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Time-Delay Signature Suppression Using a Photonic Filter in Delayed Feedback Semiconductor Lasers

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- 6 semiconductor lasers5.

7 Abstract

- 8 Physiological phenomena are often accompanied by time delay effects which may lead to oscillatory
- 9 and even chaotic dynamics in their behaviors. Analogous dynamics is found in semiconductor lasers
- subject to delayed optical feedback where the dynamics typically includes a signature of the time
- delay. In many applications of semiconductor lasers, the suppression of the time delay signature is
- essential for applications and hence several approaches have been adopted for that purpose. In this
- paper experimental results are presented wherein photonic filters are utilized in order to suppress
- 14 time-delay signatures in semiconductor lasers subject to delayed optical feedback effects. Two kinds
- of semiconductor lasers are used: discrete mode semiconductor lasers and vertical-cavity surface-
- emitting lasers (VCSELs). It is shown that, by the use of photonic filters, complete suppression of the
- 17 time-delay signature may be affected in discrete mode semiconductor lasers but that a remnant of the
- 18 signature persists for VCSELs.

19 1 Introduction

- 20 The study of the effects of time-delay has been identified as an aid to characterizing physiological
- 21 systems and their regulatory mechanisms. It is found, for example, that oscillations and chaos can be
- 22 established in blood flow due to time-delay effects (Holstein-Rathlou 1993). Analogous oscillatory
- 23 and chaotic behavior has been studied in considerable theoretical and experimental detail in
- semiconductor lasers subject to delayed optical feedback (Soriano et al. 2013). Because of their ease
- of operation, semiconductor lasers offer a convenient testbed for exploring the diverse dynamical
- behavior which may arise when the laser is subject to optical feedback (Kane and Shore 2005;
- 27 Ohtsubo 2013). There is a considerable variety of semiconductor lasers and their response to such
- 28 time-delayed optical feedback is dependent upon detailed characteristics of the lasers. In turn, such
- 29 varieties of behavior may be instructive for the exploration of dynamical behaviors arising in
- 30 physiological systems in which time delay effects play a significant role in the determination of
- 31 physiological phenomena.
- 32 In general, when time delays are the drivers of dynamics, there is a characteristic signature of those
- delays contained within the system dynamics. The finite time of signal propagation between nodes of
- a network may manifest itself as a time delay signature (TDS). Such a signature is often undesirable
- and hence effort has been given to suppression of the TDS. Thus, for example, in the case of chaotic

- semiconductor lasers being used for secure communications (Argyris et al. 2005), the persistence of a
- 37 time delay signature (TDS) may compromise the security of data transmission (Rontani et al. 2009).
- In this context, substantial efforts have been dedicated to erase time-delay signatures (Shahverdiev
- and Shore 2009; Nguimdo et al. 2011; Li, Liu, and Chan 2012; Niangiang Li et al. 2012; Zhong et al.
- 40 2013; Hong 2013; A. Wang et al. 2013; Xiang et al. 2014; Hong, Spencer, and Shore 2014; Li and
- 41 Chan 2015; Mu et al. 2016; Hong et al. 2016; D. Wang et al. 2017; J. Zhang et al. 2017; 2018; Li, Li,
- 42 and Chan 2018; Jiang et al. 2018; Zhao et al. 2019; Ma et al. 2020; R. Zhang et al. 2020; Cui et al.
- 43 2022). These efforts encompass various methods, including modulated optoelectronic feedback,
- 44 distributed feedback from a fiber Bragg grating, phase-modulated feedback, chaos optical injection,
- 45 mutual injection, cascaded injection, and the influence of factors like fiber scattering and dispersion.
- 46 Most of these investigations have centered on vertical-cavity surface-emitting lasers (VCSELs) or
- distributed feedback (DFB) semiconductor lasers.
- 48 Recent research, however, has uncovered unique characteristics of chaos generated in discrete mode
- 49 (DM) semiconductor lasers, demonstrating the possibility of achieving flat broadband chaos through
- optical feedback under optimized conditions (Chang et al. 2020). However, the study of the TDS of
- 51 chaos generated in optically injected DM lasers remains unexplored. DM lasers are a distinct type of
- 52 Fabry–Pérot (FP) lasers that etch a small number of features along the ridge waveguide, modifying
- 53 the cavity spectrum to amplify a single cavity mode while suppressing others, ensuring single-mode
- operation (Osborne et al. 2007). DM lasers offer several advantages, including cost-effectiveness,
- resilience to optical feedback, stable single mode emission, a broad operational temperature range,
- and high bandwidth. In this paper, a novel approach to eliminate time delay signatures by using
- 57 photonic filters in a DM laser is explored. To facilitate comparison, the same experimental
- 58 configuration is applied to a VCSEL. The findings of this study underscore the exceptional efficacy
- of photonic filters in suppressing time-delay signatures in DM lasers, whereas in the case of
- 60 VCSELs, complete signature suppression remains elusive.

