

Optimal Evacuation of Process Plants in Case of Tank Fires

Nima Khakzad^{a,*}, Paul Amyotte^b

^aToronto Metropolitan University, Toronto, Canada

^bDalhousie University, Halifax, Canada

nima.khakzad@torontomu.ca

Effective firefighting and evacuation as integral parts of emergency response in petrochemical plants play a key role in protecting human lives in the event of major tank fires. Compared to firefighting, however, studies devoted to planning and optimizing evacuation plans in the event of tank fires, and particularly concurrent tank fires, have been very few. In the present study, considering the thermal dose as the main cause of casualties in outdoor fires, an innovative methodology is developed to identify proactive evacuation plans for credible fire scenarios. The methodology consists of three main parts: (1) For a given fire scenario (e.g., a single or multiple tank fires), the tank terminal is modelled as a thermal graph in which the weight of each node presents the corresponding heat flux, and the weight of each edge presents the thermal dose between the connected nodes; (2) Dijkstra's algorithm is used to find the shortest paths (a series of connected edges with the least total thermal dose) to the safe spots (e.g., shelters); (3) Considering the limited capacities of safe spots, mathematical programming is used to identify the number of evacuees to be assigned to each safe spot so as to minimize the total risk of casualties during evacuation. Application of the methodology to an illustrative process plant resulted in intuitive evacuation plans, which is indicative of the methodology's validity, particularly in the absence of similar studies for comparison and validation purposes.

1. Introduction

Among industrial plants, chemical and process plants are very susceptible to accidental and intentional fires due to the presence of large quantities of flammable chemicals and a variety of ignition sources. Fire at chemical and process plants may vary from small fires, which can safely be handled by portable fire extinguishers, to major tank fires, which demand emergency response measures, including plant evacuation and firefighting. Despite several studies on fire protection (Janssens et al., 2015; Landucci et al., 2015; Ovidi et al., 2021) and optimal firefighting of process plants (Khakzad, 2018, 2021), works devoted to evacuation of chemical and process plants in the event of major fires have relatively been very few.

Previous research has usually come up with general recommendations for evacuation during major safety and security events (Hosseinnia, et al., 2018), has investigated the issue from an economic perspective – is it economically viable to shut down and evacuate the plant? (Reniers et al., 2007), or has been devoted to evacuation in the event of accidents other than fires (Zhang et al., 2017; Yoo and Choi, 2019). Also, available guidelines and standards such as CAAP (2010) and API RP 2001 (2011) are too general to be used to identify optimal evacuation plans in chemical and process plant fires.

The present study is aimed at developing a methodology for optimal evacuation of process plants in the event of major tank fires. To this end, considering the thermal dose as the main cause of casualties, Dijkstra's algorithm is used to identify the shortest evacuation path from an operating unit to a safe spot given single or concurrent tank fires, with the distance from node i to node $i+1$ being equal to the received thermal dose from i to $i+1$. This way, the shortest path would be a path with the least accumulated thermal dose, and would thus be the safest path. That being said, throughout this manuscript, shortest path and safest path are used interchangeably. In case of having multiple limited-capacity safe spots, mathematical programming can be used to optimally disperse the evacuees among the safe spots in order to minimize the risk of casualties. This way, pre-planned evacuation procedures can be identified and presented in the form of decision-making tables to facilitate evacuation of process plants in the event of fire scenarios.

2. Methods and Materials

2.1 Thermal grid

Exposed to fire, the thermal dose (D) received by a human is dependent on the intensity of heat flux (q) and exposure time (t_e) (Assael and Kakosimos, 2010):

$$D = t_e \cdot q^{4/3} \quad (1)$$

For a fire, q (W/m^2) at a distance can be calculated using a variety of analytical and numerical models (e.g., the point source mode). The exposure time t_e (s) can be calculated using the relationship below (Assael and Kakosimos, 2010):

$$t_e = t_r + \frac{L}{u} \quad (2)$$

where t_r (s) is the reaction time; L (m) is the distance the exposed person should run to get the safe spot; u is the average speed of the person (~ 4 m/s). For trained personnel who expect fires and explosions at the workplace, $t_r \sim 3$ s while for a lay person $t_r \sim 8$ s.

