



# Molecules with ALMA at Planet-forming Scales (MAPS). XIII. HCO<sup>+</sup> and Disk Ionization Structure

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## Abstract

We observed HCO<sup>+</sup>  $J = 1 - 0$  and H<sup>13</sup>CO<sup>+</sup>  $J = 1 - 0$  emission toward the five protoplanetary disks around IM Lup, GM Aur, AS 209, HD 163296, and MWC 480 as part of the MAPS project. HCO<sup>+</sup> is detected and mapped at 0''3 resolution in all five disks, while H<sup>13</sup>CO<sup>+</sup> is detected ( $S/N > 6\sigma$ ) toward GM Aur and HD 163296 and tentatively detected ( $S/N > 3\sigma$ ) toward the other disks by a matched filter analysis. Inside a radius of  $R \sim 100$  au, the HCO<sup>+</sup> column density is flat or shows a central dip. At outer radii ( $\gtrsim 100$  au), the HCO<sup>+</sup> column density decreases outward, while the column density ratio of HCO<sup>+</sup>/CO is mostly in the range of  $\sim 10^{-5} - 10^{-4}$ . We derived the HCO<sup>+</sup> abundance in the warm CO-rich layer, where HCO<sup>+</sup> is expected to be the dominant molecular ion. At  $R \gtrsim 100$  au, the HCO<sup>+</sup> abundance is  $\sim 3 \times 10^{-11} - 3 \times 10^{-10}$ , which is consistent with a template disk model with X-ray ionization. At the smaller radii, the abundance decreases inward, which indicates that the ionization degree is lower in denser gas, especially inside the CO snow line, where the CO-rich layer is in the midplane. Comparison of template disk models with the column densities of HCO<sup>+</sup>, N<sub>2</sub>H<sup>+</sup>, and N<sub>2</sub>D<sup>+</sup> indicates that the midplane ionization rate is  $\gtrsim 10^{-18} \text{ s}^{-1}$  for the disks around IM Lup, AS 209, and HD 163296. We also find hints of an increased HCO<sup>+</sup> abundance around the location of dust continuum gaps in AS 209, HD 163296, and MWC 480. This paper is part of the MAPS special issue of the Astrophysical Journal Supplement.

*Unified Astronomy Thesaurus concepts:* [Astrochemistry \(75\)](#); [Planetary system formation \(1257\)](#); [Protoplanetary disks \(1300\)](#)

*Supporting material:* figure set

## 1. Introduction

Protoplanetary disks are the birth site of planetary systems, including our solar system. The rate and degree of ionization are important parameters for both the physical and chemical evolution of the disk, and thus for the formation of planetary systems. The disk gas is much denser, and thus its ionization

degree  $x_i$ , which is the relative abundance of electrons to H<sub>2</sub>, is much lower than in parental molecular clouds (e.g., Umebayashi & Nakano 1988).<sup>25</sup> Yet the ionization degree is expected to be sufficient for the gas to be partially coupled with the magnetic fields present in the disk, which could induce magnetohydrodynamic instabilities, disk winds, and thus the

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<sup>25</sup> Considering neutrality, the electron abundance should be the same as the total abundance of cations. In dense midplane regions, grain particles can be the dominant charge carrier.

angular momentum transfer needed for mass accretion (e.g., Suzuki & Inutsuka 2009; Bai & Stone 2013). More specifically, the ionization degree, and thus the coupling between gas and magnetic fields (i.e., nonideal MHD effects), should vary spatially within the disk, which affects the physical structure of the disk (e.g., Béthune et al. 2017). Ionization also triggers ion–molecule reactions in the disk. For example, carbon monoxide, which is the main tracer of disk gas, can be converted to other species by ion–molecule reactions within the typical evolutionary timescale of the disk ( $10^6$  yr), if the ionization rate  $\zeta$  is similar to or higher than the cosmic-ray (CR) ionization rate in the interstellar medium ( $10^{-17}$  s $^{-1}$ ; Bergin et al. 2014; Furuya & Aikawa 2014; Bosman et al. 2018; Schwarz et al. 2018).

The ionization degree is determined by the ionization rate, gas density, and number density and size distribution of dust grains. For protoplanetary disks, there are several possible ionization sources: X-rays from the central star, CRs and stellar energetic particles, and the decay of short-lived radio active nuclei (SLRs) (e.g., Umebayashi & Nakano 1981; Glassgold et al. 1997; Umebayashi & Nakano 2009; Rab et al. 2017). X-rays are the dominant ionization source in the disk surface. However, X-rays are significantly attenuated before reaching the disk midplane. The attenuation length corresponds to a hydrogen column density of  $N_{\text{H}} \sim 10^{22}$  cm $^{-2}$  at 1 keV, while the hydrogen column densities of our target disks are  $\sim 10^{23}$ – $10^{25}$  cm $^{-2}$  at the radius of 100 au (Zhang et al. 2021). Although the attenuation length is larger at higher energies, the X-ray ionization rate is still expected to be  $\lesssim 10^{-18}$  s $^{-1}$  in the midplane (e.g., Section 4; see also Rab et al. 2018). The CR ionization rate is  $\sim 5 \times 10^{-17}$  s $^{-1}$  in molecular clouds (Dalgarno 2006), and its attenuation length is much larger than that of X-rays. While Umebayashi & Nakano (1981) evaluated the attenuation length to be 96 g cm $^{-2}$ , more recent work by Padovani et al. (2018) reassessed the propagation of CR particles and obtained an even larger attenuation length. But CRs can be scattered by magnetized stellar winds and/or magnetic fields in the disk (e.g., Umebayashi & Nakano 1981; Cleeves et al. 2014; Padovani et al. 2018). Stellar energetic particles could also be disturbed by magnetic fields. Finally, the ionization rate from the decay of  $^{26}\text{Al}$  is estimated to be  $10^{-18}$  s $^{-1}$  in the primordial solar system based on meteorite analysis (e.g., Umebayashi & Nakano 2009). While the abundance of SLRs should vary among star-forming regions, recent chemo-hydrodynamic simulations of the Milky Way predict that the abundance of  $^{26}\text{Al}$  in the primordial solar system may be typical for other star-forming regions (Fujimoto et al. 2018). In summary, the dominant ionization source and ionization degree should vary spatially within the disk and could be different between disks.

The importance of understanding ionization processes motivates the observation of molecular ions in protoplanetary disks. Theoretical models show that the major molecular ions in disks are  $\text{H}_3^+$ ,  $\text{HCO}^+$ ,  $\text{N}_2\text{H}^+$ , and their deuterated isotopologues (e.g., Aikawa & Herbst 2001; Bergin et al. 2007; Willacy 2007; Aikawa et al. 2015, 2018). The most abundant molecular ion varies both radially and vertically in disks (Figure 1). The disk surface is the photon-dominated region (PDR); photoionization makes atomic ions such as  $\text{C}^+$  and  $\text{S}^+$  the main charge carriers. Deeper in the disk,  $\text{H}_3^+$  becomes the most abundant ion, while  $\text{HCO}^+$  becomes dominant when the abundance ratio  $n(\text{CO})/n(\text{e})$  is higher than  $\sim 10^3$ , where  $n(i)$  denotes the number density of species  $i$  (Aikawa et al. 2015). In the regions where  $T < 20$  K (i.e., below the CO snow surface and outside the CO snow line), CO freezes out onto grains, which enhances the  $\text{N}_2\text{H}^+$  abundance. As temperature

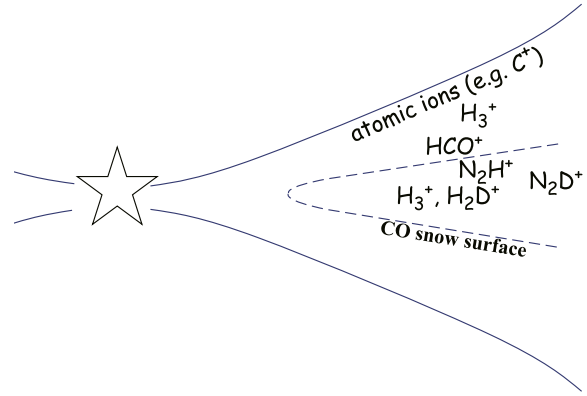


Figure 1. Schematic distribution of major ions in protoplanetary disks.

declines toward deeper layers, the dominant ion changes from  $\text{N}_2\text{H}^+$  to  $\text{H}_3^+$  and its deuterated isotopologues. Unfortunately,  $\text{H}_3^+$  cannot be observed at millimeter wavelengths, and its deuterated isotopologues have not been detected in disks so far.  $\text{N}_2\text{D}^+$  is considered to be an alternative probe to constrain the ionization degree in the cold midplane (Cleeves et al. 2014).

