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MATHEMATICAL REASONING AND SELF REGULATED LEARNING ACCORDING TO STUDENT'S COGNITIVE STAGE Gunawan¹, Ambar Prawoto², Utari Sumarmo³ 1SMK Ponpes Abu Manshur, Jalan Nyi Gede Cangkring Kabupaten Cirebon, Jawa Barat, Indonesia 2SMPS 2 Almuhajirin, Jalan Ipik Ganda Manah Purwakarta, Jawa Barat, Indonesia 3IKIP Siliwangi, Jalan Terusan Jendral Sudirman Cimahi, Jawa Barat, Indonesia 40526 gunawantujuh7@gmail.com¹, ambarprawoto34@gmail.com², utari.sumarmo@gmail.com³ Received: XXXXX X, XXXX; Accepted: XXXXX X, XXXX
Abstrak This study was a descriptive survey having a goal to examine attainment of student's mathematical reasoning (MR) and self regulated learning(SRL) according to student's cognitive stage. The survey implicate 36 eleventh grade students of 17...

years old, test of logical thinking (TOLT), an essay MR test,a SRL scale. By using TOLT, the survey investigated many students with 17 years old had not reached formal cognitive stage, namely 19 % students at formal stage, 25 % students at transition stage, and rest 56% students at concrete stage.

In addition, survey invented that entirely students obtained MR at very low grade level, and according to student's cognitive stage, formal students obtained higher grade MR than the grade of transision students and concrete students. Even if, those grades were still at low and very low level. Either entirely or based on student's cognitive stage there were no different grades on student's SRL and those grade were fairly good level.

SRL at fairly good grade level, transision stage students attained MR and SRL at medium grade Other finding, there was medium association between cognitive stage and MR, but therewere no association between cognitive stage and MR, and SRL and between MR and SRL. In general, these findings were, that in normal condition formal

cognitive stage will reach by students in 12 -13 years old, or in 13-14 years old, even in specific condition in 19 – 20 years old; and that formal students possess higher abilities than concrete students on completing HOTS tasks such as MR tasks which needed formal operational thinking. Keywords: cognitive stage, TOLT, mathematical reasoning, self regulated learning How to Cite: Gunawan., Prawoto, Ambar., & Sumarmo, Utari.

(2019). **Mathematical Reasoning and Self Regulated Learning** According to Student's Cognitive Stage. JIML, X (X), XX-XX. _ _ INTRODUCTION To examine student's cognitive stage, our discourse will relate tightly to the well-known theory that was Piaget's theory (Sumarmo, 1987) of cognitive child development.

IN the beginning, some readers believed that student's cognitive development is determined by biological age, such as by knowing student's age a reader we know student's cognitive stage directly. This opinion was serious inaccuracy. Basically, Inhelder and Piaget (Sumarmo, 1987) by using conscientious observation and in depth interview, they identified student's reasoning abilities on various reasoning tasks. Then they classified **kinds of reasoning** which able and not **able to do** by each groups of children from infant up to adult.

Based on student's ways of reasoning, then Inhelder and Piaget (Sumarmo, 1987) then categorized them into five main cognitive stages, namely: sensory-motor operational stage (infant-2 years old), pre-concrete operational stage (2 - 7 year old), concrete operational stage (7 – **12 years old**), and **formal operational stage** stage (13-14 years old or 14-15 years old).

To avoid time consuming in implementation of accurate observations and interviews, Capie and Tobin (Sumarmo, 1987) compiled a written test to substitute Inhelder and Piaget's technique for determining student's cognitive stage for **number of students in shorter time and all at once together**. The test was known as **test of logical thinking (TOLT) and** it constituted of ten items measuring controlling variable reasoning, proportional reasoning, probability reasoning, and combinatorial reasoning.

In order to obtain valid instrument of the TOLT, then Capie and Tobin (Sumarmo, 1987) carried out cross-cultural studies on TOLT with a **number of student** from eighth grade up to tertiary (college) students. The cross-cultural **studies found that** many students of more than **15 years old had not reached formal operational stage** yet, but in higher student's grade school there found greater percentage of formal students' and lower percentage of concrete students.