For a given fire scenario, such as a tank fire, a process plant can be modeled as a two-dimensional grid. The intensity of heat flux for each node of the grid can be calculated and assigned as the weight of that node. Subsequently, by combining Eq (1) and Eq (2), the thermal dose an evacuee may receive while escaping from their location (at node $i = 0$) to the safe spot (at node j) can be calculated as (Khakzad, 2023):

$$D = t_r q_0^{4/3} + \sum_{i=1}^j \left(\frac{q_i + q_{i-1}}{2} \right)^{4/3} \frac{\Delta x}{u} \quad (3)$$

where q_i and q_{i+1} are two adjacent nodes on the grid; Δx is the distance between the adjacent nodes; q_0 is the heat flux at the initial location of the evacuee. As an example, consider a thermal grid in Figure 1 where for a given fire, an evacuee should leave their initial location at node $i = 0$ and seek shelter at the safe spot at node $i = 3$. In doing so, the evacuee decides to traverse nodes $i = 0, 1, 2,$ and 3 in sequence. The heat flux intensity at each node has been calculated and shown as q inside the node.

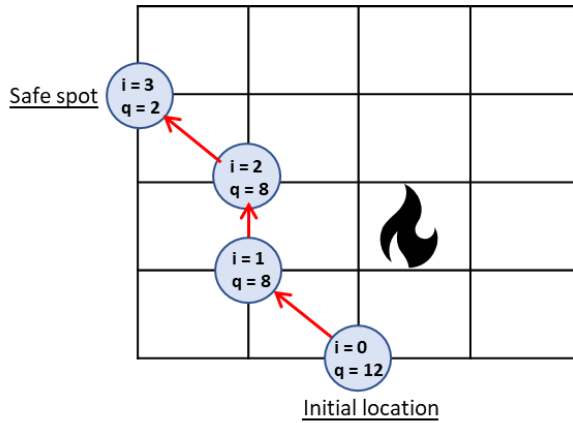


Figure 1. Thermal grid given a fire in the process plant. Each node is indicated with two indices: i refers to the node number while q (kW/m^2) shows the intensity of heat flux at that node. An evacuee is supposed to escape from their location at $i = 0$ to a safe spot at $i = 3$. The presented path here is for illustrative purposes and is not necessarily the shortest (safest) available path.

Further, assume that the distances between the adjacent nodes are $\Delta_{01} = 40$ m, $\Delta_{12} = 20$ m, and $\Delta_{23} = 40$ m. Assuming $t_r = 3$ s and $u = 4$ m/s, the total thermal dose the evacuee would receive while escaping from the 'initial location' to the 'safe spot' can be calculated as:

$$D = t_r q_0^{4/3} + \sum_{i=1}^j \left(\frac{q_i + q_{i-1}}{2} \right)^{4/3} \frac{\Delta x}{u} = 3(12000)^{4/3} + \left(\frac{12000+8000}{2} \right)^{4/3} \frac{40}{4} + \left(\frac{8000+8000}{2} \right)^{4/3} \frac{20}{4} + \left(\frac{8000+2000}{2} \right)^{4/3} \frac{40}{4} = 4,633,617 \text{ (W}^{4/3}\text{m}^{-8/3}\text{s)}.$$

Given the thermal dose, dose-response relationships can be used to estimate the probability of injury (e.g., 2nd degree burns) or death. The following probit function can be used to estimate the death probability due to heat exposure (Assael and Kakosimos, 2010):

$$Y = -36.38 + 2.56 \ln(D) \quad (4)$$

$$P = F_c \cdot \Phi(Y - 5) \quad (5)$$

Where Y is the probit value; F_c is the clothing coefficient, accounting for the role of clothing in protecting an exposed human, with typical values of 0.85 and 0.18 for summer and winter outfits, respectively; $\Phi(\cdot)$ is the cumulative density function for standard normal distribution.

2.2 Dijkstra's algorithm

Dijkstra's shortest path algorithm (Dijkstra, 1959) is a greedy algorithm to identify the shortest path between two nodes on a graph (or mesh). In Dijkstra's algorithm, the state of a node is identified by two variables: the distance value of the node d_j , which is its distance from the starting node, and the status label of the node, which can be permanent (p) or temporary (t). The status label is permanent only if the distance value of the node is the shortest distance from the starting node. Dijkstra's algorithm measures and updates the distance values of the nodes until all the status labels become permanent. The algorithm for finding the shortest paths from a starting node to other nodes of the graph includes three stages: Initialization, Updating, and Termination.

