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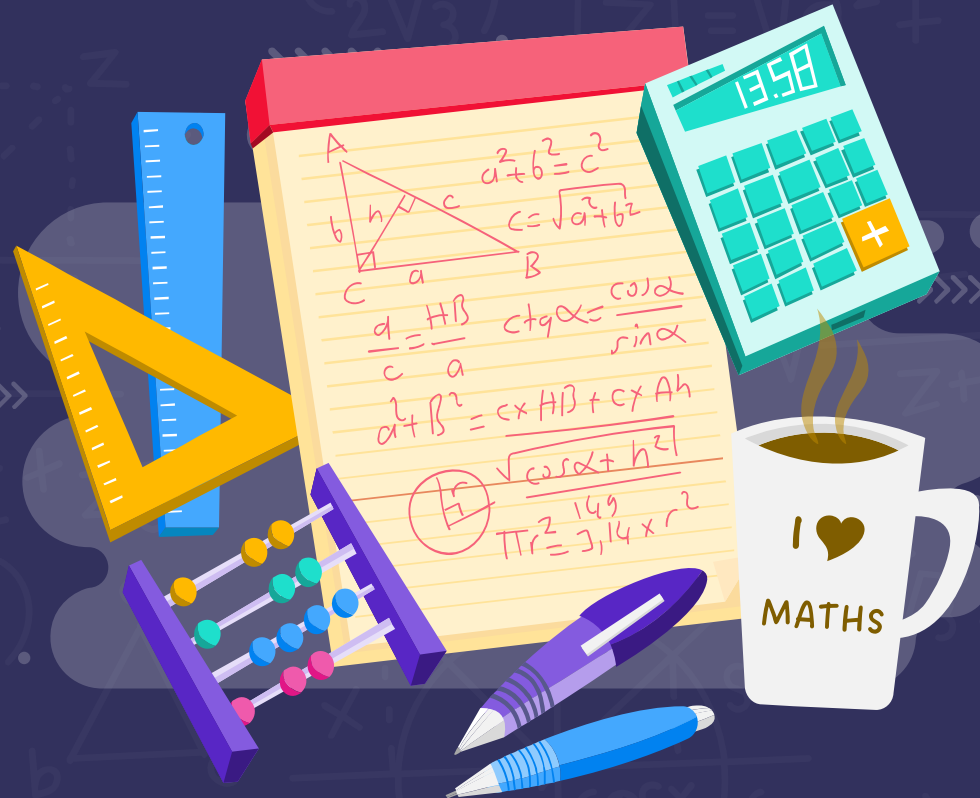
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Practicality or Pedagogy?

Exploring the rationale Primary Mathematics teachers give for using manipulatives in their classrooms



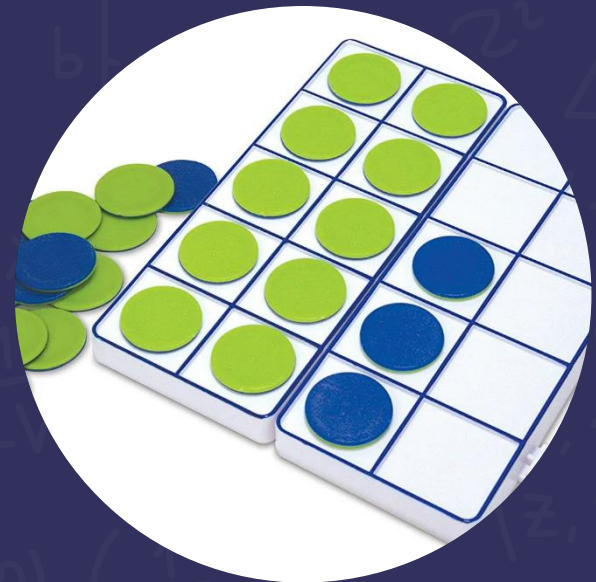
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Programme Leader for Distance Learning (International) PGCE

- Over 60 countries
- Community, State and International Schools
- Placement trainees, non-teaching staff and experienced (unqualified) teachers
- Mirrors most aspects of our on-campus ITT provision

How do primary mathematics teachers' perceptions of Teaching for Mastery (TfM) inform their choices when selecting and using manipulatives (concrete resources) within their lessons?




