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ABSTRACT

In this paper the possibility of using a Multilayer Percep-
tron (MLP) network trained with the Backpropagation
Algorithm for detecting location and size of a damage in
a civil engineering structure is investigated. The struc-
ture considered is a 20 m high steel lattice mast sub-
jected to wind excitation. The basic idea is to train a
neural network with simulated patterns of the relative
changes in natural frequencies and corresponding sizes
and locations of damages in order to recognize the be-
haviour of the damaged as well as the undamaged struc-
ture. Subjecting this trained neural network to mea-
sured values should imply information about damages
states and locations. The training data are obtained by
an FEM of the mast. Different damage scenarios are
established by simulating a damage in one of the eight
lower diagonals. The eight lower diagonals are cut and
provided with bolted joints. Each bolted joint consists
of 4 slice plates giving the possibilities of simulating a
1/4, 1/2, 3/4 and full reduction of the area of a diag-
onal. A damage is simulated by removing one or more
splice plates in these bolted joints. The utility of the
neural network approach is demonstrated by a simula-
tion study as well as full-scale tests where the mast is
identified by an ARMA-model. The results show that
a neural network trained with simulated data is capable
for detecting location of a damage in a steel lattice mast
when the network is subjected to experimental data.

NOMENCLATURE

x_{lj}: Output of the jth node in the lth layer

θ_{lj}: a threshold of the jth neuron in the lth layer

N_0: Number of network input

N_k: Number of network output

$f(\cdot)$: Activation function

E: Error function

y_j: Desired output

$\hat{y}_j$: Actual output

$w_{lj,i}$: Connection weight from node i and node j

η: Learning rate

α: Momentum term

1. INTRODUCTION

A sudden failure in a structure can be very costly and
may be catastrophic in terms of human life and property
damage. Many techniques of non-destructive evaluation
are currently available to detect a damage in structures.
Such techniques include e.g. visual inspections, ultra-
sonic testing, acoustic emission, etc. However most of
these techniques are inconvenient in many situations due
to the need for the investigator to have assess to the
structure. This inconvenience can be avoided through
the use of vibration-monitoring techniques. During the
last years major research efforts have been directed to-
wards developing techniques for damage assessment based
on changes in vibration characteristics. One of the con-
sequences of the development of a crack is a decrease in
local stiffness which in turn results in a decrease in some
of the natural frequencies. The most commonly applied
vibration based inspection damage assessment technique
is based on changes of natural frequencies only. This is
attractive since natural frequencies can be obtained from
measurements at a single point on the structure. If mea-
surements at a several points are carried out the mode
shapes in discrete points of the structure corresponding
to the different natural frequencies may be established.
Then, mode shape information can also be used for dam-
age assessment. However, in order to be able to evaluate
the deterioration state of a structure by vibration based
inspection it is also necessary to estimate size and lo-
cation of the damage, damage assessment. A review of
vibration based damage assessment techniques can be
found in Rytter [1].

The problem of damage assessment on the basis of measured data is essentially one of the pattern recognition. Measured data from an undamaged structure must be distinguishable from measured data from a damaged structure. Different pattern recognition approaches have been proposed in the literature, see e.g. Yin et al. [2], Samman et al. [3]. In these papers pattern recognition techniques are presented to estimate the damage presence and location but not magnitude of the damage. However, recently, artificial neural networks are proving to be an effective tool for pattern recognition in a variety of applications, see e.g Hertz et al. [4] and among these also for damage assessment. The basic idea is to train a neural network in order to recognize the behaviour of the damaged as well as the undamaged structure. Subjecting this trained neural network to information from vibration tests should imply information about damage state and location. During the last years this neural network based damage assessment approach has been proposed in different papers. In Thomsen et al. [5] a neural network was implemented and trained to classify measured ultrasonic power spectra of composite laminates, according to fabrication quality. Kudva et al. [6] used a neural network to determine location and size of a damage in a structure from measured strain values at discrete locations. The neural network is trained by finite-element data. Strain patterns are used as inputs and the damage location and size as outputs to train the neural network to a desired level of accuracy. The trained network can then be used to determine the location, size and effect of any unknown damage using measured strain values (at the same locations as before) as inputs to the neural network. The damage assessment approach proposed in Kudva et al. [6] has also been used in Worden et al. [7]. In a simulation study, Wu et al. [8] demonstrate a damage detecting network trained on measured frequency response functions from the system. Elkordy et al. [9] trained a neural network with simulated mode shape ratios in order to diagnose damages states obtained experimentally from series of shaking table tests of a five-storey steel frame. In Kirkegaard et al. [10] a neural network is trained with the relative changes in natural frequencies obtained by an FEM. The network is then used to estimate location and size of a damage in a beam from measured natural frequencies. In all the papers, mentioned above, a basic Multi-Layer Perceptron network trained with the backpropagation algorithm was used.

