

# VIRTUAL REALITY FOR ASSEMBLY METHODS PROTOTYPING

## A REVIEW

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### Abstract

Assembly planning and evaluation is an important component of the product design process in which details about how parts of a new product will be put together are formalized. A well designed assembly process should take into account various factors such as optimum assembly time and sequence, tooling and fixture requirements, ergonomics, operator safety, and accessibility, among others.

Existing computer-based tools to support virtual assembly either concentrate solely on representation of the geometry of parts and fixtures and evaluation of clearances and tolerances or use simulated human mannequins to approximate human interaction in the assembly process. Virtual reality (VR) technology has the potential to support integration of natural human motions into the computer aided assembly planning environment (CAAP) [1]. This would allow evaluations of an assembler's ability to manipulate and assemble parts and result in reduced time and cost for product design.

This paper provides a review of the research in virtual assembly and categorizes the different approaches. Finally, critical requirements and directions for future research are presented.

**Keywords:** virtual assembly, collision detection, physics-based modeling, constraint-based modeling, virtual reality, haptics, human-computer interaction.

## 1. Introduction

Innovation is critical for companies to be successful in today's global market. Competitive advantage can be achieved by effectively applying new technologies and processes to challenges faced in current engineering design practices. Opportunities encompass all aspects of product design (including ergonomics, manufacture, maintenance, product life cycle, etc.) with the greatest potential impact during the early stages of the product development process. Prototyping and evaluation are indispensable steps of the current product creation process. Although computer modeling and analysis practices are currently used at different stages, building one-of-a-kind physical prototypes makes the current typical process very costly and time consuming.

New technologies are needed that can empower industry with a faster and more powerful decision making process. VR technology has evolved to a new level of sophistication during the last two decades. VR has changed the ways scientists and engineers look at computers for performing mathematical simulations, data visualization, and decision making [2-5]. VR technology combines multiple human-computer interfaces to provide various sensations (visual, haptic, auditory, etc.) which give the user a sense of presence in the virtual world. This enables users to become immersed in a computer-generated scene and interact using natural human motions. The ultimate goal is to provide an "invisible interface" that allows the user to interact

with the virtual environment as they would with the real world. This makes VR an ideal tool for simulating tasks that require frequent and intuitive manual interaction such as assembly methods prototyping.

Several definitions of virtual assembly have been proposed by the research community. For example, in 1997, Jayaram et al. [6] defined virtual assembly as “The use of computer tools to make or “assist with” assembly-related engineering decisions through analysis, predictive models, visualization, and presentation of data without physical realization of the product or supporting processes.” Kim and Vance [7] in 2003, described virtual assembly as the “ability to assemble CAD models of parts using a three-dimensional immersive, user interface and natural human motion”. This definition included the need for an immersive interface and natural interaction as a critical part of virtual assembly. As VR continues to advance we would like to expand previous definitions to provide a more comprehensive description.

Virtual assembly in this paper is defined as the capability *to assemble virtual representations of physical models through simulating realistic environment behavior and part interaction to reduce the need for physical assembly prototyping resulting in the ability to make more encompassing design/assembly decisions in an immersive computer generated environment.*

## **2. Why Virtual Assembly?**

Assembly process planning is a critical step in product development. In this process, details of assembly operations, which describe how different parts will be put together, are formalized. It has been established that assembly processes often constitute the majority of the cost of a product [8]. Thus, it is crucial to develop a proper assembly plan early in the design stage. A good assembly plan incorporates considerations for minimum assembly time, low cost,

ergonomics and operator safety. A well-designed assembly process can improve production efficiency and product quality, reduce cost and shorten product's time to market.

Expert assembly planners today typically use traditional approaches in which the three-dimensional (3D) CAD models of the parts to be assembled are examined on two dimensional (2D) computer screens in order to assess part geometry and determine assembly sequences for a new product. As final verification, physical prototypes are built and assembled by workers who identify any issues with either the assembly process or the product design. As assembly tasks get more complicated, such methods tend to be more time consuming, costly and prone to errors.

Computer aided assembly planning (CAAP) is an active area of research that focuses on development of automated techniques for generating suitable assembly sequences based primarily on intelligent identification and groupings of geometric features [9-14]. These methods rely on detailed information about the product geometry, but they do not account for the expert knowledge held by the assembler that may impact the design process. This knowledge, based on prior experience, is difficult to capture and formalize and could be rather extensive[15]. Ritchie et al. [1] proposed the use of immersive virtual reality for assembly sequence planning. System functionality was demonstrated using an advanced electromechanical product in an industrial environment. Holt et al. [16] propose that a key part of the planning process is the inclusion of the human expert in the planning. They base their statements on research in cognitive ergonomics and human factors engineering. Leaving the human aspect out of the assembly planning could result in incorrect or inefficient operations. Another limitation of the computer aided assembly planning methods is that as the number of parts in the assembly increase, the possible assembly sequences increase exponentially and thus it becomes more difficult to characterize criteria for choosing the most suitable assembly sequence for a given product [17].

Once again, the human input is critical to arriving at a cost-effective and successful assembly sequence solution.

Modern CAD systems are also used in assembly process planning. CAD systems require the user to identify constraint information for mating parts by manually selecting the mating surfaces, axes and/or edges to assemble the parts. Thus, these interfaces do not reflect human interaction with complex parts. For complex assemblies, such part-to-part specification techniques make it difficult to foresee the impact of individual mating specifications on other portions of the assembly process, for example ensuring accessibility for part replacement during maintenance, or assessing the effects of changing the assembly sequences. Such computer-based systems also lack in addressing issues related to ergonomics such as awkward to reach assembly operations, etc.

VR technology plays a vital role in simulating such advanced 3D human-computer interactions by providing users with different kinds of sensations (visual, auditory and haptic) creating an increased sense of presence in a computer generated scene. Virtual assembly simulations allow designers to import concepts into virtual environments during the early design stages and perform assembly/disassembly evaluations that would only be possible much later, when the first prototypes are built. Using virtual prototyping applications, design changes can be incorporated easily in the conceptual design stage thus optimizing the design process towards Design for Assembly (DFA). Using haptics technology designers can touch and feel complex CAD models of parts and interact with them using natural and intuitive human motions. Collision and contact forces calculated in real-time can be transmitted to the operator using robotic devices making it possible for him/her to feel the simulated physical contacts that occur during assembly. In addition, the ability to visualize realistic behavior and analyze complex

human interactions makes virtual assembly simulations ideal for identifying assembly related problems such as awkward reach angles, insufficient clearance for tooling, and excessive part orientation during assembly, etc. They also allow designers to analyze tooling and fixture requirements for assembly.

In addition to manufacturing, virtual assembly systems could also be used to analyze issues that might arise during service and maintainability operations such as inaccessibility to parts that require frequent replacement, etc. Expert assembly knowledge and experience that is hard to document could be captured by inviting experienced assembly workers from the shop floor to assemble a new design and provide feedback for design changes [18]. Disassembly and recycling factors can also be taken into account during the initial design stages allowing for an environmentally conscious design. Virtual assembly training can provide a platform for offline training of assembly workers which is important when assembly tasks are hazardous or specially complicated [19].

In order to simulate physical mockups in an effort to provide a reliable evaluation environment for assembly methods, virtual assembly systems must be able to accurately simulate real world interactions with virtual parts, along with their physical behavior and properties [20]. To replace or reduce the current prototyping practices, a virtual assembly simulation should be capable of addressing both the geometric and the subjective evaluations required in a virtual assembly operation. Boothroyd, et al. [21] describes the more subjective evaluations of assembly as the following:

- Can the part be grasped in one hand?
- Do parts nest or tangle?
- Are parts easy or difficult to grasp and manipulate?

- Are handling tools required?
- Is access for part, tool or hands obstructed?
- Is vision of the mating surfaces restricted?
- Is holding down required to maintain the part orientation or location during subsequent operations?
- Is the part easy to align and position?
- Is the resistance to insertion sufficient to make manual assembly difficult?

If successful, this capability could provide the basis for many useful virtual environments that address various aspects of the product life cycle such as ergonomics, workstation layout, tooling design, off-line training, maintenance, and serviceability prototyping (Figure 1).

### 3. Virtual Assembly - Challenges

Several technical challenges must be overcome to realize virtual assembly simulations,



**Fig. 1:** Applications of a Virtual Assembly/Disassembly Simulation

namely: accurate collision detection, inter-part constraint detection and management, realistic physical simulation, data transfer between CAD and VR systems, intuitive object manipulation (inclusion of force feedback), etc. In the following section, these challenges are described and previous approaches in each area are summarized.

### **3.1 Collision Detection**

Virtual assembly simulations present a much larger challenge than virtual walkthrough environments as they require frequent human interaction and real time simulation involving complex models. Real world assembly tasks require extensive interaction with surrounding objects including grabbing parts, manipulating them realistically and finally placing them in the desired position and orientation. Thus, for successfully modeling such a complex interactive process, the virtual environment not only needs to simulate visual realism, it also needs to model realistic part behavior of the virtual objects. For example, graphic representations of objects should not interpenetrate and should behave realistically when external forces are applied. The first step to accomplish this is implementing accurate collision detection among parts [22].

Contemporary CAD systems typically used in product development incorporate precise geometric models consisting of hierarchical collections of Boundary Representation (B-Rep) solid models bounded with trimmed parametric NURBS surfaces. These representations are typically tessellated for display, and the resulting polygonal graphics representations can be used to detect collisions. However, the relatively high polygon counts required to represent complex part shapes generally result in relatively long computation time to detect collisions. In virtual environments where interactive simulation is critical, fast and accurate collision detection among dynamic objects is a challenging problem.



