# Efficient Functional Encryption and Proxy Re-cryptography for Secure Public Cloud Data Sharing

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*Abstract*—with the rapid development in cloud computing, public cloud data sharing concept has been extending and expanding by many scholars. In 2014, Liang et al. proposed a general notion for proxy re-encryption (PRE), which is called deterministic finite automata-based functional PRE (DFA-based FPRE). Motivated by the issues of efficiency and flexibility associated with this new primitive, we propose outsourcing decryption scheme to increase the flexibility of users by delegating their decryption rights to the semi trusted proxy. Through analysis we showed that our scheme is provably secure and efficient.

Keywords-Deterministic Finite Automata (DFA), Proxy re-encryption (PRE), Outsourcing Decryption, Cloud Computing.

# I. INTRODUCTION

With the rapid development in availability of cloud services, the techniques for securely outsourcing the prohibitively expensive computation to untrust servers are brings more attention in the scientific community. In the outsourcing computation paradigm, the resource-constrained devices can enjoy the unlimited computation resources in a pay-per-use manner, which allows users to concentrate on their core business issues rather than incurring substantial hardware, software, or personal costs. However, owners still have to remain cautious to protect their data from being pirated [1]. The cloud service provider is semi-trusted [2]. In this sense, the semi-trusted cloud service provider follows the normal flow of the protocol in the system. For instance, during the interaction with the users, a CSP may collect user's personal information and consumption profiles, which inspires a serious security concern for cloud user. Proxy re-encryption (PRE) technique [3] is devised to prevent the CSP from accessing the data in semi-trusted cloud environment.

Functional Encryption (FE) is a useful cryptographic primitive that guarantees the confidentiality of data and also enhances the flexibility of data sharing as stated in [4] and [5]. Recently (Kaitai Liang et al., 2014 [6]) introduced a general notion for proxy re-encryption (PRE), which is called deterministic finite automata-based functional PRE (DFA-based FPRE). In their scheme, a message is

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encrypted in a ciphertext associated with an arbitrary length index string w, and a decryptor is legitimate if and only if a DFA associated with his/her secret key accepts the string w. Furthermore, the above encryption is allowed to be transformed to another ciphertext associated with a new string by a semi trusted proxy to whom a re-encryption key is given. However, the proxy cannot gain access to the underlying plaintext. In addition, their scheme having proved to be secure against CCA in the standard model. In this paper, based on the new primitive introduced by Liang et al., we propose outsourcing decryption scheme to increase the flexibility of users by delegating their decryption rights to the semi trusted proxy. Our scheme can be proved as fully chosen-ciphertext secure in the standard model.

The rest of this paper is organized as follows. In next Section the preliminaries required in this paper are presented. Our scheme based on DFA-based FPRE scheme is presented in Section [3]. Analysis of our scheme is discussed in Section [4]. Finally, the conclusion and future work are introduced in Section [5].

### II. PRELIMINARIES

Our scheme relies on a DFA-based functional proxy re-encryption scheme. We will briefly introduce the DFA-based functional proxy re-encryption scheme and the groups underlying our encryption scheme.

# A. Composite Order Bilinear Groups

Let  $\mathbb{G}$  and  $\mathbb{G}_T$  be multiplicative cyclic groups of same order  $N = P_1 P_2 P_3$  (where  $P_1, P_2, P_3$  are distinct primes). We call a map  $e: \mathbb{G} \times \mathbb{G} \to \mathbb{G}_T$  bilinear if it should satisfy the following properties [7]:

Bilinear.  $e(g^a, h^b) = e(g, h)^{ab}, \forall g, h \in \mathbb{G}$ 

And  $\forall a, b \in \mathbb{Z}_N^*$ ; and Non-degenerate. There exists  $g \in \mathbb{G}$  such that e(g, g) is a generator of  $\mathbb{G}_T$ .

