Supporting Information

SF₆⁺: Stabilizing Transient Ions in Helium Nanodroplets

Simon Albertini, Stefan Bergmeister, Felix Laimer, Paul Martini, Elisabeth Gruber, Fabio Zappa, Milan Ončák,* Paul Scheier,* Olof Echt*

- * E-mail addresses: milan.oncak@uibk.ac.at, paul.scheier@uibk.ac.at, olof.echt@unh.edu
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S1. The Fate of Multiply Charged HNDs in the Pickup and Evaporation Cells

Multiply charged He_{N}^{z+} droplets become unstable with respect to spontaneous fission when their size *N* falls below the critical size $N_z = 3.54 \times 10^4 z^{3/2}$, i.e. $N_2 = 10^5$, $N_3 = 1.84 \times 10^5$, etc.¹ These values have been measured for undoped HNDs but there is no reason why they should not also apply to doped HNDs as long as the volume occupied by the dopant is small. In the present work, HNDs with $N/z \approx 3.5 \times 10^5$ were selected; their maximum possible charge state is $z_{\text{max}} = 97$. A more realistic upper limit is $z_{\text{max}} = 26$, computed from the average size of the neutral HNDs, $N_{av} \approx 4 \times 10^6$. The distribution of *z* will also depend on the energy and current of the ionizing electrons. The charges will be localized on He₂⁺ (or He₃⁺, see S3 below) which will reside near the surface of the HND because of the mutual Coulomb repulsion.

When a *z*-fold charged HND picks up a SF₆, charge transfer from one of the embedded He₂⁺ to SF₆ will release approximately 8 eV (see S3 below) which exceeds the cohesive energy of bulk helium by a factor 1.3×10^4 . If the ion remains trapped in the HND, the energy will be dissipated by evaporation of that many helium atoms. The new size *N* may drop below the critical size of the current charge state, and the HND will fission. A very small singly charged dopant ion dressed with a few He atoms will be ejected; the remaining *z*-1 charges will remain in the HND that retains nearly all the He atoms.¹ The light fragment will recoil out of the beam; the heavy one will remain near the beam axis.

Another SF₆ colliding with the HND in the pickup cell may come close to another embedded He₂⁺ releasing, once again, about 8 eV upon charge transfer, or it may attach to a SF₆⁺ (or SF₅⁺) and release a much smaller energy. Either way, the droplet will keep shrinking.

Eventually a droplet of reduced size and charge will exit the pickup cell and enter the collision cell where it suffers multiple collisions with thermal helium gas. Each collision transfers about 50 meV to the HND,² causing the evaporation of about 80 He atoms. At some point the size of the doped HND drops below 5×10^4 , the critical size of doubly charged droplets, and it fissions one last time. After another ≈ 600 collisions the doped singly charged droplet will have shed all or nearly all of its He atoms, and it will appear in the mass region of interest.

S2. The Lifetime of He₈SF₆⁺

 SF_6^+ ions that are observed must have survived for about 3 ms, from the exit of the evaporation cell to the extraction region of the mass spectrometer. Their mean lifetime can be obtained from the CID measurements. When mass-selected He₈SF₆⁺ ions pass through the collision cell (which is not deliberately filled with a collision gas), the ion beam exiting the cell consists of He₈SF₆⁺ (92.6 %) and smaller He_nSF₆⁺ (7.4 %, summed over *n* < 8). Other ions are absent (see the mass spectrum in Fig. 3a).

The distance between the exit of the quadrupole mass filter and the region where ions are extracted into the TOFMS measures 0.37 m. If we assume that the precursor ions do not suffer any collisions in the collision cell, the lifetime τ of the ions is obtained from $I = I_0 \exp(-t/\tau)$ with the transit time $t = 79.5 \,\mu\text{s}$ calculated from the ion energy ($E_{\text{lab}} = 20 \,\text{eV}$). One obtains $\tau = 1.03 \,\text{ms}$. This represents a lower limit to the true lifetime because the pressure in the collision cell is finite even if no gas is introduced.