In addition, the cross cultural studies also invented that in higher school grade study

found greater percentage of formal students and smaller percentage concrete students. In principle, those findings supported statement that TOLT was a valid written test for measuring cognitive **operational stage of** students according to Piaget's theory.

Discussion on logical reasoning our discussion closed to mathematical reasoning term. Teachers aware that mathematical reasoning (MR) is one of essential mathematics ability should be mastered **by high school students**. The last statement not only caused of MR is enclosed in the goal of mathematics teaching (NCTM, 2000; **Peraturan Menteri Pendidikan Nasional** No.

81a Tahun 2013 tanggal 27 Juni 2013 tentang Implementasi KurikulumStandar Isi, n.d.) but it was agreeable to some mathematics experts' opinion as well. The goal of teaching mathematics, **among other things** were: to develop student's potency to become a critical, creative, logical, accurate, and innovative human (Peraturan **Menteri Pendidikan Nasional** No. 81a Tahun 2013 tanggal 27 Juni 2013 tentang Implementasi KurikulumStandar Isi, n.d.).

There are some experts' notion about MR namely: a. MR is to derive conclusion based on proper data, event, facts, evidence, and or sources (Hendriana, Rohaeti, & Sumarmo, 2014; Kusnandi & Sumarmo, 2010); b.MR is to think logically about and with mathematicsobject (Kusnandi & Sumarmo, 2010).

When we pay deep attention on mathematical processes involved in MR, it portraits that MR was higher order thinking (HOT) in mathematics. It implied in solving MR beside students should master mathematics content, they also should own certain disposition as well, such as having self confidence, habit to work hard and to monitor his learning,ability to manage his learning. Such kind of mathematical disposition was **self regulated learning** (SRL).

Some experts (Butler, 2002; Kerlin, 1992; L. & Randi, 1999; Paris & Winograd, 1998; Schunck & Zimmerman, 1998; Sumarmo, 2006), defined SRL in different expressions, but they containsome similar components, **namely: to plan** self learning objective; to select strategy; and to monitor, **to evaluate learning** processes and to compare them to a certain standard.

In addition, some studies (Aminah, Kusumah, Suryadi, & Sumarmo, 2017; Bernard & Rohaeti, E, 2016; Maya & Sumarmo, 2014; Qohar & Sumarmo, 2014) by implementiing various teaching approaches invented that students obtained MR at low to medium grade level. Likewise, other studies (Damayanti, Sumarmo, & Maya, 2018; Qohar & Sumarmo, 2014; Sumarni & Sumarmo, 2017) detected that students attained SRL at

fairly good grade level.

Those aforementioned arguments stimulated researchers to execute a study to analyze role of cognitive stage on obtaining student's MR, SRL and then we compile research questions as follows. What are student's percentage on each cognitive stage measured by using TOLT? What are student's grade on MR and on SRL for entirely students and according to its cognitive stage? What kind of student's difficulties on solving MR tasks? Is there any association between cognitive stage and MR, between cognitive stage and SRL, and between MR and SRL and SRL. 1.1.

Theoretical Review Stage of Child's Cognitive Development To analyze the way of children reasoning, Inhelder and Piaget (Sumarmo, 1987) executed a series of accurate observations through experiment and individual interviews toward a number of subjects of various age groups from children up to adult from various best of schools in Geneva.

Based on those observations and interviews then Inhelder and Piaget (Sumarmo, 1987) identified cognitive abilities which able to do or not able to do by each age group of children. By analyzing the structure of each age group of children, then Inhelder and Piaget (Sumarmo, 1987) classified subjects into four main stages of thinking or stage of child cognitive development, namely: a) Sensory-motor stage (infant up to 2 years old); b) Pre-concrete operational stage (2 – 7 years old); c) Concrete operational stage (7-12 years old); d) formal operational stage (13-14 years old or 14-15 years old).

