



UvA-DARE (Digital Academic Repository)

Learning from Samples of Variable Quality

Dehghani, M.; Mehrjou, A.; Gouws, S.; Kamps, J.; Schölkopf, B.

Publication date

2019

Document Version

Final published version

Published in

Learning from Limited Labeled Data

[Link to publication](#)

Citation for published version (APA):

Dehghani, M., Mehrjou, A., Gouws, S., Kamps, J., & Schölkopf, B. (2019). Learning from Samples of Variable Quality. In *Learning from Limited Labeled Data: ICLR 2019 Workshop OpenReview*. <https://openreview.net/forum?id=SkxwBgpmDE>

General rights

It is not permitted to download or to forward/distribute the text or part of it without the consent of the author(s) and/or copyright holder(s), other than for strictly personal, individual use, unless the work is under an open content license (like Creative Commons).

Disclaimer/Complaints regulations

If you believe that digital publication of certain material infringes any of your rights or (privacy) interests, please let the Library know, stating your reasons. In case of a legitimate complaint, the Library will make the material inaccessible and/or remove it from the website. Please Ask the Library: <https://uba.uva.nl/en/contact>, or a letter to: Library of the University of Amsterdam, Secretariat, Singel 425, 1012 WP Amsterdam, The Netherlands. You will be contacted as soon as possible.

LEARNING FROM SAMPLES OF VARIABLE QUALITY

Mostafa Dehghani

University of Amsterdam
dehghani@uva.nl

Arash Mehrjou

MPI for Intelligent Systems
amehrjou@tuebingen.mpg.de

Stephan Gouws

Google Brain
sgouws@google.com

Jaap Kamps

University of Amsterdam
kamps@uva.nl

Bernhard Schölkopf

MPI for Intelligent Systems
bs@tuebingen.mpg.de

ABSTRACT

Training labels are expensive to obtain and may be of varying quality, as some may be from trusted expert labelers while others might be from heuristics or other sources of weak supervision such as crowd-sourcing. This creates a fundamental quality-versus-quantity trade-off in the learning process. Do we learn from the small amount of high-quality data or the potentially large amount of weakly-labeled data? We argue that if the learner could somehow know and take the label-quality into account, we could get the best of both worlds. To this end, we introduce “fidelity-weighted learning” (FWL), a semi-supervised student-teacher approach for training deep neural networks using weakly-labeled data. FWL modulates the parameter updates to a *student* network, trained on the task we care about on a per-sample basis according to the posterior confidence of its label-quality estimated by a *teacher*, who has access to limited samples with high-quality labels.

1 INTRODUCTION

“All samples are equal, but some samples are more equal than others.”

—Inspired by George Orwell quote, Animal Farm, 1945

The success of deep neural networks to date depends strongly on the availability of labeled data and usually it is much easier and cheaper to obtain small quantities of high-quality labeled data and large quantities of unlabeled data. For a large class of tasks, it is also easy to define one or more so-called “weak annotators” (Ratner et al., 2016), additional (albeit noisy) sources of *weak supervision* based on heuristics or weaker, biased classifiers trained on e.g. non-expert crowd-sourced data or data from different domains that are related. While easy and cheap to generate, it is not immediately clear if and how these additional weakly-labeled data can be used to train a stronger classifier for the task we care about.

Assuming we can obtain a large set of weakly-labeled data in addition to a much smaller training set of “strong” labels, the simplest approach is to expand the training set simply by including the weakly-supervised samples (all samples are equal). Alternatively, one may pretrain on the weak data and then fine-tune on strong data, which is one of the common practices in semi-supervised learning. We argue that treating weakly-labeled samples uniformly (i.e. each weak sample contributes equally to the final classifier) ignores potentially valuable information of the label quality (Dehghani et al., 2017c;b). Instead, we introduce Fidelity-Weighted Learning (FWL), a Bayesian semi-supervised approach that leverages a small amount of data with true labels to generate a larger training set with *confidence-weighted weakly-labeled samples*, which can then be used to modulate the fine-tuning process based on the fidelity (or quality) of each weak sample (Dehghani et al., 2018). By directly modeling the inaccuracies introduced by the weak annotator in this way, we can control the extent to which we make use of this additional source of weak supervision: more for confidently-labeled weak samples close to the true observed data, and less for uncertain samples further away from the observed data.

2 FIDELITY-WEIGHTED LEARNING (FWL)

In this section, we describe FWL. We assume we are given a large set of unlabeled data samples, a heuristic labeling function called the *weak annotator*, and a small set of high-quality samples labeled by experts, called the *strong dataset*, consisting of tuples of training samples x_i and their true labels y_i , i.e. $\mathcal{D}_s = \{(x_i, y_i)\}$. We consider the latter to be observations from the true target function that we are trying to learn. We use the weak annotator to generate labels for the unlabeled samples. Generated labels are noisy due to the limited accuracy of the weak annotator. This gives us the *weak dataset*

