

Home Search Collections Journals About Contact us My IOPscience

Optimized generation of spatial qudits by using a pure phase spatial light modulator

This content has been downloaded from IOPscience. Please scroll down to see the full text.

2014 J. Phys. B: At. Mol. Opt. Phys. 47 225504

(http://iopscience.iop.org/0953-4075/47/22/225504)

View the table of contents for this issue, or go to the journal homepage for more

Download details:

IP Address: 157.92.4.71

This content was downloaded on 10/11/2014 at 17:06

Please note that terms and conditions apply.

Optimized generation of spatial qudits by using a pure phase spatial light modulator

J J M Varga¹, L Rebón², M A Solís-Prosser^{3,4}, L Neves⁵, S Ledesma¹ and C lemmi¹

E-mail: rebon@fisica.unlp.edu.ar

Received 18 June 2014, revised 10 September 2014 Accepted for publication 6 October 2014 Published 7 November 2014

Abstract

We present a method for preparing arbitrary pure states of spatial qudits, namely, D-dimensional $(D \ge 2)$ quantum systems carrying information in the transverse momentum and position of single photons. For this purpose, a set of D slits with complex transmission are displayed on a spatial light modulator (SLM). In a recent work we have shown a method that requires a single phase-only SLM to control independently the complex coefficients which define the quantum state of dimension D. The amplitude information was codified by introducing phase gratings inside each slit, and the phase value of the complex transmission was added to the phase gratings. After a spatial filtering process, we obtained in the image plane the desired qudit state. Although this method has proven to be a good alternative to compact the previously reported architectures, it presents some features that could be improved. In this paper we present an alternative scheme to codify the required phase values that minimizes the effects of temporal phase fluctuations associated to the SLM where the codification is carried out. In this scheme, the amplitudes are set by appropriate phase gratings addressed at the SLM, while the relative phases are obtained by a lateral displacement of these phase gratings. We show that this method improves the quality of the prepared state and provides very high fidelities of preparation for any state. An additional advantage of this scheme is that a complete 2π modulation is obtained by shifting the grating by one period; hence the encoding is not limited by the phase modulation range achieved by the SLM. Numerical simulations, that take into account the phase fluctuations, show high fidelities for thousands of qubit states covering the whole Bloch sphere surface. Similar analyses are performed for qudits with D = 3 and D = 7.

Keywords: quantum information, optical processors, correlators, modulators, gratings

1

(Some figures may appear in colour only in the online journal)

1. Introduction

One of the main challenges in the field of quantum information science is the ability to generate, modify, and measure the quantum systems which are the information carriers in quantum information processing and computing protocols [1]. In this context, photons are the natural choice for

communications, since they are easily transportable, slowly affected by decoherence, and have several degrees of freedom to encode information [2]. Among the feasible degrees of freedom, those that allow one to codify quantum systems of high dimensions, such as orbital angular momentum [3–5] and longitudinal momentum [6], have attracted particular interest. Another typical encoding are the so-called spatial

¹ Departamento de Física, FCEyN, Universidad de Buenos Aires, Buenos Aires 1428, Argentina

² Departamento de Física, IFLP, Universidad Nacional de La Plata, C.C. 67, 1900 La Plata, Argentina

³ Center for Optics and Photonics, Universidad de Concepción, Casilla 4016, Concepción, Chile

⁴ Departamento de Física, MSI-Nucleus on Advanced Optics, Universidad de Concepción, Concepción, Chile

⁵ Departamento de Física, Universidade Federal de Minas Gerais, Caixa Postal 702, Belo Horizonte, MG 30123–970, Brazil

qudits, namely, D-dimensional $(D \ge 2)$ quantum systems carrying information in the discretized transverse momentum and position of single photons [7, 8]. In the simplest approach, this discretization is achieved when the photons are made to pass through an aperture with D slits which sets the qudit dimension [9]. Due to this simplicity, spatial qudits enable one to work in high dimensions without cumbersome optical setups. For that reason they have drawn interest for miscellaneous applications such as quantum information protocols [10], quantum games [11], quantum algorithms [12], and quantum key distribution [13]. Most of those applications have benefited from the recent developments on the control of spatial qudits based on the technology of electrically addressed spatial light modulators (SLMs). SLMs have dramatically simplified and broadened the range of operations that can be implemented in real time on spatial qudits for state preparation, transformation, and measurement [14–17].