MANIPULATIVES



Choice overload?

Supporting resources

Work in pairs.

- ① Think of a 2-digit number between 40 and 100.
- ② Use  to show the number in tens and ones.
- ③ Ask your partner to write the number.

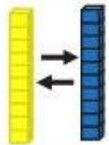
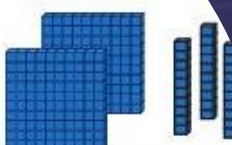
Example

58




Take turns to repeat ①

...demonstrating the relative size of place value columns. Support ...
 ...al to ten tens and so on. Can also be used to represent addition and ...

...ed for ...
 ...s is ...
 ...e ten.

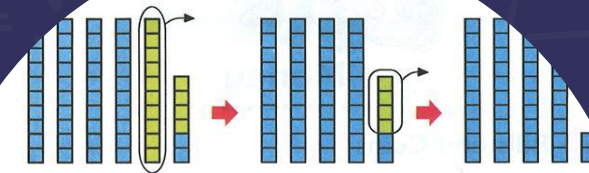
...e used to represent and compare numbers and can be used alongside a bead ...
 ...When calculating, number lines may act as a jotting of the steps of a mental ...
 ...Pupils will have experienced this most through adding tens then ones as sho



Deriving facts


...pils use known f

Subtract 14 from 56.

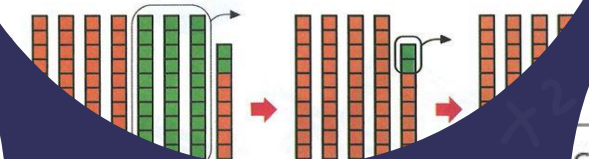


$56 - 14 = \square$

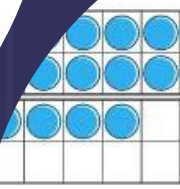
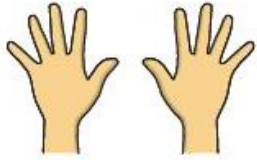
$56 - 10 - 4$



6. Subtract 32 from 78.

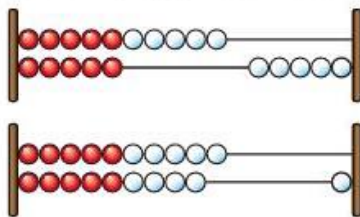


...ers are shown?

Give your answers in numerals and words.

