



# Article DFT Studies of the Adsorption of Propane and Propene on Metallic Surfaces in Ag/ZrO<sub>2</sub> Catalysts as a Model for Catalytic Combustion Reactions of Light Hydrocarbons

José F. Ruggera \*<sup>®</sup>, Marco A. Ocsachoque, Maia Montaña <sup>†</sup><sup>®</sup>, Mónica L. Casella and Ileana D. Lick \*<sup>®</sup>

ocmarco@quimica.unlp.edu.ar (M.A.O.); maia.montana@urjc.es (M.M.); casella@quimica.unlp.edu.ar (M.L.C.) \* Correspondence: jfruggera@quimica.unlp.edu.ar (J.F.R.); ilick@quimica.unlp.edu.ar (I.D.L.)

<sup>+</sup> Current affiliation: Department of Chemical, Energy and Mechanical Technology, Rey Juan Carlos University, C/Tulipán s/n, 28933 Móstoles, Spain.

Abstract: Molecular modelling studies were carried out at the DFT level of the adsorption of propane and propene on Ag surfaces as a model of the interaction of light hydrocarbons with Ag/ZrO<sub>2</sub> catalysts for catalytic combustion reactions. It was found that the most stable mode of adsorption of propene through its  $\pi$  system on Ag atom has energies consistent with chemisorption and generates an elongation of the C1=C2 bond, which would explain the increase in the activity of the catalysts as a function of its metallic charge. The results obtained from the DFT calculations explain the different types of interactions between propene and propane with the metallic surface. The propene is chemisorbed on the Ag surface, distorting its bonds and generating its activation. This would imply that a higher metallic charge in the catalyst would increase the number of active sites in which this activation occurs, generating a higher activity. In addition, with the addition of O, the binding energy between the propene and the metal surface increased. On the other hand, the presence of a metallic surface is not enough for the activation of the propane molecule. This would explain why, by increasing the amount of metal in the catalyst, the activity for the combustion of propane is practically not affected.

Keywords: propane; propene; combustion; DFT; silver

# 1. Introduction

The increasingly strict legislation regarding the control of contaminants present in sources of gaseous emissions generates a challenge for the development of clean technologies and environmental catalysis [1,2]. These emissions can come from stationary sources, mainly from the petrochemical industry, or from mobile sources, mainly from diesel engine exhausts. The pollutants usually present in gaseous emissions are nitrogen oxides (NOx), carbon oxides (COx), sulphur oxides (SOx), particulate matter, and volatile organic compounds (VOCs), among others. In particular, within the volatile organic compounds, hydrocarbons can be found in the C2–C10 range and those with the shortest chain, C2–C3, are the most difficult to remove [3].

One of the most widely used technologies to eliminate hydrocarbon molecules present in emissions is catalytic oxidation, also called catalytic combustion. To carry out this process, filters or converters are needed, which contain catalytic phases capable of lowering the combustion temperatures to temperatures below ~400 °C [4,5]. As is widely reported in the literature, several types of materials catalyse the combustion reactions of alkanes, alkenes, and polyaromatics, including those whose active phases are noble metals such as Pt, Pd, Au, Rh, Ag, etc. [6–9]. These metallic catalysts exhibit good catalytic properties due to their high activity at low temperatures and resistance to poisoning. However, the



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Centro de Investigación y Desarrollo en Ciencias Aplicadas "Dr. Jorge J. Ronco" (CINDECA, CCT CONICET—La Plata, UNLP, CICPBA), Calle 47 No. 257, La Plata 1900, Buenos Aires, Argentina;

high costs and low availability of these noble metals mean their optimisation needs to be maximised. For this, much research has been conducted on the choice of the active-phase support system, the optimisation of metallic content, and, in particular, the elucidation of the site where the reaction proceeds to improve their performance.

