Original Paper

Derivation of the temperature dependent constants for KAIO₂ and NaAIO₂ in a viscosity predictive model for high aluminosilicate melts

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The compositional dependence of the viscosity was studied for two high aluminosilicate melt series: $Na_2O-CaO-Al_2O_3-SiO_2$ (NCAS) and $K_2O-Na_2O-CaO-Al_2O_3-SiO_2$ (KNCAS). The viscosity and the glass transition temperature were measured by concentric cylinder viscometry and differential scanning calorimetry, respectively. This work discusses the viscosity predictive model set up by Bottinga and Weill. The temperature dependent constant, *D*, defining the relative impact of each component on the viscosity, was derived for the compositional range from 35 to 45 mol% SiO₂ for KAIO₂ and NaAlO₂, respectively. With the newly derived *D*-values, a good agreement was achieved between measured and predicted values.

1. Introduction

Mineral wool production, traditionally, relies on locally available rocks and slag. Some variations in the chemical compositions are commonly accepted as long as the basic melt and glass properties are maintained. The melt viscosity is one of the parameters that have to be within rather narrow limits to ensure good process conditions. Therefore, predictive viscosity models are commonly used. The stone wool industry often applies the viscosity model set up by Bottinga and Weill [1] (the BW model). The model is valid for a broad range of chemical compositions, and it still appears to be one of the most accurate models for the prediction of melt viscosity, even thirty years after it was published. However, for melts with a silica content between 35 and 45 mol% data is limited, and the calculation of viscosity relies, to some extent, on analogous assumptions.

The BW model [1] is based on the assumption that each component of the melt contributes to a change in the viscosity (η , where the viscosity is calculated in 10⁻¹ Pa s using equation (1)), according to the amount of the component in the melt:

$$\ln \eta = \Sigma (X_{\rm i} \cdot D_{\rm i}) \tag{1}$$

where X_i is the molar fraction of the component, and D_i is a temperature dependent constant for a given component. The *D*-values from (1) were found by fitting the model to a set of viscosity data for different melts. The data set consists

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270

of 2440 data points collected over the years and covers the temperature range from 1473 to 2073 K with 50 K intervals.

The *D*-values are given for various intervals of the SiO_2 content. The number of *D*-values at the lowest SiO_2 content of 35 to 45 mol% is limited. The *D*-values for NaAlO₂ and KAlO₂ are missing: in fact, *D*-values for KAlO₂ are missing in all the SiO₂ intervals. Even though directions for application of *D*-values for neighbouring SiO₂ intervals are given [1], better documentation for high aluminosilicate melts containing Na⁺ and K⁺ is desired.

The purpose of the present paper is to derive new temperature dependent constants, to be included in the BW model. This is done by studying melts containing SiO₂, CaO, Al₂O₃, Na₂O and K₂O. All the studied melts are high aluminosilicate melts with a low content of SiO₂ (37.3 mol%). Viscosity measurements of these melts provide a set of *D*-values for NaAlO₂ and KAlO₂ for temperature intervals of 25 K according to the method used in [1].

Establishing these *D*-values can improve the applicability of the BW model and contribute to the understanding of the effect of Na^+ and K^+ on the viscosity of high aluminosilicate melts.

Two compositional joins were examined in the interval 35 to 45 mol% SiO₂. The melts are depolymerized, and the ratio of nonbridging to tetrahedrally coordinated oxygen (NBO/T) is equal to 1. The first join, called the NCAS series, contains six melts with a constant amount of SiO₂ (37.3 mol%) and Al₂O₃ (14.7 mol%), whereas the amounts of Na₂O and CaO were changed throughout the melt series to increase the ratio 2Na/(2Na+Ca) from 0 to 0.42. The



Figure 1. The heat flow rate versus temperature showing the determination of T_{g} .

viscosities of the NCAS melt series were measured, and *D*-values for NaAlO₂ were found by fitting the model to the obtained viscosity data. The second join, called the KNCAS series, contains five melts with a constant amount of SiO₂ (37.3 mol%), Al₂O₃ (14.7 mol%) and CaO (39.9 mol%), whereas the amounts of Na₂O and K₂O were changed throughout the series to increase the ratio K/(K+Na) from 0 to 1. This was done in order to establish the *D*-values for KAlO₂ with the same method as for NaAlO₂.

2. Experimental methods

The high aluminosilicate melts from the NCAS and KNCAS melt series were synthesized from the analytical chemicals SiO_2 , Al_2O_3 , $CaCO_3$, Na_2CO_3 and K_2CO_3 in a Pt-crucible at 1773 K for 4 h. Subsequently, the melts were quenched on a brass disc at room temperature. The chemical compositions were analysed by X-ray fluorescence spectroscopy (XRF) (Philips 1404, Eindhoven (Netherlands)).

