

Pressure dependent line intensity and continuum absorption for pure CO₂: experimental results

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Knowledge for Tomorrow



Introduction

- Radiative transfer models: Line intensities are pressure-independent
 - Intensity decrease with increasing pressure known for HF in Xe 2%/atm [Kouzov 2000] and HCl in Ar 1%/atm [Boulet 2004]
 - Recent confirmation by Tran, 2023, pure HCl 3%/atm, HCl in CO₂ 3%/atm, HCl in air 0.8% - no intensity decrease for HCl in He
 - CO in N₂ only 0.3%/atm, no effect for CO in He [Reed 2023]
 - Strong rotational quantum number dependence, largest decrease for low J
 - Confirmation of intensity decrease by re-quantized Classical Molecular Dynamics Simulations (rCMDS)
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- Is there any intensity decrease for the atmospheric relevant molecule CO₂?
 - If yes, how does this affect the CO₂ retrieval?
-
- Experimentally „easy“ situation: pure CO₂



CO₂ 1.6 μm range measurement conditions

| | |
|---------------------------------|---|
| Source | Halogen lamp |
| Spectrometer | Bruker IFS 125 HR |
| Cell | Multireflection, 80 cm base length |
| Optical filter | 1.5 μm high-pass |
| Detector | Internal InGaAs, cut-on 5800 cm ⁻¹ |
| Maximum optical path difference | 100 cm |

| # | p _{CO2} (mbar) | p _{CO2,equiv} (mbar) | l(cm) | T(K) | t _{meas} (min) | SNR _{RMS} |
|----|-------------------------|-------------------------------|--------------|------------|-------------------------|--------------------|
| 1 | 10.0002(62) | 10.0007 | 1456.40(29) | 294.23(10) | 880 | 14000 |
| 2 | 30.115(20) | 30.119 | 1456.40(29) | 294.23(10) | 82 | 4700 |
| 3 | 75.227(24) | 75.256 | 1456.40(29) | 294.23(10) | 82 | 4900 |
| 4 | 151.443(24) | 151.561 | 1456.40(29) | 294.22(10) | 82 | 5000 |
| 5 | 298.696(24) | 299.158 | 1456.40(29) | 294.22(10) | 82 | 4800 |
| 6 | 503.693(40) | 505.011 | 1456.40(29) | 294.23(10) | 82 | 4900 |
| 7 | 749.742(60) | 752.670 | 1456.40(29) | 294.23(10) | 82 | 4900 |
| 8 | 982.351(79) | 987.390 | 1456.40(29) | 294.23(10) | 82 | 4900 |
| 9 | 10.0052(62) | | 11695.92(98) | 294.23(10) | 1017 | 14000 |
| 10 | 100.721(24) | | 11695.92(98) | 294.23(10) | 82 | 4000 |