We denote by  $G_{P_1}$ ,  $G_{P_2}$  and  $G_{P_3}$  the subgroups of  $\mathbb{G}$  of respective orders  $P_1$ ,  $P_2$  and  $P_3$ .

# B. Complexity Assumptions

Definition 1 (The Source Group l-Expanded Bilinear Diffie-Hellman Exponent (l-Expanded BDHE) Assumption in a Subgroup [6]).

Given a group generator g and a positive integer l, we define the following distribution:

$$N = (P_1 P_2 P_3, \mathbb{G}, \mathbb{G}_T, e) \leftarrow \mathcal{G}, g_1 \leftarrow \mathbb{G}_{P_1},$$

$$g_2 \leftarrow \mathbb{G}_{P_2}, g_3 \leftarrow \mathbb{G}_{P_3}, a, b, d, m, n, c_0, \dots, c_{l+1} \leftarrow \mathbb{Z}_N,$$

$$D = (N, \mathbb{G}, \mathbb{G}_T, e, g_1, g_2, g_3, g_2^{a}, g_2^{b}, g_2^{ab/dx},$$

$$g_2^{b/dx}, g_2^{ab/x}, g_2^{n}),$$

$$\forall i \in [0, 2l+1], i \neq l+1, j \in$$

$$[0, l1]g_2^{a^{imn}}, g_2^{a^{ibmn}/c_jx},$$

$$N = (0, l+1) = (i = g_1^{id} = g_2^{a^{bc_i/2}}, g_2^{bc_i/2})$$

$$\begin{array}{l} \forall \ i \in [0, l+1] g_2^{\circ i}, g_2^{\circ u}, g_2^{\circ u$$

The advantage of an algorithm  $\mathcal{A}$  in breaking this assumption is  $Adv_{\mathcal{A}}^{l-BDHE}(1^n) = |\Pr[\mathcal{A}(D,T_0) = 1] \Pr[\mathcal{A}(D,T_1) = 1]|$ . We say that  $\mathcal{A}$  satisfies the l-Expanded BDHE Assumption if  $Adv_{\mathcal{A}}^{l-BDHE}(1^n)$  is negligible for any PPT algorithm  $\mathcal{A}$ .

Definition 2 (The Source Group Modified q Bilinear Diffie-Hellman Exponent (q-BDHE) Assumption in a Subgroup [6]).

Given a group generator q, we define the following distribution:

$$N = (P_1 P_2 P_3, \mathbb{G}, \mathbb{G}_T, e) \leftarrow \mathcal{G}, \quad g_1 \leftarrow \mathbb{G}_{P_1}, \quad g_2 \leftarrow \mathbb{G}_{P_2}, \quad g_3$$

$$\stackrel{R}{\leftarrow} \mathbb{G}_{P_3}, \quad c, a, e, f \leftarrow \mathbb{Z}_N,$$

$$D = (N, \mathbb{G}, \mathbb{G}_T, e, g, g_2, g_3, g_2^{e}, g_2^{a}, g_2^{eaf}, g_2^{c+f/c},$$

 $g_2^{c^2}, \ldots, g_2^{c^q}, g_2^{1/ac^q}, T_0 = g_2^{aec^{q+1}}, T_1 \stackrel{\kappa}{\leftarrow} \mathbb{G}_{P_2}.$ 

The advantage of an algorithm  $\mathcal{A}$  in breaking this assumption is  $Adv_{\mathcal{A}}^{q-BDHE}(1^n) = |\Pr[\mathcal{A}(D,T_0) = 1] \Pr[\mathcal{A}(D,T_1)=1]|$ . We say that g satisfies the Source Group Modified q-BDHE Assumption if  $Adv_{\mathcal{A}}^{q-BDHE}(1^n)$ is negligible for any PPT algorithm  $\mathcal{A}$ .

