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1 Lightning parameters of sprites and diameter of halos

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10 Abstract

- 11 Transient Luminous Events (TLEs) above thunderclouds have been associated with variables 12 such as the lightning Charge Moment Change (CMC), charge height, charge transfer, and 13 rise-time. We show for the first time a survey of the CMC, rise-time, fall-time, peak electric 14 field, and peak current of the lightning discharges associated with 11 column, 11 carrot, and 15 18 sprites with halo. We found that carrot sprites are induced by a lightning discharge with 16 CMC, peak electric field, and peak current greater and less than that for column sprites and 17 sprites with halo, respectively. Sprites with a halo are initiated by a lightning discharge with a 18 longer rise-time and fall-time than that for column and carrot sprites. Column sprites top 19 altitude and carrot sprites brightest region altitude positively correlate with lightning rise-20 time. Lightning fall-time, peak electric field, and peak current increase with a decrease in the 21 top and brightest region altitudes for carrot sprites. For the altitude of the sprites brightest 22 region, column sprites correlate negatively with lightning fall-time, peak electric field, and 23 CMC, and column sprites top altitude also correlates negatively with lightning peak electric 24 field. Sprites with a halo top altitude increased with lightning fall-time and peak current, and 25 sprites with a halo brightest altitude increased with an increase in lightning CMC. Halo 26 diameters correlate positively with lightning fall-time, peak electric field, and peak current.
- 27 Keywords: Lightning rise-time; lightning fall-time; lightning Charge Moment Change;28 Lightning electric field; Lightning current; Transient Luminous Events altitude

30 1. Introduction

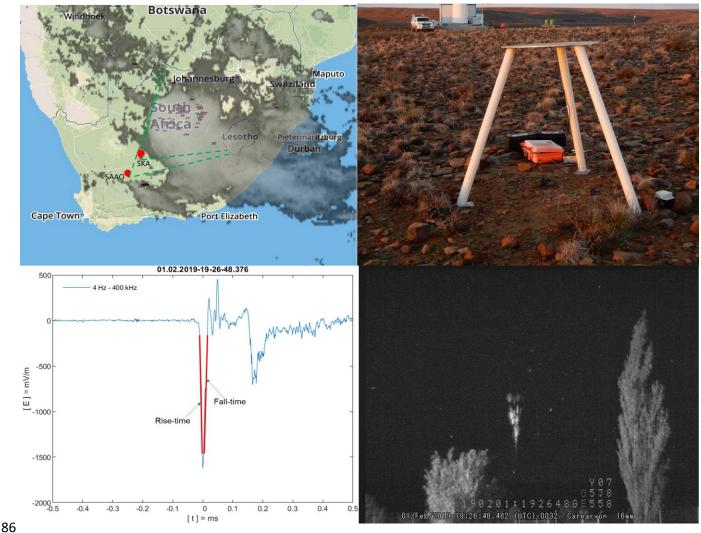
31 Sprites are vertically oriented luminous electric discharges induced by the cloud-to-ground 32 (CG) lightning quasi-static electric field and continuing current. They appear at stratospheric 33 and mesospheric altitudes of about 40 to 100 km (Füllekrug et al., 2006; Liu et al., 2015; 34 Pasko, 2010; Pasko et al., 2013; Siingh et al., 2012; Surkov and Hayakawa, 2020). In 35 contrast, halos manifest as a horizontal disc of luminous emission, also generated by the CG 36 lightning quasi-static electric field and continuing current, at ionospheric altitudes of about 85 37 km. The duration of the electric field at a certain altitude is almost equivalent to the local 38 Maxwellian relaxation time, which is defined as the permittivity of free space over the local 39 conductivity. The local Maxwellian relaxation time increases with a decrease in atmospheric 40 altitude (Liu et al., 2015; Pasko et al., 1997). 41 Sprites and halos may be induced by mainly positive CG lightning electric fields, although 42 some are generated by negative CG lightning discharge. Sprite streamers tend to develop 43 from halos (Luque & Ebert, 2009). Column sprites are associated with only the downwards 44 propagation of streamers, whereas carrot sprites are associated with both downwards and 45 upwards streamer propagation (Bór, 2013). The Transient Luminous Events (TLE) manifest 46 themselves about 1—100 ms after the parent CG lightning flash. (Bering et al., 2004; Chen et 47 al., 2019; Frey et al., 2007; Liu et al., 2015; McHarg et al., 2002; Siingh et al., 2012; 48 Williams et al., 2012). The parent lightning waveforms are shorter than the duration of the 49 TLE luminosity. 50 Parameters such as lightning charge height, charge transfer, rise-time, and Charge Moment 51 Change (CMC) are essential in determining whether the lightning stroke initiates sprites or 52 halos (Asano et al., 2008; Yaniv et al., 2014; Haspel et al., 2020; Li et al., 2008; Mashao et 53 al., 2021). Lightning with a mean and minimum CMC value of approximately 1480 C-km 54 and 63 C-km has been associated with the generation of sprites (Chen et al., 2019). 55 Enhancement in sprites brightness with an increase in lightning CMC has been reported by 56 Yaniv et al. (2014), Yang et al. (2017), and Nnadih et al. (2018). Mashao et al. (2021) 57 demonstrated a positive correlation between lightning CMC and sprites top altitude. The 58 importance of lightning rise-time on sprites has been established by Asano et al. (2008) using 59 a two-dimensional computer simulation for summer and winter storm conditions. According 60 to Asano et al. (2008), lightning charge height, charge transfer, and rise-time are essential in 61 the generation and development of sprites. The sprites breakdown region reduces in altitude

62 for a longer rise-time (>25 μ s) (Asano et al., 2008). We are not aware of any reported 63 lightning fall-time regarding TLEs.

64 The altitudes of sprites have been well established using different techniques and high-speed 65 cameras. The sprites top altitude has been observed to vary from 73 to 96 km, whereas the 66 altitude of the sprites brightest region has been found to span from 50 to 84.1 km (Füllekrug 67 et al., 2019; Luque et al., 2016; Mashao et al., 2021 Malagón-Romero et al., 2020; Sentman 68 et al.,1995; Stenbaek-Nielsen et al., 2010; Wescott et al., 1998). Mashao et al. (2021) found 69 that the average sprites top altitude in South Africa occurred at approximately 84.3 km. Other 70 authors found sprite top altitudes at 88 km (Sentman et al., 1995), 86.4 km (Wescott et al., 71 1998), and 79-96 km (Stenbaek-Nielsen et al., 2010). Mashao et al. (2021) found that the 72 average altitude of maximum brightness in South Africa occurred at approximately 69 km. 73 Other authors found the altitude of maximum brightness at 70 km (Malagon-Romero et al., 74 2020) and 71.2-72.4 km (Luque et al., 2016). Wescott et al. (2001) observed that the top 75 altitude of sprites with halos varied from 73.5 km to 85.2 km, with an apparent diameter of 76 about 66 km. Taylor et al. (2008) found a diameter of about 89± 5 km for a negative CG 77 sprite with a halo. According to Miyasato et al. (2002), the average halo diameter was about 78 86 km.