61 **2** Experimental setup

- 62 The schematic experimental setup is shown in Figure 1. In the experiment, two distinct types of laser
- diodes (LD) are employed to conduct the experiment. Firstly, we utilize a discrete mode (DM) laser
- 64 (EP1550-DM-01-FA) from Eblana Photonics. Secondly, we employ VCSELs of the RayCan
- RC330001-FFA type. Both LDs are driven by a low-noise current source (Thorlabs LDC201 CU)
- and maintained at room temperature stability through a highly precise temperature controller
- 67 (Lightwave LDT-5412) and the lasing wavelengths are around 1550 nm.
- 68 For the conventional feedback setup, the feedback loop is formed by an optical circulator (OC), fiber
- 69 couplers (FC1 and FC2), a semiconductor optical amplifier (SOA), a variable optical attenuator
- 70 (VA), and a polarization controller (PC). Within this feedback loop, the SOA serves to amplify the
- feedback power, the VA is used to adjust the feedback power, and the PC regulates the polarization
- of the feedback beam to ensure maximum efficiency on the dynamics of the lasers.
- 73 In the photonic filter feedback setup, a variable fiber coupler (VFC: Newport F-CPL-1550 N-FA
- FC3) is integrated into the feedback loop, as indicated by the dashed frame. The photonic filter
- 75 feedback configuration is established by connecting ports 2 and 4 of the VFC. This arrangement is
- 76 commonly referred to an infinite impulse response single-source microwave photonic filters (IIR
- SSMPFs) or fiber ring resonators, and its specification details have been comprehensively discussed
- 78 in (Capmany, Ortega, and Pastor 2006)

- 79 In the detection section, 10% of the optical power is split using FC1 and directed towards an optical
- 80 spectrum analyzer (OSA: Agilent 86141B with a resolution of 0.06 nm) for optical spectrum
- 81 measurements. Simultaneously, FC2 separates 50% of the power from the feedback loop and directs
- it to a third fiber coupler (FC3). FC3 further divides the optical power evenly and routes it to two 82
- photodetectors: a 12 GHz photodetector (PD1: New Focus 1544-B) and a 40 GHz photodetector 83
- 84 (PD2: Thorlabs, RXM40AF). The outputs of PD1 and PD2 are recorded by an oscilloscope (OSC,
- Tektronix TDS 7404) with a bandwidth of 4 GHz and an electrical spectrum analyzer (RF, R&S 85
- FSEK20) with a bandwidth of 40 GHz, respectively. The oscilloscope operates at a sampling rate of 86
- 20 GS/s, with a total time duration of 2 μ s. 87
- 88 In this paper, the optical feedback ratio is defined as the ratio of the feedback power to the output
- 89 power of the free-running laser. The optical feedback power is the power of the feedback beam
- before it enters the laser. It is measured at port 1 of the OC, taking into consideration the loss from 90
- 91 port 1 to port 2 of the OC. In the experiment, we also investigate the effect of the coupling ratio of
- 92 the VFC on the TDS. The coupling ratio is defined as the percentage of the power transferred from
- 93 port 1 to port 4 in the VFC, as shown in Figure 1.