Algorithms have been developed to detect collisions using different object representations. Several algorithms that use polygonal data for collision detection were designed by researchers at the University of North Carolina and include I-collide [23], SWIFT [24], RAPID [25], V-collide [26], SWIFT++ [27], and CULLIDE [28]. Other methods such as V-Clip [29] and VPS [30] have also been proposed to use in immersive VR applications. A comprehensive review of collision detection algorithms can be found in [31, 32] and a taxonomy of collision detection approaches can be found in [33].

Once implemented, collision detection prevents part interpenetration. However, collision detection does not provide feedback to the user regarding how to change position and orientation of parts to align them for completing the assembly operation [34]. Two main classifications of techniques for implementing part positioning during an assembly include physics-based modeling and constraint-based modeling. Physics-based modeling simulates realistic behavior of parts in a virtual scene. Parts are assembled together with the help of simulated physical interactions that are calculated in real-time. The second technique utilizes geometric constraints similar to those used by modern CAD systems. In this approach, geometric constraints such as concentricity, coplanar surfaces, etc. are applied between parts thus reducing the degrees-of-freedom and facilitating the assembly task at hand.

### **3.2 Inter-part Constraint Detection and Management**

Due to the problems related to physics-based modeling (instability, difficult to attain interactive update rates, accuracy etc.), several approaches using geometric constraints for virtual assembly have been proposed. Constraint-based modeling approaches use inter-part geometric constraints (typically predefined and imported, or defined on the fly) to determine relationships between components of an assembly. Once constraints are defined and applied, a constraint

solver computes the new and reduced degrees-of-freedom of objects and the object's resulting motion.

A vast amount of research focused on solving systems of geometric constraints exists in the literature. Numerical constraint solver approaches translate constraints into a system of algebraic equations. These equations are then solved using iterative methods such as Newton-Raphson [35]. Good initial values are required to handle the potentially exponential number of possible solutions. Although solvers using this method are capable of handling large non-linear systems, most of them have difficulties handling over-constrained and under-constrained instances [36] and are computationally expensive which makes them unsuitable for interactive applications such as virtual assembly [37]. Constructive constraint approaches are based on the fact that in principle, most configurations of engineering drawings can be solved on a drawing board using standard drafting techniques [38]. In the rule-constructive method, "solvers use rewrite rules for discovery and execution of construction steps". Although complex constraints are easy to handle, exhaustive computation requirements (searching and matching) of these methods make them inappropriate for real world applications [39]. Examples of this approach are described in [40-42]. Graph-constructive approaches are based on analysis of the constraint graph. Based on the analysis, a set of constructive steps are generated. These steps are then followed to place the parts relative to each other. Graph constructive approaches are fast, methodical and provide means for developing robust algorithms [38, 39, 43, 44]. An extensive review and classification of various constraint solving techniques is presented in [36].

### **3.3 Physics-Based Modeling**

The physics-based modeling approach relies on simulating physical constraints for assembling parts in a virtual scene. Physical modeling can significantly enhance the user's sense

of immersion and interactivity, especially in applications requiring intensive levels of manipulation [45]. Physics-based algorithms simulate forces acting on bodies in order to model realistic behavior. Such algorithms solve equations of motion of the objects at each time step, based on their physical properties and the forces and torques that act upon them.

Physics-based modeling algorithms can be classified into three categories based on the method used, namely the penalty force method, the impulse method, and the analytical method. In the penalty force method, a spring-damper system is used to prevent interpenetration between models. Whenever a penetration occurs, a spring-damper system is used to penalize it [30, 46]. Penalty based methods are easy to implement and computationally inexpensive, however they are characterized with problems caused by very high spring stiffness leading to stiff equations which are numerically intractable [47]. The impulse based methods [48-50] simulate interactions among objects using collision impulses. Static contacts in this approach are modeled as a series of high frequency collision impulses occurring between the objects. The impulse based methods are more stable and robust than penalty force methods. However, these methods have problems handling stable and simultaneous contacts (such as a stack of blocks at rest) and also in modeling static friction in certain cases like sliding [51]. The Analytical method [52, 53] checks for interpenetrations. If found, the algorithm backtracks the simulation to the point in time immediately before the interpenetration. Based on contact points, a system of constraint equations is solved to generate contact forces and impulses at every contact point [54]. The results from this method are very accurate however it requires extensive computation time when several contacts occur simultaneously.

Thus, although various algorithms for physics-based modeling have evolved over the years, simulating realistic behavior among complex parts interactively and accurately is still a challenging task.

## **4 Review of Virtual Assembly Applications**

Progress in constraint modeling and physics-based modeling has supported substantial research activity the area of virtual assembly simulations. In this paper we categorize these assembly applications as either constraint-based or physics-based systems.

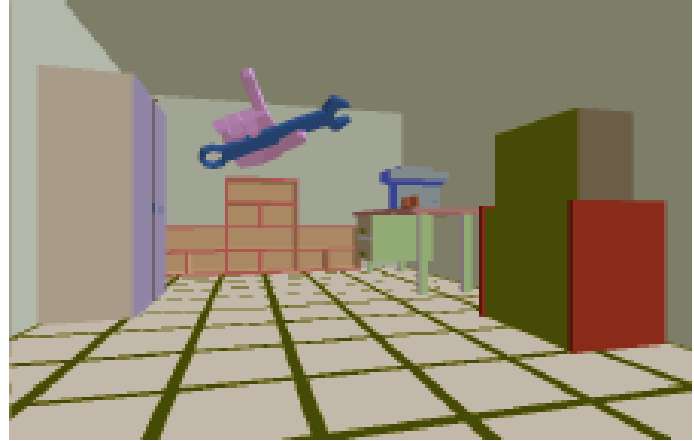
### **4.1 Constraint-Based Assembly Applications**

The first category consists of systems that use constraints to place parts in their final position and orientation in the assembly. Constraints in the context of this research are of two types. The first are positional constraints, which are pre-defined final part positions. The second are geometric constraints which relate part features and are applied when related objects are in proximity. Geometric constraints are useful in precise part positioning tasks in a virtual environment where physical constraints are absent [55, 56]. Constraint based methods summarized in section 3.2 are used to solve for relative object movements.

#### ***4.1.1 Systems Using Positional Constraints***

IVY (Inventor Virtual Assembly) developed by Kuehne and Oliver [57] used IRIS Open Inventor graphics library from Silicon Graphics and allowed designers to interactively verify and evaluate the assembly characteristics of components directly from a CAD package. The goal of IVY was to encourage designers to evaluate assembly considerations during the design process to enable design-for-assembly (DFA). Once, the assembly was completed, the application rendered a final animation of assembly steps in a desktop environment.

The high cost of VR systems encouraged researchers to explore the use of personal computers (PC) for VR-based assembly simulations. A PC-based system “Vshop” (Figure 2) was developed by Pere et al. [58] for mechanical assembly training in virtual environments. The research focused on



**Figure 2: VShop User Interface**

exploring PC-based systems as a low cost alternative and utilizing commercial libraries for easy creation of interactive VR software. The system implemented bounding-box collision detection to prevent model interpenetration. The system provided grasping force feedback to the user and recognized gestures using a Rutgers Master II haptic exoskeleton. Hand gesture recognition was used for various tasks like switching on and off navigation and moving forward/backward in the environment.

An experimental study investigating the potential benefits of VR environments in supporting assembly planning was conducted by Ye et al. [59]. For virtual assembly planning, a non-immersive desktop and an immersive CAVE [60, 61] environment were evaluated. The desktop VR environment consisted of a Silicon Graphics workstation. The CAVE environment was implemented with an IRIS Performer CAVE



**Fig. 3** Presentation of Aircylinder assembly in Ye's Application

interface and provided the subjects with a more immersive sense of virtual assemblies and parts. The experiment compared assembly operations in a traditional engineering environment and immersive and non-immersive VR environments. The three conditions differed in how the assembly was presented and handled. The assembly task was to generate an assembly sequence for an air-cylinder assembly (Figure 3) consisting of 34 parts. The results from the human subject study concluded that the subjects performed better in VEs than in traditional engineering environments in tasks related to assembly planning.

Anthropometric data was utilized to construct virtual human models for addressing ergonomic issues that arise during assembly [62]. A Head Mounted Display (HMD) was used for stereo viewing and a data glove was used for gesture recognition. Head and hand tracking was implemented using magnetic trackers. While performing assembly tasks, the users could see their human model in the virtual environment. The system calculated the time and cost involved in assembly and also produced a script file describing the sequence of actions performed by the user to assemble the product.

An industrial study was performed at BMW to verify assembly and maintenance processes using virtual prototypes [63]. A Cyber Touch glove device was used for gesture recognition, part manipulation and for providing tactile force feedback to the user. A proximity snapping technique was used for part placement and the system used voice input and provided acoustic feedback to provide information about the material properties of the colliding object. Gestures from the glove device were also used for navigating the virtual environment. Five different groups with diverse backgrounds participated in the user study. It was concluded that force feedback is crucial when performing virtual assembly tasks.