To overcome time consuming for implementing depth observation and interview for a number of students in shorter time at once, Tobin and Capie (Sumarmo, 1987) developed a written tes called test of logical thinking (TOLT) which compiled based on theory of Inhelder and Piaget child cognitive development. The TOLT was in multiple choice form of five option accompanied with 5 choices of reason.

The tests measured four reasoning abilities those were: controlling variables, proportional reasoning, probabilistics reasoning, corelational reasoning, and combinatorial reasoning. Capie and Tobin (Sumarmo, 1987) with a number of subjects from primary school up to college students, reported their findings as in Table 1. Those findings pointed out that the TOLT was group test that measured formal thinking ability for a number of students of various age and cultures in shorter time at once. Table 1.

Findings in Validation Studies on TOLT of Tobin dan Capie _ _ Subject _ N _ % Concrete Stage _ % Transition Stage _ % Formal Stage _ _ 6th grade student _ 100 _ 97 _ 3 _ 0 _ _ 7 th grade student _ 86 _ 96 _ 2 _ 2 _ _ 8 th grade student _ 167 _ 86 _ 9 _ 5 _ _ 11 th grade student _ 82 _ 32 _ 17 _ 51 _ _ College student _ 247 _ 45 _ 18 _ 37 _ _ Source: Tobin and Capie 1981

(Sumarmo, 1987) Those studies found many subjects of more than 15 years old had not attained formal operational stage yet.

However, studies also found in higher school grade there were greater percentage formal subjects and smaller percentage concrete students. Those findings were fitting to further hypothesis of Inhelder and Piaget that normal subject will reach formal operational stage in between 11- 12 years old up to 14 – 15 years old, even in other condition in 18 – 20 years old. 1.2.

Mathematical Reasoning Ability and Self Regulated Learning Based on some experts' conception (Aminah et al., 2017), Classified MR into two kinds those are inductive and deductive mathematical reasoning (Sumarmo, 2006). Then, inductive MR was to derive conclusion based on observed data or process. Further, she detailed inductive MR into some kinds of activities, namely: a.

transductive reasoning; b. Analogical reasoning; c. Generalization; d. Predicting solution or tendency; e. Giving explanation based on model, facts, attributes, relation or pattern; and f. Applying relationship of pattern for analyzing situation, and compiling conjecture (Sumarmo, 2006).

While deductive MR was to attract conclusion based on proper rules. Deductive MR involed some activities: a.To carry out calculation agreed to proper rules and principles; b.To reason based on the rules of inference (propositional reasoning); To examine validity of an argument, to prove and to compile valid argument; c.To reason based on ratio between two or more components (proportional reasoning) (Aminah et al., 2017); d.

To conclude based on combination of some elements (combinatorial reasoning) (Aminah et al., 2017); e.To conclude based on probability of an event (probabilistic reasoning); f. To correlate relationships between two different situations (Aminah et al., 2017); g. To proof the truth of statement directly, indirectly, or proving by mathematics induction.

When we paid deep attention to those processes involved on MR, we get impression there were various level of thinking of those processess from medium to very high level. Therefore, we have to determine definite indicators fitting for certain school level of students. For examples, for junior high school students, we restrict indicators of MR on transductive, analogical, generalization and proportional reasoning, predicting, and executing enumeration based on certain rules and principles.

Whereas, for senior high school or university students almost all indicators of mathematical reasoning are able to be assessed to them provided they are relevant to the learned mathematics contents. Based on indicators of MR we inferred that MR was HOT mathematics tasks which it needed strong mathematics disposition in solving MR tasks. That disposition involved high motivation, habit to work hard, and ability to organize self-learning. That kind of disposition was self regulated learning (SRL).

Some writers defined SRL in various expression as follow: a. SRL is was to design and to observe self learning process carefully in completing academic task (Kerlin, 1992); b. SRL was ability to observe self behaviour and as hard work human personality (Kerlin, 1992).

Further he elaborates activities of SRL more detailed, such as: to assess own-self, to determine learning goal and conception; to collect, to notation; c. SRL is learning process affected by thinking, feeling, strategy, and own behaviour oriented to the realizing goal. SRL involves three phases namely: to design and to observe learning activities, and to assess and to reflect learning out comes (Schunck & Zimmerman, 1998); SRL was cycle of recursive cognitive activities that holds to analyze task, to choose, to adopt, or to invent strategy for obtaining the goal of task, and to monitor learning out comes; d.

