

Plasmonic response of complex nanoparticle assemblies

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Abstract

²
³ Optical properties of nanoparticle assemblies reflect the distinctive characteristics of
⁴ their building blocks and their spatial organization, giving rise to emergent phenomena.
⁵ Integrated experimental and computational studies have established design principles
⁶ connecting structure to properties for assembled clusters and superlattices. However,
⁷ conventional electromagnetic simulations are too computationally expensive to treat
⁸ more complex assemblies. Here we establish a fast, materials agnostic method to simu-
⁹ late the optical response of large nanoparticle assemblies incorporating both structural

10 and compositional complexity. This many-bodied, mutual polarization method resolves
11 limitations of established approaches, achieving rapid, accurate convergence for con-
12 figurations including thousands of nanoparticles, some overlapping. We demonstrate
13 these capabilities by reproducing experimental trends and uncovering far- and near-field
14 mechanisms governing the optical response of plasmonic semiconductor nanocrystal
15 assemblies, including structurally complex gel networks and compositionally complex
16 mixed binary superlattices. This broadly applicable framework will facilitate design of
17 complex, hierarchically structured, and dynamic assemblies for desired optical charac-
18 teristics.

19 The tunable optical response of plasmonic nanoparticle assemblies makes them at-
20 tractive for applications including sensing,^{1,2} energy conversion,³⁻⁵ and theranostics.^{6,7}
21 Developing and employing methods for electrodynamics simulation of metallic nanopar-
22 ticle assemblies are essential for advancing conceptual understanding and design. The
23 resonant interaction of free charge carriers in nanoparticles with light (localized surface
24 plasmon resonance, LSPR) results in strong electromagnetic near-fields and enhanced
25 absorption and scattering.^{8,9} Due to LSPR coupling, the spectral response of plas-
26 monic assemblies is sensitive to the nanoparticle spatial arrangement, i.e., structure,
27 with amplified electromagnetic fields or hot spots emerging in the gaps between closely
28 spaced nanoparticles.¹⁰⁻¹³ Analytical approaches such as Mie theories¹⁴ or plasmon
29 hybridization theory^{11,15} and numerical solution of the classical electromagnetic scat-
30 tering equations^{10-12,16-21} have clarified the influence of nanoparticle morphology and
31 coupling in small plasmonic clusters, oligomers, and periodic arrays. However, an open
32 question is how to compute the optical response of significantly more complex assem-
33 blies with characteristic structural features involving large numbers of nanoparticles,
34 such as compositionally disordered superlattices²²⁻²⁴ or gel networks.^{13,25-29}

35 Structural complexity of extended, disordered nanoparticle assemblies poses chal-
36 lenges for conventional electromagnetic simulation techniques. Discretization require-
37 ments for the most flexible approaches—discrete dipole approximation, finite difference
38 time domain, finite element, and boundary element methods^{19,20}—render them too

39 computationally demanding to simulate configurations with a large number N ($> 10^3$)
40 of nanoparticles. This shortcoming can be avoided for assemblies of spherical nanopar-
41 ticles using strategies like the multisphere T-matrix method,^{30–34} which is based on
42 generalized Mie theory¹⁴ and does not require spatio-temporal discretization. However,
43 even these approaches become slow to converge or fail altogether when nanoparticle
44 pairs touch or overlap, which inevitably occurs in large configurations generated from
45 simulations of assembly using coarse-grained models. The ability to predict the optical
46 response of complex assemblies, including those from simulated nanoparticle configu-
47 rations, is needed to match the complexity of emerging experimental systems^{22–24,26,27}
48 and accelerate their development.

49 Building on a framework from electrostatics, here we establish a mutual polariza-
50 tion method (MPM) capable of rapidly simulating the frequency-dependent optical
51 response of large, complex assemblies of spherical nanoparticles with arbitrary di-
52 electric functions (Fig. 1), accommodating configurations with particle overlaps and
53 triply periodic boundary conditions. We use this approach to predict and interpret
54 experimental spectra for disordered systems with characteristic features that comprise
55 more nanoparticles than would be practical to analyze by conventional electromag-
56 netic simulations: 1) two-dimensional randomly mixed binary superlattices and 2)
57 three-dimensional nanoparticle gel networks. Our analysis shows how far-field spec-
58 tral features emerge from heterogeneous, structure-dependent near-field coupling and
59 illustrates how MPM helps integrate data from structural and optical measurements
60 to provide insights about ordering across length scales in complex assemblies.

61 Mutual Polarization Method

62 MPM computes the optical response based on the polarization of each particle by
63 the applied field \mathbf{E}_0 and by the electric dipoles of the other $N - 1$ particles in the
64 system. The polarization depends on the particle’s composition as reflected by its
65 dielectric function $\varepsilon_i(\omega)$, where ω is the frequency of light. Spherical particles of any