Shear viscosities in the range from 1823 K to the temperature of crystallization were measured at 25 K intervals in air atmosphere using concentric cylinder viscometry (ccv) (Paar Physica, Physica Rheolab MC 1, Stuttgart (Germany)). The main parts of the viscometer are a 30 mm long Pt80Rh20 cylinder with a 16 mm diameter, including conical ends, and a 70 mm high Pt80Rh20 crucible with a 22 mm diameter. A speed of rotation of approximately 40 rpm was maintained throughout the measurements. Viscosity measurements continued for one hour at each temperature.

The glass transition temperature (T_g) was determined by differential scanning calorimetry (DSC), (Jupiter, NETZSCH STA 449 C, Cell, Selb (Germany)), using heating and cooling rates of 10 K/min. T_g was defined as the onset temperature of the heat flow rate versus the temperature curve (figure 1). The dimensions of the glass samples were (5x5x1) mm³.

3. Results

Table 1 displays the chemical compositions of the melts. Figures 2 and 3 show the viscosity-temperature relationship for the two melt series NCAS and KNCAS, respectively. The viscosities cover the range from 0.3 to 13 Pa s and are summarized in tables 2 and 3. Figure 2 shows that, for the NCAS melt series, there is no pronounced compositional dependence of the viscosity except for NCAS 0, which has a slightly lower viscosity, at a certain temperature, than the other melts. Figure 3 shows the viscosity-temperature relationship for the KNCAS melt series. At a certain temperature, the viscosity increases with increasing substitution of K⁺ for Na⁺.

The T_g values are given in table 4. T_g decreases almost linearly as the 2Na/(2Na+Ca) ratio increases for the NCAS melt series. For the KNCAS melt series an increase in the K/(K+Na) ratio leads to a nonlinear increase of T_g .

Modelling with the BW model

In the BW model, each component in the melt has a unique contribution to the viscosity. A component is defined as a structural unit in the melt structure. The structural units are primarily SiO₂ tetrahedra, but also Al_2O_3 forms tetrahedral units when charge balancing cations are present. Other structural units are network-modifying cations in the form of oxide units such as CaO and Na₂O [1 and 3].

If more than one charge balancing cation is available, their willingness to combine with Al^{3+} is defined by the following order $K^+ > Na^+ > Ba^{2+} > Sr^{2+} > Ca^{2+} > Mg^{2+}$ > Mn^{2+} . This order corresponds to that of structural stability of aluminosilicate melts as discussed below. Due to this order the amount of KAlO₂ is calculated first, then NaAlO₂, and so forth.

The contribution to the viscosity from each component is an empirically determined D-value times the molar ratio of the component (equation (1)). The D-value defines the impact the component has on the viscosity. A component with a high D-value has a larger contribution to the viscosity than a component with a small or even negative Dvalue.

In the BW model, data are grouped according to the amount of SiO₂ (35 to 45, 45 to 55, 55 to 65, 65 to 75, 75 to 81 mol%) in the melts. Therefore, each SiO₂ interval has a set of *D*-values for each component and each temperature. In the SiO₂ interval of 35 to 45 mol%, *D*-values for NaAlO₂ and KAlO₂ are not available. Bottinga & Weill recommend using the *D*-values for NaAlO₂ from the neighbouring SiO₂ interval (45 to 55 mol%) for both NaAlO₂ and KAlO₂. However, estimates of *D*-values for both NaAlO₂ and KAlO₂ have been based upon the results of this study (table 5).

The *D*-values given in [1] are listed for a certain temperature with steps of 50 K. In order to calculate model viscosities at 25 K intervals, the *D*-values as a function of 1/T were linearly extrapolated to cover temperatures in between (table 5). The difference between the measured and the modelled viscosity was minimized by altering the *D*-values for NaAlO₂ and KAlO₂, respectively. The *D*-values for NaAlO₂ were found using the viscosity data from the NCAS series, Table 1. Compositions of the melts analysed by XRF given in mol%. In the KNCAS series the numbers, e.g. 2-6, correspond to the approximate mol% of K_2O and Na_2O , respectively. The sample NCAS 8 was used as the pure Na-bearing end member in the KNCAS series.