Although it is a highly studied topic, which has given rise to numerous bibliographical reviews, the question of whether to optimise a catalytic formulation using one or a certain group of molecules as a model remains. In many cases, similar molecules share similar reaction mechanisms. However, there are catalytic phases that are very active for the combustion of some hydrocarbons that present low activity in others, or they act with different efficiencies or reaction mechanisms depending on the hydrocarbons' nature or chain. For example, for the combustion of alkanes and alkenes over  $Pt/Al_2O_3$  and  $Pt/TiO_2$ catalysts, the reaction orders are positive and negative, respectively [10]. This fact suggests a different coverage of the hydrocarbon on the surface, a different rate-limiting step of the reaction, or the distinctive roles of other reactants, such as oxygen or concomitants, in the mechanism. In this context, the Langmuir-Hinshelwood and the Eley-Rideal mechanisms are two of the three proposed mechanisms for the total oxidation of hydrocarbons [11-13]. In the first one, a bimolecular mechanism, the molecules of hydrocarbon and dioxygen adsorb onto the catalytic surface in the first reaction step [14]. In the second one, a molecule of hydrocarbon adsorbs on the surface and then reacts with oxygen from gas phase [12]. Both mechanisms propose that the first step in the reaction mechanism is the adsorption of the hydrocarbon molecule onto the catalytic surface. However, the ability of an active phase to adsorb a reactant depends on the nature of the active phase, and the adsorbate, especially, depends on its molecular structure.

Throughout decades, evidence has been published about the reaction mechanisms followed in combustion reactions. In the case of oxide catalysts, the occurrence of a redox mechanism (Mars–van Krevelen (MVK) mechanism) [15] is easy to support from empirical data (O<sub>2</sub>–TPD, kinetic data, TPR, etc.) [16–20]. In addition, some authors also found evidence of the occurrence of a Langmuir–Hinshelwood (L–H) mechanism for catalysts containing oxide phases. For example, Feng et al. [21] proposed an L–H mechanism for the total oxidation of propane at low temperatures on  $MnO_2$ , and similar results were found by Heynderickx et al. using CuO-CeO<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> catalysts [22].

On the other hand, when catalysts with supported metallic phases are used, the occurrence of the Langmuir–Hinshelwood and the Eley–Rideal mechanisms is usually considered more likely, especially with catalysts that contain metals capable of adsorbing and/or dissociating the reactants (hydrocarbons and/or O<sub>2</sub>) [23–25]. There are catalytic systems where the discussion is still open. For example, in a previous work carried out in our research group with palladium-promoted cobalt oxide catalysts supported on zinc aluminate, it was observed that the redox activation of propene in the absence of molecular oxygen occurred at a notoriously higher temperature range than the range where the catalytic reaction occurred. The experiments demonstrated that the catalysts could provide oxygen to oxidize the propene and/or activate it through the occurrence of a surface redox reaction. However, this phenomenon occurred at temperatures substantially higher than those where propene combustion is observed. These results indicated that the activity could not only be attributed to a redox mechanism [26]. In addition, these same catalysts were very active for the combustion of propene and had very little activity for the combustion of propane, making it evident that the active site was more efficient for the combustion of the unsaturated hydrocarbon. A similar behaviour was found with gold catalysts supported on zirconia, which were very active for the combustion of naphthalene and presented low activity for the propane combustion [27].

As mentioned, it is evident that both the chemical nature of the active phases and those of the hydrocarbon have a significant influence on the catalytic activity, and there are physicochemical interactions between the reagents and the catalytic surface that still need to be elucidated. In recent years, theoretical chemistry papers have appeared that help understand some of the mechanistic aspects of oxidation reactions of gaseous pollutants (i.e., VOCs, CH<sub>4</sub>, CO, etc.) [2,16,19,24,28–38].