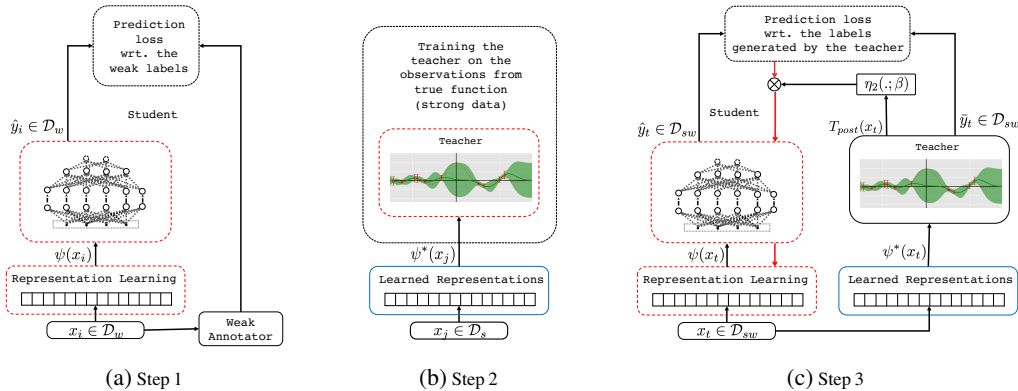


Figure 1: Illustration of Fidelity-Weighted Learning: Step 1: Pre-train student on weak data, Step 2: Fit teacher to observations from the true function, and Step 3: Fine-tune student on labels generated by teacher, taking the confidence into account. Red dotted borders and blue solid borders depict components with trainable and non-trainable parameters, respectively.

consisting of tuples of training samples x_i and their weak labels \tilde{y}_i , i.e. $\mathcal{D}_w = \{(x_i, \tilde{y}_i)\}$. Note that we can generate a large amount of weak training data \mathcal{D}_w at almost no cost using the weak annotator. In contrast, we have only a limited amount of observations from the true function, i.e. $|\mathcal{D}_s| \ll |\mathcal{D}_w|$.

Our proposed setup comprises a neural network called the **student** and a Bayesian function approximator called the **teacher**. The training process consists of three phases which we summarize in Figure 1.

Step 1 Pre-train the student on \mathcal{D}_w using weak labels generated by the weak annotator.

The main goal of this step is to learn a *task dependent* representation of the data as well as pretraining the student. The student function is a neural network consisting of two parts. The first part $\psi(\cdot)$ learns the data representation and the second part $\phi(\cdot)$ performs the prediction task (e.g. classification). Therefore the overall function is $\hat{y} = \phi(\psi(x_i))$. The student is trained on all samples of the weak dataset $\mathcal{D}_w = \{(x_i, \tilde{y}_i)\}$. For brevity, in the following, we will refer to both data sample x_i and its representation $\psi(x_i)$ by x_i when it is obvious from the context.

Step 2 Train the teacher on the strong data $(\psi(x_j), y_j) \in \mathcal{D}_s$ represented in terms of the student representation $\psi(\cdot)$ and then use the teacher to generate a soft dataset \mathcal{D}_{sw} consisting of $\langle \text{sample}, \text{predicted label}, \text{confidence} \rangle$ for all data samples.

We use a Gaussian process as the teacher to capture the label uncertainty in terms of the student representation, estimated w.r.t the strong data. A prior mean and covariance function is chosen for \mathcal{GP} . The learned embedding function $\psi(\cdot)$ in Step 1 is then used to map the data samples to dense vectors as input to the \mathcal{GP} . We use the learned representation by the student in the previous step to compensate lack of data in \mathcal{D}_s and the teacher can enjoy the learned knowledge from the large quantity of the weakly annotated data. This way, we also let the teacher see the data through the lens of the student.

The \mathcal{GP} is trained on the samples from \mathcal{D}_s to learn the posterior mean \mathbf{m}_{post} (used to generate soft labels) and posterior co-variance $K_{\text{post}}(\cdot, \cdot)$ (which represents label uncertainty)¹. We then create the *soft dataset* $\mathcal{D}_{sw} = \{(x_t, \tilde{y}_t)\}$ using the posterior \mathcal{GP} , input samples x_t from $\mathcal{D}_w \cup \mathcal{D}_s$, and predicted labels \tilde{y}_t with their associated uncertainties as computed $T(x_t) = g(\mathbf{m}_{\text{post}}(x_t))$ and $\Sigma(x_t) = h(K_{\text{post}}(x_t, x_t))$. The generated labels are called *soft labels*. Therefore, we refer to \mathcal{D}_{sw} as a soft dataset. $g(\cdot)$ transforms the output of \mathcal{GP} to the suitable output space. For example in classification tasks, $g(\cdot)$ would be the softmax function to produce probabilities that sum up to one. For multidimensional-output tasks where a vector of variances is provided by the \mathcal{GP} , the vector $K_{\text{post}}(x_t, x_t)$ is passed through an aggregating function $h(\cdot)$ to generate a scalar value for the uncertainty of each sample. Note that we train \mathcal{GP} only on the strong dataset \mathcal{D}_s but then use it to generate soft labels $\tilde{y}_t = T(x_t)$ and uncertainty $\Sigma(x_t)$ for samples belonging to $\mathcal{D}_{sw} = \mathcal{D}_w \cup \mathcal{D}_s$.

Step 3 Fine-tune the weights of the student network on the soft dataset, while modulating the magnitude of each parameter update by the corresponding teacher-confidence in its label.

The student network of Step 1 is fine-tuned using samples from the soft dataset $\mathcal{D}_{sw} = \{(x_t, \tilde{y}_t)\}$ where $\tilde{y}_t = T(x_t)$. The corresponding uncertainty $\Sigma(x_t)$ of each sample is mapped to a confidence value, and this is then used to determine the step size for each iteration of the stochastic gradient descent (SGD).