melt	oxide content in mol%					2Na/(2Na+Ca)	K/(K+Na)
	SiO ₂	Al ₂ O ₃	CaO	Na ₂ O	K ₂ O		
NCAS 0*	37.3	14.7	47.9	-	-	0	
NCAS 4	36.9	15.3	43.6	4.2	-	0.09	- 8
NCAS 8	37.3	15.0	39.4	8.3	-	0.16	0
NCAS 12	37.3	14.9	35.3	12.5	-	0.26	-
NCAS 16	37.1	14.9	31.4	16.6	-	0.35	_
NCAS 20	37.3	14.4	28.2	20.1	-	0.42	_
KNCAS 2-6	36.9	14.9	40.0	6.2	2.0	F	0.33
KNCAS 4-4	37.0	15.1	39.6	4.4	3.8		0.46
KNCAS 6-2	37.4	14.7	40.0	2.1	5.9	—	0.73
KNCAS 8-0	36.3	15.2	40.6	0.2	7.6		1.0

* Values are from [2].



Figure 2. lg η as a function of 1/T for the NCAS series.



Figure 3. lg η as a function of 1/T for the KNCAS series.

and the *D*-values from [1], listed in table 5. The *D*-values for KAlO₂ were found using the viscosity data from the KNCAS series, the *D*-values given in [1], and the estimated *D*-values for NaAlO₂ (table 5). *D*-values for components given in [1] are reasonably accurate because they are based on a comprehensive data set.

272

Table 2. Viscosities η for melt series NCAS 0 measured by concentric cylinder viscometry at various temperatures *T*. Values are from [2].

T in K	η in Pa s		
1849	0.31		
1825	0.37		
1801	0.43		
1776	0.51		
1776	0.60		
1752	0.73		
1728	0.90		
1704	1.13		
1679	1.44		
1655	1.89		
1631	2.52		
1607	3.47		
1583	4.94		

The application of the new D-values for NaAlO₂ and KAlO₂ for prediction of the viscosity was tested on a melt with the following composition (in wt%): 31.3 SiO₂, 20.3 Al₂O₃, 0.6 TiO₂, 10.3 FeO, 20.5 CaO, 8.3 MgO, 3.0 Na₂O, 3.2 K₂O and 0.5 MnO. The viscosity was measured by GLAFO, Växjö (Sweden). Figure 4 shows the measured viscosity, the viscosity predicted when including the new Dvalues for NaAlO₂ and KAlO₂, the viscosity predicted using the D-values for NaAlO₂ from the SiO₂ interval 45 to 55 mol% (which is the neighbouring SiO₂ interval) for both KAlO₂ and NaAlO₂, for the remaining components the Dvalues are from the SiO₂ interval 35 to 45 mol% (a method suggested in [1]), and finally the viscosity predicted without including D-values for NaAlO2 and KAlO2. Figure 4 shows that it is not reasonable to predict the viscosity without including the D-values for NaAlO2 and KAlO2. Furthermore, the D-values derived for NaAlO2 and KAlO2 were found to be reasonable, since the predicted viscosities were in good agreement with the measured ones.

5. Discussion

The ability for a cation to charge-balance an alumina tetrahedron is determined by the field strength. Ions with high

Derivation of the temperature dependent constants for KAIO2 and NaAIO2 in a viscosity predictive model ...

T in K	η in Pa s								
2 2	NCAS 4	NCAS 8	NCAS 12	NCAS 16	NCAS 20	KNCAS 2-6	KNCAS 4-4	KNCAS 6-2	KNCAS 8-0
1823	0.49	0.51	0.47	0.48	0.44	0.51	0.71	0.75	0.79
1798	0.58	0.59	0.57	0.63	0.54	0.64	0.88	0.95	1.03
1773	0.70	0.73	0.71	0.73	0.65	0.81	1.06	1.11	1.28
1748	0.85	0.88	0.84	0.86	0.82	1.01	1.30	1.41	1.61
1723	1.07	1.12	1.05	1.06	1.01	1.27	1.57	1.83	2.13
1698	1.37	1.35	1.28	1.31	1.29	1.56	1.97	2.22	2.68
1673	1.76	1.64	1.63	1.58	1.69	1.95	2.42	2.85	3.39
1648		2.06	2.06	2.00	2.07	2.46	3.13	3.63	4.42
1623		2.60	2.53	2.52	2.55	3.13	4.16	4.79	5.99
1598			3.29	3.18	3.27				
1573			4.30	4.11	4.16				
1548				5.28	5.26				
1523				6.99	6.82				
1498				9.31	8.89				
1473				12.73	11.90				

Table 4. Glass transition temperatures measured with DSC, where heating and cooling rates of 10 K/min were used.

melt series	$T_{\rm g}$ in K			
NCAS 0	1075			
NCAS 4	1025			
NCAS 8	992			
NCAS 12	961			
NCAS 16	933			
NCAS 20	906			
KNCAS 2-6	997			
KNCAS 4-4	1008			
KNCAS 6-2	1028			
KNCAS 8-0	1054			