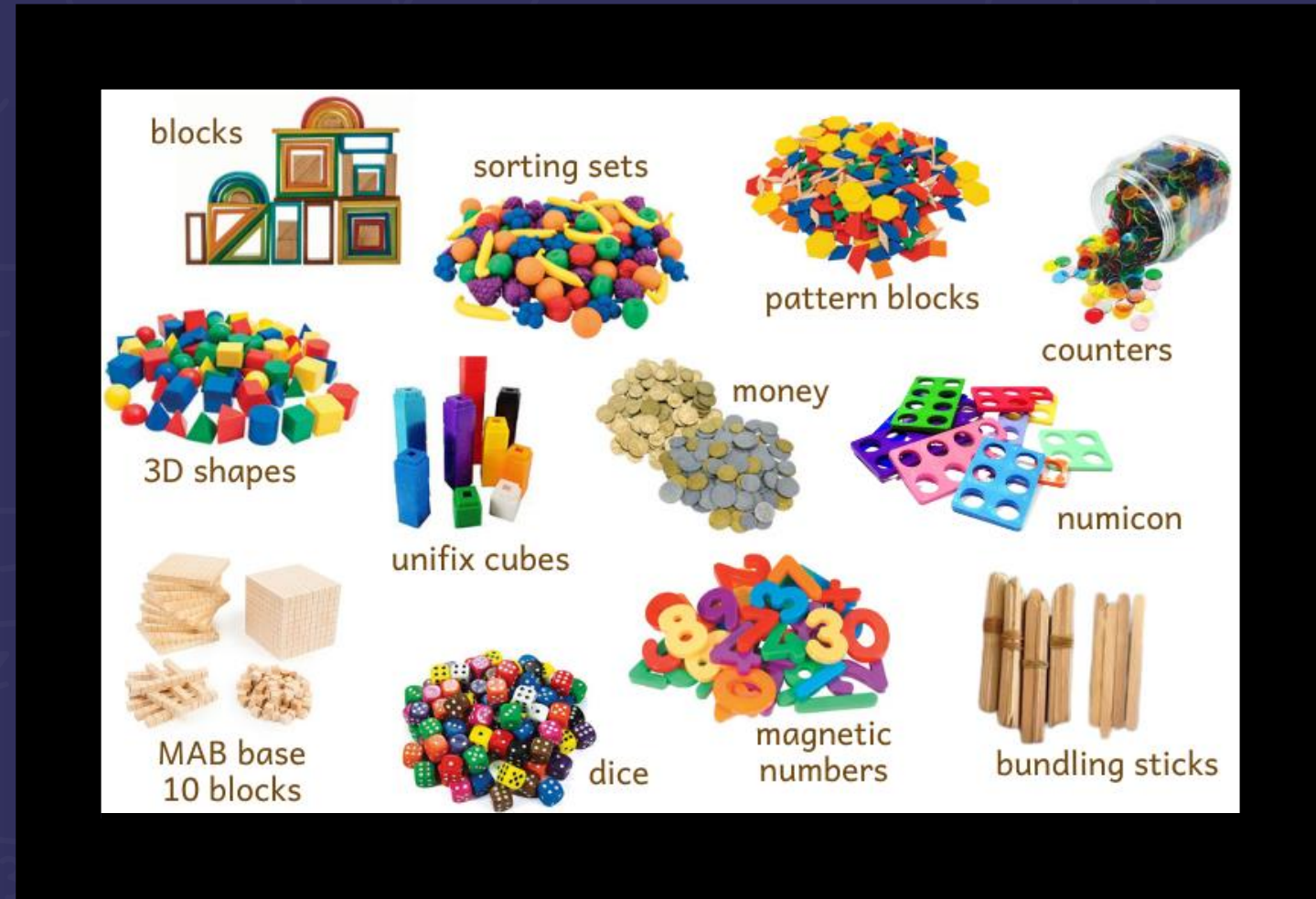
What number is shown on each Rekenrek?



...wers in numerals and words.



- Carbonneau, Marley & Selig (2013) highlight the importance of effective instructional strategy in the use of manipulatives to improve achievement.
- Success is dependent upon:
 - ✓ The level of instructional guidance
 - ✓ The type of manipulative
 - ✓ The age of the learners
 - ✓ The learning environment
- 'Manipulatives are not magic... [they] are not, of themselves, carriers of meaning or insight' (Moyer, 2001, p. 176).



[Maths] Mastery – are we all on the same page?



Duckworth et al. (2015)

Mastery in theory may be easier to
define than in practice



National Association of
Mathematics Advisors (2015)

We suggest that idea of the
existence of a single definition is
a myth.



Garry (2020)

The first thing to bear in mind about mastery
is that it is a contested concept. There are
fierce battles being waged (online and in
person) about what mastery means, and
about what does or does not constitute a
mastery approach.

TENSIONS



DEFINITIONS

See previous slide



KNOWLEDGE

"we have no problem [in the UK] with allowing a great number of teachers with little deep subject knowledge to teach maths to primary-age pupils" (Garry, 2020, p. 17)



EXPORT

"despite difficulties in even defining the concept of an 'East Asian teaching method', policymakers continue to believe this to be a key reason why mathematics achievement is so much greater in the East than the West" (Jerrim & Vignoles, 2015, p.5)



IMPLEMENTATION

the disconnection between educational recommendations and teachers' beliefs (Golafshani, 2013)

Teaching for Mastery (TfM)

- Based on the *Learning for Mastery* ideas of Benjamin Bloom (1968) and 'Mastery' curricula which are popular in South-East Asia
- Questioned by some as policy borrowing, e.g. Clapham & Vickers (2018)
- Mastery has since undergone "numerous remasters, remixes or mash-ups" (Boylan, 2019, p.14)
- Introduced by the National College for Excellence in the Teaching of Mathematics (NCETM) following the introduction of *National Curriculum 2014*

