

Computational Discovery of Superior Vanadium Niobates Based Cathode Materials for Next-Generation All-Solid-State Lithium-Ion Battery Applications

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All-solid-state lithium-ion batteries (ASSLIBs) are at the forefront of green and sustainable energy development research. One of the key challenges in the development of ASSLIBs for commercial applications is to find cathode materials that have high capacity, voltage and power density. Using a combination of first-principles calculations and various crystal structure prediction algorithms, we explore the $\text{LiVO}_2\text{-Li}_3\text{NbO}_4$ pseudobinary tieline to identify novel stoichiometries with improved properties as cathode materials for ASSLIB applications. Based on more than 10,000 Density Functional Theory (DFT + U) calculations using crystal structures obtained from *ab initio* random structure searching (AIRSS), genetic algorithm, and configuration enumeration procedures, we predict five novel stoichiometries, $\text{Li}_{23}\text{Nb}_7\text{V}_2\text{O}_{32}$, $\text{Li}_{10}\text{Nb}_3\text{VO}_{14}$, $\text{Li}_7\text{Nb}_2\text{VO}_{10}$, $\text{Li}_{11}\text{Nb}_3\text{V}_2\text{O}_{16}$, Li_4NbVO_6 , along with an experimentally known stoichiometry, $\text{Li}_5\text{NbV}_2\text{O}_8$. All the novel stoichiometries are found to have cation-disordered rock-salt crystal structures and fall within 30 meV/atom from the convex hull of the parent compositions. These new phases are predicted to have superior properties compared to the current vanadium-niobates-based electrode materials, including a higher theoretical capacity, lower band gap, higher average Li intercalation voltage, minor volume change upon full Li delithiation, good mechanical & dynamical stability, improved Li-conduction activation barrier and high-temperature stability. Our results are anticipated to inspire further experiments to synthesise and test these specific vanadium-niobate-based materials for their actual performance as Li-ion cathode materials.

1 Introduction

Since the commercialisation of rechargeable lithium-ion batteries (LIBs) in 1991¹, LIBs have come a long way as a solution to clean and effective electrochemical energy storage. Owing to their high energy density, good rate capability, long shelf-life and low maintenance cost, rechargeable LIBs have earned their reputation as the enabling technology for the transportation, aviation, aerospace, and stationary energy storage sectors^{2–8} including all-electric vehicles (EVs)⁹ and large scale stationary storage¹⁰. Despite these successes, scaling-up LIBs has been challenging owing to safety reasons primarily attributed to the commonly used organic electrolyte solutions. They can be volatile, flammable and even explosive, potentially causing catastrophic failures, particularly when used in excessive amounts to power energy-intensive applications.

To mitigate the safety risks associated with the conventional liquid electrolytes used in LIBs, all solid-state lithium-ion batteries (ASSLIBs), which utilise a solid electrolyte, have drawn soaring attention in recent years^{11,12}. Beyond mitigating safety concerns, solid state electrolytes can also provide superior battery performance due to their higher energy density. One of the major re-

maining roadblocks for the commercialisation of ASSLIBs is the lack of a suitable high-capacity positive electrode material. Thus, to meet the stringent energy demand there is an ever-growing need for developing next-generation battery technologies, in particular, advanced electrode materials that can deliver high power as compared to existing ones.

The full potential of ASSLIBs as next-generation batteries can be unlocked by the discovery of new battery materials with superior performance such as higher capacity and energy density, safer operation, better stability, higher longevity, faster charge rates, better component compatibility, and economical viability. Over the years, many oxide- and phosphate-based cathode materials have been studied extensively as promising candidates for cathode materials^{11,13}. However, some of the commonly used cathode materials suffer from their low theoretical capacity (Q_{max}) which is a measure of the amount of charge (lithium ions) that can be stored by the material. An extensive (although incomplete) list of such materials is reported by Nitta and co-workers⁸ where the majority have Q_{max} values below 300 mAh/g, except for Li_2MnO_3 whose Q_{max} is 458 mAh/g.

Li_2MnO_3 and its derivatives have been studied extensively in the past decade as cathode materials^{14–20} which show anomalously high reversible capacity with relatively good capacity retention. However, Li_2MnO_3 suffers from capacity and voltage fading during electrochemical cycles²⁰ owing to the layered-to-spinel phase transformation coupled with gradual oxygen loss, which restricts its use for commercial applications. Sim-

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ilarly, $\text{LiVO}_2\text{-Li}_3\text{NbO}_4$ -based systems have also been studied recently by Yabuuchi and co-workers^{21–23} as a new family of high-capacity cathode materials for rechargeable LIBs. In their work, a particular focus was given to $\text{LiVO}_2\text{-Li}_3\text{NbO}_4$ solid solutions where they were able to synthesize two specific stoichiometries, $\text{Li}_{1.3}\text{Nb}_3\text{V}_4\text{O}_{20}$ ($\text{Li}_{1.3}\text{Nb}_{0.3}\text{V}_{0.4}\text{O}_2$)²¹ and $\text{Li}_5\text{NbV}_2\text{O}_8$ ($\text{Li}_{1.25}\text{Nb}_{0.25}\text{V}_{0.5}\text{O}_2$)²³ with reversible capacity of 230 mAh/g ($Q_{\text{max}} = 390$ mAh/g) and 240 mAh/g ($Q_{\text{max}} = 375$ mAh/g), respectively. Their work suggests that there is room for further increasing the reversible capacity and energy density, which motivates a more systematic exploration of new $\text{LiVO}_2\text{-Li}_3\text{NbO}_4$ materials.

In this work, we explore the $\text{LiVO}_2\text{-Li}_3\text{NbO}_4$ pseudobinary tieline to search for new stoichiometries that could have superior cathode properties for use in ASSLIBs and other conventional LIBs using a combination of first-principles calculations and crystal structure prediction algorithms. To sample the composition space, we develop a database containing more than 10,000 structures optimised using density functional theory (DFT) and obtained from a combination of major databases and our own crystal structure prediction (CSP) calculations. We predict five novel stoichiometries, $\text{Li}_{23}\text{Nb}_7\text{V}_2\text{O}_{32}$, $\text{Li}_{10}\text{Nb}_3\text{VO}_{14}$, $\text{Li}_7\text{Nb}_2\text{VO}_{10}$, $\text{Li}_{11}\text{Nb}_3\text{V}_2\text{O}_{16}$, and Li_4NbVO_6 ; along with an experimentally known stoichiometry, $\text{Li}_5\text{NbV}_2\text{O}_8$ ²³. All the stoichiometries are predicted to have a cation-disordered rock-salt crystal structure which is in good agreement with previous experimental findings^{21,23}. Interestingly, our newly discovered stoichiometries are predicted to have higher Q_{max} value, lower band gap, higher average Li intercalation voltage, minor volume changes upon full Li delithiation, good mechanical stability, improved Li^+ -conduction activation barriers, and high-temperature stability. In particular, we predict that some of the new stoichiometries may have improved cathode properties compared to the experimentally known ones. Thus, our work advances the discovery of new lithium vanadium niobate (Li-V-Nb-O) materials and may inspire further experimental work to synthesise and test the actual performance of our new stoichiometries as Li-ion cathode materials.

2 Methods

2.1 Density functional theory calculations

All total energy calculations were performed using plane-wave Density Functional Theory (DFT) as implemented in the Vienna Ab Initio Simulation Package (VASP, v.6.2.1)^{24–26}. The Perdew-Burke-Ernzerhof (PBE) exchange-correlation functional²⁷ and Projector Augmented Wave (PAW) pseudopotentials²⁸ were used to represent each element. The Hubbard U (GGA+ U) approach^{29,30} to the V $3d$ states was applied. The value of $U = 3.25$ eV was chosen to be consistent with those used for calculations in the Materials Project (MP) database^{31,32} and other studies³³. All DFT calculations were spin-polarized except otherwise noted, initialized in a ferromagnetic spin configuration. A plane-wave cutoff energy of 520 eV was used to expand the orbitals, and the Brillouin zone was sampled using the Methfessel-Paxton scheme. Monkhorst-Pack grids³⁴ with a spacing of 0.314 \AA^{-1} were used. The atomic coordinates were fully relaxed during the DFT simulations until the forces on each atom were within 0.05 eV/\AA .