A DFA-Based Functional Proxy Re-Encryption Scheme

For more details we refer the reader to [5] for the definition of DFA and DFA-based FE. The DFA-based functional proxy re-encryption scheme consists of the following seven algorithms [6]:

 $(PP, MSK) \leftarrow Setup(1^n, \Sigma)$  : The system setup algorithm takes a security parameter n and the description of a finite alphabet  $\Sigma$  as input. It outputs the public parameters *PP* and a master key *MSK*, where  $n \in N$ . Here, we note that *PP* implicitly includes  $\Sigma$ .  $SK_M \leftarrow$  $k. Gen(MSK, M = (Q, \tau, g_0, F))$ : The key generation algorithm takes the master key MSK and a DFA description M as input. It outputs a private key  $SK_M$ , where Q is a set of states,  $\tau$  is a set of transitions,  $g_0 \in$ Q is a start state and  $F \subseteq Q$  is a set of accept states.

 $RK_{M \to w} \leftarrow ReKeyGen(SK_M, w)$ : This algorithm takes  $SK_M$  for a DFA description M and an arbitrary length string  $w \in \sigma$  as input. It outputs a re-encryption key  $RK_{M \to w}$ . Using the re-encryption key any ciphertext under a string w' (in which ACCEPT(M, w')), it can

converted to another ciphertext under w.

 $CT \leftarrow DFA. E(PP, w, m)$ : The encryption algorithm takes the public parameters *PP*, a message m and a  $w \in \sigma$ as input. It outputs the ciphertext CT under w.

 $CT^R \leftarrow DFA. E(PP, w, m)$ : The encryption algorithm takes  $RK_{M\to w}$  and CT (under w'). If ACCEPT(M, w'), it outputs the ciphertext  $CT^R$  under w.

 $\tilde{m}/L \leftarrow DFA.D(SK_M, CT)$ : The decryption algorithm takes a secret key  $SK_M$  and ciphertext CT (under w) as input. The decryption can be done if ACCEPT(M, w), then it outputs a message m; otherwise, outputs an error symbol  $\perp$ .

 $m/ \vdash CFA. D_R(SK_M, CT^R)$ : The decryption algorithm takes a secret key  $SK_M$  and ciphertext  $CT^R$  (under w) as input. The decryption can be done if ACCEPT(M, w), then it outputs a message m; otherwise, outputs an error symbol  $\perp$ .

## **III. PROPOSED SCHEME**

### A. Intuition

- To tackle the focusing issue on efficiency, our proposed construction operates as follows: In the key generation phase, the secret key  $SK_M$  is divided in to two parts denoted as  $SK_M = (\{M, \varepsilon, \Omega\}, DK)$  for each user.
- In transformation phase, the user first sends his partial decryption key DK to the semi trusted proxy, which is part of his private key. Then semi trusted proxy transforms the ciphertext  $CT_m$  to  $CT_{m'}$  and finally sends  $CT_{m'}$  back to the user.
- In decryption phase, upon receiving the  $CT_{m'}$  value the user can retrieve the plain massage m with only one exponential operation instead of 12 pairing operations. Since the computation of bilinear pairings has been considered the prohibitively expensive operation [8] [9], therefore our scheme is considered as more efficient.

### B. Concrete Construction

In this section, we will explain a detailed construction for the proposed scheme as follows:

#### System setup 1)

Setup $(1^n, \Sigma)$  The setup algorithm selects random group elements  $g, g_0, z, h_0 \in \mathbb{G}_{P_1}$  and randomly chooses an exponents  $\alpha$ , k, a, b,  $\alpha_{End}$ ,  $\alpha_{Start} \in \mathbb{Z}_N^*$ . Then set  $H_{Start} = g^{\alpha_{Start}}$ ,  $H_{End} = g^{\alpha_{End}}$  and  $H_k = g^k$ . In addition,  $\forall \sigma \in \Sigma$ it chooses random  $\alpha_{\sigma} \in \mathbb{Z}_{N}^{*}$  and set $H_{\sigma} = g^{\alpha\sigma}$ . After that it choose a one-time symmetric encryption scheme Sym =(sym. Enc, sym. Dec), a one-time signature scheme Ots and two target collision resistant (TCR) hash functions namely  $H_1$  and  $H_2$ , where  $H_1: \mathbb{G}_T \to \mathbb{Z}_N^*$  and  $H_2: \mathbb{G}_T \to$  $\{0,1\}^{poly(n)}$ . Finally, the public authority publishes the public parameters PP = $(e(g,g)^{\alpha}, g, g^{ab}, z, h_0, H_{Start}, H_{End}, H_k, \forall \sigma \in \Sigma H_{\sigma})$ 