For the more studied metals, for example Pt, it has been proposed that the reason for their different behaviour in catalytic combustion between alkanes and alkenes is the presence of a C=C double bond in alkenes, which can facilitate the strong adsorption of hydrocarbon molecules on the surface of noble metal through the interaction between the  $\pi$  orbitals of the alkene and the d orbitals of the transition metals [6,39]. On the other hand, alkanes interact with the metal surface through van der Waals forces, which are much weaker, causing the reaction mechanisms to be different [40,41]. In most of the proposed reaction mechanisms, the rate-determining step of the reaction is estimated from the reaction order data. There are few works in the literature that show the theoretical results of what occurs at the molecular level on the catalyst surface. For predictive purposes or with the purpose of being able to explain experimental results, it is very interesting to understand in depth how a different type of interaction between the substrate/hydrocarbon and the metal surface can condition the activity of a species and/or modify the step that determines the rate of a reaction or even the mechanism of it. Currently, surface science, through the application of theoretical calculations, makes it possible to study and understand fundamental aspects of the operation/behaviour of heterogeneous catalysts. For example, this method allows analysing the adsorption phenomenon of the species that are part of the reaction. In recent decades, from the implementation of DFT (density functional theory) to periodic systems, it has been possible to model with greater precision what occurs at the atomic level on the surface of catalysts. Several authors have studied the adsorption of C1, C2, and C3 species on the surfaces of different metals by applying DFT calculations. Arya et al. [42] reported the energies of the transition states for the rupture of the C–H model bond on different metals as a model of activation energies for the alkanes' combustion reaction. These authors found that the activation energy decreased in the following order Ag > Au > Al > Cu > Pt > Pd > Ni > Co > Rh > Fe. Wang et al. [34] studiedthe combustion of formaldehyde in a Ag cluster. The results showed that in the oxidation of formaldehyde in a Ag cluster, where there are also chemisorbed O atoms (active species), the energy of the transition state was lower than that calculated for the Ag cluster in the absence of O. A similar result was found by Porter et al. [43] who studied different reaction pathways for the epoxidation of propene on different metals from DFT calculations.

In a previous work reported in our work group, it was found that catalysts based on metallic silver supported on zirconia presented different behaviours when they were used in the combustion reactions of propane and propene [9]. No computational chemistry results that explain this behaviour have been reported in the literature; therefore, it is interesting to model the silver surface and its interaction with short-chain hydrocarbon molecules such as propane and propene. In this work, structure–activity relationships were studied from the theoretical calculations of the molecular modelling of a Ag surface. In addition, the effect of the presence of oxygen surface atoms on the hydrocarbon–catalytic surface interaction was analysed in order to explain the difference in activity previously found.

#### 2. Results and Discussion

Figure 1a,b show the results of the activity in terms of the  $T_{ini}$  and  $T_{50}$  ( $T_{ini}$  = the temperature at which 5% of the hydrocarbon was converted, and  $T_{50}$  = the temperature at which 50% of the hydrocarbon was converted) of the Ag catalysts supported on zirconia for the combustion of propane and propene. A part of these results was reported in a previous work carried out in our group [9] using catalysts with a Ag content of 1, 5, and 10 wt.% denominated Ag1/Z, Ag5/Z, and Ag10/Z, respectively. In the catalyst's absence, propane and propene were oxidised in an O<sub>2</sub>/He atmosphere, and this homogeneous reaction started at higher temperatures ( $T_{ini}$  propane = 510 °C and  $T_{ini}$  propene = 570 °C) and reached 50% conversion at 600 °C and 630 °C, respectively. The bare support exhibited activity for the combustion of both hydrocarbons, and the  $T_{50}$  obtained for both hydrocarbons decreased by 110 °C compared to that found for the reaction in the absence of a

catalyst. Instead, the influence of Ag and its metallic load on the activity depended strongly on the nature of the molecule to be oxidised. For the combustion of propane, the Agx/Z catalysts presented a  $T_{ini}$  similar to that found with the support, and a slight decrease in  $T_{50}$  was observed with the increase in silver content, while for the combustion of propene, the presence of silver strongly influenced the activity. The silver's impact on the propene conversion and catalytic activity increased with the increase in metallic charge. The  $T_{ini}$ and  $T_{50}$  obtained with the Agx/Z catalysts decreased appreciably compared to those found with the support, indicating a notable contribution of the supported metal phase.



**Figure 1.** (a)  $T_{ini}$  obtained with Agx/Z catalysts (x = 1, 5 and 10). (b)  $T_{50}$  obtained with Agx/Z catalysts (x = 1, 5 and 10).

## 2.1. Adsorption on Ag(111)

Considering that the main objective of this work is to explain the difference in the behaviour of the Agx/Z catalysts facing the propane and propene combustion reactions, molecular modelling studies using DFT calculations were performed with a simplified model based on a flat surface of Ag(111). Although there is general agreement that the rate-determining step for propane combustion is the first C–H bond cleavage [44,45] in the case of propene, the elucidation of the mechanism is still under debate.