79 In this paper, we demonstrate for the first time the importance of lightning CMC, peak 80 electric field, peak current, rise-time, and fall-time on sprites altitude and halo diameters for 81 different sprites morphologies. This is done by evaluating the linear correlation between 82 lightning CMC, peak electric field, peak current, rise-time, and fall-time versus the top 83 altitude and altitude of the brightest region of column sprites, carrot sprites, and any sprites 84 with halos. In addition, we measure the diameter of halos in South Africa for the first time.

85 2. Observations



87 Fig. 1. South African map (top left panel, obtained from EarthNetworks) denoting the thunderstorm which 88 initiated some of the TLEs in this paper and observation sites (red dots) of the South African Astronomical 89 Observatory (SAAO) and Square Kilometre Array (SKA) in the Northern Cape, South Africa. The green dotted 90 lines show camera viewing directions. The yellow plus, yellow negative, and pink dash-like symbols denote the 91 positive CG, negative CG, and intracloud lightning, respectively. Lightning vertical electric field (bottom left 92 panel) associated with a carrot sprite (bottom right panel) measured by the ELF receiver (4 Hz- 400 kHz) (top 93 right panel). The red lines (bottom left panel) indicate where the rise-time and fall-time were calculated from 94 90% to 10% of the maximum electric field signal deflection from the background. A carrot sprite recorded on 01 95 February 2019 at 19:26:48.558 UTC (bottom right panel) using a Watec 910Hx camera.

96 2.1 Camera systems

97 The 2019 sprites campaign was conducted from 28 January to 15 February 2019. Out of 98 about 208 TLEs, 40 TLEs consisting of 11 column, 11 carrot, and 18 sprites with halos were 99 selected for our analysis. The TLEs presented here were recorded using Watec 910Hx 100 cameras (Bór, 2013; Gamerota et al., 2011; Liu et al., 2016; Soula et al., 2009; Stenbaek-

101 Nielsen et al., 2010; Yaniv et al., 2014). We selected the TLEs that only contain column, 102 carrot, and sprites with a halo to make a fair parent lightning parameters comparison. 103 However, sprites with a halo consist of column, carrot, wishbone, and jellyfish sprites. Fig. 1 104 (top left panel) shows two distinct locations; the Square Kilometre Array (SKA) (30.97° S, 105 21.98° E) and the South African Astronomical Observatory (SAAO) (32.38° S, 20.81° E), 106 where the Watec 910Hx cameras were operated. Both locations are in the Karroo desert of 107 the Northern Cape of South Africa, see Fig. 1 (top left panel). Several Mesoscale Convection 108 Systems (MCS) initiated the TLEs, moving from the northwest to the southeast over South 109 Africa on 29 and 30 January as well as 1, 2, and 11 February 2019. The MCS produce TLEs 110 for about 4 hours on average each night. Fig. 1 (top left panel) shows one MCS that induced 111 the observed TLEs events (https://www.earthnetworks.com/product/decision-support-112 collaboration-tools/sferic-maps/). The 40 TLEs presented here were recorded on 29, 30 113 January and 11 February 2019 from SAAO and 1 and 2 February 2019 from SKA. Fig. 1 114 (bottom right panel) shows an example carrot sprite observed from SKA on 1 February 2019. 115 The Watec 910Hx cameras had a 8.0 mm f/1.4 C-mount lens, giving a field of view (FOV) of 116 46.2° horizontal and 29° vertical. The Watec 910Hx cameras operated under fixed gain and a 117 gamma factor of 0.45. The observation systems recorded sprites video clips at 25 fps with a 118 40 ms frame period. A GPS video timer installed in one camera system provided millisecond 119 timing. A Network Timing Protocol server provided timing accuracy of about 1 ms for the 120 other camera systems at SKA and SAAO. The camera systems operated with 8-bit intensity 121 resolution. The video images had a size of 640x480 pixels with an angular resolution of 122 0.072° horizontal and 0.061° vertical per pixel. Thus, 1 pixel is 0.061° in elevation angle.

123 2.2 Altitude estimation

124 The stars in the sprites image background allowed us to determine the azimuth and elevation 125 angle of every pixel. The stars declination and right ascension from the star almanac, event 126 time, and observation site were used to fit the modeled stars onto the real stars in the sprites 127 image background in order to find the camera pointing direction and FOV, and to determine 128 the azimuth and elevation angle of each pixel. To estimate the altitude of sprites, we assumed 129 that sprites were induced directly above their parent CG lightning strokes. This supposition is 130 usually used in TLEs studies (Füllekrug et al., 2019; Li et al., 2008; Luque et al., 2016; 131 Mashao et al., 2021; McHarg et al., 2007). The sprites altitude was estimated from their 132 elevation angle and ground distance from the observation location. This was done by 133 employing planar trigonometry in the vertical plane and spherical trigonometry in the

134 horizontal plane. The method is fully described in Mashao et al. (2021). The altitude of 135 sprites uncertainty, which depends on the slant distance between observation location and 136 targeted sprites altitude, spanned ± 0.33 -0.47 km.

137 The sprites altitudes were estimated for two regions: the top altitude and the altitude of the 138 brightest region. For a vertical profile through each TLE, the top altitude is the highest 139 elevation angle pixel with an intensity value greater than the background. The diameter of the 140 halos is determined in the same way for a horizontal profile. The altitude of maximum 141 brightest is taken from the pixel of greatest intensity value within the TLE. The sprite top 142 altitude is where electric field energy within a sprite is normally less than the altitude 143 dependent critical breakdown field. The brightest region is where photon production 144 maximizes due to collisions between the accelerated electrons and background neutrals (Liu 145 et al., 2015; Mashao et al., 2021).

