

## Research Article

# A Novel Method to Predict the Permeability of Heterogeneous Sandstones Using Multiple Echo Spacing NMR Measurements

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We propose a novel method for estimating the permeability of heterogeneous sandstones based on the nuclear magnetic resonance (NMR) data with multiple echo spacings. The decaying curves and their corresponding spectra are obtained for different echo spacings to investigate the relaxation property, the diffusion term, and the signal loss contributed by higher echo spacing. Moreover, an empirical model is developed to correlate permeability with the differential decay rate. The result shows that the geometric transversal relaxation time is positively related to echo spacing, which disobeys the traditional cognition. Moreover, the absolute value of the differential decay rate is positively correlated with the echo spacing and exhibits a power law behavior. More interestingly, it is observed that the permeability diminishes in a power law behavior with respect to fitting parameters. This marks the first attempt to establish a relationship between the permeability and NMR data with different echo spacings, which is hopeful to be extended to other complex reservoirs with the availability of multiple echo spacing data.

## 1. Introduction

The low-field nuclear magnetic resonance (NMR) technique acts as an important tool in petroleum and geological studies. Compared with other geophysical data, the signal originates from hydrogen and provides valuable lithology-independent information such as pore size, porosity, permeability, fluid saturation, viscosity, as well as wettability [1–3]. The transversal relaxation time ( $T_2$ ) generated by the Carr-Purcell-Meiboom-Gill pulse sequence is the most frequently used parameter nowadays. Over the past few decades, there have been tremendous examples of permeability estimation using NMR data such as the Schlumberger-Doll Research equation and the Timur-Coates equation. Although both

equations provide a trend in permeability prediction, their shortcomings are obvious and they are demonstrated to have large errors in complex reservoirs such as carbonate, tight sand, shale, and mudstone [4–9]. The most widely used and improved permeability models are based on the two well-known equations incorporating the rock typing strategy, multiple regressions, and combination with other geophysical data [10–14]. Some models adopting the transformation of  $T_2$  and raw decaying signals are also reported to achieve favorable results [5].

However, the precision of these models is strongly dependent on the accuracy of the NMR data. It is recognized that the NMR measurement can be easily distorted due to inadequate signal acquisition, low signal-to-noise

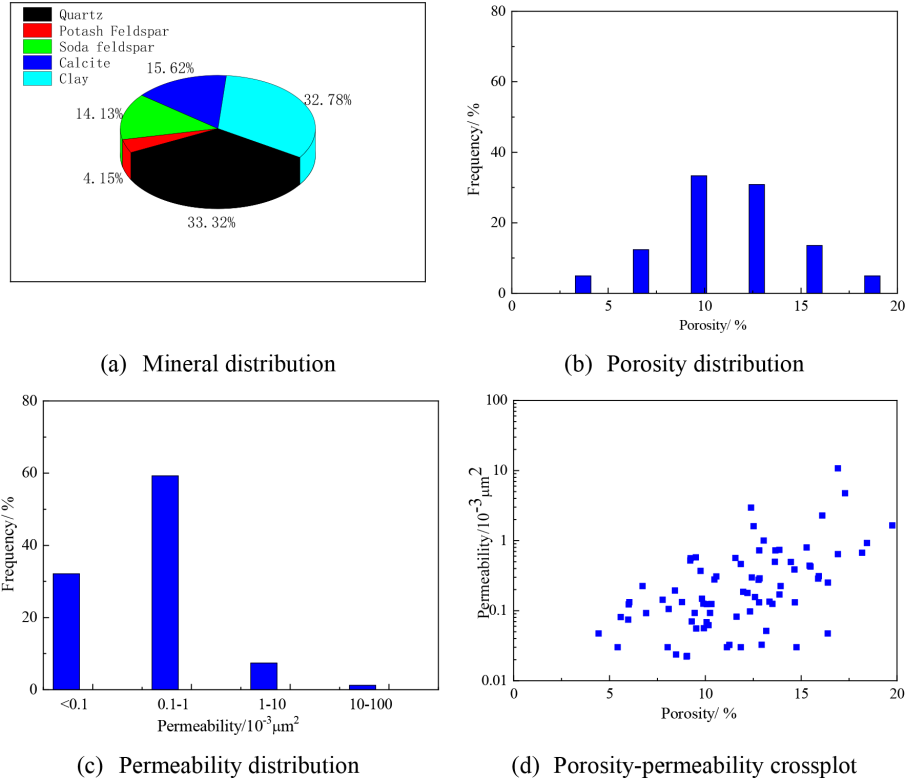


FIGURE 1: General lithology and reservoir property of the studied area.

ratio, inaccurate inversion algorithm, as well as the presence of paramagnetic materials [15, 16], resulting in an unreliable result.