Sym, Ots,  $H_1, H_2$  along with the description of the group **G** and the alphabet  $\Sigma$ , while the  $MSK = (g^{-\alpha}, X_3)$ , is kept

secretly. Here,  $X_3$  is a generator of  $\mathbb{G}_{P_3}$ .

2) Kev Generation

k. Gen(MSK, 
$$M = (Q, \tau, g_0, F)$$

The key generation algorithm takes the master key MSK and a DFA description M as input. It outputs a private key  $SK_M$ , where Q, is a set of states  $q_0, \ldots, q_{|Q|-1}, \tau$ is a set of transitions, for each transition  $t \in T$  is a triple  $(x, y, \sigma) \in Q \times Q \times \Sigma$ .  $q_0 \in Q$ , is a start state and  $F \subseteq Q$  is a set of accept states. The algorithm chooses random group elements  $D_0, D_1, \dots, D_{|Q|-1} \in \mathbb{G}_{P_1}$ , where  $D_i$ is associated with state  $q_i$ , for each transition  $t \in T$  it randomly selects  $r_t \in \mathbb{Z}_N^*$ , for all  $q_x \in F$  it randomly selects  $r_{End_x} \in \mathbb{Z}_N^*$ , and selects  $u \in \mathbb{Z}_N^*$ . It also randomly selects.

 $R_{Start_1}, R_{Start_2}, R_{Start_3}, R_{t,1}, R_{t,2}, R_{t,3}, R_{End_{x,1}}, R_{End_{x,2}} \in$ 

 $\mathbb{G}_{P_3}$ , it also selects randoms  $\varepsilon, \Omega \in \mathbb{G}_T$  and random  $r_{Start} \in$  $\mathbb{Z}_N^*$ . The algorithm computes the private key as follows.

Firstly it computes:

 $K_{Start_1} = D_0 \cdot (H_{Start})^{r_{Start}} \cdot R_{Start_1},$  $K_2 = g^{r_{Start}} \cdot R_{Start_2},$  $K_2 = g^u \cdot R_{Start_3}$ .

Secondly, for each transition  $t = (x, y, \sigma) \in \tau$  it computes:

 $\bar{K}_{t,1} = D_x^{-1} \cdot z^{r_t} \cdot R_{t,1} ,$  $K_{t,2} = g^{r_t} \cdot R_{t,2},$  $K_{t,3} = D_y \cdot (H_{\sigma})^{r_t} \cdot R_{t,3}.$ Thirdly, for all  $q_x \in F$  the algorithm sets:  $K_{End_{x,1}} = g^{-\alpha} \cdot D_x \cdot (H_{End} \cdot g^{ab})^{r_{End_x}} \cdot g^{ku} \cdot R_{End_{x,1}},$  $K_{End_{x,2}} = g^{r_{End_x}} \cdot R_{End_{x,2}}.$ 

Finally, generates the  $SK_M$ , and sends it to the authorized user in secure channel.  $SK_M$ , is denoted as:

