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Efficiency and survivability analysis of a point-absorber wave energy converter using DualSPHysics

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Abstract

Smoothed Particle Hydrodynamics (SPH) method is used here to simulate a heaving point-absorber with a Power Take-Off system (PTO). The SPH-based code DualSPHysics is first validated with experimental data of regular waves interacting with the point-absorber. Comparison between the numerical and experimental heave displacement and velocity of the device show a good agreement for a given regular wave condition and different configurations of the PTO system. The validated numerical tool is then employed to investigate the efficiency of the proposed system. The efficiency, which is defined here as the ratio between the power absorbed by the point-absorber and its theoretical maximum, is obtained for different wave conditions and several arrangements of the PTO system. Finally, the effects of highly energetic sea states on the buoy are examined through alternative configurations of the initial system. A survivability study is carried out by computing the horizontal and vertical forces exerted by focused waves on the wave energy converter (WEC). The yield criterion is used to determine that submerging the heaving buoy at a certain depth is the most effective strategy to reduce the loads acting on the WEC and its structure, while keeping the WEC floating at still water level is the worst-case scenario.

Keywords: point-absorber, WEC, survivability, efficiency, CFD, SPH

1. Introduction

Wave energy is nowadays recognised as one of the renewable energy resources with the highest potential, availability, and predictability (Chongwei et al., 2014). However, the wave energy potential is still not fully exploited. Despite the efforts of the scientific community (Bozzi et al., 2018, Kamranzad and Hadadpour, 2020), an agreement about the proper type of Wave Energy Converters (WECs) has not been achieved yet. The wave devices are, in most cases, placed offshore, where wave energy potential is higher but where they are subjected to great forces. Eventual rogue waves arising from a random sea state are potentially dangerous for the device and need to be correctly characterised. This may be accomplished by means of single events with a specific crest height and an associated period, known as focused waves. Therefore, the WEC design needs to be based not only on the efficiency but also on the survivability of the devices, which is key to harness wave energy in a safe and cost-effective way. Many ingenious systems have been developed but only a few are generating electricity commercially (Drew et al., 2009). One of the most widespread devices are the point-absorbers, which typically consist of a floater whose oscillating motion, heaving and/or pitching, is converted into electricity by means of a Power Take-Off (PTO) system (Ahamed et al., 2020). They are non-directional devices that can absorb energy from all directions through their movement at/near the water surface. Their simplicity makes point-absorbers more resilient to extreme wave conditions than other wave energy devices.

Numerical modelling plays a fundamental role as a complementary tool for physical experiments during the design stage of WECs. It has become a game-changer in the wave energy industry thanks to the exponential growth of the computational resources, which makes possible to simulate large and complex systems at

46 reasonable computational runtime (Folley, 2016). On one hand, numerical methods allow reducing costs and
47 time when different configurations need to be evaluated. The data obtained from the simulations can be of great
48 help to determine design loads, stresses, or any other meaningful information, which is hard or even impossible
49 to evaluate during physical tests. On the other hand, numerical models purposely developed for efficiency
50 analysis of WECs may not be appropriate to evaluate their survivability. The numerical model should be able to
51 solve the interaction between incoming waves and floating structures, and to reproduce the behaviour of the
52 PTO systems in an accurate way. Several modelling approaches have been employed to analyse the
53 hydrodynamic response of WECs as shown in the following review papers: Li and Yu (2012); Folley et al.
54 (2012); Markel and Ringwood (2016); Penalba et al. (2017); Zabala et al. (2019); Davidson and Costello (2020).
55 However, only a few numerical pieces of research include the mechanical constraints of the PTO system.

56 Traditionally, the most widely used models to describe the response of a WEC under operational sea states are
57 based on potential flow theory (see e.g., Newman, 2018). They are either time or frequency domain models that
58 apply the boundary element method (BEM) to solve the frequency-dependent dynamics of the device. Many
59 works have assessed the performance of point-absorbers using potential flow theory, e.g. Beatty et al. (2015),
60 De Andrés et al. (2013), and Rahmati and Aggilis (2016). Nevertheless, potential flow-based codes, such as
61 WAMIT (Lee, 1995) or NEMOH (Babarit and Delhommeau, 2015), assume the fluid to be incompressible,
62 inviscid and irrotational, the motion of the device to have small amplitude, and the waves to be linear. These
63 assumptions are likely to be violated when a WEC is placed at sea, especially under energetic sea states.
64 Conversely, CFD (Computational Fluid Dynamics) methods are more time consuming and complex, but they
65 do not require any of the previous simplifications. They are based on the Navier-Stokes equations, which may
66 be solved following an Eulerian approach (mesh-based methods) or a Lagrangian approach (mesh-free methods).
67 The mesh-based methods have proved to be very robust since they have been developed for many years. In
68 particular, the finite volume method has been applied to a wide range of free-surface problems providing
69 accurate results. Power efficiency analysis of point-absorbers using these methods have been conducted by Yu
70 and Li (2013), Jin et al. (2018), and Reabroy et al. (2019), amongst others. The interaction of focused waves
71 with vertical cylinders has been studied by Westphalen et al. (2012) and Hu et al. (2016) using the mesh-based
72 codes STAR-CCM+ and OpenFOAM, respectively. Nevertheless, defining an appropriate mesh can be very
73 inefficient for complex systems with moving boundaries. On the other hand, meshless methods can be applied
74 to highly nonlinear problems with arbitrary and changing geometries, difficult to handle with mesh-based
75 methods.

76 Different meshless approaches have been developed in the last decades. One of the most popular methods is the
77 Smoothed Particle Hydrodynamics (SPH), which has reached the required maturity level to be used for
78 engineering purposes (Violeau and Rogers, 2016). The continuum fluid in SPH is treated as discrete *smoothed*
79 quantities at locations named *particles*. The physical quantities are computed at each *particle* as an interpolation
80 of the quantities of the surrounding particles using a weighted function (kernel) based on the distance between
81 particles and solving the Navier-Stokes equations. The SPH technique presents several advantages over mesh-
82 based methods to simulate free-surface flows since there is no special detection of that free surface. Large
83 deformations can be efficiently treated (there is no mesh distortion), and violent impacts of extreme waves with
84 fixed or fluid-driven objects can be easily tackled. In addition, rapidly moving complex geometries are handled
85 with SPH in a straightforward way, without problems related to mesh generation or updating at each time step.
86 There are several papers that show the robustness of SPH for coastal engineering applications, such as Gotoh
87 and Khayyer (2018), Khayyer et al. (2018), and González-Cao et al. (2018). With a focus on the WEC modelling,
88 the pioneering works of Rafiee et al. (2013) and Edge et al. (2014) presented the SPH simulation of oscillating
89 wave surge devices. Westphalen et al. (2014) compared the hydrodynamic response of a point-absorber obtained
90 with SPH and with a finite volume method, whilst Omidvar et al. (2013) and Yeylaghi et al. (2015) are the first
91 works to deal with the interaction between extreme waves and point-absorbers using SPH methods.

92 Among the different SPH codes, DualSPHysics software is considered one of the most efficient SPH solvers
93 (Crespo et al., 2015). DualSPHysics is open-source (www.dual.sphysics.org) and allows applying the SPH
94 method to real engineering problems. It can be executed not only on CPUs, but also on GPU (Graphics

95 Processing Unit) cards with powerful parallel computing that can be installed in a personal computer (Altomare
 96 et al., 2018). The DualSPHysics code has been applied in this work since it includes the coupling with the open-
 97 source multiphysics platform Project Chrono (Tasora et al., 2016), which is capable of simulating collisions and
 98 kinematic restrictions such as springs, hinges, pulleys, etc. In this manner, the coupling of DualSPHysics with
 99 Project Chrono allows the complex mechanisms of the PTO system to be reproduced within the same meshless
 100 framework. DualSPHysics has proven its capability to generate and propagate waves (Altomare et al., 2017;
 101 Domínguez et al., 2019a) and to simulate satisfactorily their interaction with WECs such as an Oscillating Water
 102 Column in Crespo et al. (2017, 2018) and an Oscillating Wave Surge Converter in Brito et al. (2020). The first
 103 work where DualSPHysics was employed to simulate a point-absorber device was presented in Tagliafierro et
 104 al. (2019). Other works, like Verbrugge et al. (2018, 2019), combined the capabilities of a fully nonlinear
 105 potential flow solver and DualSPHysics, allowing the simulation of large domains and, at the same time,
 106 accurate and detailed modelling of the interactions between waves and the WEC.

107 This research is focused on the simulation of a wave energy converter consisting of a cylindrical heaving-buoy
 108 attached to a PTO system, as described by Zang et al. (2018), who conducted experiments with a model scale of
 109 1:10. The PTO system is a direct-drive linear generator in which the rod connected to the buoy moves the
 110 alternator in the presence of a stationary magnetic field, inducing an electric current in the stator, according to
 111 Faraday's law of induction (Eriksson et al., 2005). The present manuscript includes a complete numerical study
 112 in terms of SPH modelling of a point-absorber converter since it contains: i) validation with experiments, ii)
 113 efficiency analysis and iii) survivability under extreme waves. This work is organised as follows: Section 1 is
 114 the introductory part and provides the state-of-the-art, Section 2 describes the DualSPHysics code, Section 3
 115 shows the validation comparing numerical results with experimental data using one regular wave condition,
 116 Section 4 includes an efficiency study simulating several conditions of regular waves, Section 5 presents the
 117 loads exerted onto the point-absorber under the action of focused waves considering different scenarios and,
 118 finally, conclusions are synthesised in Section 6.

119

120 2. Numerical model

121 The fundamental concept in the SPH methodology is to discretise the fluid into a set of particles, where the
 122 physical quantities (position, velocity, density, and pressure) are obtained as an interpolation of the
 123 corresponding quantities of the surrounding particles. The weighted contribution of those particles is obtained
 124 using a kernel function (W_{ab}) with an area of influence that is defined using a characteristic *smoothing length*
 125 (h). The quintic Wendland kernel (Wendland, 1995) is used in DualSPHysics and it is defined to vanish beyond
 126 $2h$. Note that particles are initially created with an interparticle distance, dp , which is used as a reference value
 127 to define the smoothing length using $h=2dp$.