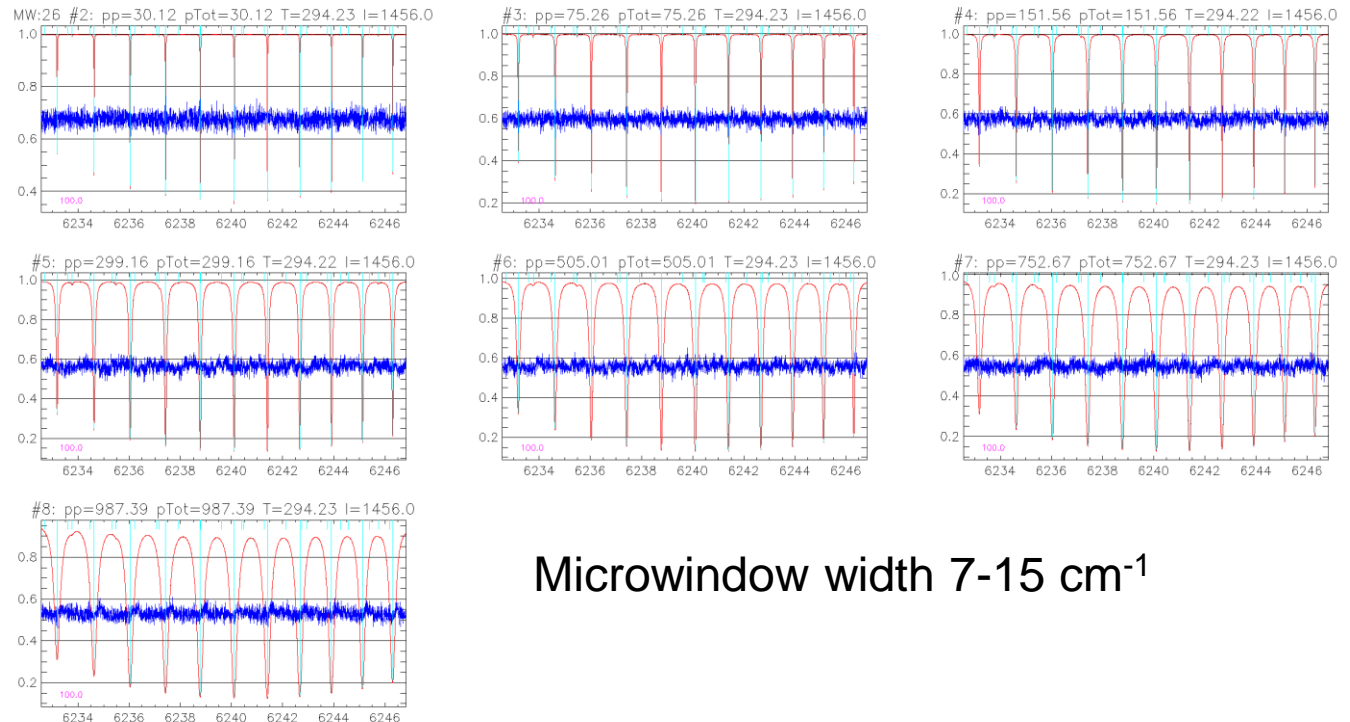
| # | p _{CO2} (mbar) | p _{CO2,equiv} (mbar) | l (cm) | T (K) | T _{fit} (K) | Inhom (%) | t _{meas} (min) | SNR _{RMS} |
|----|----------------------------|----------------------------------|--------------|------------|-------------------------|--------------|----------------------------|--------------------|
| 11 | 9.9989(62) | 9.9989 | 1456.33 (29) | 210.25(10) | 210.03(10) | 0 | 880 | 15000 |
| 12 | 518.928(42) | 522.681 | 1456.33 (29) | 210.26(10) | 211.75(30) | 2.1 | 54 | 3800 |
| 13 | 749.619(60) | 757.409 | 1456.33 (29) | 209.99(10) | 212.36(30) | 3.2 | 54 | 4000 |
| 14 | 998.961(80) | 1012.725 | 1456.33 (29) | 210.32(10) | 212.95(30) | 3.6 | 54 | 3800 |

Multispectrum fit

- Line model: Hartmann-Tran + Rosenkranz line mixing
- Quadratic baseline
- Consecutive fit: Ambient temperature, 212 K
- Depletion parameter: $S(p) = S(p=0) * [1 - d_{self} * p(atm)]$

Example of microwindow with ambient temperature spectra

| Parameter | # of lines |
|--------------------|------------|
| σ | 1178 |
| S | 1169 |
| $d_{self,294K}$ | 202 |
| $\gamma_{0,self}$ | 1193 |
| $\gamma_{2,self}$ | 346 |
| v_{vc} | 62 |
| $Y_{self,294K}$ | 255 |
| $\delta_{0,self}$ | 1198 |
| $\delta_{2,self}$ | 80 |
| $d_{self,212K}$ | 194 |
| n_{self} | 632 |
| $n_{\gamma2,self}$ | 113 |
| $Y_{self,212K}$ | 298 |
| $T\delta_{0,self}$ | 234 |