¹In practice, we use cluster-GP, see Appendix B.

Table 1: Descriptions of baseline models.

| | |
|--|---|
| WA | The weak annotator, i.e. the unsupervised method used for annotating the unlabeled data. |
| NN_s | Full Supervision Only, i.e. the student trained only on strong labeled data (\mathcal{D}_s). |
| NN_w | Weak Supervision Only, i.e. the or the student trained only on weakly labeled data (\mathcal{D}_w). |
| NN_{w/s+} | Weak Supervision + Oversampled Strong Supervision, i.e. the student trained on samples that are alternately drawn from \mathcal{D}_w without replacement, and \mathcal{D}_s with replacement. Since $ \mathcal{D}_s \ll \mathcal{D}_w $, it oversamples the strong data. |
| NN_{w→s} | Weak Supervision + Fine Tuning, i.e. the student trained on weak dataset \mathcal{D}_w and fine-tuned on strong dataset \mathcal{D}_s . |
| NN_{w^ω→NN_s} | The student trained on the weak data, but the step-size of each weak sample is weighted by a fixed value $0 \leq \omega \leq 1$, and fine-tuned on strong data. As an approximation for the optimal value for ω , we have used the mean of η_2 of our model (below). |
| FWL $\setminus \Sigma$ | The student trained on the weakly labeled data and fine-tuned on examples labeled by the teacher without taking the confidence into account. This baseline is similar to (Veit et al., 2017). |

So, intuitively, for data points where we have true labels, the uncertainty of the teacher is almost zero, which means we have high confidence and a large step-size for updating the parameters. However, for data points where the teacher is not confident, we down-weight the training steps of the student. This means that at these points, we keep the student function as it was trained on the weak data in Step 1.

More specifically, we update the parameters of the student by training on \mathcal{D}_{sw} using SGD:

$$\begin{aligned} \mathbf{w}^* &= \operatorname{argmin}_{\mathbf{w} \in \mathcal{W}} \frac{1}{N} \sum_{(x_t, \bar{y}_t) \in \mathcal{D}_{sw}} l(\mathbf{w}, x_t, \bar{y}_t) + \mathcal{R}(\mathbf{w}), \\ \mathbf{w}_{t+1} &= \mathbf{w}_t - \eta_t (\nabla l(\mathbf{w}, x_t, \bar{y}_t) + \nabla \mathcal{R}(\mathbf{w})) \end{aligned}$$

where $l(\cdot)$ is the per-example loss, η_t is the total learning rate, N is the size of the soft dataset \mathcal{D}_{sw} , \mathbf{w} is the parameters of the student network, and $\mathcal{R}(\cdot)$ is the regularization term.

We define the total learning rate as $\eta_t = \eta_1(t)\eta_2(x_t)$, where $\eta_1(t)$ is the usual learning rate of our chosen optimization algorithm that anneals over training iterations, and $\eta_2(x_t)$ is a function of the label uncertainty $\Sigma(x_t)$ that is computed by the teacher for each data point. Multiplying these two terms gives us the total learning rate. In other words, η_2 represents the *fidelity* (quality) of the current sample, and is used to multiplicatively modulate η_1 . Note that the first term does not necessarily depend on each data point, whereas the second term does. We propose $\eta_2(x_t) = \exp[-\beta\Sigma(x_t)]$ to exponentially decrease the learning rate for data point x_t if its corresponding soft label \bar{y}_t is unreliable (far from a true sample). In practice, when using mini-batches, we implement this by multiplying the loss of each example in the batch by its fidelity score and average over these fidelity-weighted losses in the batch when calculating the batch gradient based on that loss. β is a positive scalar hyper-parameter that controls the contribution of weak and strong data to the training procedure. A small β results in a student which listens more carefully to the teacher and copies its knowledge, while a large β makes the student pay less attention to the teacher, staying with its initial weak knowledge. Hence, β gives a handle to control the bias-variance trade-off. In Appendix A, we apply FWL to a one-dimensional toy problem to illustrate its various steps.

3 EXPERIMENTS

In this section, we apply FWL to *document ranking* task and evaluate its performance compared to the baselines presented in Table 1. Document Ranking is the core information retrieval problem and is challenging as the ranking model needs to learn a representation for long documents and capture the complex notion of relevance between queries and documents. Furthermore, the size of publicly available datasets with query-document relevance judgments is unfortunately quite small (~ 250 queries). We employ a state-of-the-art pairwise neural ranker architecture as the student (Dehghani et al., 2017d) in which the ranking is cast as a regression task. Given each training sample x as a triple of query q , and two documents d^+ and d^- , the goal is to learn a function $\mathcal{F}: \{ \langle q, d^+, d^- \rangle \} \rightarrow \mathbb{R}$, which maps each data sample x to a scalar output value y indicating the probability of d^+ being ranked higher than d^- with respect to q .

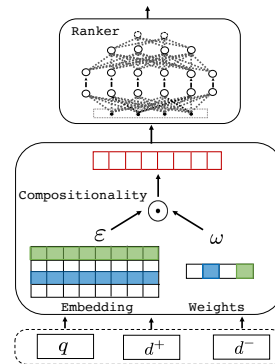


Figure 2: The student.