While the rotational transitions of  $\text{HCO}^+$ ,  $\text{N}_2\text{H}^+$ , and their isotopologues have been observed toward several disks, a quantitative evaluation of their column densities and the disk ionization degree has been reported only in a limited number of references. Öberg et al. (2011b) used the IRAM 30 m telescope to observe  $\text{H}^{13}\text{CO}^+ J = 3 - 2$  in the disk of DM Tau. They combined their observation with previous Submillimeter Array (SMA) data of  $\text{N}_2\text{H}^+ J = 3 - 2$ ,  $\text{HCO}^+ J = 3 - 2$ , and  $\text{DCO}^+ J = 3 - 2$  to estimate the ionization degree in three temperature regions of the disk: in the upper warm molecular layer ( $T > 20$  K), the ionization degree  $x_i$  is estimated to be  $4 \times 10^{-10}$  based on the  $\text{HCO}^+$  data. In the cooler molecular layer ( $T = 16$ – $20$  K), where  $\text{N}_2\text{H}^+$  and  $\text{DCO}^+$  would be abundant,  $x_i$  is derived to be  $3 \times 10^{-11}$ , while in the cold, dense midplane ( $T < 16$  K), the nondetection of  $\text{H}_2\text{D}^+$  constrains  $x_i$  to be  $< 3 \times 10^{-10}$ . Teague et al. (2015) observed  $\text{HCO}^+ J = 1 - 0$  and  $J = 3 - 2$  and  $\text{DCO}^+ J = 3 - 2$  in DM Tau at  $\sim 1''5$  resolution using the Plateau de Bure Interferometer. The column densities of  $\text{HCO}^+$  and  $\text{DCO}^+$  at a radius of 100 au are derived to be  $9.8 \times 10^{12}$  cm $^{-2}$  and  $1.2 \times 10^{12}$  cm $^{-2}$ , respectively. They derive an ionization degree of  $\sim 10^{-7}$  from the abundance ratio of  $\text{DCO}^+/\text{HCO}^+$ , assuming steady-state balance between  $\text{H}_3^+ + \text{HD} \rightarrow \text{H}_2\text{D}^+ + \text{H}_2$ ,  $\text{H}_2\text{D}^+ + \text{CO} \rightarrow \text{DCO}^+ + \text{H}_2$ , and the destruction of  $\text{DCO}^+$  (Caselli et al. 2002). Cleeves et al. (2015) calculated chemical models of the disk around TW Hya for various CR ionization rates  $\zeta_{\text{CR}}$  and X-ray spectra. Instead of evaluating molecular column densities from the observational data, they calculated the disk-integrated flux of molecular lines from the models to compare with their own  $\text{HCO}^+$  and  $\text{H}^{13}\text{CO}^+ J = 3 - 2$  observations of TW Hya and  $\text{HCO}^+$ ,  $\text{H}^{13}\text{CO}^+$ , and  $\text{N}_2\text{H}^+$  data from the literature (e.g., Qi et al. 2013a, 2013b). They concluded that the observations are best reproduced by the model with low CR ionization rate  $\zeta_{\text{CR}} \lesssim 10^{-19}$  s $^{-1}$  and modest X-ray spectra, in which the ionization degree is  $\sim 10^{-11}$ – $10^{-10}$  near the midplane outside of a radius of  $\sim 100$  au. Since the ionization degree varies spatially and between disks, observations with higher spatial resolution and toward more targets are highly desirable.

In light of the ring–gap structures observed in the millimeter dust continuum of many disks in recent years

(e.g., Andrews et al. 2018; Huang et al. 2018; Cieza et al. 2021), it is also interesting to investigate whether and how the molecular ion abundances and ionization degree correlate with the dust substructures. Theoretical studies predict that  $\text{HCO}^+$  is sensitive to, and thus could be a good probe of, gas density and/or small dust abundance. In the region where  $\text{HCO}^+$  is the most abundant positive charge carrier, its abundance (i.e., ionization degree) should be proportional to  $n_{\text{H}}^{-1/2}$  (e.g., Duley & Williams 1984). In the gap region, the ionization degree could also be enhanced owing to deeper penetration of X-rays. Aikawa & Nomura (2006), on the other hand, showed that the  $\text{HCO}^+$  column density declines as the abundance of sub-micron-sized dust grains decreases with grain growth. This is because the PDR, in which atomic ions dominate over molecular ions, extends deeper into the disk when the abundance of submicron dust grains decreases. Similar results are obtained in models of disks around Herbig Ae stars (Jonkheid et al. 2007; see also Wakelam et al. 2019). While these models do not include any ring-gap structures, they indicate that the  $\text{HCO}^+$  abundance could vary over the substructures. The  $\text{HCO}^+$  abundance would be higher in the gap than in the ring, if the gas density is lower but the UV attenuation is sufficient in the gap. On the other hand, the  $\text{HCO}^+$  abundance would be lower in the gap if the UV penetration is significant (see also Smirnov-Pinchukov et al. 2020).

In the present work, we analyze the  $J=1-0$  transition of  $\text{HCO}^+$  and  $\text{H}^{13}\text{CO}^+$  toward five disks around IM Lup, GM Aur, AS 209, HD 163296, and MWC 480 observed as a part of the Molecules with ALMA at Planet-forming Scales (MAPS) Large Program (Öberg et al. 2021, project code 2018.1.01055.L). For a given column density of  $\text{HCO}^+$  at a lukewarm temperature (a few tens of kelvin), which corresponds to the CO-rich molecular layer in the disk, the  $J=1-0$  line tends to be optically thinner than higher transitions and thus useful to derive the column density. Our spatial resolution,  $0''.3$ , is high enough to investigate the radial distribution of  $\text{HCO}^+$  and to marginally resolve the continuum gap regions. We also combine our results with the analysis of CO isotopologues,  $\text{N}_2\text{H}^+$ , and  $\text{N}_2\text{D}^+$  in the companion MAPS papers by Zhang et al. (2021) and Cataldi et al. (2021) to estimate the radial variation in the ionization degree and the ionization rate in the disks. Various data products of the MAPS project, including the present work, such as reduced observational data, zeroth-moment maps, as well as derived  $\text{HCO}^+$  column densities can be downloaded at [www.alma-maps.info](http://www.alma-maps.info).

The outline of this paper is as follows. We briefly describe the observations in Section 2. Section 3 describes the observational results: the zeroth-moment maps, radial emission profiles, azimuthally averaged spectra, and molecular column densities. We derive the  $\text{HCO}^+$  abundance, which corresponds to a lower limit of the ionization degree in the warm molecular layer, and compare our results with a template disk chemistry model in Section 4. Our conclusions are presented in Section 5.

## 2. Observations

The observational setup chosen by MAPS covered four spectral setups: two in Band 3 at  $\sim 3$  mm and two in Band 6 at  $\sim 1$  mm. The  $J=1-0$  transitions of  $\text{HCO}^+$  and  $\text{H}^{13}\text{CO}^+$  are in one of the Band 3 setups. The spectral resolution is  $0.237$  km  $\text{s}^{-1}$  for  $\text{HCO}^+$  and  $0.488$  km  $\text{s}^{-1}$  for  $\text{H}^{13}\text{CO}^+$ . Molecular data for the targeted lines are taken from the CDMS database<sup>26</sup> (Müller et al. 2001; Endres et al. 2016) and summarized in Table 1.

**Table 1**

Molecular Data of the Targeted Lines Taken from the CDMS Database

Transition	Frequency (GHz)	$A_{ij}^a$ ( $\text{s}^{-1}$ )	$E_u^b$ (K)
$\text{HCO}^+ J=1-0$	89.1885247	$4.2512 \times 10^{-5}$	4.28
$\text{H}^{13}\text{CO}^+ J=1-0$	86.7542884	$3.8534 \times 10^{-5}$	4.16

**Notes.**

<sup>a</sup> Einstein A-coefficient.

<sup>b</sup> Upper-state energy.

Two array configurations were used: a short-baseline configuration that was sensitive to extended structure, and a long-baseline configuration to achieve high angular resolution. The details of the data calibration are described in Öberg et al. (2021). The MAPS collaboration produced images from the calibrated visibilities using the CLEAN algorithm implemented in the CASA `tclean` task. Details of the imaging procedure are described in Czekala et al. (2021). We use the fiducial images provided by MAPS, which have a  $0''.3$  circular beam. This beam size corresponds to a physical size of 30.3 au at the distance of HD 163296, which is the closest target, and 48.6 au at the distance of MWC 480, which is the most distant. Basic properties of the data cubes such as noise levels are summarized in Tables 11 and 12 in Öberg et al. (2021).