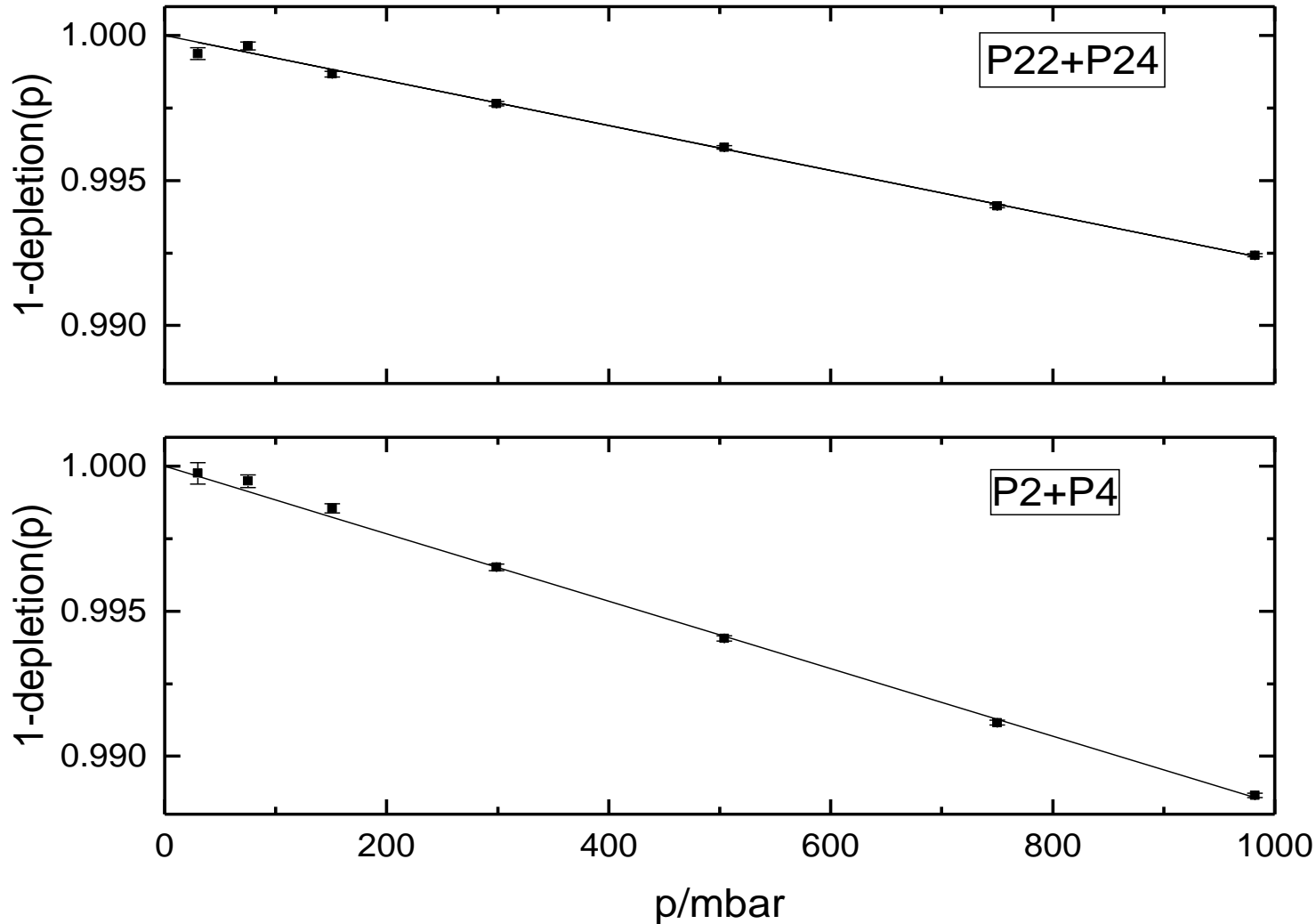


Microwindow width 7-15 cm^{-1}

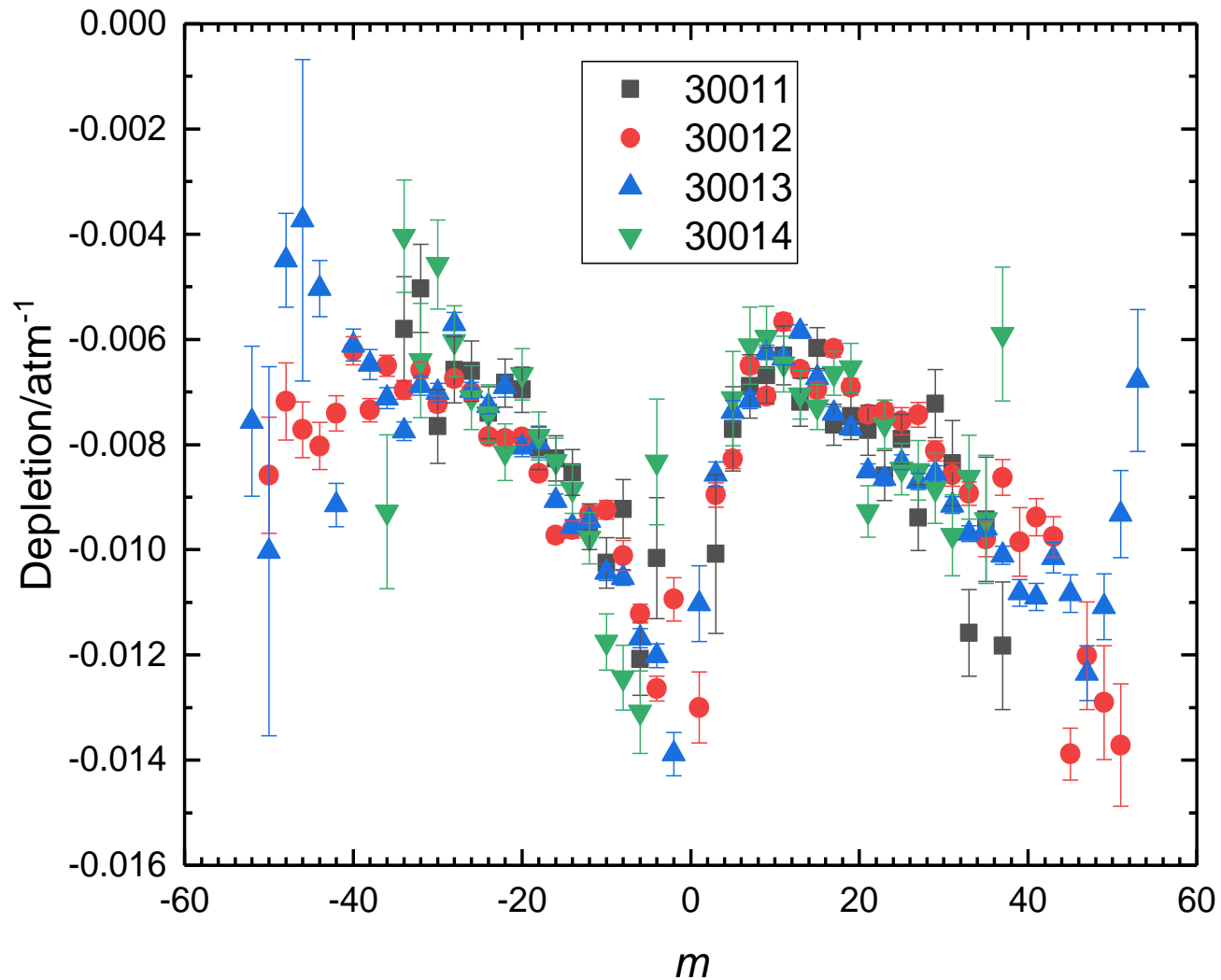


Linearity of intensity depletion vs. Pressure