3 **Time Delay Signature Analysis Methods**

- Numerous techniques are available for a qualitative assessment of the TDS, for example, mutual 95
- information (Rontani et al. 2009; Nguimdo et al. 2011; N. Li et al. 2012; Li and Chan 2015; D. Wang 96
- 97 et al. 2017; J. Zhang et al. 2017), autocorrelation coefficient (ACC)(Rontani et al. 2009; Shahverdiev
- 98 and Shore 2009; Li, Liu, and Chan 2012; N. Li et al. 2012; Zhong et al. 2013; Hong 2013; A. Wang
- 99 et al. 2013; Xiang et al. 2014; Hong, Spencer, and Shore 2014; Li and Chan 2015; Mu et al. 2016;
- Hong et al. 2016; D. Wang et al. 2017; J. Zhang et al. 2017; 2018; Li, Li, and Chan 2018; Jiang et al. 100
- 2018; Zhao et al. 2019; Ma et al. 2020; R. Zhang et al. 2020; Cui et al. 2022), permutation entropy 101
- 102 (PE)(Zhong et al. 2013; Hong 2013; Xiang et al. 2014; Mu et al. 2016; Cui et al. 2022). In this study,
- 103 we utilize both the ACC and PE methods to detect the TDS. The ACC, denoted as C is defined as
- 104 follows

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$$C(\Delta t) = \frac{\left\langle \left[I(t + \Delta t) - \left\langle I(t + \Delta t) \right\rangle \right] \left[I(t) - \left\langle I(t) \right\rangle \right] \right\rangle}{\sqrt{\left\langle \left[I(t + \Delta t) - \left\langle I(t + \Delta t) \right\rangle \right]^{2} \left\langle \left[I(t) - \left\langle I(t) \right\rangle \right]^{2} \right\rangle}}$$

- 106 where I represents the output intensity of the laser, < denotes a time average, and Δt is the delay time.
- The value of C falls within the range of -1 to 1. A value of 1 signifies complete positive correlation, 107
- 108 while -1 indicates full negative (anti) correlation. When the value is 0, it denotes a state of complete
- 109 randomness, indicating no correlation whatsoever.

- 111 The PE method, initially introduced by Bandt and Pompe (Bandt and Pompe 2002), involves a time
- 112 series $\{I_t, t=1, 2, ..., N\}$, which represents the measures N samples of the output intensities of the laser.
- Given the time series $\{I_t, t=1,2,...,N\}$, subsets S_q , each containing M samples (M>1) of the measured 113
- 114 intensities, are formed with an embedding delay time $\tau = nT_s$, where n is an integer number and T_s is the reciprocal of the sampling rate. The ordinal patterns of subsets are expressed as $S_q = [I(t), I(t+\tau),$ 115
- ...I(t+(M-1)τ)]. For practical purposes, Bandt and Pompe recommended choosing M within the range 116
- 117 of 3 to 7. In this work, we have selected M to be 5. Each subset Sq can be organized as [I(t+(r₁-
- $1)\tau \le I(t+(r_2-1)\tau) \le ... \le I(t+(r_M-1)\tau)]$. Thus, each subset can be uniquely represented as an "ordinal 118

- pattern" $\pi = (r_1, r_2, ..., r_M)$, which is one of the possible permutations of subset S_q with M dimensions.
- The permutation entropy is derived from the probability distribution $p(\pi)$ as follows:

121
$$p(\pi) = \frac{\#\{t | t \le N - M - n + 1; S_q \text{ has type } \pi\}}{N - M - n + 1}$$

- where the symbol # denotes "number". The permutation entropy is then determined using the probability $p(\pi)$:
- $h(p) = -\sum p(\pi)\log p(\pi)$