146 2.3 Lightning detection

147 We obtained the lightning information (time, position, peak current) of the TLEs parent CG 148 lightning strokes from the South African Weather Service (SAWS) and Earth Networks (EN) 149 (Gijben, 2012; Zhu et al., 2017). The parent CG lightning strokes were located between 242 150 and 707.5 km away from the observation sites, so well within the maximum observing range 151 (900 km). The parent lightning strokes were all of the positive polarity with a peak current 152 spanning from 32 to 179 kA. Based on timing data, SAWS and EN did not detect all 153 lightning discharges which initiated the TLEs. This limited the number of TLEs to report.

154 2.4 Electromagnetic Waveforms

155 A wideband digital ELF radio receiver, co-located with the cameras, detected the lightning 156 vertical electric field strength associated with the optical sprites in the frequency ranging 157 from ~4 Hz to ~400 kHz with a sampling frequency of 1 MHz and timing accuracy of 12 ns 158 (see Fig. 1, top right panel) (Füllekrug, 2010). The ELF radio receiver was positioned in a 159 low radio interference area near the SKA site. The TLEs parent lightning electric field 160 strength span 1.0-3.8 V/m at the ELF radio receiver location. The lightning rise-time and fall-161 time were computed from the vertical electric field measured simultaneously with the optical 162 observations (Füllekrug, 2010; Füllekrug et al., 2019). The rise-time calculations were from 163 90% to 10% of the maximum electric field signal deflection from background. The same 164 method was applied to the fall-time (see Fig. 1, bottom left panel).

165 The lightning CMC values ranged from 689 to 6,780 C-km and were computed from the far166 field magnetic field data recorded by a broadband ELF system installed in the Bieszczady
167 mountains in Poland (49.20° N, 22.54° E), using the method described by Mlynarczyk et al.
168 (2015). The ELF system measures the two horizontal magnetic field components in the
169 frequency range from 0.01 to 1,000 Hz with a sampling frequency of 3 kHz (Mlynarczyk et
170 al., 2018). Due to signal noise and unknown locations of the parent lightning strokes, we
171 could compute the lightning CMC for 31 TLEs, see Table 1 in the appendix.

172 All data are summarized in Table 1 in the appendix.

173 3. Results and discussions

174 An analysis of lightning rise-time, fall-time, peak electric field, peak current, and CMC 175 associated with TLEs was conducted on 11 column sprites, 11 carrot sprites, and 18 any 176 sprites with halos. Note that the sprites with halos have different morphologies, i.e., column, 177 carrot, wishbone, and jellyfish. The lightning electric radiated fields propagate as $\frac{1}{r^2}$, 178 where r is the distance from the lightning location to the receiver location (Cooray and 179 Lobato, 2020). For comparison, we normalized the lightning peak electric field values for the 180 distance from the ELF receiver to the lightning stroke location. This was done by multiplying 181 the lightning peak electric field values by the distance squared (in km) relative to 1 km 182 (Taylor and Jean, 1959).

The lightning normalized peak electric field, peak current, rise-time, fall-time, and CMC 184 associated with the analyzed TLEs vary from 93 to 914 kV/m, 32 to 179 kA, 6 to 25 μ s, 1 to 185 91 μ s, and 689 to 6,780 C-km, respectively. Most of the investigated TLEs producing parent 186 lightning had a very short rise-time (<15 μ s) and short fall-time (<25 μ s); see Table 1. We 187 found that TLEs top altitudes vary from 71 to 90.5 km, with an average and standard 188 deviation of 79.8 and 5.2 km, respectively. The TLEs top altitudes are in the altitude range 189 previously reported in the literature (Füllekrug et al., 2019; Luque et al., 2016; Mashao et al., 190 2021 Malagón-Romero et al., 2020; Sentman et al.,1995; Stenbaek-Nielsen et al., 2010; 191 Wescott et al., 1998). The analyzed TLEs brightest region altitude ranged from 50 to 73 km, 192 with an average and standard deviation of 61.5 and 6.4 km, respectively. The TLEs altitude 193 of maximum brightness are in the altitude range reported in the literature (Füllekrug et al., 194 2019; Luque et al., 2016; Mashao et al., 2021 Malagón-Romero et al., 2020; Sentman et 195 al.,1995; Stenbaek-Nielsen et al., 2010; Wescott et al., 1998).

196 The top altitude for column sprites, carrot sprites, and sprites with halos (halo top) varied 197 from 72.4 to 86.4 km, 70.7 to 87 km, and 71.5 to 90.5 km, respectively. We obtained an 198 average top altitude for column sprites, carrot sprites, and sprites with halos of about 80.4, 199 80.6, and 78.9 km, with the standard deviation of about 4.6, 5.1, and 5.6 km, respectively. 200 The brightest region altitude for column sprites, carrot sprites, and sprites with halos ranged 201 from 55.1 to 73 km, 50 to 68.5 km, and 50 to 68 km, respectively. The average altitude for 202 column, carrot, and sprites with halos was 66 (6.5), 61 (5.5), and 59 (5.2) km, where the 203 value in parenthesis is the standard deviation.

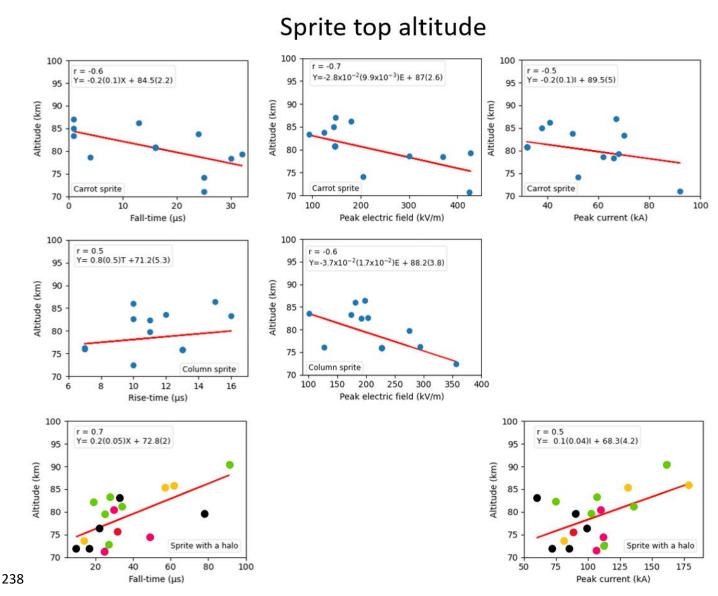
204 The lightning peak electric field, peak current, CMC, rise-time, and fall-time for column 205 sprites ranged from 101 to 355 kV/m, 34 to 87 kA, 880 to 2,410 C-km, 7 to 16 μs, and 1 to 30 206 μs, respectively, with an average of 211 (74) kV/m, 48.5 (15.2) kA, 1,674 (583) C-km, 11.1 207 (2.8) μs, and 15.3 (8.1) μs, where the value in parentheses is the standard deviation. Carrot 208 sprites were induced by lightning flashes with peak electric field, peak current, CMC, rise-209 time, and fall-time varying from 93 to 427 kV/m, 32 to 92 kA, 1,360 to 3,060 C-km, 6 to 19 210 μs, and 1 to 32 μs, respectively, with an average of 233 (125) kV/m, 58 (17.4) kA, 2,187 211 (601) C-km, 11 (5) μs, and 15.6 (12.2) μs. The lightning peak electric field, peak current, 212 CMC, rise-time, and fall-time, which initiated any sprites with halos, had values ranging from 213 180 to 914 kV/m, 60 to 179 kA, 639 to 6,780 C-km, 8 to 25 μs, and from 10 to 91 μs, 214 respectively, with an average of 519 (210) kV/m, 106.2 (30.6) kA, 2,909 (1,983) C-km, 12.8 215 (4.8) μs, and 36.3 (22.4) μs.