The choice of the surface was based on the following: in the Ag/support catalysts, the Ag nanoparticles are supported on zirconia ( $ZrO_2$ ), and the contribution of the support to the activity is similar for both reactants (Figure 1); hence, in the model proposed in this work, only the metallic surface was considered. According to the experimental data obtained in previous works, metallic and oxidic silver species coexist on the catalytic surface, but the Ag(0) species predominates [9]. With this objective, the propane and propene adsorption energies were calculated and compared as a first approach to understand which is the fundamental step in the catalytic combustion reaction of both substances on a silver metallic surface.

Figure 2 shows the optimised structures for the adsorption studies of both hydrocarbons on the Ag surface and for propene in the presence of an adsorbed O atom. One stable structure was found (Figure 2a) for propane, while two stable structures were found (Figure 2b,c) for propene. In addition, only one stable structure was also found for the propene adsorption in the presence of oxygen surface atoms in the vicinity of the adsorption site (Figure 2d). Figure 2b shows the optimised structure for the adsorption mode that can be called the "bridge", in which the C1=C2 double bond is located in parallel above the bond between two vicinal silver surface atoms. In Figure 2c, it can be observed that the vertical view of one of the propene adsorption modes can be called the "top", in which the C1=C2 double bond is located just above a Ag surface atom (Figure 3). In the top adsorption mode, propene was adsorbed onto a single Ag surface atom through a  $\pi$  bond, while in the bridge adsorption mode, propene interacted with two Ag atoms through two  $\sigma$  bonds.



**Figure 2.** Side and top view of optimized geometries of (**a**) propane on Ag(111); (**b**) propene bridge mode on Ag(111); (**c**) propene top mode on Ag(111); (**d**) propene top mode on Ag(111) with O adatom.



**Figure 3.** Top view of first layer of the Ag(111) surface and the considered sites (shown in the colours indicated) used in the simulation.

Table 1 shows the results obtained for the distances between the C1 and C2 carbon atoms and the Ag surface atom(s) closest to them. In addition, the C1–C2 bond length

for the propane and propene molecules before and after adsorption are shown. The same table also shows the adsorption energies for the different cases calculated with Equation (1) (please see the Section 3.).

|                | Distances<br>C <sub>1</sub> –Ag (Å) | Distances<br>C <sub>2</sub> –Ag (Å) | Bond Length<br>C <sub>1</sub> –C <sub>2</sub> Free<br>(Å) | Bond Length<br>C <sub>1</sub> –Adsorbed<br>C <sub>2</sub> (Å) | E <sub>ads</sub> (eV) |
|----------------|-------------------------------------|-------------------------------------|---|---|-----------------------|
| Propane        | 3.57                                | 3.87                                | 1.52  | 1.52  | -0.14                 |
| Propene bridge | 3.10                                | 3.25                                | 1.34  | 1.34  | -0.21                 |
| Propene top    | 2.58                                | 2.74                                | 1.34  | 1.35  | -0.77                 |
| Propene O      | 2.50                                | 2.66                                | 1.34  | 1.36  | -0.87                 |

**Table 1.** Distances  $C_1$ –Ag and  $C_2$ –Ag for all adsorbed species (Å), bond length  $C_1$ – $C_2$  before and after adsorbed (Å) and adsorption energies calculated with Equation (1) (eV).

The distances between the carbon atoms of the propane molecule and the Ag metal surface C1–Ag and C2–Ag were 3.57 Å and 3.87 Å, respectively. These distances were greater than those found between the surface and the C1 and C2 atoms of propene in its two adsorption modes (bridge and top). On the other hand, the results showed that in the top adsorption mode, the substrate was closer to the surface than in the bridge adsorption mode. The calculated distances between C1 and C2 and the Ag atom for the top adsorption mode were 2.58 Å and 2.74, respectively, while the values obtained for the bridge adsorption mode were 3.10 Å and 3.25 Å, respectively.

Lian et al. [46] studied the adsorption of propane and propene on a Pt (111) surface, and found that the distance between the propane and Pt surface is approximately 3 Å, while the distance between propene and Pt surface is 2.14 Å. These values are slightly higher (approx. 0.5 Å) than the distances found in this work. In this sense, Yang et al. [47] also found, from DFT studies, that molecular propane is repelled by the metal surface, drifting over the Pt surface, showing that propane is weakly physiosorbed on both Pt(111) and Pt(211).