An electronic convergence criterion of 10^{-8} eV and a Gaussian smearing factor of 0.2 eV were adopted, and the VASP default settings for the fast Fourier transform (FFT) grid and optimisation of the projection operators were employed. For the analysis of band structure, density of states, and estimation of band gap values, we used the PYMATGEN³⁵ software package. All the database management and the convex hull plotting tasks were done by the MATADOR package³⁶. All crystal structures were visualized with the VESTA³⁷ software package.

To study Li^+ diffusion and high-temperature stability, *ab initio* molecular dynamics (AIMD) simulations were carried out in the NVT ensemble as implemented in VASP^{24–26}. We performed non-spin-polarised DFT calculations with an energy cutoff of 400 eV for all the AIMD simulations to reduce computational costs. We used supercells with the minimum lattice dimension larger than 10 \AA to minimize the finite cell size effect and a Γ -centered $1 \times 1 \times 1$ k-mesh was used for the sampling of the Brillouin zone. The time step was set to 2 fs. For the analysis of Li-ion diffusion and the pair radial distribution function (RDF), we generated at least 50 and 10 ps AIMD trajectories, respectively.

To investigate the mechanical stability of the selected stoichiometries we carried out elastic constant calculations based on the energy-strain method as implemented in VASPKIT³⁸ where the total energy values were obtained from VASP. We applied a strain of ± 0.015 on selected fully relaxed stoichiometries to obtain the full elastic tensor and derived mechanical properties. Using the computed elastic constants, the mechanical stability criteria were evaluated following Mouhat and co-workers³⁹ using the VASPKIT³⁸ code.

The dynamical stability of selected novel structures was verified with phonon calculations using the finite displacement method in conjunction with diagonal supercells⁴⁰ as implemented in the PHONOPY package^{41,42}. For the compounds with larger primitive cells, this approach becomes computationally prohibitive so instead we used the more efficient finite displacement method in conjunction with nondiagonal supercells^{43,44}.

To estimate Li^+ vacancy diffusion barriers we carried out climbing image nudged elastic band (CI-NEB) calculations^{45,46} as implemented in ASE⁴⁷. All the calculated NEB paths comprised of five intermediate images. Overall charge neutrality was achieved by adding a positive background charge. All the ionic forces were converged to within 0.05 eV/\AA with the spring constant set to 0.1 eV/\AA . To estimate the energy at the saddle point, cubic splines were fit through the images along each hop as implemented in ASE⁴⁷. Bond valence site energies (BVSEs) were calculated using the SOFTBV program^{48–50} to rapidly identify the Li^+ diffusion pathways and to estimate the Li^+ migration barrier in our complex disordered structures. The structural information required for the BVSE calculations was collected from the CIF files generated using VESTA/ASE. The energetics of different Li^+ ions, E_{BVSE} , were calculated using grids spanning the structure model with a resolution of 0.1 \AA .



2.2 Crystal structure prediction

We employed a variety of crystal structure prediction schemes to sample the composition-structure space spanned by the LiVO_2 - Li_3NbO_4 pseudobinary tieline as comprehensively as possible. The databases used in this work are the Materials Project (MP)^{31,32}, the Open Quantum Materials Database (OQMD)^{51,52}, Novel Materials Discovery (NOMAD)⁵³⁻⁵⁵, and Automatic FLOW for Materials Discovery (AFLOW)⁵⁶; and the CSP calculations used *ab initio* random structure searching (AIRSS)^{57,58}, a genetic algorithm (GA)⁵⁹⁻⁶¹, and configuration enumeration (ENUM)⁶². These CSP schemes are discussed next.

2.2.1 *Ab initio* random structure searching

At the core of the searching efforts we used the *ab initio* random structure searching (AIRSS) method^{57,58} to generate random “sensible” structures constrained by space group symmetry, density, and atomic bond-length. AIRSS has been recognised as a successful tool to efficiently sample the vast composition space in many materials^{57,58}. Upon generating the structures, we fully optimized them using DFT to locate their local minima. All relaxations were performed individually, that is, without any dependence between calculations. Our initial pool of trial structures was ~ 10000 in the entire LiVO_2 - Li_3NbO_4 pseudobinary tieline with no constraints on stoichiometry. However, to reduce the computational cost we imposed a volume constraint V_c based on the total number of Li, Nb, V, and O atoms N_{atoms} in the unit cell such that $5N_{\text{atoms}} \text{ \AA}^3 \leq V_c \leq 15N_{\text{atoms}} \text{ \AA}^3$.

2.2.2 Evolutionary search

We also used an evolutionary search scheme to identify (meta-)stable structures based on a genetic algorithm (GA) as implemented in the USPEX code featuring local optimization, real-space representation, and flexible physically motivated variation operators⁵⁹⁻⁶¹. For computational efficiency, instead of a full variable-composition evolutionary algorithm to sample the entire quaternary composition space, we instead only used USPEX for selected chemical compositions that were less than 200 meV/atom from the hull as found by the AIRSS searches. Due to the associated computational cost, we could simulate up to a maximum number of 28 atoms per unit cell. The number of structures in the initial generation and each subsequent generation was set to 50. In each generation (except the first generation), 40% of structures were generated using heredity, 40% were generated by mutation (20% by soft mutation, 15% by transmutation, and 5% using spin mutation), and 20% were generated randomly. During the structure search process, the structures in each generation were relaxed through a three-step process with increasing precision. Underlying structure relaxations and energy calculations were done using the VASP package.

2.2.3 Configuration enumeration

The symmetrically distinct cation ordering in the LiVO_2 - Li_3NbO_4 pseudobinary tieline was also evaluated by means of configuration enumeration (ENUM). To do this we started with a supercell of the $I43m$ - Li_3NbO_4 structure (64 atoms), removed and replaced Li/Nb sites with V sequentially while maintaining charge balance.

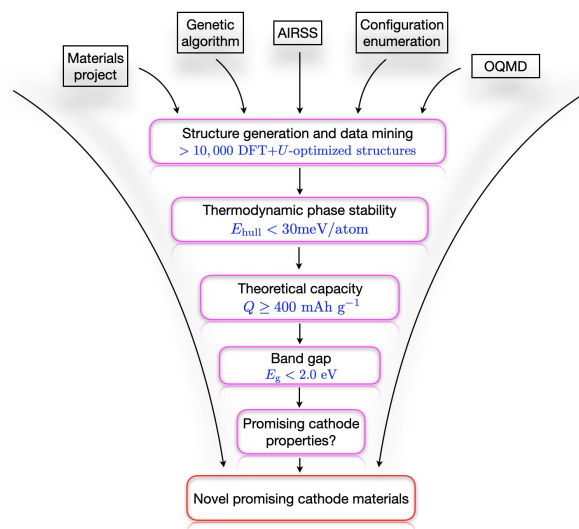


Fig. 1 Computational search workflow. A schematic high-throughput computational workflow is shown that is used in this work to search for novel promising cathode materials.

For each step of the removal/addition process, all configurations were enumerated and subsequently relaxed using VASP. The best candidates, based on a Boltzmann probability distribution and taking into account configurational entropy, were selected as the starting point for the next step where again the removal/addition process was carried out until we reached the $R3m$ - LiVO_2 composition. Overall, about 100 cation ordering configurations were produced along the LiVO_2 - Li_3NbO_4 pseudobinary tieline.