This work discusses the NMR relaxation of the heterogeneous sandstone with different echo spacings to investigate the correlation between the permeability and the differential decay rate, aiming to propose a novel method for predicting the permeability. The rest of the paper is organized as follows. In Section 2, we describe the NMR theory and the experimental procedure. In Section 3, we analyzed the NMR responses at different echo spacings and proposed a novel model. We provide the conclusion and discussion in the last section.

## 2. Theory and Experiment

According to the NMR principle, the transversal relaxation time of the porous media is expressed as [2],

$$\frac{1}{T_2} = \frac{1}{T_{2s}} + \frac{1}{T_{2b}} + \frac{1}{T_{2d}} = \rho_2 \frac{S}{V} + \frac{1}{T_{2b}} + \frac{D(\gamma T_E)^2}{12} \quad (1)$$

where  $T_{2s}$ ,  $T_{2b}$ , and  $T_{2d}$  represent the surface transverse relaxation time, the bulk transverse relaxation time, and the diffusion transverse relaxation time, respectively.  $S$  is the surface area of pore space,  $V$  is the pore volume,  $\rho_2$  is the transversal surface relaxivity,  $D$  is the diffusion coefficient,  $\gamma$  is the gyromagnetic ratio,  $T_E$  is the echo spacing, and  $G$  is the magnetic field gradient.

In many studies, bulk and diffusion relaxations are often neglected. Consequently, the transversal relaxation time can be expressed as [2],

$$\frac{1}{T_2} = \frac{1}{T_{2s}} = \rho_2 \frac{S}{V} = \rho_2 \frac{F_s}{r} \quad (2)$$

where  $F_s$  is the pore shape factor and  $r$  is the pore radius.

Most pore structure evaluation methods and permeability models are based on the above assumption. However, the diffusion term cannot be ignored when the internal gradient is strong or the echo spacing is large, particularly in volcanic and shale reservoirs [17–19].

For well-defined porous media with a single intrinsic relaxation time, the differential decay rate between two different echo spacings is stated as [20],

$$\nabla \frac{1}{T_2} = \frac{1}{T_{2El}} - \frac{1}{T_{2Es}} = \frac{DG^2\gamma^2(T_{El}^2 - T_{Es}^2)}{12} \quad (3)$$

where  $T_{El}$  and  $T_{Es}$  represent the long and short echo spacings, respectively, and  $T_{2El}$  and  $T_{2Es}$  are the geometric transversal relaxation time of the long and short echo spacings.

The echo signal inverse problem can be transformed into a linear equation-solving problem:

$$y = Ax + \varepsilon \quad (4)$$

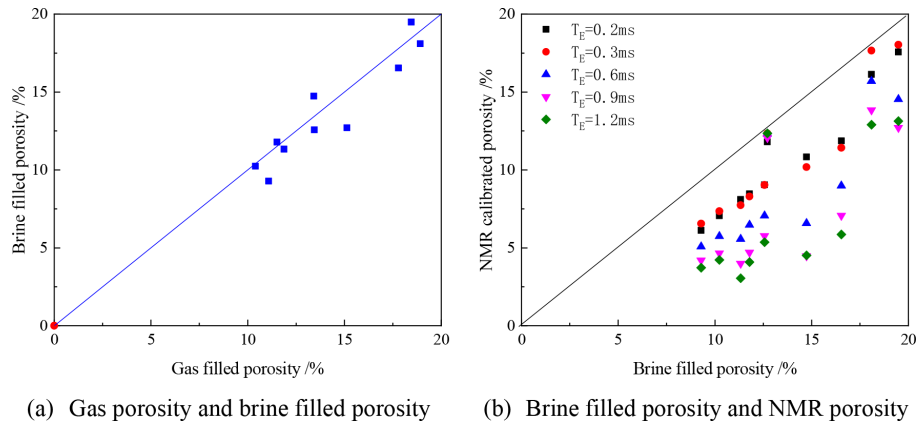


FIGURE 2: Comparisons among the porosity measured with different methods.

where  $y$  is the measured echo signal;  $A = \exp(-t/T_2)$ ;  $\varepsilon$  is the error; and  $x$  is the vector to be solved.