Table 5. *D*-values for the BW model for the components KAlO₂ and NaAlO₂ found by a least squares fit to the viscosity data, valid for the SiO₂ interval 35 to 45 mol%. Using the *D*-values derives the viscosity in 10^{-1} Pa s. *D*-values for $1/_2$ CaAl₂O₄ are from [1]. (There appears to be a misprint in the *D*-value for CaO at 1723 K given in [1], which is seen clearly when *D*-values for CaO are compared versus temperature. Therefore, the *D*-value has been changed from 0.71 to -0.71 in this work.)

T in K	<i>D</i> -values							
	KAlO ₂	NaAlO ₂	¹ / ₂ CaAl ₂ O ₄	CaO	Na ₂ O	SiO ₂		
1623	10.55	5.43	2.70	0.39	-4.93	4.43		
1648	9.71	4.82	2.43	0.12	-4.97	4.30		
1673	9.00	4.50	2.16	-0.16	-5.00	4.17		
1698	8.77	4.30	2.09	-0.44	-5.02	4.04		
1723	8.65	4.12	2.01	-0.71	-5.03	3.90		
1748	7.89	3.70	2.47	-0.94	-5.07	3.79		
1773	7.23	3.52	2.93	-1.17	-5.11	3.67		
1798	8.49	4.43	3.09	-2.33	-5.16	3.54		
1823	9.45	5.27	3.25	-3.48	-5.20	3.41		

field strength polarize the bridging oxygens, thereby they weaken the network-forming bonds and destabilize the overall structure of the melt. Cations with low field strength

1.0 -lgη (η in Pa s)-0.5 0.0 2 -0.5 Measured, Glafo (Växjö, Sweden) 0 Calculated with new D-values С Δ Calculated with neighbouring D-values for NaAlO -1.0 Calculated without NaAlO, and KAIO, D-values 1500 1600 1700 1800 -T in K-

Figure 4. lg η as a function of the temperature for the melt with the following composition (in wt%): 31.3 SiO₂, 20.3 Al₂O₃, 0.6 TiO₂, 10.3 FeO, 20.5 CaO, 8.3 MgO, 3.0 Na₂O, 3.2 K₂O and 0.5 MnO. The figure shows the measured viscosity, the viscosity predicted when including the new *D*-values for NaAlO₂ and KAlO₂, the viscosity predicted using the neighbouring *D*-values for NaAlO₂ to calculate for both NaAlO₂ and KAlO₂ (as suggested in [1]) and, finally, the viscosity predicted without including *D*-values for NaAlO₂ and KAlO₂.

affect the network forming bonds less strongly than cations with high field strength. The result is that cations with low field strength will create a less perturbed structure with stronger bonds. The mobility of structural units decreases, thereby the resistance of the melt to flow increases, and hence also the viscosity [3 and 4]. Cations can therefore be listed according to their charge-balancing ability in the following order $Cs \approx Rb > K > Na > Li \approx Ba > Pb > Sr > Ca > Mg$ [5]. This order is in agreement with the allocation given in [1] based on viscosity data, and it also reflects the increasing ability of the cation to compete with the Al^{3+} or Si^{4+} for bonding to bridging oxygen [3].

In the low viscosity range, no dramatic change in viscosity was demonstrated for the NCAS melt series when



1.0 1623 K 1748 K • ∇ 1648 K Δ 1773 K 0.8 1673 K 0 1798 K ٠ 1698 K 1823 K . 0.6 gn (n in Pa s) 0 1723 K . 0.4 . \diamond \diamond 0.2 ∇ 0 ∇ ∇ Δ \diamond 0 Δ 0.0 ∇ 0 V A 0 -0.2 0 0 0.0 0.2 0.4 0.6 0.8 1.0 K/(K+Na)

Figure 5. Isothermal plot of $\lg \eta$ as a function of the 2Na/(2Na+Ca) ratio.

substituting $2Na^+$ for Ca^{2+} as seen in figure 5. However, the slight increase in viscosity (at a given temperature) from melt NCAS 0 to NCAS 4 is a response to the initial substitution of Na⁺ for Ca²⁺, because the ability of Na⁺ to charge-balance for Al tetrahedrons is higher than that of Ca²⁺. The charge-balancing by Na⁺ instead of Ca²⁺ may stabilize the melt structure and thereby increase the viscosity. Both melt NCAS 16 and melt NCAS 20 contain more Na⁺ than required for charge-balancing Al³⁺, and the excess Na⁺ acts as modifying ions. Figure 2 shows that substitution of two network modifying Na⁺ for one network modifying Ca²⁺ does not influence the viscosity-temperature relationship. The network modifying 2Na⁺ plays the same role as the modifying Ca²⁺ in the melt.