In this paper the aim is to investigate the use of artificial neural networks for damage assessment of a civil engineering structure. Training of the network is performed with patterns of the relative changes of the natural frequencies that occur due to a damage. This implies that each pattern represents the computed changes of the natural frequencies due to a crack of a particular size at a particular location. The changes are estimated by using an FEM.

In section 2 a short description of artificial neural networks is given and a neural network based damage assessment approach is proposed. In section 3 the proposed damage assessment approach is used in an example with a 20 m high steel lattice mast. The damage assessment approach is investigated with simulated as well as experimental data. At last in section 4 conclusions are given.

2. NEURAL NETWORKS

The past decade has seen an explosive growth in the studies of artificial neural networks. In part this was the result of technological advances in personal and mainframe computing, enabling neural network investigators to simulate and test ideas in ways not readily available before 1980.

Artificial neural networks are computational models inspired by the neuron architecture and operation of the human brain. The pioneering work in this field is usually attributed to McCulloch and Pitts in 1943. They developed a simplified model of a neuron. The brain is composed of neurons of many different types, see McCulloch et al. [11].

An artificial neural network is an assembly (network) of a large number of highly connected processing units, the so-called nodes or neurons. The neurons are connected by unidirectional communication channels ("connections"). The strength of the connections between the nodes is represented by numerical values which normally are called weights. Knowledge is stored in the form of a collection of weights. Each node has an activation value that is a function of the sum of inputs received from other nodes through the weighted connections. The neural networks are capable of self-organization and knowledge acquisition, i.e learning. One of the characteristics of neural networks is the capability of producing correct, or nearly correct, outputs when presented with partially incorrect or incomplete inputs. Further, neural networks are capable of performing an amount of generalization from the patterns on which they are trained. Most neural networks have some sort of "training" rule whereby the weight of connections are adjusted on the basis of presented patterns. In other words neural networks "learns" from examples, just like children learn to recognize dogs from examples of dogs, and exhibit some structural capability for generalization. Training consists of providing a set of known input-output pairs, patterns, to the network. The network iteratively adjusts the weights of each of the nodes so as to obtain the desired outputs (for each input set) within a requested level of accuracy. Error is defined as a measure of the difference between the computed pattern and the expected output pattern. For a more detailed description of neural networks, see e.g. Hertz et al. [4] and Hush et al. [12].

2.1 Multilayer Perceptron

Since McCulloch-Pitts in 1943 there have been many studies of mathematical models of neural networks. Many different types of neural networks have been proposed by changing the network topology, node characteristics and learning procedures. Examples of those are e.g. the Hopfield network, see Hopfield [13], the Kohonen network, see Kohonen [14] and the so-called multilayered perceptron (MLP) network trained by means of the back-propagation algorithm. The MLP trained by the back-propagation algorithm is currently given the greatest attention by application developers, see e.g. Rumelhart et al. [15]. The multilayered perceptron network belongs to the class of layered feed-forward nets with supervised learning. A multilayered neural network is made up of one or more hidden layers placed between the input and output layers, see fig. 1. Each layer consists of a number of nodes connected in the structure of a layered network. The typical architecture is fully interconnected, i.e. each node in a lower level is connected to every node in the higher level. Output units cannot receive signals directly from the input layer. During the training phase activation flows are only allowed in one direction, a feed-forward process, from the input layer to the output layer through the hidden layers. The input vector feeds each of the first layer nodes, the outputs of this layer feed into each of the second layer nodes and so on.
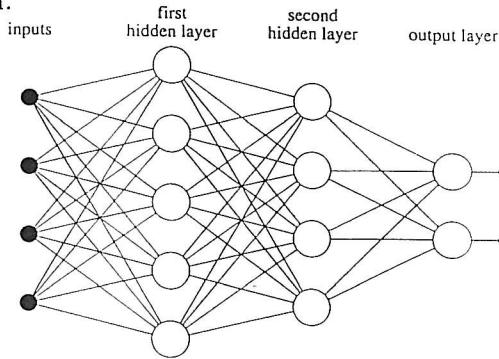

Fig. 1: Principle of a multilayer perceptron neural network.