The formula obtained after regularization [21, 22]:

$$x_\alpha = \operatorname{argmin}\{\|Ax - y\|_2^2 + \alpha^2\|Lx\|_2^2\} \quad (5)$$

where  $\alpha$  is the regularization parameter and  $L$  matrix is the regularization operator.

The studied area is located in the eastern segment of Alkin Piedmont, Qaidam Basin, western China. Figure 1(a) presents the mineral distributions from the X-ray diffraction analysis. It is shown that the main constituents are quartz and clay. Figure 1(b) and Figure 1(c) represent the frequency distributions of gas porosity and gas permeability, indicating that the reservoir property is poor. Figure 1(d) shows the crossplot of the porosity and the permeability for typical samples. It is obvious that the relationship between the porosity and the permeability is scattered, indicating high heterogeneity.

Ten core samples were selected to conduct NMR experiments. After the necessary pretreatments, the gas porosity and steady-state permeability were measured first. Then, we used a 2 MHz NMR benchtop developed by the NIUMAG Corporation to detect the relaxation signals of brine-saturated samples. The detailed experimental procedure was elaborated in our previous publications [23]. The NMR acquisition parameters are as follows: the number of scans is 50, the waiting time is 6 seconds, the receiving gain is 80%, and the echo spacing series are 0.2 ms, 0.3 ms, 0.6 ms, 0.9 ms, and 1.2 ms, respectively.

### 3. Results and Analysis

Figure 2(a) shows the comparison between the gas porosity and the brine-filled porosity. It is seen that the porosity measured by both methods is equivalent. A slight deviation is attributed to the experimental error. Figure 2(b) depicts the relationship between the brine-filled porosity and the NMR porosity at different echo spacings. Generally, the NMR porosity is lower than the brine-filled porosity. The phenomenon reveals that the porosity is underestimated

by NMR measurements, which may be contributed by the fast relaxation components or other factors. In addition, the NMR porosity is generally inversely proportional to the echo spacing [20, 24]. However, each sample has its unique deviation trend with the echo spacing.

Figure 3 represents the  $T_2$  spectra measured at different echo spacings for brine-saturated samples. It is seen that the amplitude is also inversely proportional to the echo spacing but with different trends. More interestingly, substantial signal losses are observed for samples with high echo spacing, indicating the insufficient acquisition of fast relaxation components.

$$T_{2,mean} = \frac{\sum f_i T_{2i}}{\sum f_i} \quad (6)$$

Where  $T_{2,mean}$  is the geometric  $T_2$  mean;  $T_{2i}$  is the  $i$ th  $T_2$  relaxation; and  $f_i$  is the amplitude of the  $i$ th  $T_2$  relaxation component.

It is obvious from Figure 4(a) that the geometric  $T_2$  mean is positively correlated with the echo spacing. Consequently, a negative differential decay rate is observed, as shown in Figure 4(b). The possible reason may be that the influence of the signal loss caused by the echo spacing is more distinct than the diffusional relaxation induced by the internal gradient. The phenomenon is of great importance for petrophysicists, and special precautions should be taken when using the NMR data for formation evaluation. Moreover, the power function can be used to describe the relationship between the differential decay rate and the echo spacing, which is expressed as,

$$\left(-\nabla \frac{1}{T_2}\right) = AT_E^B \quad (7)$$

where  $A$  and  $B$  are fitting parameters.

Figure 4(c) and 4(d) show the relationship between the permeability and the above two fitting parameters. Interestingly, it is observed that the permeability exponentially decays with  $A$ , which is expressed by,