128 The Navier-Stokes equations can be then written in a discrete SPH formalism using W_{ab} as the kernel function,
 129 which depends on the normalised distance between particle a and neighbouring b particles

$$130 \frac{d\mathbf{r}_a}{dt} = \mathbf{v}_a \quad (1)$$

$$132 \frac{d\mathbf{v}_a}{dt} = - \sum_b m_b \left(\frac{p_b + p_a}{\rho_b \cdot \rho_a} + \Pi_{ab} \right) \nabla_a W_{ab} + \mathbf{g} \quad (2)$$

$$134 \frac{d\rho_a}{dt} = \sum_b m_b \mathbf{v}_{ab} \nabla_a W_{ab} + 2\delta hc \sum_b (\rho_b - \rho_a) \frac{\mathbf{v}_{ab} \nabla_a W_{ab}}{r_{ab}^2} \frac{m_b}{\rho_b} \quad (3)$$

135 where t is the time, \mathbf{r} is the position, \mathbf{v} is the velocity, p is the pressure, ρ is the density, m is the mass, c is the
 136 numerical speed of sound, and \mathbf{g} is the gravitational acceleration. The artificial viscosity (Π_{ab}) proposed in
 137 Monaghan (1992) and the density diffusion term proposed by Fourtakas et al. (2020) (using $\delta=1$) are applied
 138 here.
 139

140 The previous equations allow computing the position, velocity, and density of each SPH particle. However, a
 141 new equation to compute pressure is required. In the DualSPHysics code, the fluid is treated as weakly
 142 compressible (WCSPH), so that an equation of state is used to calculate fluid pressure as a function of density,
 143 rather than solving a Poisson-like equation. Hence the system is closed by using the polytropic equation, Eq.
 144 (4), where the speed of sound has been adjusted to obtain a reasonable time step:

$$145 \quad p = \frac{c^2 \rho_0}{\gamma} \left[\left(\frac{\rho}{\rho_0} \right)^\gamma - 1 \right] \quad (4)$$

146 with $\gamma=7$ the polytropic constant (Ma, 2010), and $\rho_0=1000 \text{ kg m}^{-3}$, the reference density of the fluid.
 147

148 One of the most interesting capabilities of SPH models is the simulation of fluid-driven objects (Canelas et al.,
 149 2015). First, the net force on each individual particle of a floating object is computed as the summation of the
 150 contributions of all surrounding fluid particles (b). In this way, each floating particle q experiences a force per
 151 unit of mass \mathbf{f}_q given by:

$$152 \quad \mathbf{f}_q = \frac{d\mathbf{v}_q}{dt} = \sum_{b \in \text{fluid}} \frac{d\mathbf{v}_{qb}}{dt} \quad (5)$$

153 where the interactions between particles q and b are solved according to Eq. (2).

154 It is important to note that here the object is being considered as rigid, so the basic equations of rigid body
 155 dynamics are solved to obtain the motion of the floating object:

$$156 \quad M \frac{d\mathbf{V}}{dt} = \sum_{q \in \text{body}} m_q \mathbf{f}_q \quad (6)$$

$$157 \quad I \frac{d\boldsymbol{\Omega}}{dt} = \sum_{q \in \text{body}} m_q (\mathbf{r}_q - \mathbf{R}) \times \mathbf{f}_q \quad (7)$$

158 where M is the total mass of the object, I the moment of inertia, \mathbf{V} the velocity, $\boldsymbol{\Omega}$ the rotational velocity, \mathbf{R} the
 159 centre of mass, and m_q and \mathbf{r}_q are, respectively, the mass and position of each floating particle q . Equations (6)
 160 and (7) are integrated in time in order to obtain the values of \mathbf{V} and $\boldsymbol{\Omega}$ at the beginning of the next time step.
 161 Each particle that belongs to the object moves according to the velocity, \mathbf{v}_q , given by:

$$162 \quad \mathbf{v}_q = \mathbf{V} + \boldsymbol{\Omega} \times (\mathbf{r}_q - \mathbf{R}) \quad (8)$$

163 The accuracy of DualSPHysics to simulate fluid-driven objects under the action of regular waves was studied
 164 in Domínguez et al. (2019b), where the numerical results of nonlinear waves interacting with a freely floating
 165 box were compared with the experimental data from Ren et al. (2015). A good agreement was obtained for the
 166 motions of the box in terms of heave, surge, and pitch time series.

167 The capabilities of DualSPHysics are extended, thanks to the coupling with the multiphysics library Project
 168 Chrono (<https://projectchrono.org/>) that allows solving mechanical constraints applied on rigid bodies during the
 169 fluid-structure interaction. Among the different features that can be defined, springs and dampers are
 170 straightforward. A more complete description of the coupling between DualSPHysics and Chrono is presented
 171 in Canelas et al. (2018), which also provides validation of the features as implemented into the new framework.

172 The coupled DualSPHysics-Chrono code is employed in this work to simulate a heaving point-absorber whose
 173 PTO system is modelled as a linear damper:

$$174 \quad F_{PTO}(t) = b_{PTO} \cdot v_z(t) \quad (9)$$

175 where F_{PTO} represents the force exerted by the PTO system, b_{PTO} its damping coefficient and v_z the heave
 176 velocity.

177

178 3. Validation

179 The WEC under study is the point-absorber described in Zang et al. (2018). It is composed of a heaving buoy
 180 connected to a PTO system at its bottom. More specifically, the PTO system is a direct-drive linear generator,
 181 whose effects on the dynamics of the WEC were simulated in the experimental campaign thanks to various air-
 182 dampers (Zang et al., 2018) while, mathematically, they can be modelled simply as a linear damper (Eriksson
 183 et al., 2005), as shown in Eq. (9). The heaving buoy is a cylinder 0.22 m high with a diameter (D) of 0.50 m
 184 and density 500 kg/m^3 , which results in a mass of 21.6 kg. Therefore, the draft of the buoy at equilibrium is
 185 half its height (0.11 m).

186 Zang et al. (2018) conducted several experiments to study the response of the WEC under regular waves for
 187 different values of the damping coefficient b_{PTO} (Eq. 9). The physical tests conducted with regular waves of
 188 wave height $H=0.16$ m, period $T=1.5$ s, water depth $d=1.10$ m, and an associated wavelength $L=3.40$ m are
 189 considered here to validate the numerical code. Three values of the damping coefficient, $b_{PTO}=0, 240, 1100$
 190 Ns/m, are used in the validation to take the effect of the PTO into account.

191 A numerical tank (Fig. 1) is designed to mimic the physical flume. The width of the numerical domain is reduced
 192 to twice the buoy diameter ($2D$), lateral periodic boundary conditions are applied to minimise the effects of
 193 radiated waves from the lateral walls. A piston, whose movement generates the desired wave, is located on the
 194 left of the tank (as seen in Fig. 1). The buoy is located at one wavelength (L) from the piston. Wave dissipation
 195 is guaranteed on the right side of the tank (Fig. 1) thanks to the combination of a dissipative beach with a slope
 196 of $\alpha=1:2$, starting at $L/4$ from the buoy, and a numerical damping applied along the longitudinal axis (x) of the
 197 beach.

198 The numerical damping system consists in gradually reducing the velocity of the fluid particles at each time step
 199 according to their location, as suggested in Altomare et al. (2017). In this manner, the velocity of a fluid particle
 200 a located within the damping zone is reduced from its initial velocity $\mathbf{v}_{a,0}$ to its final velocity \mathbf{v}_a according to
 201 $f_r(x_a, \Delta t)$:

$$202 \quad \mathbf{v}_a = \mathbf{v}_{a,0} \cdot f_r(x_a, \Delta t) \quad (10)$$

203 where x_a is the longitudinal position of the particle, Δt is the duration of the last time step and $f_r(x_a, \Delta t)$ is the
 204 reduction function, which employs a quadratic decay:

$$205 \quad f_r(x_a, \Delta t) = 1 - \Delta t \cdot \beta \cdot \left(\frac{x_a - x_0}{x_1 - x_0} \right)^2 \quad (11)$$

206 being x_0 and x_1 the initial and final position of the damping zone along the x -axis, respectively, and β a coefficient
 207 that is fixed at $\beta = 10$ for all simulations.

208 The overall absorption capabilities of the beach with numerical damping are quantified by means of the reflection
 209 coefficient, K_R , which is calculated here using the Healy method (Eagleson and Dean, 1966):

$$210 \quad K_R = \frac{H_{max} - H_{min}}{H_{max} + H_{min}} \quad (12)$$

211 where H_{max} and H_{min} are, respectively, the maximum and minimum numerical wave height. In this way, the
 212 reflection coefficient of the numerical tank shown in Fig. 1, for the regular wave previously described, is lower
 213 than 2%, which means that over 98% of the incident wave energy is being dissipated.

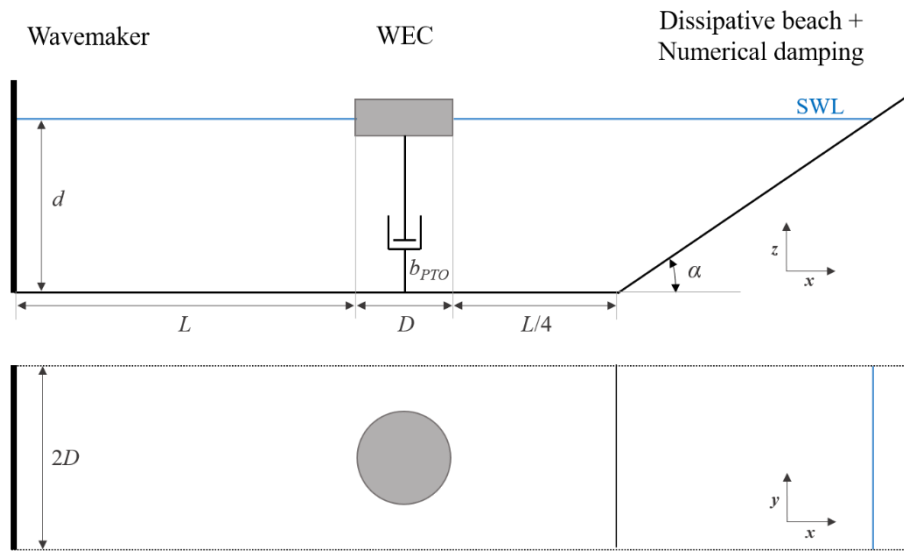


Fig. 1. Numerical tank to simulate the interaction of the WEC under regular waves.