S3. The Energy Released upon Charge Transfer to SF₆ Embedded in a HND

The adiabatic ionization energies (AIE) of He, He₂ and He₃ can be derived from the IE of He (24.59 eV) and the adiabatic dissociation energies of He₂⁺ (2.35 eV) and He-He₂⁺ (0.17 eV).^{3,4} Thus, the adiabatic IEs of He₂⁺ and He₃⁺ equal 22.24 eV and 22.07 eV, respectively. The AIE of SF₆ equals 14.11 eV.⁵

If charge transfer between SF₆ and He⁺, He₂⁺ or He₃⁺ were to occur in the gas phase, an energy of 10.5 eV, 8.1 eV, or 8.0 eV, respectively, would be released. Charge transfer within a helium droplet will change these values slightly because of the polarization of the surrounding helium.

S4. Mass Analysis

The mass resolution equals about 15 000, measured at full-width-at-half-maximum (FWHM), corresponding to a FWHM = 0.010 u at 146 u. The position of a mass peak, obtained by fitting a Gaussian, is determined with a precision of ± 0.0003 u. The presence of He_n⁺ ions provides a highly accurate mass calibration. If the mass peaks due to He₃₆⁺ (144 u) and He₃₇⁺ (148 u) are used to calibrate the mass scale, the mass of the two peaks observed at 146 u agrees with the values expected for ³²SF₆⁺ and He₃₂H₂O⁺ within better than 0.0005 u, see Fig. S1.

One might argue that the mass peak at 146 u is due to a hypothetical $[SF_5H_3O]^+$ rather than SF_6^+ . However, the mass of the former exceeds that of the latter by 0.020 u, about twice the full-width-at-half-maximum in this mass range. The mass spectrum in Fig. S1 illustrates that the presence of $[SF_5H_3O]^+$ can be safely ruled out. The calculated geometry and energetics of $[SF_5H_3O]^+$ are presented in Section S6.



Fig. S1: Three sections of a mass spectrum recorded at an evaporation pressure of 0.15 Pa. Dashed lines connect the data points. The mass peaks due to He_{36}^+ and He_{37}^+ are used to calibrate the mass scale. The expected positions of mass peaks due to ${}^{32}SF_6^+$ and $He_{32}H_2O^+$ are indicated by arrows; the agreement with the observed peaks is excellent. The hypothetical $[{}^{32}SF_5H_3O]^+$ ion, on the other hand, is not observed.

S5. Theoretical Results for SF₆⁺ and HeSF₆⁺

Table S1: Cartesian coordinates (in Å) and electronic energies (in Hartree) for atoms and ions optimized at the CCSD/aug-cc-pVDZ level including the ZPE correction.

F

E = -99.547749 F 0.000000 0.000000 0.000000

He

E = -2.889548 He 0.000000 0.000000 0.000000

HeSF5+

E = -898.308865S -0.093458 0.033760 -0.000000 F 0.969425 1.193286 -0.000002 F 0.471366 -0.483999 -1.339761 F -1.232499 1.075568 -0.000002 F 0.471364 -0.483993 1.339764 F -1.154707 -1.128040 0.000001 He 2.885385 -1.047780 0.000003

SF_5^+

E = -895.418733 S 0.000000 0.000000 0.000000 F -0.000000 1.543797 0.000000 F 1.336967 -0.771898 -0.000000 F -1.336967 -0.771898 0.000000 F -0.000000 -0.000000 1.572896 F 0.000000 -0.000000 -1.572896

HeSF₆⁺, IIa

$$\begin{split} & E = -997.859648 \\ & S \ -0.357085 \ -0.108891 \ -0.049004 \\ & F \ -0.736331 \ -1.345081 \ 0.848985 \\ & F \ 0.220626 \ 0.604230 \ 1.192031 \\ & F \ 0.491334 \ -1.032355 \ -0.949516 \\ & F \ -1.843592 \ 0.099157 \ -0.405331 \\ & F \ 0.041243 \ 1.123704 \ -0.939841 \\ & F \ 2.846466 \ 0.161499 \ 0.148377 \\ & He \ -1.732174 \ 2.620933 \ 0.865854 \end{split}$$