Mastering maths means pupils acquiring a deep, long-term, secure and adaptable understanding of the subject.

ncetm.org.uk





Two years contributing to research and innovation work groups with the local Maths Hub:

- What Manipulative When? (2021-22)
- Which Manipulative Why? (2022-23)



THIS RESEARCH



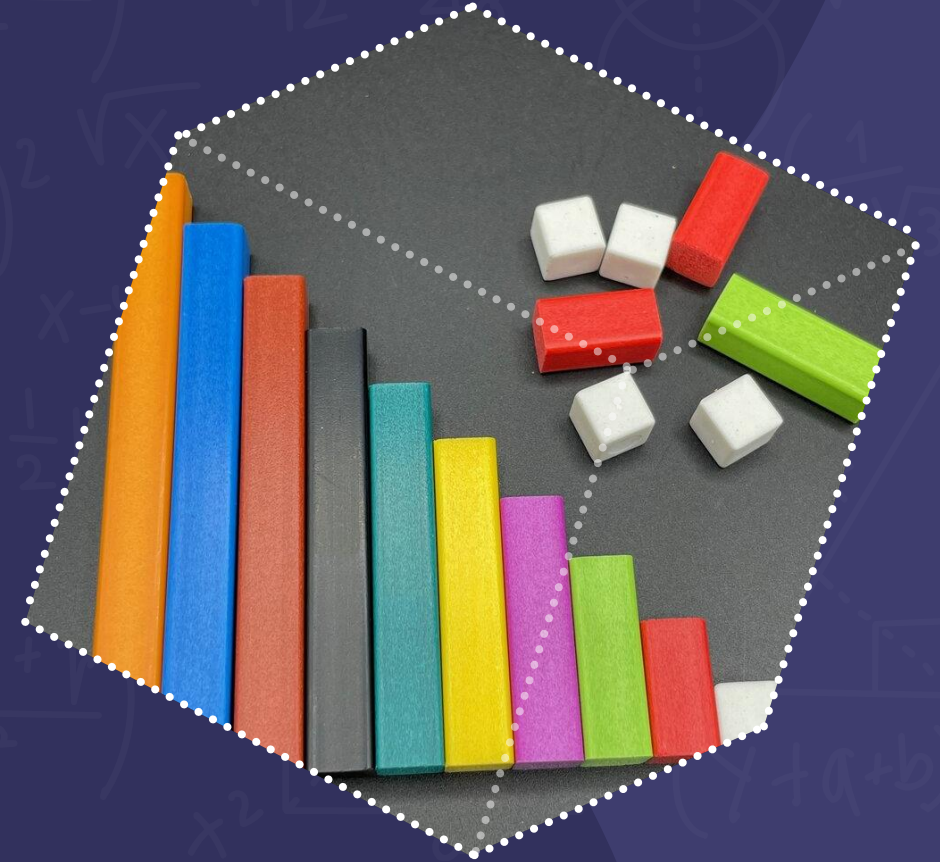
AIMS TO:

- document which manipulatives are used in primary classrooms
- record teachers' rationale for their selection and deployment
- establish the extent to which these decisions are informed by pedagogical content knowledge