214

215

216

217 The resolution is given by the initial interparticle distance dp , which is employed to create the particles involved
 218 in the simulation. Altomare et al. (2017) and Rota-Roselli et al. (2018) proved that using around ten particles
 219 per wave height ($H/dp=10$) provides a reasonable compromise between accuracy and computational time. In
 220 this validation, two different resolutions are employed: $dp=0.02$ m and $dp=0.01$ m corresponding to $H/dp=8$ and
 221 $H/dp=16$, respectively. The total number of particles is approximately 800,000 for the simulations with $dp=0.02$
 222 m, and 6,500,000 with finer resolution $dp=0.01$ m, as presented in Table 1. The table also shows the
 223 computational time required to simulate fifteen seconds of physical time using a GeForce RTX 2080 Ti GPU
 224 card. It can be observed that the lower the dp , the higher the number of particles and, therefore, longer runtimes
 225 are needed.

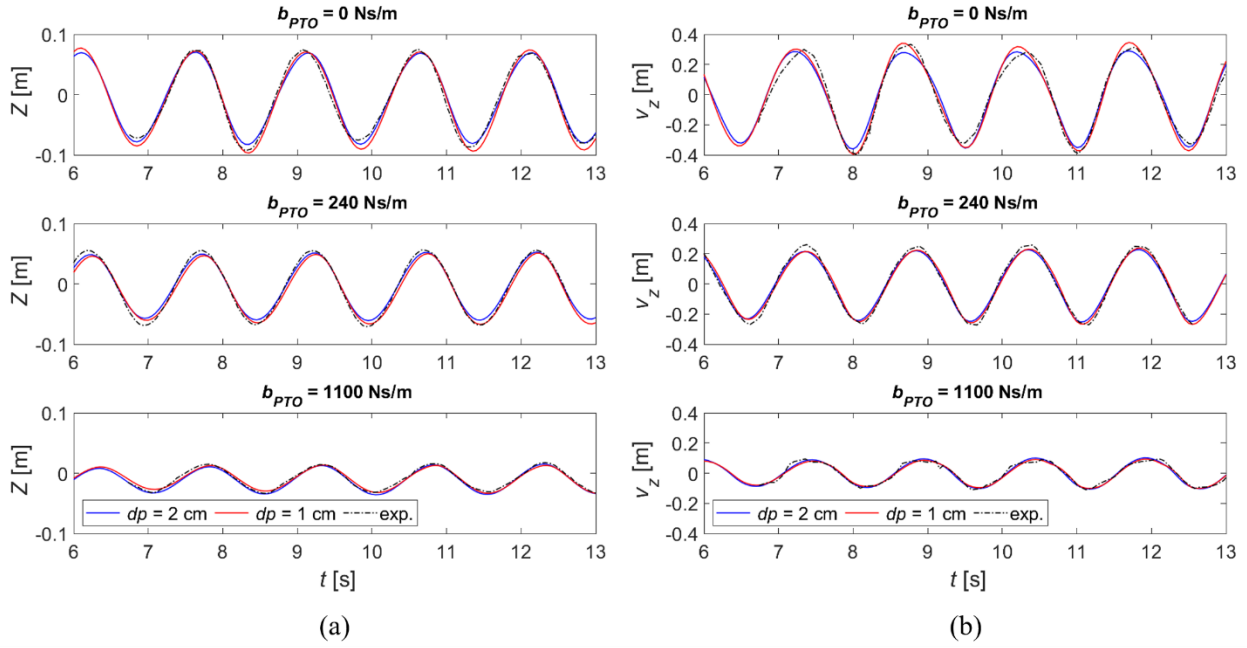
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Table 1. Number of particles and GPU runtimes (GeForce RTX 2080 Ti).

b_{PTO} [Ns/m]	dp [m]	Particles	Runtime [h]
0	0.02	$0.8 \cdot 10^6$	1.9
	0.01	$6.7 \cdot 10^6$	19.1
240	0.02	$0.8 \cdot 10^6$	2.3
	0.01	$6.7 \cdot 10^6$	33.5
1100	0.02	$0.8 \cdot 10^6$	2.2
	0.01	$6.7 \cdot 10^6$	33.5

227

228 Fig. 2 compares the experimental and numerical time series of heave displacement and velocity of the device
 229 for the three values of b_{PTO} . Qualitatively, the agreement for the three cases is satisfactory in terms of both
 230 amplitude and phase. Fig. 2 shows that when $b_{PTO}=0$ Ns/m, the heave displacement amplitude is maximum, and
 231 its value is comparable to the incident wave height ($H=0.16$ m) since the buoy is freely floating on the surface.
 232 As it is expected, the higher the damping coefficient of the PTO system, the lower the amplitude of the heave
 233 displacement and velocity, reaching a reduction of over 2/3 when comparing $b_{PTO}=0$ Ns/m with $b_{PTO}=1100$ Ns/m.
 234 Fig. 2 also proves that, regardless of the value of b_{PTO} , the period of the heave movement is always equal to the
 235 wave period ($T=1.5$ s) and the phase lag between heave displacement and velocity is of $\pi/2$ rad. On the other
 236 hand, looking closely at Fig. 2 it can be noted that varying b_{PTO} causes a slight phase shift in the time series of
 237 both Z and v_z . This shift was analysed in detail by Zang et al. (2018).



238

239 **Fig. 2.** Numerical and experimental time series of heave displacement (a), and velocity (b) of the point-absorber for b_{PTO}
 240 = 0, 240 and 1100 Ns/m.

241

242 To quantify the accuracy of the results, the index of agreement d_1 defined by Willmott et al. (1985) is used here
 243 as non-dimensional error estimator:

$$244 \quad d_1 = 1 - \frac{\sum_{n=1}^N |C_n - E_n|}{\sum_{n=1}^N (|C_n - \bar{E}| + |E_n - \bar{E}|)} \quad (13)$$

245 where N is the total number of records of the studied variable, C and E are, respectively, the values obtained
 246 numerically and experimentally (or theoretically when possible) and the overbar represents the average. The
 247 index of agreement is bounded between 0 and 1, where 1 means that the numerical and experimental (or
 248 theoretical) time series are coincident.

249 Table 2 collects the different values of d_1 for the time series of Z and v_z shown in Fig. 2, i.e. for three values of
 250 b_{PTO} and two values of dp . The index of agreement ranges from 0.91 to 0.94 in all cases, which implies a very
 251 high level of coincidence between the numerical and experimental time series. Table 2 also shows that the
 252 improvement in accuracy obtained when using the finest resolution ($dp=0.01$ m) is barely noticeable.
 253 Consequently, the lower resolution ($dp=0.02$ m) was chosen for all simulations hereinafter since the
 254 computational time increases tenfold when using $dp=0.01$ m (see Table 1). This proves the capability of
 255 DualSPHysics to reproduce with accuracy the response of a point-absorber under these regular waves for
 256 different configurations of the PTO system at very reasonable computational times.

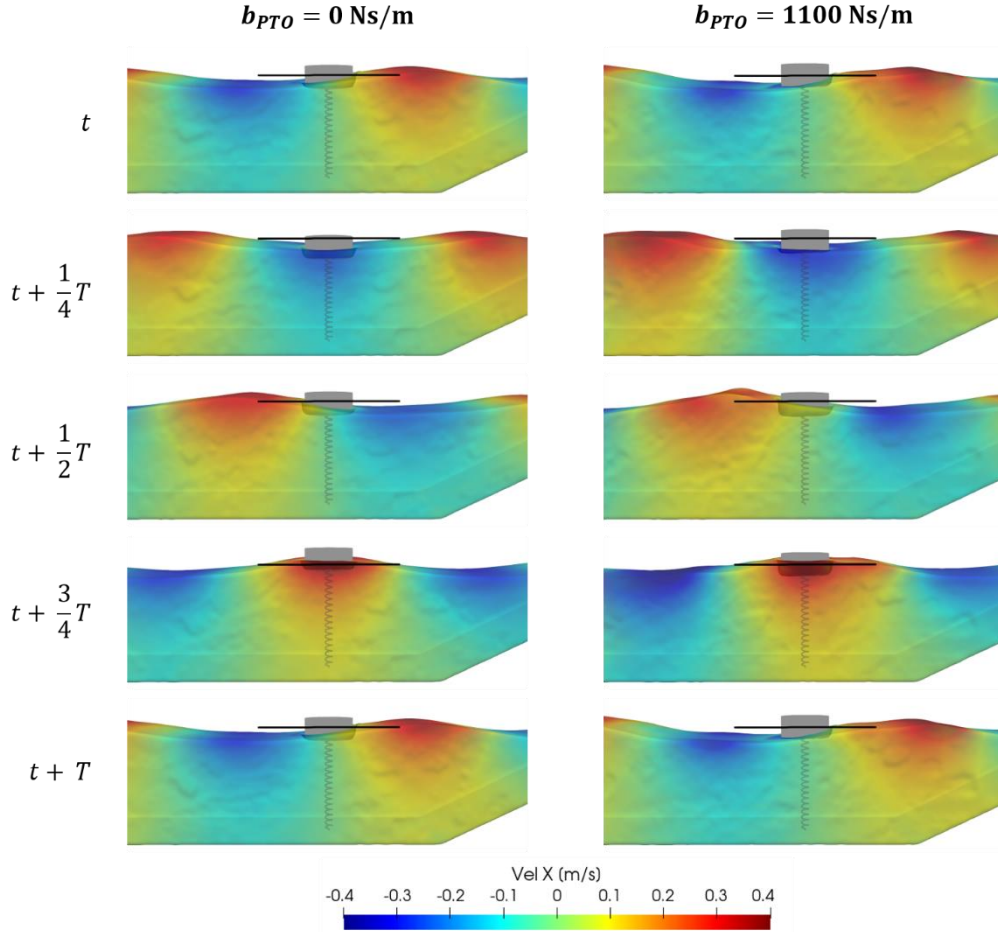
257

Table 2. Index of agreement of the heave displacement and velocity for each simulation.

b_{PTO} [Ns/m]	dp [m]	d_1	
		Z	v_z
0	0.02	0.93	0.92
	0.01	0.94	0.93
240	0.02	0.94	0.91
	0.01	0.93	0.91
1100	0.02	0.91	0.91
	0.01	0.91	0.91

258

259 Five different instants of the simulations with $b_{PTO}=0$ Ns/m and $b_{PTO}=1100$ Ns/m ($d_p=0.02$ m) are shown in Fig.
 260 3. Note that the instants cover one complete wave period (in fact, the first and last instants are coincident). The
 261 colourmap represents the velocity of the fluid particles in the longitudinal axis. Minimum values are observed
 262 at wave troughs and maximum values at the crests. The black solid line represents the initial still water level; it
 263 emphasises the differences in the motion of the buoy when varying the damping coefficient of the PTO system.
 264 For the frames at $1/4T$ and $3/4T$, it can be easily observed that the heave amplitude is significantly lower using
 265 $b_{PTO}=1100$ Ns/m than using $b_{PTO}=0$ Ns/m.