HeSF₆⁺, IIb E = -997.859457

S -0.486684 -0.002489 -0.016635 F 0.453613 1.096170 -0.556346 F -0.032216 -1.074770 0.996739 F -1.949095 -0.027002 -0.507762 F -0.060125 -0.945028 -1.200867 F -0.891831 0.941419 1.176056 F 2.674927 -0.456188 0.323723 He 3.014744 2.114198 -0.908864

$\mathrm{HeSF_{6}^{+}}$, IIc

$$\begin{split} & E = -997.859370 \\ & S \ 0.443412 \ -0.011766 \ 0.000003 \\ & F \ 1.218889 \ -1.381447 \ -0.000003 \\ & F \ -0.193825 \ -0.382095 \ -1.356750 \\ & F \ -0.193802 \ -0.382092 \ 1.356767 \\ & F \ 1.781230 \ 0.757108 \ -0.000012 \\ & F \ -0.350785 \ 1.344644 \ 0.000008 \\ & F \ -2.676851 \ -0.778685 \ -0.000014 \\ & He \ -1.679143 \ 3.795678 \ -0.000004 \end{split}$$

SF₆⁺, Ia

$$\begin{split} & E = -994.969542 \\ F & -1.462023 & -0.382150 & -0.000000 \\ S & 0.110397 & -0.392088 & -0.000000 \\ F & 0.112237 & -1.935227 & -0.000000 \\ F & -0.755217 & 2.703288 & 0.000000 \\ F & 0.112237 & 0.345507 & 1.356185 \\ F & 1.684267 & -0.379881 & 0.000000 \\ F & 0.112237 & 0.345507 & -1.356185 \end{split}$$

SF_6^+ , Ib E = -994.968170 F 0.000000 0.000000 -3.795338 S 0.000000 0.000000 0.558856 F -0.000000 1.336137 1.331833 F -0.000000 -1.336137 1.331833 F 1.573406 -0.000000 0.560905 F -1.573406 0.000000 0.560905 F 0.000000 0.000000 -0.983661

S6. Theoretical Results for [SF₅H₃O]⁺



Fig. S2: Three configurations of [SF₅H₃O]⁺.

Table S2: Dissociation energies of $[SF_5H_3O]^+$, calculated at the B3LYP/aug-cc-pVDZ level (in eV). Calculations at the M06-2X/aug-cc-pVDZ level are provided for comparison.

products	B3LYP	M06-2X
SF_4^+ . $H_2O + HF$	0.62	0.65
$H_3O^+ + SF_5$	0.76	0.70
$SF_3H_2O^+.HF + F$	0.95	0.88
$SF_5H^+ + H_2O$	1.34	1.40
$SF_4^+ + H_2O + HF$	1.92	2.09
SF_5^+ . $H_2O + H$	3.48	2.83
$SF_{5}^{+} + H_{2}O + H$	4.88	4.56
$SF_5^+ + H_3O$	5.53	5.33

Table S3: Cartesian coordinates (in Å) and electronic energies (in Hartree) for atoms and ions optimized at the B3LYP and M06-2X levels along with the aug-cc-pVDZ level basis set including the ZPE correction.