Initially, Lima et al [15] have shown that by imaging the output beam of an amplitude-only SLM onto a phase-only SLM, one may obtain complete and independent control of the amplitude and phase of the complex coefficients that define the qudit state. Therefore, this scheme requires two SLMs at each link of the setup (preparation, transformations, and measurements) in order to implement arbitrary operations at each one. Besides being costly in terms of optical resources, this approach entails two drawbacks: (i) the overall diffraction efficiency at each link is very low, and (ii) in order to avoid even more losses, the image of the first SLM must match the second one pixel by pixel, which is difficult in practice. In a recent letter [16], we presented a proof-ofprinciple demonstration of a method which proposed the use of a single phase-only SLM to control independently the amplitude and phase of the state coefficients. This method is, less costly; offers a much higher diffraction efficiency (we estimated a 10 times higher efficiency), which is relevant when working with single photon sources; and does not require an optical system for projecting the image of an SLM onto a second one in order to obtain the complex modulation. Among the different techniques to represent a complex function in a single SLM [18-20], our method follows the proposals of [21, 22] for encoding amplitude and phase information onto a phase-only SLM. To this end, phase diffraction gratings were displayed in those zones corresponding to the slits. The desired amplitude of the complex coefficients was obtained by controlling the amount of light diffracted on the first order, which is a function of the phase modulation depth of the grating. The phase of the complex coefficients, which defines the required relative phase, was achieved by adding a constant phase value to the grating. The required complex light distribution was obtained after filtering the first diffracted order in the Fourier plane. We shall refer to this method as the phase-addition (PA) method.

Although the PA method gives, on average, good fidelities of preparation for spatial qubits and qudits of dimension at least up to 7, we observed that many of the prepared states had their fidelities reduced under the same experimental conditions for state preparation and characterization. In that paper [16], we pointed out that this effect was possibly due to temporal phase fluctuations of the used SLM, which was based on liquid crystal on silicon (LCoS) technology. In fact, LCoS may lead to a flicker in the optical beam because of the digital addressing scheme (pulse width modulation) which introduces, among other undesirable effects, those phase fluctuations [23, 24] that affect the quality of the encoded state. This spurious effect will be amplified as the number of SLMs in a given setup increases, so it is desirable to eliminate or at least minimize it.

In this paper we first analyze, by numerical simulation, the effects of the phase fluctuations on the quality of the states prepared by the PA method and compare the results with the experimental ones shown in the previous work. Our results corroborate the conjecture that those fluctuations are primarily responsible for the reduction of the fidelities. After that, we propose an alternative scheme of encoding spatial qudits that minimizes those effects and, consequently, improves the quality of the preparation. In this scheme, the amplitudes of the slits also are controlled by means of blazed gratings, but the values of the phases of the state coefficients are obtained by performing lateral displacements of the gratings instead of by adding a constant phase. In this way, the required phase is controlled only by the grating position, which is not affected by phase fluctuations. We shall refer to this method as the grating-displacement (GD) method. Besides improving the preparation, the new encoding scheme is more flexible than the previous one regarding the phase modulation range achieved by the SLM. The PA method requires an SLM with a phase modulation of at least 2π , while the GD method is not limited by this condition, since a complete 2π modulation is obtained by shifting the grating by one period. This fact is important, especially when long wavelengths (usually near IR), such as those obtained by parametric down-conversion [25–28], are used. The performance of the GD method is analyzed by simulating the preparation of arbitrary states and their tomographic reconstruction. We report the results obtained for thousands of qubit states covering the whole Bloch sphere surface and spatial qudits of dimension D = 3and D = 7. By studying the fidelities of preparation, we show that the GD method overcomes the PA one.

2. The grating-displacement method

The encoding process for the generation of pure states of spatial qudits can be explained as follows. When a paraxial and monochromatic single-photon field is transmitted through an aperture described by a complex transmission function $A(\mathbf{x})$, its state, assumed here to be pure, is transformed as

$$|\Psi\rangle = \int d\mathbf{x} \, \psi(\mathbf{x}) |\mathbf{x}\rangle \stackrel{A(\mathbf{x})}{\Longrightarrow} \int d\mathbf{x} \, \psi(\mathbf{x}) A(\mathbf{x}) |\mathbf{x}\rangle,$$
 (1)

where $\mathbf{x} = (x, y)$ is the transverse position coordinate and $\psi(\mathbf{x})$ is the normalized transverse probability amplitude for this state; i.e., $\int d\mathbf{x} |\psi(\mathbf{x})|^2 = 1$. Now, let us consider that $A(\mathbf{x})$ is an array of $D \ge 2$ rectangular slits of width 2a, period d and length $L(\gg a, d)$, where each slit ℓ has a transmission