266
 267 **Fig. 3.** Different instants of the simulation using DualSPHysics with $b_{PTO}=0$ and 1100 Ns/m.
 268

269 4. Efficiency

270 The previous section has proved the ability of the DualSPHysics numerical code to provide an accurate response
 271 of the point-absorber under regular waves of $T=1.50$ s, $H=0.16$ m, and $d=1.10$ m, and for three different values
 272 of the damping coefficient. In this section, a study of the evolution of the absorbed power and the system
 273 efficiency with the wave frequency, considering the effect of different configurations of the PTO, is performed.
 274 Regular waves with the same wave height and depth, but with periods ranging from 0.97 s to 4.40 s are simulated
 275 for several values of the PTO damping coefficient.

276 First, it is important to define the wave power per meter of width of the wave front, denoted as J and obtained
 277 as indicated in Falnes (2002):

$$278 \quad J = \frac{1}{16} \rho g H^2 \frac{\omega}{k} \left[1 + \frac{2kd}{\sinh(2kd)} \right] \quad (14)$$

279 where $k=2\pi/L$ is the wavenumber and $\omega=2\pi/T$ the angular wave frequency.

280 The absorbed power by the point-absorber under study is analysed by comparison with J in order to obtain the
 281 efficiency for different regular wave conditions. Table 3 contains the characteristics of the regular waves that
 282 are simulated, namely period (T), angular frequency (ω), wavelength (L), Ursell number (Ur) and wave power
 283 per meter of width of the wave front (J).

284 **Table 3.** Wave conditions simulated in the efficiency analysis.

T [s]	ω [rad/s]	L [m]	Ur	J [W/m]
0.97	6.48	1.47	0.26	23.8
1.00	6.28	1.56	0.29	24.56
1.05	5.98	1.72	0.36	25.84
1.09	5.76	1.85	0.41	26.92
1.15	5.46	2.06	0.51	28.58
1.20	5.24	2.24	0.60	30.04
1.30	4.83	2.61	0.82	33.22
1.50	4.19	3.40	1.39	40.46
1.70	3.70	4.19	2.11	48.14
1.90	3.31	4.98	2.98	55.36
2.10	2.99	5.75	3.97	61.74
2.40	2.62	6.87	5.68	69.56
2.80	2.24	8.33	8.34	77.28
3.30	1.90	10.10	12.27	83.84
4.40	1.43	14.15	23.23	91.86

285
 286 In Fig. 4, the Le Méhauté abacus (Le Méhauté, 1976) shows the most appropriate theory to model each regular
 287 wave. All of them fall within the Stokes' theory zone of the abacus: waves with period equal and lower than
 288 1.70 s are of third order, being the rest second order Stokes' waves. Nevertheless, all of them are generated
 289 according to the second order theory implemented in DualSPHysics (Madsen, 1971). This implies the
 290 assumption that the third order terms of the Stokes' perturbative series are negligible with respect to the second
 291 order terms. Furthermore, to guarantee that the second order terms do not cause spurious crests and troughs that
 292 may prevent the wave free-surface profile from having a constant form in time, it is required that the second
 293 order terms are significantly lower than the first order terms of the Stokes' expansion. The Ursell number (Ursell,
 294 1953), mathematically defined as $Ur=HL^2/d^3$, provides the relation between the amplitudes of the second and
 295 first order terms of the free-surface elevation. According to the theory developed by Madsen (1971) and
 296 implemented in DualSPHysics, the wave free-surface profile is constant if $Ur<8\pi^2/3$. Table 3 shows that the
 297 Ursell number increases with the wave period but it is always below the required threshold.

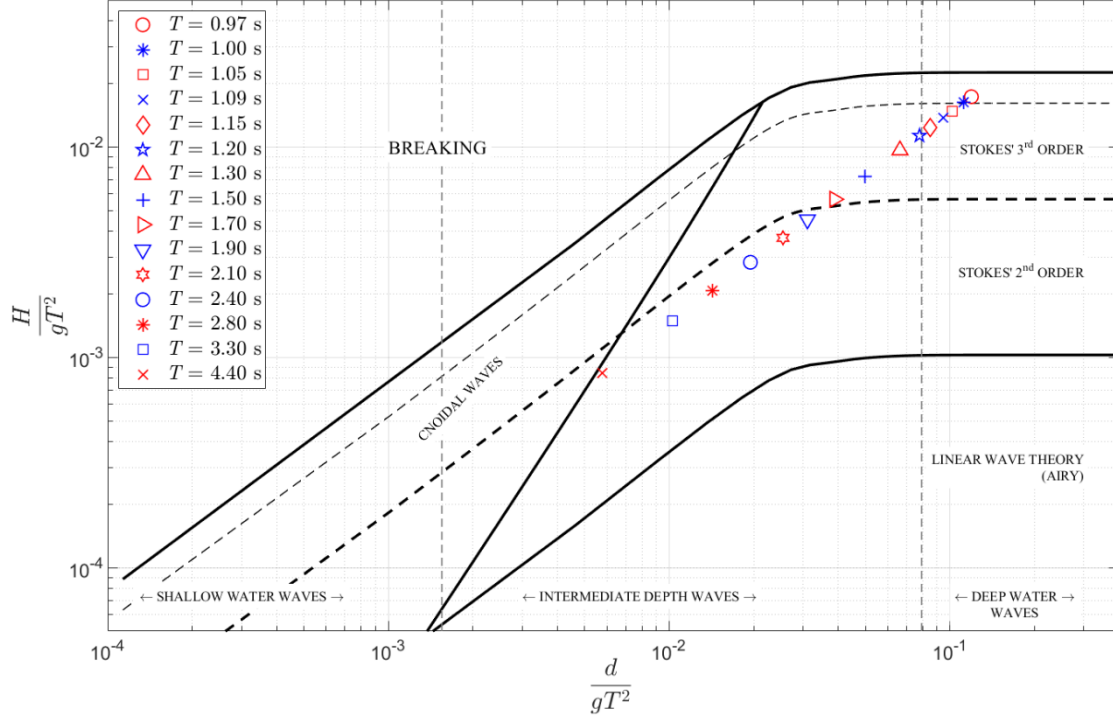


Fig. 4. Regular wave conditions as classified in Le Méhauté abacus.

298

299

300

301 The numerical tank used to perform the efficiency analysis is the same as used before (Fig. 1). The width and
 302 still water depth are the same used for the validation case. However, since the buoy is located one wavelength
 303 away from the piston and one quarter of wavelength away from the beginning of the beach, the total length of
 304 the domain now varies in accordance with the wavelength of each condition. The slope of the dissipative beach,
 305 α , is chosen for each wave condition such that, in combination with the numerical damping previously explained,
 306 it yields a reflection coefficient always lower than 6%. Specifically, $\alpha=1:2$ is used for regular waves with $T=1.5$
 307 s and lower; $\alpha=1:4$ for $T=1.7, 1.9, 2.1$ and 2.4 s; $\alpha=1:4$ for $T=2.8$ and 3.3 s; and $\alpha=1:12$ for $T=4.4$ s.

308 The power absorbed by the device and its energetic efficiency are computed as explained below. The instant
 309 wave power captured by the WEC is proportional to the damping force of the PTO system, given by Eq. (9),
 310 following:

$$311 \quad P_{abs}(t) = F_{PTO}(t) \cdot v_z(t) = b_{PTO} \cdot v_z^2(t) \quad (15)$$

312 The integral of Eq. (15) over a time period provides the averaged power absorbed by the device:

$$313 \quad P_a = \frac{1}{T} \int_{t_0}^{t_0+T} P_{abs}(t) dt \quad (16)$$

314 Taking a constant time interval Δt , the averaged absorbed power can be further approximated by a discrete
 315 summation:

$$316 \quad P_a = \frac{1}{N} \sum_{n=1}^N P_{abs}(t_0 + n\Delta t) \quad (17)$$

317 where $T=N \cdot \Delta t$, being N the total number of records taken in a period.

318 Budal and Falnes (1975), Evans (1976), and Newman (1976) independently derived the expression for the
 319 theoretical maximum absorbed power by an axisymmetric body oscillating only in heave, such as the point-
 320 absorber considered in this paper, as:

$$321 \quad P_{a,max} = \frac{J}{k} \quad (18)$$

322 where J denotes the wave power per meter of width of the wave front (Eq. 14) and k is the wavenumber.