The student follows the architecture proposed in (Dehghani et al., 2017d). The first layer of the network, i.e. representation learning layer $\psi: \{ \langle q, d^+, d^- \rangle \} \rightarrow \mathbb{R}^m$ maps each input sample to an m -dimensional real-valued vector. In general, besides learning embeddings for words, function ψ learns to compose word embedding based on their global importance in order to generate query/document embeddings. The representation layer is followed by a simple fully-connected feed-forward network

Table 2: Performance of FWL approach and baseline methods for ranking task. \star^i indicates that the improvements with respect to the baseline i are statistically significant at the 0.05 level using the paired two-tailed t-test with Bonferroni correction.

| Method | Robust04 | | ClueWeb | |
|--|--|--|--|--|
| | MAP | nDCG@20 | MAP | nDCG@20 |
| WA _{BM25} | 0.2503 \star^{37} | 0.4102 \star^{37} | 0.1021 \star^{37} | 0.2070 \star^{37} |
| NN _W (Dehghani et al., 2017d) | 0.2702 \star^{137} | 0.4290 \star^{137} | 0.1297 \star^{137} | 0.2201 \star^{137} |
| NN _S | 0.1790 | 0.3519 | 0.0782 | 0.1730 |
| NN _{S+W} | 0.2763 \star^{1237} | 0.4330 \star^{1237} | 0.1354 \star^{1237} | 0.2319 \star^{1237} |
| NN _{W→S} | 0.2810 \star^{1237} | 0.4372 \star^{1237} | 0.1346 \star^{1237} | 0.2317 \star^{1237} |
| NN _{Wω→S} | 0.2899 \star^{123457} | 0.4431 \star^{123457} | 0.1320 \star^{12347} | 0.2309 \star^{12347} |
| FWL \ Σ | 0.2980 \star^{123457} | 0.4516 \star^{123457} | 0.1386 \star^{123457} | 0.2340 \star^{123457} |
| FWL | 0.3124$\star^{12345678}$ | 0.4607$\star^{12345678}$ | 0.1472$\star^{12345678}$ | 0.2453$\star^{12345678}$ |

with a sigmoidal output unit to predict the probability of ranking d^+ higher than d^- . The general schema of the student is illustrated in Figure 2. More details are provided in Appendix C.1.

The teacher is implemented by clustered \mathcal{GP} algorithm. See Appendix C.2 for more details. The weak annotator is BM25 (Robertson & Zaragoza, 2009), a well-known unsupervised method for scoring query-document pairs based on statistics of the matched terms. More details are provided in Appendix C.3. Description of the data with weak labels and data with true labels as well as the setup of the document-ranking experiments is presented in Appendix C.4 in more details.

Results and Discussions. We conducted k-fold cross-validation on \mathcal{D}_s (the strong data) and report two standard evaluation metrics for ranking: mean average precision (MAP) of the top-ranked 1,000 documents and normalized discounted cumulative gain calculated for the top 20 retrieved documents (nDCG@20). Table 2 shows the performance on both datasets. As can be seen, FWL provides a significant boost on the performance over all datasets. In the ranking task, the student is designed in particular to be trained on weak annotations (Dehghani et al., 2017d), hence training the network only on weak supervision, i.e. NN_W performs better than NN_S. This can be due to the fact that ranking is a complex task requiring many training samples, while relatively few data with true labels are available.

Alternating between strong and weak data during training, i.e. NN_{S+W} seems to bring little (but statistically significant) improvement. However, we can gain better results by the typical fine-tuning strategy, NN_{W→S}. We can gain improvement by fine-tuning the NN_W using labels generated by the teacher without considering their confidence score, i.e. FWL \ Σ. This means we just augmented the fine-tuning process by generating a fine-tuning set using teacher which is better than \mathcal{D}_s in terms of quantity and \mathcal{D}_w in terms of quality. This baseline is equivalent to setting $\beta = 0$. However, we see a big jump in performance when we use FWL to include the estimated label quality from the teacher, leading to the best overall results.

Sensitivity of the FWL to the Quality of the Weak Annotator.

Our proposed setup in FWL requires defining a so-called “weak annotator” to provide a source of weak supervision for unlabelled data. In this section, we study how the quality of the weak annotator may affect the performance of the FWL on the Robust04 dataset. To do so, besides BM25 (Robertson & Zaragoza, 2009), we use three other weak annotators: vector space model (Salton & Yang, 1973) with binary term occurrence (BTO) weighting schema and vector space model with TF-IDF weighting schema, which are both weaker than BM25, and BM25+RM3 (Abduljaleel et al., 2004) that uses RM3 as the pseudo-relevance feedback method on top of BM25, leading to better labels. Figure 3 illustrates the performance of these four weak annotators in terms of their mean average precision (MAP) on the test data, versus the performance of FWL given the corresponding weak annotator. As it is expected, the performance of FWL depends on the quality of the employed weak annotator. The percentage of improvement of FWL over its corresponding weak annotator on the test data is also presented in Figure 3. As can be seen, the better the performance of the weak annotator is, the less the improvement of the FWL would be.

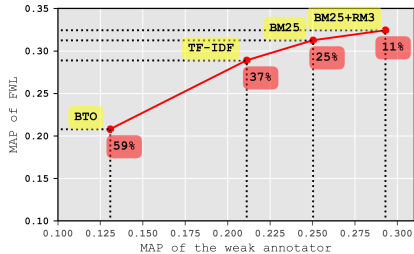


Figure 3: Performance of FWL versus performance of the correspondence weak annotator.