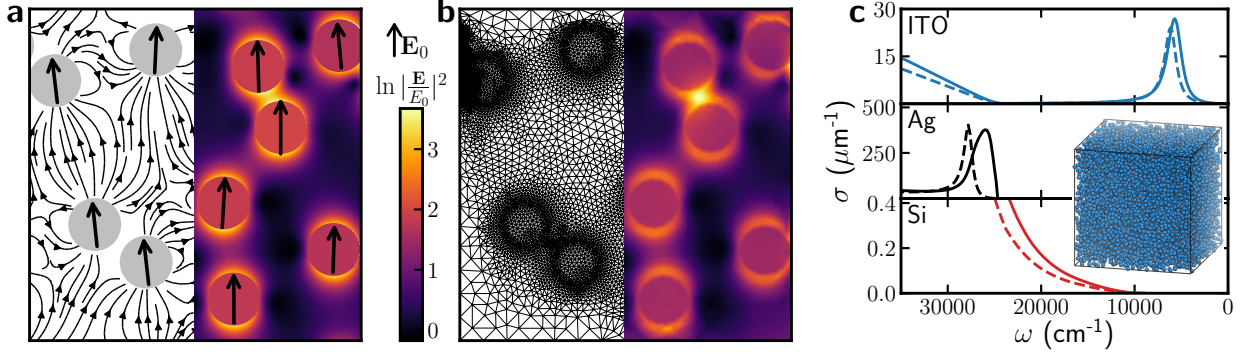


Figure 1: **Broad applicability of MPM.** Schematic illustrations and resultant electric field maps generated using (a) MPM and (b) finite element methods for ITO nanocrystals at area fraction of 0.20. (c) Calculated extinction coefficients for dilute (dashed lines) and concentrated (volume fraction 0.20, solid) dispersions of ITO, silver, and silicon nanoparticles using MPM with the dielectric functions shown in Table S3. Coupling redshifts and broadens the LSPR peaks for silver and ITO at high concentration (configuration shown in inset).

66 dielectric function can be treated (Fig. 1c), however here we only consider particles in
 67 the quasistatic limit, where their radius a is small compared to the wavelength of light.
 68 This simplification is broadly applicable for LSPR coupling in nanoparticle assemblies,
 69 and it allows the $3N$ particle dipole moment components $\mathbf{p}_1, \dots, \mathbf{p}_N$ to be determined
 70 by solving the electrostatics limit of Maxwell’s equations, i.e., the Poisson and Laplace
 71 equations.

72 Like other approaches based on generalized Mie theory,¹⁴ MPM does not require
 73 fine spatial discretization to solve the electromagnetic scattering problem, though its
 74 predictions compare favorably with those from finite element solutions (Fig. 1b and S1-
 75 S3). MPM neglects multipole moments induced by local field gradients, yet it captures
 76 all significant structure-dependent trends in the far- and near-field optical response.
 77 As a result, MPM can compute the optical response of assemblies with more complex
 78 structures involving large particle numbers.

79 Once the electric dipole for each particle i is determined from MPM, the local
 80 electric field $\mathbf{E}(\mathbf{x})$ can be computed at any position \mathbf{x} . A sum of the incident field
 81 and the fields of the scattered waves, it can be expressed (to lowest order in ω) as
 82 $\mathbf{E}(\mathbf{x}) = \mathbf{E}_0 + \sum_i^N (4\pi\epsilon_m r^3)^{-1} (3\hat{\mathbf{r}}\hat{\mathbf{r}} - \mathbf{I}) \cdot \mathbf{p}_i$, where $\mathbf{r} = \mathbf{x} - \mathbf{x}_i$, \mathbf{x}_i is particle i ’s position,

83 $r = |\mathbf{r}|$, $\hat{\mathbf{r}} = \mathbf{r}/r$, \mathbf{I} is the identity tensor, and ε_m is the (real and frequency-independent)
 84 permittivity of the medium. Particle i 's dipole can be further expressed in terms of
 85 the local field, $\mathbf{p}_i = \varepsilon_m \alpha_i(\omega) \mathbf{E}(\mathbf{x}_i)$, where $\alpha_i(\omega) = 4\pi a^3 [\varepsilon_i(\omega) - \varepsilon_m] / [\varepsilon_i(\omega) + 2\varepsilon_m]$ is
 86 the dipolar polarizability. Other observables related to the optical response—such as
 87 frequency-dependent extinction coefficient σ or transmittance through a nanoparticle
 88 film—can be readily computed from these quantities using Maxwell's equations (Sup-
 89 porting Information Sec. 1.2 and 4.2).

90 The heart of the many-body MPM computation is efficient solution of the linear
 91 system of equations for the N particle dipoles,

$$\mathbf{E}_0 = \sum_j^N \mathbf{M}_{ij} \cdot \mathbf{p}_j \quad (1)$$

92 Here, we have introduced a scattering matrix with elements \mathbf{M}_{ij} ,

$$\mathbf{M}_{ij} = \begin{cases} \frac{1}{\varepsilon_m \alpha_i} \mathbf{I} & i = j \\ \frac{1}{4\pi \varepsilon_m r_{ij}^3} (\mathbf{I} - 3\hat{\mathbf{r}}_{ij} \hat{\mathbf{r}}_{ij}) & i \neq j, r_{ij} \geq 2a, \\ \frac{1}{4\pi a^3 \varepsilon_m} \left[\left(1 - \frac{9r_{ij}}{16a} + \frac{r_{ij}^3}{32a^3} \right) \mathbf{I} + \left(\frac{3r_{ij}^3}{32a^3} - \frac{9r_{ij}}{16a} \right) \hat{\mathbf{r}}_{ij} \hat{\mathbf{r}}_{ij} \right] & i \neq j, r_{ij} < 2a \end{cases}, \quad (2)$$