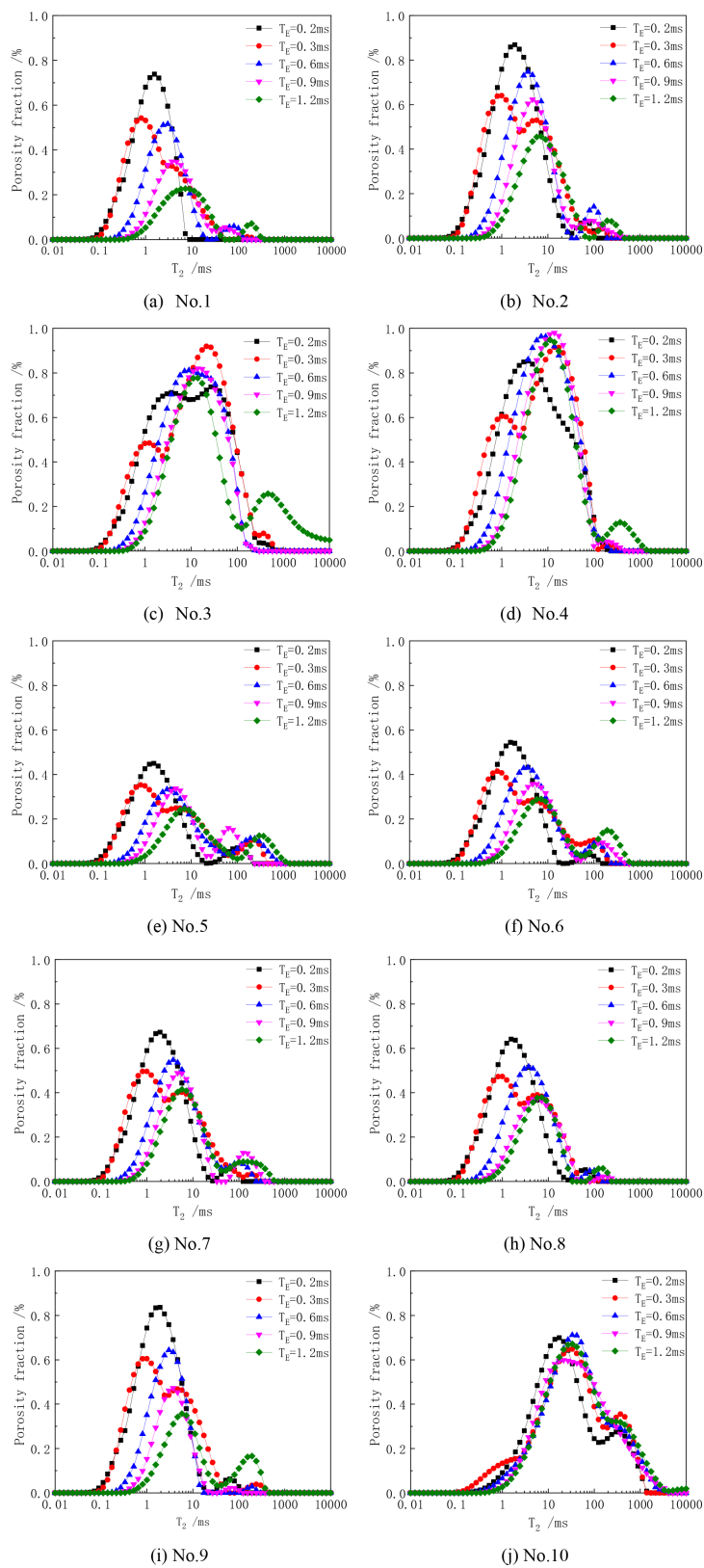


FIGURE 3: NMR  $T_2$  spectra of brine-saturated samples at different echo spacings.