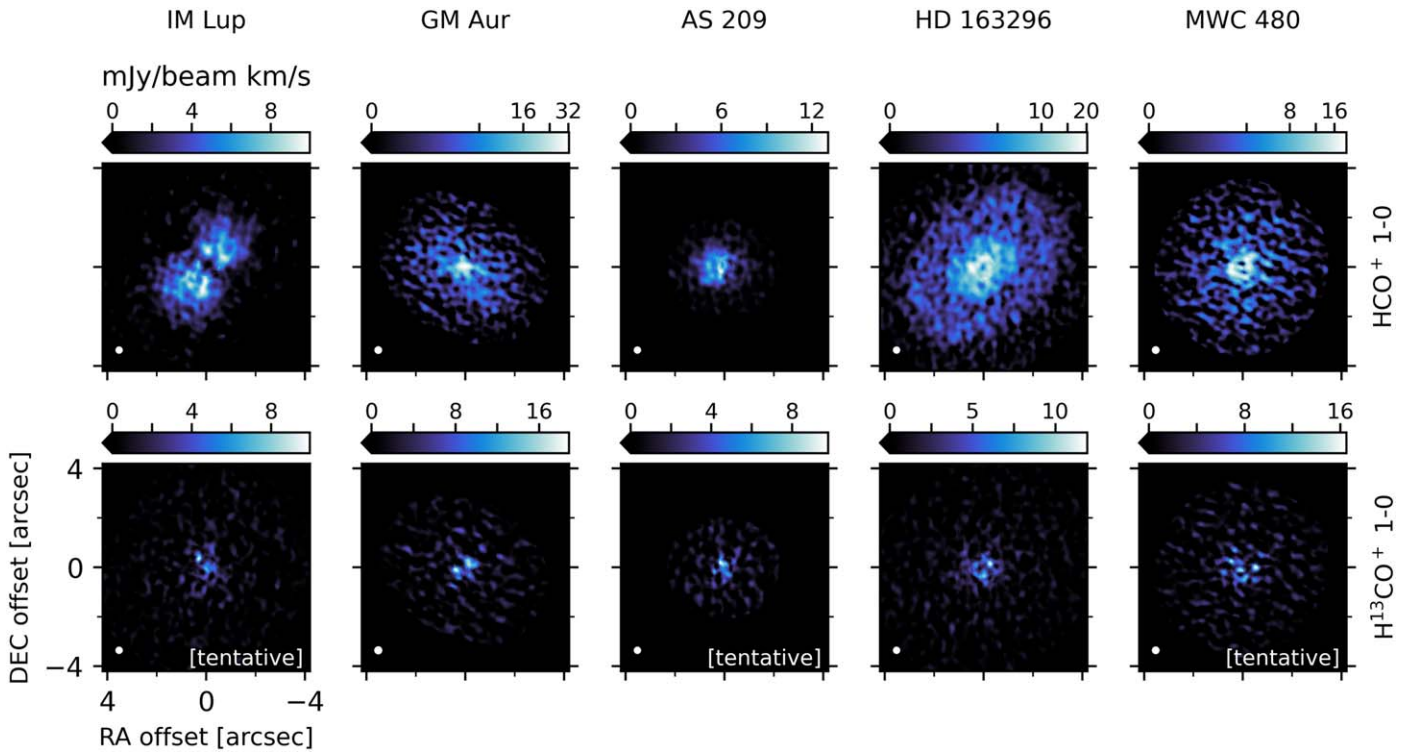
## 3. Observational Results

### 3.1. Zeroth-moment Maps, Disk-integrated Fluxes, and Radial Emission Profiles

The MAPS collaboration produced zeroth-moment maps by applying a Keplerian mask to the data cubes and integrating over the velocity axis (Law et al. 2021a). The mask parameters are conservatively chosen to incorporate all  $^{13}\text{CO } J=2-1$  emission, which is the most widespread emission of any species except for CO  $J=2-1$ . The mask parameters for the five disk are summarized in Table 1 in Czekala et al. (2021). The stellar masses adopted for the generation of the masks are listed in Table 1 in Öberg et al. (2021). These maps were used for all scientific analysis, in particular to derive radial emission profiles (Law et al. 2021a). A Keplerian mask, however, introduces spatial variance in noise distribution, since the number of channels summed to create the zeroth-moment maps varies spatially. The discontinuous noise distribution occasionally causes arc-like artifacts, which could be mistaken as real substructure, in the central regions. To mitigate such artifacts, MAPS also produced “hybrid” zeroth-moment maps by combining a Keplerian mask and a smoothed  $\sigma$ -clip mask (thus their name “hybrid”; see Law et al. 2021a, Appendix A). The latter removes the pixels with an S/N below a given threshold. We emphasize that by using a clipping mask with a threshold larger than  $0\sigma$ , some emission is inevitably lost. Therefore, the hybrid zeroth-moment maps are for presentational purposes only and are not used for any quantitative analysis.

In Figure 2, we show hybrid zeroth-moment maps for  $\text{HCO}^+ J=1-0$  and  $\text{H}^{13}\text{CO}^+ J=1-0$ . We choose the best-looking  $\sigma$ -clip value by visual inspection:  $1\sigma$  for  $\text{HCO}^+ J=1-0$  toward IM Lup, and  $0\sigma$  for the other maps. Hybrid zeroth-moment maps with a  $0''.5$  tapered beam are shown in Figure 13 in Appendix A; the faint emission is more easily seen in the lower spatial resolution images.

<sup>26</sup> <https://cdms.astro.uni-koeln.de/>



**Figure 2.** Gallery of hybrid zeroth-moment maps for  $\text{HCO}^+ J=1-0$  (top row) and  $\text{H}^{13}\text{CO}^+ J=1-0$  (bottom row) for the MAPS sample, ordered from left to right by increasing stellar mass (see Table 1 in Öberg et al. 2021). These maps were generated by combining a Keplerian mask with a smoothed  $\sigma$ -clip mask (Appendix A of Law et al. 2021a). The color scales employ either linear or arcsinh stretches, with the lower end saturating at 0  $\text{mJy beam}^{-1} \text{km s}^{-1}$ . The synthesized beam is shown by the white ellipse in the lower left corner of each panel. Due to the use of a mask, the noise level is not constant across a map. Lines that are only tentatively detected in total flux or matched filter are marked in the lower right corner of the panel.

**Table 2**  
Disk-Integrated Fluxes

	$\text{HCO}^+ 1-0$			$\text{H}^{13}\text{CO}^+ 1-0^{\text{a}}$			$\text{H}^{13}\text{CO}^+ 1-0^{\text{b}}$		
	$r_{\text{min}}^{\text{c}}$ (au)	$r_{\text{max}}^{\text{d}}$ (au)	Flux ( $\text{mJy km s}^{-1}$ )	$r_{\text{min}}$ (au)	$r_{\text{max}}$ (au)	Flux ( $\text{mJy km s}^{-1}$ )	$r_{\text{min}}$ (au)	$r_{\text{max}}$ (au)	Flux ( $\text{mJy km s}^{-1}$ )
IM Lup	0	700	$519 \pm 53$	0	700	$<46$	0	400	$23 \pm 6$
GM Aur	0	500	$412 \pm 42$	0	500	$<43$	0	400	$27 \pm 7$
AS 209	0	300	$178 \pm 19$	0	300	$<33$	0	200	$<26$
HD 163296	0	550	$1002 \pm 101$	0	550	$<54$	50	400	$27 \pm 7$
MWC 480	0	550	$323 \pm 34$	0	550	$<34$	50	100	$<18$

**Notes.** Upper limits are at  $3\sigma$  significance.

<sup>a</sup> For a Keplerian mask with the same radial extent as used for  $\text{HCO}^+ 1-0$ .

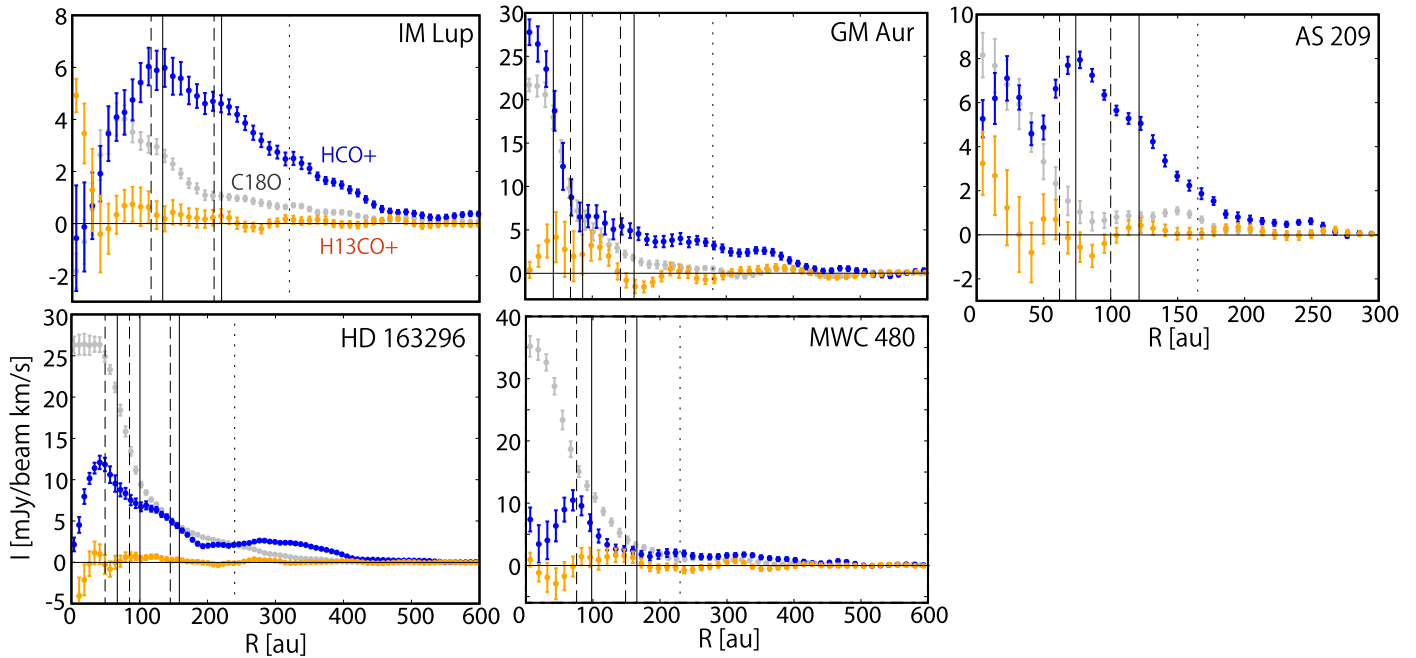
<sup>b</sup> For a Keplerian mask with the same radial extent as the matched filter that maximizes the S/N of the filter response (see Appendix B and Figure 14).

<sup>c</sup> Minimum radius of the Keplerian mask.

<sup>d</sup> Maximum radius of the Keplerian mask.

The  $\text{HCO}^+ J=1-0$  line is clearly detected in all five disks. The emission is relatively bright inside a radius of  $\sim 200$  au, while its diffuse emission extends to  $\gtrsim 400$  au, except for the disk of AS 209, in which the emission extends only up to  $R \sim 300$  au. In AS 209, the emission from the west side of the disk is absorbed by a foreground cloud, which happens to have a similar line-of-sight velocity (Öberg et al. 2011a). We thus performed all analysis for AS 209 only on the unobscured east side of the disk within a  $\pm 55^\circ$  wedge centered on the semimajor axis (Teague et al. 2018b; Law et al. 2021a). The emission of  $\text{H}^{13}\text{CO}^+ J=1-0$  is very weak and is not clearly seen in the zeroth-moment maps.