2.3 Computational workflow

The computational workflow used in this work is schematically presented in Figure 1. Here we have employed three different CSP techniques ‘independently’ with no shared information with each other at the time of structure generation. We collate all the structures from the different sources only at the stage of analysis. In the very first step, we collected all the structures that contain Li-Nb-V-O including the end-members (LiVO_2 and Li_3NbO_4) from the major databases MP, OQMD, NOMAD, and AFLOW. Then, we started generating our own structures along the LiVO_2 - Li_3NbO_4 pseudobinary tieline using AIRSS. After generating a few thousand structures we got a good estimate on the relevant stoichiometries with low formation energy (usually less than 100 meV/atom) to do more guided/directed searches using USPEX and ENUM. This approach proved to be very efficient for our system, and we collected a total of 11,435 DFT-computed data to qualitatively describe the quaternary Li-Nb-V-O composition-structure space. The thermodynamic phase stability of the candidates in this pool of data was then evaluated by means of plotting a convex hull where we screened the materials whose hull distance was less than 30 meV/atom. Through this screening process, we identified six different stoichiometries which were then subjected to more detailed analysis (see **Results and Discussions** section). The first quantity that we compute is the theoretical capacity Q_{max} , and our screening criterion for selecting structures



for the next stage was $Q_{\max} \geq 400 \text{ mAh g}^{-1}$. In the next step, we chose candidates having band gap values smaller than 2.0 eV. In the next step, we carry out multiple other cathode property calculations including volume change, average voltage profile, mechanical and dynamical (only selected compositions due to computational cost) stability, Li^+ migration pathways, and high-temperature stability. Finally, combining all this information, we propose the best candidates as cathode materials along with a design strategy to search for even better possible cathode materials.

3 Results and discussions

3.1 0K phase stability and crystal structures

To determine the thermodynamic phase stability at 0K and to identify novel (meta-)stable structures along the LiVO_2 - Li_3NbO_4 pseudobinary tieline, we calculate a convex hull where the end members are Li_3NbO_4 and LiVO_2 . The formation energy E_f of any stoichiometry in this tieline are calculated as

$$E_f[(\text{LiVO}_2)_x(\text{Li}_3\text{NbO}_4)_{(1-x)}] =$$

$$E[(\text{LiVO}_2)_x(\text{Li}_3\text{NbO}_4)_{(1-x)}] - xE[\text{LiVO}_2] - (1-x)E[\text{Li}_3\text{NbO}_4], \quad (1)$$

where $E[\text{LiVO}_2]$ and $E[\text{Li}_3\text{NbO}_4]$ are the DFT computed total energy of the $R3m$ - LiVO_2 and $I43m$ - Li_3NbO_4 structures, taken from the Materials Project (MP) database^{31,32} and subsequently optimized with the same DFT settings applied to all other structures. The computed convex hull based on a total of about 10,000 DFT-optimized crystal structures that include both (i) available data in public databases and (ii) our own generated structures based on AIRSS, GAs, and ENUM, is shown in Figure 2 with points colored by the provenance of each structure.

We identify five chemical compositions, along with an experimentally known stoichiometry, which are within 30 meV/atom of the convex hull, as marked by the yellow dashed horizontal line in Figure 2, which is a reasonable choice of synthesisability of a material in high-throughput studies^{33,63-65}. Of these six phases, four were identified with the GA and two with ENUM. The predicted ground-state structures for all six compositions, which exhibit a disordered rock-salt crystal structure, are shown in Figure 3 along with their effective space group. Further details about them are provided in Table 1 and Table 2 and an extended convex hull plot is provided in the SI (Fig. S1).

3.2 Theoretical capacity

The theoretical capacity Q_{\max} is an important metric for the design and discovery of novel cathode materials, as it reflects the battery capacity in terms of storing charged ions such as Li^+ . We calculate Q_{\max} for all our six selected stoichiometries to gain insights into their charging capacity. To estimate Q_{\max} , we use the following equation

$$Q_{\max} = \frac{nF}{3600 \times M_w} \times 1000 \text{ mAh g}^{-1}. \quad (2)$$

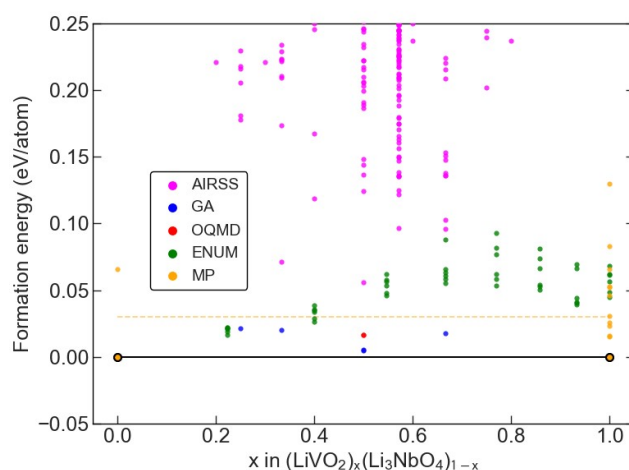


Fig. 2 Convex hull diagram. Convex hull plot along the pseudobinary tieline of LiVO_2 and Li_3NbO_4 showing the formation energy (eV/atom) versus composition along the tieline. The different colors represent the different data sources. The dashed horizontal line is the 30 meV/atom limit on the formation energy, which we take as the 0K thermodynamic limit.

Here, n represents the number of charge carriers, F is the Faraday constant, and M_w is the molecular weight of the material. Using Eq. 2, we estimate the value of Q_{\max} for all six stoichiometries in this work. The results are shown in Figure 4. We observe an almost linear behavior of the Q_{\max} with composition x on the LiVO_2 - Li_3NbO_4 pseudobinary tieline. This observation suggests that higher Q_{\max} can be obtained towards the Li_3NbO_4 -rich side of the LiVO_2 - Li_3NbO_4 pseudobinary tieline. Comparing the computed Q_{\max} values with those of known cathode materials suggests that the novel stoichiometries are found to outperform others by having higher capacities. However, we note that the experimental capacity of $\text{Li}_5\text{NbV}_2\text{O}_8$ is lower than the computed Q_{\max} (Fig. 4). There could be many factors behind this, since the experimental measurement of electrochemical performance depends on optimising the device used for the testing, which is highly dependent on selecting the correct mixture of active phase, carbon and polymer, and the protocol used for dispersing these, which are not included in our theoretical calculations.

3.3 Electronic structure, density of states, and band gap

The electronic band structure provides useful information about the occupancy of the electronic energy levels of an electron within the solid. In Figure 5 we compile the electronic band structures and the total and element-decomposed density of states (DOS) of all the novel phases discovered in this work. The calculated band structures of the end members ($R3m$ - LiVO_2 and $I43m$ - Li_3NbO_4) are shown in the SI (Fig. S2), and the presence of high-energy V 3d states in the valence band makes the band gap of LiVO_2 significantly lower than that of Li_3NbO_4 . One may expect that the intermediate stoichiometries that lie along the $R3m$ - LiVO_2 and $I43m$ - Li_3NbO_4 pseudobinary tieline would also have a reduced band gap compared to that of Li_3NbO_4 . Interestingly, for $\text{Li}_{2.3}\text{Nb}_7\text{V}_2\text{O}_{32}$ (Figure 5a) we observe flat bands corresponding to V 3d states