H 0.817171 -0.471794 -0.199541

B3LYP/aug-cc-pVDZ

	H -0.817171 -0.471794 -0.199541	
F		
E = -99.739495	Н	
F 0.000000 0.000000 0.000000	E = -0.501657	
	H 0.000000 0.000000 0.000000	
H ₂ O		
E = -76.423418	HF	
O 0.000000 0.000000 0.117802	E = -100.451507	
H -0.000000 0.764237 -0.471206	F 0.000000 0.000000 0.092564	
Н -0.000000 -0.764237 -0.471206	Н 0.000000 0.000000 -0.833073	
H ₃ O	SF_4^+ .H ₂ O	
E = -76.900955	E = -873.568713	
0 0 000000 0 000000 0 095165	S 0.177302 -0.000015 -0.156210	
0.0000000.0000000.000000	S 0.177302 -0.000015 -0.156210	
H 0.000000 0.967942 -0.253773	S 0.177302 -0.000015 -0.156210 F 1.747119 -0.000216 -0.344327	
H 0.000000 0.967942 -0.253773 H 0.838263 -0.483971 -0.253773	S 0.177302 -0.000015 -0.156210 F 1.747119 -0.000216 -0.344327 F 0.075271 -1.646303 -0.269181	
H 0.000000 0.967942 -0.253773 H 0.838263 -0.483971 -0.253773 H -0.838263 -0.483971 -0.253773	S 0.177302 -0.000015 -0.156210 F 1.747119 -0.000216 -0.344327 F 0.075271 -1.646303 -0.269181 F 0.104296 0.000067 1.407615	
H 0.000000 0.967942 -0.253773 H 0.838263 -0.483971 -0.253773 H -0.838263 -0.483971 -0.253773	S 0.177302 -0.000015 -0.156210 F 1.747119 -0.000216 -0.344327 F 0.075271 -1.646303 -0.269181 F 0.104296 0.000067 1.407615 F 0.075692 1.646328 -0.269289	
H 0.000000 0.967942 -0.253773 H 0.838263 -0.483971 -0.253773 H -0.838263 -0.483971 -0.253773 H ₃ O ⁺	S 0.177302 -0.000015 -0.156210 F 1.747119 -0.000216 -0.344327 F 0.075271 -1.646303 -0.269181 F 0.104296 0.000067 1.407615 F 0.075692 1.646328 -0.269289 O -2.008273 0.000094 -0.137621	
H 0.000000 0.967942 -0.253773 H 0.838263 -0.483971 -0.253773 H -0.838263 -0.483971 -0.253773 H $_{3}O^{+}$ E = -76.680712	S 0.177302 -0.000015 -0.156210 F 1.747119 -0.000216 -0.344327 F 0.075271 -1.646303 -0.269181 F 0.104296 0.000067 1.407615 F 0.075692 1.646328 -0.269289 O -2.008273 0.000094 -0.137621 H -2.396064 -0.790022 -0.561870	
H 0.000000 0.967942 -0.253773 H 0.838263 -0.483971 -0.253773 H -0.838263 -0.483971 -0.253773 H $_{3}O^{+}$ E = -76.680712 O 0.000000 0.000000 0.074828	S 0.177302 -0.000015 -0.156210 F 1.747119 -0.000216 -0.344327 F 0.075271 -1.646303 -0.269181 F 0.104296 0.000067 1.407615 F 0.075692 1.646328 -0.269289 O -2.008273 0.000094 -0.137621 H -2.396064 -0.790022 -0.561870 H -2.395974 0.790626 -0.561176	

SF₃H₂O⁺.HF E = -874.268902S 0.932299 0.318324 -0.166713 F 2.375891 -0.331115 0.081051 F 0.452881 0.117073 1.328031 F 0.323747 -0.983391 -0.820116 O -1.090132 1.090471 -0.582131 F -3.052902 -0.541229 0.292792 H -3.937435 -0.764393 0.102439 H -1.272623 2.025198 -0.396716 H -1.882224 0.570201 -0.317080 SF_4^+ E = -797.097631 S 0.000047 -0.000152 -0.239929 F 0.000086 1.216095 0.729946 F -1.614372 0.001155 -0.515664 F -0.000089 -1.218002 0.727935 F 1.614291 0.001023 -0.515677 SF₅⁺.H₂O E = -973.413584 S -0.150741 -0.000243 0.002070 F -0.005132 -1.594482 0.026489 F -1.716670 0.000119 -0.110866 F -0.002299 1.594185 -0.016792 F-0.148498 0.021702 1.591430 O 1.786996 -0.000680 0.162064 H 2.197277 0.804677 -0.217824 H 2.198738 -0.798945 -0.231005 F 0.063696 -0.021125 -1.588127 $SF_{5}H_{3}O^{+}$ E = -974.043130S 0.659432 0.019791 -0.178439 F -1.054952 -0.774656 -0.212655 F -0.098528 1.505835 -0.236124 F 1.278140 -1.498130 -0.311354 F 2.110542 0.696360 -0.287893 F 0.613618 -0.029738 1.399253 O -3.289078 0.130008 -0.010972 H -2.294938 -0.236581 -0.103985 H -3.780939 -0.281918 0.724184 H -3.801794 0.064756 -0.838450 SF₅.H₃O⁺ E = -974.036578S -0.275005 0.136403 0.000055 F-0.159128 0.070100 1.651620 F -1.786354 -0.287326 0.002685 F -0.164741 0.068640 -1.652008 F -0.455197 1.710436 -0.000392 O 0.236183 -1.993189 0.000856