amplitude β_{ℓ} . Thus, $A(\mathbf{x})$ will be given by

$$A(\mathbf{x}) = \operatorname{rect}\left(\frac{x}{L}\right) \times \sum_{\ell=0}^{D-1} \beta_{\ell} \operatorname{rect}\left(\frac{y - \eta_{\ell} d}{2a}\right), \tag{2}$$

where $\eta_{\ell} = \ell + (D-1)/2$. Without loss of generality and for simplicity, we will assume that $\psi(\mathbf{x})$ is constant across the region of the slits. Hence, the state of the transmitted photon in (1) will be [7]

$$|\psi\rangle = \sum_{\ell=0}^{D-1} \tilde{\beta}_{\ell} |\ell\rangle, \tag{3}$$

where $\tilde{\beta}_{\ell} = \beta_{\ell} / \sqrt{\sum_{j=0}^{D-1} |\beta_{j}|^{2}}$, and $|\ell\rangle$ denotes the state of the photon passing through the slit ℓ .

As we have shown in [16], in order to prepare arbitrary states of the form (3) with a single phase-only SLM, a phase one-dimensional diffraction grating is displayed on the different regions of the SLM, each of them corresponding to a particular slit. In this work, a blazed phase profile is selected to achieve the maximum diffraction efficiency in the first order, which can be expressed as [29]

$$\epsilon_1 = \operatorname{sinc}^2 \left(1 - \frac{\varphi_0}{2\pi} \right), \tag{4}$$

where φ_0 is the phase modulation $\operatorname{sinc}(u) = \sin (\pi u)/(\pi u)$. When $\varphi_0 = 2\pi$, the first order efficiency has a maximum value of 100%. By selecting another value for φ_0 , it is possible to modulate the amount of light diffracted on the order and consequently the amplitude of each slit. Equation (4) corresponds to an ideal blazed profile with continuous modulation. Nevertheless, given that the representation of the grating period is carried out through a finite number of pixels, this imposes a discretization in the phase levels used to generate the blazed profile. Thus if N is the number of quantization levels, the maximum efficiency value will be assigned to the maximum amplitude of the slit i.e., $|\tilde{\beta}_{\ell}| = 1$ coefficients; corresponds $\varphi_0 = (N-1)/N \times 2\pi$. Other amplitude values will correspond to other values of φ_0 , which are obtained from (4). If the employed SLMs do not reach 2π phase modulation, then the relative slit amplitudes should be recalculated with respect to the maximum efficiency achieved. In order to avoid the introduction of additional phases in the encoding process, the phase gratings should be designed with zero mean value. However, as the SLM can only display positive phase values, the gratings are generated with a mean value equal to half of the maximum phase modulation depth, $(N-1)/N \times \pi$ for a blazed grating.

Let us now describe the GD method to control the phase of the complex coefficients, $\arg(\tilde{\beta}_{\ell})$, in (3). It can be understood by analyzing the transfer function of the grating. If it is assumed that when the grating is centered at x = 0 its phase value is zero, the transfer function of the slit ℓ in the far field

can be written as:

$$T_{\ell}(x) = \sum_{n} t_n e^{-i\frac{2\pi}{p} xn}, \qquad (5)$$

where t_n is the amplitude of the *n*th diffraction order, x is the position along the grating, and p is the grating period, both measured in pixel units. A lateral displacement of the grating by a distance of δ_{ℓ} pixels from x = 0 introduces a phase shift

$$\phi_{\ell n} = \frac{2\pi n}{p} \delta_{\ell} \tag{6}$$

in the *n*th order, since the transfer function now is given by

$$T_{\ell}(x-\delta_{\ell}) = \sum_{n} t_{n} e^{-i\frac{2\pi}{p}(x-\delta_{\ell})n} = \sum_{n} t_{n} e^{-i\frac{2\pi}{p}xn} e^{i\frac{2\pi}{p}\delta_{\ell}n}.$$
 (7)

By selecting the first diffraction order to obtain the required complex modulation, the transfer function of the grating will be

$$T_{\ell}^{(1)}\left(x-\delta_{\ell}\right) = t_{1} e^{-i\frac{2\pi}{p}x} e^{i\frac{2\pi}{p}\delta_{\ell}},\tag{8}$$

and the phase shift introduced by the translation is $\phi_{\ell 1} = 2\pi\delta_{\ell}/p$. When the maximum amplitude t_1 is normalized, regardless of what happens in the other diffraction orders, its value coincides with $\sqrt{\varepsilon_1}$ in (4).