93 constructed to avoid singularities, unphysical property predictions, and convergence
 94 problems when solving for the dipoles (Fig. S4 and S5) due to particles with overlap-
 95 ping optical cores ($r_{ij} < 2a$). Overlaps can naturally occur in large configurations of
 96 simulated assemblies due to coarse-grained model nanoparticle interactions, but this
 97 scattering matrix is readily inverted to obtain well-behaved solutions of eq 1 for any
 98 spatial arrangement of the particles. Similar regularization strategies have been ap-
 99 plied to treat overlaps while simulating other physical phenomena, e.g., many-bodied
 100 hydrodynamic^{35,36} and magnetic^{37,38} interparticle forces in colloidal suspensions, which
 101 require assigning sharp particle interfaces (for continuum property modeling) together
 102 with soft-particle interactions (for dynamics). For triply-periodic geometries, \mathbf{M}_{ij} can
 103 be expressed in a compact form (eq S3) amenable to a highly efficient, spectrally accu-

104 rate Ewald summation method³⁹ that allows the linear system for dipoles to be solved
 105 efficiently using the generalized minimal residual method (GMRES).⁴⁰ Our implemen-
 106 tation of MPM is publicly available (see Methods).

107 Mixed Nanocrystal Superlattices

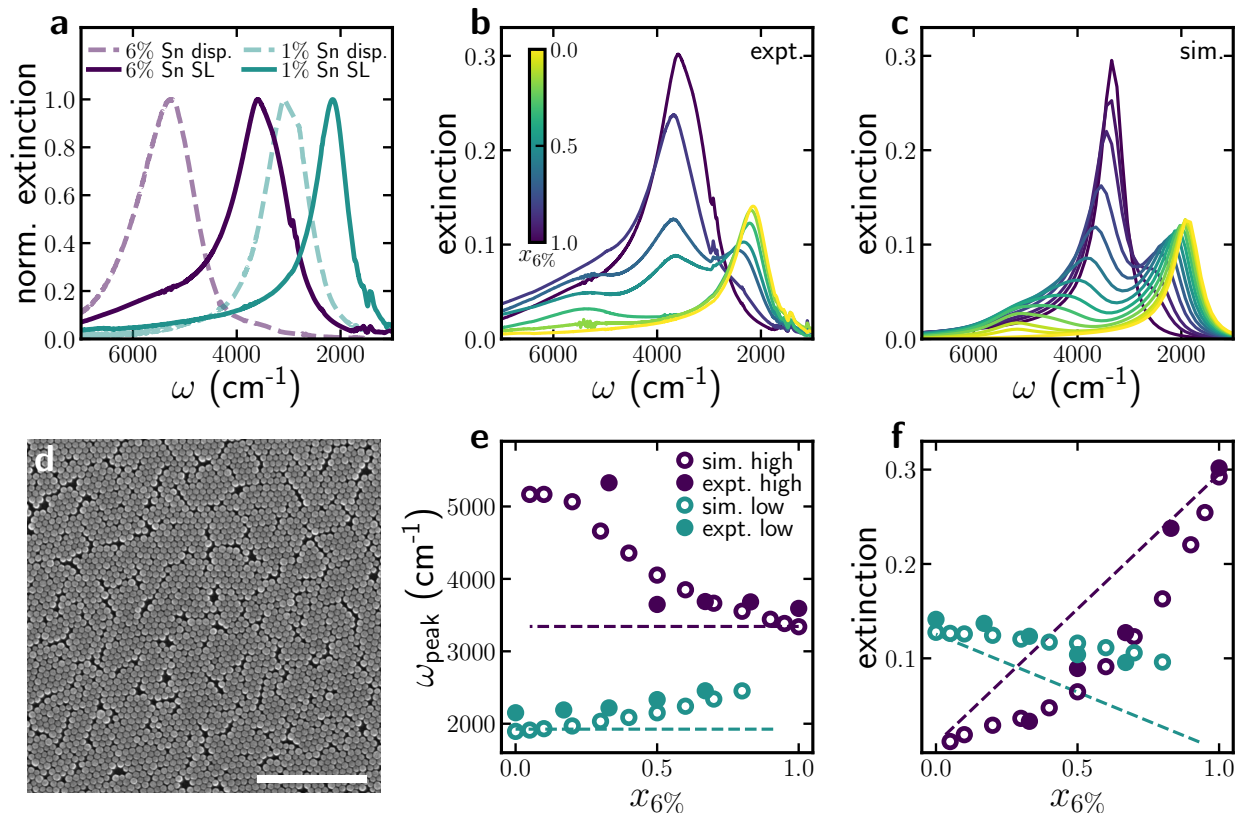


Figure 2: **Spectral response of mixed ITO nanocrystal superlattices.** (a) Experimental extinction spectra for nanocrystal dispersions (dashed) and single-component superlattices (solid). (b) Experimental and (c) simulated extinction spectra for various compositions $x_{6\%}$ of mixed superlattices. (d) Scanning electron micrograph of a mixed superlattice comprising 1% Sn and 6% Sn ITO nanocrystals (scale bar 500 nm). (e) Extinction peak locations ω_{peak} and (f) heights from b and c as a function of $x_{6\%}$. The dashed lines indicate the values that would result from simple linear mixing of the pure 6% and pure 1% superlattice spectra.