The C1–C2 bond length of a free hydrocarbon molecule in the vacuum can be different from that adsorbed onto a catalytic surface. Changes in this bond length can provide information about the interactions between the C1–C2 bond and the metallic surface. As shown in Table 1, the C1–C2 bond length calculated for propane was constant, at a value of 1.52 Å, before and after its adsorption over the surface. From these results, a stretching of the C–C bond, which was allowed supposing its activation, was not observed.

The calculations indicated that propene exhibits a different behaviour than that observed with propane. The C1–C2 bond length of the propene, adsorbed in the top mode, was slightly greater (1.35 Å) than that found for the same bond in the vacuum. These results show that there may be an interaction between the alkene molecule and the catalytic surface. The silver surface has the capacity to activate the double bond and lead to a rupture of the C=C bond.

Finally, the last column of Table 1 shows the adsorption energies calculated from Equation (1) (Section 3). The adsorption energies obtained corroborated the analysis carried out from the results of the bond lengths. The most stable structure was found for propene adsorption. An adsorption energy of -0.77 eV was calculated for the top mode, and -0.21 eV was found for the adsorption in the bridge mode. These values showed a strong interaction, i.e., chemisorption, between the alkene and the Ag surface. On the other hand, the propane adsorption on the metallic surface presented an energy of -0.14 eV. This low adsorption energy was consistent with physical adsorption or physisorption.

The results obtained from the DFT calculations explain the different types of interaction between propene and propane with the metallic surface. The propene is chemisorbed on the Ag surface, distorting its bonds and generating its activation. This would imply that a higher metallic charge in the catalyst would increase the number of active sites in which this activation occurs, generating a higher activity. On the other hand, the presence of a metallic surface is not enough for the activation of the propane molecule. This would explain why by increasing the amount of metal in the catalyst, the activity for the combustion of propane is practically not affected.

The interaction energy of the propane with the metallic surface calculated through the DFT was -0.14 eV; this energy suggests a weaker interaction than the one found for propene in the two adsorption modes, and it is also of the order of van der Waals-type interactions. These results agree with what was reported by Lian et al. [15], who studied propane adsorption on Pt catalysts. The interaction energies between propane and the platinum metal surface were between -0.01 and -0.35 eV, depending on the functional used. These values are typical for physisorption energies. In this work, by DFT calculations, it was found that for the optimised structure of the physiosorbed propane molecule on the Ag(111) surface, the C1–C2 bond length was the same as for free propane. This indicated that this physisorption did not generate any distortion in the C1–C2 bond and, consequently, did not induce the activation of the hydrocarbon. These results explain the low dependence of the catalyst activity on the silver content for the propane combustion reaction. Since metallic silver does not intervene in a decisive way in the reaction mechanism, the increase in the metallic charge of this metal in the catalyst does not lead to a substantial increase in its activity.

On the other hand, the adsorption energies calculated for the propene adsorption on the metal surface in the bridge mode and the top mode were -0.21 and -0.77 eV, respectively. The propene adsorption on a silver surface atom, through the  $\pi$  system, was more stable than their adsorption on two silver surface atoms, through two  $\sigma$  type bonds of C1 and C2, in the bridge mode. In the top mode, the propene molecule adsorbed was closer to the metallic surface than in the bridge mode. In addition, in the top mode, a slight stretching of the C1=C2 bond was observed. This stretching was not observed in the bridge mode.

These results suggest the presence of a chemisorption phenomenon, preferentially through the propene  $\pi$  system on a Ag atom, which generates a slight stretching of the C1=C2 bond, activating it for a break. These results agree with those reported by other authors, who propose that this rupture is the determining step of the reaction rate for the combustion of propene [2,16,17].

# 2.2. Adsorption on Ag(111) in the Presence of Oxygen

As suggested by the XPS results (Table 2), metallic and oxidised silver species coexist on the catalytic surface [9]. As was previously reported, all three silver catalysts, Ag1/Z, Ag5/Z, and Ag10/Z, contained silver on their catalytic surface. From the quantification of the Ag3*d* and Zr3*d* signals, it was determined that the Ag/Zr atomic ratio increased with the increase in the silver concentration. Furthermore, from the analysis of the silver signals in the Auger region of the spectra, it was possible to propose the coexistence of metallic and oxidic silver species on the catalytic surface. The signal representing the kinetic energy of the AgM<sub>5</sub>N<sub>45</sub>N<sub>45</sub> Auger transition presented a shoulder at ca. 349.5 eV associated with the presence of oxidic species [9]. This shoulder represents 3% and 6% of the signal for the Ag5/Z and Ag10/Z catalysts, respectively. These results suggest the presence of O atoms associated with surface silver species. Therefore, an O atom was added to the surface to model/simulate a slightly oxidised surface for propene adsorption. The influence of a superficial O atom was studied only for the case of propene adsorption in the top mode because it is the one that presented the highest adsorption energy.