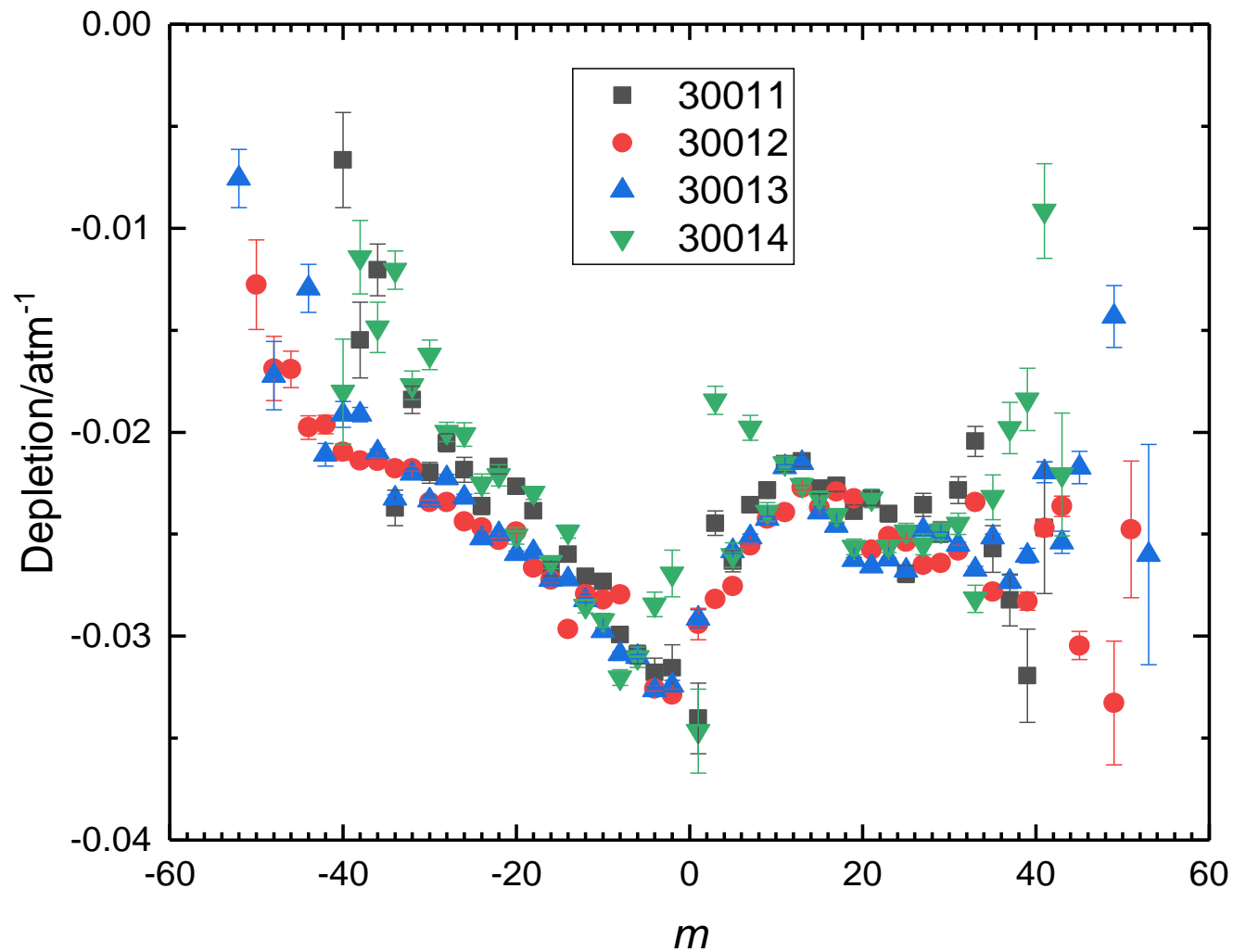
Symbols: depletion for individual measurements, line $1+d_{\text{self}} \cdot P$