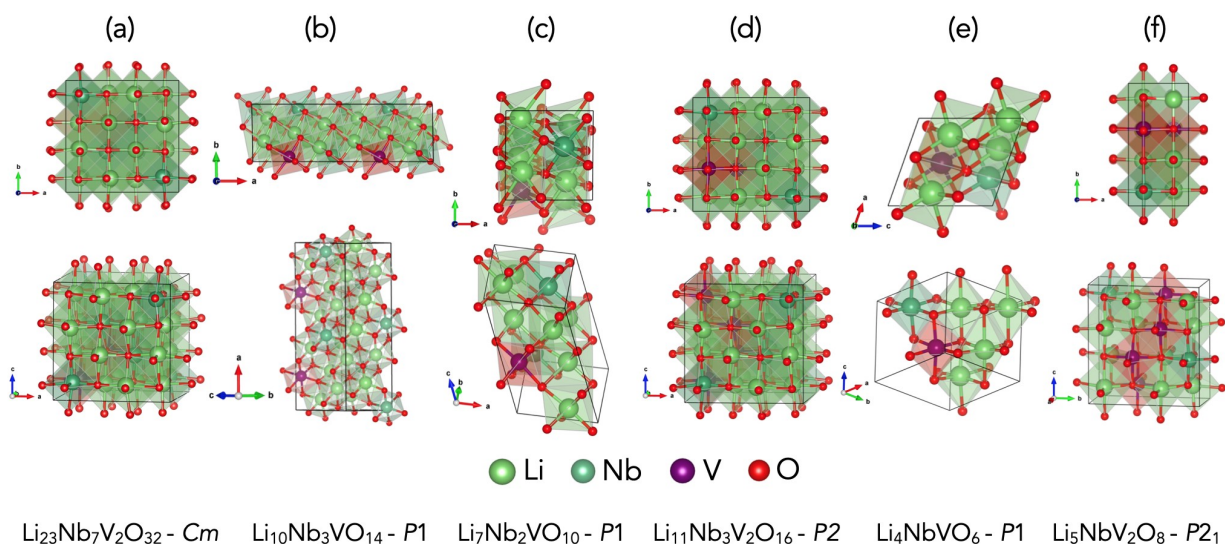


Fig. 3 Predicted ground state crystal structures. Ground state crystal structures found by different crystal structure prediction algorithms whose formation energy value lies within 30 meV/atom from the convex hull of LiVO_2 - Li_3NbO_4 pseudobinary tieline.

Table 1 Chemical formula, composition, hull distance, space group, and provenance of the six crystal structures identified using our computational framework that are predicted to be synthesisable.

Chemical formula	x in $(\text{LiVO}_2)_x (\text{Li}_3\text{NbO}_4)_{(1-x)}$	Hull distance (E_{hull}) (meV/atom)	Space group	Provenance (eV)
$\text{Li}_{23}\text{Nb}_7\text{V}_2\text{O}_{32}$	0.22	16.5	<i>Cm</i>	ENUM
$\text{Li}_{10}\text{Nb}_3\text{VO}_{14}$	0.25	21.3	<i>P1</i>	GA
$\text{Li}_7\text{Nb}_2\text{VO}_{10}$	0.33	20.2	<i>P1</i>	GA
$\text{Li}_{11}\text{Nb}_3\text{V}_2\text{O}_{16}$	0.40	26.4	<i>P2</i>	ENUM
Li_4NbVO_6	0.5	5.0	<i>P1</i>	GA
$\text{Li}_5\text{NbV}_2\text{O}_8$	0.67	17.5	<i>P2</i> ₁	GA

Table 2 Optimized conventional unit cell lattice parameters of different stoichiometries.

Chemical formula	a (Å)	b (Å)	c (Å)	α (deg)	β (deg)	γ (deg)
$\text{Li}_{23}\text{Nb}_7\text{V}_2\text{O}_{32}$	8.506	8.378	8.506	90.0	90.0	90.0
$\text{Li}_{10}\text{Nb}_3\text{VO}_{14}$	15.914	5.207	6.567	103.5	90.5	90.9
$\text{Li}_7\text{Nb}_2\text{VO}_{10}$	5.172	5.322	7.769	70.5	108.3	95.5
$\text{Li}_{11}\text{Nb}_3\text{V}_2\text{O}_{16}$	8.571	8.326	8.529	90.0	90.0	90.0
Li_4NbVO_6	5.116	5.145	5.183	100.5	78.3	61.9
$\text{Li}_5\text{NbV}_2\text{O}_8$	4.079	8.297	8.830	90.0	90.0	90.0



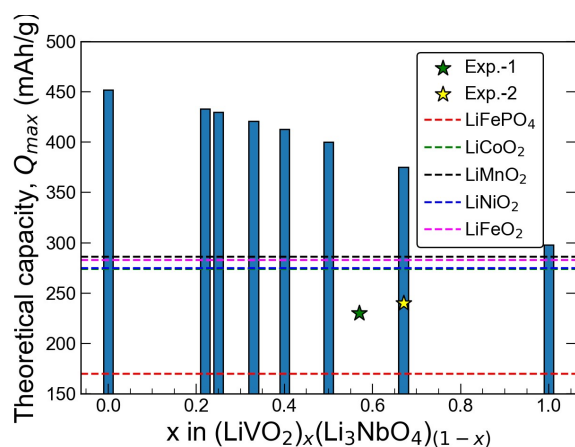


Fig. 4 Theoretical capacity as a function of composition. Theoretical capacity as a function of composition along the LiVO_2 - Li_3NbO_4 tieline. Exp.-1 and Exp.-2 values are taken from Ref. ²¹ and Ref. ²³, respectively.

(black solid lines) both above and below the Fermi level. We rationalize this observation by noting that the small amount of V atoms per cell act as an impurity in $\text{Li}_{23}\text{Nb}_7\text{V}_2\text{O}_{32}$, giving rise to the flat bands that significantly reduce the gap of the system compared to the end member materials. As the relative amount of V atoms increases by adding more LiVO_2 to Li_3NbO_4 , the flat bands broaden. We also observe that the total DOS near the top of the valence band, arising mostly from V $3d$ states, increases almost linearly with increasing LiVO_2 composition, approaching the DOS of LiVO_2 . Overall, doping Li_3NbO_4 with a minimal amount of V atoms leads to a decrease in band gap, and observation that may serve as a design rule for the discovery of novel cathode materials.

The band gap of a material is directly related to its electronic conductivity, and the electronic resistance of electrode materials can be analyzed using DOS plots. For an ideal cathode material, the band gap should be as small as possible, ideally a metallic one so that electrons can move freely without any resistance. In this work, we compute the band gap with DFT+ U for all the novel stoichiometries from their difference between CBM and VBM in the band structures shown in Figure 5. We show the computed band gaps in Figure 6(a). For all structures, the band gap is below 2.0 eV, which is significantly lower compared to that of $R3m$ - LiVO_2 and $I43m$ - Li_3NbO_4 , and also comparable to the gap of other well-known cathode materials^{66–68}. Note that the band gap values that we report here correspond to the fully lithiated structures and thus represent the theoretical upper limit, which may nonetheless be difficult to achieve in reality. For completeness, we also computed the band gap of the fully delithiated structures (theoretical lower limit) where band gaps are fully closed due to their metallic nature. Therefore, we expect that the newly proposed stoichiometries will have lower band gaps for practical applications compared to the values reported here. Overall, the lower band gaps found in all the stoichiometries, especially at low LiVO_2 content ($\text{Li}_{23}\text{Nb}_7\text{V}_2\text{O}_{32}$), further endorses the potential of these compositions as cathode materials.

3.4 Volumetric change

Low volumetric changes of the electrode materials are desired to minimise the risk of dewetting and cracking of an ASSB battery during cycling. To estimate the change in volume upon full lithiation/delithiation in the new promising stoichiometries, we use the following expression³³:

$$\Delta V = \frac{V_{\text{de}} - V_0}{V_0} \times 100\%, \quad (3)$$

where V_{de} and V_0 represent the volume of the cell upon full delithiation and lithiation (the predicted original structure in this work), respectively. Consequently, ΔV represents the maximum theoretical limit of volume change of the cathode materials during actual battery application. Using this equation, we compute the ΔV value for all six stoichiometries (along with the end members for comparison) and the results are shown in Figure 6(b). We see that, except for the experimentally known stoichiometry of $\text{Li}_5\text{NbV}_2\text{O}_8$, all other five novel stoichiometries have ΔV values smaller than 7.5%, which indicates their notable structural stability upon full lithiation/delithiation as compared to many other known cathode materials^{8,69}. The overall small volume change observed in our calculations for LiNbVO is consistent with the work of Yabuuchi and co-workers²³, where they attributed the small volume change with the migration of V atoms into small and narrow tetrahedral sites. This process leads to an increase in the electrostatic interaction in LiNbVO and as a result, the crystal lattice expands upon Li extraction, a feature we also observe in our calculations that results in a positive ΔV in most cases.