- **127 4 Results**
- 128 4.1 Discrete Mode (DM) Laser
- The DM laser used in this experiment has a threshold current of 12.5 mA at room temperature and is
- biased at 80 mA. Initially, conventional optical feedback is introduced by disconnecting ports 2 and 4
- of the VFC.
- Figure 2 shows the time traces (top row), autocorrelation coefficient curves (middle row) and the PE
- curves (bottom row) of the output of the DM laser subject to optical feedback. The left, middle and
- right columns are for the feedback ratio of -14.5 dB, -10.5 dB and -1.5 dB, respectively. In Figure
- 135 2(A), the red line represents the DM laser's time trace without optical feedback. From the time traces
- in Figure 2, it can be seen that the laser exhibits random fluctuations in all three feedback ratios,
- indicating chaos dynamics. To identify the TDS, their corresponding autocorrelation coefficient C as
- a function of the delay time are calculated and shown in the middle row of Figure 2. At a feedback
- ratio of -14.6 dB (Figure 2(D)), a significant peak occurs at around 116.8ns, corresponding to the
- feedback round trip time (τ_1) , is observed. This peak, referred to as TDS, is quantified using the peak
- value of the autocorrelation coefficient at around the feedback round trip time (C_p) . For Figure 2(D),
- the TDS is approximately 0.82. As the feedback ratio increases to -10.5dB, the TDS decreases to
- about 0.39, as shown in Figure 2(E). Further increasing the feedback ratio to -1.5 dB results in a
- reduced TDS of approximately 0.2, as depicted in Figure 2(F).
- We also utilize PE to investigate the TDS, as shown in the bottom row of Figure 2. In Figure 2(G-I),
- many troughs attributable to harmonics and sub-harmonics of the feedback round trip time can be
- observed. Notably, the deepest troughs, occurring around $\tau_1 \approx 116.8$ ns, are less pronounced in the PE
- analysis compared to the autocorrelation coefficient analysis (middle row of Figure 2). Therefore, we
- focus on the autocorrelation coefficient for the remaining investigation.
- 150 The peak value of the autocorrelation coefficient at the feedback round trip time as a function of the
- 151 feedback ratio is calculated and presented in Figure 3. The result indicates that the TDS decreases as
- the feedback ratio increases when the feedback ratio is less than approximately -7 dB. Beyond this
- threshold, the TDS begins to rise as the feedback ratio increases, peaking around a feedback ratio of -
- 3.5 dB. Subsequently, with further increases in the feedback ratio, the TDS diminishes once more.
- Notably, the minimum TDS of 0.24 is achieved at the maximum feedback ratio of -1.5 dB. This is
- 156 corroborated by the autocorrelation coefficient curve displayed in Figure 2(F), which distinctly
- identifies the time delay signature at 116. 8 ns.

- Moving to photonic filter feedback, we connect port ports 2 and 4 of the VFC. Initially, the coupling
- ratio is set at 50%, equally splitting the powers between ports 3 and 4. In Figure 4, the time traces
- 160 (upper row) and autocorrelation coefficient curves (bottom row) are presented for the DM laser with
- photonic filter feedback. The feedback ratios for the left, middle and right columns in Figure 4 match
- those in Figure 2: -14.5 dB, -10.5 dB, and -1.5 dB, respectively. The red line in Figure 4(A)
- 163 corresponds to the free-running DM laser's output.
- Similar to conventional feedback, the laser exhibits random fluctuations in all three feedback ratios,
- indicative of chaotic dynamics. The corresponding autocorrelation coefficient curves are displayed in
- the bottom row of Figure 4. In Figure 4(D), aside from the highest peak at approximately 116.8ns,
- smaller peaks appear around 20.5 ns, 127.05 ns and 137.3ns. These additional peaks are attributed to
- the time delay introduced by the ring cavity recirculation. Each recirculation within the ring cavity
- introduces a delay time (τ_2) of approximately 10.25ns. The highest peak has a value of approximately
- 170 0.68. In the case of -10.5 dB feedback ratio, as shown in Figure 4(E), the maximum peak value
- decreases to about 0.37. When the feedback ratio increases to approximately -1.5dB, as demonstrated
- in Figure 4(F), no distinguishable peaks are observed. The TDS has been completely concealed.
- The maximum peak value of the autocorrelation coefficient at the feedback round trip times (τ_1 ,
- $\tau_1 + \tau_2$, $\tau_1 + 2\tau_2$, τ_2 , or other combinations) as a function of the feedback ratio is presented in Figure 5.
- 175 The result demonstrates a consistent decrease in the TDS as the feedback ratio increases. When the
- feedback ratio reaches approximately -2.0dB, the TDS value is approximately 0.03. Further increases
- in the feedback ratio yield minimal changes in TDS due to the absence of distinguishable peaks in the
- 178 autocorrelation curves.
- 179 The influence of the coupling ratio of the photonic filter on the time delay signature is also explored.
- In Figure 6, curve A represents the scenario with conventional feedback, while the remaining curves
- correspond to setups involving photonic optical feedback, each with different coupling ratios. It is
- evident that at lower feedback ratios, photonic filter feedback does not show any advantage in
- suppressing the TDS compared to conventional feedback. However, as the optical feedback intensity
- increases, the addition of photonic filter feedback proves advantageous in suppressing the TDS,
- particularly when the coupling ratio approaches 50%.