 $SK_M = (\{M, \varepsilon, \Omega\}, DK)$ , where  $DK = (DK_1 =$  $\begin{aligned} &K_{M} = ((H_{1}, e, X_{2}), BK) \quad , \quad \text{where} \quad BK = (DK_{1} = EK_{1}), \\ &K_{start_{1}} = (DK_{1}, e, X_{2}), BK = K_{start_{2}} = (DK_{1}), \\ &T(DK_{t,1} = K_{t,1} = K_{t,1}), DK_{t,2} = K_{t,2} = K_{t,3} = K$ Re-encryption Key Generation *ReKeyGen(SK<sub>M</sub>, w)* 

To generate the re-encryption key  $RK_{M\to w}$  for authorized user this algorithm works as follows:

Firstly, selects random  $\beta^r \in \mathbb{Z}_N^*$  for all  $q_x \in F$ . Then compute  $RK_1 = K_{Start_1}^{H_1(\Omega)}$ ,  $RK_2 = K_{Start_2}^{H_1(\Omega)}$ ,  $RK_3 = K_{Start_3}^{H_1(\Omega)}$ , for all  $t \in \tau(RK_{t,1} = K_{t,1}^{H_1(\Omega)}, RK_{t,2} = K_{t,2}^{H_1(\Omega)}, RK_{t,3} = K_{t,3}^{H_1(\Omega)}$ ,

For all 
$$q_x \in F(RK_{End_{x,1}} = K_{End_{x,1}}^{H_1(\Omega)})$$
  
 $H_{End}^{\beta^r}, RK_{End_{x,2}} = K_{End_{x,2}}^{H_1(\Omega)} \cdot g^{\beta^r}).$ 

Finally, the  $RK_{M \to W} = (M, RK_1, RK_2, RK_3, RK_3)$  $t \in$  $\tau(RK_{t,1}, RK_{t,2}, RK_{t,3}, q_x \in F(RK_{End_{x,1}}, RK_{End_{x,2}}))$ 

Encryption DFA.E(PP, w, m)encryption The algorithm randomly selects  $\lambda_0, \lambda_1, ..., \lambda_l \in \mathbb{Z}_N^*$ , run  $(ssk, svk) \leftarrow key. Gen(1^n)$  and computes  $CT_m$  as:

First set:

 $C_m = m \cdot e(g,g)^{\alpha \cdot \lambda_l}, C_{Start_1} = C_{0,1} = g^{\lambda_0}, \ C_{Start_2} =$  $(H_{Start})^{\lambda_0}$ ,  $C_{Start_3} = (g_0^{svk}h_0)^{\lambda_0}$ , for i = 1 to l

set: 
$$C_{i,1} = g^{\lambda_i}, C_{i,2} = (h_{wi})^{\lambda_i} \cdot z^{\lambda_i - 1}$$
  
Finally, set:  
 $C_{End_1} = C_{l,1} = g^{\lambda_l}, C_{End_2} = (H_{End} \cdot g^{ab})^{\lambda_l}, C_{End_3}$   
 $= (H_k)^{\lambda_l}, C_{End_4}$   
 $= Sign(ssk, (w, C_m, C_{Start_1}, C_{Start_2}, C_{Start_3}, (C_{1,1}, C_{1,2}), ..., (C_{End_1}, C_{l,2}), C_{End_2}, C_{End_3})).$   
The ciphertext  $CT_m$  is:  
 $CT_m = (svk, w, C_m, C_{Start_1}, C_{Start_2}, C_{Start_3}, (C_{1,1}, C_{1,2}), ..., (C_{End_1}, C_{l,2}), C_{End_2}, C_{End_3}, C_{End_4})$   
Re-encryption  $ReEec(RK_{M \to w'}, CT_m)$   
The process in this phase represented as follows:

Check

 $verify(svk, (w, C_m, C_{Start_1}, C_{Start_2}, C_{Start_3}, (C_{1,1}, C_{1,2}), ...,$ =1 $(C_{End_1}, C_{l,2}), C_{End_2}, C_{End_3}))$ 

and  $e(C_{Start_1}, g_0^{svk}h_0) = e(g, C_{Start_3})$ , outputs "True" if valid and "False" otherwise. If the verification is hold then proceed.