108 To demonstrate the utility of MPM for design of compositionally complex nanopar-
 109 ticle assemblies we analyze the collective optical response of mixed nanocrystal super-
 110 lattices, where the mixing ratio allows continuous tuning of effective properties. Tin-

111 doped indium oxide (ITO) nanocrystals have a near-ideal metallic dielectric function
 112 with a tunable LSPR depending on the chosen dopant concentration (% Sn). Consis-
 113 tent with previous reports of other nanocrystal compositions,²²⁻²⁴ we found that ITO
 114 nanocrystals with different % Sn readily form intermixed two-dimensional hexagonal
 115 superlattices, as long as their sizes are closely matched (here, $a \approx 15$ nm, Fig. 2d, S6,
 116 and S7).

117 At infrared wavelengths, the ITO permittivity is well-described by a simple Drude
 118 dielectric function:

$$\varepsilon_p(\omega) = \varepsilon_\infty - \frac{\varepsilon_0 \omega_p^2}{\omega^2 + i\gamma\omega} \quad (3)$$

119 where ε_∞ is the high-frequency permittivity, set equal to $4\varepsilon_0$, while doping changes both
 120 ω_p , that primarily controls the LSPR peak position, and γ that determines peak width.
 121 Plasmonic coupling causes a large redshift of the extinction spectrum upon assembly
 122 into a superlattice (Fig. 2a). However, when scaled by ω_p , the magnitude of this shift is
 123 independent of % Sn (Table S1). In this sense, the range of attainable optical responses
 124 is limited for single-component superlattices, even when the nanocrystal building blocks
 125 themselves have continuously tunable properties.

126 Although binary superlattices with ordered arrangements of two components^{41,42}
 127 are difficult to assemble experimentally, they are simple to study computationally be-
 128 cause they can be modeled using a small periodic unit cell. Conversely, randomly
 129 mixed superlattices are computationally challenging; a large number of particles must
 130 be used to prevent periodic boundary conditions imposing artificial sublattice ordering
 131 and to adequately sample the possible nanocrystal arrangements.

132 We vary the mixing ratio of 1% Sn and 6% Sn ITO nanocrystals in superlattices
 133 continuously, changing the fraction of 6% Sn nanocrystals, $x_{6\%}$, from 0 to 1. Qual-
 134 itatively, the normal incidence extinction spectra of the mixed superlattices evolve
 135 systematically between the spectra of the two single-component assemblies, but nei-
 136 ther the peak positions nor the heights reflect simple linear mixing (Fig. 2b). Electron
 137 transfer is not expected to occur between nanocrystals,⁴³ but LSPR coupling between

138 neighboring nanocrystals should depend on their % Sn.

139 These spectral trends are accurately reproduced in simulations of superlattice ex-
140 tinction using MPM (Fig. 2c). We model the superlattices by constructing 2D hexag-
141 onal lattices containing 11600 nanocrystals, each having one of two Drude dielectric
142 functions using parameters (ω_p and γ) determined by fitting the extinction spectra of
143 dilute solvent dispersions of the corresponding nanocrystals (Fig. S8 and Table S2).⁴⁴
144 Using MPM, we simulate the normal incidence extinction spectra, averaged over 2
145 polarizations and 20 superlattices independently prepared by randomly arranging the
146 nanocrystals. The correspondence with the experimental spectra supports our suppo-
147 sition that the lattices are well-mixed, with little to no phase segregation between the
148 two types of ITO nanocrystals, an outcome that would be difficult to directly verify
149 by electron microscopy owing to their very similar electron densities.

150 As such, we interpret the shifting peak positions with composition ($x_{6\%}$) as aris-
151 ing from a changing average number of spectrally resonant neighboring nanocrystals
152 (Fig. 2e). For instance, compared to a pure 1% Sn superlattice ($x_{6\%} = 0$), the lower
153 frequency extinction peak blueshifts with increasing $x_{6\%}$ as each 1% Sn nanocrystal has
154 fewer 1% Sn neighbors with which to couple. The same is true of the higher frequency
155 peak moving away from $x_{6\%} = 1$. A third peak, around 5100 cm^{-1} , arises only for
156 intermediate compositions, ascribed to “isolated” 6% Sn nanocrystals with relatively
157 few 6% Sn neighbors.

158 To understand the trends in peak heights (Fig. 2f) requires microscopic insight made
159 possible by visualizing the spatial variation of the dipolar polarizations and the result-
160 ing local electric fields (Fig. 3) and quantifying their probability distributions (Fig. S9).
161 For instance, starting from $x_{6\%} = 1$, the intensity of the high frequency peak drops
162 much more quickly with changing $x_{6\%}$ than would be expected from linear mixing.
163 For a superlattice containing a fraction $x_{6\%} = 0.80$ of 6% Sn nanocrystals, examining
164 the dipoles induced by excitation at the peak, we find that the 1% Sn nanocrystals
165 are effectively acting as dielectric spacers that have minimal polarization, so 6% Sn
166 nanocrystals near 1% Sn nanocrystals have significantly reduced dipoles because they