- Initialization

Assign zero to the distance value and 'permanent' to the status label of the starting node $i = 0$: The state of this node is now $(0, p)$. Assign to every other node a distance value ' ∞ ' and a status label 'temporary'. The states of the other nodes are now (∞, t) . Designate the starting node $i = 0$ as the 'current' node.

- Updating distance values

Find the set J of nodes with temporary labels that can be reached from the current node via a single link. For each $j \in J$, the distance value of node j is updated as: $d_j = \min \{d_j, d_i + w_{ij}\}$, where w_{ij} is the weight of the edge linking node i to node j . Among the nodes, the one with the smallest updated distance value (node j^*) is added to the set of current nodes and its status is changed to 'permanent'. The state of this node is thus updated to (d_j^*, p) .

- Termination

The previous step should be repeated by finding the set of nodes with temporary labels that can be reached from any of the current nodes i or j^* via a single edge. The algorithm terminates when the status labels of all the nodes (or the destination node of interest) that can be reached from the starting node $i = 0$ turns to 'permanent'. An application of Dijkstra's algorithms has been exemplified in Figure 2 to find the shortest path between nodes A and D.

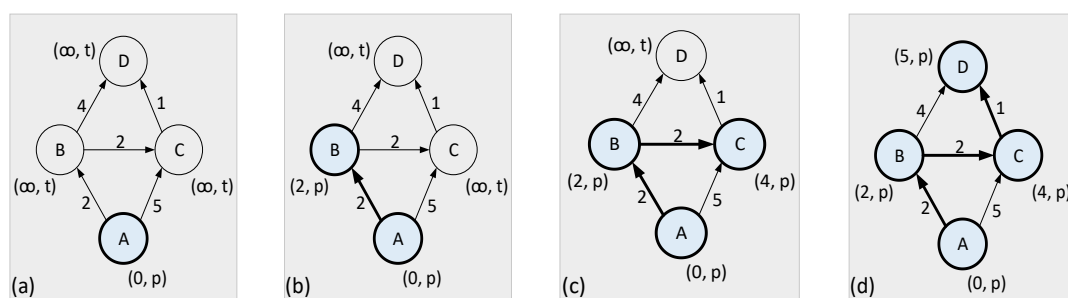


Figure 2. Application of Dijkstra's algorithm to find the shortest path and distance from node A to node D. Panels (a)-(d) present the sequential steps via the algorithm (Khakzad, 2023).

2.3 Mathematical programming

Mathematical programming includes a number of techniques to maximize or minimize the value of a function (known as objective function) by finding the best values of the function parameters. Maximum or minimum value of the function and thus the optimal values of its variables would be subject to some constraints. In some mathematical programming techniques, a feasible solution (i.e., the set of optimal values of variables) can be obtained only if all the constraints are satisfied. However, some other techniques such as goal programming

can render a feasible solution even if some less important constraints are violated in favor of more important constraints. Mathematical programming in the form of minimization, for instance, can be presented as:

$$\begin{aligned} & \text{minimize } Z = f(X) \\ & \text{Subject to: } \begin{cases} g(X) \leq 0 \\ h(X) = 0 \end{cases} \end{aligned} \quad (6)$$

where $X = \{X_1, \dots, X_n\}$ is the set of variables, or function parameters; Z is the objective function as a function of X ; and $g(X)$ and $h(X)$ are the constraint functions.

3. Methodology

3.1 Case study

Consider a process area with two operating units, two gasoline storage tanks and two fire shelters in Figure 2. Given concurrent tank fires at Tank #1 and #2, the process area can be modelled as a thermal grid showing the intensity of heat flux at each node of the grid. The heat flux intensity at each node can be calculated for each tank fire via a number of models and techniques (e.g., the point source model) knowing the tank size and weather conditions, and then in case of multiple simultaneous fires these heat flux intensities can be superimposed to find the total heat flux intensity at each node. For the sake of exemplification, assume that the heat flux intensities for each tank fire were already calculated, superimposed, and presented inside each node with q . This way, each node of the grid can be indexed with a number 'i' and its corresponding heat flux intensity 'q'.