m-dependence of depletion, d_{self} , at ambient temperature

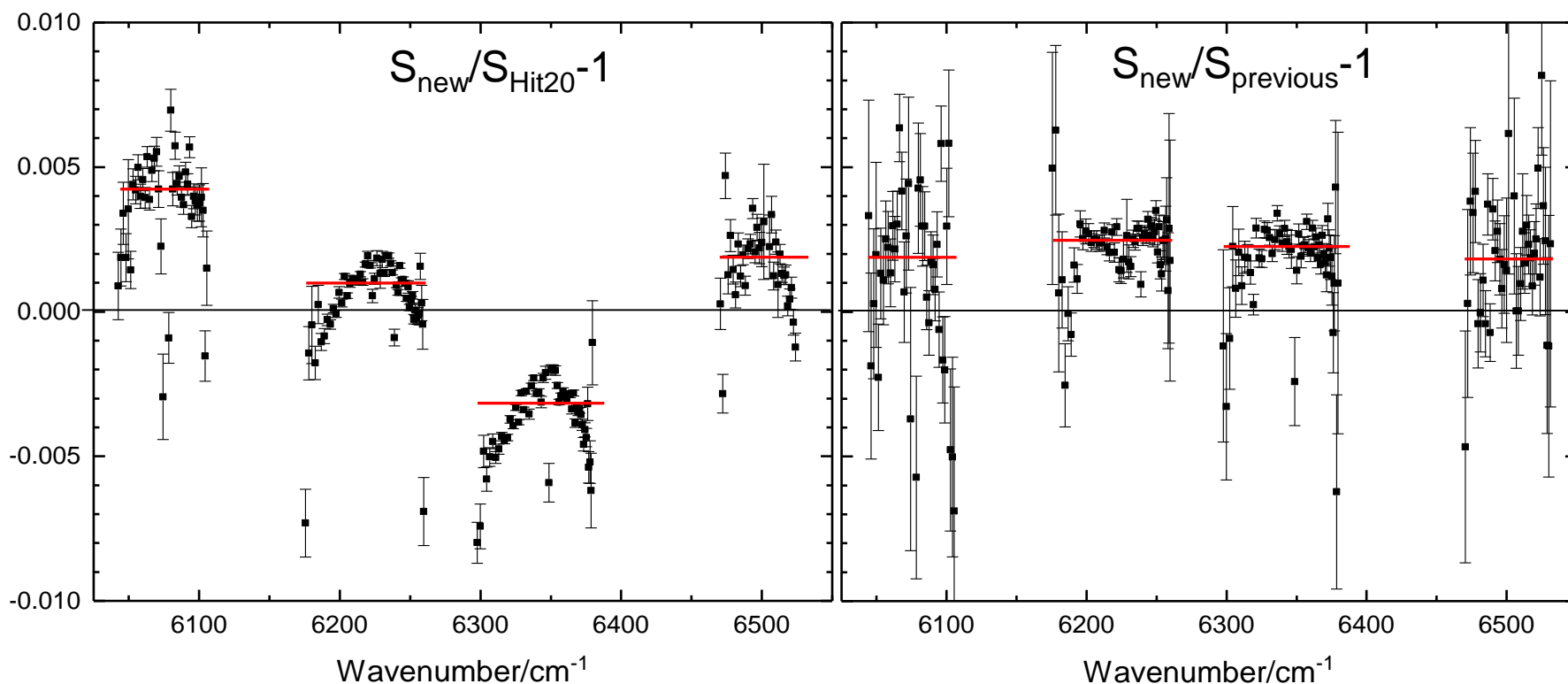


m-dependence of depletion, d_{self} , at 212 K



Improved line intensities: Systematic uncertainty <0.06%

- Previous work: Birk et al., “High accuracy CO₂ Fourier transform measurements in the range 6000–7000 cm⁻¹”, JQSRT 2021, systematic uncertainty 0.15%
- New intensities 0.2% larger than previous
- m-dependent differences to HITRAN20 spanning 0.4%