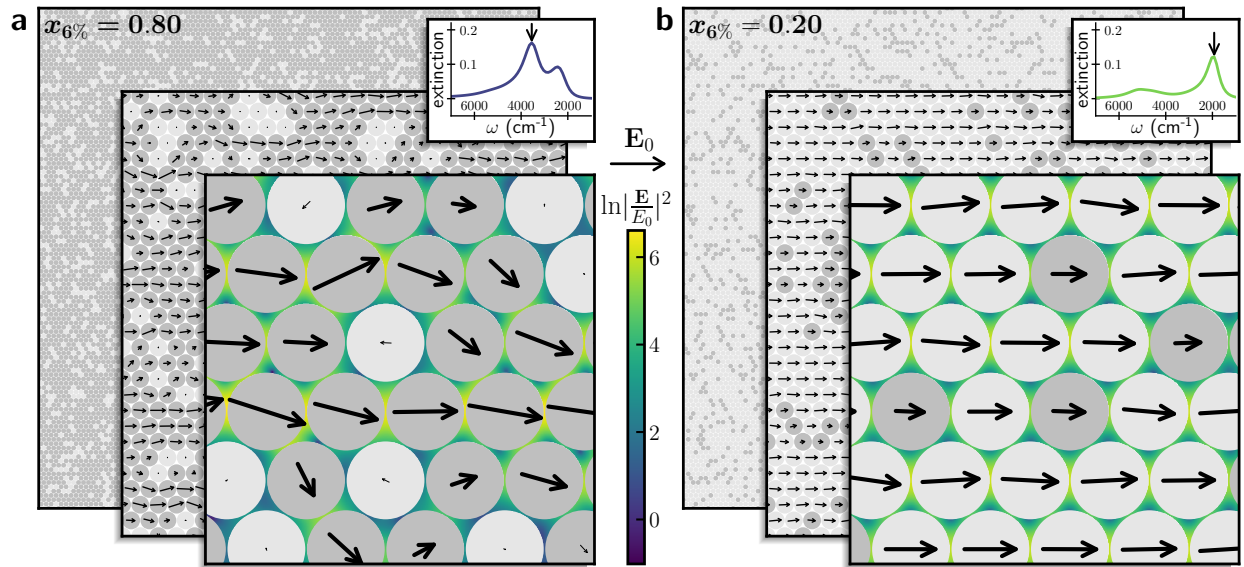


Figure 3: **Electric near-field maps for mixed nanocrystal superlattices.** Spatial maps of the local field intensity at (a) the high-frequency LSPR for $x_{6\%} = 0.80$ and (b) the low-frequency LSPR for $x_{6\%} = 0.20$. Foreground panels magnify small areas within the entire simulated configuration shown in the backmost panel. Dark (6% Sn) and light (1% Sn) gray indicate the nanocrystal type, arrow lengths indicate the magnitude and direction of the imaginary part of each particle's dipole moment. Corresponding extinction spectra are inset with the excitation frequency indicated.

167 do not get a mutual polarization boost (Fig. 3a). These effects weaken the overall
168 response, reducing the extinction intensity. The field is also highly concentrated along
169 the paths formed by 6% Sn nanocrystals, resulting in a heterogeneous distribution of
170 field strengths and dipole orientations (Fig. S9). In a superlattice with only a fraction
171 $x_{6\%} = 0.20$ of 6% Sn nanocrystals, conversely, the 1% Sn nanocrystals' polarization is
172 enhanced by coupling to neighboring 1% Sn and 6% Sn nanocrystals alike, strengthen-
173 ing and better aligning their dipoles with the applied field (Fig. 3b). As a result, the
174 low frequency extinction peak intensity falls off more gradually than expected from lin-
175 ear mixing as $x_{6\%}$ increases, and the local field enhancement is more evenly distributed
176 (Fig. S9). The spectral redistribution of extinction and spatial redistribution of electric
177 field intensity hint at a rich variety of effective metamaterial properties and near-field
178 phenomena that could be realized in mixed nanocrystal superlattices. MPM's abil-
179 ity to rapidly screen a large compositional parameter space will be enabling in the
180 exploration of these possibilities.

181 Nanocrystal Gels

182 Nanocrystal gels have structural complexity that spans length scales, which has so far
183 hampered the use of simulations to predict or rationalize their structure-dependent
184 optical properties. Although plasmonic nanoparticle gels have been reported to ex-
185 hibit spectrally shifted and broadened extinction spectra compared to their constituent
186 nanoparticles, these effects vary widely and unpredictably for different nanoparticle
187 compositions and gel preparation strategies.^{13,25-27} We demonstrate the value of MPM
188 for understanding gel structure and optical properties by considering networks of ITO
189 nanocrystals ($a \approx 6$ nm, 6.0% Sn) linked by dynamic covalent bonding²⁶ (Fig. 4, S10,
190 and S11).