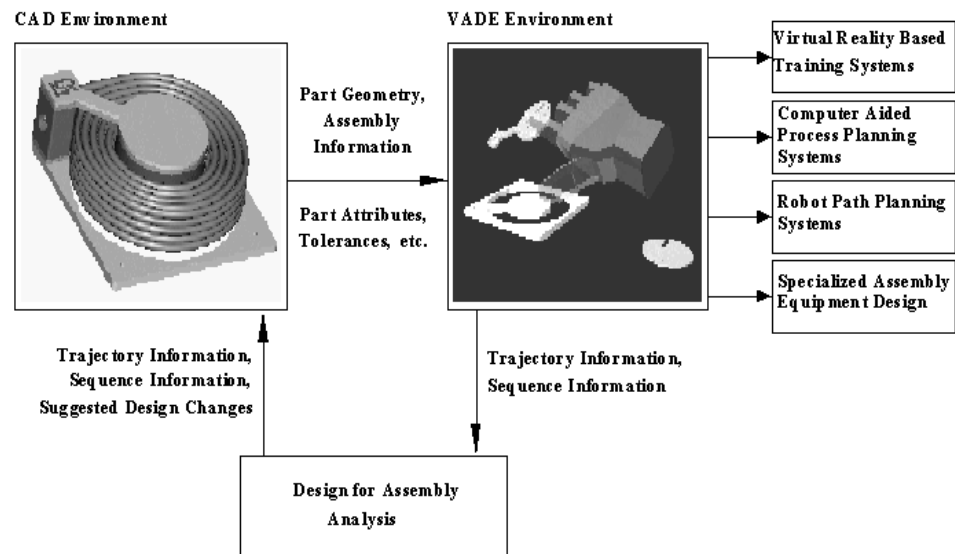
#### ***4.1.2 Systems Using Geometric Constraints***

One of the early attempts at utilizing geometric constraints to achieve accurate 3D positioning of solid models was demonstrated by Fa et al. [64] in 1993. The concept of allowable motion was proposed to constrain the free 3D manipulation of the solid model. Simple constraints such as against, coincident, etc. were automatically recognized and the system computed relative motion of objects based on available constraints.

VADE (Virtual Assembly Design Environment) [6, 65-68] developed in collaboration with NIST and Washington State University utilized constraint-based modeling [55] for assembly simulations. The system used Pro/Toolkit to import assembly data (transformation matrices, geometric constraints, assembly hierarchy etc.) from CAD to perform assembly operations in the virtual environment. Users could perform dual handed assembly and dexterous manipulation of

objects (Figure 4).

A CyberGrasp haptic device was used for tactile feedback during grasping. A physics-based algorithm with limited



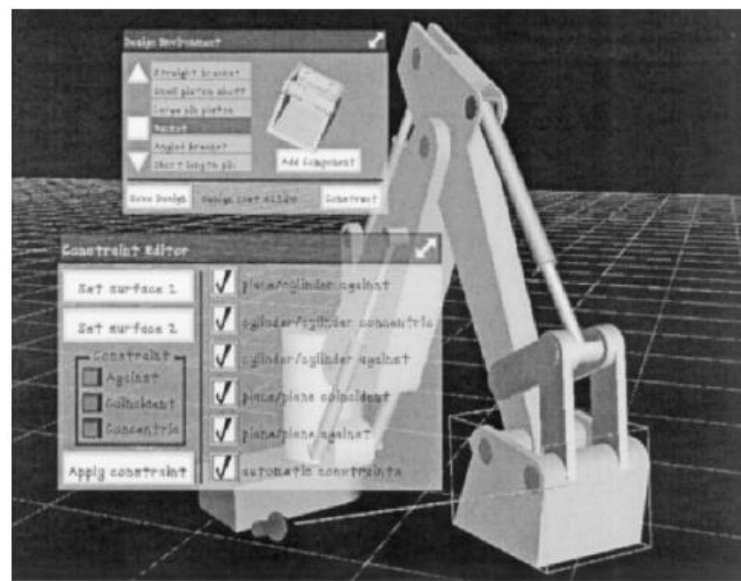
**Fig. 4** VADE Usage Scenarios

capabilities was later added to VADE for simulating realistic part behavior [69]. A hybrid approach was introduced where object motion is guided by both physical and geometric constraints simultaneously. Stereo vision was provided by an HMD or an Immersadesk [70]

system. Commercial software tools were added to the system to perform ergonomic evaluation during assembly [71, 72]. The VADE system was the used to conduct industry case studies and demonstrate downstream value of virtual assembly simulations in various applications such as ergonomics, assembly installation, process planning, installation, and serviceability [73].

Different realistic hand grasping patterns involving complex CAD models have been explored by Wan et al. [74, 75] using a multimodal system called MIVAS (A Multi-Modal Immersive Virtual Assembly System). They created a detailed geometry model of the hand using metaball modeling [76, 77] and tessellated it to create a graphic representation which was texture mapped with images captured from a real human hand [78]. A three layer model (skeletal layer, muscle layer and skin layer) was adapted to simulate deformation in the virtual hand using simple kinematics models. Hand to part collision detection and force computations were performed using fast but less accurate VPS software [30] while part to part collision detection was implemented using the RAPID [79] algorithm. Geometric constraints were utilized in combination with collision detection to calculate allowable part motion and accurate part placement. Users could feel the size and shape of digital CAD models via the CyberGrasp haptic device from Immersion Corporation [80].

Commercial constraint solvers such as D-Cubed [81] have also been utilized for simulating kinematic



**Fig. 5** Marcelino's Constraint Manager Interface



behavior in constraint-based assembly simulations. Marcelino et al. [56] developed a constraint manager for performing maintainability assessments using virtual prototypes. Instead of importing geometric constraints from CAD systems using proprietary toolkits, a constraint recognition algorithm was developed which examined part geometries (surfaces, edges etc.) within certain proximity to predict possible assembly constraints. Geometric constraint approach was utilized to achieve real time system performance in a realistic kinematic simulation. The system (Figure 5) imported B-Rep CAD data using Parasolid [82] geometry format. A constraint manager was developed which was capable of validating existing constraints, determining broken constraints and enforcing existing constraints in the system. The constraint recognition algorithm required extensive model preprocessing steps in which bounding boxes were added to all surfaces of the objects before they could be imported.

The concept of assembly ports [83, 84] in combination with geometric constraints have been used by researchers for assembly and tolerance analysis. Liu et al. [85] created a system which used assembly ports containing information about the mating part surfaces, for example geometric and tolerance information, assembly direction and type of port (hole, pin, key etc.). If parts were modified by a design team, the system used assembly port information to analyze if new designs could be re-assembled successfully. Different rules were created (proximity, orientation, port type and parameter matching) for applying constraints among parts. Gesture recognition was implemented using a CyberGlove device. A user study was conducted which confirmed that constraint-based modeling was beneficial for users when performing precise assembly positioning tasks [86].

Attempts have also been made at integrating CAD systems with virtual assembly and maintenance simulations [65, 87]. A CAD-linked virtual assembly environment was developed

by Wang et al. [88] which utilized constraint-based modeling for assembly. The desktop-based system ran as a standalone process and maintained communication with Autodesk Inventor® CAD software. Low level-of-detail (LOD) proxy representations of CAD models were used for visualization in the virtual environment. The assembly system required persistent communication with the CAD system using proprietary APIs for accessing information such as assembly structure, constraints, B-rep geometry and object properties. The concept of proxy entity was proposed which allowed the system to map related CAD entities (surfaces, edges, etc.) to their corresponding triangle mesh representations present in VR.

Yang et al. [89] used constraint-based modeling for assembly path planning and analysis. Assembly tree data, geometric data of parts and predefined geometric constraints could be imported from different parametric CAD systems using a special data converter. A data glove device and a hand tracker were used for free manipulation of objects in the virtual environment. The automatic constraint recognition algorithm activated the pre-defined constraints when bounding boxes of the interrelated parts collided. The users were required to confirm the constraint before it could be applied. These capabilities were applied to the integrated virtual assembly environment (IVAE) system.

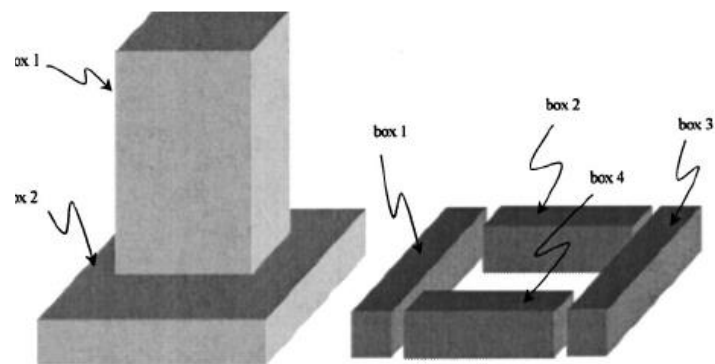
## **4.2 Physics-Based Modeling Applications**

The second category of applications includes assembly systems which simulate real world physical properties, friction, and contact forces to assemble parts in a virtual environment. These applications allow users to move parts freely in the environment. When a collision is detected, physics-based modeling algorithms, are used to calculate subsequent part trajectories to allow for realistic simulation.

Assembly operators working on the shop floor rely on physical constraints among mating part surfaces for completing assembly tasks. In addition, physical constraint simulation is important during assembly planning as well as maintenance assessments to check if there is enough room for parts and tooling. One of the early attempts at implementing physics-based modeling for simulating part behavior was made by Gupta [90, 91]. The desktop-based system called VEDA (Virtual Environment for Design for Assembly) used a dual Phantom® interface for interaction and provided haptic, auditory and stereo cues to the user for part interaction. However, the system was limited to render multimodal interactions only among 4-5 polygons and handled only 2D models to maintain an interactive update rate.

Collision detection and physical constraint simulation among complex 3D models was attempted by Fröhlich et al. [92]. They used CORIOLIS™ [93] physics-based simulation algorithm to develop an interactive virtual assembly environment using the Responsive Workbench [94]. Different configurations of spring based virtual tools were developed to interact with objects. The system implemented the workbench in its table-top configuration and supported multiple tracked hands and users to manipulate an object. The system's update rates dropped below interactive levels when several hundred collisions occurred simultaneously, and at least five percent tolerance was necessary to avoid numerical instabilities which sometimes resulted in system failure.