4.2 VCSELs

- 187 To investigate whether the concealment of the TDS is solely attributable to photonic filter feedback,
- we conducted a similar experiment using a VCSEL. The threshold current of the VCSEL used in the
- experiment is 1.8 mA at the room temperature and is biased at 4 mA. Figure 7 displays the TDS as a
- 190 function of the feedback ratio in the VCSEL with various coupling ratios. Notably, the addition of
- 191 photonic filter feedback at coupling ratios of 50% or 72% effectively suppressed TDS across all
- 192 feedback ratios, which is similar to the results observed in DFB lasers (Cui et al. 2022). However, for
- coupling ratios below 13%, the TDS exhibit little deviation from conventional optical feedback, in
- 194 contrast to DM lasers, where TDS suppression with photonic filter feedback is primarily observed at
- higher feedback ratios. Remarkably, even a lower coupling ratio as 7% still significantly contributes
- 196 to TDS suppression in DM lasers at higher feedback ratios. The optimal coupling ratio for TDS
- suppression in the VCSEL is determined to be 72%. The minimum TDS achieved in the VCSEL is

- approximately 0.12 at a feedback ratio of around 1.0 dB with the coupling ratio of 72%, which is
- higher than the minimum TDS of 0.03 observed in the DM laser.
- Figure 8 presents the autocorrelation coefficient curve obtained under the influence of photonic filter
- 201 feedback with optimal coupling ratio and the optical feedback ratio in the VCSEL. This curve
- exhibits three distinct peaks, with delay times of approximately 10.25ns, 112.45ns and 122.7ns,
- 203 corresponding to τ_2 , τ_1 , and $\tau_1+\tau_2$, respectively. This observation indicates that the presence of
- 204 photonic filter feedback in the VCSEL is unable to entirely eliminate TDS.

5 Conclusion

- In this study, we conducted experimental investigations into the TDS of semiconductor lasers under
- 208 conventional feedback and photonic filter feedback conditions. Specifically, two types of
- semiconductor lasers, namely, DM lasers and VCSELs, are comprehensively examined. Our findings
- 210 highlight the substantial advantages of photonic filter feedback in TDS suppression, particularly
- evident in the case of DM lasers. At the optimal coupling ratio and optical feedback ratio, we
- achieved remarkable TDS reduction, with the TDS minimized to as low as 0.03, effectively
- 213 concealed within the background noise. For DM lasers, the benefits of photonic filter feedback in
- TDS suppression manifest primarily at higher feedback ratios. Conversely, in the case of VCSELs,
- 215 photonic filter feedback proves advantageous across a wider spectrum of feedback ratios, particularly
- in the coupling ratio range of approximately 50% to 72%. Nevertheless, it is worth noting that in
- VCSELs, while photonic filter feedback induces significant TDS suppression with an appropriate
- coupling ratio, a residual TDS signature remains discernible. The reason the photonic filter can
- suppress the TDS is that the photonic filter feedback is equivalent to optical feedback from multiple
- external cavities with different lengths, and due to the multiple Vernier effect, the TDS is suppressed.
- The disparity between DM lasers and VCSELs can be attributed to their respective laser structures.
- 222 DM lasers feature multiple etching features along the ridge waveguide, which alter the characteristics
- of the laser spectrum. This modification, in turn, mitigates the occurrence of recurring features
- induced by optical feedback. Combining the multiple Vernier effect with the modified laser spectrum
- 225 totally conceals the TDS in the discrete mode laser with photonic filter feedback. However, the
- effectiveness of photonic filter feedback for TDS suppression is diminished in VCSELs because they
- lack the same special spectrum characteristics as discrete mode lasers. Without the specific spectrum
- 228 provided by the multiple etching features along the ridge waveguide, the photonic filter cannot totally
- suppress the TDS in VCSELs.
- 230 This research serves not only to enhance our comprehension of TDS control in semiconductor lasers
- but also holds significance in the context of physiological phenomena. Physiological processes often
- exhibit time delay effects, which can contribute to oscillatory and even chaotic dynamics in their
- behaviors. The insights gained from this study can contribute to the better understanding and
- 234 management of physiological phenomena marked by time-delayed feedback, opening new avenues
- for research and applications in the realm of controlling and regulating complex physiological
- 236 systems.