Disk-integrated fluxes of  $\text{HCO}^+ J=1-0$  and  $\text{H}^{13}\text{CO}^+ J=1-0$  are presented in Table 2. These were calculated by integrating the flux within a Keplerian mask. The radial extent of the Keplerian mask is different from that used for the zeroth-moment maps. For  $\text{HCO}^+$ , the radial extent of the mask is visually determined from the extent of the emission seen in the radial emission profile (see Figure 3 and Table 2). For  $\text{H}^{13}\text{CO}^+$ , we measured fluxes by using the same radial extents as for  $\text{HCO}^+$ . In an attempt to increase the signal-to-noise ratio (S/N), we computed additional fluxes by adopting the same radial extent as the Keplerian models that maximize the S/N in the matched filter analysis in the  $u-v$  plane (Appendix B,



**Figure 3.** Radial emission profiles of  $\text{HCO}^+ J=1-0$ ,  $\text{H}^{13}\text{CO}^+ J=1-0$ , and  $\text{C}^{18}\text{O} J=1-0$  for IM Lup, GM Aur, AS 209, HD 163296, and MWC 480. The error bar shows the  $\pm 1\sigma$  error. The size of the radial bins is  $0''.075$ , which is a quarter of the beam size. The vertical lines indicate the positions of rings (solid), gaps (dashed), and the edge of millimeter dust continuum (dotted) referring to Huang et al. (2018), Long et al. (2018), Liu et al. (2019), and Law et al. (2021a) (see also Sierra et al. 2021).

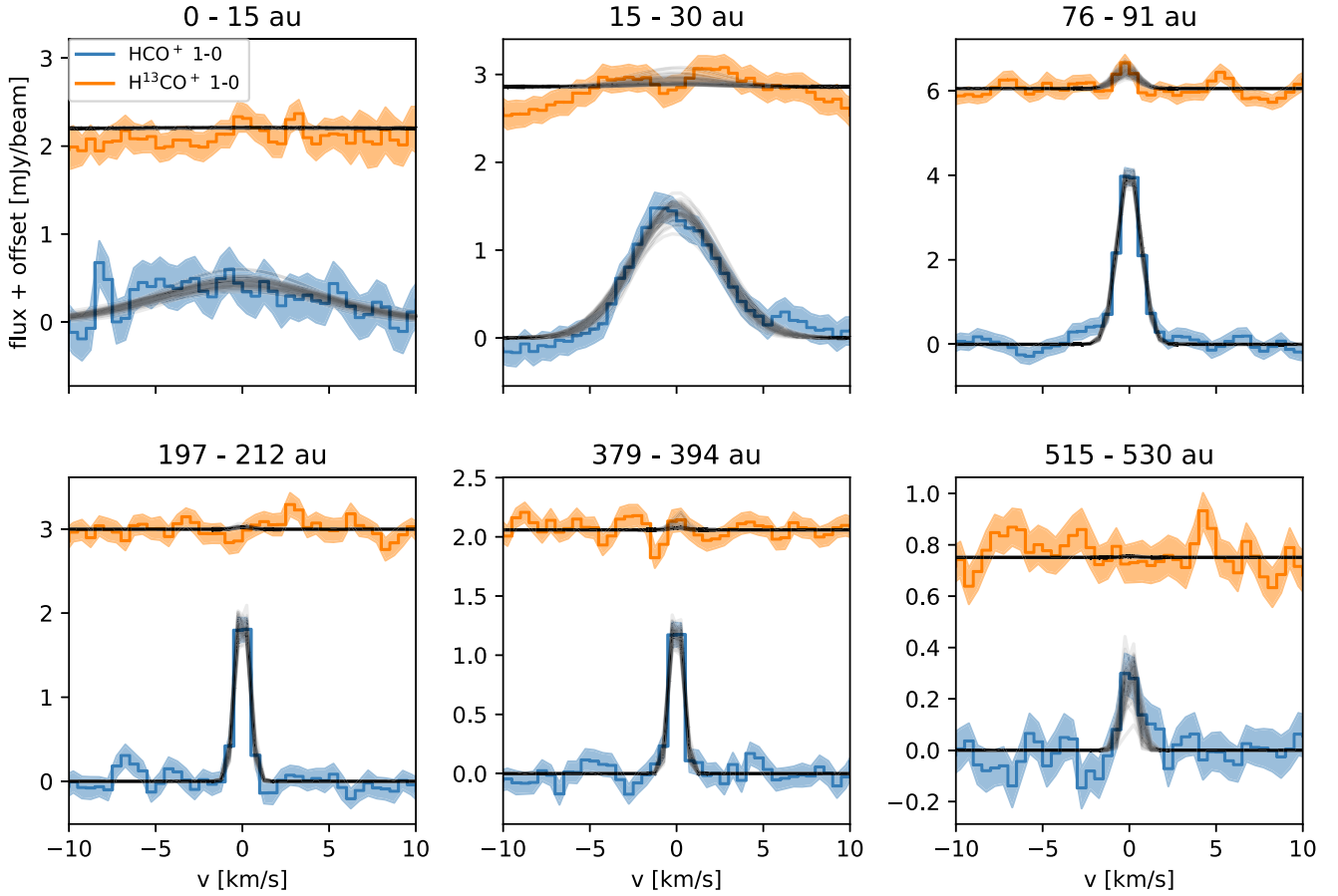
Figure 14), as shown in the right column of Table 2. Errors were calculated by repeating the flux measurement procedure at off-source positions and taking the standard deviation of the off-source fluxes. A 10% flux calibration error was added in quadrature. If the resulting S/N was smaller than 3, Table 2 reports the  $3\sigma$  upper limit. To calculate these disk-integrated fluxes and errors, we used the image cubes that are not corrected for the primary beam. This is because for primary-beam-corrected images, the noise increases toward the edges of the image, making our approach to estimate the error from off-source positions invalid. However, we verified that the difference to fluxes extracted from primary-beam-corrected images is negligible. For deriving radially resolved column density profiles, we use the primary-beam-corrected images.

$\text{H}^{13}\text{CO}^+$  is seen with  $\text{S/N} > 3$  for IM Lup, GM Aur, and HD 163296, if we use the masks with the extent informed by the matched filter analysis. The matched filter analysis itself (Appendix B) gives a response larger than  $6\sigma$  for GM Aur and HD 163296 and larger than  $3\sigma$  for the other disks. Thus, we consider  $\text{H}^{13}\text{CO}^+ J=1-0$  detected in GM Aur and HD 163296, and tentatively detected for the other three disks. We note that the values in Table 2 are different from those in Table 12 in Öberg et al. (2021), who adopted the same Keplerian masks to generate zeroth-moment maps and to estimate disk-integrated fluxes.

Figure 3 shows the radial emission profiles of the  $J=1-0$  transitions of  $\text{HCO}^+$  and  $\text{H}^{13}\text{CO}^+$ . These profiles are produced by azimuthally averaging the zeroth-moment maps that were produced with a Keplerian mask only (i.e., without a  $\sigma$ -clip mask). The inclination and position angles of each disk are listed in Table 1 in Öberg et al. (2021). Since  $\text{HCO}^+$  is expected to be formed by  $\text{CO} + \text{H}_3^+$  and to be a dominant molecular ion in CO gas-rich layers, we also plotted the radial emission profile of  $\text{C}^{18}\text{O} J=1-0$  derived by Law et al. (2021a). The vertical lines indicate the radius of rings (solid),

gaps (dashed), and the dust disk edge (dotted) observed in the millimeter dust continuum (Huang et al. 2018; Long et al. 2018; Liu et al. 2019; Law et al. 2021a; Sierra et al. 2021). Both  $\text{HCO}^+$  emission and  $\text{C}^{18}\text{O}$  emission extend out to several hundred astronomical units. In the IM Lup disk, the radial emission profile of  $\text{HCO}^+ J=1-0$  is similar to that of  $\text{C}^{18}\text{O}$ , showing a ring-like distribution, although the peak position of the  $\text{HCO}^+$  emission is  $\sim 36$  au outside of the  $\text{C}^{18}\text{O}$  peak. In GM Aur, on the other hand, both the  $\text{C}^{18}\text{O}$  emission and  $\text{HCO}^+$  emission are centrally peaked. The radial emission profiles of  $\text{C}^{18}\text{O}$  and  $\text{HCO}^+$  are quite different in AS 209: around a radius of  $\sim 77$  au, the  $\text{HCO}^+$  emission has a local maximum, while the radial gradient of  $\text{C}^{18}\text{O}$  changes from negative to plateau. Interestingly, the peak position of the  $\text{HCO}^+$  emission coincides with that of a dust continuum ring. In the disks around the Herbig Ae stars, HD 163296 and MWC 480, the  $\text{HCO}^+$  emission shows a central dip, while  $\text{C}^{18}\text{O}$  is flat for HD 163296 and centrally peaked for MWC 480.