Figure 3 illustrates the performance of these four weak annotators in terms of their mean average precision (MAP) on the test data, versus the performance of FWL given the corresponding weak annotator. As it is expected, the performance of FWL depends on the quality of the employed weak annotator. The percentage of improvement of FWL over its corresponding weak annotator on the test data is also presented in Figure 3. As can be seen, the better the performance of the weak annotator is, the less the improvement of the FWL would be.

4 CONCLUSION

Training neural networks using large amounts of weakly annotated data is an attractive approach in scenarios where an adequate amount of data with true labels is not available, a situation which often arises in practice. In this paper, we introduced fidelity-weighted learning (FWL), a new student-teacher framework for semi-supervised learning in the presence of weakly labeled data. We applied FWL to document ranking and empirically verified that FWL speeds up the training process and improves over state-of-the-art semi-supervised alternatives.

REFERENCES

- Nasreen Abdul-jaleel, James Allan, W. Bruce Croft, O Diaz, Leah Larkey, Xiaoyan Li, Mark D. Smucker, and Courtney Wade. Umass at trec 2004: Novelty and hard. In *TREC-13*, 2004.
- Gordon V. Cormack, Mark D. Smucker, and Charles L. Clarke. Efficient and effective spam filtering and re-ranking for large web datasets. *Inf. Retr.*, 14(5):441–465, 2011.
- Mostafa Dehghani, Sascha Rothe, Enrique Alfonseca, and Pascal Fleury. Learning to attend, copy, and generate for session-based query suggestion. In *Proceedings of The international Conference on Information and Knowledge Management (CIKM'17)*, 2017a.
- Mostafa Dehghani, Aliaksei Severyn, Sascha Rothe, and Jaap Kamps. Learning to learn from weak supervision by full supervision. In *NIPS2017 workshop on Meta-Learning (MetaLearn 2017)*, 2017b.
- Mostafa Dehghani, Aliaksei Severyn, Sascha Rothe, and Jaap Kamps. Avoiding your teacher’s mistakes: Training neural networks with controlled weak supervision. *arXiv preprint arXiv:1711.00313*, 2017c.
- Mostafa Dehghani, Hamed Zamani, Aliaksei Severyn, Jaap Kamps, and W. Bruce Croft. Neural ranking models with weak supervision. In *SIGIR'17*, 2017d.
- Mostafa Dehghani, Arash Mehrjou, Stephan Gouws, Jaap Kamps, and Bernhard Schölkopf. Fidelity-weighted learning. In *International Conference on Learning Representations, ICLR'18*, 2018.
- Thomas Desautels, Andreas Krause, and Joel W. Burdick. Parallelizing exploration-exploitation tradeoffs in gaussian process bandit optimization. *Journal of Machine Learning Research*, 15(1): 3873–3923, 2014.
- Diederik Kingma and Jimmy Ba. Adam: A method for stochastic optimization. In *ICLR*, 2015. arXiv preprint arXiv:1412.6980.
- Tomas Mikolov, Ilya Sutskever, Kai Chen, Greg S. Corrado, and Jeff Dean. Distributed Representations of Words and Phrases and their Compositionality. In *NIPS '13*, pp. 3111–3119, 2013.
- Vinod Nair and Geoffrey E. Hinton. Rectified linear units improve restricted boltzmann machines. In *Proceedings of the 27th international conference on machine learning (ICML-10)*, pp. 807–814, 2010.
- George Orwell. *Animal Farm: A Fairy Story*. Secker and Warburg, London, England, 1945.
- Greg Pass, Abdur Chowdhury, and Cayley Torgeson. A picture of search. In *InfoScale '06*, 2006.
- Alexander J. Ratner, Christopher M. De Sa, Sen Wu, Daniel Selsam, and Christopher Ré. Data programming: Creating large training sets, quickly. In *Advances in Neural Information Processing Systems*, pp. 3567–3575, 2016.
- Stephen Robertson and Hugo Zaragoza. The probabilistic relevance framework: BM25 and beyond. *Foundations and Trends in Information Retrieval*, 3(4):333–389, 2009.
- Gerard Salton and Chung-Shu Yang. On the specification of term values in automatic indexing. *Journal of documentation*, 29(4):351–372, 1973.
- Yirong Shen, Matthias Seeger, and Andrew Y. Ng. Fast gaussian process regression using kd-trees. In *Advances in neural information processing systems*, pp. 1225–1232, 2006.

Nitish Srivastava, Geoffrey Hinton, Alex Krizhevsky, Ilya Sutskever, and Ruslan Salakhutdinov. Dropout: A simple way to prevent neural networks from overfitting. *J. Mach. Learn. Res.*, 15(1): 1929–1958, 2014.

Michalis K. Titsias. Variational learning of inducing variables in sparse gaussian processes. In *International Conference on Artificial Intelligence and Statistics*, pp. 567–574, 2009.

Andreas Veit, Neil Alldrin, Gal Chechik, Ivan Krasin, Abhinav Gupta, and Serge Belongie. Learning from noisy large-scale datasets with minimal supervision. In *The Conference on Computer Vision and Pattern Recognition*, 2017.