F 2.337533 0.351546 -0.001360 H 0.774995 -2.218101 0.783868 H 0.762134 -2.222520 -0.789580 H 3.024468 0.983120 -0.006918 $SF_5.H_3O^+$ E = -974.029102S 0.693926 -0.002458 -0.249467 F 0.670116 1.647503 -0.302481 F-0.338430 0.015195 1.060701 F -0.701969 -0.023206 -1.245860 F 1.985625 0.020611 0.734130 F 0.686893 -1.649825 -0.251261 O -2.921036 -0.076791 0.385486 H -1.970155 -0.006948 0.691703 H -2.962439 0.025921 -0.589325 H -3.522045 0.542190 0.848137

SF_5H^+

E = -897.570390 S -0.241133 -0.000542 -0.142690 F -0.072902 0.015333 1.406169 F -0.152598 1.631764 -0.322689 F -1.798031 -0.057440 -0.285658 F -0.027339 -1.615024 -0.308729 F 2.165414 -0.042324 -0.204945 H 2.827238 0.617906 -0.274307

SF_5

E = -897.334624 S -0.000002 0.000003 -0.203300 F 0.000155 -1.670387 -0.258429 F -1.670491 -0.000089 -0.258522 F 1.670496 0.000222 -0.258523 F -0.000157 1.670429 -0.258251 F 0.000001 -0.000180 1.395146

SF_5^+

E = -896.938902 S 0.000000 0.000000 0.000000 F 0.000000 1.557201 -0.000000 F 1.348576 -0.778600 0.000000 F -1.348576 -0.778600 -0.000000 F 0.000000 0.000000 1.583619 F 0.000000 0.000000 -1.583619

M06-2X/aug-cc-pVDZ

F

E = -99.705436 F 0.000000 0.000000 0.000000

H_2O

E = -76.387120 O -0.000000 0.000000 0.117476 H -0.000000 0.762103 -0.469904 H -0.000000 -0.762103 -0.469904

H_3O

E = -76.856490 O 0.000000 -0.000000 0.103176 H 0.000000 0.950269 -0.275137 H 0.822957 -0.475134 -0.275137 H -0.822957 -0.475134 -0.275137

H_3O^+

E = -76.645514 O 0.000000 -0.000000 0.074808 H 0.000000 0.942332 -0.199488 H 0.816084 -0.471166 -0.199488 H -0.816084 -0.471166 -0.199488

Η

E = -0.497898 H 0.000000 0.000000 0.000000

HF

E = -100.413546 F 0.000000 0.000000 0.092136 H 0.000000 0.000000 -0.829224

SF4⁺.H2O

E = -873.366712 S 0.165540 -0.000020 -0.167246 F 1.718503 -0.000336 -0.313099 F 0.059043 -1.614571 -0.263625 F 0.082662 0.000013 1.376702 F 0.059759 1.614613 -0.263581 O -1.909852 0.000344 -0.138248 H -2.324936 -0.794389 -0.522027 H -2.324587 0.794480 -0.523631