191 Gel structure commonly depends on sample history and preparation protocol, and
192 we find that the structure factor S acquired by small-angle X-ray scattering (SAXS) of
193 ITO nanocrystal gels evolves systematically with the amount of the non-coordinating

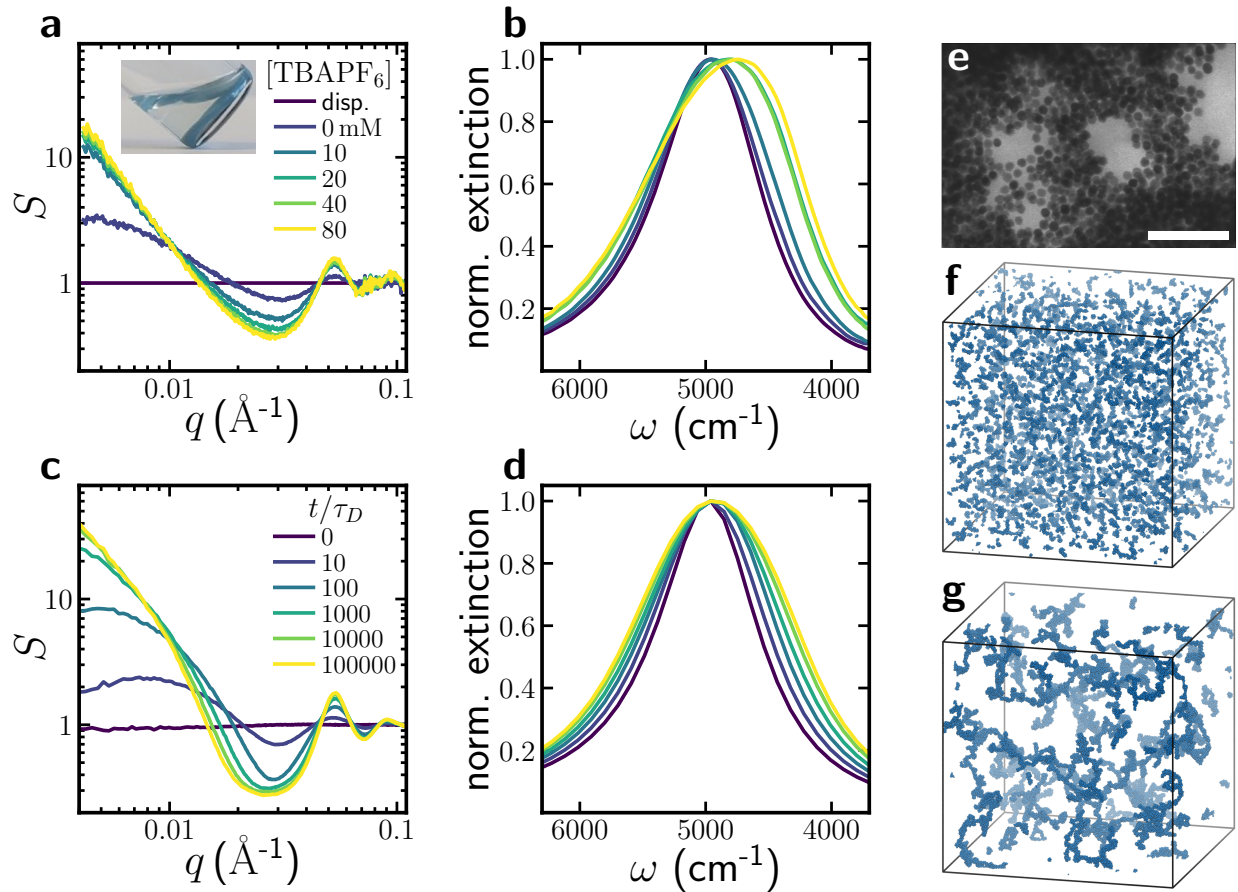


Figure 4: **Structural and optical evolution of ITO nanocrystal gels.** (a) Experimental SAXS structure factors S (gel seen in blue, photo inset) and (b) extinction spectra of a dispersion and gels 11 days after preparation. Simulated (c) S and (d) extinction spectra. (e) Scanning transmission electron micrograph of a gel (scale bar, 100 nm). Simulation snapshots at coarsening times (f) $t = 1000\tau_D$ and (g) $100000\tau_D$.

194 salt, tetrabutylammonium hexafluorophosphate (TBAPF₆), present during gel for-
195 mation (Fig. 4a and S12). The enhancement of the primary peak at wavenumber
196 $q \sim 0.05 \text{ \AA}^{-1}$ and progressive deepening of the minimum at lower q are reminiscent
197 of coarsening,⁴⁵ suggesting the salt concentration determines the extent of structural
198 evolution approaching arrest. These features are replicated in Brownian dynamics sim-
199 ulations of coarsening of nanoparticles with strong, short-ranged attractions (Fig. 4c,f,g
200 and S13). Indeed, the S at higher [TBAPF₆] superposes with S for a lower [TBAPF₆]
201 gel at longer aging time, supporting a correspondence between the effects of salt con-
202 centration and time (Fig. S14). However, other structures, like cluster fluids of varying
203 cluster fractal dimension, can have similar S , so S alone is not sufficient to determine
204 the microstructural evolution (Fig. S15).