Other term of SRL namely self-direction on learning (SDL) is responsible individual learning process in planning, executing, and assessing his learning (Wongsri, Cantwell, & Archer, 2002); e. Hoban, Sersland, Raine (Wongsri et al., 2002) name SDL as self efficacy that is individual view point toward his own abilities. Some indicators of SRL as follow: a. Awareness toward learning goal so that learning becomes more directed, concentrated, and keep going for long time; b.

Awareness toward learning responsible; c. Learning continuously so that it composes ordered learning habits; d. Learning actively through reading various sources, and relating prior and new knowlegde, working in a group actively and creatively and posing question actively toward unclear matters; e.

Learning efficiently by arranging time fitting to depth and wideness of learning material (Djamarah & Zain, 2002; Paris & Winograd, 1998) Some writers offer some suggestion to enhance student's SRL, among other as follow: a. SRL ables to improve by any relevant teaching approach (Sumarmo, 2006; Wongsri et al., 2002); b. Teacher ought to assist student to carry out SRL cycles flexibly and as creatively through: analyzing task, selecting and implementing strategy, self monitoring and reflecting (Butler, 2002; Sumarmo, 2006); c.

Other some suggestion for developing SRL are: Create conducive learning environment,

remember student to follow certain guidelines, Motivate student to comprehend the true procedure in solving task, assist student to manage time, promote student's self confidence that he is able to complete the task, stimulate student to control his emotion and not easily be panic, show student's success and assist student to look for learning help.

Other writers (Zumbrunn, Tadlock, & Robert, 2011) pose some strategy for forming SRL as follows: a. Setting short and long term goal; b. Planning self managing; c. Promoting own self motivation; d. Developing own attention control; e. Executing flexible strategy; f) Carrying out self monitoring; g. Trying help seeking; h. Performing self evaluation. Further, based on writers' conception (Butler, 2002; L.

& Randi, 1999; Paris & Winograd, 1998; Schunck & Zimmerman, 1998; Sumarmo, 2006; Wongsri et al., 2002). Indicators of SRL as follows: a. To have intrinsic learning initiative and motivation; b. To own habits to diagnose learning needs c. To determine learning target; d To monitor, to manage, and to control self learning; e. to regard difficulty as challenge; f.

To use and to seek relevant sources; g. To select and to carry out strategy; h. To assess learning process and outcomes; i. To perform self efficacy (Sumarmo, 2006) 1.3. Relevant Studies Beside aforementioned studies' findings, since long ago, there were some studies reported superiorities of formal stage subjects than concrete stage subjects on various mathematics abilities.

For examples: McDonald (Sumarmo, 1987) on structure of geometry of tenth grade students, and Lawson & Lawson (Sumarmo, 1987) on composing argument and testing hypothesis of college students. In order to use written test for determining student's cognitive stage on Indonesia students, Translated TOLT into Indonesian culture and validated the test to original TOLT (Sumarmo, 1987).

Further, by implementing translated TOLT and Longeot test carried out precise survey with 414 eleventh grade students of 17,43 years old from some Senior High School in seven cities in West of Java. The survey invented that 48% students had reached formal stage, 22% students at transition stage, and 30% students still at concrete stage.

In addition, the survey reported superiority of formal stage than transition stage, and the excellence of transitional stage than concrete stage students on mathematical understanding and reasoning. Likewise. Those findings were fitting to Piaget's theory that formal stage students were smarter than concrete stage students in solving HOT mathematics tasks which required formal process of thinking (Sumarmo, 1987)

Moreover, other some recent studies (Koswara, Sumarmo, & Kusumah, 2012; Kusnandi & Sumarmo, 2010; Offirston & Sumarmo, 2012; Rijaya, Sumarmo, & Syaban, 2018; Setiawati, 2014; Sumarni & Sumarmo, 2017) by using various teaching approaches detected that students obtained MR at medium to fairly good grade level. Similarly, other studies (Mulyana & Hendriana, 2015; Retnaningsih & Sugandi, 2018; Rohaeti, Budiyanto, & Sumarmo, 2014; Setiawati, 2014) found that students attained SRL at fairly good grade level. Seemingly, for high school students to solve MR tasks were more difficult than to perform SRL attitudes.