Researchers at the Georgia Institute of Technology utilized a similar approach demonstrated by



**Fig. 6** Geometry in HIDRA

Gupta et al. [91] to create a desktop based virtual assembly system called HIDRA (Haptic Integrated Dis/Re-assembly Analysis) [95, 96]. This approach used GHOST (General Haptic Open Software Toolkit) from Sensable Technologies [97] and dual Phantom® configuration for part grasping. OpenGL was used for visualization on a 2D monitor and V-Clip in conjunction with Q-hull and SWIFT++ were used for collision detection. Because the system (Figure 6) treated the user's finger tip as a point rather than a surface, users had difficulty manipulating complicated geometries. Also, using GHOST SDK for physical modeling combined with the "polygon soup" based collision detection of SWIFT++, HIDRA had problems handling non-convex CAD geometry.

Researchers [7, 98] evaluated several collision detection and physics-based algorithms and found VPS [30] software from The Boeing Company to be the most applicable for handling the rigorous real time requirements while operating on complex 3D CAD geometry. The system utilized approximated triangulated representations of complex CAD models to generate a volumetric

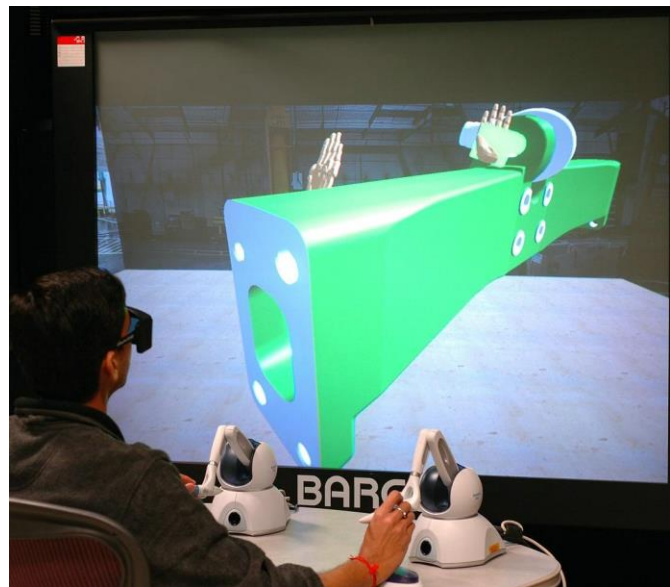


**Fig. 7** Data Glove in a Six-Sided CAVE

representation that was used for collision computations. Four and six sided CAVE systems were supported and a virtual arm model was constructed by using multiple position trackers that were placed on the user's wrist, forearm and upper arm (Figure 7). Dual handed assembly was supported and gesture recognition was done using wireless data glove devices from 5DT Corporation [99].

Techniques developed during this research were expanded to facilitate collaborative assembly [100] through the internet. A combination of peer-to-peer and client-server network architectures was developed to maintain the stability and consistency of the system data. A “Release-but-not-released - RNR” method was developed for allowing computers with different performance capabilities to participate in the network. The system architecture required each virtual environment to be connected to a local PC machine to ensure 1 Khz haptic update rate for smooth haptic interaction. Volumetric approximation of complex CAD models resulted in a fast but inaccurate simulation (with errors up to ~15mm) and thus did not allow low clearance parts to be assembled.

A dual-handed haptic interface (Figure 8) for assembly/disassembly was created by Seth et al. [101, 102]. This interface was integrated into SHARP: System for Haptic Assembly and Realistic Prototyping and allowed users to simultaneously manipulate and orient CAD models to simulate dual handed assembly operations. Collision force feedback was provided to the user during



**Fig. 8** Dual-handed Haptic Interface in SHARP

assembly. Graphics rendering was implemented with SGI Performer, the Open Haptics Toolkit library was used for communicating with the haptic devices, and VPS [30] for collision detection and physics-based modeling. Using VRJuggler [103] as an application platform, the system could operate on different VR systems configurations including low-cost desktop configurations,

Barco Baron [104], Power Wall, four-sided and six sided CAVE systems. Different modules were created to address issues related to maintenance (swept volumes), training (record & play) and to facilitate collaboration (networked communication). Industrial applications of this work demonstrated promising results for simulating assembly of complex CAD models from a tractor hitch. This research was later expanded to gain collision detection accuracy at the cost of computation speed for simulating low-clearance assembly. SHARP demonstrated a new approach [105] by simulating physical constraints using by accurate B-Rep data from CAD systems which allowed the system to detect collisions with an accuracy of 0.0001mm. Although physical constraints were simulated very accurately, users could not manipulate parts during very low clearance scenarios with the required precision because of the noise associate with the 3D input devices. Geometric constraints were utilized in combination with physics to achieve precise part manipulation required for low-clearance assembly.

Garbaya et al. [106] created a physics-based virtual assembly system which used spring-damper model to provide the user with collision and contact forces during the mating phase of an assembly operation. The PhysX® software toolkit was used for collision detection and physically-based modeling. Grasping force feedback was provided using a CyberGrasp™ haptic device and collision force was provided using CyberForce™ haptic device from Immersion Corporation. An experimental study was conducted to check system effectiveness and user performance in real and virtual environments. The study concluded that user performance increased when inter-part collision forces were rendered as compared to when only grasping forces were provided to the user.

HAMMS (Haptic Assembly, Manufacturing and Machining System) was developed by researchers at the Heriot-Watt University to explore the use of immersive technology and haptics

in assembly planning [107]. The system uses a Phantom® device and stereo glasses. The application is based on OpenHaptics Toolkit, VTK and AGEIA PhysX® software. The unique aspect of this application is its ability to log user interaction. This tracking data can be recorded and examined later to generate an assembly procedure. This work is ongoing with future evaluations to be performed.

## **5 Haptic Interaction**

Today's virtual assembly environments are capable of simulating visual realism to a very high level. The next big challenge for the virtual prototyping community is simulating realistic interaction. Haptics is an evolving technology that offers a revolutionary approach to realistic interaction in VEs. "Haptics means both force feedback (simulating object hardness, weight, and inertia) and tactile feedback (simulating surface contact geometry, smoothness, slippage and temperature)" [45]. Force cues provided by haptics technology can help designers feel and better understand the virtual objects by supplementing visual and auditory cues and creating an improved sense of presence in the virtual environment [108-110]. Research has shown that the addition of haptics to virtual environments can result in improved task efficiency times [111, 112].

Highly efficient physics-based methods that are capable of maintaining high update rates are generally used for implementing haptic feedback in virtual assembly simulations. Various approaches for providing haptic feedback for assembly have been presented in the past which focused on developing new methods for providing tactile [58, 65, 74, 87, 113], collision [100-102] and gravitational force feedback [108, 114]. The high update rate (~1KHz) requirement for effective haptics has always been a challenge in integrating this technology. As stated earlier, most physics-based algorithms used highly coarse model representations to maintain the update

rate requirements. The resulting lack of part shape accuracy of such approaches presents problems when detailed contact information is necessary. Simulating complex part interactions such as grasping is also demanding as it requires the simulation to detect collisions and generate contact forces accurately for each individual finger [74, 75, 87, 115]. Maintaining update rates for haptic interaction (~1 KHz) while performing highly accurate collision/physics computations in complex interactive simulations such assembly remains a challenge for the community.

In addition, there are several limitations of the haptics technology currently available. Non-portable haptic devices such as Sensable Technologies' PHANTOM® [97, 116], Immersion's CyberForce™ [80], Haption Virtuose [117], and Novint Falcon [118] devices [89] among others [119, 120] have workspace limitations which results in restricted user motion in the environment. Additionally, because these devices need to be stably mounted, their use with immersive virtual environments becomes unfeasible.

In contrast, wearable haptic gloves and exoskeleton devices such as CyberTouch™, CyberGrasp™ [80], Rutgers Master II [121] among others [114] provide a much larger workspace for interaction. However, they provide force feedback only to fingers and palm and thus are suitable for tasks that involve only dexterous manipulations. In addition, the weight and cable attachments of such devices make their use unwieldy. A detailed discussion on haptics issues can be found in [22]. The challenges presented here among several others must be addressed, before the community can explore the real potential of haptics technology in virtual prototyping.

## **6 CAD-VR Data Exchange**

CAD-VR data exchange is one of the most important issues faced by the virtual prototyping community. CAD systems used by the industry to develop their product models are



generally unsuitable for producing optimal representations for VR applications. Most VR applications take advantage of scene-graphs (e.g., Openscenegraph, OpenSG, OpenGL Performer, etc.) for visualization which are simply hierarchical data structures comprised of triangulated mesh geometry, spatial transforms, lighting, material properties, and other metadata. Scene graph renderers provide the VR application with methods to exploit this data structure to ensure interactive frame rates. Translating CAD data into a scene graph requires tessellation of the individual precise parametric surface and/or B-rep solids, often multiple times, to produce several “level-of-detail” polygonal representations of each part. During this translation process, the parametric (procedural modeling history and constraints) information of the CAD model generally does not get imported into the VR application. In addition, pre-existing texture maps may not be included in these visually optimized model representations. In virtual assembly simulations, geometric constraint-based applications that depend on parametric model definitions to define inter-part constraint relationships generally have to deal with two representations of the same model: one for visualization and another for constraint modeling algorithms for performing assembly. Similarly, physics modeling applications also use dual model representations: high-fidelity model for visualization and a coarser representation used for interactive physics calculations [92, 101].