205 The optical extinction spectra of the gels also depend on salt concentration (Fig. 4b),
206 providing complementary information to help understand their structures. At higher
207 [TBAPF₆], the extinction broadens and redshifts. We use MPM to test whether coars-
208 ening can explain these changes. ITO nanocrystals in this size range are known to have
209 a radially varying free electron concentration, so we model their dielectric function with
210 a Drude-type plasmonic core and a dielectric shell, complexity easily incorporated into
211 MPM. As before, the parameters describing the dielectric function are determined
212 by fitting the LSPR spectrum of a dilute nanocrystal dispersion (Fig. S8, Tables S2
213 and S3).⁴⁴ At each of six stages of coarsening from the Brownian dynamics trajec-
214 tory, we use MPM to compute the polarization-averaged extinction spectrum for the
215 64000-nanoparticle configuration (Fig. 4d). The simulations reproduce the asymmetric
216 broadening observed experimentally, while other candidate microstructures like cluster
217 fluids with similar trends in S show the opposite optical broadening trends (Fig. S15).
218 However, the local density increases much more, by over an order of magnitude, during
219 coarsening (Fig. S16), drastically changing the dipolar coupling environment and insti-
220 gating the optical broadening. This example illustrates the power of MPM to combine
221 structural and optical information to provide mechanistic insights across length scales
222 in structurally complex assemblies.

223 Outlook

224 Building on advances presented here, MPM’s computational efficiency will enable on-
225 the-fly evaluation of optical properties in dynamic, nanoparticle-based simulations,
226 making possible the design of complex plasmonic assemblies with targeted near- or
227 far-field responses using inverse methods.⁴⁶ Computation-guided design of disordered
228 structures with desired optical properties is particularly compelling for soft hybrid ma-
229 terials, e.g., plasmonic gels^{13,25–27} that can dynamically reconfigure—modulating how
230 they interact with light—in response to stimuli. In design of hybrid materials, MPM
231 can readily compute optical properties for networks comprising both dielectric (e.g.,
232 semiconductor) and metal nanoparticles or with hierarchical nanoparticle ordering,
233 significantly expanding the design space where computation can enhance experimental
234 discovery. An intriguing possibility is the creation of plasmonic materials with inhom-
235 geneous electric fields in compositionally-specific locations within the assembly, e.g.,
236 to enhance molecular detection sensitivity, plasmon-driven chemistry, or non-linear
237 optical effects.

238 Though the present work focuses on optical extinction and transmission, MPM can
239 be extended to address related properties of interest. One example is treating circu-
240 larly polarized electric fields, enabling simulation and design of plasmonic materials
241 with chiroptical responses.^{21,47} Here we have established MPM’s ability to quantify
242 many-body contributions to the optical response of complex assemblies, treated at the
243 level of dipoles. This approach explicitly incorporates structural complexity, explaining
244 and predicting optical phenomena that cannot be captured in effective medium and
245 mean field theories. Though many-bodied dipoles are sufficient to describe most obser-
246 vations of nanoparticle assemblies, it is possible, though increasingly computationally
247 intensive, to make MPM more quantitatively predictive by systematically including
248 higher-order polarization moments (quadrupoles, etc.) in the analysis. Finally, strate-
249 gies for treating nonspherical nanoparticles have been developed as extensions to Mie
250 theory,¹⁴ and similar approaches may be pursued to extend MPM to handle triaxial

251 ellipsoids or cubes.

252 **Methods**

253 **Synthesis and characterization of ITO nanocrystals.** ITO nanocrystals were
254 synthesized via established colloidal methods.^{26,27} The size of the nanocrystals was ex-
255 tracted either from a spheroid fit of the SAXS pattern of a dilute nanocrystal dispersion
256 (Fig. S12) or from statistics in bright-field scanning transmission electron microscope
257 (STEM) or scanning electron microscopy (SEM) images (Fig. S6). STEM and SEM
258 images were collected using a Hitachi S5500 on carbon support films on copper grids
259 and Si substrates, respectively. The Sn atomic doping concentration was determined
260 by Inductively Coupled Plasma-Optical Emission Spectrometry (ICP-OES) using a
261 Varian 720-ES instrument following acid digestion. Dielectric functions were extracted
262 by fitting to the heterogeneous Drude approximation model, which accounts for sur-
263 face depletion and heterogeneity among the nanocrystal ensemble.⁴⁴ Fitting was based
264 on optical transmission spectra (see below) collected on dilute nanocrystal dispersions
265 with concentration determined using ICP-OES.

266 **Mixed ITO nanocrystal superlattice assembly.** ITO nanocrystal superlattices
267 were formed by a liquid-air interface assembly method. After cleaning a 2 cm × 2 cm Si
268 substrate with Hellmanex (2 wt%) and acetone solution, 250 μL of water was dropped
269 on the substrate. On top of the water droplet, 100 μL of nanocrystal dispersion was
270 dropped. Nanocrystals were dispersed in the 2:1 mixture of hexane and toluene with
271 the addition of 5 μL of oleic acid. The amount of 1% Sn and 6% Sn ITO nanocrystals
272 were adjusted to the desired mixing ratio while maintaining the total nanocrystal con-
273 centration in the solution at 1 mg/mL. After depositing the nanocrystal dispersion,
274 the substrate was partially covered with a glass slide to control the evaporation rate
275 and convection flow. After evaporation of the solvent, the substrate was dried in air.