Associated with each connection between node i and node j in the preceding layer $l - 1$ and following layer l is a numerical value $w_{lj,i}$ which is the strength or the weight of the connection. At the start of the training process these weights are initialized by random values. Signal pass through the network and the jth node in layer l computes its output according to

$$x_{lj} = f(\sum_{i=1}^{N_{l-1}} w_{lj,i}x_{l-1,i} + \theta_{lj}) \qquad (1)$$

for $j = 1, .., N_l$ and $l = 1, .., k$, where x_{lj} is the output of the jth node in the lth layer. θ_{lj} is a bias term or a threshold of the jth neuron in the lth layer. The kth layer is the output layer and the input layer must be labelled as layer zero. Thus N_0 and N_k refer to the numbers of network inputs and outputs, respectively. The function $f(\cdot)$ is called the node activation function and is assumed to be differentiable and to have a strictly positive first derivative. For the nodes in the hidden layers, the activation function is often chosen to be a so-called sigmoidal function

$$f(\beta) = \frac{1}{1 + e^{-\beta}} \qquad \beta > 0 \qquad (2)$$

The activation function for the nodes in the input and output layers are often chosen as linear.

During the training phase, representative examples of input-output patterns are presented to the network. Each presentation is followed by small adjustments of weights and thresholds if the computed output is not correct. If there is any systematical relationship between input and output and the training examples are representative of this, and if the network topology is properly chosen, then the trained network will often be able to generalize beyond learned examples. Generalization is a measure of how well the network performs on the actual problem once training is complete. It is usually tested by evaluating the performance of the network on new data outside the training set. Generalization is most heavily influenced by three parameters: the number of data samples, the complexity of the underlying problem and the network architecture. Currently, there are no reliable rules for determining the capacity of a feed-forward multilayer neural network. Generally, the capacity of a neural network is a function of the number of hidden layers, the number of processing units in each layer, and the pattern of connectivity between layers. However, it is shown in Cybenko [16] and Funahashi [17] that one hidden layer is sufficient to approximate all continuous functions.

2.2 Back-Propagation

The first stage of creating an artificial neural network to model an input-output system is to establish the appropriate values of the connection weights $w_{lj,i}$ and thresholds θ_{lj} by using a learning algorithm. A learning algorithm is a systematic procedure for adjusting the weights in the network to achieve a desired input/output relationship, i.e. supervised learning. The most popular and successful learning algorithm used to train multilayer neural networks is currently the Back-propagation routine, see e.g. Rumelhart [15]. The so-called Back-propagation algorithm employs a gradient descent search

technique for minimizing an error normally defined as the mean square difference between desired y_j and actual outputs $\hat{y}_j$. I.e. the error E is given as

$$E = 0.5 \sum_{j=1}^{N_k} (y_j - \hat{y}_j)^2 \qquad (3)$$

If the error is considered small enough, the weights and thresholds are not adjusted. If however, a significant error is obtained the weights and thresholds are adjusted in the negative gradient direction, so that the error criterion E is reduced. A typical weight $w_{lj,i}$, which could belong to any layer, is adjusted from its old value $w_{lj,i}^{old}$ to its new value $w_{lj,i}^{new}$ according to

$$w_{lj,i}^{new} = w_{lj,i}^{old} + \Delta w_{lj,i} \qquad (4)$$

where $\Delta w_{lj,i}$ is given by, see e.g. Billings [18]

$$\Delta w_{lj,i} = \eta \delta_{li} x_{l-1,i} \qquad (5)$$

δ_{li} is the error in the output of the ith node in layer l and η is termed a "learning rate". The error δ_{li} is not known a priori but must be constructed from the known errors δ_{ki} at the output layer. The errors are passed backwards through the net and a training algorithm uses the error to adjust the connection weights moving backwards from the output layer, layer by layer, hence the name "Back-propagation". In practice the "learning rate" η is chosen as large as possible (0.01-0.9) without leading to intolerable oscillations. To overcome this problem, a momentum term α is usually introduced into the update rule implying

$$w_{lj,i}^{new} = w_{lj,i}^{old} + \eta \delta_{li} x_{l-1,i} + \alpha \Delta w_{lj,i}^{old} \qquad (6)$$