The intensity ratio of the  $\text{C}^{18}\text{O}$  and  $\text{HCO}^+$  lines varies significantly with radius and among objects. For example, the ratio reaches  $\sim 5$  toward the center of the MWC 480 disk, while  $\text{HCO}^+$  is brighter than  $\text{C}^{18}\text{O}$  around  $R \sim 77$  au in AS 209. Although this indicates that the abundance (column density) ratio of  $\text{HCO}^+$  to  $\text{C}^{18}\text{O}$  also varies, we need to consider the line optical depth. Under LTE conditions with an excitation temperature of 30 K, which is a typical temperature in the warm molecular layers, the optical depth of  $\text{C}^{18}\text{O} J=1-0$  reaches unity for a  $\text{C}^{16}\text{O}$  column density of  $\sim 6 \times 10^{18} \text{ cm}^{-2}$ , assuming a  $^{16}\text{O}/^{18}\text{O}$  isotope ratio of 557 (Wilson 1999). Zhang et al. (2021) derived the radial column density distribution of CO by analyzing several transitions of CO and its isotopologues. The CO column density exceeds  $6 \times 10^{18} \text{ cm}^{-2}$  inside a radius of  $\sim 100$  au in the GM Aur, HD 163296, and MWC 480 disks. At least for these inner radii,  $\text{C}^{18}\text{O} J=1-0$  is optically thick, and thus the intensity ratio of  $\text{C}^{18}\text{O}$  to  $\text{HCO}^+$  does not



**Figure 4.** Examples of  $\text{HCO}^+$  and  $\text{H}^{13}\text{CO}^+$   $J = 1 - 0$  model spectra fit to azimuthally averaged spectra of HD 163296 for a few radial bins. The orange and blue solid lines show the data, with the shaded regions corresponding to the  $1\sigma$  uncertainty. The black curves show 50 randomly selected models drawn from the Monte Carlo chain, with the selection probability being proportional to the posterior probability of the model. Spectra are vertically offset for clarity.

reflect their column density ratio. We also need to evaluate the optical depth of  $\text{HCO}^+$  to derive its column density; the optical depth of  $\text{HCO}^+$   $J = 1 - 0$  reaches unity for a  $\text{HCO}^+$  column density of  $\sim 1 \times 10^{13} \text{ cm}^{-2}$  under LTE conditions at a temperature of 30 K.

### 3.2. Azimuthally Averaged Spectra and Radial Profiles of the $\text{HCO}^+$ Column Density

In order to evaluate the radial profile of the optical depth and column density of  $\text{HCO}^+$ , we first derive the azimuthally averaged spectrum for radial bins with a width of half the beam size. Due to the Keplerian rotation of the disk, at each spatial location in the data cube, the spectrum is shifted with respect to the systemic velocity. We thus shift each spectrum by the Keplerian velocity projected to the line of sight before averaging the spectra azimuthally. This results in all individual spectra being centered at the systemic velocity, which increases the S/N of the azimuthally averaged spectrum (Teague et al. 2016; Yen et al. 2016; Matrà et al. 2017). The calculation of the error bars of the averaged spectrum is described in detail in Appendix D of Cataldi et al. (2021). Briefly, we calculate both the standard deviation of the spectrum in regions without line emission and an analytical error bar based on the number of independent samples included in the average. We then adopt the maximum of the two as our final error bar. Figure 4 shows examples of extracted spectra of HD 163296. The full gallery of spectra is found in Appendix C.

**Table 3**  
Free Parameters for Fitting of Azimuthally Averaged Spectra to Derive the  $\text{HCO}^+$  Column Density

Parameter	Prior Low <sup>a</sup>	Prior High <sup>b</sup>	Units
$\log N_{\text{HCO}^+}$	1	16	$\log(\text{cm}^{-2})$
$T_{\text{ex}}$	10	100	(K)
$\text{FWHM}_{\text{kernel}}$	0.5 <sup>c</sup>	variable <sup>d</sup>	$(\text{km s}^{-1})$
$\Delta v_{\text{HCO}^+}$ <sup>e</sup>	-0.3	0.3	$(\text{km s}^{-1})$
$\Delta v_{\text{H}^{13}\text{CO}^+}$	-0.3	0.3	$(\text{km s}^{-1})$

**Notes.**

<sup>a</sup> Lower bound of flat prior.

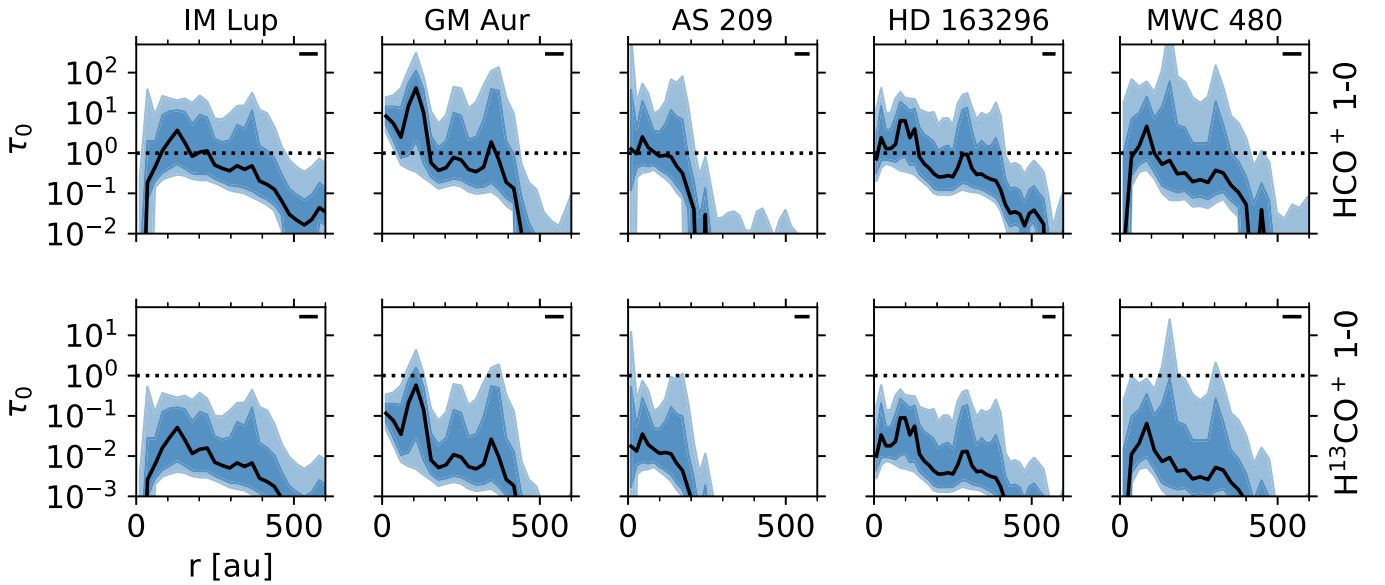
<sup>b</sup> Upper bound of flat prior.

<sup>c</sup> Equal to the channel width.

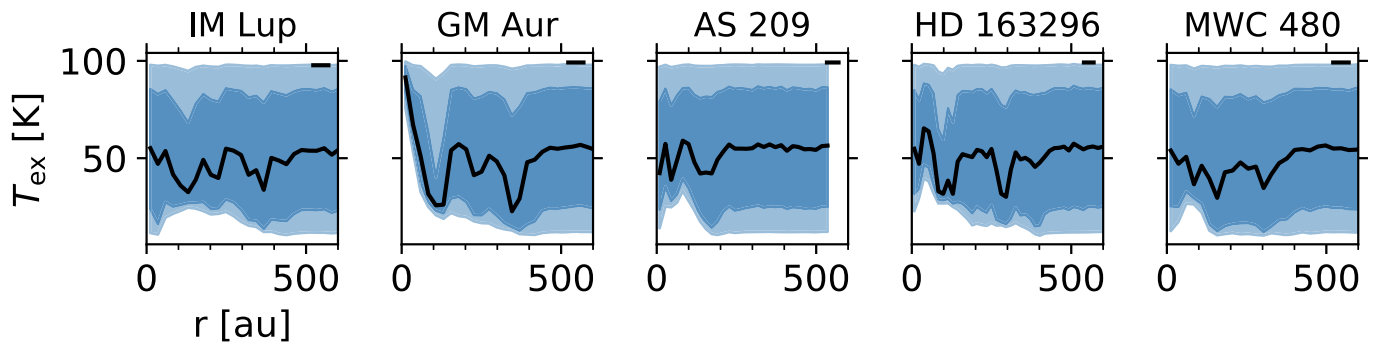
<sup>d</sup> Initial value for innermost radial bin is  $20 \text{ km s}^{-1}$ . Dynamically adjusted when sequentially fitting larger and larger radii (see Cataldi et al. 2021, for details).

<sup>e</sup> Offset of the line center with respect to the systemic velocity.

We then calculate the column density of  $\text{HCO}^+$ ,  $N(\text{HCO}^+)$ , at each radial bin by simultaneously fitting the azimuthally averaged spectra of  $\text{HCO}^+$  and  $\text{H}^{13}\text{CO}^+$ . We employ the same fitting procedure as Cataldi et al. (2021). Briefly, for a given  $\text{HCO}^+$  column density, we compute  $\text{HCO}^+$   $J = 1 - 0$  and  $\text{H}^{13}\text{CO}^+$   $J = 1 - 0$  model spectra that can be compared to the data. There are five free parameters: the logarithm of the  $\text{HCO}^+$  column density, the excitation temperature, an offset  $\Delta v$  of the line center with respect to the systemic velocity for each



**Figure 5.** Optical depth profiles of  $\text{HCO}^+$  ( $J = 1 - 0$ ) and  $\text{H}^{13}\text{CO}^+$  ( $J = 1 - 0$ ) derived from fitting azimuthally averaged spectra. The black lines show the median of the posterior probability, while the shaded regions extend from the 16th to 84th percentile and from the 2.3th to 97.7th percentile. The beam size is shown as a horizontal line in the upper right corner.



**Figure 6.** The excitation temperature derived from fitting azimuthally averaged spectra. The black lines show the median of the posterior probability, while the shaded regions extend from the 16th to 84th percentile and from the 2.3th to 97.7th percentile. The beam size is shown as a horizontal line in the upper right corner.