The string  $w = w_1, ..., w_l$  is associated with the  $CT_m$ , and the DFA  $M = (Q, \tau, g_0, F)$  is associated with the user's re-encryption key  $RK_{M \to w'}$  where ACCEPT(M, w). There must exist a sequence of l + 1 states  $\mu_0, ..., \mu_l$  and ltransitions  $t_0, ..., t_l$  where  $\mu_0 = q_0$  and  $\mu_l \in F$ , we have  $t_i = (\mu_{i-1}, \mu_i, w_i) \in \tau$ . The key server re-encrypts  $CT_m$  as follows.

First computes 
$$\varphi_0 = e(C_{Start_1}, RK_1) \cdot e(C_{Start_2}, RK_2)^{-1} = e(g, D_0)^{\lambda_0 \cdot H_1(\Omega)}.$$

For 
$$i = 1$$
 to  $l$ , computes:  $\varphi_i = \varphi_{i-1} \cdot e(C_{(i-1)}, RK_{t_{i,1}})$ 

 $e(C_{i,2}, RK_{t_{i,2}})^{-1} \cdot e(C_{i,1}, RK_{t_{i,3}}) = e(g, D_{\mu_i})^{\lambda_i \cdot H_1(\Omega)}$ 

Whenever *M* accepts *w*, we have that  $\mu_l = q_x$  for some  $q_x \in F$ , and  $\varphi_l = e(g, D_x)^{\lambda_l \cdot H_1(\Omega)}$ .

 $\varphi_{End} = \varphi_l \cdot e(C_{End_{r,1}}, RK_{End_{r,1}}) \cdot$ Then sets  $e(C_{End_{x,2}}, RK_{End_{x,2}})^{-1} \cdot e(C_{End_{x,3}}, RK_3) =$ 

 $e(g, D_{\mu_i})^{\alpha \cdot \lambda_l \cdot H_1(\Omega)}$ 

Selects random  $\gamma \in \mathbb{G}_T$  and sets  $\pi_1 =$ sym.  $Enc(H_2(\gamma), A)$ , and  $\pi_2 = DFA. E(PP, w', \gamma)$ where  $A = (CT_m)||\varphi_{End})$ . Finally, the re-encrypted ciphertext  $CT_m^R = (\pi_1, \pi_2).$ 

Transform  $(DK, CT_m)$ 

The user sends his partial decryption key \$DK\$ to the semi trusted proxy for partial decryption, the semi trusted proxy works the following:

$$\begin{aligned} If \ verify(svk, (w, C_m, C_{Start_1}, C_{Start_2}, C_{Start_3}, (C_{1,1}, C_{1,2}), ... \\ (C_{End_1}, C_{1,2}), \ C_{End_2}, \ C_{End_3})) &= 1 \end{aligned}$$

And  $e(C_{Start_1}, g_0^{svk}h_0) = e(g, C_{Start_3})$ , outputs "True" if valid and "False" otherwise. If the verification is hold then proceed.

Then the semi trusted proxy computes  $CT_{m'}$  as follows:

$$\theta_0 = e(C_{Start_1}, DK_1) \cdot e(C_{Start_2}, DK_2)^{-1} = e(g, D_0)^{\lambda_0 \cdot H_1(\epsilon)}.$$

For 
$$i = 1$$
 to  $l$ , computes:  $\theta_i = \theta_{i-1} \cdot e(C_{(i-1)}, DK_{t_{i,1}})$ .

$$\begin{split} e(C_{i,2}, DK_{t_{i,2}})^{-1} \cdot e\Big(C_{i,1}, DK_{t_{i,3}}\Big) &= e(g, D_{\mu_i})^{\lambda_i \cdot H_1(\epsilon)} \\ \text{Whenever } M \text{ accepts } w, \text{ we have that } \mu_l = q_x \text{ for} \end{split}$$

some  $q_x \in F$  and  $\theta_l = e(g, D_x)^{\lambda_l \cdot H_1(\epsilon)}$ .