3.5 Average voltage

Electrochemical average voltages for the new structures were calculated from the available DFT total energies. The average voltage \bar{V} for a given stoichiometry, $\text{Li}_{x_1}\text{NbVO}$ and $\text{Li}_{x_2}\text{NbVO}$ with $x_1 > x_2$, is given by⁷⁰:

$$\bar{V} = -\frac{\Delta G}{(x_1 - x_2)F} \approx -\frac{\Delta E}{(x_1 - x_2)F} \quad (4)$$

$$= -\frac{E(\text{Li}_{x_1}\text{NbVO}) - E(\text{Li}_{x_2}\text{NbVO}) - (x_1 - x_2)E(\text{Li})}{(x_1 - x_2)F} \quad (5)$$

$$= -\frac{E(\text{Li}_{x_1}\text{NbVO}) - E(\text{NbVO}) - (x_1)E(\text{Li})}{(x_1)F} \quad (6)$$

$E(\text{Li}_{x_1}\text{NbVO})$ and $E(\text{NbVO})$ are the DFT-computed total energies of the fully lithiated and delithiated phases, respectively. In Eq. 4, we set $x_2 = 0$ assuming all the Li ions are removed from the structure, yielding a simple approximation to \bar{V} compared to a complete piece-wise approximation to the voltage curve^{33,69,71}. The computed value of \bar{V} for all six stoichiometries is shown in Figure 6(c). We find that stoichiometries with a smaller LiVO_2 content have a higher \bar{V} . The experimentally known stoichiometry, $\text{Li}_5\text{NbV}_2\text{O}_8$, has the lowest value of \bar{V} . The calculated achievable values of \bar{V} for the stoichiometries on the Li_3NbO_4 -rich side compare well to other well-known cathode materials^{8,69}, encouraging further work to find even higher \bar{V} values and suggesting a design rule for the discovery of improved cathode materials.



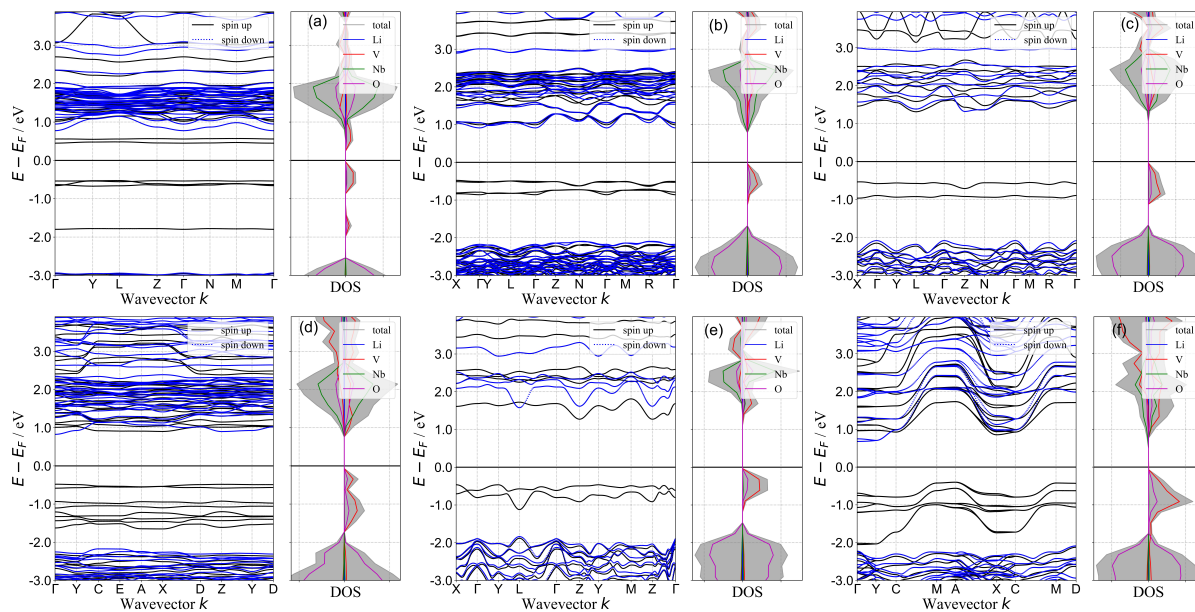


Fig. 5 Band structure and density of states plots. Electronic band structure and element-decomposed density of states of (a) $\text{Li}_{23}\text{Nb}_7\text{V}_2\text{O}_{32}$ (b) $\text{Li}_{10}\text{Nb}_3\text{VO}_{14}$ (c) $\text{Li}_7\text{Nb}_2\text{VO}_{10}$ (d) $\text{Li}_{11}\text{Nb}_3\text{V}_2\text{O}_{16}$ (e) Li_4NbVO_6 and (f) $\text{Li}_5\text{NbV}_2\text{O}_8$ structures.

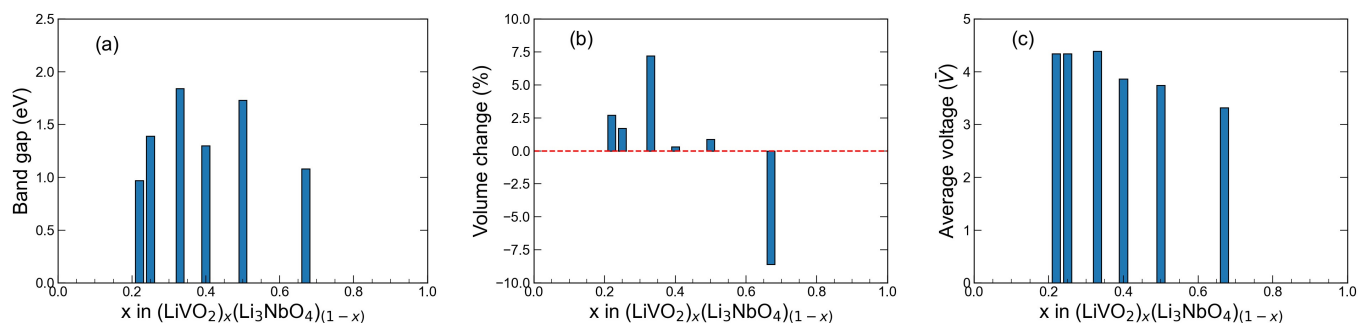


Fig. 6 Band gap, volume change and average voltage plots. (a) Band gap, (b) volume change upon full delithiation and (c) average voltage upon full delithiation for the predicted stoichiometries in this work.



Table 3 Average mechanical properties: Bulk Modulus B (in GPa), Shear Modulus G (in GPa), Pugh's Ratio B/G , Young's Modulus E (in GPa), and Poisson's Ratio ν for different stoichiometries.

Chemical formula	B	G	B/G	E	ν
$\text{Li}_{23}\text{Nb}_7\text{V}_2\text{O}_{32}$	97.4	58.0	1.68	145.3	0.25
$\text{Li}_{10}\text{Nb}_3\text{VO}_{14}$	97.6	63.2	1.54	156.0	0.23
$\text{Li}_7\text{Nb}_2\text{VO}_{10}$	52.3	36.8	1.42	89.5	0.21
$\text{Li}_{11}\text{Nb}_3\text{V}_2\text{O}_{16}$	98.5	60.8	1.62	151.4	0.24
Li_4NbVO_6	106.5	70.1	1.52	172.4	0.23
$\text{Li}_5\text{NbV}_2\text{O}_8$	109.7	81.6	1.34	196.1	0.20

Here it is to be noted that to calculate a typical piece-wise voltage profile for every novel stoichiometry, finding a ground state is required for the new composition emerged upon removal of Li^+ from the host stoichiometry. However, this is a challenging task, as the solid-solutions phases are metastable at 0K and more advanced computational techniques such as DFT-based cluster expansion together with grand canonical Monte Carlo simulations⁷⁰ are necessary to identify such phases, which are not included in this work. Therefore, we provided a rather simple, but insightful criterion, "average" voltage values to compare our candidate materials, which has also been used successfully in other studies^{33,69,71}. Full open-circuit voltage profiles can be computed for comparing with the measured ones when the candidate materials are synthesised, but they are not crucial at this point to evaluate the potential of different stoichiometries.