APPENDICES

A TOY EXAMPLE

To better understand FWL, we apply FWL to a one-dimensional toy problem to illustrate the various steps. Let $f_t(x) = \sin(x)$ be the true function (red dotted line in Figure 4a) from which a small set of observations $\mathcal{D}_s = \{x_j, y_j\}$ is provided (red points in Figure 4b). These observations might be noisy, in the same way that labels obtained from a human labeler could be noisy. A weak annotator function $f_w(x) = 2\text{sinc}(x)$ (magenta line in Figure 4a) is provided, as an approximation to $f_t(\cdot)$.

The task is to obtain a good estimate of $f_t(\cdot)$ given the set \mathcal{D}_s of strong observations and the weak annotator function $f_w(\cdot)$. We can easily obtain a large set of observations $\mathcal{D}_w = \{x_i, \tilde{y}_i\}$ from $f_w(\cdot)$ with almost no cost (magenta points in Figure 4a).

As the teacher, we use standard Gaussian process regression² with this kernel:

$$k(x_i, x_j) = k_{\text{RBF}}(x_i, x_j) + k_{\text{White}}(x_i, x_j) \quad (1)$$

where,

$$k_{\text{RBF}}(x_i, x_j) = \exp\left(-\frac{\|x_i - x_j\|^2}{2^2}\right)$$

$$k_{\text{White}}(x_i, x_j) = \text{constant_value}, \quad \forall x_1 = x_2 \text{ and } 0 \text{ otherwise}$$

We fit only one \mathcal{GP} on all the data points (i.e. no clustering). Also during fine-tuning, we set $\beta = 1$. The student is a simple feed-forward network with the depth of 3 layers and width of 128 neurons per layer. We have used \tanh as the nonlinearity for the intermediate layers and a linear output layer. As the optimizer, we used Adam (Kingma & Ba, 2015) and the initial learning rate has been set to 0.001. We randomly sample 100 data points from the weak annotator and 10 data points from the true function. We introduce a small amount of noise to the observation of the true function to model the noise in the human labeled data.

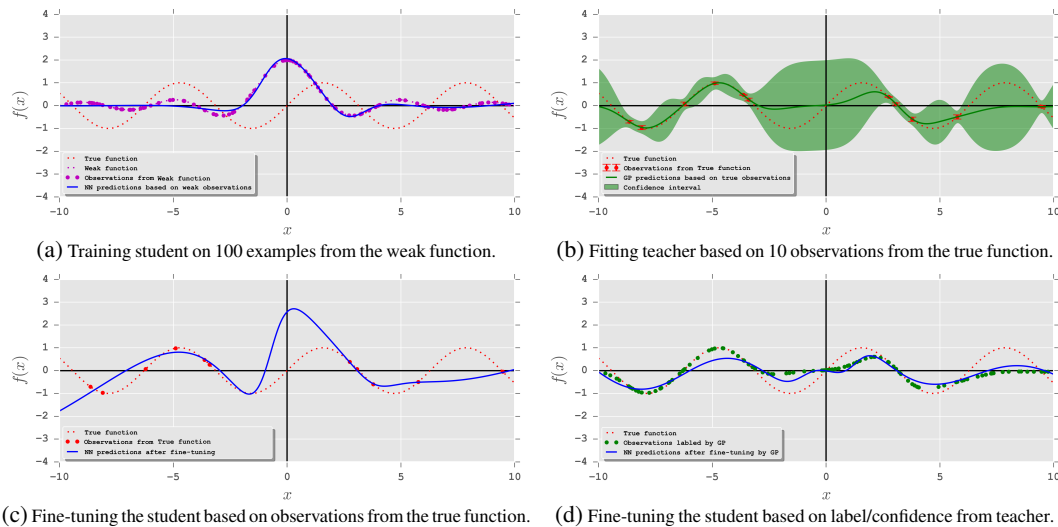


Figure 4: Toy example: The true function we want to learn is $y = \sin(x)$ and the weak function is $y = 2\text{sinc}(x)$.

We consider two experiments:

1. A neural network trained on weak data and then fine-tuned on strong data from the true function, which is the most common semi-supervised approach (Figure 4c).
2. A teacher-student framework working by the proposed FWL approach.

As can be seen in Figure 4d, FWL by taking into account label confidence, gives a better approximation of the true hidden function. We repeated the above experiment 10 times. The average RMSE with respect to the true function on a set of test points over those 10 experiments for the student, were as follows:

²<http://gpflow.readthedocs.io/en/latest/notebooks/regression.html>

Algorithm 1 Clustered Gaussian processes.

- 1: Let N be the sample size, n the sample size of each cluster, K the number of clusters, and c_i the center of cluster i .
- 2: Run K-means with K clusters over all samples with true labels $\mathcal{D}_s = \{x_i, y_i\}$.

$$\text{K-means}(x_i) \rightarrow c_1, c_2, \dots, c_K$$

where c_i represents the center of cluster C_i containing samples $D_s^{c_i} = \{x_{i,1}, x_{i,2}, \dots, x_{i,n}\}$.

- 3: Assign each of K clusters a Gaussian process and train them in parallel to approximate the label of each sample.

$$\begin{aligned} \mathcal{GP}_{c_i}(\mathbf{m}_{\text{post}}^{c_i}, K_{\text{post}}^{c_i}) &= \mathcal{GP}(\mathbf{m}_{\text{prior}}, K_{\text{prior}}) | D_s^{c_i} = \{(\psi(x_{s,c_i}), y_{s,c_i})\} \\ T_{c_i}(x_t) &= g(\mathbf{m}_{\text{post}}^{c_i}(x_t)) \\ \Sigma_{c_i}(x_t) &= h(K_{\text{post}}^{c_i}(x_t, x_t)) \end{aligned}$$

where \mathcal{GP}_{c_i} is trained on $D_s^{c_i}$ containing samples belonging to the cluster c_i . Other elements are defined in Section 2

- 4: Use trained teacher $T_{c_i}(\cdot)$ to evaluate the soft label and uncertainty for samples from \mathcal{D}_{sw} to compute $\eta_2(x_t)$ required for step 3 of FWL. We use $T(\cdot)$ as a wrapper for all teachers $\{T_{c_i}\}$.