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Data Availability Statement

239 Datasets are available on request:

- 240 The raw data supporting the conclusions of this article will be made available by the authors, without
- 241 undue reservation.

242 Conflict of Interest

- 243 The authors declare that the research was conducted in the absence of any commercial or financial
- relationships that could be construed as a potential conflict of interest.

245 6 Author Contributions

- 246 YH: Conceptualization, Data curation, Formal Analysis, Investigation, Methodology, Software,
- Writing-original draft, Writing-review and editing. ZQZ: Data curation, Formal Analysis, Project
- administration, Writing-review and editing. KAS: Data curation, Writing-original draft, Writing-
- review and editing.

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Figure Captions

Figure 1. Experimental setup

Figure 2. The time traces (top row), autocorrelation coefficient curves (middle row) and the PE curves (bottom row) of the output of the DM laser subject to optical feedback. The feedback ratios are -14.5 dB (left column), -10.5 dB (middle column) and -1.5 dB (right column). The red line in Figure 2(A) is the free-running DM laser output.

Figure 3. The TDS as a function of the feedback ratio for the conventional feedback.

Figure 4. The time traces (top row) and autocorrelation coefficient curves (bottom row) of the output of the DM laser with photonic filter feedback with the coupling ratio of 50%. The feedback ratios are -14.5 dB (left column), -10.5 dB (middle column) and -1.5 dB (right column). The red line in Figure 4(A) is the free-running DM laser output.

Figure 5. TDS as a function of the feedback ratio for the photonic filter feedback with the coupling ratio of 50%.

Figure 6. TDS as a function of the feedback ratio in the DM laser with optical feedback. Curve A is for conventional optical feedback. Curves B, C, D, E, F and G are for photonic filter feedback with the coupling ratio of 7%, 13%, 26%, 50%, 72% and 94%, respectively.

Figure 7. TDS as a function of the feedback ratio in the VCSEL with various coupling ratios.

Figure 8. The autocorrelation coefficient curve of the output of the VCSEL with photonic filter feedback with the coupling ratio of 72% and the feedback ratio of 1.0 dB.