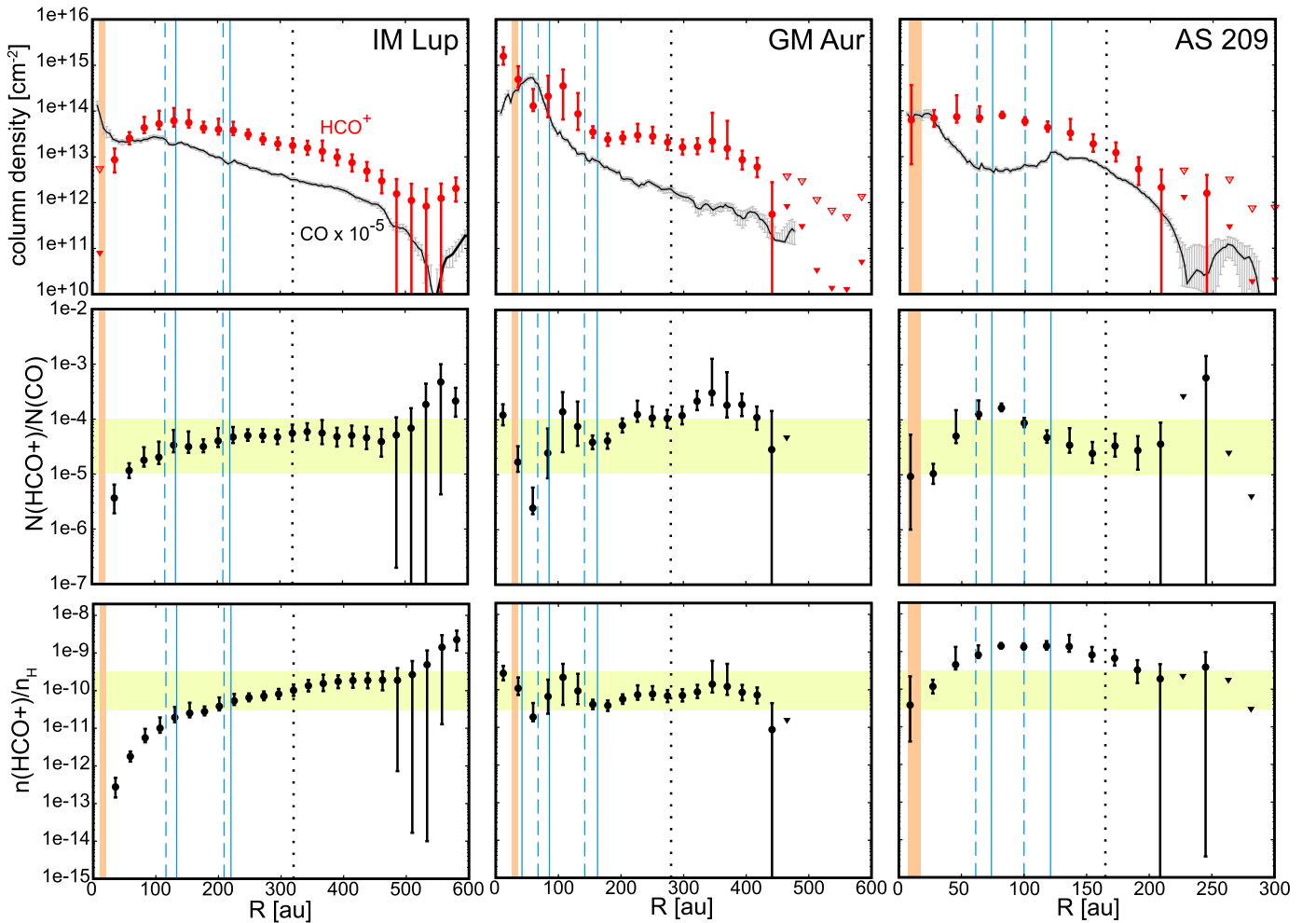
line, and the FWHM of the Gaussian kernel with which the model spectra are convolved to mimic observational broadening. The  $\text{H}^{13}\text{CO}^+$  column density is fixed to 1/68 of the  $\text{HCO}^+$  column density (Milam et al. 2005). We use a Markov Chain Monte Carlo (MCMC) method implemented in the `emcee` package (Foreman-Mackey et al. 2013) to explore the parameter space and assume flat priors. We employ 200 walkers taking 5000 steps each, and we discard the first 2500 steps from the analysis. The free parameters and the prior boundaries are listed in Table 3. The full details of the fitting procedure can be found in Cataldi et al. (2021). Figure 4 shows examples of model spectra fitted to the HD 163296 data. The full gallery of models is shown in Appendix C.

Figures 5 and 6 show the optical depths and excitation temperature derived by fitting the azimuthally averaged spectra, respectively. We find that  $\text{HCO}^+$   $J = 1 - 0$  is optically thick at the column density peaks. However, we are still able to constrain the  $\text{HCO}^+$  column density because the  $\text{H}^{13}\text{CO}^+$   $J = 1 - 0$  transition is in the optically thin regime. The top panels in Figure 7 present the derived  $\text{HCO}^+$  column densities.

The excitation temperature is poorly constrained for large radial regions of the disks, as shown in Figure 6. However, at

least a lower limit on the excitation temperature can be placed in some disk locations. The innermost  $\sim 50$  au of GM Aur stand out with an apparently well-constrained  $T_{\text{ex}} \approx 90$  K. This region also requires a large FWHM of  $17 \text{ km s}^{-1}$ . These rather extreme parameters might indicate that the fit is not reliable. In fact, considerable broadening is seen for all disks for the two innermost radial bins (i.e., within one beam FWHM from the disk center) owing to beam smearing of the large velocity gradient in the inner disk (see Figures 16). Therefore, the column density estimates for the two innermost radial bins should be considered with caution.

In Appendix D, we show optical depth and column density profiles for additional fits where the excitation temperature has been fixed to 30 K, which is a typical temperature for the warm molecular layer where  $\text{HCO}^+$  is expected to be present. The corresponding models are shown in Figure 16. The column densities generally agree well with the fits where  $T_{\text{ex}}$  is a free parameter, as can be seen in Figure 17. Furthermore, for both fits, the model spectra fit the data well (Figure 16). One exception is the region inward of  $\sim 150$  au toward GM Aur, where the models with  $T_{\text{ex}}$  as a free parameter generally provide a better fit, especially for the two innermost



**Figure 7.** Top: column densities of  $\text{HCO}^+$  (red) and CO column density scaled by  $10^{-5}$  (black lines with gray error bars). The error bars correspond to 10% or  $1\sigma$  for CO (see Section 3.2), while they show the 16th and 84th percentiles for  $\text{HCO}^+$ . At radii where the median value of the molecular column density is lower than the value at 16th percentile by a factor of  $>10$ , we plot the upper limits as inverted triangles (84th percentile for closed triangles and 98th percentile for open triangles). The vertical orange bars mark the CO snow line as inferred from the model by Zhang et al. (2021) with error of  $\pm 5$  au. The blue solid and dashed lines depict the radius of rings and gaps, respectively, in dust continuum. The black dotted lines depict the outer edge of the millimeter dust continuum. Middle: the column density ratio of  $\text{HCO}^+$  to CO. The yellow bars mark the  $\text{HCO}^+$ /CO column density ratio of  $10^{-5} - 10^{-4}$ . Bottom: abundance of  $\text{HCO}^+$  relative to hydrogen nuclei in the CO gas-rich layer. The yellow bars mark the abundance of  $3 \times 10^{-11} - 3 \times 10^{-10}$ . In the middle and bottom panels, we consider only the error in  $\text{HCO}^+$  column density, since it dominates over the error of CO column density estimates. At radii where the median value of the  $\text{HCO}^+$  column density is lower than the value at 84th percentile by a factor of  $>10$ , we plot the value that corresponds to the  $1\sigma$  upper limit (i.e., 84th percentile of  $\text{HCO}^+$  column density) with an inverted triangle.

radial bins discussed in the previous paragraph (Figure 16). The other exception is the region inward of 76 au toward HD 163296, where the fits with  $T_{\text{ex}} = 30$  K underpredict the  $\text{HCO}^+$  emission and overpredict the  $\text{H}^{13}\text{CO}^+$  emission (Figure 16). Here, the models with  $T_{\text{ex}}$  as a free parameter provide a better fit and predict a column density smaller by a factor of a few compared to the fits where  $T_{\text{ex}} = 30$  K.

In Figure 7, we also plot the column densities of CO that are derived from  $\text{C}^{18}\text{O } J=2-1$  emission in Zhang et al. (2021). For each disk, they constructed a thermochemical model that reproduces the spectral energy distribution. The model provides the 2D ( $R, Z$ ) distributions of temperature and CO abundance. Then, they introduced a CO depletion factor, which is varied from 0.001 to 50 with a step size of 1.1 in a logarithmic scale, at each radial bin, and calculated the CO flux for a grid of models to find the best-fit depletion factor. The uncertainty in the CO column density is thus 10% in most of the disk radii. Exceptions are the innermost and outermost radii; at these radii, the  $\text{C}^{18}\text{O}$  line fluxes have relatively large uncertainties, and the error of the CO column density is  $1\sigma$ . They also derived

the CO column densities using the  $J=2-1$  transition of  $^{13}\text{CO}$  and  $J=1-0$  transition of  $^{13}\text{CO}$ ,  $\text{C}^{18}\text{O}$ , and  $\text{C}^{17}\text{O}$ , which are in reasonable agreement with the value based on  $\text{C}^{18}\text{O } (J=2-1)$ .