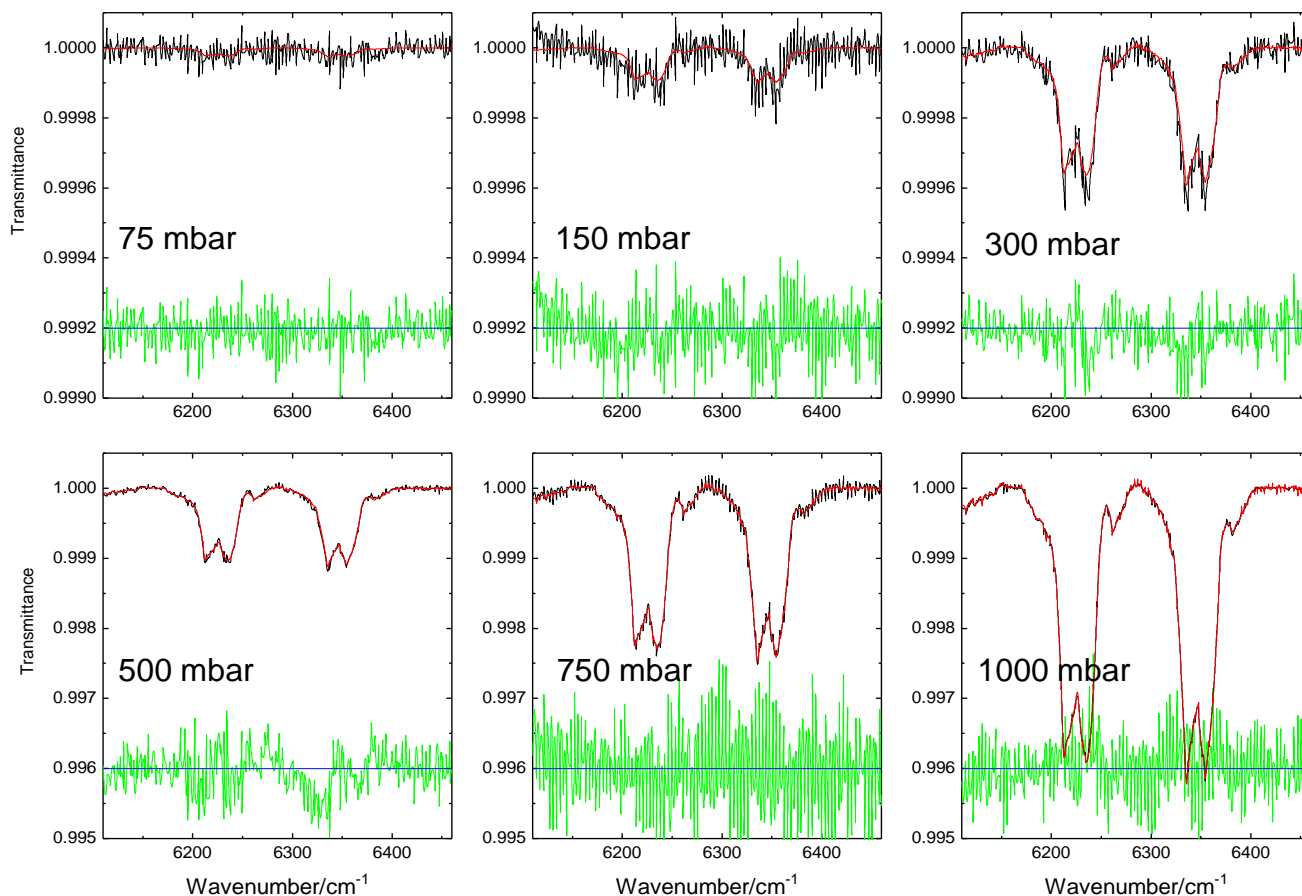


Fit of in-band self continuum

- From fitted baselines of multispectrum fit, spectra cut in 3 cm^{-1} wide microwindows (method see Birk et al., „3 μm water vapor self- and foreign-continuum: New method for determination and new insights into the self-continuum”, JQSRT 2020).
- Advantage: line parameters and continuum from same spectra

Observed and calculated baselines from fitted continuum, 294 K.