We will show in the next sections that as the phase of the complex coefficients is determined by the grating position, its value is almost unaffected by phase fluctuations.

3. Numerical simulations for state preparation

3.1. Proposed experimental setup

In order to analyze the performance of both PA and GD encoding methods against the variation of the different parameters of the SLM (phase fluctuation levels, number of pixels used to represent a grating period, etc.), we carried out numerical simulations of a realistic optical setup designed to prepare and characterize spatial qudit states. The proposed experimental setup is depicted in figure 1. A given source generates a single-photon field in the pure state given by the left part of (1). As mentioned earlier, we assume that the transverse probability amplitude $\psi(\mathbf{x})$ is constant across the region where the slits are displayed in the SLM. In the upper part of the setup, used for state preparation, a phase-only SLM (SLM1) is addressed with a phase mask—either by the PA or GD method—corresponding to the spatial qudit state intended to be prepared. SLM1 is placed in the front focal plane of lens L1, and an iris diaphragm is placed at its back focal plane in order to filter the first diffracted order which carries the required information [16]. In the lower part of the setup, used to reconstruct the quantum states by tomography, the Fourier transform of the first diffracted order is projected onto a second SLM (SLM2) and placed at the back focal plane of L2. SLM2 is used to encode the measurement bases employed to perform the tomographic process as described in [15]. A single pixel detector is placed at the Fourier transform plane of SLM2, in the center of its first diffraction order (x = 0).

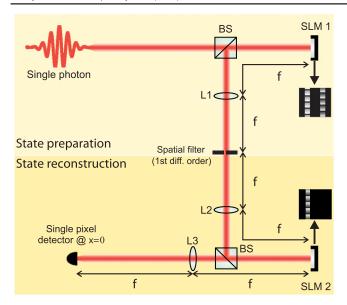


Figure 1. Proposed experimental setup to simulate the preparation and characterization of spatial qudit states with a single phase-only SLM subjected to temporal phase fluctuations. BS: beam splitter; L: lens; SLM: reflective phase-only spatial light modulator; *f*: focal length of the lenses. The insets show examples of phase masks addressed at the SLMs for state preparation (top) and tomography (bottom).

This detector registers the single count rates that, after normalization, give us the probabilities to reconstruct the states. It is important to note that with this configuration it is possible to perform arbitrary projections of the input state without the need to carry on measurements in the near field. In this way, the optical setup remains unchanged. In particular, we perform projections onto the informational complete set of a mutually unbiased basis [30, 31], following the experiment reported in [15]. Finally, we apply the maximum likelihood technique to obtain the best state estimation consistent with the requirements of a physical state [32, 33].

3.2. Model for temporal phase fluctuations

As mentioned previously, reflective SLMs, such as LCoSs, are usually employed to obtain pure phase modulation. In these displays, a high-frequency series of binary pulses, known as an addressing sequence, leads to the desired graylevel representation. Unlike analogue drive schemes, which need to control the applied voltages carefully, the digital drive schemes are stable and offer a repeatable performance. The sequences are conformed by a train of binary and equally weighted bit planes which differ in sequence length and addressable phase levels. It is assumed that the limited viscosity of the liquid crystal means that the addressing frequency cannot be resolved, and, in this way, the desired gray level is obtained through the effectively analogue liquid crystal molecule position. Nevertheless, the digital addressing scheme produces a superimposed modulation (flicker) with a frequency that depends on the employed sequence. In many devices the digital addressing sequence can be programmed. Shorter sequences offer the possibility a of higher repetition

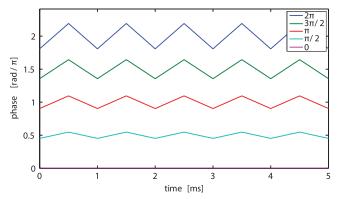


Figure 2. Model for the temporal fluctuations used in the numerical simulations. Here, the different curves correspond to different phase modulations addressed on the SLM, when the amplitudes' fluctuation is 20% of the average phase value.

rate in a frame period, which partially compensates the problem of the low viscosity and leads to a reduction in the flicker amplitude; however, the number of addressable phase levels is lower in these cases [34]. In a previous paper [23, 35], a simple model has been proposed to describe the phase fluctuations (flicker) that are associated with these devices. Although the exact shape of the perturbation varies from one SLM to another, and depends on the pulse width modulation sequence used to address the electrical signal and the selected gray level, a suitable approximation that describes the general behavior is a triangular phase fluctuation whose height increases linearly with the phase value. According to the selected sequence, the phase fluctuations can reach values as high as 120% of the average phase value [24]. Therefore, to illustrate their effects on each method (PA and GD), we chose different amplitudes of fluctuation, corresponding to intermediate sequences, to perform the numerical simulations. We have considered phase fluctuations ranging from 20-60% of the average phase value. As an example, a model for a typical temporal fluctuation is shown in figure 2, where the amplitudes' fluctuation is 20% of the average phase value.