In contrast to the high temperature-viscosity relationship, a pronounced decrease in T_g with increasing substitution of Na⁺ for Ca²⁺ was seen. This reflects a different structural response to the substitution of Na⁺ for Ca²⁺ in the low temperature range from that in the high temperature range.

The *D*-values in table 5 illustrate that the contribution of Na⁺ to the change in viscosity is higher than that of Ca²⁺/2. That was to be expected because Na⁺ is believed to be a better charge-balancing ion than Ca²⁺ and, therefore, the contribution to the viscosity per tetrahedron must be higher for Na⁺ than for Ca²⁺.

In the KNCAS melt series, the Ca^{2+} , Si^{4+} , and Al^{3+} contents were maintained constant whereas Na^+ was stepwise replaced with K^+ . In this way, the different effect on the viscosity of applying either K^+ or Na^+ as the chargebalancing ion was observed. The effect on the viscosity due to the charge-balancing ability of the cations (K^+ and Na^+) is modest compared to the effect on the viscosity due to the low concentration of both K_2O and Na_2O relative to the CaO concentration. However, an increase in the viscosity is expected due to the replacement of Na^+ with K^+ . This replacement resulted in an increase in the viscosity at a specific temperature in the high temperature range (figure 6). This suggests that K^+ , in contrast to Na^+ , strengthens the structural network even more when it acts as the charge-

Figure 6. Isothermal plot of $\lg \eta$ as a function of the K/(K+Na) ratio.



Figure 7. Compositional dependence of the 1, 1.6, 2.5 and 10^{12} Pa s isokom temperature. The 10^{12} Pa s isokom temperature is equal to $T_{\rm g}$ of each melt.

balancing ion. The reason is that K^+ has higher field strength, causing a lower polarizing ability.

When Na^+ is stepwise replaced with K^+ , a negative deviation from the linearity in $T_{lg\eta}$ as a function of composition occurred in the high viscous range, however, not in the low viscous range (figure 7). This negative deviation is shown as the 10¹² Pas isokom temperature, denoted as $T_{\lg\eta=12}$. $T_{\lg\eta=12}$ is equal to T_g of each melt because the viscosity at T_g is generally assigned to 10^{12} Pa s. The deviation from linearity in the high viscous range is a reflection of the mixed alkali effect. This mixing phenomenon has previously been reported in [6 to 9]. However, the mixed alkali effect for the KNCAS melt series is not as pronounced as for the glass series 16(Na, K)₂O·10CaO·74SiO₂ (in mol%) (named in the following as the NKCS melt series) described in [7]. The mixed alkali effect vanishes with increasing temperature because the topological contribution to the configurational entropy is predominant compared to the chemical contribution [10]. The mixed alkali effect is less pronounced in the KNCAS melt series than in the NKCS melt series as a consequence of the much higher NBO/T for the KNCAS than for the NKCS melt series. Furthermore, a high content of Ca²⁺ will reduce the mixed alkali effect.

It is seen from the *D*-values in table 5 that $KAIO_2$ contributes more to the viscosity of the melt than $NaAIO_2$. This indicates, as mentioned previously, that K^+ as a charge-balancing ion with aluminium in silicate melts results in a more stable network than Na^+ .

6. Conclusion

In the high viscous range, the substitution of Na⁺ for Ca²⁺ in the NCAS melt series showed a decrease in T_g with increasing 2Na/(2Na+Ca). In the low viscosity range, the substitution had a less pronounced effect on the viscosity. In the KNCAS melt series, the viscosity for a specific high temperature increases with increasing K/(K+Na). The negative deviation from linearity in T_g values of the KNCAS melt series is caused by the mixed alkali effect.

For the SiO₂ interval, 35 to 45 mol%, *D*-values for KAlO₂ and NaAlO₂ are derived. The *D*-values derived for KAlO₂ are the first derived *D*-values for KAlO₂ at all. At a specific temperature, *D*-values for KAlO₂ were found to be higher than *D*-values for NaAlO₂. Likewise, *D*-values for NaAlO₂ were found to be higher than *D*-values for $^{1/2}CaAl_2O_4$. In conclusion, the efficiency of the charge-balancing ions is in agreement with the succession given by the field strength. By including the *D*-values for KAlO₂ and NaAlO₂, the BW model becomes more accurate in predicting the viscosity for melts in the compositional range from 35 to 45 mol% SiO₂.

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