (a). Influence of propylene glycol mass flow rate (b) and ice slurry mass flow rate (c) over heat exchanger improvement ratio for smooth tube heat exchangers with 25 % ice content and propylene glycol outlet temperature of 0°C .

Figure 6. Influence of propylene glycol mass flow rate (a) and ice slurry mass flow rate (b) over the heat exchanger's overall heat transfer coefficient for smooth tube heat exchangers with 25 % ice content and propylene glycol outlet temperature of 0°C .

Figure 7. Improvement ratio (a), heat transfer ratio (b) and pumping power ratio (c) for corrugated tube heat exchangers with an ice slurry mass flow rate of $1500 \text{ kg}\cdot\text{h}^{-1}$ and a propylene glycol mass flow rate of $1250 \text{ kg}\cdot\text{h}^{-1}$ and outlet temperature of $0 \text{ }^\circ\text{C}$.

Figure 8. Improvement ratio (a), heat transfer ratio (b) and pumping power ratio (c) for corrugated tube heat exchangers with an ice slurry mass flow rate of $1500 \text{ kg}\cdot\text{h}^{-1}$ and a propylene glycol mass flow rate of $1250 \text{ kg}\cdot\text{h}^{-1}$ and outlet temperature of $50 \text{ }^\circ\text{C}$.

Figure 9. Improvement ratio for maximum, minimum and standard mass flow rate conditions (a). Influence of propylene glycol mass flow rate (b) and ice slurry mass flow rate (c) over heat exchanger improvement ratio for corrugated tube heat exchangers with 25 % ice content and propylene glycol outlet temperature of 0°C .