It was noted through the numerical simulations that the influence of the synchronization between the temporal signals sent to both modulators (SLMs 1 and 2 in figure 1) on the final result is irrelevant. As a consequence, we have decided to consider the second SLM, employed to perform the tomographic projections, as a device without fluctuations and to transfer the phase fluctuations of both elements to the first SLM used to prepare the state.

In order to validate the mentioned assumptions and the proposed model, we compared the experimental results obtained in [16] with the corresponding numerical simulation. To this end, we used the same setup and encoding scheme (PA method) of the previous work, considering the case of a blazed grating. Here and in the following section, we quantify the quality of the preparation process with the fidelity $F \equiv \langle \psi | \hat{\rho} | \psi \rangle$ between the state intended to be prepared, $|\psi\rangle$, and the density matrix of the state actually prepared and reconstructed by tomography, $\hat{\rho}$. Ideally, it is desirable to

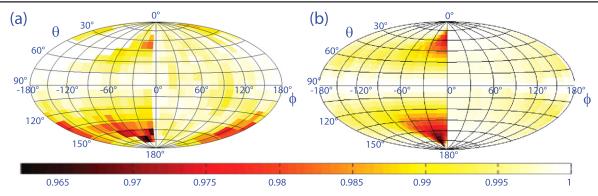


Figure 3. Bloch spheres showing the fidelities of preparation of spatial qubit states using the phase-addition method: (a) experimental results from [16] of 561 states uniformly distributed on the surface, and (b) numerical simulations of the preparation of 2112 states, taking into account our model of phase fluctuations in the SLM (see figure 2). The latitude $\theta \in [0, \pi]$ and the longitude $\phi \in (-\pi, \pi]$ parametrize an arbitrary pure state $|\psi\rangle = \cos(\theta/2)|0\rangle + e^{i\phi}\sin(\theta/2)|1\rangle$ on the sphere surface.

have F=1. The Bloch spheres showing the fidelities of preparation of spatial qubits are shown in figure 3. The color map goes from white, for ideal fidelity F=1, to black for the minimum obtained value. Figure 3(a) corresponds to the experimental results of [16], and figure 3(b) corresponds to the results obtained by numerical simulation. Although the experimental results show a region of low fidelities around $\phi=\pi$ that are not reproduced by the simulation, the similarity between them is apparent in all other regions of the Bloch's sphere. This slight difference between both results arises from the fact that the model used to simulate the temporal fluctuations is just a first order approximation. Besides, the aim of this study is to compare the performance of both encoding methods under phase fluctuations and not to exactly reproduce its shape.

4. Results

As mentioned above, it is expected that the proposed encoding method (GD) be barely affected by phase fluctuations, since the phase of the complex coefficients is determined by the grating positions, which are not influenced by those fluctuations. Nevertheless, a possible drawback is that, in principle, there are fewer available phase levels than in the PA method. In the latter, the available phase values are determined by the digital sequence used to address the LCoS, whereas in the GD method, the phase values are quantized by the number of pixels used to represent a grating period, i.e., the minimum phase shift is $\phi = 2\pi/p$. We will show here that for a sufficiently large value of p, this drawback has smaller effects than the phase fluctuations in the PA method.

Considering spatial qubits, let us see how the choice of the grating period p affects the quality of the preparation. For blazed gratings with p = 4, 8, and 16 pixels, we simulated the preparation of 2112 states uniformly distributed over the Bloch sphere surface. The results are shown in figures 4(a)–(c). In these figures, a different color map to that of figure 3 was chosen to allow visualizing the loss of fidelity between the different prepared states from F = 1 (white) to the minimum obtained value (black).

For each p, we see that a fidelity decrease with a periodic distribution that depends on how far or close is the phase of the quantum state from the phase value that we are able to represent. This decrease is due to the phase quantization rather than the phase fluctuations introduced by the LCoS, and, as expected, it becomes smaller as p increases. Figure 4(a) shows the fidelities obtained with a 4-pixel grating period. In figure 4(b), with an 8-pixel grating period, the results are much better, and for p = 16 in figure 4(c), the obtained fidelities are excellent. In a realistic scenario, a grating with a 16-pixel period provides high diffraction efficiency and enables the first diffraction order to be placed far away from the 0th order on the Fourier plane. In this way it can be easily filtered, and the light distribution is not corrupted by unwanted noise. Gratings with larger periods will improve the phase resolution, but the first and 0th order will be so close that it would be difficult to perform the filtering. Hence, to compare the performance of both methods (PA and GD) under fluctuations on the SLMs, we have chosen a grating with a 16-pixel period.