276 **Gelation of AL-functionalized ITO nanocrystals.** Aldehyde-terminated lig-
277 and (AL) was synthesized via previously reported synthetic protocols.²⁶ ITO nanocrys-

278 tals were functionalized by AL via a direct ligand exchange (Fig. S10), dispersed in
 279 N,N-dimethylformamide (DMF), and mixed with oxalyldihydrazide in ethylene glycol
 280 and TBAPF₆ in DMF to induce assembly. Gel structures were characterized by SAXS
 281 of capillaries measured in transmission using a SAXSLAB Ganesha; a dilute dispersion
 282 of nanocrystals was measured to record the form factor used in computing S for the
 283 gels (Fig. S12).

284 **Optical measurements.** For gels, the freshly prepared mixtures of AL-functionalized
 285 ITO nanocrystals and organics were injected into home-made glass sandwich cells with
 286 25-micron-thick thermoplastic spacer and sealed with Kapton film (Fig. S17). Extinc-
 287 tion spectra of both gels and superlattices were measured in transmission using an
 288 Agilent Cary 5000 for near-infrared and a Bruker Vertex 70 FTIR for mid-infrared.

289 **Mutual polarization simulations.** MPM simulations were performed in MAT-
 290 LAB using in-house code freely available at github.com/zeesherman/mutual-polarization.
 291 These simulations use a system of dimensionless units where $a = 1$, $\varepsilon_m = 1$, and $E_0 = 1$.
 292 For each frequency ω , the nanoparticle permittivity was set to $\varepsilon_p(\omega)$ and the N par-
 293 ticle induced dipoles \mathbf{p}_{ij} were computed for a particular field polarization $\mathbf{E}_0 = E_0 \hat{\mathbf{e}}_j$
 294 ($i = 1, \dots, N$, $j = x, y, z$) by solving eq 1 using GMRES with a relative error toler-
 295 ance of 10^{-3} . During each iteration, the right side of eq 1 is evaluated to an absolute
 296 error tolerance of 10^{-3} using an Ewald summation procedure discussed in Supporting
 297 Information Sec. 1.2 and Ref. 39. The polarization-averaged extinction cross-section
 298 per nanoparticle volume is $\sigma = \sum_j \sigma_j / N_E$, where $\sigma_j = \frac{3\sqrt{\mu_m \omega}}{4\pi a^3 \sqrt{\varepsilon_m} E_0^2} \text{Im}[\sum_i \mathbf{p}_{ij} \cdot \mathbf{E}_0 / N]$
 299 and N_E is the number of field polarizations. The electric field at any point and other
 300 quantities are also computed from \mathbf{p}_{ij} as detailed in Supporting Information Sec. 1.2.
 301 All dielectric functions used in this work are summarized in Table S3. σ in Fig. 1c
 302 was averaged over three polarizations and 20 equilibrated hard sphere configurations
 303 of $N = 8000$ from the Brownian dynamics method in Supporting Information Sec. 4.3.

304 **Simulation of mixed nanocrystal superlattices.** $N = 11600$ spherical nanopar-
 305 ticles of radius a were placed on a two-dimensional hexagonal lattice of area frac-
 306 tion 0.87 on the $z = 0$ plane inside a triply-periodic box, with a length of $50a$

307 in the z -direction normal to the lattice plane. Particles were randomly assigned to
 308 one of two %Sn dopant concentrations in proportion to the intended mixing fraction,
 309 with simple Drude dielectric functions described in Table S3. Two MPM simulations
 310 were performed for $\mathbf{E}_0 = E_0 \hat{\mathbf{e}}_j$ ($j = x, y$). The average dipole for each polarization
 311 was then computed $\langle \mathbf{p}_j \rangle = \sum_i \mathbf{p}_{ij}/N = \langle p_j \rangle \mathbf{e}_j$ and averaged over field polarizations
 312 $\langle p \rangle = (\langle p_x \rangle + \langle p_y \rangle)/2$. This process was repeated and $\langle p \rangle$ averaged over a total of 20
 313 independently prepared lattices. The fraction of incident light transmitted T for the su-
 314 perlattices when placed on a $500 \mu\text{m}$ thickness silicon substrate is then computed from
 315 $\langle p \rangle$ through the procedure described in Supporting Information Sec. 4.2 and extinction
 316 reported as $-\log T$.

317 **Simulation of nanocrystal gels.** Brownian dynamics simulations were per-
 318 formed in HOOMD-blue (v2.9.7)⁴⁸ with $N = 64000$ spherical nanoparticles of mean
 319 thermodynamic radius $a = 7.32 \text{ nm}$, polydispersity of $0.10a$, and volume fraction of
 320 $\eta = 0.01$ in a triply-periodic box with an integration time step of $\Delta t = 10^{-4} \tau_D$, where
 321 $\tau_D = \gamma^H a^2/k_B T$ is the diffusion time in terms of the hydrodynamic drag coefficient
 322 γ^H . Nanoparticles interacted with hard sphere repulsions and short-ranged attractions
 323 of approximate range $0.1a$ and contact strength $10k_B T$. Three MPM simulations for
 324 each sampled configuration were performed to find the polarization-averaged extinc-
 325 tion cross-section using an optical radius of 5.9 nm for all nanoparticles and a core-shell
 326 Drude dielectric function described in Table S3. The extinction spectra were normal-
 327 ized by dividing by their maximum values.

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341 Supporting Information Available

342 Additional details of the mutual polarization method, nanocrystal synthesis and as-
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Graphical TOC Entry

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