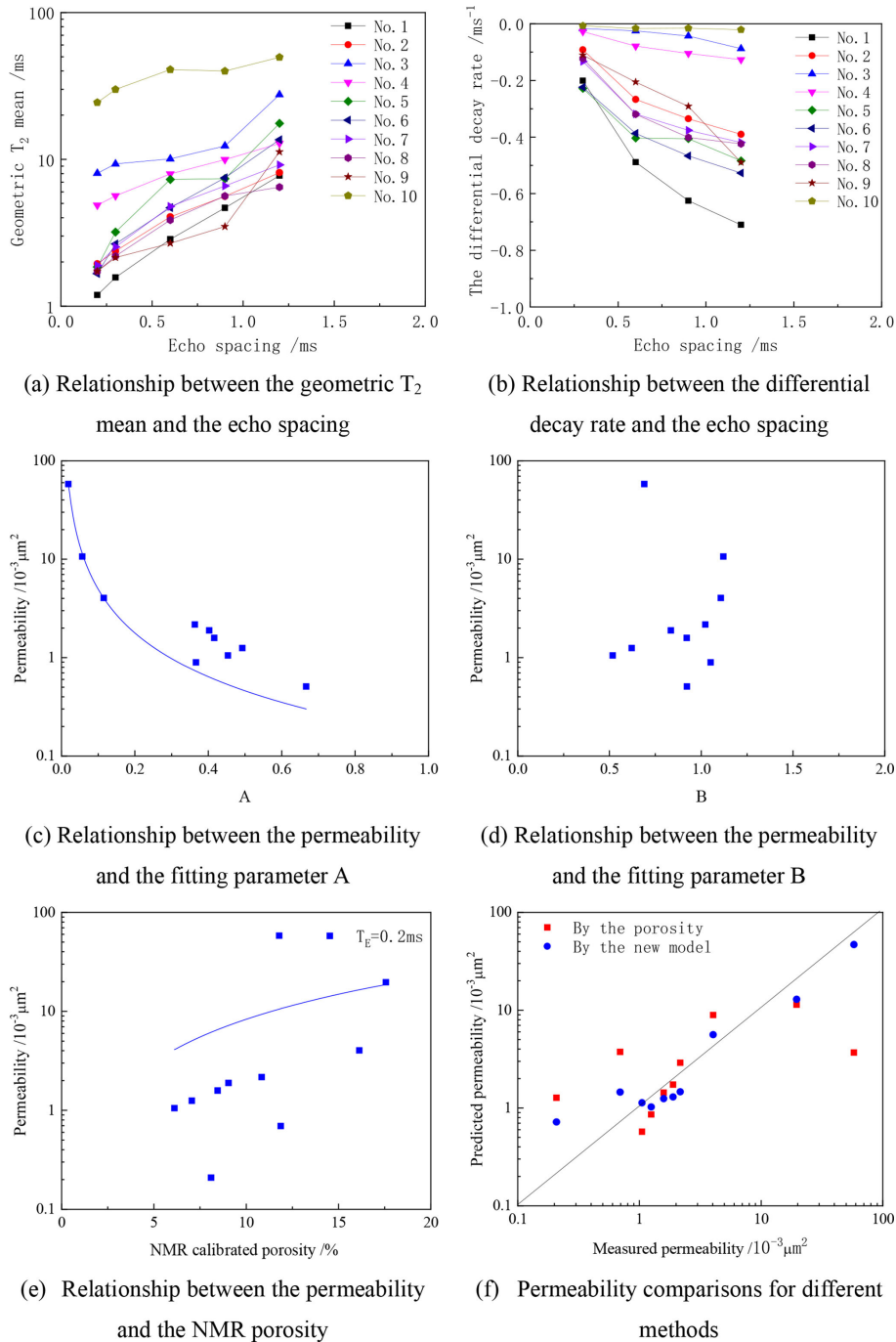


FIGURE 4: NMR  $T_2$  spectra of brine-saturated samples at different echo spacings.

$$K = cA^{-d} = c \left( \frac{\log\left(-\frac{1}{T_2}\right)}{B \log(T_E)} \right)^{-d} \quad (8)$$

where  $K$  is the permeability and  $c$  and  $d$  are fitting parameters. In this study, they are 0.447 and 1.172, respectively. The correlation coefficient is 0.946.

Meanwhile, the conventional porosity-permeability crossplot is also implemented to fit permeability, as is shown in Figure 4(e). It is obvious that the correlation is poor. Figure 4(f) compares the predicted permeability and

the measured permeability for all core samples. It is seen that the NMR-based permeability achieves higher reliability compared with the regression of the porosity although the theoretical fundamentals are not known.

#### 4. Conclusions

Based on NMR measurements of heterogeneous sandstone samples at different echo spacings, we have reached the following conclusions:

- (1) The echo spacing has a significant influence on NMR signals. Both the NMR porosity and the amplitude of  $T_2$  spectra are inversely proportional to the echo spacing.
- (2) The differential decay rate is negatively correlated with the echo spacing, indicating that the influence of the echo spacing is larger than the internal gradient.
- (3) The permeability is strongly correlated with the fitting parameter, and a power law behavior was observed between the absolute differential decay rate and the echo spacing.
- (4) The proposed permeability utilizing multiple echo spacing NMR data achieves favorable results compared with the conventional porosity-permeability crossplot model.

However, much work should be done to extend this model to field applications and other complex reservoirs. The theoretical fundamentals and the intrinsic mechanism of the relationship between the permeability and the echo spacing should be further investigated.

## Data Availability

The data that support the findings of this study are available on request from the corresponding author. The data are not publicly available due to privacy restrictions.

## Conflicts of Interest

The authors declare that they have no conflicts of interest.

## Acknowledgments

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