Green: (obs-calc)x2 (upper graphs), x10 (lower graphs)



Depletion, continuum, and 2nd virial coefficient

- Striking agreement for both temperatures and both bands between
 - ☞ intensity-weighted depletion,
 - ☞ continuum area at 1 atm divided by ΣS
 - ☞ depletion predicted from 2nd virial coefficient – fraction of monomers in pairs
- Depleted intensity is transferred to continuum – total band intensity pressure-invariant

| | 294 K | | 212 K | |
|---|----------------|----------------|----------------|----------------|
| | 30012 | 30013 | 30012 | 30013 |
| Intensity-weighted depletion [atm ⁻¹] | 0.00948 | 0.00967 | 0.02751 | 0.02832 |
| Continuum area/ ΣS | 0.01018 | 0.00978 | 0.02894 | 0.02747 |
| Real gas pressure correction | 1.00525 | 1.00525 | 1.01423 | 1.01423 |
| Predicted depletion from pressure correction | 0.01045 | 0.01045 | 0.02806 | 0.02806 |



Continuum fitted from depleted intensities and pressure independent super-Lorentzians including line mixing

- Agreement indicates that only small contribution of bound dimers may be present – bound dimers: different band shapes + intensities

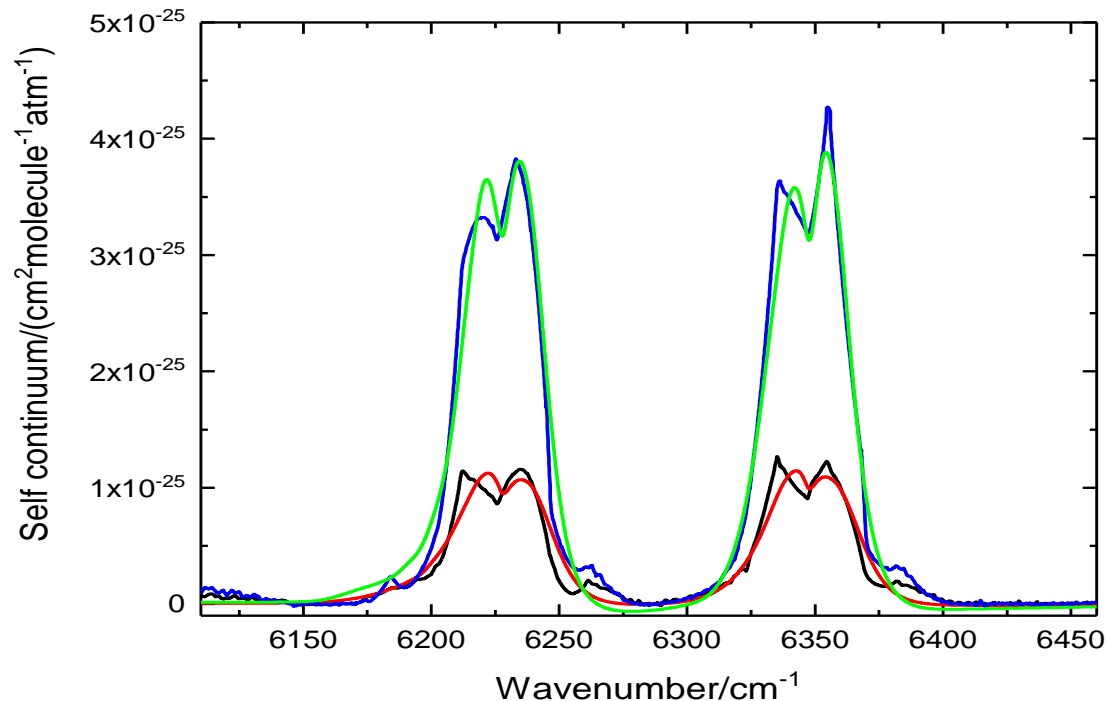
Fitted and measured continua

212 K measured

212 K calculated

294 K measured

294 K calculated



| Fitted parameter | 294 K | 212 K |
|---------------------------------|-----------------------|-----------------------|
| Global depletion scaling | 1.035 | 1.041 |
| Lorentz width @ m=0 | 1.33 cm ⁻¹ | 1.90 cm ⁻¹ |
| Lorentz width increase/ m | 0.24 cm ⁻¹ | 0.18 cm ⁻¹ |
| Rosenkranz parameter increase/m | -0.00294 | -0.00323 |



2nd virial coefficient

- Fraction of monomers in pairs = fraction of depleted intensity
- These pairs undergo non-Markovian collisions resulting in super-Lorentzians – Theory see poster Ha Tran et al., „Pressure dependent line intensity and continuum absorption for pure CO₂: predictions by requantized molecular dynamics simulations”, Poster O34
- Discrepancy to continuum theory [Serov 2017] where super-Lorentzians were regarded as characteristic of monomers only, not affecting the 2nd virial coefficient.
- 2nd virial coefficient $B(T)$ can be calculated from intermolecular potential [e.g. Bock et al., 2000]:

$$B(T) = \frac{N_A}{2} \int \left\langle 1 - e^{-\beta V} \left[1 + \frac{\beta^2}{12} (H_0 V) \right] \right\rangle_{\omega_A \omega_B} dR,$$