Overall, the radial profile of the  $\text{HCO}^+$  column density is similar to that of CO. The panels in the middle row of Figure 7 show the column density ratio  $N(\text{HCO}^+)/N(\text{CO})$ . Since the CO column density was calculated on a finer radial grid than  $\text{HCO}^+$ , we interpolated the CO column density at the radii of  $\text{HCO}^+$ . The error bars in the middle panels reflect only the error of  $\text{HCO}^+$  column density, which dominates over that of CO column density. The ratio is mostly within  $10^{-5} - 10^{-4}$  at  $\sim 100 - 500$  au, which suggests a close chemical link between these species, as expected from chemical models (e.g., Aikawa et al. 2015; Teague et al. 2015).

In the disk of IM Lup, the column densities of both  $\text{HCO}^+$  and CO increase inward from  $R \sim 500$  to 100 au, where the  $\text{HCO}^+/\text{CO}$  column density ratio is remarkably constant. The  $\text{HCO}^+$  column density then declines at  $\lesssim 100$  au, while the CO column density becomes flat and rises inward at  $\lesssim 50$  au.



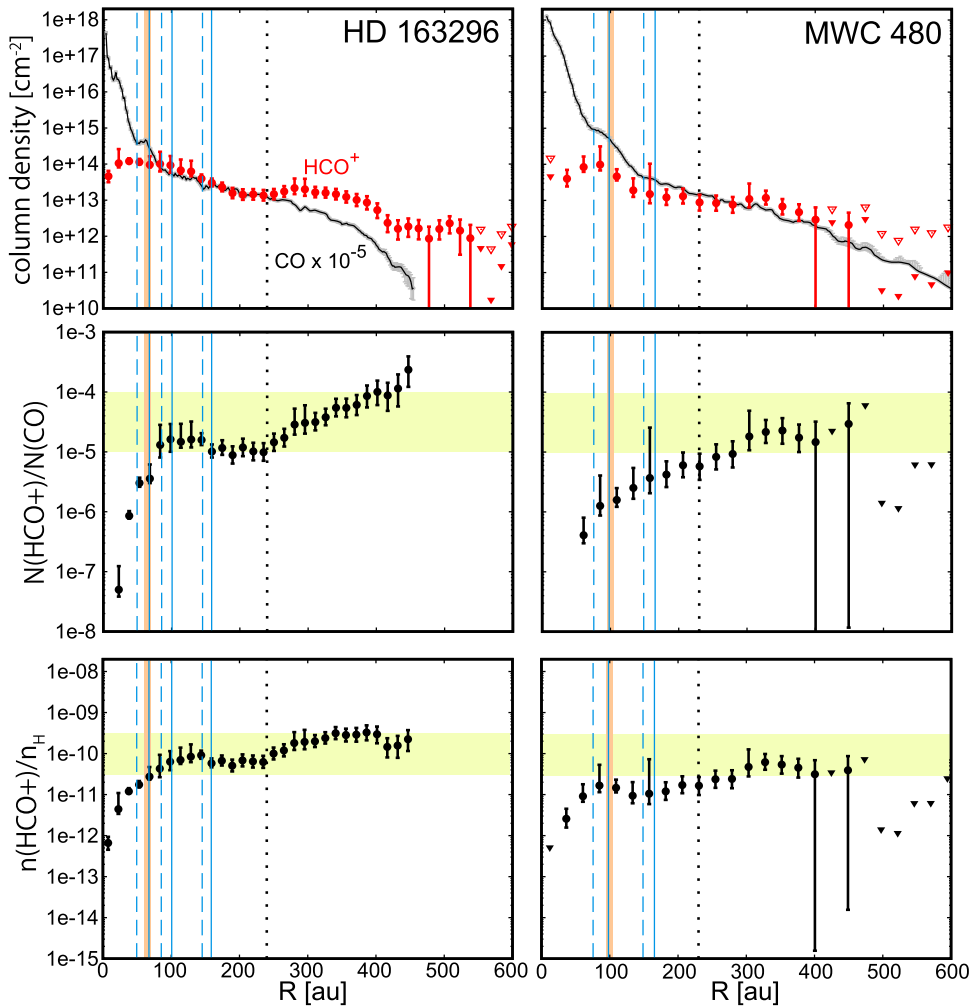


Figure 7. (Continued.)

In the GM Aur disk, the  $\text{HCO}^+/\text{CO}$  column density ratio exceeds  $10^{-4}$  outside the dust continuum edge. Both the  $\text{HCO}^+$  and  $\text{CO}$  column densities increase inward up to  $\sim 100$  au, while they have small local humps. At  $R \sim 60$  au, the  $\text{CO}$  column density has a local maximum, while that of  $\text{HCO}^+$  has a local minimum. This coincidence needs to be taken with caution, however, since the beam size of  $\text{HCO}^+$  data is two times larger than that of  $\text{CO}$ , and since the column density estimates at the innermost radii suffer line broadening due to the velocity gradient within a beam. In the disk of AS 209, the radial profile of  $\text{HCO}^+$  significantly differs from that of  $\text{CO}$  at  $R \lesssim 100$  au. While the  $\text{CO}$  column density shows a broad depression at  $R \sim 45\text{--}120$  au, the  $\text{HCO}^+$  column density increases inward up to  $\sim 75$  au and stays constant at inner radii within the error bars. In the disk around HD 163296, the column density ratio of  $\text{HCO}^+/\text{CO}$  decreases inward up to  $R \sim 240$  au, which corresponds to the edge of the millimeter dust continuum. From 240 to 65 au, the ratio stays constant or has a shallow rise, while both the  $\text{CO}$  and  $\text{HCO}^+$  column densities increase inward. Inside the radius of  $\sim 65$  au, which coincides with the  $\text{CO}$  snow line in the thermochemical model, the  $\text{HCO}^+$  column density is roughly constant, while the  $\text{CO}$  column density increases toward the center by more than an order of magnitude. The sharp rise of  $\text{CO}$  column density and relatively flat distribution of  $\text{HCO}^+$  column density inside the  $\text{CO}$  snow line are also seen in MWC 480, while the overall column density ratio

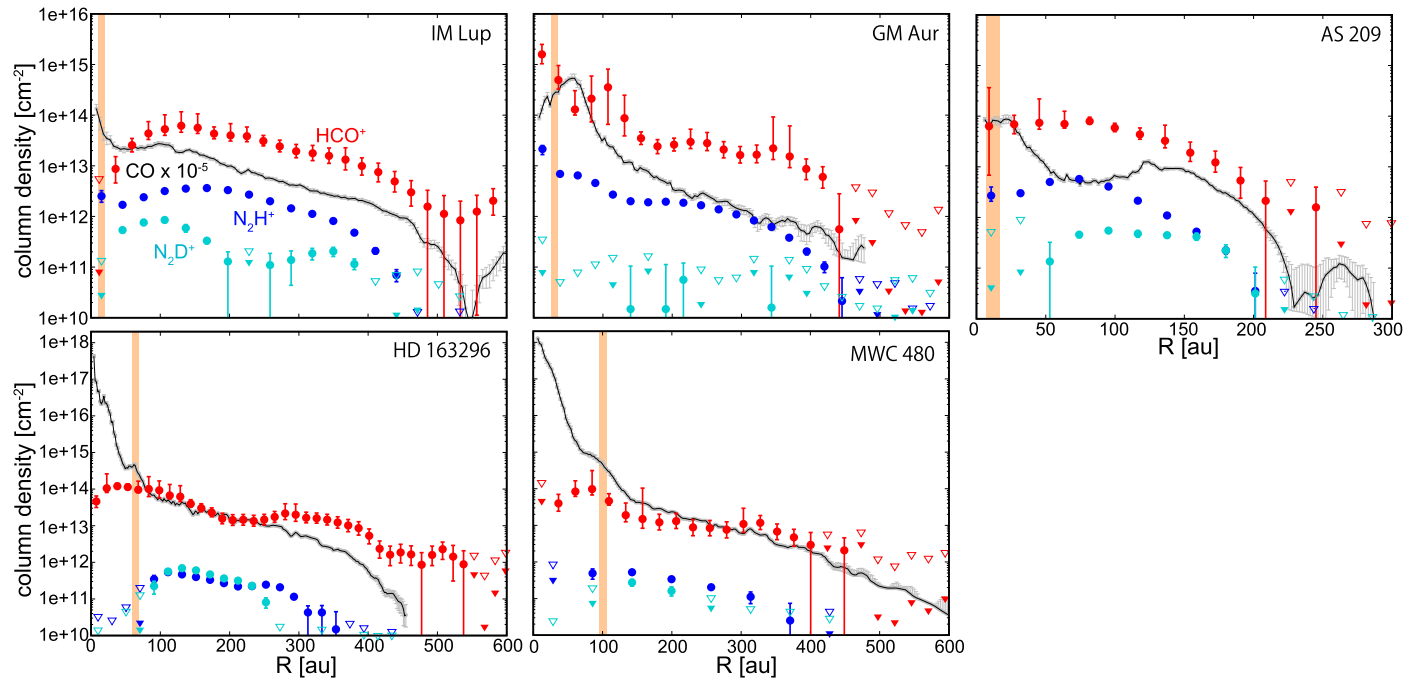
of  $\text{HCO}^+/\text{CO}$  is slightly lower than that in HD 163296. We note that the X-ray spectrum of MWC 480 is significantly softer than that of HD 163296 (Dionatos et al. 2019). Since X-rays are the major ionization source in the molecular layer (see Section 4.3), the relatively low  $\text{HCO}^+/\text{CO}$  column density ratio in MWC 480 could be due to the lack of high-energy X-rays ( $\gtrsim$  a few keV).