In the top adsorption mode, the presence of an O atom close to the Ag site caused a decrease in the distance between the propene carbons and the surface with respect to the Ag(111) surface without oxygen. The results obtained suggest that the presence of oxygen atoms in the vicinity of the active sites leads to an increase in the interaction. Furthermore, the calculated C1–C2 bond length of the propene molecule when it was adsorbed on a surface containing surface O atoms increased from 1.34 Å to 1.36 Å.

|   | Ag1/Z | Ag5/Z        | Ag10/Z     |
|---|-------|--------------|------------|
| KE AgM <sub>4</sub> N <sub>45</sub> N <sub>45</sub> | -     | 357.5        | 357.9      |
| KE AgM-NN   | _     | 352.5 (97) * | 352.8 (94) |
| KL Agivi51 451 45                                   |       | 349.5 (3)    | 349.4 (6)  |
| Ag/Zr atomic ratio                                  | 0.009 | 0.154        | 0.213      |

Table 2. Silver XPS and Auger signals [9].

\* the percentage contribution is shown in parentheses.

With the addition of O, the binding energy between the propene and the metal surface increased 0.1 eV from -0.77 eV to -0.87 eV. The slight increase of C1=C2 bond length, the decrease in distance between the propene molecule and the surface (0.08 Å) and the increase in the adsorption energy are evidence of the strengthened propene–surface interaction, and, in the presence of oxygen surface atoms, the system was even more capable of activating the double bond. These results agreed with those reported by Huang and White [18] who, through O<sub>2</sub>-TPD and RAIRS studies, demonstrated that at low O coverages, propene was adsorbed onto the surface of Ag(111) preferentially through its  $\pi$  system. This adsorption occurred on a Ag atom with a slight inclination of the plane of the molecule concerning the Ag surface. Probably, the presence of a surface oxygen atom generates Ag atoms deficient in electrons, and, due to this, the  $\pi$  system of the propene interacts more strongly with the surface.

Both for propane and propene combustion, the silver surface, in addition to presenting lattice oxygen, could dissociatively adsorb  $O_2$ , as was previously reported [48,49]. The adsorption can occur in adjacent surface sites, to favour a subsequent interaction between the adsorbed species. The ability of the Ag surface to selectively chemisorb propene would favour the formation of reaction intermediates, which could later lead to the formation of CO<sub>2</sub>. Garetto et al. proposed a similar mechanism for the propane combustion reaction on Pt-supported catalysts [50].

### 2.3. Electronic Structure Studies

Figure 4 shows the total and projected DOS curves of propane and propene, free and adsorbed, on a Ag surface, and on a Ag surface with an O atom. In all cases, the Fermi level is at zero energy. As can be seen in the Figure 4a, the PDOS of propane adsorbed on a Ag surface has virtually no drift with respect to DOS free propane. This is consistent with a very weak interaction between the propane and the Ag surface atoms, which is in agreement with the adsorption energy results. However, in Figure 4b, we can see that the adsorbed propene PDOS drifted to a lower energy than the free propene DOS. This shift to lower energies was due to an increase in the interaction between the propene and the Ag surface. Particularly, when the Ag surface was present, an O atom near the adsorption site increased the shift to a lower energy. These results indicate that the presence of superficial O produces a greater stabilization of the adsorbed propene.

The results of the theoretical calculations indicate that the greater interaction of propene with the metallic surface, the energies of the order of chemisorption, the lower distances between the molecule and the surface, the increase in the C1–C2 bond length, and the presence of oxygen surface atoms are essential for bond activation in a possible reaction. Therefore, on a surface with higher silver content, there exists a greater possibility of interaction between the propene molecules that come from the gas phase and the catalyst. This interaction is not favoured when the reactant is propane; therefore, its poor activity does not depend on metallic charge.