METHOD This study is a descriptive survey having a goal to explore relation of student's cognitive stage on attainment of MR and SRL. The survey involved 36 eleventh grade students of a school determined purposively, TOLT of Cpaie and Tobin (Sumarmo, 1987), an essay MR test and a SRL scale developed special for this survey.

The MR test consists of 5 items, and by using a guide it was obtained characteristic of MR test and SRL scale were attached in Table 2 (Hendriana & Sumarmo, 2014). Data analysis of this survey involved: computation for items scoring for SRL scale, percentage computation, t testing hypothesis of mean difference, (2 for testing of existence of association of two variables, and other rational analysis for relevant data. Table 2.

Characteristics of Instruments of This Study

| Test and Scale | N | Subject | Item Test & Scale | Discriminat power | difficulty index | Item validity | Reliability | TOLT* |
|----------------|----|---------|-------------------|-------------------|------------------|---------------|-------------|-------|
| MR** | 36 | 5 | .15 | .50 | .12 | .53 | .23 | .67 |
| SRL** | 36 | 30 | .00 | .53 | .63 | .88 | 1.87 | 4.44 |

Note: * adopted from McDonald (Sumarmo, 1987) **analyzed in Gunawan et.all., 2019 2.1. In the following we attached some sample of instruments of this study.

1 2 3 4 5 ? 4 w ? ? 10 w 5 w ? 5 w ? 3 w

Figure 1. Figure Sample item of TOLT (The Pendulum's Length) Suppose you wanted to do an experiment to find out if changing the length of a pendulum changed the amount of time it takes to swing back and forth.

Which of the pendulum would you use for the experiment? 1 and 4 2 and 4 1 and 3 2 and 5 All Reasons: The longest pendulum should be tested against the shortest pendulum. All pendulum need to be tested against one another. As the length is increased the number of washers should be decreased. The pendulum should be the same length but the number of washers could be different.

The pendulums should be different lengths but the number of washers should be the same. 2.2. Sample Item of Mathematical Reasoning (MR): analogical reasoning It is given

a square of its side is 10 unit. Through middle point of each side, draw a second square. Observe a triangle inside of first square and out side of second square. Name **the area of the first** triangle is L1.

Through middle point of each **side of the second square**, then draw the third square and observe a triangle inside of second square and out side of third square. Name **the area of the second** triangle is L2. Those processess is continued up to fifth triangle. Draw that situation and indentified each triangle and its area. Determine sum of area of first triangle up to fifth triangle and explain concepts and rule used in each step of solving it. 2.3.

Sample items of **Self Regulated Learning (SRL)** Scale No. Activity, feeling, or opinion
QO O S QS 1. Select difficult mathematics task about general form of pattern Pn
caused of liking to do it. 2. Try to identify self weakness in learning aritmetics
and geometry **sequence and series** 3.

To learn arithmetics **sequence and series** without target will lighten learning task. 4.
Note: QO quiet often ; O: often; S: seldom; QS: quiet seldom RESULTS AND
DISCUSSION Description of MR, and SRL in entirely and grounded on student's cognitive
stage were attached **in Table 2.** Table 2.

Description of **Student's Mathematical Reasoning and** Student's Self Regulateg Learning
Grounded on Student's Cognitive Stage Variable Statists Concrete Stage N (%)
Transition Stage n (%) Formal Stage n (%) Total n MR (IS =69) ?? 10.40 20
56% 23.57 7 19% 36.33 9 25% 19.44 36 100% 15.07% 34.16% 52.66%
28.18% s 7.39 4.31 10.52 13.48 SRL (IS =120) ?? 93.35
20 56% 93.86 7 19% 94.00 9 25% 93.61 36 100% 77.79% 78.21%
78.33% 78.01% s 7.94 7.31 11.90 8.71 From Table 2, for entirely
students and transition and concrte students survey found MR at very low grade level,
and formal students attained MR at low grade level.