Figure 5 shows, for both methods (PA, first column; and GD, second column), the fidelities of preparation for qubit states considering three different phase fluctuation amplitudes: 20% (figures 5(a) and (b)), 30% (figures 5(c) and (d)) and 60% (figures 5(e) and (f)) of the average phase value. As in the previous cases, we have chosen a different color map from those of figures 3 and 4. The mean value and standard deviation were calculated from the collection data obtained from the simulation. For each phase fluctuation amplitude, the GD method achieves higher average values of fidelity, and, unlike the PA method, there are not significant variations of the fidelity between different states on the Bloch sphere, which is reflected in a smaller standard deviation. Moreover, increasing the phase fluctuations amplitude results in lower reconstruction fidelities for the PA method with respect to the GD method. Therefore, from these results it is clear that while the PA method is strongly dependent on the phase fluctuation amplitude, the GD method remains almost unaffected.

Two thousand arbitrary pure states corresponding to spatial qudits of higher dimension have been prepared. The histograms shown in figure 6 represent the number of states of

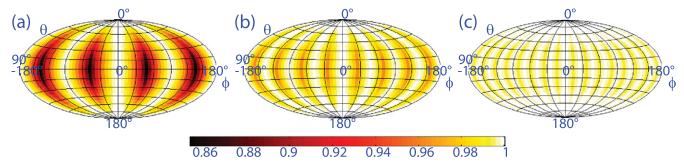


Figure 4. Bloch spheres showing the fidelities of preparation of spatial qubit states using the grating-displacement method. All graphics were obtained from numerical simulations with 4 (a), 8 (b), and 16 (c) displacements of the diffraction grating.

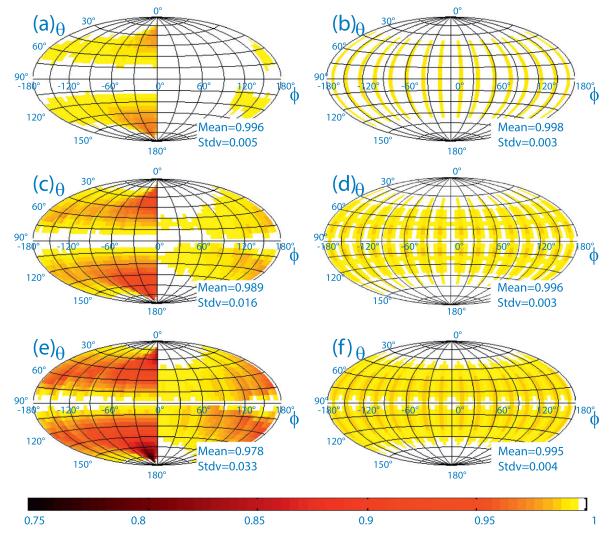


Figure 5. Bloch spheres showing the fidelities of preparation of 2112 spatial qubit states using the PA (first column) and GD (second column) method. The corresponding phase fluctuation amplitudes are: 20% (first row), 30% (second row), and 60% (third row) of the average phase value. The insets show the mean fidelity and its standard deviation.

dimension D = 3 whose fidelity values belong to a particular interval. Figures 6(a) and (b) correspond, respectively, to the results obtained with the PA and GD encoding method for phase fluctuations of 20% of the average phase value. Figures 6(c) and (d) show the equivalent results for phase fluctuations of 30%, and figures 6(e) and (f) the same for fluctuations of 60%. The results for qudits of dimension D = 7 are shown in figure 7. Again, the left column represents the

histograms obtained from the PA method, and the right column to those obtained from the GD method. Figures 7(a) and (b) correspond to phase fluctuations of 20%, figures 7(c) and (d) to fluctuations of 30%, and figures 7(e) and (f) to phase fluctuations of 60%. In a similar way as in the case of a Hilbert space of dimension D = 2, the results obtained for dimensions D = 3 and D = 7 show that the GD method leads to an increase of the mean fidelity and to a diminution of the

