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## Optical cavities and quantum emitters

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# **OPTICAL CAVITIES AND QUANTUM EMITTERS**



# **OPTICAL CAVITIES AND QUANTUM EMITTERS**

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*Tomorrow, we will do beautiful things.*

-A. Gaudí



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