1. Student is trained on weak data (blue line in Figure 4a): 0.8406,
2. Student is trained on weak data then fine tuned on true observations (blue line in Figure 4c): 0.5451,
3. Student is trained on weak data, then fine tuned by soft labels and confidence information provided by the teacher (blue line in Figure 4d): 0.4143 (best).

B DETAILED DESCRIPTION OF CLUSTERED GP

We suggest using several $\mathcal{GP} = \{GP_{c_i}\}$ to explore the entire data space more effectively. Even though inducing points and stochastic methods make \mathcal{GP} s more scalable we still observed poor performance when the entire dataset was modeled by a single \mathcal{GP} . Therefore, the reason for using multiple \mathcal{GP} s is mainly empirically inspired by (Shen et al., 2006) which is explained in the following:

We used the Sparse Gaussian Process implemented in GPflow. The algorithm is scalable in the sense that it is not $O(N^3)$ as original \mathcal{GP} is. It introduces inducing points in the data space and defines a variational lower bound for the marginal likelihood. The variational bound can now be optimized by stochastic methods which make the algorithm applicable in large datasets. However, the tightness of the bound depends on the location of inducing points which are found through the optimization process. The pseudo-code of the clustered \mathcal{GP} is presented in Algorithm 1. When the main issue is computational resources (when the number of inducing points for each \mathcal{GP} is large), we can first choose the number n which is the maximum size of the dataset on which our resources allow to train a \mathcal{GP} , then find the number of clusters $K = N/n$ accordingly. The rest of the algorithm remains unchanged.

C DETAILED SETUP OF THE MODEL AND EXPERIMENTS

C.1 DETAILED ARCHITECTURE OF THE STUDENTS

The employed student is proposed in (Dehghani et al., 2017d). The first layer of the network models function ψ that learns the representation of the input data samples, i.e. (q, d^+, d^-) , and consists of three components: (1) an embedding function $\varepsilon: \mathcal{V} \rightarrow \mathbb{R}^m$ (where \mathcal{V} denotes the vocabulary set and m is the number of embedding dimensions), (2) a weighting function $\omega: \mathcal{V} \rightarrow \mathbb{R}$, and (3) a compositionality function $\odot: (\mathbb{R}^m, \mathbb{R})^n \rightarrow \mathbb{R}^m$. More formally, the function ψ is defined as:

$$\begin{aligned} \psi(q, d^+, d^-) &= [\odot_{i=1}^{|q|} (\varepsilon(t_i^q), \omega(t_i^q)) \parallel \\ &\quad \odot_{i=1}^{|d^+|} (\varepsilon(t_i^{d^+}), \omega(t_i^{d^+})) \parallel \\ &\quad \odot_{i=1}^{|d^-|} (\varepsilon(t_i^{d^-}), \omega(t_i^{d^-}))], \end{aligned} \tag{2}$$

where t_i^q and t_i^d denote the i^{th} term in query q respectively document d . The embedding function ε maps each term to a dense m - dimensional real value vector, which is learned during the training phase. The weighting function ω assigns a weight to each term in the vocabulary. It has been shown that ω simulates the effect of inverse document frequency (IDF), which is an important feature in information retrieval (Dehghani et al., 2017d).

The compositionality function \odot projects a set of n embedding-weighting pairs to an m - dimensional representation, independent from the value of n :

$$\bigodot_{i=1}^n (\varepsilon(t_i), \omega(t_i)) = \frac{\sum_{i=1}^n \exp(\omega(t_i)) \cdot \varepsilon(t_i)}{\sum_{j=1}^n \exp(\omega(t_j))}, \quad (3)$$

which is in fact the normalized weighted element-wise summation of the terms' embedding vectors. Again, it has been shown that having global term weighting function along with embedding function improves the performance of ranking as it simulates the effect of inverse document frequency (IDF). In our experiments, we initialize the embedding function ε with word2vec embeddings (Mikolov et al., 2013) pre-trained on Google News and the weighting function ω with IDF.

The representation layer is followed by a simple fully connected feed-forward network with l hidden layers followed by a softmax which receives the vector representation of the inputs processed by the representation learning layer and outputs a prediction \tilde{y} . Each hidden layer z_k in this network computes $z_k = \alpha(W_k z_{k-1} + b_k)$, where W_k and b_k denote the weight matrix and the bias term corresponding to the k^{th} hidden layer and $\alpha(\cdot)$ is the non-linearity. These layers follow a sigmoid output. We employ the cross entropy loss:

$$\mathcal{L}_t = \sum_{i \in B} [-y_i \log(\hat{y}_i) - (1 - y_i) \log(1 - \hat{y}_i)], \quad (4)$$

where B is a batch of data samples.