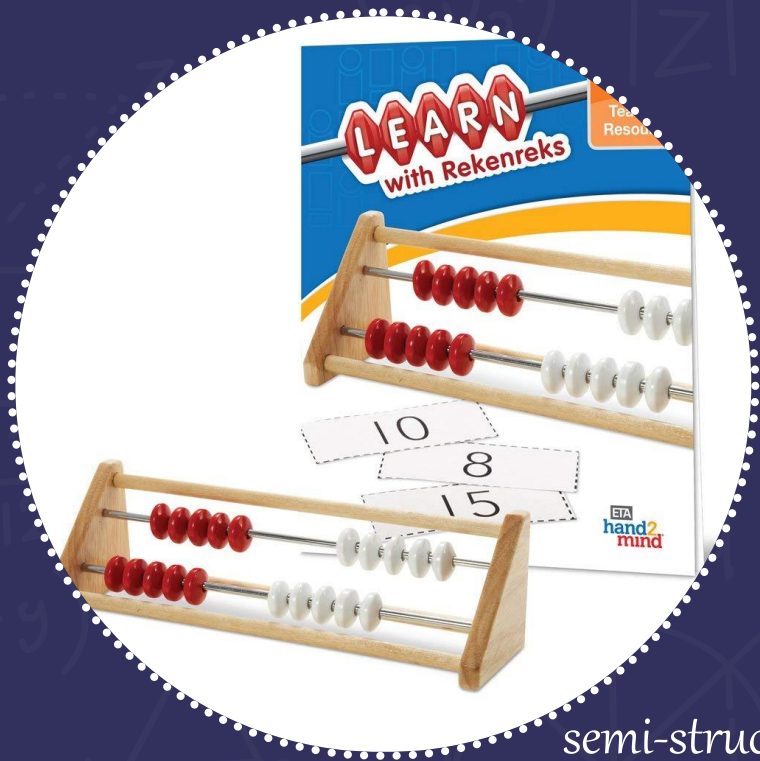
IS IMPORTANT BECAUSE:

- The Education Endowment Foundation states that "practitioners' understanding of mathematical concepts needs to be strong in order to use manipulatives and representations effectively" (EEF, 2020, p.21)
- Whilst the Nuffield Report found that "teachers' choice of manipulatives was subject to disparate factors rather than pedagogical principles" (Griffiths, Back & Gifford, 2017)



METHODOLOGY

wide distribution to Maths Hub membership



semi-structured; explore questionnaire responses in detail

single, critical case study approach

Case study

questionnaire

interviews

observations

document analysis

non-participant; validate that the planned use of manipulatives reflects classroom practice

lesson planning; each use of manipulatives is mapped to the relevant curriculum objective(s)

WHAT AM I FINDING?



POLITICAL LANDSCAPE

The ever-changing government agenda heavily influences the messages and CPD delivered by the Maths Hub and teacher rhetoric