This findings were different with findings of previous studies (Bernard & Rohaeti, E, 2016; Mulyana & Hendriana, 2015; Prasetio, Sumarmo, & Sugandi, 2018; Sumarni & Sumarmo, 2017) that students getting treatment with **various innovative teaching** attained MR at medium grades. But that **findings were similar to** findings of other studies (Aminah et al.,

2017; Dasari & Sumarmo, 2010; Kusnandi & Sumarmo, 2010; Maya & Sumarmo, 2014; Rohaeti et al., 2014; Setiawati, 2014; Sumarmo, Hidayat, Zulkarnaen, & Hamidah, Sariningsih, 2012) that students obtained at low grade level. Seemingly, innovative

teaching mathematics gave different result on students' grades of MR from low level up to good level.

The low students' grades on MR were found on studies with **senior high school students** and on intermediate mathematics course such as system of equation of two and more variables, (Aminah et al., 2017; Setiawati, 2014) and on proving problems (Dasari & Sumarmo, 2010; Kusnandi & Sumarmo, 2010; Maya & Sumarmo, 2014). Testing hypothesis on mean difference on MR of each student's stage were attached on Table 3. Table 3.

Testing Hypotesis of Mean Difference **of Mathematical Reasoning and Self Regulated Learning** according to Student's Cognitive Stage __ Variable _Cognitive Stage _ ?? _S _N _Sig (1-tailed). _ Interpretation __ MR _Formal _36.33 _10.52 _9 _010 < .05 _MRT > MRT _ __Transition _23.57 _4.31 _7 _ _ _ _Transition _23.57 _4.31 _7 _0.00 < .05 _MRT > MRC _ __Concrete _10.40 _7.39 _20 _ _ _ _SRL _Formal _94.00 _11.90 _9 _978 > .05 _No different SRLF and SRLT __Transition _93.86 _7.31 _7 _ _ _ _Transition _93.86 _7.31 _7 _883 > .05 _No different SRLT and SRLC __Concrete _93.35 _9.79 _20 _ _ _ _Note: MR: mathematical reasoning Ideal score MR: 69 SRL: **self regulated learning** Ideal scoreSRL:120 Further analysis was concerned with student's difficulties on solving MR tasks. The data were illustrated in Table 4.

The survey found that, all students (concrete, transition, and formal stage) realized difficulties in all items test of MR. **These findings were similar to** findings on other previous studies (Aminah et al., 2017; Bernard & Rohaeti, E, 2016; Koswara et al., 2012; Mulyana & Hendriana, 2015; Rohaeti et al.,

2014; Setiawati, 2014; Sumarni & Sumarmo, 2017) that many students experienced many difficulties on accomplishing MR tasks. Table 4. Mean **Score of Each Item of Mathematical Reasoning** According to Student's Cognitive Stage __ Cognitive Stage _Item number. _No.1 _No 2. _No.3 _No.4 _N0. 5 _ _ _Ideal score _12 _15 _15 _15 _12 _ _Formal _ ?? _6.67 _8.22 _10.00 _5,00 _2.12 _ _ % of IS _55.58% _54.80% _66.67% _33.33% _3.07% _ _Transition _ ?? _4.86 _7.57 _5.57 _3.00 _2.57 _ _ % of IS _40.05% _50.47% _37.13% _20.00% _21.42% _ _Concrete _ ?? _3.20 _85 _2.20 _1.35 _2.80 _ _ % of IS _26.67% _5.67% _14.67% _9% _23.33% _ _ Mathematical Reasoning Ideal score MR: 69 Afterward analysis were contigency computation between cognitive stage and MR, between cognitive stage and SRL, and between MR and SRL.