323 The efficiency of the wave energy converter can be characterised as the ratio between the power absorbed by
324 the device and its theoretical maximum:

$$325 \quad \frac{P_a}{P_{a,max}} = 2\pi \frac{P_a}{JL} \quad (19)$$

326 The capture width (CW) and capture width ratio (CWR) are two parameters often used when performing an
327 efficiency analysis. The former represents the width of the wave front that is being completely absorbed by the
328 device, whereas the latter represents the ratio between the absorbed power and the available power contained in
329 the wave interacting with the device, which is defined as $P_w=JD$ (being D the buoy diameter). They can be
330 mathematically described as:

$$331 \quad CW = \frac{P_a}{J} \quad (20)$$

$$332 \quad CWR = \frac{P_a}{P_w} \quad (21)$$

333 Capture width has units of meters, hence CWR is a dimensionless parameter given by CW over the device
334 dimension perpendicular to wave propagation, in this case the buoy diameter D . Their maximum values can be
335 obtained from Eq. (18). Therefore, the energetic efficiency can also be characterised using the ratio CW/CW_{max}
336 or CWR/CWR_{max} since:

$$337 \quad \frac{CWR}{CWR_{max}} = \frac{CW}{CW_{max}} = \frac{P_a}{P_{a,max}} = 2\pi \frac{P_a}{JL} \quad (22)$$

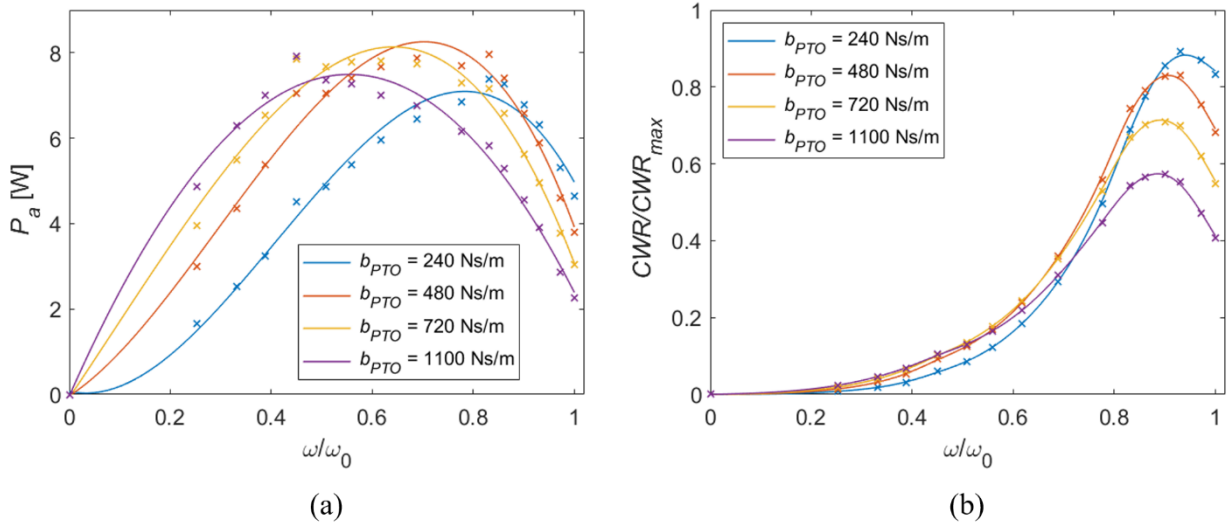
338 The response of the heaving point-absorber is highly frequency-dependent, being the energy conversion more
339 important near the resonance condition. When the WEC is operating at resonance, its heaving velocity and the
340 excitation force are in phase. The excitation force is made up of the force due to the non-perturbed incoming
341 wave acting on the WEC (Froude-Krylov force) and the force due to the diffraction of the flow bypassing the
342 buoy. As shown in Falnes (2002), the resonance condition is automatically satisfied when the wave frequency
343 matches the natural frequency of the device, which is given by:

$$344 \quad \omega_0 = \sqrt{\frac{\rho g A_{wet}}{M + m_{add}(\omega)}} \quad (23)$$

345 where A_{wet} is the wetted surface (cross-section of the cylinder), M is the mass of the buoy, and m_{add} is the added
346 mass. The added mass term is due to the radiated waves emitted by the oscillating buoy, and it varies with the
347 wave frequency, which implies that the natural frequency is frequency-dependent as well. The open-source
348 solver NEMOH (Babarit and Delhommeau, 2015) is used to obtain the added mass. NEMOH is a boundary
349 element method (BEM) code that solves the radiation-diffraction problem assuming linear waves and neglecting
350 viscosity. Note that the calculation of the natural frequency is only used here to define the non-dimensional
351 variable ω/ω_0 , which allows identifying whether the point-absorber is operating near its resonance condition.
352 Therefore, the simplifications made to obtain the natural frequency have no effect on the calculus of the absorbed
353 power, since this is obtained from the heave velocity time series computed with DualSPHysics, which simulates
354 with accuracy non-linear waves and does include viscous forces.

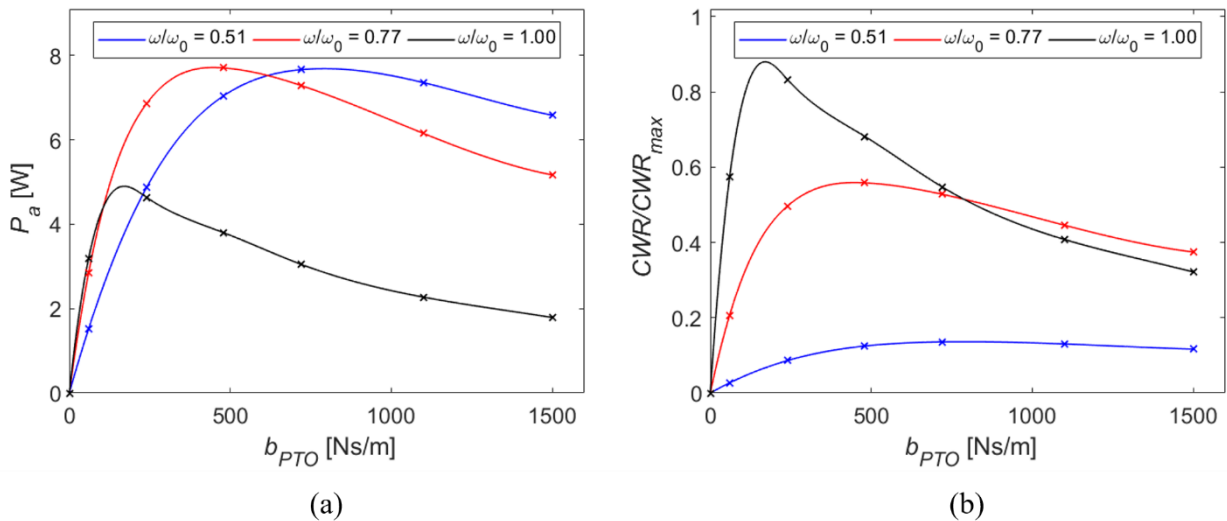
355 Fig. 5 shows the evolution of the absorbed power and the energetic efficiency as functions of the ratio ω/ω_0 for
356 different values of b_{PTO} , namely 240, 480, 720, and 1100 Ns/m. When ω tends to zero or infinity, so does the
357 ratio ω/ω_0 , since ω_0 takes finite (and non-zero) values for all ω , and the absorbed power and energetic efficiency
358 tend to be zero. Both the absorbed power and the energetic efficiency reach a maximum between $\omega/\omega_0=0$ and
359 $\omega/\omega_0=1$, respectively. However, the wave frequency that maximises P_a is different from the one that maximises
360 the energetic efficiency. This is due to the fact that the wave power per meter of width of the wave front, Eq.

361 (14), decreases when the wave frequency increases, as shown in Table 3. Fig. 5(a) shows that the maximum
 362 absorbed power occurs at around $\omega/\omega_0=0.5$ for $b_{PTO}=1100$ Ns/m, and around $\omega/\omega_0=0.8$ for $b_{PTO}=240$ Ns/m. The
 363 peak of P_a tends to appear at frequencies close to the natural frequency as the damping coefficient of the PTO
 364 decreases. A similar behaviour is observed in Fig. 5(b) for the energetic efficiency (defined here as
 365 CWR/CWR_{max}) but, in this case, the peak of efficiency takes place at frequencies slightly lower than ω_0 for all
 366 the values of b_{PTO} . Note as well that the maximum energetic efficiency is higher as b_{PTO} decreases, being around
 367 0.6 for $b_{PTO}=1100$ Ns/m and close to 0.9 for $b_{PTO}=240$ Ns/m.



368
 369 **Fig. 5.** Variations of absorbed power (a) and CWR/CWR_{max} (b) with the frequency of regular waves for different values of
 370 b_{PTO} .

371
 372 Fig. 6 shows the dependence on the damping coefficient of the PTO of the absorbed power (P_a) and energetic
 373 efficiency (CWR/CWR_{max}) for three different wave frequencies, namely $\omega/\omega_0=0.51$, 0.77 and 1.00. When $b_{PTO}=0$
 374 Ns/m, the PTO system is disconnected and the wave energy is not being harvested, as indicated mathematically
 375 in Eq. (15). On the other hand, when b_{PTO} tends to infinity the device response is overdamped and the absorbed
 376 power, thus the efficiency, tends asymptotically to zero. There is a value of b_{PTO} for each wave condition that
 377 maximises both P_a and CWR/CWR_{max} . When the device is operating at resonance ($\omega/\omega_0=1$), the maximum
 378 efficiency is achieved when b_{PTO} is between 60 and 240 Ns/m. Comparing the three different wave conditions
 379 shown in Fig. 6, it is clear that the further away from resonance, the higher the optimum value of b_{PTO} and the
 380 less steep the curves, i.e. the range of b_{PTO} for which P_a and energetic efficiency are near their maximum is
 381 wider.



382

383

Fig. 6. Variations of absorbed power (a) and CWR/CWR_{max} (b) with b_{PTO} for different values of ω/ω_0 .

384

385 5. Survivability

386 The final numerical analysis with the point-absorber under study in this work is related to survivability. As
 387 previously introduced, the use of an SPH-based code presents several advantages, which make the simulation
 388 of violent impacts between sea waves and floating devices easy and straightforward. In this section, the loads
 389 acting on the device under an extreme wave condition are obtained numerically with DualSPHysics. Different
 390 survival strategies are defined, considering the effects of submerging the device and simulating the WEC fixed
 391 or oscillating. A simplified structure is assumed to show a general methodology that may be followed to design
 392 the structure for a point-absorber.