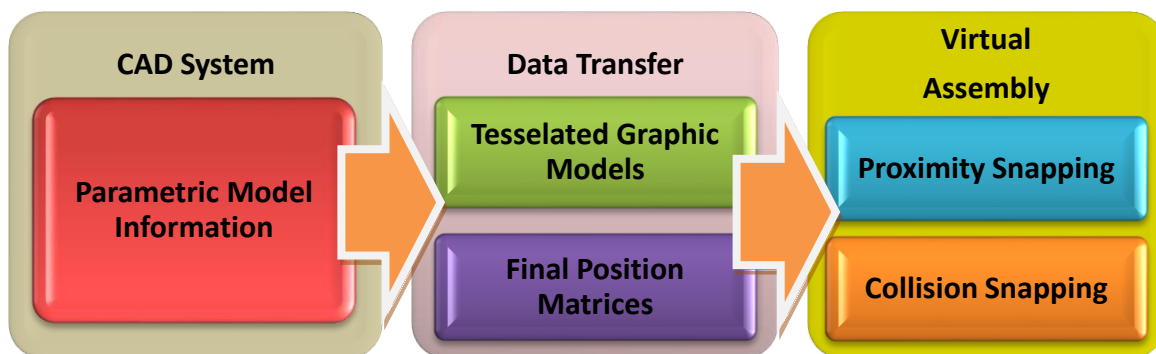
Commercial CAD systems (for example AutoCAD, UGS, Dassault Systems, etc.) have made various attempts to embed capabilities for immersive and desktop stereo visualization into available commercial software to some degree. Attempts have also been made by academia to provide haptic interaction and immersive visualizations for assembly/disassembly applications with commercial CAD systems [87, 88]. Thus, although addressed to some degree by industry

and academia, there is still no general non-proprietary way to convert CAD assemblies into a representation suitable for VR.

Additionally, today's VR applications have matured to a level where they provide users with the ability to identify meaningful design changes however, translating these changes back to CAE applications (such as CAD systems) is currently not possible. The efforts mentioned above represent a promising basis for this research, but as yet, it remains a major bottleneck to broader adoption of VR.

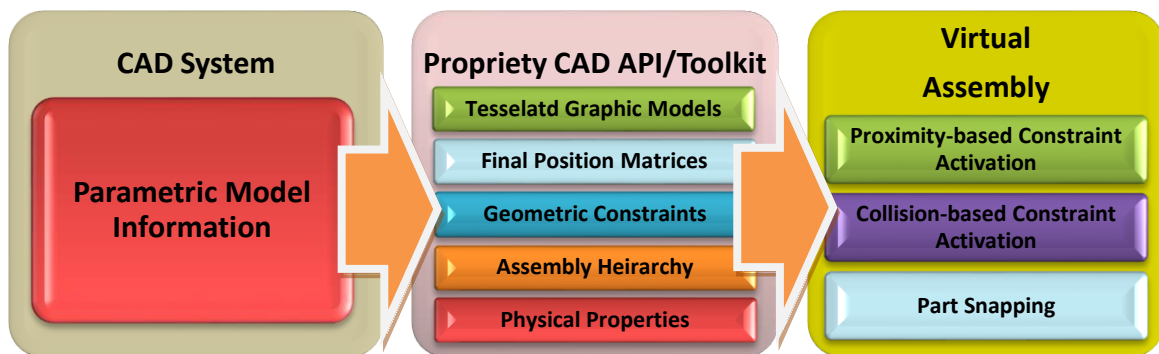
## 7 Summary

Many virtual assembly applications have been developed by various research groups, each with different features and capabilities. The review in the previous section indicated that initial efforts in simulating assembly used pre-defined transformation matrices of parts for positioning in the virtual scene. In such systems, as users moved parts in the environment they were snapped in place based on collision or proximity criteria [122] (Figure 9). Most of the early applications did not implement collision detection among objects which allowed them to interpenetrate during the simulation.



**Fig. 9** Data Transfer in Positional Constraint Applications

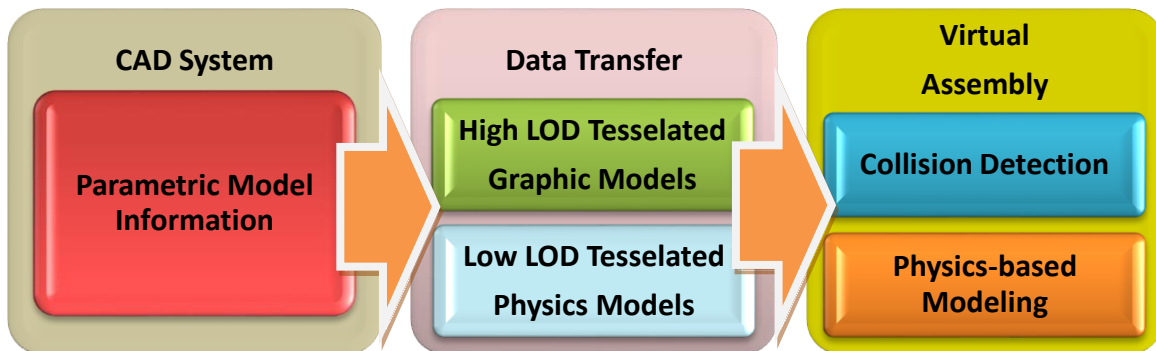
Later, researchers used pre-defined geometric-constraint relationships which were imported from a CAD system for assembling parts. Here, the pre-defined constraints were activated when related parts came close to each other in the environment. Once geometric-constraints were recognized, constrained motion could be visualized between parts which were then assembled using pre-defined final position [65]. Constraint-based approaches have shown promising results in the past. They present lower computation and memory requirements as compared to physics-based methods. In addition, when combined with accurate models (e.g., parametric surface representations, or B-Rep solids) constraint-based approaches allow users to manipulate and position parts in an assembly with very high fidelity. However, some of these applications required special CAD toolkits to extract relevant CAD metadata (Figure 10) that was required for preparing an assembly scenario[65, 74, 123]. These special data requirements and their dependence on specific CAD systems prevented widespread acceptance of these



**Fig. 10** Data Transfer in Geometric Constraint-based Applications applications. Many constraint-based virtual assembly systems also incorporated collision detection between models to prevent model interpenetration during assembly. Advanced constraint-based methods were successful in identifying, validating and applying constraints on-the-fly and thus did not require importing predefined CAD constraints [56, 124]. Although, systems using constraint-based modeling prove successful in simulating object's kinematics for

assembly; simulating realistic behavior among objects involving physical constraints and rigid body dynamics is not possible.

Other research incorporated simulation of the real world physical behavior of parts (Figure 11). Physics-based methods allow for testing scenarios similar to those possible only by physical mock-ups by calculating part trajectories subsequent to collisions, possibly incorporating friction, gravity, and other forces that act on the objects. Physics-based solvers generally sacrifice computation accuracy to keep the update rate of the visual simulation realistic [32]. Most previous efforts used a simplified and approximated polygon mesh representations of CAD models for faster collision and physics calculations. Some of these efforts generated even coarser representations by using cubic voxel elements for physics and collision calculations [30, 125, 126]. Assembly configurations like a tight peg in a hole caused several hundreds of collisions to occur which often resulted in numerical instabilities in the system [92]. Due to these



**Fig. 11** Data Transfer in Physics-based Applications

limitations, very few attempts rely on simulating physical constraints for assembly/disassembly simulations.

In addition, physics-based methods also lay the foundation for the implementation of haptic interfaces for virtual prototyping applications. Such haptic interfaces allow users to touch and feel virtual models that are present in the simulation. Haptic interfaces require much higher

update rates of  $\sim 1$  KHz which results in trade-offs in accuracy of collision and physics computations. In order to complete assembly tasks with tight tolerances, nominal part size modification may be required [93, 102]. However, because assembly operations require mating with small clearance, it is generally not possible to assemble low-clearance parts with actual dimensions using physics-based methods. The demand for highly accurate physics/collision results while maintaining simulation interactivity is still a challenge for the community. In prototyping applications like virtual assembly, attempts have been made to provide collision and tactile forces to the users for more intuitive interaction with the environment [75, 95, 100-102].

## **8 Discussion & Future Directions**

Collision detection algorithms unquestionably form the first step towards building a virtual assembly simulation system. Although they add to simulation realism by preventing part interpenetration; collision detection alone does not model part behavior or define relative part trajectories necessary to facilitate the assembly operation. Part interaction methods are key to a successful immersive virtual assembly experience.

In general, while constraint-based approaches provide capabilities for precise part positioning in VEs; physics-based approaches, on the other hand, enable virtual mock-ups to behave as their physical counterparts. Identifying physical constraints among an arbitrary set of complex CAD models in a dynamic virtual simulation is a computationally demanding challenge. Collision and physics responses need to be calculated fast enough to keep up with the graphics update rate ( $\sim 30$  Hz) of the simulation. Both of these approaches serve different purposes which are crucial in making a virtual assembly simulation successful.

A research direction that appears promising would be to develop a hybrid method by combining physics-based and constraint-based algorithms. The resulting virtual assembly

application would be able to simulate realistic environment behavior for enhanced sense of presence and would also be able to position parts precisely in a given assembly (Table 1). An attempt has been made to implement physics-based algorithm with limited capabilities to an existing constraint based assembly system [69]. However, limitations of the physics algorithm, part snapping and excessive metadata requirements using a CAD system dependent toolkit prevented its widespread impact.

	Collision Detection	Constraint Based Methods	Physics Based Methods	Hybrid Method (Collision + Geometric Constraint + Physics Modeling)
Prevent Part Interpenetration	<b>X</b>		<b>X</b>	<b>X</b>
Realistic Part Behavior			<b>X</b>	<b>X</b>
Precise Part Movement		<b>X</b>		<b>X</b>
Low Computational Load		<b>X</b>		
Haptic (Collision/Tactile) Feedback			<b>X</b>	<b>X</b>

**Table 1** Comparison of Assembly Simulation Methods

Such an approach would incorporate physics-based methods for simulating realistic part behavior combined with automatic constraint identification, application and haptic interaction. Constraint-based methods would come into play when low clearance assembly needs to be performed to allow for precise movement of parts into their final position. The challenge in this approach is that physics-based methods should be able to take into account the presence of a geometric constraint and the “hybrid solver” should be able to calculate part trajectories in such a way that both physical and geometric constraints are satisfied at any given point of time.