216 Clearly, column and carrot sprites require a less lightning CMC and smaller lightning rise217 time and fall-time compared to any sprites with a halo. Sprites with halos require a
218 significantly greater lightning CMC and significantly longer lightning fall-time when
219 compared to carrot and column sprites, as shown in Table 1. Column sprites require a lower
220 lightning electric field and peak current compared to carrot sprites and sprites with a halo.
221 The lightning discharges which initiate carrot sprites have a CMC, peak electric field, and
222 peak current greater and less than that of the column sprites and sprites with halo,
223 respectively.

224 We correlated the various lightning parameters against the brightest region and top altitude of 225 column, carrot, and sprites with halo, and their relationships are presented below. According 226 to Peat et al. (2009), Pearson's linear correlation coefficients spanning from 0.1 to 0.3 are 227 small correlations, 0.3 to 0.5 are moderate correlations, and greater than 0.5 are high 228 correlations.

229 3.1 Sprites top altitude

230 Fig. 2 shows the relationship between lightning fall-time $(X, \mu s)$ (top left row), normalized 231 peak electric field (E, kV/m) (top middle row), and peak current (I, kA) (top right row) versus 232 the top altitude (Y, km) of carrot sprites. Fig. 2 also shows lightning rise-time $(T, \mu s)$ (middle 233 left row) and normalized peak electric field (E, kV/m) (middle center row) versus the top 234 altitude (Y, km) of column sprites, as well as lightning fall-time $(X, \mu s)$ (bottom left row) and 235 peak current (I, kA) (bottom right row) versus top altitude (Y, km) of sprites with a halo. The 236 Pearson correlation coefficient (r) and the linear fit equation (Y, km) are denoted on the top 237 corner of each panel. The weak correlations are insignificant and therefore not presented.



239 Fig. 2. Lightning fall-time $(X, \mu s)$ (top left row), normalized peak electric field (E, kV/m) (top middle row), and 240 peak current (I, kA) (top right row) versus the top altitude (Y, km) of carrot sprites. Lightning rise-time $(T, \mu s)$ 241 (middle left row) and normalized peak electric field (E, kV/m) (middle center row) versus the top altitude (Y, km

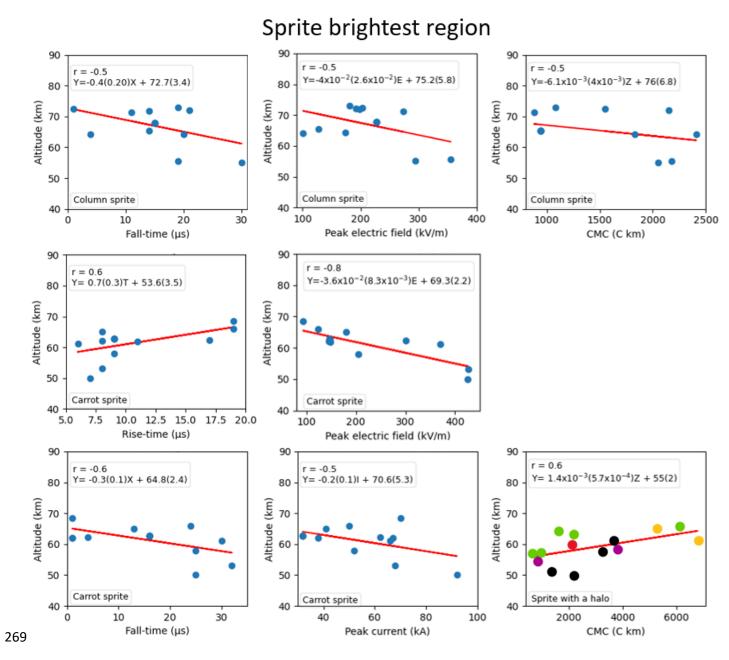
242 km) of column sprites. Lightning fall-time (X, μs) (bottom left row) and peak current (I, kA) (bottom right row) 243 versus top altitude (Y, km) of sprites with a halo. Green, purple, red, yellow, and black dots on the sprite with a 244 halo plot shows column, carrot, wishbone, jellyfish, and "column and carrot" sprites, respectively. The Pearson 245 correlation coefficient (r) and the linear fit equation (Y, km) are denoted on the top corner of each panel. The 246 value in parentheses in the linear fit equation is the uncertainty.

247 The top altitude of column sprites against lightning rise-time and peak electric field showed 248 good positive and negative linear correlations (0.5) and (-0.6), respectively. The good 249 positive (0.5) and weak negative (-0.2) (not shown) correlations found between the lightning 250 rise-time and fall-time against the top altitude of column sprites, respectively, might be 251 associated with the downward propagation of streamers and the lack of upward propagating 252 streamers during column sprites initiation processes (Bór, 2013).

253 The top altitude of carrot sprites against lightning fall-time, peak electric field, and peak 254 current showed good negative linear correlations (-0.6), (-0.7), and (-0.5), respectively. The 255 top altitude of sprites with halos against lightning fall-time and peak current showed good 256 positive linear correlations (0.7) and (0.5), respectively. For carrot sprites, this suggests that 257 the electrical breakdown region decreases in altitude for a longer fall-time, greater peak 258 electric field, and greater peak current.