393

394

5.1. Extreme wave description

395 Puertos del Estado (www.puertos.es) provides measures of the sea-state under extreme weather conditions in
 396 the northern coast of Spain. The survivability of the WEC is analysed at a location in the north coast of Spain 4
 397 km offshore from the Port of Gijón, where the water depth is 54 m. A directional buoy owned by Puertos del
 398 Estado provides the irregular extreme sea-state at this location from data recorded from March 2004 to January
 399 2017. A storm is defined as a situation during which the significant wave height H_s (mean wave height of the
 400 highest third of the records) exceeds a predefined threshold, following the Peak Over Threshold method. The
 401 irregular sea-state of each storm is characterised by the maximum H_s in a five-day period and its associated peak
 402 period, T_p , is obtained from an empirical equation based on a least-squares fitting. Given a desired lifetime of
 403 the device L_{WEC} , and a limit state which has an associated exceedance probability P_L , the design wave height H_d
 404 of the irregular extreme sea-state at the specified location can be obtained as explained below. The exceedance
 405 probability P_L is the probability that the design wave height H_d is exceeded during the lifetime L_{WEC} and is given
 406 by:

$$407 \quad P_L(H_d) = 1 - (1 - P_{ann}(H_d))^{L_{WEC}} \quad (24)$$

408 where $P_{ann}(H_d)$ is the probability that H_d is exceeded in a year, defined as

$$409 \quad P_{ann}(H_d) = 1 - \exp\left(-\lambda(1 - F_w(H_d))\right) \quad (25)$$

410 being λ the average number of storms in a year and F_w the Weibull distribution (Weibull, 1951) of exceedance
 411 of wave height, given by

$$412 \quad F_w(H_d) = 1 - \exp\left(-\left(\frac{H_d - \alpha_w}{\beta_w}\right)^{\gamma_w}\right) \quad (26)$$

413 The parameters α_w , β_w and γ_w define the specific Weibull distribution and are provided by Puertos del Estado,
 414 along with λ . Considering a lifetime L_{WEC} of 22 years and an exceedance probability $P_L=0.53$, corresponding to
 415 the Damage Limitation limit state, a design wave height of $H_d=0.985$ m (after 1:10 Froude scaling) is obtained
 416 from Eqs. (24) – (26). The corresponding peak period, T_p , is calculated from the design wave height by means
 417 of the empirical equation provided by Puertos del Estado, obtaining a value of $T_p=5.30$ s, calculated at 1:10
 418 model scale.

419 These design wave height and peak period define the irregular extreme sea-state at a specific location for the
 420 Damage Limitation limit state of a device with a lifetime of 22 years. A complete statistic representation of a
 421 real sea state consists of an irregular wave train of at least 300 waves (Boccotti, 2004). The importance of the
 422 time series duration in wave-structures interactions has been highlighted by other authors (e.g. Romano et al.,
 423 2015). In practice, 1000 waves are employed to represent real sea states, when reproduced experimentally.
 424 Numerical models based on full Navier-Stokes equations, either mesh-based or meshless, must often cope with
 425 huge computational costs associated with such long test durations, especially for 3-D modelling. Therefore,

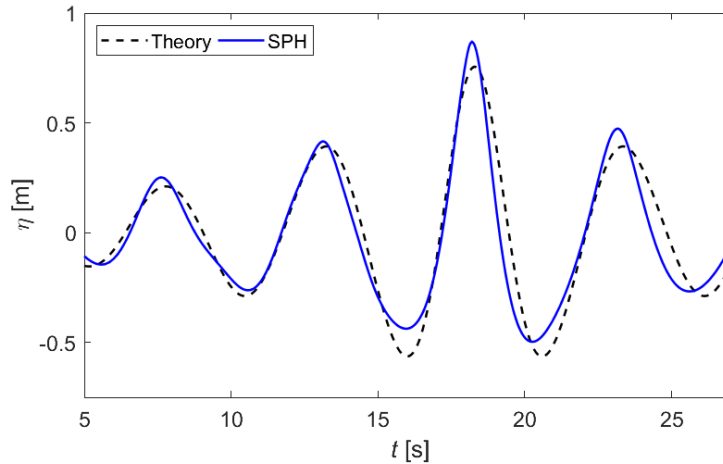
426 instead of a full sea state, a focused wave group is simulated. To account for the possibility of a sporadic freak
 427 wave of wave height significantly higher than H_d within this sea-state, a focused wave is defined as follows: a
 428 1000-wave train is used to build the Rayleigh distribution of the wave height and the one with only 3%
 429 probability to be exceeded is selected as the focused wave height, being in this case $H_f=1.31$ m.

430 In the present work, a unidirectional crest-focused wave, defined according to the so-called NewWave method
 431 (Whittaker, 2017) is employed. The NewWave linear theory developed by Tromans et al. (1991) defines the
 432 free-surface elevation $\eta(x,t)$, which is related to the Fourier Transform of the sea state power density spectrum
 433 $S(\omega)$, as a linear superposition of N wave modes

$$434 \quad \eta(x,t) = \frac{A_{cr}}{\sigma^2} \sum_{n=1}^N S(\omega_n) \cos(k_n(x - x_f) - \omega_n(t - t_f)) \Delta\omega \quad (27)$$

435 being $\sigma^2 = \sum S(\omega_n) \Delta\omega$ the variance of the discrete irregular sea state, ω_n and k_n the angular frequency and
 436 wavenumber of each n -mode, and x_f and t_f the position and time, respectively, at which the free-surface elevation
 437 reaches its maximum, $\eta(x_f, t_f) = A_{cr}$, i.e. where and when the wave train *focuses*. Whittaker (2017) noted that
 438 whenever a focused wave group is generated by a wavemaker that moves according to the NewWave linear
 439 theory spurious waves arise. To prevent this, the second-order wave generation theory proposed by Madsen
 440 (1971) is used here. Correction for bound-long waves is neglected in the present application.

441 The generation and propagation of the focused wave at a desired focus location is validated by running a 2-D
 442 simulation without the WEC. The focused wave is generated using $H_f=1.31$ m, $T_p=5.30$ s and $d=5.40$ m (obtained
 443 after the 1:10 Froude scaling of the sea depth). The free-surface elevation measured numerically with
 444 DualSPHysics at $x_f=15.00$ m is compared with the second-order analytical solution given by Madsen (1971) in
 445 Fig. 7. The crest-focused wave reaches the focus location, where the mid-point of the device will be placed, at
 446 $t_f=18.30$ s. The matching between the numerical and theoretical free-surface elevation is quantified by means of
 447 the index of agreement defined in Section 3. By applying Eq. (13) to the time series of η shown in Fig. 7, a value
 448 of $d_I=0.86$ is obtained, which validates the generation and propagation of the focused wave with DualSPHysics.



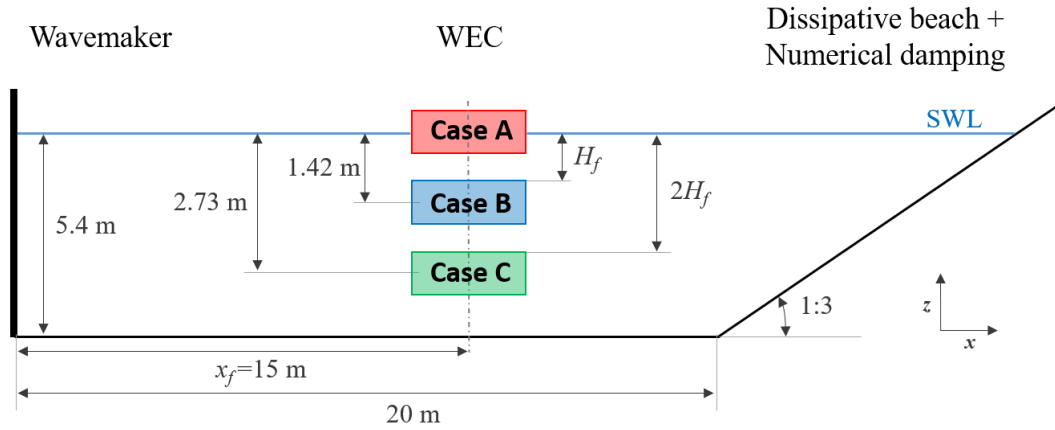
449
 450 **Fig. 7.** Numerical and theoretical time series of the free-surface elevation at x_f .

451

452 5.2. Numerical tank and setup of the cases

453 Fig. 8 depicts a lateral view of the 3-D numerical tank employed for the simulations hereinafter. As in the
 454 previous cases, the tank width is twice the diameter of the buoy, and periodic boundary conditions are applied
 455 to the lateral walls. Nevertheless, the still water level is now at $d=5.40$ m above the sea bottom, and the mid-
 456 point of the device is placed 15.00 m away from the wavemaker. In addition, a different anti-reflective beach
 457 has to be arranged at the end of the tank because of the high energetic content of the wave to be absorbed. To
 458 guarantee an adequate wave dissipation, a 1:3 steep beach beginning at 5.00 m from the axis of the buoy acts
 459 together with a numerical damping, as defined in Eqs. (10) and (11). The wavemaker is a piston-type one that

460 moves according to a steering function, which guarantees that the focused wave described in the previous section
 461 focuses at x_f (Fig. 7).



462

463

Fig. 8. Numerical tank configuration for the different cases in the survivability study.

464

465 Fig. 8 also illustrates the different depths to submerge the device, being $H_f=1.31$ m as explained in the previous
 466 section. Six different cases are considered in the survivability study. In all of them the PTO system is temporarily
 467 switched off to avoid an eventual damage to the most expensive and fragile part of the WEC, which means
 468 $b_{PTO}=0$ Ns/m. The loads exerted on the device are measured for the different scenarios that differ about the
 469 degrees of freedom of motion and the location of the device. Table 4 helps to define the different scenarios,
 470 where they are named with an upper-case letter and a number. The letter refers to the different levels of
 471 submergence, denoting A, B, and C that the centre of mass of the device is at still water level (SWL), submerged
 472 1.42 m below SWL, or submerged 2.73 m below SWL, respectively. The number that follows refers to the
 473 degrees of freedom of the device, being 1 only-heave motion and 2 all degrees of freedom restricted, i.e. the
 474 device is completely fixed.