The thresholds are adjusted in the same way as the weights. The process of computing the gradient and adjusting the weights and thresholds is repeated until a minimum of the error E (or a point sufficiently close to the minimum) is found. However it is generally true that the convergence of the Back-propagation algorithm is fairly slow. Attempts to speed learning include variations on simple gradient search, line search techniques and second order techniques, see e.g. Hertz et al.[4], Billings et al. [18] and Enevoldsen [19].

2.3 Use of Neural Networks for Damage Assessment

The problem of damage assessment on the basis of measured dynamic data is essentially a pattern recognition problem. Since artificial neural networks are proving to be an effective tool for pattern recognition the basic idea in a neural based damage assessment approach is to train a network with patterns of the changes in quantities describing the dynamic behaviour that occur due to a damage. This implies that each pattern represents the computed changes of e.g. the response spectrum, natural frequencies, mode shapes etc. due to a damage of a particular size at a particular location. The patterns of the quantities describing the dynamic behaviour are used as inputs and the damage location and size as outputs to train the neural network. Then the trained network subjected to measured patterns of the quantities describing the dynamic behaviour can be used to determine the location, size and of a damage. A hierarchical, two step approach can also be used. This implies that the patterns of the quantities describing the dynamic behaviour are used as inputs and the location of the crack is used as output in one network and size of the crack as output in an other network, see Kirkegaard et al. [10].

The training of a neural network with appropriate data containing the information about the cause and effect is a key requirement of a neural based damage assessment technique. This means that the first step is to establish the training sets which can be used to train a network in a way that the network can recognize the behaviour of the damaged as well as the undamaged structure from measured quantities. Therefore, ideally, the training sets should contain data of the undamaged as well as the damaged structure in various damage states. These data can be obtained by measurements, model tests or through numerical simulation, or through a combination of all three types of data. This possibility of using all obtained information, or only a part, in a neural network based damage assessment technique is a capability which is not available in traditional damage assessment techniques.

In order to verify how well a trained network has learned the training cases the trained network is tested by subjecting it to the training sets. The important generalization capability of a neural network damage assessment technique is tested by subjecting the trained network to data not included into the training sets. How well a trained network is to generalize depends on the adequacy of the selected network architecture and the information about the damage as well as undamaged structure included in the training sets.

3. EXAMPLE

In this example the proposed neural network approach for damage assessment is applied to a 20 high steel lattice structure, see fig. 2. The four chords K-frame test mast with a 0.9x0.9 m cross section was bolted with twelve bolts, three for each chord, to a concrete foundation block founded on chalk and covered by sand. The mast was constructed with welded connections. The eight lower diagonals were cut and provided with a bolted joint. Each bolted joint consists of 4 slice plates giving the possibility of simulating a 25, 50, 75 and 100 per cent reduction of the area of a diagonal. A damage was simulated by removing one or more splice plates in these bolted joints. Six different damage states (1,2,5,6,9,10) were considered. The damage state 1,2,5 and 6 correspond to a 100 per cent reduction of the sectional area of diagonal AB101, BC101, AB102 and BC102, respectively, see fig. 2. Damage states 9 and 10 correspond to a fifty per cent reduction of the sectional area of diagonal AB101 and AB102, respectively.