259 3.2 Sprites brightest region altitude

260 Fig. 3 shows the relationship between lightning fall-time (X, μs) (top left row), normalized 261 peak electric field (E, kV/m) (top middle row), and CMC (Z, C-km) (top right row) versus 262 the altitude (Y, km) of the brightest region for column sprites. Fig. 3 also shows lightning 263 rise-time (Y, μs) (middle left row), normalized peak electric field (Y, Y) (middle center 264 row), fall-time (Y, Y) (bottom left row), and peak current (Y) (bottom center row) versus 265 the altitude (Y, Y) of the brightest region for carrot sprites (middle row), as well as lightning 266 CMC (Y, Y) (bottom right row) versus the altitude (Y, Y) of the brightest region for 267 sprites with a halo (bottom row). The Pearson correlation coefficient (Y) and the linear fit 268 equation (Y, Y) are denoted on the top corner of each panel.



270 Fig. 3. Lightning fall-time $(X, \mu s)$ (top left row), normalized peak electric field (E, kV/m) (top middle row), and 271 CMC (Z, C-km) (top right row) versus the altitude (Y, km) of the brightest region for column sprites. Lightning 272 rise-time $(T, \mu s)$ (middle left row), normalized peak electric field (E, kV/m) (middle center row), fall-time $(X, 273 \mu s)$ (bottom left row), and peak current (I, kA) (bottom center row) versus the altitude (Y, km) of the brightest 274 region for carrot sprites (middle and bottom row). Lightning CMC (Z, C-km) (bottom right row) versus the 275 altitude (Y, km) of the brightest region for sprites with a halo (bottom right row). Green, purple, red, yellow, and 276 black dots on the sprite with a halo plot show column, carrot, wishbone, jellyfish, and "column and carrot" 277 sprites, respectively. The Pearson correlation coefficient (r) and the linear fit equation (Y, km) are denoted on 278 the top corner of each panel. The value in parentheses in the linear fit equation is the uncertainty.

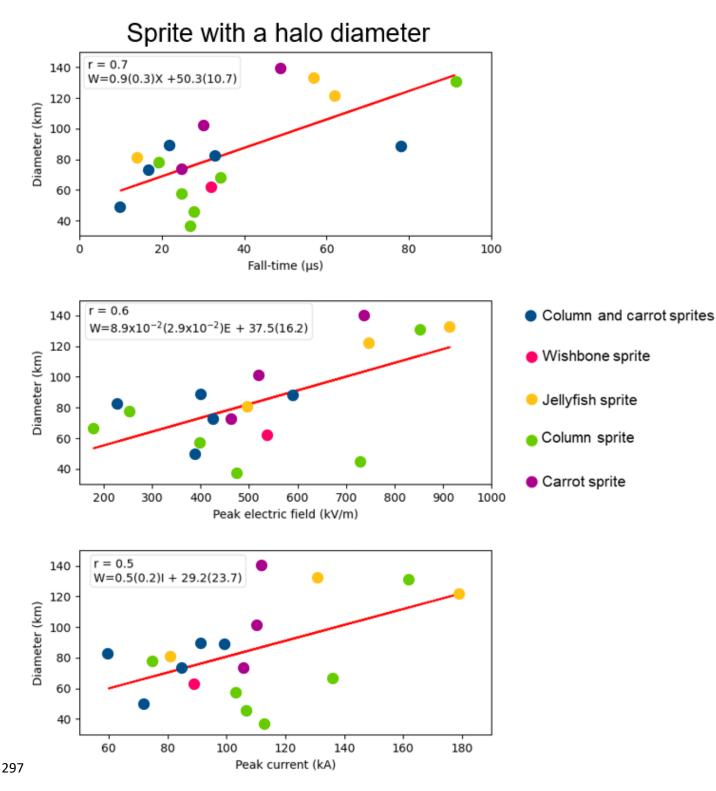
279 For column sprites, there are good negative correlations for the altitude of maximum 280 brightness versus lightning fall-time (-0.5), peak electric field (-0.5), and CMC (-0.5). The

281 altitude of maximum brightness for carrot sprites shows a good positive correlation against 282 lightning rise-time (0.6) and a good negative correlation against lightning peak electric field 283 (-0.8), peak current (-0.5), and fall-time (-0.6). The good positive and negative correlation for 284 carrot sprites against lightning rise-time and fall-time, respectively, might be related to the 285 downward and upward propagation of streamers during carrot sprites initiation (Bór, 2013). 286 On the other hand, for any sprites with halos, the altitude of maximum brightness has a good 287 positive correlation with lightning CMC (0.6).

288 The results indicate that lightning with a longer fall-time, larger electric field, larger peak 289 current, and larger CMC tend to deposit more energy at lower altitudes for column and carrot 290 sprites, as shown in Fig. 3. However, lightning with larger CMC tends to deposit more energy 291 at higher altitudes for sprites with a halo.

292 3.3 Sprites with a halo diameter

293 Fig. 4 shows the relationship between lightning fall-time $(X, \mu s)$ (top panel), normalized peak 294 electric field (E, kV/m) (middle panel), and peak current (I, kA) (bottom panel) versus halo 295 diameters (W, km) for different types of sprites. The Pearson correlation coefficient (r) and 296 the linear fit equation (W, km) are denoted on the top corner of each panel.



298 Fig. 4. Lightning fall-time $(X, \mu s)$ (top panel), normalized peak electric field (E, kV/m) (middle panel), and peak 299 current (I, kA) (bottom panel) versus halo diameters (W, km) for different types of sprites (color coded). Note 300 that the "column and carrot sprites" are where both types occur together. The Pearson correlation coefficient (r) 301 and the linear fit equation (W, km) are denoted on the top corner of each panel. The value in parentheses in the 302 linear fit equation is the uncertainty.

303 We found that halo diameters span between 37 and 140 km with an average of 84 (31) km, 304 where the standard deviation is given in parentheses. A correlation coefficient of 0.7 exists 305 between lightning fall-time and halo diameter, and a correlation coefficient of 0.6 exists 306 between normalized lightning peak electric field and halo diameter. The lightning peak 307 current and halo diameter show a good correlation (0.5), see Fig. 4. In all cases, the larger the 308 lightning peak electric field, peak current, and fall-time, the larger the halo diameters.

309 A decrease in lightning parameter with altitude follows the behaviour of the electric field and 310 Maxwellian relaxation time in the Earth's atmosphere (Liu et al., 2015). It is known that the 311 lightning CMC magnitude also depends on the duration of the continuing current. Thus, a 312 longer continuing current enhances the lightning CMC magnitude estimate. The results 313 suggest that the larger lightning CMC and fall-time are capable of sustaining maximum 314 photon production at a low altitude compared to small lightning CMC and fall-time. The 315 lightning CMC, peak electric field, peak current, rise-time and fall-time are essential in the 316 generation and development of TLEs or sprites morphologies.