3.6 Mechanical stability

One of the primary reasons for the degradation of cathode materials of LIBs is the phase transformation that may take place during the charge-discharge process. A phase transformation can happen if the structure is mechanically unstable, while a mechanically stable structure can go through many charge-discharge cycles improving the lifetime of the material. In order to estimate the mechanical stability of the newly identified stoichiometries, we calculate their elastic constants C_{ij} and derive relevant mechanical properties that are useful for the design of cathode materials and that can be compared directly with experiments. The computed values of C_{ij} for all stoichiometries are listed in the SI Sec. III. All our structures turn out to be mechanically stable according to stability criteria laid down by Mouhat and co-workers⁷², confirming that these structures may go through many charge-discharge cycles as required for promising cathode materials. Moreover, we find that the values of C_{11} , C_{22} , and C_{33} are significantly higher than the values of C_{44} , C_{55} , and C_{66} for all six stoichiometries, suggesting strong resistance to uniaxial stress implying that shear deformations are more likely to occur⁷³, as observed in other Li-ion cathode materials^{74,75}.

From the values of C_{ij} , we further calculate the bulk modulus B , the shear modulus G , Pugh's Ratio B/G , Young's modulus E , and Poisson's Ratio ν . These parameters play a critical role in determining the mechanical stability against an external force change and ductility of materials. In this work, we use the Voigt-Reuss-Hill (VRH) approximation^{76,77} to calculate the polycrystalline properties, which is the average of the Voigt and Reuss equations representing the upper and lower limits of the poly-

crystalline constants, respectively. The values of E and ν are then deduced using the following relationships^{76,77}:

$$E = \frac{9BG}{3B + G} \quad (7)$$

$$\nu = \frac{3B - 2G}{6B + 2G} \quad (8)$$

All the values of these polycrystalline properties are listed in Table 3. The B and G moduli are a measure of resistance to volume change by an applied pressure and a measure of resistance to reversible deformations upon shear stress, respectively. E represents the ratio of stress and strain and can reflect the hardness of materials. For all our stoichiometries, we note that the values of B are much larger than the corresponding values of G , suggesting that they have a higher resistance to volume deformations under hydrostatic pressure, which is also observed in other Li-ion cathode materials^{74,75}. Another important empirical metric used to characterize the brittle-ductility behavior of materials is Pugh's ratio B/G ⁷⁸. A high B/G ratio is associated with ductility, whereas a low value generally represents brittleness. The critical value distinguishing the two behaviors is found by Ravindran and co-workers⁷⁹ and fixed to about 1.75. The Poisson ratio ν indicates the covalent nature of materials⁸⁰ and higher values of ν are associated with better elastic properties⁷⁵.

Interestingly, we find that moving towards the Li_3NbO_4 -rich side, B , G , and E decrease but B/G and ν increase. The relatively lower values of B , G , and E for Li_3NbO_4 -rich compositions indicate that they possess improved mechanical properties, whereas the higher values of B/G and ν indicate that they exhibit more ductile character helping reduce Li dendrite formation role, a key advantage for ASSB applications. This suggests that, the newly discovered stoichiometries towards the Li_3NbO_4 -rich side of the LiVO_2 - Li_3NbO_4 pseudobinary tieline will have better mechanical properties than the experimentally known stoichiometries of $\text{Li}_{1.3}\text{Nb}_{0.3}\text{V}_{0.4}\text{O}_2$ ²¹ and $\text{Li}_{1.25}\text{Nb}_{0.25}\text{V}_{0.5}\text{O}_2$ ²³ with $\text{Li}_{23}\text{Nb}_7\text{V}_2\text{O}_{32}$ having the best ductile properties. Our results further suggest that it may be possible to search for even more ductile materials by considering more Li_3NbO_4 -rich compositions for which B/G can reach values up to 1.75 and higher and thus may serve as a design rule for finding cathode materials with improved mechanical properties.

3.7 Dynamical stability

Figure 7 shows the phonon dispersion and corresponding density of states (DOS) calculated under the harmonic approximation for two of our most promising stoichiometries: (a) $\text{Li}_{23}\text{Nb}_7\text{V}_2\text{O}_{32}$ and (b) Li_4NbVO_6 . The absence of imaginary modes indicates that these two structures are dynamically stable, with no predicted phase transitions. We note that there is an imaginary mode with small frequency near Γ approaching from the $(0,0,0.5)$ point for $\text{Li}_{23}\text{Nb}_7\text{V}_2\text{O}_{32}$, but this can be attributed to an artifact of the Fourier interpolation which could only be removed by calculating explicit dynamical matrices on a finer grid in this direction, but this is computationally very expensive given the size of our disordered supercell and should not impact our conclusion that both



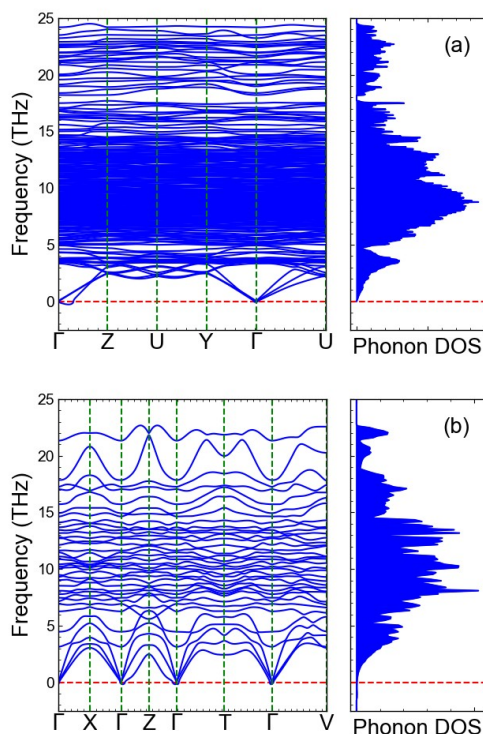


Fig. 7 Phonon dispersion plots. Phonon dispersion under the harmonic approximation and the corresponding density of states for (a) $\text{Li}_{23}\text{Nb}_7\text{V}_2\text{O}_{32}$ and (b) Li_4NbVO_6 . The absence of imaginary frequencies confirms the dynamical stability of the structures.

of these structures are dynamically stable.

3.8 Kinetics of Li^+ transport

Understanding the kinetics of Li^+ transport is crucial for the design of any battery component. Atomistic mechanisms of Li^+ transport, such as diffusion pathways and corresponding activation barriers, can provide useful information that is otherwise difficult to obtain from experiments. Over the past few decades, the kinetic transport of several Li-excess transition-metal oxide cathodes and anodes has been well studied based on percolation theory^{81–86}. In this work, we have mainly utilized three common methodologies to get a qualitative understanding of atomistic diffusion processes in these materials: (i) AIMD (ii) CINEB, and (iii) BVSE. We initially ran a 40 ps computationally expensive AIMD simulation on the various stoichiometries with and without Li^+ vacancies at low (600 K), medium (1000 K) and high (1400 K) temperatures (Fig. S9). In all cases, we did not find significant Li^+ movement during the 40 ps run, revealing the sluggish nature of Li^+ diffusion in these materials, likely owing to the rock-salt crystal framework. This is in good agreement with previous reports on Li_3NbO_4 ⁸⁷ and LiVO_2 ⁸⁸. Next, we used another computationally expensive technique called the CI-NEB method on the simplest stoichiometry, Li_4NbVO_6 , containing only 12 atoms in the unit cell with 4 unique Li sites. We chose this stoichiometry for the convenience of CI-NEB calculations where identifying predefined diffusion pathways is a requirement. However, a few of our stoichiometries contain large supercells where identifying unique

Li sites and enumerating all possible corresponding unique diffusion pathways is a challenging task. Therefore, in the last step we used a computationally inexpensive BVSE approach to qualitatively estimate diffusion barriers and reaction pathways in these complex disordered materials.