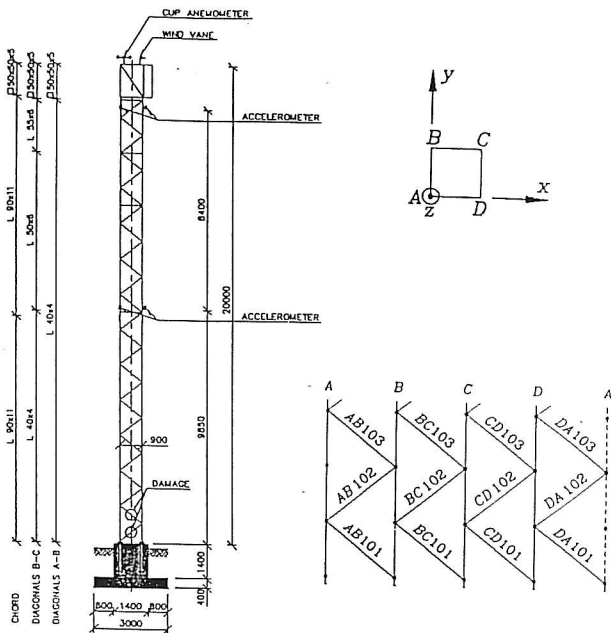Fig. 2 Elevation of mast and diagonals of the lower two sections of the mast.

The data acquisition and the analysis of the sampled data were performed with the MATLAB, see PC-MATLAB [20], based on program to Structural Time Domain Identification, STDI, see Kirkegaard et al. [21]. A throughout description of the test arrangement can be found in Kirkegaard et al. [22].
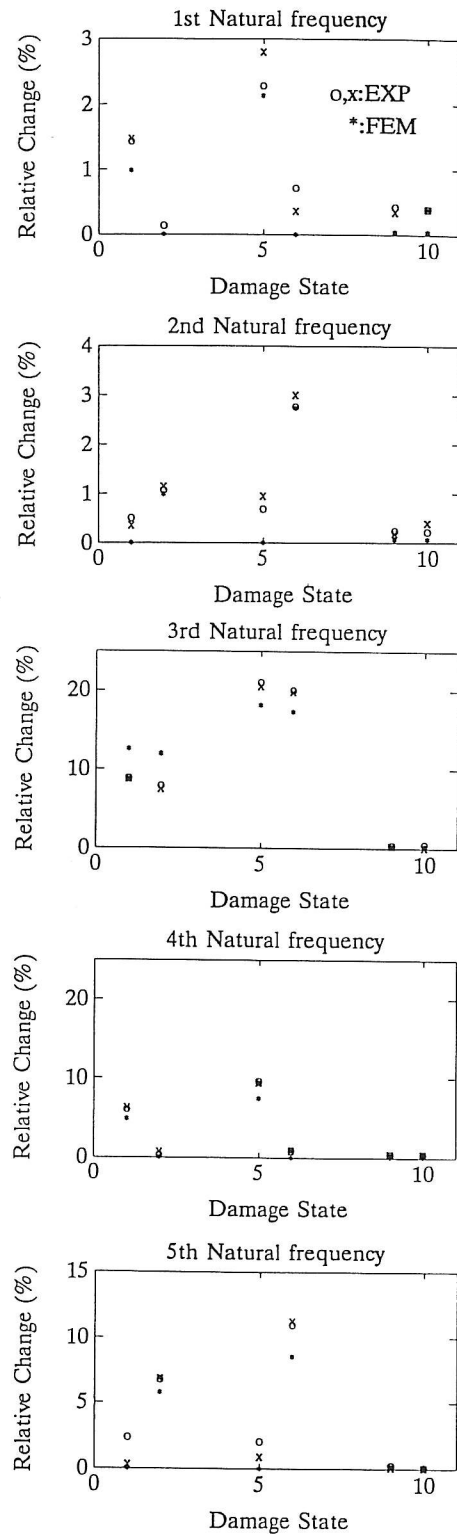
Fig. 3: Experimental versus finite-element results.

3.1 Simulated and Experimental Results

The applicability of the neural based damage assessment method is investigated by training a neural network with the relative changes of the natural frequencies of the 5 lowest modes. The natural bending frequencies no. 1 and no. 4, the natural bending frequencies no. 2 and no. 5 and the rotational natural frequency no. 3 corresponding to deflection parallel to the x-axis, deflection parallel to the y-axis and rotation, respectively. A relative change in a natural frequency is defined as the change in a natural frequency divided by the same natural frequency of the undamaged mast. The relative changes of the natural frequencies due to a damage were estimated by an FEM of the mast. Each diagonal was modelled by three elements where the element in the middle was used to simulate a damage. After the FEM was calibrated by using experimental data a damage was simulated by a reduction of the sectional area. This calibration was performed to secure that the FEM described the mast in the best possible way. The quality of the predictions from any method of damage assessment is critically dependent on the accuracy of the damage model, see e.g. Rytter [1].