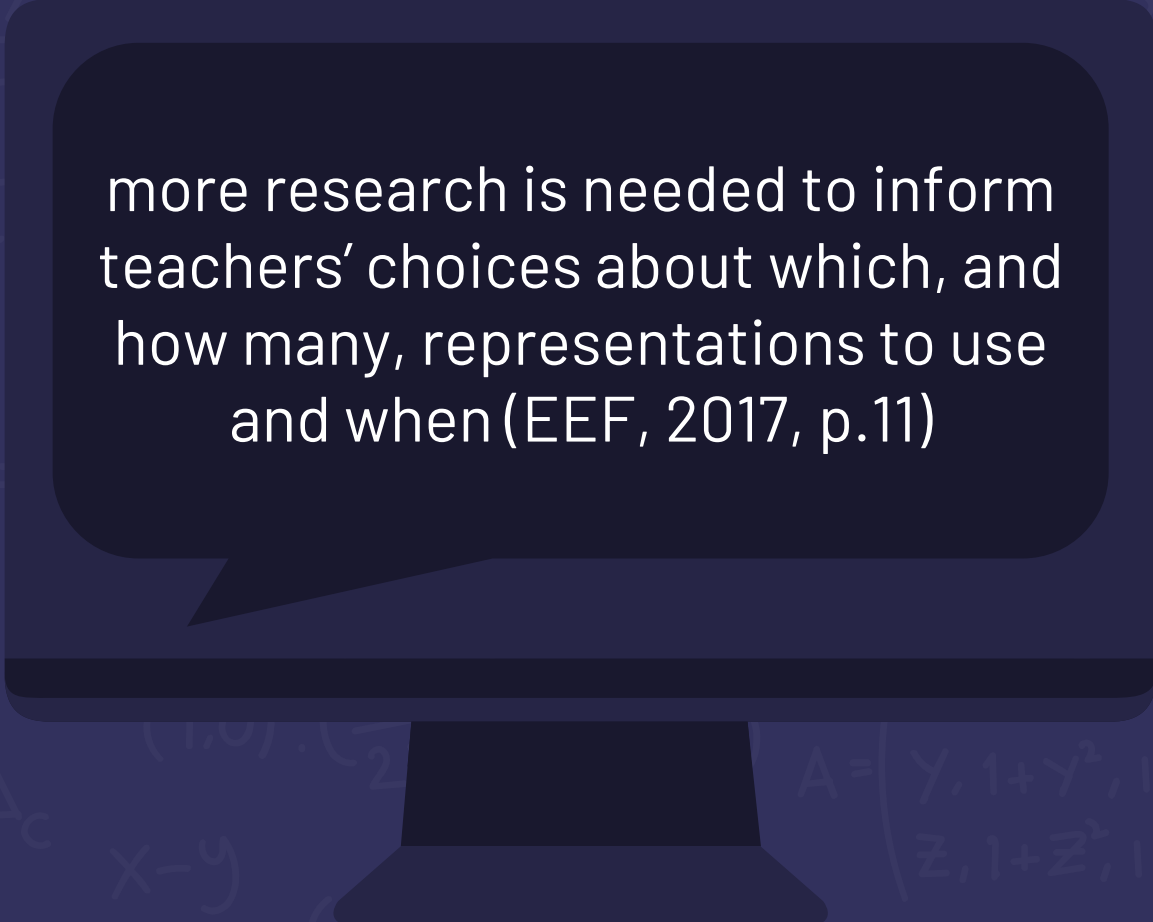
VARIATION

Content Knowledge (CK) and Pedagogical Content Knowledge (PCK) is hugely variable, even within individual schools



PRACTICALITY BEFORE PEDAGOGY?

Manipulatives seem to be valued by their practicality, e.g. versatility, rather than their pedagogical merit for a certain task



more research is needed to inform teachers' choices about which, and how many, representations to use and when (EEF, 2017, p.11)

Practicality

vs.

Pedagogy



AVAILABILITY

What is available in my classroom? Are there sufficient sets for the groups/class? Is it cheap or expensive?



VERSATILITY

Can this manipulative be used for multiple applications? Or is it topic/task specific?



LOGISTICS

Is it 'easy' to administer and oversee?
Is it explained in the scheme of work?



CONTENT KNOWLEDGE

Do I understand how to use this manipulative?



PEDAGOGICAL CONTENT KNOWLEDGE

Am I confident instructing others how to use this manipulative for this task?



KNOWLEDGE CREATION

Is the manipulative driving the task?
Is the task driving the manipulative?

The literature tells us:



PEDAGOGICAL CONSIDERATIONS:

- a clear rationale for manipulative use in the context of the mathematical content being delivered
- the appropriate level of guidance is provided
- allow sufficient time
- the perceptual richness or blandness of the manipulative is considered
- manipulative use is linked to the abstract ideas being represented

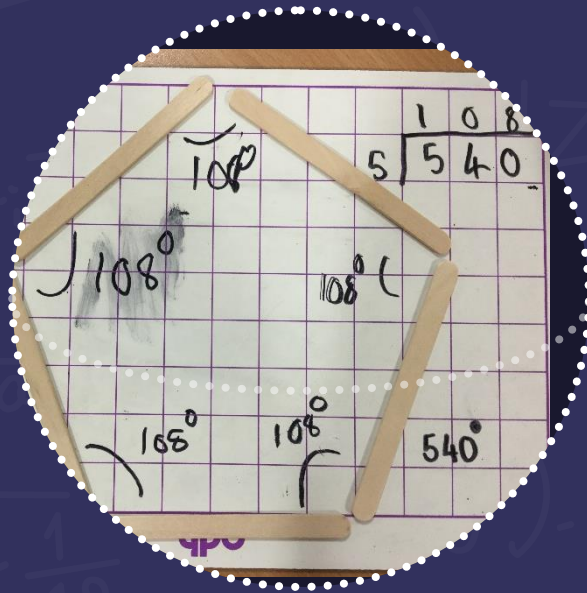


PRACTICAL CONSIDERATIONS:

- practical organisation, including the amount of time given



Why is it important?



COLLABORATION

Sharing best practice with the many, not the few



CREATIVITY

Teaching mathematics in a way that inspires children



CONSISTENCY

Ensuring each child gets the same opportunities to enjoy mathematics

Your thoughts, opinions & questions



What does *maths mastery* look like in UK schools currently?

What are the opportunities and threats?