In Figure 8, we compile our CI-NEB and BVSE findings for Li_4NbVO_6 to benchmark these two methods. The results for the remaining stoichiometries are shown in Figs. S3–S7 in the SI (BVSE-computed full diffusion pathways and corresponding diffusion barriers). Figure 8(a) represents the unit cell of the Li_4NbVO_6 crystal structure with four symmetrically unique Li sites marked on it. The various possible elementary Li^+ jumps are marked with different colors. In Figure 8(b), CI-NEB computed Li^+ migration barriers are shown with the same color coding that represents the different elementary Li^+ hops in Figure 8(a). The lowest CI-NEB barrier is found for the $\text{Li1} \rightarrow \text{Li4} \rightarrow \text{Li1} \rightarrow \text{Li4}$ pathway along the (001) direction, with an activation barrier of 0.559 eV (Path-3). The full $\text{Li1} \rightarrow \text{Li4} \rightarrow \text{Li1} \rightarrow \text{Li4}$ pathway can be easily visualized in Figure 8(c) in a larger supercell, marked by black arrows.

For the other stoichiometries, as mentioned earlier, we have a more complex spatial distribution of Li, Nb, and V ions in a rather large unit cell, making the CI-NEB approach unfeasible. Therefore, we use the BVSE method which is computationally fast and provides useful information for complex disordered materials. Since BVSE is rather less accurate in estimating activation barriers than CI-NEB, we first compare the BVSE-computed activation barrier for 1D, 2D, and 3D percolation networks and also the MEP with that of the CI-NEB computed results. In Figure 8(d) we show the BVSE produced Li^+ pathway and the corresponding activation barriers for 1D, 2D, and 3D percolation networks which are 1.13 eV, 1.33 eV, and 1.70 eV, respectively. These values are significantly overestimated as compared to the CI-NEB computed value of 0.559 eV, likely due to the use of rigid structures in BVSE as opposed to CI-NEB. This suggests that BVSE computed diffusion barriers may act as an upper limit; however, the BVSE method does correctly identify the MEP for Li^+ along the (001) direction (marked by black arrows in Figure 8(e)) in agreement with the CI-NEB method. This endorses the suitability of the BVSE method for a qualitative comparison of the activation barriers corresponding to 1D, 2D, and 3D Li^+ percolation networks for our other complex stoichiometries. The resulting BVSE activation barriers of Li^+ migration are compiled in Table 4.

We highlight that the end member materials of the LiVO_2 - Li_3NbO_4 tieline, that is, LiVO_2 and Li_3NbO_4 , have a rather high Li^+ activation energy barrier^{87,88} as compared to some of our stoichiometries discovered in this work. In particular, the lowest activation energy path for Li_3NbO_4 is found to be 1.13 eV⁸⁷ and Panchmatia and co-workers reported that stoichiometric LiVO_2 does not have mobile Li^+ ⁸⁸. They were, however, able to increase Li^+ mobility in lithiated non-stoichiometric LiVO_2 compounds. In this regard, our Li_3NbO_4 -rich compounds, such as $\text{Li}_{23}\text{Nb}_7\text{V}_2\text{O}_{32}$, appear more promising as evidenced by BVSE computed low 1D, 2D, and 3D percolation network Li^+ migration barriers, likely due to the presence of a small amount of V doping. However, further study is required to get a complete picture of atomic diffusion



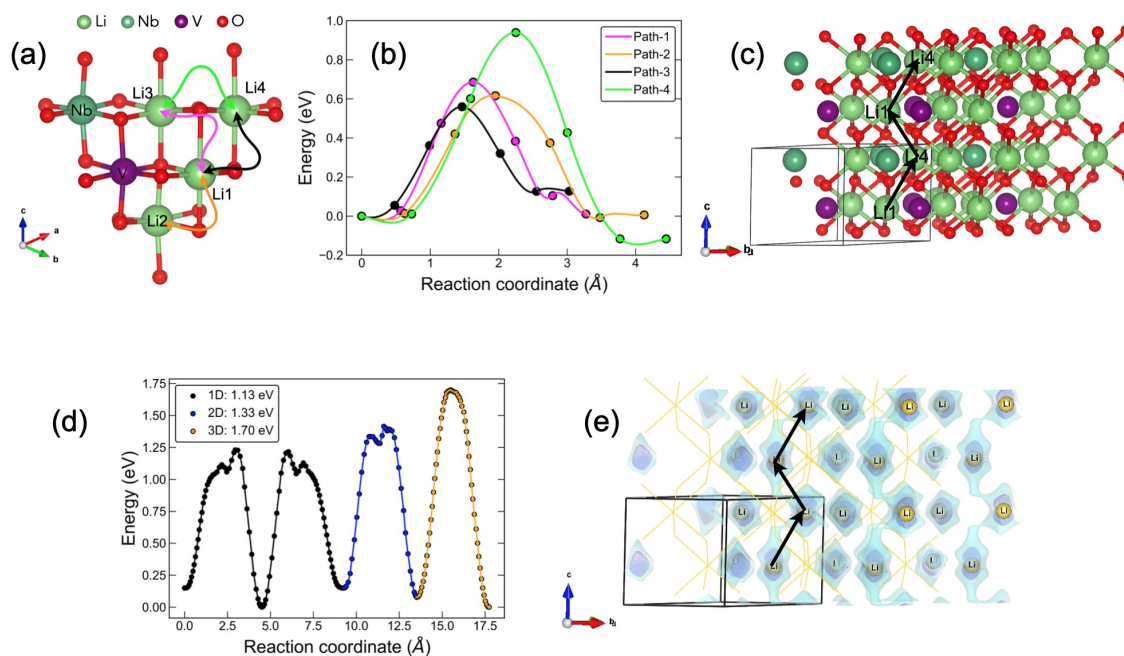


Fig. 8 Schematic overview of the Li^+ diffusion in Li_4NbVO_6 . (a) Unit cell of Li_4NbVO_6 showing all possible elementary Li^+ hops colored according to their diffusion barriers. (b) DFT-CI-NEB computed energy barriers where the different colors correspond to the elementary jumps shown in (a). (c) The long-range minimum energy pathway for Li^+ ($\text{Li1} \leftrightarrow \text{Li4}$) is shown in a $2 \times 2 \times 2$ supercell identified to be along the (001) direction marked by black arrows. (d) BVSE computed Li^+ migration pathway for 1D, 2D, and 3D percolation network with corresponding activation barriers. (e) 3D network of Li^+ pathways (blue isosurface) calculated by BVSE. The minimum energy pathway for Li^+ migration is identified to be along the (001) direction (marked by black arrows) and matches exactly with the CI-NEB results shown in (c).

Table 4 Overall activation energy barrier for the 1D, 2D, and 3D percolation network of Li^+ migration in the different novel stoichiometries estimated by BVSE.

Chemical formula	1D (eV)	2D (eV)	3D (eV)
$\text{Li}_{23}\text{Nb}_7\text{V}_2\text{O}_{32}$	0.61	0.62	0.63
$\text{Li}_{10}\text{Nb}_3\text{VO}_{14}$	0.76	0.98	1.41
$\text{Li}_7\text{Nb}_2\text{VO}_{10}$	1.01	1.09	1.33
$\text{Li}_{11}\text{Nb}_3\text{V}_2\text{O}_{16}$	0.75	0.77	0.91
Li_4NbVO_6	1.13	1.33	1.70
$\text{Li}_5\text{NbV}_2\text{O}_8$	1.18	1.34	3.40

processes and how to enhance Li^+ movement in these promising stoichiometries.