317 The results show that the lightning rise-time, fall-time, CMC, peak current, and peak electric 318 field are essential in determining whether the lightning discharge initiated the TLEs or what 319 type of sprites morphologies were initiated. The lightning rise-time, which is not usually 320 reported (Asano et al., 2008; Haspel et al., 2020) and lightning fall-time, which has not been 321 reported in TLEs literature, should be included in the future lightning and TLEs studies.

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328 Data availability

329 On request from the author (s)

330 References

331 Asano, T., Hayakawa, M., Cho, M. and Suzuki, T., 2008. Computer simulations on the 332 initiation and morphological difference of Japan winter and summer sprites. *J. Geophys. Res.* 333 *Space Phys, 113*(A2). https://doi.org/10.1029/2007ja012528

- 334 Bering III, E. A., Benbrook, J. R., Bhusal, L., Garrett, J. A., Paredes, A. M., Wescott, E. M.,
- 335 ... and Lyons, W. A. 2004. Observations of transient luminous events (TLEs) associated with
- 336 negative cloud to ground (- CG) lightning strokes. *Geophys. Res. Lett.* 31(5).
- 337 https://doi.org/10.1029/2003gl018659
- 338 Bór, J. 2013. Optically perceptible characteristics of sprites observed in Central Europe in
- 339 2007–2009. J. Atmos. Sol. Terr. Phys. 92, 151-177.
- 340 https://doi.org/10.1016/j.jastp.2012.10.008
- 341 Chen, A.B.C., Chen, H., Chuang, C.W., Cummer, S.A., Lu, G., Fang, H.K., Su, H.T. and
- 342 Hsu, R.R., 2019. On negative sprites and the polarity paradox. Geophys. Res. Lett. 46(16),
- 343 9370-9378. https://doi.org/10.1029/2019gl083804
- 344 Cooray, V. and Lobato, A., 2020. The Energy, Momentum, and Peak Power Radiated by
- 345 Negative Lightning Return Strokes. Atmos. 11(12), 1288.
- 346 https://doi.org/10.3390/atmos11121288
- 347 Earthnetworks.com. (2019). Sferic Maps [online] Available at:
- 348 https://www.earthnetworks.com/product/decision-support-collaboration-tools/sferic-maps/>
- 349 [Accessed 01 February 2019]
- 350 Frey, H.U., Mende, S.B., Cummer, S.A., Li, J., Adachi, T., Fukunishi, H., Takahashi, Y.,
- 351 Chen, A.B., Hsu, R.R., Su, H.T. and Chang, Y.S., 2007. Halos generated by negative cloud-
- 352 to-ground lightning. Geophys. Res. Lett. 34(18). https://doi.org/10.1029/2007gl030908
- 353 Füllekrug, M., Mareev, E.A. Rycroft, M.J. eds., 2006. Sprites, Elves and intense Lightning
- 354 Discharges (Vol. 225). NATO Science Series II. Mathematics, physics and chemistry,
- 355 Dordrecht: Springer, ISBN 1-4020-4628-630-42, 30-32. https://doi.org/10.1007/1-4020-
- 356 4629-4
- 357 Füllekrug, M., 2010. Wideband digital low-frequency radio receiver. Meas. Sci. Technol.
- 358 21(1), 1-9. https://doi.org/10.1088/0957-0233/21/1/015901
- 359 Füllekrug, M., Nnadih, S., Soula, S et al., 2019. Maximum sprite streamer luminosity near the
- 360 Stratopause. Geophys. Res. Lett. 46(21), 12572-12579.
- 361 https://doi.org/10.1029/2019GL084331
- 362 Gamerota, W.R., Cummer, S.A., Li, J., Stenbaek-Nielsen, H.C., Haaland, R.K. and McHarg,
- 363 M.G., 2011. Comparison of sprite initiation altitudes between observations and models. J.
- 364 Geophys. Res. Space. Phys. 116(A2). https://doi.org/10.1029/2010ja016095

- 365 Gijben, M., 2012. The lightning climatology of South Africa. *S. Afr. J. Sci*, *108*(3), 1-10. 366 https://doi.org/10.4102/sajs.v108i3/4.740
- 367 Haspel, C., Tzabari, M. and Yair, Y., 2020. The influence of symmetric and non-symmetric 368 charge configurations on the possibility of sprite inception: Numerical experiments with a 3D 369 electrostatic model. *J. Atmos. Sol. Terr. Phys.* 202, 105245.
- 370 https://doi.org/10.1016/j.jastp.2020.105245
- 371 Li, J., Cummer, S.A., Lyons, W.A. and Nelson, T.E., 2008. Coordinated analysis of delayed 372 sprites with high-speed images and remote electromagnetic fields. *J. Geophys. Res. Atmos.* 373 *113*(D20). https://doi.org/10.1029/2008JD010008
- 374 Liu, N., McHarg, M.G. and Stenbaek-Nielsen, H.C., 2015. High-altitude electrical discharges 375 associated with thunderstorms and lightning. *J. Atmos. Sol. Terr. Phys.* 136, 98-118. 376 https://doi.org/10.1016/j.jastp.2015.05.013
- 377 Liu, N., Boggs, L.D. and Cummer, S.A., 2016. Observation-constrained modeling of the 378 ionospheric impact of negative sprites. *Geophys. Res. Lett.* 43(6), 2365-379 2373. https://doi.org/10.1002/2016gl068256
- 380 Luque, A. and Ebert, U., 2009. Emergence of sprite streamers from screening-ionization 381 waves in the lower ionosphere. *Nat. Geosci.* 2(11), 757-760. https://doi.org/10.1038/ngeo662
- 382 Luque, A., Stenbaek-Nielsen, H.C., McHarg, M.G. and Haaland, R.K., 2016. Sprite beads 383 and glows arising from the attachment instability in streamer channels. *J. Geophys. Res.*
- 384 Space. Phys. 121(3), 2431-2449. https://doi.org/10.1002/2015ja022234
- 385 Malagón-Romero, A., Teunissen, J., Stenbaek-Nielsen, H.C., McHarg, M.G., Ebert, U. and 386 Luque, A., 2020. On the emergence mechanism of carrot sprites. *Geophys. Res. Lett.* 47(1), 387 e2019GL085776. https://doi.org/10.1029/2019gl085776
- 388 Mashao, D.C., Kosch, M.J., Bór, J et al., 2021. The altitude of sprites observed over South 389 Africa. *S. Afr. J. Sci.* 117(1-2), 1-8. https://doi.org/10.17159/sajs.2021/7941
- 390 McHarg, M.G., Haaland, R.K., Moudry, D. and Stenbaek-Nielsen, H.C., 2002. Altitude-time 391 development of sprites. *J. Geophys. Res. Space Phys.* 107(A11), SIA-9. 392 https://doi.org/10.1029/2001ja000283
- 393 McHarg, M.G., Stenbaek-Nielsen, H.C. and Kammae, T., 2007. Observations of streamer 394 formation in sprites. *Geophys. Res. Lett.* 34(6), L06804.
- 395 https://doi.org/10.1029/2006GL027854