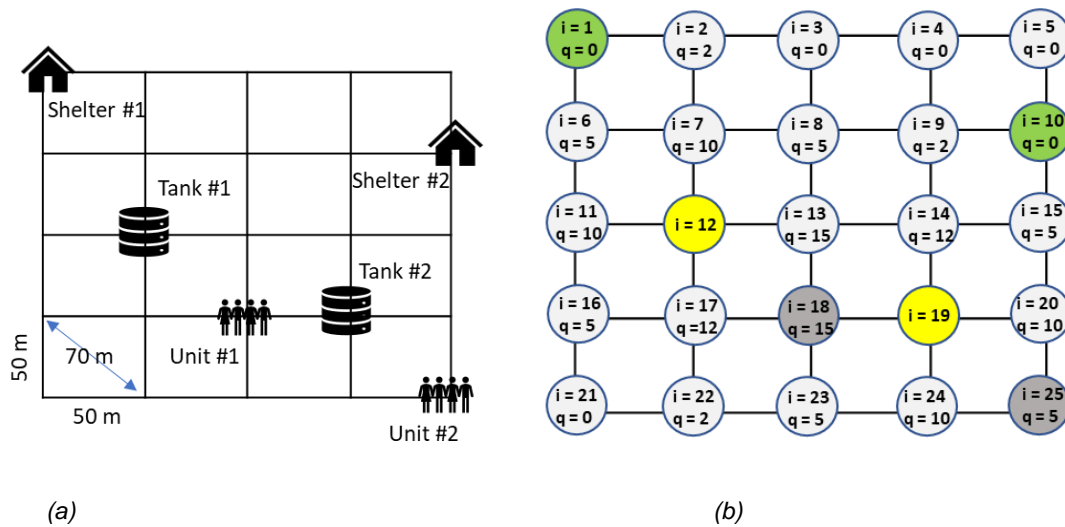


Figure 2. (a) A process area, consisting of two operating units, two gasoline storage tanks, and two fire shelters. (b) Modelling the process area as a thermal grid given tank fires at the storage tanks. Each node has been identified with a node number i and the intensity of heat flux q at that node (in kW/m^2).

Knowing the heat flux intensities and the distance between adjacent nodes in Figure 2, the thermal dose one would receive while traversing between two adjacent nodes, either horizontally or diagonally, can be calculated using Eq (3). The results can then be summarized in the form of a thermal-dose graph in which the weight assigned to the edge connecting node 'i' and 'i+1' shows the corresponding thermal dose when one moves from the former to the latter or vice versa. Regarding the process area in Figure 2, since the aim is to find the shortest paths from the operating units (nodes $i = 18, 25$) to the shelters (nodes $i = 1, 10$), $t_r q_0^{\frac{4}{3}}$ on the right-hand side of Eq (3) can be ignored as this term contributes equally to all the paths and thus its omission would be fine for comparison purposes (Khakzad, 2023). Figure 3 shows the thermal-dose graph for the process area where the weight of each edge shows the respective thermal dose in 105 W/m^2 , presuming that an evacuee would not run toward the tank fires while escaping to the shelters. Due to this presumption, the edges running from tank fires' adjacent nodes toward the tank fires have been deleted from the graph for simplification.

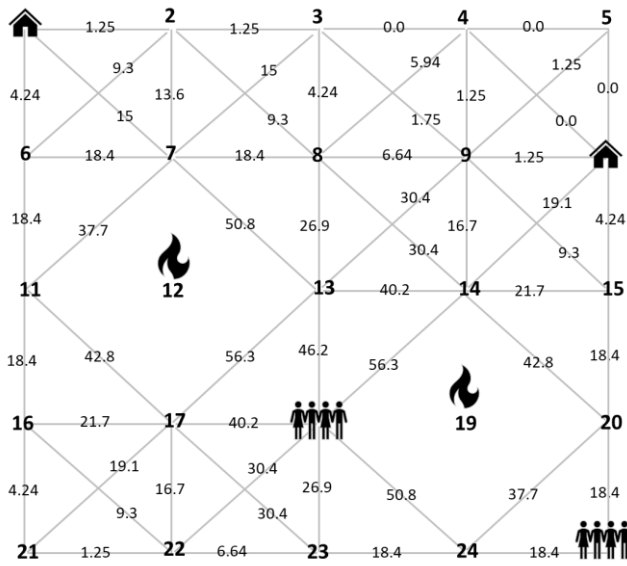


Figure 3. Modelling the process area as a thermal-dose graph. The weights assigned to each edge show the corresponding thermal dose while an evacuee traverses between the nodes connected by that edge. Presuming that an evacuee would not run directly toward a tank fire, such edges have been deleted from the graph. The node numbers are presented with bold numbers.