475

Table 4. Setup of the different cases.

Case	Initial depth [m]	Fixed / Heaving
A1	0 (SWL)	Heaving
A2	0 (SWL)	Fixed
B1	1.42	Heaving
B2	1.42	Fixed
C1	2.73	Heaving
C2	2.73	Fixed

476

477 When the buoy is fully submerged, the difference between the upward buoyancy force (equal to the weight of
 478 the displaced fluid) and the downward force due to its own weight results in a vertical net force F_{net} . Since the
 479 density of the buoy is half the density of the fluid, the net force is positive (upward) and equal to the weight of
 480 the buoy: $F_{net}=212$ N. In the cases B1 and C1, the device is fully submerged and heaving around the desired
 481 depth, thus it is necessary to have a downward force that balances the upward net force in still water.
 482 Numerically, it can be modelled as an elastic force (F_s) using:

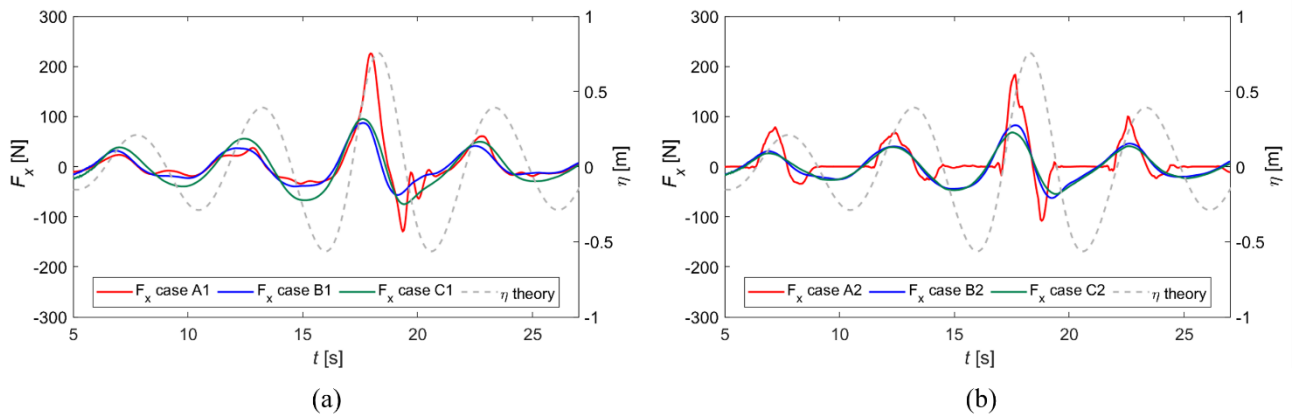
$$483 \quad F_s(t) = -k_s(l(t) - l_{eq}) \quad (28)$$

484 such that $F_s(t=0)=-F_{net}$ and that the spring length $l(t)$ is longer than the equilibrium length, l_{eq} , during the
 485 simulation to guarantee that the spring force direction remains unchanged. Setting the spring stiffness to $k_s=321$
 486 N/m, these requirements are satisfied, and the buoy is able to oscillate at the desired depth.

487

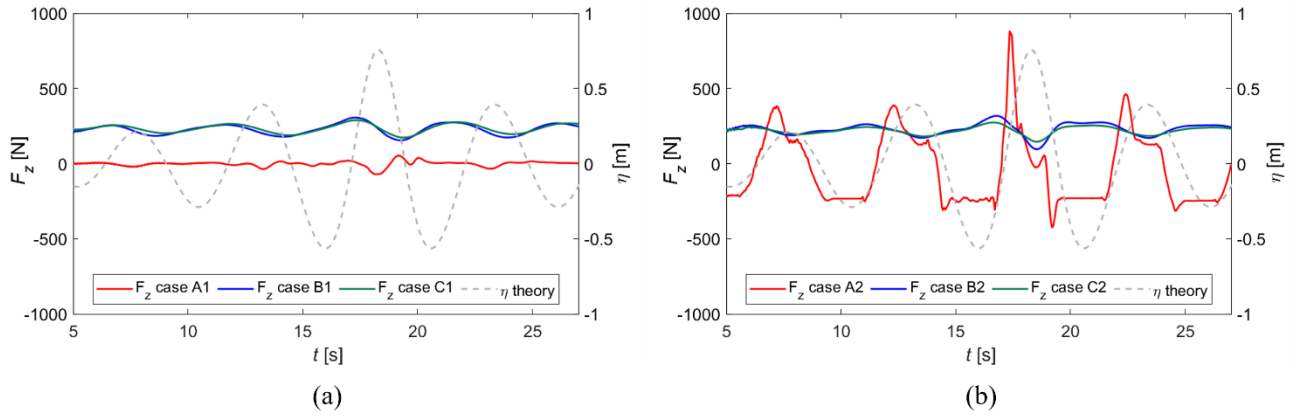
489 The focused wave presented in Section 5.1 is simulated for each scenario described in Table 4 using the
 490 numerical tank shown in Fig. 8. The forces acting on the device in each case are calculated using the post-
 491 processing tools of DualSPHysics. Figs. 9 and 10 show the time series of the forces in the x (longitudinal
 492 direction) and z (vertical direction) axis, respectively, along with the theoretical time series of the free-surface
 493 elevation at x_f in the secondary axis. For the sake of clarity, the results are split into two plots in both figures,
 494 corresponding to the cases where heave motion is allowed (a) and where the device remains fixed (b). Note that,
 495 since the focused wave is unidirectional (along the x -axis) and the geometry of the buoy is axially symmetric,
 496 the force acting in the y -axis is not taken into account.

497 As shown in Fig. 9, the time series of the force in the x -direction, F_x , follows the trend of the free-surface
 498 elevation, η . The maximum values of the horizontal force take place approximately during the peaks of the
 499 elevation time series. Fully submerging the buoy significantly reduces the maximum amplitude of F_x , since it is
 500 lower for cases B and C than for cases A. This difference in the behaviour of F_x with the submergence is due to
 501 the variation of the longitudinal acceleration of the fluid in the vertical direction. Comparing the results of F_x
 502 for the heaving and fixed devices initially placed at the same depth, the magnitude of F_x is lower when the device
 503 is fixed. However, the effect of holding the device fixed is minimized significantly when the WEC is completely
 504 submerged.



505
 506 **Fig. 9.** Time series of the forces in the x -direction (F_x) acting on the heaving (a) and fixed (b) device for each case.

507
 508 Fig. 10 shows that the forces in the z -direction, F_z , oscillate around zero when the device is initially at SWL and
 509 around the value of the vertical net force ($F_{net}=212$ N) when it is fully submerged, since the density of the floater
 510 is lower than the density of the water. Although a slightly lower amplitude of F_z is observed for case C1, the
 511 values of the vertical force are very similar for the cases when the device is completely submerged (cases B1,
 512 B2, C1, C2), regardless of whether it remains fixed or it oscillates. However, comparing the results of F_z for the
 513 heaving and fixed device initially semi-submerged (cases A1 and A2, respectively), a great difference can be
 514 observed in Fig. 10. As a matter of fact, configuration A1 minimises the vertical force, while configuration A2
 515 maximises it.



516

517 **Fig. 10.** Time series of the forces in the z -direction (F_z) acting on the heaving (a) and fixed (b) device for each case.

518

519 In absence of any stronger physical phenomenon, the behaviour of F_z is driven by the vertical acceleration of
 520 the fluid particles during wave propagation. This acceleration is in antiphase with the wave free-surface
 521 elevation, so that F_z will be in antiphase with η as well. Different situations can be found in Fig. 10. Case A1
 522 (where the WEC is moving at SWL) and cases B2 and C2 (where the WEC is fixed at a certain depth) follow
 523 the general behaviour mentioned before, i.e., F_z is in antiphase with η . However, in cases B1 and C1 (where the
 524 WEC is submerged and heaving), the spring force, needed to keep the device oscillating at the given depth,
 525 slightly shifts F_z , being consequently in phase with the heave motion.

526 The atypical behaviour of the forces observed for case A2 (fixed device at SWL) deserves a more detailed
 527 explanation. Fig. 7 showed that the absolute maximum and minimum values of the free-surface elevation are
 528 clearly higher than the height of the buoy. Therefore, when the device is fixed at SWL, the focused wave crest
 529 leads to a huge and sudden overtopping, whereas the troughs cause the free surface to be below the bottom of
 530 the cylinder. In this way, the forces acting on the WEC increase suddenly during the crest of the focused wave.
 531 On the other hand, the only force acting on the device during the troughs is its own weight, which explains the
 532 interval of time observed in Figs. 9 and 10 during which F_x and F_z are constant, specifically at $F_x=0$ N and
 533 $F_z=212$ N. It is also worth noting that there is an instant, after the wave crest has passed the buoy and before the
 534 next trough arrives, in which the device is also bearing the weight of the overtopping water that remains on its
 535 top surface, leading to the negative peaks of F_z .

536 The analysis of the forces alone does not clearly determine the best and worst-case scenario. If only forces in
 537 the x -axis are considered, case A1 would seem to be the most harmful to the structure. However, case A1 would
 538 be the least harmful when only vertical forces are considered. Thus, a criterion that takes into account both
 539 contributions is needed.