- Both, the real gas correction as well as the non-Markovian collisions, are linked to the intermolecular potential V
- Potential minimum required for real gas pressure reduction as well as intensity depletion
- Notable fraction of bound dimers when potential minimum $>kT$ (example H₂O self continuum)
- Whether continuum areas (in absence of bound complexes) and intensity depletions can be calculated from 2nd virial coefficient needs to be investigated for other pure gases and gas mixtures



Impact of depletion and continuum for remote sensing

- Example CO2M Mission requirements:
global bias from spectroscopy <0.5%, differential error <0.1%, p-p residuals
1.6 μm 0.063%, 2 μm 0.077%
- Retrieval simulations applying simplified modelled satellite observations
 - ☞ Larger impact of continuum
 - ☞ Continuum impact larger for opaque 2 μm band
 - ☞ Requirements not met in **several cases**

Global bias and residuals

| | 1.6 μm | | 2 μm | |
|----------------|-----------------------------|----------------|-----------------------------|----------------|
| Impact of | CO ₂ col. dev./% | p-p residual/% | CO ₂ col. dev./% | p-p residual/% |
| depletion | -0.47 | 0.036 | -0.46 | 0.143 |
| depletion+cont | +0.38 | 0.195 | +2.76 | 2.101 |
| cont | +0.85 | 0.187 | +3.22 | 2.046 |

Differential errors

| | 1.6 μm | | 2 μm | |
|----------------|-------------------|------------------|-----------------|------------------|
| Impact of | TRO-SAW/% | TRO(0 km-2 km)/% | TRO-SAW/% | TRO(0 km-2 km)/% |
| depletion | 0.247 | -0.021 | 0.314 | -0.006 |
| depletion+cont | -0.108 | 0.025 | -0.878 | -0.094 |
| cont | -0.357 | 0.045 | -1.197 | -0.087 |



Impact of depletion and continuum for remote sensing

- Example CO2M Mission requirements:
global bias from spectroscopy <0.5%, differential error <0.1%, p-p residuals 1.6 μm 0.063%, 2 μm 0.077%
- Retrieval simulations applying simplified modelled satellite observations
 - ☞ Air continuum and depletion deduced from pure CO2 results + 2nd virial coefficients
 - ☞ Larger impact of continuum
 - ☞ Continuum impact larger for opaque 2 μm band
 - ☞ Requirements not met in **several cases**

Bias for tropical atmosphere and residuals

| | 1.6 μm | | 2 μm | |
|----------------|-----------------------------|----------------|-----------------------------|----------------|
| Impact of | CO ₂ col. dev./% | p-p residual/% | CO ₂ col. dev./% | p-p residual/% |
| depletion | -0.17 | 0.019 | -0.17 | 0.036 |
| depletion+cont | +0.29 | 0.100 | +1.48 | 1.078 |
| cont | +0.46 | 0.097 | +1.65 | 1.086 |

Differential errors

| | 1.6 μm | | 2 μm | |
|----------------|-------------------|------------------|-----------------|------------------|
| Impact of | TRO-SAW/% | TRO(0 km-2 km)/% | TRO-SAW/% | TRO(0 km-2 km)/% |
| depletion | 0.128 | -0.001 | 0.157 | -0.006 |
| depletion+cont | -0.054 | 0.032 | -0.465 | -0.037 |
| cont | -0.183 | 0.033 | -0.623 | -0.043 |



Conclusion

- High accuracy pure CO₂ measurements for 294 K and 212 K, pressures up to 1 atm
- Multispectrum fitting of microwindows applying Hartmann-Tran profile with 1st order Rosenkranz line mixing
- Improved spectroscopic database, line intensity accuracy better than 0.06%
- Intensity depletion detected, ca. 1%/atm at 294 K, 3%/atm at 212 K
- Continua determined, areas in agreement with depleted intensity at both temperatures
- Continua could be approximated as sum of pressure-independent super-Lorentzian+line mixing contributions applying depleted intensities
- Amount of monomer pairs calculated from real gas pressure correction applying 2nd virial coefficient in agreement with average intensity depletion at both temperatures
- Continua theory stating that super-Lorentzian contributions are a characteristic of monomers not linked to the 2nd virial coefficient may have to be reconsidered
- Continuum and depletion were found to have significant impact on satellite-based CO₂ retrievals
- Further investigations of other pure gases and mixtures regarding intensity depletion, continua, and 2nd virial coefficients are needed