By using contigency table and statistic Pearson-Chi Square ((2) the survey found contigency of those variables such as in Table 5, Table 6, and Table 7, and their hypothesis testing were in Table 8. Table 5. Contigency Table of Cognitive Stage (CS)

and Mathematical Reasoning (MR) __ CS MR _Formal Stage _Trans. Stage _Concr. Stage
_Total __High _7 _1 _0 _8 __Medium _2 _6 _11 _19 __Low _0 _0 _9 _9 __Total _9 _7 _20
_36 __ Table 6. Contingency Between Cognitive Stage (CS) Table 7.

Contingency Between MR **and Self Regulated Learning (SRL)** and SRL __ CS SRL _Formal
Stage _Trans. Stage _Concr. Stage _Total _SRL MR _High _Medium _Low _Total __High
_3 _1 _5 _9 _High _3 _3 _2 _8 __Medium _3 _4 _10 _17 _Medium _4 _9 _6 _19 __Low _3 _2
_5 _10 _Low _2 _5 _2 _9 __Total _9 _7 _20 _36 _Total _9 _17 _10 _36 __According to
findings on Table 5, Table 6, Table 7, and Table 8 survey invented there was high
association between student's CS and MR, even if **there were no** association between
student's CS and SRL and between MR and SRL.

Those findings were understandable caused of both CS and MR tasks measured similar
cognitive abilities namely reasoning tasks. While CS and SRL, and MR and SRL measured
different abilities such as cognitive and affective variables. Table 8. Test of Pearson-Chi
Square and Contingency Coefficient between Cognitive Stage, **Mathematical Reasoning
and Self Regulated Learning** _Association Between Variable _Pearson-Chi Square ((2)
_DF _Contingency Coefficient (C) _Sig. (2-tailed) _Interpretation __CSt and MR _27.392a _4
_.657 _000 < .05 _High Association __CSt and SRL _1.275a _4 _185 _866 > .05 _No
Association _MR and SRL _1.160a _4 _177 _885> .05 _No Association __ CONCLUSION
According to findings and discussion, the survey derived conclusion as follow.

By employing TOLT, the survey found many students with 17, **45 years old had not
reached** formal stage, such as 19% students were at formal stage, 25 % students were at
transition stage, and 46 % students were at concrete stage. In entirety, students
obtained mathematical reasoning at very low grade level. While according to student's
cognitive stage, formal students attained higher grade **mathematical reasoning than** the
grades of transitional stage students, and concrete students and all MR grades were at
very low grades level.

Like that, either entirely or according to student's cognitive stage all students realized
difficulties in all items of MR tasks. Other conclusion were there was high association
between cognitive stage and mathematical reasoning, but **there were no** association
between cognitive stage **and self regulated** learning, and between **mathematical
reasoning and self regulated** learnig.

In general, findings of survey were sturdy with Inhelder and Piaget's of Child Cognitive
Development, that in normal students formal stage will reach in 12 to 13 years old, or 13
to **14 years old**, or **in other cases** in 19 to 20 years old, and formal students possessed
higher abilities than transition students and concrete students on compiling any task

which needed formal operational thinking.

To determine cognitive stage of students according to Piaget's theory was not by biological age of students, but by student's abilities on completing logical reasoning tasks such as measured in TOLT (Sumarmo, 1987) or Longeot test (Sumarmo, 1987). To enhance student's HOTS of mathematical reasoning, it was suggested to strengthen student's mastering of mathematics prerequisite contents and processes and to familiarize students to solve non routine and opened problems and to make students realize on rules and concepts which used in each step of enumeration.

Further, to improve better students' self regulated learning, it was suggested: Perform teacher's behaviour as wish in SRL attitudes; accustomize students and teacher to behave as wish in SRL attitudes, and carry out integrated and continuous mathematics teaching process.

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Thank you to Prof. Utari Sumarmo, M.Pd as a Lecturer in the Masters in Mathematics Education who has guided in conducting this research. Thank you to the parties who helped in conducting this research. REFERENCES Aminah, M., Kusumah, Y. ., Suryadi, D., & Sumarmo, U. (2017). The Effect of Metacognitive Teaching and Mathematical Prior Knowledge on Mathematical Logical Thinking Ability and Self-Regulated Learning.

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