In fig. 3 the experimental results are shown together with the finite-element results for the mast. Fig.3 shows the relative changes in the natural frequencies as a function of damage state. For each of the six damage states three values are shown. One value obtained by the FEM and two experimental values. These experimentally determined relative changes are estimated from measurements obtained for the undamaged and the damaged mast under the same environmental conditions. This is important since it is shown in Kirkegaard et al. [22] that the frequencies are sensitive to changes in environmental conditions.

In general, fig. 3 shows that there is a good agreement between theoretical predictions and experimental results.

3.2 Training and Testing of Neural Network

First a neural network was trained with simulated estimates of the relative changes of the lowest five natural frequencies. These changes were estimated for a 20, 40, 60, 80 and 100 per cent reduction of the sectional area of diagonal AB101, BC101, AB102 and BC102, respectively. Further, the relative changes of the frequencies also were estimated for the undamaged mast. This means that the input to the network was 21 training sets. By a trial-and-error approach it is found that a 4 layers neural network with 5 input nodes, 5 nodes in each of the two hidden layers and 4 output nodes gave the

network with smallest output error. Each output node corresponds to a damage in one of the diagonals AB101, BC101, AB102 and BC102, respectively. The value for a single diagonal adopts the value 1 when not damaged, the value 0 when totally damaged and 0.2 corresponds to a 80 per cent reduction of a sectional area etc. The input and output nodes were chosen as linear while the nodes used in the hidden layers were of the sigmoidal type.

The network was tested by subjecting the simulated input data corresponding to a 100 per cent reduction of the sectional area of the four diagonals AB101, BC101, AB102 and BC102, respectively, to the network. Next, the network was subjected to input data corresponding to 50 per cent reduction of the sectional areas of the two diagonals AB102 and BC102, respectively. I.e. data not included in the training sets. The results are given in table 1. It is seen that the neural network is capable of reproducing the location and size of a damage used in training (Damage state 1,2,5,6). Further, the table shows that the neural network is capable of making a generalization based on the training sets (Damage state 9,10).

Output Node No.	Damage State					
	1	2	5	6	9	10
1(AB101)	0.0	1.0	1.0	1.0	0.4	0.9
2(BC101)	1.0	0.0	1.0	1.0	1.1	1.1
3(AB102)	1.0	1.0	0.0	1.0	1.0	0.5
4(BC102)	1.0	1.0	1.0	0.0	0.9	1.0

Table 1: Results from network subjected to traning data and data not included in the trainig data.

Table 2 shows the outputs from the network subjected to experimental data. Since two experimental values are available for each damage state the average value is used.

Output Node No.	Damage State					
	1	2	5	6	9	10
1(AB101)	0.1	0.8	0.9	0.9	0.5	0.8
2(BC101)	0.8	0.1	0.8	1.0	0.7	0.4
3(AB102)	0.6	1.0	0.1	1.1	0.2	0.2
4(BC102)	0.9	0.9	0.9	0.0	0.9	1.1

Table 2: Results from network subjected to experimental data.

The results in table 2 show that it is possible to detect a damage corresponding to a removal of a diagonal (Damage state 1,2,5,6) by the neural network approach. It is also seen that a damage corresponding to 50 per cent reduction of the sectional area of a diagonal AB102 can be detected, but not quantified.

4. CONCLUSIONS

Results from an example with a steel mast demonstrate a diagnostic technique based on neural networks for detecting, locating and quantifying damages based on vibration measurements. The damage assessment technique relies on the measurements of small changes in natural frequencies and upon adequate theoretical prediction of these frequency changes. The results show that a neural network trained with simulated data is capable for detecting location of a damage, corresponding to a removal of a diagonal, in the steel lattice mast when the network is subjected to experimental data. The results also indicate that it is possible to detect a damage corresponding to a 50 per cent reduction of a diagonal but it is not possible to quantify the size of the damage.

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