As the technology progresses, the cost of computing and visualization technology will continue to fall as their capabilities increase. It will soon be possible to utilize this power to integrate faster and more accurate algorithms into virtual assembly simulations that will be capable of handling large assemblies with thousands of parts while incorporating physically accurate part behavior with high-fidelity visual and haptic interfaces.

## 9 References

1. Ritchie, J.M., Dewar, R.G. and Simmons, J.E.L., *The Generation and Practical use of Plans for Manual Assembly using Immersive Virtual Reality*. Proceedings of the I MECH E Part B Journal of Engineering, 1999. **213**(5): p. 461-474.
2. Bryson, S., *Virtual Reality in Scientific Visualization*. Communications of the ACM, 1996. **39**(5): p. 62-71.
3. Eddy, J., and Lewis, K. E. *Visualization of Multidimensional Design and Optimization Data using Cloud Visualization*. in *ASME Design Engineering Technical Conferences and Computers and Information in Engineering Conference (DETC2002/DAC-34130)*. 2002. Montreal, Canada.
4. Zorriassatine, F., Wykes, C., Parkin, R., and Gindy, N., *A Survey of Virtual Prototyping Techniques for Mechanical Product Development*. Institution of Mechanical Engineers, Part B: Journal of Engineering Manufacture, 2003. **217**(4): p. 513-530.
5. Xianglong, Y., Yuncheng, F., Tao, L., and Fei, W. *Solving Sequential Decision-making Problems Under Virtual Reality Simulation System*. in *Winter Simulation Conference Proceedings*. 2001. Arlington, Virginia.
6. Jayaram, S., Connacher, H. I., and Lyons K.W., *Virtual Assembly using Virtual Reality Techniques*. Computer Aided Design, 1997. **29**(8): p. 575-584.
7. Kim, C.E., and Vance, J.M. *Using Vps (Voxmap Pointshell) As The Basis For Interaction in a Virtual Assembly Environment*. in *ASME Design Engineering Technical Conferences and Computers and Information in Engineering Conference (DETC2003/CIE-48297)*. 2003. Chicago,IL.: ASME.
8. Boothroyd, G., and Dewhurst, P., *Product Design for Assembly*. 1989, New York: McGraw-Hill, Inc.
9. Baldwin, D.F., Abell, T.E., Lui, M.-C.M., De Fazio, T.L., and Whitney, D.E., *An Integrated Computer Aid for Generating and Evaluating Assembly Sequences for Mechanical Products*. IEEE Transactions on Robotics and Automation, 1991. **7**(1): p. 78-94.
10. de-Mello, L.S.H., and Sanderson, A.C. *A Correct and Complete Algorithm for the Generation of Mechanical Assembly Sequences*. in *IEEE International Conference on Robotics and Automation*. 1989. Scottsdale, AZ, USA.
11. Zha, X.F., Lim, S. Y. E., and Fok, S. C., *Integrated Intelligent Design and Assembly Planning: A Survey*. International Journal of Advanced Manufacturing Technology, 1998. **14**(9): p. 664-685.

12. Sung, R.C.W., Corney, J.R., and Clark, D.E.R., *Automatic Assembly Feature Recognition and Disassembly Sequence Generation*. Journal of Computing and Information Science in Engineering, 2001. **1**(4): p. 291-299.
13. De Fazio, T.L., and Whitney, D. E., *Simplified Generation of All Mechanical Assembly Sequences*. IEEE Journal of Robotics and Automation, 1987. **3**(6): p. 640- 658.
14. Smith, S.S.-F., Smith, G., and LIAO, X., *Automatic Stable Assembly Sequence Generation and Evaluation*. Journal of Manufacturing Systems, 2001. **20**(4): p. 225-235.
15. Ritchie, J.M., Simmons, J.E.L., Carpenter, I.D. and Dewar., R.G. *Using Virtual Reality for Knowledge Elicitation in a Mechanical Assembly Planning Environment*. in *Proceedings of 12th Conference of the Irish Manufacturing Committee*. 1995.
16. Holt, P.O., Ritchie, J. M., Day, P.N., Simmons, J.E.L., Robinson, G., Russell, G.T., Ng, F.M., *Immersive virtual reality in cable and pipe routing: design metaphors and cognitive ergonomics*. ASME Journal of Computing and Information Sciences in Engineering, 2004. **4**(3): p. 161-170.
17. Dewar., R.G., Carpenter, I.D., Ritchie, J.M. and Simmons, J.E.L. *Assembly Planning in a Virtual Environment*. in *Proceedings of Portland International Conference on management of Engineering and Technology (PICMET 97)*. 1997. Portland,OR: IEEE Press.
18. Schwartz, M., Gupta, S.K., Anand, D.K., and Kavetsky, R. *Virtual mentor: A step towards proactive user monitoring and assistance during virtual environment-based training*. in *Performance Metrics for Intelligent Systems Workshop (PerMIS '07)*. 2007. Washinton, D.C.,USA.
19. Brough, J.E., Schwartz, M., Gupta, S. K., Anand, D. K., Kavetsky, R. and, Petterson, R., *Towards the development of a virtual environment-based training system for mechanical assembly operations*. Virtual Reality, 2007. **11**(4): p. 189-206.
20. Chryssolouris, G., Mavrikios, D., Fragos, D., Karabatsou, V., *A virtual reality-based experimentation environment for the verification of human-related factors in assembly processes*. Robotics and Computer Integrated Manufacturing, 2000. **16**: p. 267-276.
21. Boothroyd, G., Dewhurst, P., Knight, W., *Product Design for Manufacture and Assembly*. 1994: Marcel Dekker, Inc.
22. Burdea, G.C. *Haptics Issues in Virtual Environments*. in *Computer Graphics International*. 2000. Geneva, Switzerland.
23. Cohen, J.D., et al., *I-COLLIDE: An Interactive and Exact Collision Detection System for Large-Scale Environments*. The 1995 ACM International 3D Graphics Conference, 1995: p. pp.189-196.
24. Ehmann, S.A. and M.C. Lin, *SWIFT: Accelerated Proximity Queries Between Convex Polyhedra By Multi-Level Voronoi Marching*. Technical report, Computer Science Department, University of North Carolina at Chapel Hill, 2000.
25. Gottschalk, S., M.C. Lin, and D. Manocha, *OBB-Tree: A Hierarchical Structure for Rapid Interference Detection*. ACM SIGGRAPH'96, 1996: p. pp. 171-180.
26. Hudson, T., et al., *V-COLLIDE: Accelerated Collision Detection for VRML*. Proceedings of the second symposium on Virtual Reality Modeling Language, 1997: p. pp. 119-125.
27. Ehmann, S.A. and M.C. Lin, *Accurate and Fast Proximity Queries between Polyhedra Using Surface Decomposition*. Eurographics. Computer Graphics Forum, 2001. **20**(3).
28. Govindaraju, N.K., Redon, S., Lin, M. C. and Manocha, D., *CULLIDE: Interactive Collision Detection Between Complex Models in Large Environments using Graphics*



- Hardware*. In Proceedings of ACM SIGGRAPH/Eurographics Workshop on Graphics Hardware, 2003: p. 25-32.
29. Mirtich, B., *V-Clip: fast and robust polyhedral collision detection*. ACM Transactions on Graphics, 1998. **17(3)**: p. pp. 177-208.
  30. McNeely, W.A., Puterbaugh, K. D. and Troy, J. J. *Six Degree-of-Freedom Haptic Rendering Using Voxel Sampling*. in *SIGGRAPH 99 Conference Proceedings, Annual Conference Series*. 1999. Los Angeles,CA.
  31. Lin, M., and Gottaschalk, S. *Collision Detection between Geometric Models: A survey*. in *Proceedings of IMA Conference on Mathematics of Surfaces*. 1998.
  32. Jiménez, P., Thomas,F., and Torras, C., *3D Collision Detection: A Survey*. Computers and Graphics, 2001. **25(2)**: p. 269-285.
  33. Borro, D., Hernantes, J., Garcia-Alonso, A., and Matey, L. *Collision Problem: Characteristics for a Taxonomy*. in *Proceedings of the Ninth International Conference on Information Visualisation (IV'05)*. 2005.
  34. Frohlich, B., Tramberend, H., Beers, A., Agarawala, M. and Baraff, D. *Physically-Based Modeling on the Responsive Workbench*. in *IEEE Virtual Reality Conference*. 2000.
  35. Light, R., and Gossard, D., *Modification of Geometric Models through Variational Geometry*. Computer Aided Design, 1982. **14(4)**: p. 209-214.
  36. Fudos, I., *Constraint Solving for Computer Aided Design*, in *Computer Sciences*. 1995, Purdue University. p. 107.
  37. Fernando, T., Murray, N., Tan, K., and Wilmalaratne, P. *Software Architecture for a Constraint-Based Virtual Environment*. in *Proceedings of the ACM symposium on Virtual Reality Software and Technology*. 1999. London, UK.
  38. Owen, J.C. *Algebraic Solution for Geometry from Dimensional Constraints*. in *ACM Symposium Foundations of Solid Modeling*. 1991. Austin,TX: ACM.
  39. Fudos, I., and Hoffman, C. M., *A Graph Constructive Approach to Solving System of geometric Constraints*. ACM Transactions on Graphics, 1997. **16(2)**: p. 179-216.
  40. Verroust, A., Schonek, F., and Roller, D., *Rule-Oriented method for Parameterized Computer-Aided Design*. Computer Aided Design, 1992. **24(3)**: p. 531-540.
  41. Sunde, G. *Specification of Shape by Dimensions and Other Geometric Constraints*. in *Geometric Modeling for CAD Applications*. 1988. North Holland IFIP.
  42. H. Suzuki, H.A., and Kimura, F., *Variation of Geometries Based on a Geometric-Reasoning Method*. Computers and Graphics, 1990. **14(2)**: p. 211-224.
  43. Bouma, W., Fudos, I., Hoffman, C. M., Cai, J., and Paige, R., *A Geometric Constraint Solver*. Computer Aided Design, 1995. **27(6)**: p. 487-501.
  44. Fudos, I., and Hoffman, C. M., *Correctness Proof of a Geometric Constraint Solver*. International Journal of Computational Geometry & Applications, 1995. **6(4)**: p. 405-420.
  45. Burdea, G.C., *Invited Review: The Synergy between Virtual Reality and Robotics*. IEEE Transactions on Robotics and Automation, 1999. **15(3)**: p. 400-410.
  46. Erleben, K., Sporning J., Henriksen, K. and Dohlmann, H., *Physics-Based Animation*. First ed. 2005, Hingham, MA: Charles River Media, Inc. 817.
  47. Witkin, A., Gleicher, M. and Welch, W., *Interactive Dynamics*. Computer Graphics, 1990. **24(2)**: p. 11-22.
  48. Hahn, J.K., *Realistic Animation of Rigid Bodies*. Computer Graphics, 1988. **22(4)**: p. 299-308.