3.2 Identification of shortest paths

Since a smaller thermal dose is attributed to a smaller probability of injury or death, an optimal evacuation path between the operating units (nodes $i = 18$ & 25) and the shelters can be considered as a path (a sequence of connected edges) with the least accumulated thermal dose.

To this end, the shortest paths from Unit #1 (node $i = 18$) to the shelters (nodes $i = 1$ & 10) can be identified by applying Dijkstra's algorithm as:

- From Unit #1 to Shelter #1: $i = 18 \rightarrow i = 22 \rightarrow i = 21 \rightarrow i = 16 \rightarrow i = 11 \rightarrow i = 6 \rightarrow i = 1$, with the total thermal dose 77×10^5 kW/m², and
- From Unit #1 to Shelter #2: $i = 18 \rightarrow i = 14 \rightarrow i = 9 \rightarrow i = 10$, with the total thermal dose 74×10^5 kW/m².

Similarly, the shortest paths from Unit #2 (node $i = 25$) to the shelters (nodes $i = 1$ & 10) can be identified as:

- From Unit #2 to Shelter #1: $i = 25 \rightarrow i = 20 \rightarrow i = 15 \rightarrow i = 10 \rightarrow i = 4 \rightarrow i = 3 \rightarrow i = 2 \rightarrow i = 1$, with the total thermal dose 43.5×10^5 kW/m², and
- From Unit #2 to Shelter #2: $i = 25 \rightarrow i = 20 \rightarrow i = 15 \rightarrow i = 10$, with the total thermal dose 41×10^5 kW/m².

Using Eq (4) and Eq (5), and considering a cloth effect of $F_C = 0.5$, the probability of death for a single evacuee who may escape from unit i to shelter j (P_{ij}) is calculated as $P_{11} = 10.5\%$, $P_{12} = 9.5\%$, $P_{21} = 1.5\%$, and $P_{22} = 0.5\%$.

3.3 Optimal allocation of evacuees

Having the shortest paths identified by applying Dijkstra's algorithm, mathematical programming can be employed for optimal allocation of evacuees to the shelters. To demonstrate this, assume that the number of evacuees at Units #1 and #2 are, respectively, 5 and 10, while the capacity of Shelters #1 and #2 are, respectively, 15 and 8. The goal is thus to determine the number of evacuees from each unit that should be sent to each shelter in order to minimize the number of casualties. Considering X_{ij} as the number of evacuees that should be sent from Unit i to Shelter j , the optimization problem can be formulated as:

$$\text{Minimize } Z = P_{11}X_{11} + P_{12}X_{12} + P_{21}X_{21} + P_{22}X_{22} \quad (7)$$

$$\text{Subject to: } \begin{cases} X_{11} + X_{21} \leq 15 \\ X_{12} + X_{22} \leq 8 \\ X_{11} + X_{12} = 5 \\ X_{21} + X_{22} = 10 \end{cases} \quad (8)$$

The first two constraints in Eq (8) are to ensure that the number of evacuees at each shelter will not exceed the shelter capacity while the last two constraints are to ensure that no one would be left out. Solving Eq (7) and Eq (8) in the Microsoft Excel Solver Tool Pak, the optimal values of the evacuation variables X_{ij} are identified as: $X_{11} = 5$, $X_{12} = 0$, $X_{21} = 2$, $X_{22} = 8$, with the total number of casualties as $Z = 0.6$. The result is completely intuitive as evacuees from each unit are first sent to the nearest (safest) shelter (Unit #1 is near Shelter #1 and Unit #2 is near Shelter #2) and then, anyone left is sent to the second nearest shelter.

4. Conclusions

Evacuation is an integral part of fire safety and protection, which plays a key role in protecting human lives in the event of major accidents in chemical and process plants. Among the major accidents, however, the majority of the previous studies have developed evacuation methodologies for release and dispersion of toxic chemicals with too little attention, if any, to major fires and particularly concurrent multiple fires.

In the present study, considering the thermal dose as the main cause of casualties during major industrial fires, a methodology was developed by integrating Dijkstra's algorithm and mathematical programming for optimal evacuation. For this purpose, Dijkstra's algorithm was employed to identify the safest path – a path with the least accumulated thermal dose – from a unit to a safe spot while mathematical programming was used to identify the number of evacuees that should be assigned to each safe spot.

The applicability of the developed methodology can further be improved by considering a wider range of process plants and fire scenarios and the combined effect of heat and smoke in the form of a heat-smoke-graph.

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