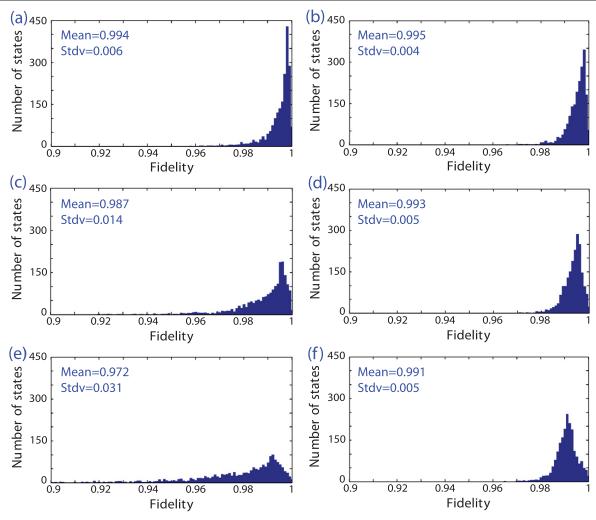


Figure 6. Occurrence fidelities of preparation of 2000 spatial qudit states, of dimension D = 3, using the PA (first column) and GD (second column) method. The corresponding phase fluctuation amplitudes are: 20% (first row), 30% (second row), and 60% (third row) of the average phase value. The insets show the mean fidelity and its standard deviation.

standard deviation, which agrees with the fact that the encoding applied in the preparation and reconstruction processes is almost not affected by phase fluctuations.

5. Conclusions

In this work we have proposed a new method to encode spatial qudit states using an LCoS as a single phase-only spatial light modulator. In this method, the complex transmissions of the D slits that are used to represent the quantum state are encoded by means of phase diffraction gratings. The amplitudes are driven through the phase modulation depth of the grating, and the required phases are controlled by performing lateral translations of the grating. Given that the phase values are determined by the grating position, the method is almost unaffected by the phase fluctuations associated to LCoSs.

We have analyzed the performance of the proposed method by numerical simulations, where we evaluated the preparation of arbitrary states in a first SLM and its tomographic reconstruction, using projective measurements onto a pre-fixed basis, in a second SLM. The proposed method (GD) has been compared with a previous one in [16] where the required phases were controlled by adding a constant phase value to the grating (PA). This has been done under different phase fluctuation intensities for qubits and for qudits of dimension D=3 and D=7. In all cases the results of the simulations have shown a greater robustness of the GD method against phase fluctuations when comparing with the PA method. In addition, the GD method offers wider experimental flexibility, allowing one to use SLMs with a maximum phase modulation below 2π . This feature is important, especially when long wavelengths (usually near IR), as those of photons obtained by parametric down-conversion, are used.

Therefore, the method proposed here may become a valuable tool for experiments based on spatial qudits, especially when one has to assemble two or more SLMs (e.g., for state preparation and transformations) subjected to phase fluctuations. By using the GD method, one minimizes the

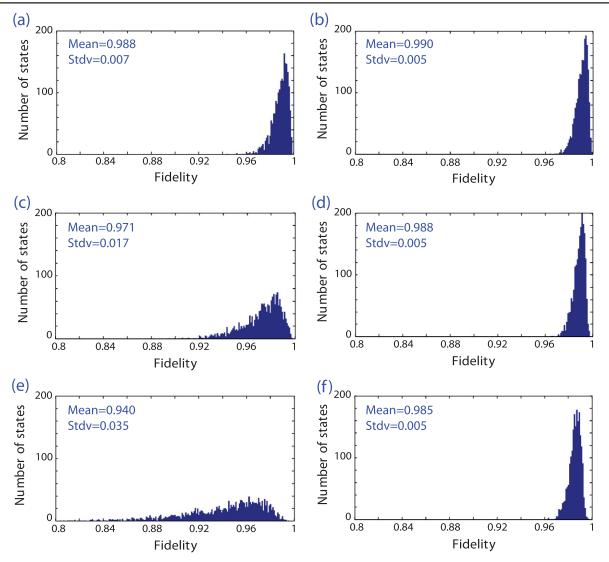


Figure 7. Occurrence fidelities of preparation of 2000 spatial qudit states, of dimension D = 7, using the PA (first column) and GD (second column) method. The corresponding phase fluctuation amplitudes are: 20% (first row), 30% (second row), and 60% (third row) of the average phase value. The insets show the mean fidelity and its standard deviation.

unwanted effects caused by the fluctuations and, consequently, improves the realization of the protocol of interest.

Acknowledgements

This work was supported by UBACyT 20020100100689, CONICET PIP 112–200801-03047, and ANPCYT PICT 2010–02179 (Argentina); CNPq 485401/2013–4 and FAPE-MIG APQ-00149–13 (Brazil); and CONICYT PFB08–24 and Milenio ICM P10–030-F (Chile). MASP acknowledges financial support from CONICYT (Chile).