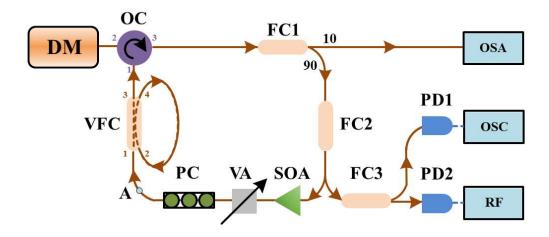


Figure 1. Experimental setup

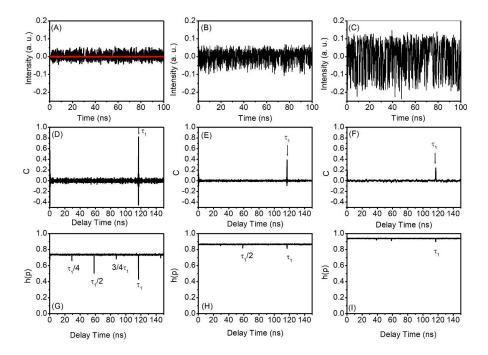
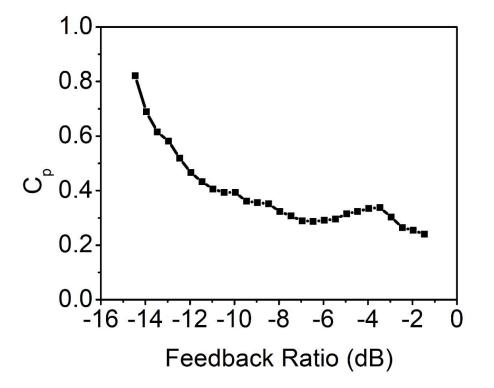
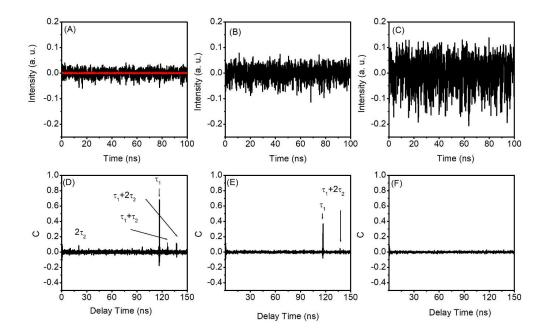
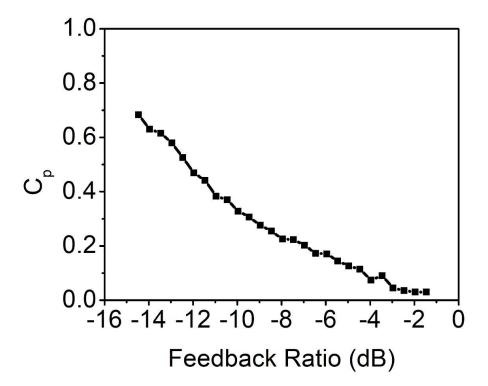
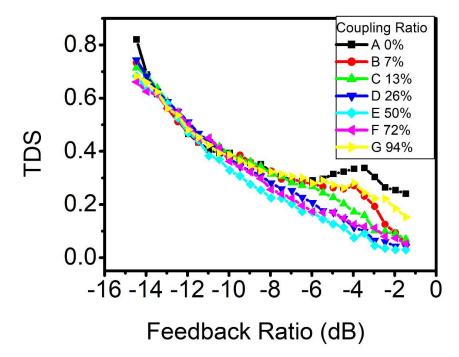


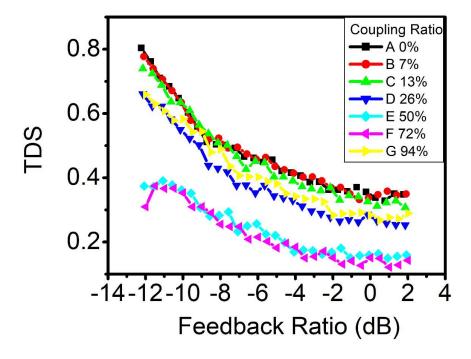
Fig. 2

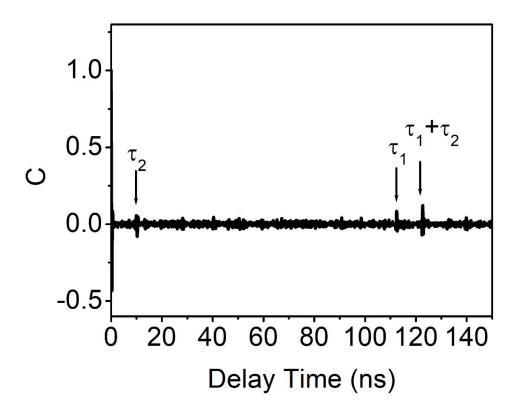












386 Fig. 8