**Figure 4.** (a) DOS curves of free propane and projected DOS of adsorbed propane on Ag; (b) DOS curves of free propene and projected DOS of adsorbed propene on Ag and on Ag with a surface O atom.

## 3. Experimental

Ab initio calculations implementing the density functional theory (DFT) with plane waves were performed using Quantum Espresso software [51,52]. An exchange and correlation functional with density gradient correction PBESOL [53] and pseudopotential type PAW (projector-augmented wave) [54] were used. For all calculations, whether for bulk, surface (slab) or for free molecules in a vacuum, the cutoff kinetic energy for plane waves and the charge density used in the calculations was 30 Ry and 120 Ry, respectively. At low to moderate pressures, molecules may be treated as isolated, non-interacting species in vacuum, thus facilitating the theoretical modelling. Many cases of studies of molecules adsorbed on metals have been studied using this approximation [37,55–60]. The convergence criterion used for the total energy was  $<10^{-4}$  Ry, and for the atomic forces, it was  $<10^{-3}$  Ry/ua. A 4  $\times$  4 Ag(111) supercell and a depth of three layers were used for the surface calculations, as can be seen in Figure 5. The spacing on the Z-axis of the supercell was around 20 Å of vacuum between one surface and the other. These dimensions of the supercell allowed us to avoid the effects of interactions with near neighbours in any dimension. During the development of the surface optimisation calculations, the positions of the Ag atoms of the two innermost layers were kept frozen, while the atoms of the most superficial layer were allowed to relax freely. In the case of the propane and propene adsorption calculations, the two internal layers were kept frozen and the relaxation of the Ag surface layer and all the atoms of the molecules and/or atoms to be adsorbed were allowed to relax. A  $3 \times 3 \times 1$  grid of k-points was used in the reciprocal space using the Monkhorst–Pack method [61]. For the adsorption studies of the molecules on the surface, two adsorption sites of high symmetry were analysed "top" and "bridge", as can be seen in Figure 3. Four positions were analysed both for the case of propene and for propane on each site. All initial geometry can be seen in Figures S1 and S2 in the Supplementary Materials. The adsorption of propene in the presence of adsorbed oxygen at a nearby site was also studied. In these cases, only the "top" site that was presented the lower adsorption energy was analysed. Two initial geometries for propene adsorption on the Ag surface with a nearby O adatom can be seen in Figure S3.



Figure 5. Side and top view of the Ag(111) supercell used for the DFT model.

The adsorption energy for each species was calculated using Equation (1), where  $E_{ads}$  is the adsorption energy for each adsorbed molecule,  $E_{molec+surf}$  is the total electronic energy of the molecule system adsorbed onto the surface,  $E_{surf}$  is the total electronic energy of the metallic surface, and  $E_{molec}$  is the energy of each of the free molecules in a vacuum.

$$E_{ads} = E_{(molec+surf)} - \left(E_{molec} + E_{surf}\right) \tag{1}$$

In order to comprise the interaction between both hydrocarbons and the Ag surfaces we calculated electronic properties such as the density of states (DOS) and atom projected density of states (PDOS) for the converged systems. A Monkhorst Pack mesh of size  $9 \times 9 \times 1$  was used to perform NSCF and DOS calculations.

#### 4. Conclusions

From the molecular modelling studies using DFT calculations, it was possible to explain the difference in the behaviour of the Ag catalysts supported on  $ZrO_2$  for both reagents in the catalytic combustion reaction.

In the case of the catalytic combustion reaction of propene, the increase in the activity of the catalysts can be explained as a function of their metal charge because the determining step of the reaction rate is the breaking of the C1=C2 bond; for this, the propene needs to be adsorbed onto the Ag nanoparticles that activate and weaken this double bond.

On the other hand, the low adsorption energy calculated for propane suggest weak interaction energies consistent with physisorption and the null deformation or activation of the C1–C2 bond. This fact explains the low dependence of the catalytic activity concerning the Ag metallic charge.

**Supplementary Materials:** The following supporting information can be downloaded at https: //www.mdpi.com/article/10.3390/catal13071068/s1: Figure S1: initial geometries for optimization calculations of propane adsorption over Ag(111), Figure S2: initial geometries for optimization calculations of propene adsorption over Ag(111), and Figure S3: initial geometries for optimization calculations of propene adsorption over Ag(111) with a O adatom.

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