49. Mirtich, B. and J. Canny, *Impulse-based Simulation of Rigid Bodies*. Symposium on Interactive 3D Graphics, 1995.
50. Guendelman, E., Bridson, R. and Fedkiw, R.P., *Nonconvex Rigid Bodies with Stacking*. ACM Transactions on Computer Graphics, 2003. **22**(3): p. 871-879.
51. Mirtich, B.V., *Impulse-based Dynamic Simulation of Rigid Body Systems*, in *Computer Science*. 1996, University of California at Berkeley. p. 246.
52. Baraff, D., *Analytical Methods for Dynamic Simulation of Non-penetrating Rigid Bodies*. Computer Graphics, 1989. **23**(3): p. 223-232.
53. Baraff, D.a.W., A., *Physically Based Modeling: Principles and Practice (Online Siggraph 97 Course Note)*, [www-2.cs.cmu.edu/~baraff/sigcourse/](http://www-2.cs.cmu.edu/~baraff/sigcourse/). 1997.
54. Baraff, D., *Curved Surfaces and Coherence for Non-penetrating Rigid Body Simulation*. Computer Graphics, 1990. **24**(4): p. 19-28.
55. Wang, Y., Jayaram, U., Jayaram, S., and Shaikh, I., *Methods and Algorithms for Constraint Based Virtual Assembly*. Virtual Reality, 2003. **6**: p. 229-243.
56. Marcelino, L., Murray, N., and Fernando, T., *A Constraint Manager to Support Virtual Maintainability*. Computers & Graphics, 2003. **27**(1): p. 19 - 26.
57. Kuehne, R., and Oliver, J. *A Virtual Environment for Interactive Assembly Planning and Evaluation*. in *Proceedings of ASME Design Automation Conference*. 1995. Boston, MA., USA.
58. Pere, E., Langrana, N., Gomez, D., and Burdea, G. *Virtual Mechanical Assembly on a PC-Based System*. in *ASME Design Engineering Technical Conferences and Computers and Information in Engineering Conference (DETC1996/DFM-1306)*. 1996. Irvine, CA.
59. Ye, N., Banerjee, P., Banerjee, A., and Dech, F., *A Comparative Study of Virtual Assembly Planning in Traditional and Virtual Environments*. IEEE Transactions on Systems, Man, and Cybernetics - Part C: Applications and Review, 1999. **29**(4): p. 546 - 555.
60. Cruz-Neira, C., Sandin, D., and DeFanti, T., *Surround-Screen Projection-Based Virtual Reality: The Design and Implementation of the CAVE*. Proceedings of SIGGRAPH 93, 1993: p. 135-142.
61. Cruz-Neira, C., Sandin, D.J., DeFanti, T.A., Kenyon, R., and Hart, J.C., *The CAVE, Audio Visual Experience Automatic Virtual Environment*. Communications of the ACM, 1992: p. 64-72.
62. Bullinger, H.J., Richer, M. and Seidel, K. A., *Virtual Assembly Planning*. Human Factors and Ergonomics in Manufacturing, 2000. **10**(3): p. 331-341.
63. Gomes de sa, A.a.Z., G., *Virtual Reality as a Tool for Verification of Assembly and Maintenance Processes*. Computers and Graphics, 1999. **23**: p. 189-403.
64. Fa, M., Fernando, T., and Dew, P.M., *Direct 3D Manipulation for Constraint-based Solid Modeling*. Computer Graphics Forum, 1993. **12**(3): p. 237-248.
65. Jayaram, S., Jayaram, U., Wang, Y., Tirumali, H., Lyons, K. and, Hart, P., *VADE: A Virtual Assembly Design Environment*. Computer Graphics and Applications, 1999. **19**(6): p. 44-50.
66. Jayaram, U., Tirumali, H. and, Jayaram, S. *A Tool/Part/Human Interaction Model for Assembly in Virtual Environments*. in *ASME Design Engineering Technical Conferences 2000 (DETC 2000/CIE-14584)*. 2000. Baltimore, MD.

67. Taylor, F., Jayaram, S. and, Jayaram, U. *Functionality to Facilitate Assembly of Heavy Machines in a Virtual Environment*. in *ASME Design Engineering Technical Conferences (DETC 2000/CIE-14590)*. 2000. Baltimore, MD.
68. Jayaram, S., Jayaram, U., Wang, Y., and Lyons, K. *CORBA-based Collaboration in a Virtual Assembly Design Environment*. in *ASME Design Engineering Technical Conferences and Computers and Information in Engineering Conference (DETC 2000/CIE-14585)*. 2000. Baltimore, MD.
69. Wang, Y., Jayaram, S., Jayaram, U., and Lyons, K. *Physically Based Modeling in Virtual Assembly*. in *ASME Design Engineering Technical Conferences and Computers and Information in Engineering Conference (DETC2001/CIE-21259)*. 2001. Pittsburg, PA.
70. Czernuszenko, M., Pape, D., Sandin, D., DeFanti, T., Dawe, G. L., and Brown, M. D., *ImmersaDesk and Infinity Wall Projection-Based Virtual Reality Displays*. *Computer Graphics*, 1997. **31**(2): p. 46-49.
71. Shaikh, I., Jayaram, U., Jayaram, S., and Palmer, C. *Participatory Ergonomics Using VR Integrated with Analysis Tools*. in *2004 Winter Simulation Conference*. 2004. Washington D.C.
72. Jayaram, U., Jayaram, S., Shaikh, I., Kim, Y., and Palmer, C., *Introducing Quantitative Analysis Methods into Virtual Environments for Real-Time and Continuous Ergonomic Evaluations*. *Computers in Industry*, 2006. **57**(3): p. 283-296.
73. Jayaram, S., Jayaram, U., Kim, Y., DeChenne, C., Lyons, K., Palmer, C., Mitsui, T., *Industry Case Studies in the Use of Immersive Virtual Assembly*. *Virtual Reality*, 2007. **11**(4): p. 217 - 228.
74. Wan, H., Gao, S., Peng, Q., Dai, G and Zhang, F. *MIVAS: A Multi-Modal Immersive Virtual Assembly System*. in *ASME Design Engineering Technical Conferences and Computers and Information in Engineering Conference (DETC 2004/CIE-57660)*. 2004. Salt Lake City, UT.
75. Zhu, Z., Gao, S., Wan, H., Luo, Y., and Yang, W. *Grasp Identification And Multi-Finger Haptic Feedback For Virtual Assembly*. in *ASME Design Engineering Technical Conferences and Computers and Information in Engineering Conference (DETC 2004/CIE-57718)*. 2004. Salt Lake City, Utah, USA.: ASME.
76. Jin, X., Li, Y., and Peng, Q., *General Constrained Deformations Based on Generalized Metaballs*. *Computers & Graphics*, 2000. **24**(2).
77. Guy, A., and Wyvill, B. *Controlled Blending for Implicit Surfaces using a Graph*. in *Implicit Surfaces*. 1995. Grenoble, France.
78. Wan, H., Luo, Y., Gao, S., and Peng, Q., *Realistic Virtual Hand Modeling with Applications for Virtual Grasping*. 2004 ACM SIGGRAPH International Conference on Virtual Reality Continuum and its Applications in Industry, 2004: p. 81-87.
79. Gottschalk, S., Lin, M. C. and Manocha, D. *OBBTree: A Hierarchical Structure for Rapid Interference Detection*. in *23rd Annual Conference on Computer Graphics and Interactive Techniques*. 1996.
80. *Immersion Corporation* (<http://www.immersion.com/>).
81. *D-Cubed* ([http://www.plm.automation.siemens.com/en\\_us/products/open/d-cubed/index.shtml](http://www.plm.automation.siemens.com/en_us/products/open/d-cubed/index.shtml)).
82. *Parasolid* ([http://www.ugs.com/en\\_us/products/open/parasolid/index.shtml](http://www.ugs.com/en_us/products/open/parasolid/index.shtml)).