C.2 DETAILED ARCHITECTURE OF THE TEACHERS

We use Gaussian Process as the teacher and pass the mean of \mathcal{GP} through the same function $g(\cdot)$ that is applied on the output of the student network. $h(\cdot)$ is an aggregation function that takes variance over several dimensions and outputs a single measure of variance. As a reasonable choice, the aggregating function $h(\cdot)$ in our sentiment classification task (three classes) is *mean* of variances over dimensions. In the teacher, linear combinations of different kernels are used in our experiments.

We use sparse variational GP regression³ (Titsias, 2009) with this kernel:

$$k(x_i, x_j) = k_{\text{Matern3/2}}(x_i, x_j) + k_{\text{Linear}}(x_i, x_j) + k_{\text{White}}(x_i, x_j) \quad (5)$$

where,

$$k_{\text{Matern3/2}}(x_i, x_j) = \left(1 + \frac{\sqrt{3} \|x_i - x_j\|}{l} \right) \exp\left(-\frac{\sqrt{3} \|x_i - x_j\|}{l} \right)$$

$$k_{\text{Linear}}(x_i, x_j) = \sigma_0^2 + x_i \cdot x_j$$

$$k_{\text{White}}(x_i, x_j) = \text{constant_value}, \quad \forall x_1 = x_2 \text{ and } 0 \text{ otherwise}$$

We empirically found $l=1$ satisfying value for the length scale of Matern3/2 kernels. We also set $\sigma_0=0$ to obtain a homogeneous linear kernel. The constant value of $K_{\text{White}}(\cdot, \cdot)$ determines the level of noise in the labels. This is different from the noise in weak labels. This term explains the fact that even in true labels there might be a trace of noise due to the inaccuracy of human labelers. We set the number of clusters in the clustered \mathcal{GP} algorithm for the ranking task to 50.

C.3 WEAK ANNOTATORS

The weak annotator is BM25 (Robertson & Zaragoza, 2009), a well-known unsupervised retrieval method. This method heuristically scores a given pair of query-document based on the statistics of their matched terms. In the pairwise document ranking setup, \tilde{y}_i for a given sample $x_j = (q, d^+, d^-)$ is the probability of document d^+ being ranked higher than d^- : $\tilde{y}_i = P_{q, d^+, d^-} = s_{q, d^+} / (s_{q, d^+} + s_{q, d^-})$, where $s_{q, d}$ is the score obtained from the weak annotator.

C.4 DATA COLLECTION, PARAMETERS AND SETUP

Collections We use two standard TREC collections for the task of ad-hoc retrieval: The first collection (*Robust04*) consists of 500k news articles from different news agencies as a homogeneous collection. The second collection

³http://gpflow.readthedocs.io/en/latest/notebooks/SGPR_notes.html

(*ClueWeb*) is ClueWeb09 Category B, a large-scale web collection with over 50 million English documents, which is considered as a heterogeneous collection. Spam documents were filtered out using the Waterloo spam scorer⁴ (Cormack et al., 2011) with the default threshold 70%.

Data with true labels We take query sets that contain human-labeled judgments: a set of 250 queries (TREC topics 301–450 and 601–700) for the Robust04 collection and a set of 200 queries (topics 1–200) for the experiments on the ClueWeb collection. For each query, we take all documents judged as relevant plus the same number of documents judged as non-relevant and form pairwise combinations among them.

Data with weak labels We create a query set Q using the unique queries appearing in the AOL query logs (Pass et al., 2006). This query set contains web queries initiated by real users in the AOL search engine that were sampled from a three-month period from March 2006 to May 2006. We applied standard pre-processing Dehghani et al. (2017d;a) on the queries: We filtered out a large volume of navigational queries containing URL substrings (“http”, “www”, “.com”, “.net”, “.org”, “.edu”). We also removed all non-alphanumeric characters from the queries. For each dataset, we took queries that have at least ten hits in the target corpus using our weak annotator method. Applying all these steps, We collect 6.15 million queries to train on in Robust04 and 6.87 million queries for ClueWeb. To prepare the weakly labeled training set \mathcal{D}_w , we take the top 1,000 retrieved documents using BM25 for each query from training query set Q , which in total leads to $\sim |Q| \times 10^6$ training samples.

Setup For the evaluation of the whole model, we conducted 3-fold cross-validation. However, for each dataset, we first tuned all the hyper-parameters of the student in the first step on the set with true labels using batched GP bandits with an expected improvement acquisition function (Desautels et al., 2014) and kept the optimal parameters of the student fixed for all the other experiments. The size and number of hidden layers for the student is selected from $\{64, 128, 256, 512\}$. The initial learning rate and the dropout parameter were selected from $\{10^{-3}, 10^{-5}\}$ and $\{0.0, 0.2, 0.5\}$, respectively. We considered embedding sizes of $\{300, 500\}$. The batch size in our experiments was set to 128. We use ReLU (Nair & Hinton, 2010) as a non-linear activation function α in student. We use the Adam optimizer (Kingma & Ba, 2015) for training, and *dropout* (Srivastava et al., 2014) as a regularization technique.

At inference time, for each query, we take the top 2,000 retrieved documents using BM25 as candidate documents and re-rank them using the trained models. We use the Indri⁵ implementation of BM25 with default parameters (i.e., $k_1 = 1.2$, $b = 0.75$, and $k_3 = 1,000$).

⁴<http://plg.uwaterloo.ca/~gvcormac/clueweb09spam/>

⁵<https://www.lemurproject.org/indri.php>