540 The structure considered in the present paper is a simplification of the one depicted in Zang et al. (2018), which
 541 assumes that the buoy is connected to the seabed by means of a clamped rod of circular cross-section. In this
 542 manner, it is possible to characterise the effects of the wave field on the buoy and its structure by performing an
 543 elastic verification based on the yield criterion. The Designers' Guide to EN 1993-1-1 Eurocode 3 defines the
 544 yield criterion for a critical point of a steel cross-section in the following general way:

$$545 \left(\frac{\sigma_x}{f_y/\gamma_{M0}} \right)^2 + \left(\frac{\sigma_z}{f_y/\gamma_{M0}} \right)^2 - \left(\frac{\sigma_x}{f_y/\gamma_{M0}} \right) \cdot \left(\frac{\sigma_z}{f_y/\gamma_{M0}} \right) + 3 \cdot \left(\frac{\tau}{f_y/\gamma_{M0}} \right)^2 \leq 1 \quad (29)$$

546 where σ_x is the longitudinal local stress, σ_z is the transverse local stress, τ is the local shear stress, f_y is the yield
 547 stress of the material and γ_{M0} is the partial factor, which is taken as 1. Since the structure considered here is a
 548 slender rod of circular cross-section, the transverse and shear stresses are negligible compared with the
 549 longitudinal stress. Thus, the yield criterion in the present application is simply given by:

$$\left(\frac{\sigma_x}{f_y}\right)^2 \leq 1 \quad (30)$$

where the longitudinal local stress is defined as:

$$\sigma_x = \frac{F_z}{A_{rod}} + \frac{F_x l_{arm}}{W_{rod}} \quad (31)$$

being $A_{rod}=\pi D_{rod}^2/4$ the cross-section area, $W_{rod}=\pi D_{rod}^3/32$ the elastic section modulus, D_{rod} the diameter of the rod and l_{arm} the lever arm (distance between the point of application of the forces in the floater and the base of the rod). A value of the yield criterion (Eq. 30) higher than 1 indicates a failure of the structure under the load produced by the event considered in the survivability analysis. Eq. (31) shows that the elastic verification considers the contribution of both F_x and F_z . Nevertheless, since $l_{arm}\gg D_{rod}$ and therefore $W_{rod}/l_{arm}\ll A_{rod}$, its behaviour is dominated by the term containing F_x .

The time series of the yield criterion for each scenario are obtained assuming a rod made of S235 steel ($f_y=235$ MPa) and for different values of D_{rod} . The maximum value for each case is presented in Table 5. If the diameter of the rod is 40 mm and the buoy is heaving at SWL (case A1), the maximum value of the yield criterion is very close to 1 and therefore, the structure of the WEC could collapse under the extreme event considered here. To avoid this, three strategies are studied: i) fixing the buoy, ii) submerging the buoy, and iii) increasing the rod diameter of the structure. Table 5 shows that when the device is initially placed at SWL, restraining all its movements reduces by approximately one third the value of the yield criterion. Submerging the buoy 1.42 m below SWL (cases B1 and B2) reduces over thirteen times the maximum yield criterion, which proves that the common practice of submerging the device is highly effective. If the initial depth of submergence is increased from 1.42 to 2.73 m below SWL (cases C1 and C2), the maximum yield criterion is approximately halved, which is, in fact, a very slight reduction compared with the one obtained between cases A and B. The elastic verification can also be satisfied by increasing the diameter of the rod. However, an increase of 50% in the rod diameter (from $D_{rod}=40$ mm to $D_{rod}=60$ mm) is needed in order to achieve values of the yield criterion similar to those obtained when fully submerging the buoy.

Table 5. Maximum values of yield criterion for each case.

D_{rod}	Case A1	Case A2	Case B1	Case B2	Case C1	Case C2
40 mm	0.989	0.666	0.068	0.051	0.037	0.016
50 mm	0.259	0.175	0.018	0.013	0.010	0.004
60 mm	0.087	0.059	0.006	0.004	0.003	0.001

The most effective strategy to reduce the wave-induced effects caused by an extreme event on the system is to submerge the device such that the top surface of the buoy is initially H_f below SWL (cases B1 and B2). Increasing the initial depth of immersion (cases C1 and C2) would require an extra economic cost very difficult to justify, since the associated reduction of the yield criterion is minimum. Fixing the device (case B2) reduces slightly the maximum yield criterion with respect to the heaving device (case B1), thus the costs and reliability of the mechanical systems needed in each case should be considered when making that choice.

6. Conclusions

The hydrodynamic response of a point-absorber under regular waves can be accurately obtained with DualSPHysics. The numerical results for different configurations of the PTO system match satisfactorily the experimental results for a given regular wave condition. Once validated, it has been shown that DualSPHysics provides a unique framework to study numerically two key aspects in the design of a WEC: efficiency and survivability under eventual extreme wave conditions.

588 The power captured by the point-absorber as well as its energetic efficiency have been obtained from the time
589 series of the device motion for a wide range of regular waves, and for several values of the damping coefficient
590 b_{PTO} . It has been shown that when the WEC operates near its resonance condition, the efficiency is maximised.
591 However, the wave frequency at which the absorbed power reaches its maximum depends on the value of b_{PTO} :
592 it approaches the natural frequency (resonance condition) as b_{PTO} decreases. The analysis has also proven that
593 there is a certain configuration of the PTO system that maximises both the absorbed power and the efficiency
594 for each wave condition. In particular, the optimum b_{PTO} value is here between 60 and 240 Ns/m when the point-
595 absorber is operating close to resonance and, it can be also observed that, the further away from this condition
596 the higher the optimum value of b_{PTO} .

597 The survivability analysis has been conducted by means of a focused wave, whose characteristics are defined
598 from the design spectrum corresponding to a certain limit state and lifetime of a device, placed at a specific
599 location. DualSPHysics has been used to generate and propagate the desired focused wave, and the forces acting
600 on the WEC were numerically computed. The yield criterion quantifies the effect of the loads exerted by the
601 extreme waves on the highly-simplified structure of the WEC for each scenario. It was shown that fully
602 submerging the device when an extreme event occurs is more effective than fixing the device or increasing the
603 size of the structure. Results for the two different depths of submergence show only a slight improvement when
604 submerging the device significantly deeper. This indicates the existence of an optimum depth of submergence.
605 However, its calculation would require a more extensive analysis as well as considering economic factors and
606 its environmental impact.

607

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617

618 **Nomenclature**

619 a, b : generic fluid particles
620 A_{cr} : maximum free-surface elevation of the focused wave (m)
621 A_{rod} : cross-section area of the rod (m²)
622 A_{wet} : wetted surface (m²)
623 b_{PTO} : damping coefficient of the PTO system (N·s/m)
624 c : numerical speed of sound (m/s)
625 C : numerically obtained value of a generic variable
626 d : depth (m)
627 d_I : index of agreement
628 D : diameter (m)
629 dp : initial interparticle distance (m)
630 D_{rod} : rod diameter (m)
631 E : experimental or theoretically obtained value of a generic variable
632 f : force per unit of mass (m/s²)
633 f_y : yield stress of the material (Pa)

634 F_{net} : vertical net force (N)

635 F_{PTO} : force exerted by the PTO system (N)

636 F_s : spring force (N)

637 F_w : Weibull distribution of exceedance of wave height

638 F_x : force in the x -direction (N)

639 F_z : force in the z -direction (N)

640 g : gravitational acceleration (m/s^2)

641 h : smoothing length (m)

642 H : wave height (m)

643 H_d : design wave height (m)

644 H_f : focused wave height (m)

645 H_s : significant wave height (m)

646 I : moment of inertia of the floating object ($kg \cdot m^2$)

647 J : wave power per meter of width of the wave front (J/m)

648 k : wavenumber (rad/m)

649 k_s : spring stiffness (N/m)

650 K_R : reflection coefficient

651 l : spring length (m)

652 L : wavelength (m)

653 l_{arm} : lever arm (m)

654 l_{eq} : equilibrium length (m)

655 L_{WEC} : lifetime of the WEC (years)

656 m : mass (kg)

657 M : mass of the floating object (kg)

658 m_{add} : added mass (kg)

659 p : pressure (Pa)

660 P_a : averaged power captured by the device (J)

661 $P_{a,max}$: theoretical maximum absorbed power by the device (J)

662 P_{abs} : instant wave power captured by the device (J)

663 P_{ann} : annual exceedance probability

664 P_L : exceedance probability

665 P_w : available wave power contained within the width of the device (J)

666 q : generic floating particle

667 r : position (m)

668 R : the centre of mass of the floating object (m)

669 S : sea state power density spectrum ($m^2 \cdot s$)

670 t : time (s)

671 T : wave period (s)

672 t_f : time when the focused wave reaches its maximum free-surface elevation (m)

673 T_p : peak period (s)

674 Ur : Ursell number

675 v : velocity (m/s)

676 V : linear velocity of the floating object (m/s)

677 $v_{a,0}$: initial velocity of fluid particle a (m/s)

678 v_z : heave velocity (m/s)

679 x_0 : initial longitudinal position of the numerical damping zone (m)

680 x_l : final longitudinal position of the numerical damping zone (m)

681 x_a : longitudinal position of fluid particle a (m)

682 x_f : position at which the focused wave reaches its maximum free-surface elevation (m)

683 x, y, z : Cartesian coordinates (m)

684 W : kernel function

685 W_{rod} : elastic section modulus (m^3)
686 Z : heave displacement (m)
687
688 *Greek letters*
689 α : beach slope
690 β : reduction function coefficient
691 α_w, β_w and γ_w : Weibull distribution parameters
692 γ : polytropic constant
693 γ_{M0} : partial factor of the cross-section
694 η : free-surface elevation (m)
695 λ : average number of storms in a year
696 Π : artificial viscosity ($m^5/kg \cdot s^2$)
697 ρ : density (kg/m^3)
698 ρ_0 : reference density (kg/m^3)
699 σ^2 : variance of the discrete irregular sea state (m^2)
700 σ_x : longitudinal local stress (Pa)
701 σ_z : transverse local stress (Pa)
702 τ : local shear stress (Pa)
703 Ω : rotational velocity of the floating object (s^{-1})
704 ω : the angular wave frequency (rad/s)
705 ω_0 : natural frequency (rad/s)
706

707 *Acronyms*

708 BEM: Boundary Element Method
709 CFD: Computational Fluid Dynamics
710 CW: Capture Width
711 CWR: Capture Width Ratio
712 PTO: Take-Off system
713 SPH: Smoothed Particle Hydrodynamics
714 SWL: Still Water Level
715 WCSPH: Weakly Compressible Smoothed Particle Hydrodynamics
716 WEC: Wave Energy Converter
717

718

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