3.9 High-temperature stability

For practical applications, cathode materials may need to operate at high temperatures, particularly in an ASSLIB setting, which can cause severe damage if the underlying crystal framework is not stable at that temperature. We use AIMD simulations at 600 K to investigate the impact of temperature on our newly discovered materials. From the AIMD trajectories, we compute the radial distribution function (RDF) of Nb-Nb and Nb-V at 0 ps and at 10 ps. We focus on these two pairs of atoms as they provide more insights into the overall structural stability during charging/discharging cycles at high temperatures compared to other pairings. Our results are shown in Figure 9. We observe sharp peaks for both Nb-Nb and Nb-V pairs for all the stoichiometries after running for 10 ps at 600 K indicating the crystalline struc-

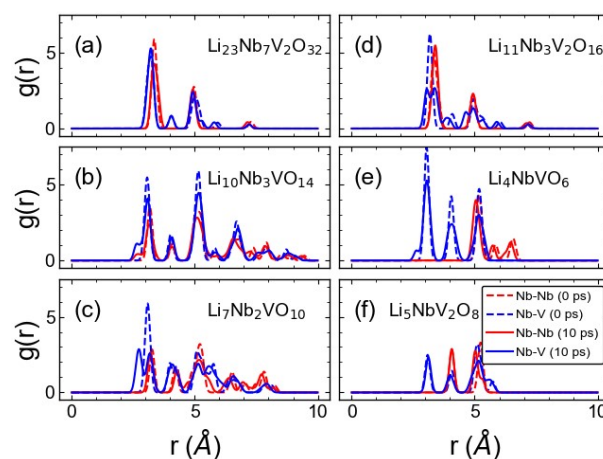


Fig. 9 Radial distribution function plots. Radial distribution function between Nb-Nb (red) and Nb-V (blue) of (a) $\text{Li}_{23}\text{Nb}_7\text{V}_2\text{O}_{32}$ (b) $\text{Li}_{10}\text{Nb}_3\text{VO}_{14}$ (c) $\text{Li}_7\text{Nb}_2\text{VO}_{10}$ (d) $\text{Li}_{11}\text{Nb}_3\text{V}_2\text{O}_{16}$ (e) Li_4NbVO_6 and (f) $\text{Li}_5\text{NbV}_2\text{O}_8$ structures at 0 ps (dashed line) and 10 ps (solid line) obtained from AIMD simulations at 600 K.



ture framework is preserved. This finding is further supported by the total energy variation with AIMD steps (Fig. S8 in SI). These results suggest that all our newly discovered structures are expected to have good thermal stability, ensuring the safety aspect for commercial battery applications.

In Table 5, we summarize our key findings. For all six promising stoichiometries, we report their corresponding property values with the * mark representing the best value among the six stoichiometries. Overall, we find that the $\text{Li}_{23}\text{Nb}_7\text{V}_2\text{O}_{32}$ composition gets the highest number of * marks, excluding the mechanical/dynamical/high-temperature stability which is common to all the six stoichiometries. This indicates that $\text{Li}_{23}\text{Nb}_7\text{V}_2\text{O}_{32}$ is likely to be the best candidate as a cathode material for all-solid-state Li-ion battery applications.

4 Conclusions

We present a comprehensive and systematic study of first-principles crystal structure prediction calculations on the LiVO_2 - Li_3NbO_4 tieline to identify novel stoichiometries with improved properties that can be used as cathode materials for ASSLIB applications. It is to be, however, noted that the applications of these materials are not limited to ASSLIBs and can be used for other conventional rechargeable Li-ion batteries which makes them even more potential candidate materials for battery applications. Based on the thermodynamic stability criterion applied over more than 10,000 DFT-computed structures, we identify five novel stoichiometries, $\text{Li}_{23}\text{Nb}_7\text{V}_2\text{O}_{32}$, $\text{Li}_{10}\text{Nb}_3\text{VO}_{14}$, $\text{Li}_7\text{Nb}_2\text{VO}_{10}$, $\text{Li}_{11}\text{Nb}_3\text{V}_2\text{O}_{16}$, Li_4NbVO_6 , along with an experimentally known stoichiometry, $\text{Li}_5\text{NbV}_2\text{O}_8$, all having a rock-salt crystal structure. From our calculations, we predict that all of them have promising cathode properties, and highlight the largely unexplored Li_3NbO_4 -rich side as having improved properties compared to the LiVO_2 -rich side. We predict that $\text{Li}_{23}\text{Nb}_7\text{V}_2\text{O}_{32}$ will have the best properties among all the stoichiometries considered in this work, having higher capacity, higher average voltage, lower band gap and lower activation barrier (see Table 5). Our work illustrates how theoretical calculations for the prediction of novel vanadium-niobate-based cathode materials can guide experimental synthesis, and paves the way for the discovery of other disordered ASSLIB cathode materials.

Data availability

The main data supporting the findings of this study are available within the paper and its Supplementary Information. Further numerical data are available from the authors upon reasonable request. All the DFT-optimized structure files are available in the GitHub repository: https://github.com/bkarasulu/Li-V-Nb-O_structures.

Code availability

All the major codes, except for VASP (see <https://www.vasp.at/>) which requires a license, used in this work are publicly-available such as AIRSS (see <https://airss-docs.github.io/>) and USPEX (see <https://uspex-team.org/en>) for crystal structure prediction, MATA-DOR for high-throughput work, database management and

convex hull plot (see <https://matador-db.readthedocs.io/en/latest/>), PYMATGEN for electronic structure and radial distribution function analysis (see <https://pymatgen.org/>), PHONOPY for phonon analysis (see <https://phonopy.github.io/phonopy/>), VASPKIT for mechanical property calculations (see <https://vaspkit.com/>), ASE for CI-NEB and general purpose use (see <https://wiki.fysik.dtu.dk/ase/>) and SOFTBV for diffusion pathway analysis (see <https://www.dmse.nus.edu.sg/asn/softBV-GUI.html>). The in-house configuration enumeration code used for CSP can be made available upon request from the corresponding authors.

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Author contributions

T.C. and B.K. contributed to the conception and design of this study, and T.C. was responsible for performing the calculations and detailed analysis. B.M. performed one of the phonon calculations and provided critical feedback regarding phonon analysis. A.T. and R.I.W. contributed to the initial discussion. T.C. drafted the original manuscript, which was then reviewed and revised by all the co-authors. All authors reviewed and approved the manuscript prior to submission.

Competing interests

The authors declare no competing interests.

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Table 5 All the computed properties of the novel stoichiometries discovered in this work. The * mark represents the best value for a given property. The band gap value without parenthesis and with parenthesis represent the indirect and direct band gap, respectively.

Chemical formula	E_{hull} (meV/atom)	Q_{max} (mAh/g)	V (V)	Band gap (eV)	ΔV (%)	Mechanically stable ?	Dynamically stable ?	High-T stable ?	Activation barrier (eV)
$\text{Li}_{23}\text{Nb}_7\text{V}_2\text{O}_{32}$	16.5	433*	4.34*	0.97 (0.98)*	+2.7	✓	✓	✓	0.61*
$\text{Li}_{10}\text{Nb}_3\text{VO}_{14}$	21.3	430	4.34*	1.39 (1.50)	+1.7	✓	N/A	✓	0.76
$\text{Li}_7\text{Nb}_2\text{VO}_{10}$	20.2	421	4.39	1.84 (1.88)	+7.2	✓	N/A	✓	1.01
$\text{Li}_{11}\text{Nb}_3\text{V}_2\text{O}_{16}$	26.4	413	3.86	1.30 (1.43)	+0.3*	✓	N/A	✓	0.75
Li_4NbVO_6	5.0*	400	3.74	1.73 (1.76)	+0.9	✓	✓	✓	1.13
$\text{Li}_5\text{NbV}_2\text{O}_8$	17.5	375	3.32	1.08 (1.55)	-8.6	✓	N/A	✓	1.18

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