SF₃H₂O⁺.HF

E = -874.066607S 0.870500 0.367763 -0.037748 F 2.183082 -0.509698 -0.008079 F 0.276436 -0.296564 1.243909 F 0.181889 -0.513130 -1.122210 O -1.019301 1.383850 -0.165583 F -2.572860 -0.769948 0.074362 H -3.405390 -1.171128 -0.007660 H -1.169566 2.199646 0.334632 H -1.815562 0.820534 -0.090194

 SF_4^+ E = -796.926912 S -0.000017 -0.000033 -0.244731 F 0.000118 1.202429 0.707925 F -1.585615 -0.000014 -0.490363 F 0.000084 -1.202315 0.708027 F 1.585443 -0.000040 -0.490511

SF5⁺.H2O

E = -973.202222 S -0.139557 -0.000056 0.001128 F 0.000147 -1.571653 0.034541 F -1.683753 -0.002304 -0.128966 F -0.000004 1.571880 -0.023155 F -0.165066 0.029073 1.568847 O 1.726121 0.002259 0.170740 H 2.153920 0.806713 -0.190198 H 2.153848 -0.806312 -0.180960 F 0.083806 -0.028949 -1.563801

SF₅.H₃O⁺

E = -973.804213 S 0.592506 0.015947 -0.186166 F -0.854260 -1.030111 -0.135406 F -0.466089 1.296534 -0.165371 F 1.493820 -1.302501 -0.331681 F 1.836109 0.987409 -0.322906 F 0.627541 -0.025265 1.373480 O -3.042856 0.040731 -0.142375 H -2.100777 -0.413497 -0.113970 H -3.027482 0.966143 0.163306 H -3.743088 -0.468227 0.305280

$SF_5.H_3O^+$

$$\begin{split} & E = -973.798769 \\ & S \ -0.152314 \ 0.192968 \ 0.000006 \\ & F \ -0.097198 \ 0.063733 \ 1.615925 \\ & F \ -1.661584 \ 0.569620 \ 0.004282 \\ & F \ -0.104327 \ 0.070184 \ -1.616442 \\ & F \ 0.421071 \ 1.644240 \ 0.001810 \\ & O \ -0.687680 \ -1.827152 \ -0.003060 \\ & F \ 2.232244 \ -0.554662 \ -0.002061 \\ & H \ -1.140437 \ -2.151283 \ 0.795412 \\ & H \ -1.161739 \ -2.145310 \ -0.791523 \\ & H \ 3.128793 \ -0.311719 \ -0.011133 \end{split}$$

$SF_5.H_3O^+$

E = -973.794227S 0.676688 0.001592 0.250824 F 0.627996 -1.617010 0.303179 F -0.264829 -0.012155 -1.079010 F -0.745072 0.036064 1.156783 F 1.995627 -0.035481 -0.645899 F 0.674257 1.617973 0.243634 O -2.887159 0.078712 -0.363525

H -1.979630 0.011340 -0.759535	S 0.000045 0.000015 -0.209526
H -2.813085 -0.029012 0.609268	F -1.636571 -0.008520 -0.248436
H -3.528840 -0.542011 -0.762907	F -0.009127 1.636416 -0.248936
	F 0.007930 -1.636415 -0.248979
SF_5H^+	F 1.636873 0.008533 -0.249244
E = -897.365635	F 0.000816 -0.000040 1.368086
S -0.251118 -0.000004 -0.151260	
F -0.020286 0.015993 1.366556	SF_{5}^{+}
F -0.157033 1.597495 -0.320875	E = -896.751698
F -1.788415 -0.048336 -0.234611	S 0.000000 0.000000 0.000000
F -0.051622 -1.584221 -0.307160	F 0.000000 1.534091 -0.000000
F 2.141216 -0.036191 -0.205555	F 1.328562 -0.767046 0.000000
H 2.903161 0.497406 -0.265038	F -1.328562 -0.767046 0.000000
	F 0.000000 0.000000 1.562457
SF ₅	F 0.000000 0.000000 -1.562457
E = -897.133095	

S7. References

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