Finally compute: 
$$\theta_{End} = \theta_l \cdot e(C_{End_{x,1}}, DK_{End_{x,1}}) \cdot e(C_{End_{x,2}}, DK_{End_{x,2}})^{-1} \cdot e(C_{End_{x,2}}, DK_3) =$$

 $e(C_{End_{x,2}}, D\Lambda_{End_{x,2}}) \rightarrow e(C_{End_{x,3}}, D\Lambda_{3}) - e(g, D_{\mu_i})^{\alpha \cdot \lambda_l \cdot H_1(\epsilon)}$  and sends the message  $CT_{m'} = \theta_{End}$  to the user.

Dec  $(SK_m, CT_m)$ 

The user can retrieve m by simply computing:

$$m = \frac{C_m}{(CT_m)^2} = \theta_{End} + \frac{1}{(\epsilon)^{-1}}$$

 $Dec_R SK_m, CT_{m'}$ 

Firstly, the user can retrieve  $\gamma$  as follows:

$$\gamma = \frac{C_{\gamma}}{\{CT_{m'}\}^{H_1(\epsilon)^{-1}}}$$

We note that  $C_{\gamma} = \gamma \cdot e(g, g)^{\alpha \cdot \lambda_l}$ , since it encrypted using the DFA. E(PP, w, m) encryption algorithm.

Secondly, the user computes A as follows:

 $A \leftarrow sem. Dec(H_2(\gamma), \pi_1)$ , where  $A = (CT_m)||\varphi_{End})$ . Thirdly, computes Key as follows: Key =

 $\varphi_{End}^{H_1(\Omega)^{-1}}$ Fourthly, verifies:

 $verify(svk, (w, C_m, C_{Start_1}, C_{Start_2}, C_{Start_3}, (C_{1,1}, C_{1,2}), ...$ 

 $(C_{End_1}, C_{l,2}), C_{End_2}, C_{End_3}) = 1$ And  $e(C_{Start_1}, g_0^{svk} h_0) = e(g, C_{Start_3})$ , outputs "True" if valid and "False" otherwise. If the verification is hold then proceed.

Finally, outputs the \$m\$ by simply computing:

$$m = {}^{C_m}/_{Key}$$

# IV. ANALYSIS

The proposed scheme ensure data confidentiality of the owner's personal data against unauthorized users and the curious semi trusted proxy. As we presented, the authorized user who's a DFA associated with his/her secret key accepts the string w will recover the massage m. For both unauthorized users and the curious semi trusted proxy cannot retrieve the desired value  $e(g,g)^{\alpha \cdot \lambda}$ , which is required for the decryption. For the reason that the two values  $\epsilon$  and  $\Omega$  are random exponents and only given to authorize user, which renders the description is impossible for unauthorized users. Hence, our scheme ensures confidentiality of the data. Besides, even if the semi trusted proxy transform the ciphertext  $CT_m$  to  $CT_{m'}$  and obtain  $CT_{m'}$  using the user's partial decryption key DK, he still cannot recover m, because he does not know the secret values  $\epsilon$  and  $\Omega$ . Therefore, both a curious semi trusted proxy and unauthorized users can read the massage.

### V. CONCLUSION

Based on DFA-based FPRE scheme, we proposed a secure and efficient outsourcing decryption scheme which increases the flexibility of users to delegate their decryption rights to the semi trusted proxy. In our scheme, the user who has a DFA associated with his/her secret key accepts the string associated with the ciphertext can quite efficiently access the encrypted data with the help of the semi trusted proxy. Furthermore, it can also prove it as fully chosen-ciphertext secure in the standard model. Moreover, it is safe to draw the conclusion that our present work could be considered a secure and high efficient. Finally, our future research will concentrate on proving the security of our scheme in the standard model.

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