References

 Barnett S M 2009 Quantum Information (New York: Oxford University Press)

- [2] Kok P and Lovett B W 2010 Introduction to Optical Quantum Information Processing (Cambridge: Cambridge University Press)
- [3] Mair A, Vaziri A, Weihs G and Zeilinger A 2001 Nature 412 313
- [4] Molina-Terriza G, Torres J P and Torner L 2008 Nat. Phys. 3 305
- [5] Malik M, Mirhosseini M, Lavery M P J, Leach J, Padgett M J and Boyd R W 2014 Nat. Commun. 5 3115
- [6] Rossi A, Vallone G, Chiuri A, de Martini F and Mataloni P 2009 Phys. Rev. Lett. 102 153902
- [7] Neves L, Lima G, Aguirre-Gómez J G, Monken C H, Saavedra C and Pádua S 2005 Phys. Rev. Lett. 94 100501
- [8] O'Sullivan-Hale M N, Ali Khan I, Boyd R W and Howell J C 2005 Phys. Rev. Lett. 94 220501
- [9] Neves L, Pádua S and Saavedra C 2004 Phys. Rev. A 69 042305
- [10] Solís-Prosser M A and Neves L 2011 Phys. Rev. A 84 012330
- [11] Kolenderski P, Sinha U, Youning L, Zhao T, Volpini M, Cabello A, Laflamme R and Jennewein T 2012 Phys. Rev. A 86 012321

- [12] Marques B, Barros M R, Pimenta W M, Carvalho M A D, Ferraz J, Drumond R C, Terra Cunha M and Pádua S 2012 Phys. Rev. A 86 032306
- [13] Etcheverry S, Cañas G, Gómez E S, Nogueira W A T, Saavedra C, Xavier G B and Lima G 2013 Sci. Rep. 3 2316
- [14] Lima G, Vargas A, Neves L, Guzmán R and Saavedra C 2009 Opt. Express 17 10688
- [15] Lima G, Neves L, Guzmán R, Gómez E S, Nogueira W A T, Delgado A, Vargas A and Saavedra C 2011 Opt. Express 19 3542
- [16] Solís-Prosser M A, Arias A, Varga J J M, Rebón L, Ledesma S, Iemmi C and Neves L 2013 Opt. Lett. 38 4762
- [17] Solís-Prosser M A and Neves L 2010 Phys. Rev. A 82 055801
- [18] Cohn R and Liang M 1994 Appl. Opt. 33 4406
- [19] Birch P, Young R, Budgett D and Chatwin C 2001 Opt. Lett. 26 920
- [20] van Putten E G, Vellekoop I M and Mosk A P 2008 Appl. Opt. 47 2076
- [21] Davis J A, Cottrell D M, Campos J, Yzuel M J and Moreno I 1999 Appl. Opt. 38 5004
- [22] Bagnoud V and Zuegel J D 2004 Opt. Lett. 29 295

- [23] Lizana A, Moreno I, Márquez A, Iemmi C, Fernández E, Campos J and Yzuel M J 2008 Opt. Express 16 16711
- [24] Lizana A, Marquez A, Lobato L, Rodange Y, Moreno I, Iemmi C and Campos J 2010 Opt. Express 18 10581
- [25] Burnham D C and Weinberg D L 1970 Phys. Rev. Lett. 25 84
- [26] Kwiat P G, Mattle K, Weinfurter H and Zeilinger A 1995 Phys. Rev. Lett. 725 4337
- [27] Kwiat P G, Waks E, White A G, Appelbaum I and Eberhard P H 1999 *Phys. Rev.* A **60** R773
- [28] Xue Y, Yoshizawa A and Tsuchida H 2010 Opt. Express 18 8182
- [29] Goodman J W 2005 Introduction to Fourier Optics (New York: McGraw-Hill)
- [30] Ivanovic I D 1981 J. Phys. A: Math. Gen. 14 3241
- [31] Wootters W K and Fields B D 1989 Ann. Phys. 191 363
- [32] Fiurášek J 2001 Phys. Rev. A 64 024102
- [33] James D F V, Kwiat P G, Munro W J and White A G 2001 *Phys. Rev.* A **64** 052312
- [34] Hermerschmidt A, Osten S, Krüger S and Blümel T 2007 *Proc.* SPIE 6584 65840E
- [35] Martínez F, Márquez A, Gallego S, Francés J and Pascual I 2014 Opt. Eng. 53 014105