83. Jung, B., Latoschik, M., and Wachsmuth, I. *Knowledge-Based Assembly Simulation for Virtual Prototype Modeling*. in *Proceedings of the 24th Annual Conference of the IEEE Industrial Electronics Society*. 1998. Aachen, Germany.
84. Singh, B., and Bettig, B., *Port-Compatibility and Connectability Based Assembly Design*. *Journal of Computing and Information Science in Engineering*, 2004. **4**(3): p. 197-205.
85. Liu, Z., and Tan, J. *Virtual Assembly and Tolerance Analysis for Collaborative Design*. in *9th International Conference on Computer Supported Cooperative Work in Design 2005*. 2005. Coventry, United Kingdom.
86. Liu, Z., and Tan, J., *Constraint Behavior Manipulation for Interactive Assembly in a Virtual Environment*. *International Journal of Advanced Manufacturing Technology*, 2007. **32**(7-8): p. 797-810.
87. Jayaram, S., Joshi, H., Jayaram, U., Kim, Y., Kate, H., and Varoz, L. *Embedding Haptic-Enabled Tools in CAD for Training Applications*. in *ASME Design Engineering Technical Conferences and Computers and Information in Engineering Conference (DETC2006-99656)*. 2006. Philadelphia, PA.
88. Wang, Q.H., Li, J. R., and Gong, H. Q. *A CAD-linked Virtual Assembly Environment*. *International Journal of Production Research*, 2006. **44**(3): p. 467-486.
89. Yang, R., Wu, D., Fax, X., and Yan, J., *Research on Constraint-Based Virtual Assembly Technologies*. *Frontiers of Mechanical Engineering in China*, 2007. **2**(2): p. 243-249.
90. Gupta, R., and Zeltzer, D. *Prototyping and Design for Assembly Analysis using Multimodal Virtual Environments*. in *Proceedings of ASME Computers in Engineering Conference and the Engineering Database Symposium*. 1995. Boston, MA.
91. Gupta, R., Whitney, D., and Zeltzer, D., *Prototyping and Design for Assembly Analysis using Multimodal Virtual Environments*. *Computer Aided Design (Special issue on VR in CAD)*, 1997. **29**(8): p. 585-597.
92. Fröhlich, B., Tramberend, H., Beers, A., Agarawala, M. and Baraff, D. *Physically-Based Modeling on the Responsive Workbench*. in *IEEE Virtual Reality Conference*. 2000.
93. Baraff, D., *Interactive Simulation of Solid Rigid Bodies*. *Computer Graphics and Applications*, 1995. **15**(3): p. 63-75.
94. Krüger, W., and Fröhlich, B., *The Responsive Workbench*. *Computer Graphics and Applications*, 1994. **14**(3): p. 12-15.
95. Coutee, A.S., McDermott, S. D., and Bras, B., *A Haptic Assembly and Disassembly Simulation Environment and Associated Computational Load Optimization Techniques*. *ASME Transactions - Journal of Computing & Information Science in Engineering*, 2001. **1**(2): p. 113-122.
96. Coutee, A.S., and Bras, B. *Collision Detection for Virtual Objects in a Haptic Assembly and Disassembly Simulation Environment*. in *ASME Design Engineering Technical Conferences and Computers and Information in Engineering Conference (DETC2002/CIE-34385)*. 2002. Montreal, Canada.
97. *Sensible Technologies* (<http://www.sensible.com/>).
98. Kim, C.E., and Vance, J.M., *Collision Detection and Part Interaction Modeling to Facilitate Immersive Virtual Assembly Methods*. *ASME Journal of Computing and Information Sciences in Engineering*, 2004. **4**(1): p. 83-90.
99. *Fifth Dimension Technologies* (<http://5dt.com/>).
100. Kim, C.E., and Vance, J.M. *Development of a Networked Haptic Environment in VR to Facilitate Collaborative Design Using Voxmap Pointshell (VPS) Software*. in *ASME*

- Design Engineering Technical Conferences and Computers and Information in Engineering Conference (DETC2004/CIE-57648)*. 2004. Salt Lake City, UT.
101. Seth, A., Su, H. J., and Vance, J. M. *A Desktop Networked Haptic VR Interface for Mechanical Assembly*. in *ASME International Mechanical Engineering Congress & Exposition (IMECE2005-81873)*. 2005. Orlando, FL, USA.
  102. Seth, A., Su, H. J., and Vance, J. M. *SHARP: A System for Haptic Assembly & Realistic Prototyping*. in *ASME Design Engineering Technical Conferences and Computers and Information in Engineering Conference (DETC2006/CIE-99476)*. 2006. Philadelphia, PA, USA.
  103. Just, C., A. Bierbaum, A. Baker, and, C. Cruz-Neira, *VR Juggler: A Framework for Virtual Reality Development*, in *2nd Immersive Projection Technology Workshop (IPT98) CD-ROM*. 1998: Ames, IA.
  104. *Barco Baron*  
(<http://www.barco.com/entertainment/en/products/product.asp?element=1192>).
  105. Seth, A., Vance, J. M., and Oliver, J. H. *Combining Geometric Constraints with Physics Modeling for Virtual Assembly Using SHARP*. in *ASME Design Engineering Technical Conferences and Computers and Information in Engineering Conference (DETC2007/CIE-34681)*. 2007. Las Vegas, NV, USA.
  106. Garbaya, S., and Zaldivar-Colado, U., *The Affect of Contact Force Sensations on User Performance in Virtual Assembly Tasks*. *Virtual Reality*, 2007. **11**(4): p. 287-299.
  107. Ritchie, J.M., Lim, T., Sung, R.S., Corney, J.R., Rea, H., *The analysis of design and manufacturing tasks using haptic and immersive VR: Some case studies*, in *Product Engineering*. 2008, Springer Netherlands. p. 507-522.
  108. Coutee, A.S., and, Bras, B. *An Experiment on Weight Sensation in Real and Virtual Environments*. in *ASME Design Engineering Technical Conferences and Computers and Information in Engineering Conference (DETC2004-57674)*. 2004. Salt Lake City, Utah, USA.
  109. Lim, T., Ritchie, J.M., Corney, J.R., Dewar, R.G., Schmidt, K., Bergsteiner, K. *Assessment of a haptic virtual assembly system that uses physics-based interactions*. in *Proceedings of the 2007 IEEE International Symposium on Assembly and Manufacturing*. 2007. Ann Arbor, MI: IEEE.
  110. Lim, T., Ritchie, J.M., Dewar, R.G., Corney, J.R., Wilkinson, P., Calis, M., Desmulliez, M., Fang, J.-J, *Factors affecting user performance in haptic assembly*. *Virtual Reality*, 2007. **11**(4): p. 241-252.
  111. Burdea, G.C., *Invited Review: The Synergy Between Virtual Reality and Robotics*. *IEEE Transactions on Robotics and Automation*, 1999. v **15**(n 3): p. 400-410.
  112. Volkov, S., and Vance, J. M., *Effectiveness of Haptic Sensation for the Evaluation of Virtual Prototypes*. *ASME Journal of Computing and Information Sciences in Engineering*, 2001. **1**(2): p. 123-128.
  113. Regnbrecht, H., Hauber, J., Schoenfelder, R., and Maegerlein, A. *Virtual Reality Aided Assembly with Directional Vibro-Tactile Feedback*. in *Proceedings of the 3rd international conference on Computer graphics and interactive techniques in Australasia and South East Asia*. 2005. Dunedin, New Zealand.
  114. Gurocak, H., Parrish, B., Jayaram, S., and Jayaram, U. *Design of a Haptic Device For Weight Sensation in Virtual Environments*. in *ASME Design Engineering Technical*

- Conferences and Computers and Information in Engineering Conference (DETC2002/CIE-34387)*. 2002. Montreal, Canada.
115. Zachmann, G., and Rettig, A. *Natural and Robust Interaction in Virtual Assembly Simulation*. in *8th ISPE International Conference on Concurrent Engineering: Research and Applications*. 2001. Anaheim, CA.
  116. Massie, T., and, Salisbury, K. *The PHANToM Haptic Interface: A Device for Probing Virtual Objects*. in *Proceedings of the ASME Winter Annual Meeting, Symposium on Haptic Interfaces for Virtual Environment and Teleoperator Systems*. 1994. Chicago, IL.
  117. Haption S.A. (<http://www.haption.com/index.php?lang=eng>).
  118. The Novint Falcon (<http://www.novintfalcon.com/>).
  119. Millman, P.A., Stanley, M., and Colgate, J.E. *Design of a High Performance Haptic Interface to Virtual Environments*. in *IEEE Virtual Reality Annual International Symposium*. 1993. Seattle, WA.
  120. Buttolo, P., and, Hannaford, B. *Pen-based Force Display for Precision Manipulation in Virtual Environments*. in *IEEE Virtual Reality Annual International Symposium*. 1995. Research Triangle Park, NC, USA.
  121. Bouzit, M., Popescu, G., Burdea, G.C., and Boian, R. *The Rutgers Master II-ND Force Feedback Glove*. in *HAPTICS 2002: Haptic Interfaces for Virtual Environment and Teleoperator Systems*. 2002. Orlando, FL.
  122. Dewar, R.G., Carpenter, I.D., Ritchie, J.M., and Simmons, J.E.L. *Assembly Planning in a Virtual Environment*. in *Proceedings of Portland International Conference on management of Engineering and Technology (PICMET 97)*. 1997. Portland, OR: IEEE Press.
  123. Chen, X., Xu, N., and Li, Y. *A Virtual Environment for Collaborative Assembly*. in *Second International Conference on Embedded Software and Systems (ICCESS'05)*. 2005.
  124. Zhang, Y., Sotudeh, R., and Fernando, T. *The Use of Visual and Auditory Feedback for Assembly Task Performance in a Virtual Environment*. in *Proceedings of the 21st spring conference on Computer Graphics*. 2005. Budmerice, Slovakia.
  125. Garcia-Alonso, A., Serrano, N., and Flaquer J., *Solving the Collision Detection Problem*. *IEEE Computer Graphics and Applications*, 1994. **14**(3): p. 36-43.
  126. Kaufman, A., Cohen, D., and Yagle, R., *Volume Graphics*. *IEEE Computer*, 1993. **26**(7): p. 51-64.