- 396 Miyasato, R., Taylor, M.J., Fukunishi, H. and Stenbaek-Nielsen, H.C., 2002. Statistical
- 397 characteristics of sprite halo events using coincident photometric and imaging data. Geophys.
- 398 Res. Lett. 29(21), 29-1. https://doi.org/10.1029/2001gl014480
- 399 Mlynarczyk, J., Bór, J., Kulak, A., Popek, M. and Kubisz, J., 2015. An unusual sequence of
- 400 sprites followed by a secondary TLE: An analysis of ELF radio measurements and optical
- 401 observations. J. Geophys. Res. Space Phys. 120(3), 2241-2254.
- 402 https://doi.org/10.1002/2014ja020780
- 403 Mlynarczyk, J., Kulak, A., Klucjasz, S., Martynski, K., Kubisz, J. and Popek, M., 2018, May.
- 404 New broadband ELF receiver for studying atmospheric discharges in Central Europe. In 2018
- 405 Baltic URSI Symposium (URSI) (pp. 155-157). IEEE.
- 406 https://doi.org/10.23919/ursi.2018.8406729
- 407 Nnadih, S., Kosch, M., Martinez, P. and Bor, J., 2018. First ground-based observations of
- 408 sprites over southern Africa. S. A. J. Sci. 114(9-10), 1-6.
- 409 https://doi.org/10.17159/sajs.2018/4272
- 410 Pasko, V.P., Inan, U.S., Bell, T.F. and Taranenko, Y.N., 1997. Sprites produced by quasi-
- 411 electrostatic heating and ionization in the lower ionosphere. J. Geophys. Res. Space.
- 412 Phys, 102(A3), 4529-4561. https://doi.org/10.1029/96ja03528
- 413 Pasko, V.P., 2010. Recent advances in theory of transient luminous events. J. Geophys. Res.
- 414 Space Phys. 115(A6). https://doi.org/10.1029/2009ja014860
- 415 Pasko, V.P., Qin, J. and Celestin, S., 2013. Toward better understanding of sprite streamers:
- 416 initiation, morphology, and polarity asymmetry. Surv. Geophys. 34(6), 797-830.
- 417 https://doi.org/10.1007/s10712-013-9246-y
- 418 Peat, J., Barton, B. and Elliott, E., 2009. Statistics workbook for evidence-based health care.
- 419 John Wiley & Sons, 93-101. https://doi.org/10.1002/9781444300499
- 420 Siingh, D., Singh, R.P., Singh, A.K., Kumar, S., Kulkarni, M.N. and Singh, A.K., 2012.
- 421 Discharges in the stratosphere and mesosphere. Space sci. rev. 169(1-4), 73-121.
- 422 https://doi.org/10.1007/s11214-012-9906-0
- 423 Stenbaek-Nielsen, H.C., Haaland, R., McHarg, M.G., Hensley, B.A. and Kanmae, T., 2010.
- 424 Sprite initiation altitude measured by triangulation. J. Geophys. Res. Space Phys. 115(A3).
- 425 https://doi.org/10.1029/2009ja014543

- 426 Soula, S., van der Velde, O., Montanyà, J., Neubert, T., Chanrion, O. and Ganot, M., 2009.
- 427 Analysis of thunderstorm and lightning activity associated with sprites observed during the
- 428 EuroSprite campaigns: Two case studies. Atmos. Res. 91(2-4), 514-528.
- 429 https://doi.org/10.1016/j.atmosres.2008.06.017
- 430 Surkov, V.V. and Hayakawa, M., 2020. Progress in the study of transient luminous and
- 431 atmospheric events: a review. Surv. Geophys. 41, 1101-1142. https://doi.org/10.1007/s10712-
- 432 020-09597-2
- 433 Taylor, W.L. and Jean, A.G., 1959. Very-low-frequency radiation spectra of lightning
- 434 discharges. NBS J. Res. Radio Propagation D, 63(2), 199.
- 435 https://doi.org/10.6028/jres.063d.021
- 436 Taylor, M.J., Bailey, M.A., Pautet, P.D et al., 2008. Rare measurements of a sprite with halo
- 437 event driven by a negative lightning discharge over Argentina. Geophys. Res. Lett. 35(14),
- 438 L14812. https://doi.org/10.1029/2008GL033984
- 439 Wescott, E.M., Sentman, D.D., Heavner, M.J et al., 1998. Observations of
- 440 'Columniform's prites. J. Atmos. Sol. Terr. Phys. 60(7-9), 733-740.
- 441 https://doi.org/10.1016/s1364-6826(98)00029-7
- 442 Wescott, E.M., Stenbaek-Nielsen, H.C., Sentman, D.D et al., 2001. Triangulation of sprites,
- 443 associated halos and their possible relation to causative lightning and micrometeors. J.
- 444 Geophys. Res. Space Phys. 106(A6), 10467-10477. https://doi.org/10.1029/2000ja000182
- 445 Williams, E., Kuo, C.L., Bór, J., Sátori, G., Newsome, R., Adachi, T., Boldi, R., Chen, A.,
- 446 Downes, E., Hsu, R.R. and Lyons, W., 2012. Resolution of the sprite polarity paradox: The
- 447 role of halos. Radio Sci. 47(02), 1-12. https://doi.org/10.1029/2011rs004794
- 448 Yang, J., Lu, G., Liu, N., Sato, M., Feng, G., Wang, Y. and Chou, J.K., 2017. Sprite possibly
- 449 produced by two distinct positive cloud-to-ground lightning flashes. TAO: Terr. Atmos.
- 450 Ocean. Sci. 28(4), 609-624. https://doi.org/10.3319/tao.2016.07.22.01
- 451 Yaniv, R., Yair, Y., Price, C., Sato, M., Hobara, Y., Cummer, S., Li, J. and Devir, A., 2014.
- 452 Ground-based observations of the relations between lightning charge-moment-change and the
- 453 physical and optical properties of column sprites. J. Atmos. Sol. Terr. Phys. 107, 60-67.
- 454 https://doi.org/10.1016/j.jastp.2013.10.018
- 455 Zhu, Y., Rakov, V.A., Tran, M.D et al., 2017. Evaluation of ENTLN performance
- 456 characteristics based on the ground truth natural and rocket-triggered lightning data acquired