Do you use manipulatives as part of your practice?

Do you have preferred or more commonly-used manipulatives?



Have you delivered or attended CPD that involved manipulatives?

Was the selection/choice of manipulatives discussed?

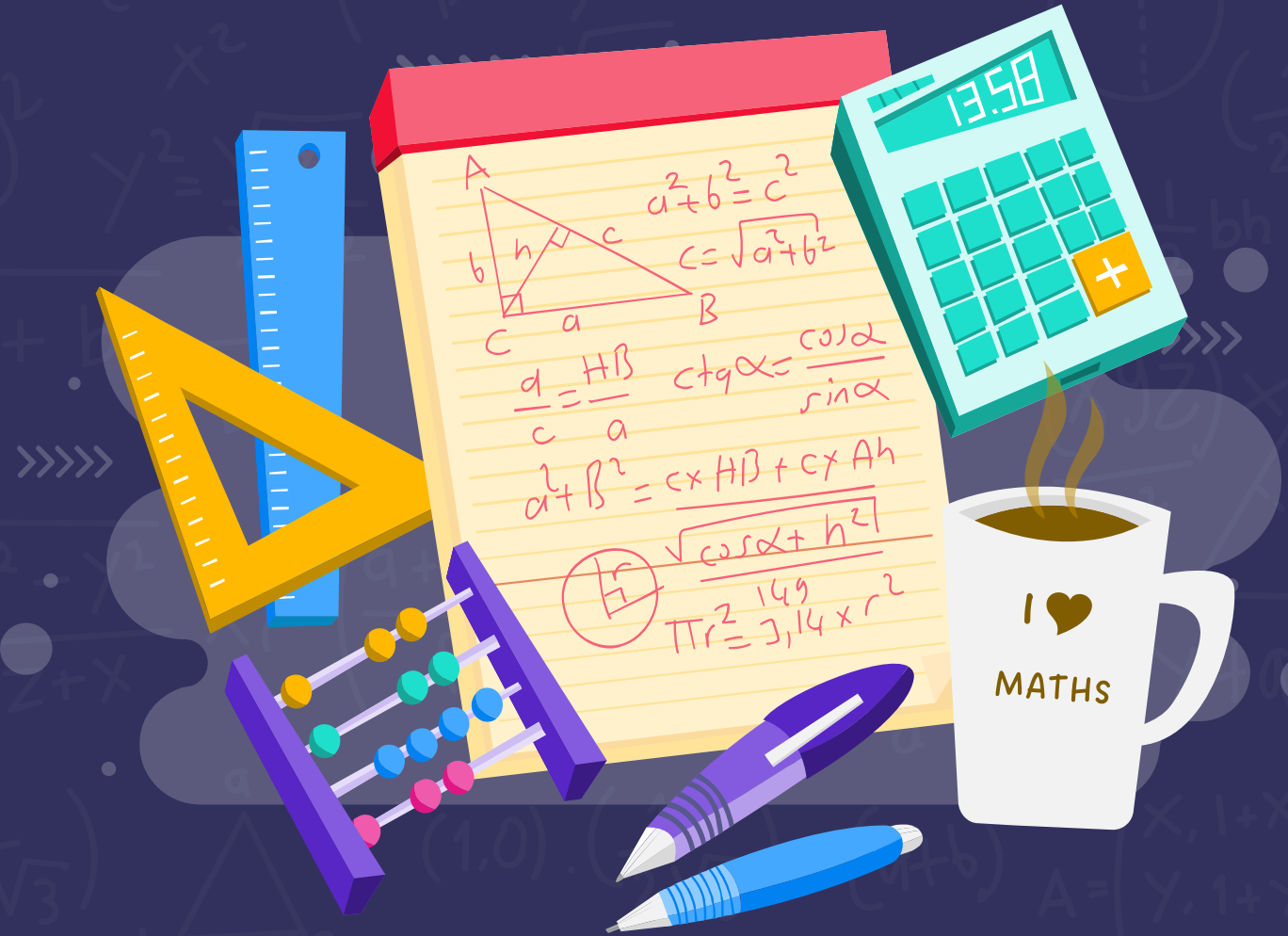


Thank you

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