457 in Florida. *J. Geophys. Res. Atmos.* 122(18), 9858-9866.458 https://doi.org/10.1002/2017JD027270

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460 Appendix

461 Table 1. Summary of column and carrot sprites and sprites with halos including time, date, 462 CG lightning strokes position and lightning peak current as reported by SAWS and EN; 463 distance from the ELF receiver to the lightning location; lightning electric fields, rise-times, 464 and fall-times computed from the ELF data; lightning CMC enumerated from the broadband 465 magnetic field recording in the Bieszczady Mountains (49.20° N. 22.54° E), Poland; and 466 TLEs estimated top altitude and altitude of the brightest region. Different font color shows 467 information related to sprites with halos (purple), column sprites (blue), and carrot sprites 468 (black).

Time (UTC)	LAT (°)	LON (°)	Peak current (kA)	Distance from ELF receiver to lightning (km)	Electric Field at 1 km from lightning location (kV/m)	Rise-time (μs)	Fall-time (μs)	CMC (C-km)	TLEs top altitude (km)	TLEs altitude of brightest region (km)	Halo diameter (km)
2019-02-01 18:45:10.752	-29.24	25.35	113	376.8	475.0	10	27	6090	72.7	65.5	37
2019-02-01 19:43:09.728	-29.60	25.07	103	333.4	396.6	11	25	2150	79.5	63.0	57
2019-02-01 20:10:11.537	-28.78	25.86	89	445.9	539.6	12	32	2130	75.6	60.2	63
2019-02-01 20:14:00.121	-29.71	25.29	60	347.3	229.3	8	33	3240	83.3	58.0	82
2019-02-01 20:29:36.130	-28.57	25.14	110	404.9	518.9	11	30	3790	80.5	58.5	102
2019-02-01 21:05:14.339	-29.24	24.62	75	319.1	255.8	22	19	689	82.3	56.6	77
2019-02-01 21:05:14.439	-29.05	24.78	72	344.3	388.8	10	10	3683	72.1	60.7	50
2019-02-01 21:18:40.722	-28.55	25.61	179	441.6	748.9	15	62	5270	86.0	65.0	122
2019-02-01 21:54:07.906	-28.90	26.63	131	504.4	914.0	8	57	6780	85.5	61.3	133
2019-02-02 20:54:36.370	-31.04	27.04	91	483.4	401.6	13	78	1340	79.9	51.4	89
2019-02-02 21:11:55.386	-30.25	26.58	99	448.6	592.4	16	22	2170	76.6	50.0	89
2019-02-02 22:44:38.719	-31.77	27.19	162	502.3	853.4	18	91	930	90.5	57.1	131
2019-02-11 19:53:57.116	-28.24	26.41	112	707.5	737.8	10	49	840	74.6	55.0	140
2019-01-30 20:40:17.642	-29.29	23.65	136	241.9	179.5	9	34	1620	81.2	64.0	67
2019-02-11 19:46:46.836	-28.22	25.66	107	656.1	727.2	8	28		83.3	68.0	45
2019-02-01 20:19:35.061	-29.02	25.34	106	389.1	463.5	10	25		71.5	59.0	73
2019-02-02 22:06:00.242	-31.18	26.98	81	476.7	496.6	25	14		73.6	57.0	81
2019-02-02 21:06:16.417	-30.96	27.19	85	496.4	425.8	14	17		72.0	50.0	73
2019-02-01 19:05:21.584	-29.38	25.21	50	357.3	355.4	10	19	2180	72.4	55.6	
2019-02-02 21:53:21.111	-31.15	27.02	50	481.0	293.6	7	30	2050	76.2	55.1	
2019-01-29 19:39:29.981	-29.42	24.39	34	289.1	100.8	12	20	1830	83.5	64.2	
2019-01-29 20:49:49.668	-29.23	24.79	56	332.7	173.7	16	4	2410	83.3	64.3	

2019-01-29 22:48:06.932	-28.18	24.71	44	406.4	203.1	10	1	1550	82.6	72.4
2019-01-29 23:03:02.432	-28.13	24.69	34	410.2	192.0	11	21	2150	82.4	72.0
2019-01-29 23:10:49.261	-27.91	24.32	51	421.3	181.1	10	19	1080	86.0	73.0
2019-01-30 21:19:28.474	-29.34	24.82	87	328.0	274.3	11	11	880	79.8	71.3
2019-01-30 22:05:21.758	-28.97	24.73	37	345.8	126.8	7	14	940	76.0	65.4
2019-01-29 23:00:17.969	-28.20	25.06	36	428.9	197.6	15	14		86.4	71.8
2019-02-01 19:24:25.922	-29.79	25.20	54	336.1	227.1	13	15		75.9	67.8
2019-02-01 19:12:42.451	-29.86	25.41	62	351.5	301.0	17	4	2050	78.6	62.3
2019-02-01 19:26:48.376	-29.56	25.04	41	332.9	179.6	8	13	1930	86.2	65.1
2019-02-01 20:09:16.344	-29.62	25.20	66	344.2	369.6	6	30	3045	78.4	61.2
2019-02-01 20:38:25.718	-28.61	25.53	68	431.1	427.4	8	32	2200	79.3	53.1
2019-01-29 19:33:50.302	-29.40	24.33	50	285.2	124.0	19	24	1360	83.7	66.0
2019-01-29 20:25:41.984	-29.51	25.18	38	347.6	144.7	8	1	3060	85.0	62.0
2019-01-29 20:38:40.528	-29.45	25.18	67	350.6	148.2	11	1	2160	87.0	62.0
2019-01-29 19:17:59.218	-30.13	24.35	70	245.9	93.3	19	1	1680	83.3	68.5
2019-02-01 19:55:34.857	-29.35	25.44	52	378.3	204.7	9	25		74.1	57.9
2019-02-01 20:15:43.526	-29.02	25.32	92	387.6	425.3	7	25		70.7	50.0
2019-02-01 19:24:26.151	-30.05	24.90	32	297.8	146.4	9	16		80.8	62.7