## 4. Discussion

### 4.1. $\text{HCO}^+$ Abundance in the Warm Molecular Layers

In the molecular layers of protoplanetary disks, the major molecular ions are  $\text{H}_3^+$ ,  $\text{HCO}^+$ , and  $\text{N}_2\text{H}^+$ , among which  $\text{H}_3^+$  cannot be observed at millimeter wavelengths. Its deuterated counterpart  $\text{o-H}_2\text{D}^+$  has not been detected so far (e.g., Chapillon et al. 2011). Figure 8 shows the radial profiles of the  $\text{HCO}^+$ ,  $\text{N}_2\text{H}^+$ , and  $\text{N}_2\text{D}^+$  column densities obtained in this work and by Cataldi et al. (2021). We can see that  $\text{HCO}^+$  has the largest column densities among the observable molecular ions in our five disks.

$\text{HCO}^+$  is expected to be the major molecular ion in the warm molecular layer where  $\text{CO}$  gas is abundant. Thus, here we assume that the majority of  $\text{HCO}^+$  coexists with  $\text{CO}$  in the warm molecular layer and derive the  $\text{HCO}^+$  abundance there, based on the  $\text{HCO}^+$ -to- $\text{CO}$  column density ratio. Furthermore, we assume that the  $\text{CO}$  abundance relative to



**Figure 8.** Column densities of  $\text{HCO}^+$  (red),  $\text{N}_2\text{H}^+$  (blue), and  $\text{N}_2\text{D}^+$  (light blue). Black lines with gray error bars depict the CO column density scaled by  $10^{-5}$ . The error bars correspond to 10% or  $1\sigma$  for CO (see Section 3.2), while they show the 16th and 84th percentiles for other species. At radii where the median value of the molecular column density is lower than the value of the 16th percentile by a factor of  $>10$ , we plot the upper limits as inverted triangles (84th percentile for closed triangles and 98th percentile for open triangles). The vertical orange bars mark the CO snow line as inferred from the model by Zhang et al. (2021).

hydrogen nuclei is equal to its canonical abundance in molecular clouds,  $5.0 \times 10^{-5}$ , multiplied by the CO depletion factor derived in Zhang et al. (2021). The bottom panels in Figure 7 show the estimated  $\text{HCO}^+$  abundance. Since the uncertainty (error) of the  $\text{HCO}^+$  column density dominates over that of the CO column density at most disk radii, and since the methods of error estimation are different between  $\text{HCO}^+$  and CO, we evaluate the error of the  $\text{HCO}^+$  abundance considering only that of the  $\text{HCO}^+$  column density. Overall, the  $\text{HCO}^+$  abundance is in a range of  $3 \times 10^{-11} - 3 \times 10^{-10}$  outside  $\sim 100$  au and tends to decline toward the disk center at the inner radii.

In those inner regions, the CO-rich molecular layer extends toward the midplane, although detailed analysis by Zhang et al. (2021) shows that the gaseous CO fractional abundance does not necessarily recover its canonical value (i.e.,  $10^{-4}$  relative to  $\text{H}_2$ ) even inside of the CO snow line. Closer to the midplane, the gas density is higher and the ionization degree, i.e., the  $\text{HCO}^+$  abundance, should be lower. Furthermore,  $\text{HCO}^+$  is suppressed by grain-surface recombination (i.e., collision with a negatively charged grain), which could be more efficient than the recombination in the gas phase at high densities. The  $\text{HCO}^+$  abundance averaged over the CO gas-rich layer should thus be lower around and inside the CO snow line than at outer radii (see Section 4.3).

Although  $\text{HCO}^+$  is expected to be one of the major molecular ions in the warm molecular layer, it is not always the most abundant ion. The relative abundances of major molecular ions,  $\text{H}_3^+$ ,  $\text{HCO}^+$ , and  $\text{N}_2\text{H}^+$ , are determined by the balance between proton transfer and recombination of relevant species, i.e.,  $\text{H}_2$ , CO, and  $\text{N}_2$  (Aikawa et al. 2015). Furthermore, if the abundance of small grains is low enough to allow significant penetration of UV radiation, atomic ions such as  $\text{C}^+$  and  $\text{S}^+$  can dominate even in the CO-rich layers (e.g., Aikawa et al. 2015). Therefore, the  $\text{HCO}^+$  abundance

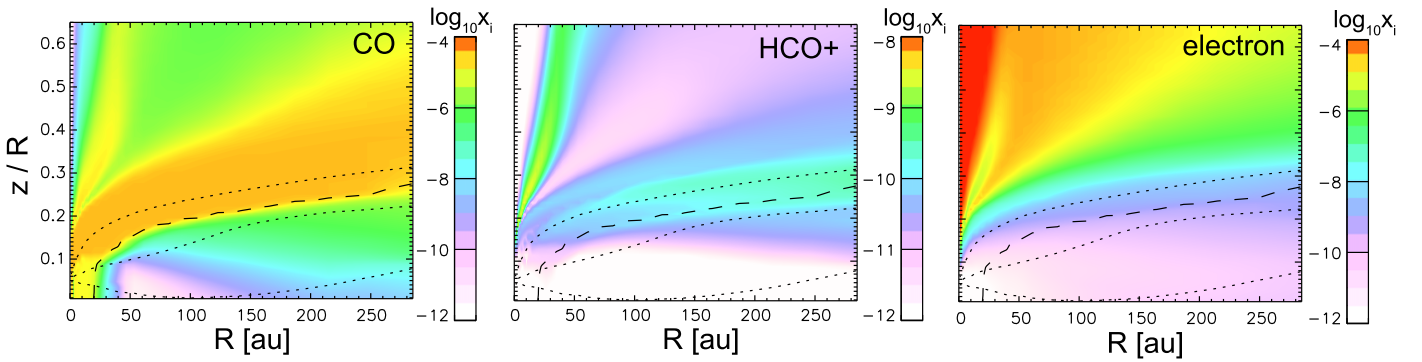
derived here should be considered as a lower limit of the ionization degree in the molecular layer.

#### 4.2. $\text{HCO}^+$ Enhancement in Gas Gaps

The  $\text{HCO}^+$  abundance exceeds  $10^{-9}$  at  $50 \text{ au} \lesssim R \lesssim 150 \text{ au}$  in AS 209, where the CO column density shows a depression. Favre et al. (2019) observed  $\text{DCO}^+ J=3-2$  in AS 209 with high resolution ( $0''.26 \times 0''.21$ ) and found a ring-like emission with its peak at  $\sim 85$  au. They suggest that the overdensity of  $\text{DCO}^+$  is caused by the more efficient ionization at the radius of gas and dust depletion, which is carved by a planet of  $\lesssim 0.3 M_{\text{Jup}}$  at  $\sim 100$  au. The high  $\text{HCO}^+$  abundance at  $50 \text{ au} \lesssim R \lesssim 150 \text{ au}$  is consistent with their scenario.

Alarcón et al. (2021), on the other hand, calculated the thermal structure in two disk models for AS 209; model A assumes a smooth gas distribution and a CO abundance drop around  $R \sim 80$  au, while model B assumes a constant CO abundance combined with a gas density drop around 80 au. They found that the radial pressure profile derived by Teague et al. (2018b) is shallower than in model B and concluded that the CO column density drop at 80 au is caused mainly by a CO abundance drop rather than a gas density drop. Self-consistent modeling of the thermal structure and the  $\text{HCO}^+$  and  $\text{DCO}^+$  chemistry would be useful to distinguish between these scenarios.

We also note correlated local enhancements of  $\text{HCO}^+$  and  $\text{DCO}^+$  in HD 163296. Flaherty et al. (2017) observed  $\text{DCO}^+ (J=3-2)$  with a beam of  $0''.5 \times 0''.59$  and found that  $\text{DCO}^+$  emission is confined to three concentric rings at 54, 124, and 214 au. The ring at 124 au is the brightest and coincides with the shoulder seen in  $\text{HCO}^+$  emission in Figure 3 and the local enhancement of the  $\text{HCO}^+/\text{CO}$  column density ratio (Figure 7). Teague et al. (2018a) analyzed the disk gas kinematics around HD 163296 and found deviations from Keplerian rotation, which



**Figure 9.** The abundances of CO (left),  $\text{HCO}^+$  (middle), and electrons (right) relative to hydrogen nuclei in the low- $\zeta$  model. The dashed line depicts the CO snow surface, and the dotted lines show the positions where the X-ray ionization rate is  $5 \times 10^{-17}$  (the upper dotted line),  $1 \times 10^{-18}$  (the middle dotted line), and  $1 \times 10^{-19}$   $\text{s}^{-1}$  (the lower dotted line),

suggests the presence of a  $1 M_{\text{Jup}}$  planet at 83 au and a  $1.3 M_{\text{Jup}}$  planet at 137 au. Hydrodynamic models of the HD 163296 disk with these planets show gas gaps (i.e., gas density decrease) around the planet orbits. The local enhancement of  $\text{DCO}^+$  and  $\text{HCO}^+$  around 125 au could be related to such gas gaps.

In MWC 480, the CO column density shows a local minimum around the gap seen in dust continuum at  $\sim 76$  au (Figure 7). We note that the  $\text{HCO}^+$  column density has a local maximum at this radius; we derived the column density distribution with radial grids of a quarter of the beam size to confirm the coincidence. It again suggests a correlation between gas gap and  $\text{HCO}^+$  enhancement. Observations of  $\text{HCO}^+$  with higher angular resolution are desirable for further studies.

#### 4.3. Constraining the Ionization Structure with a Template Disk Chemistry Model

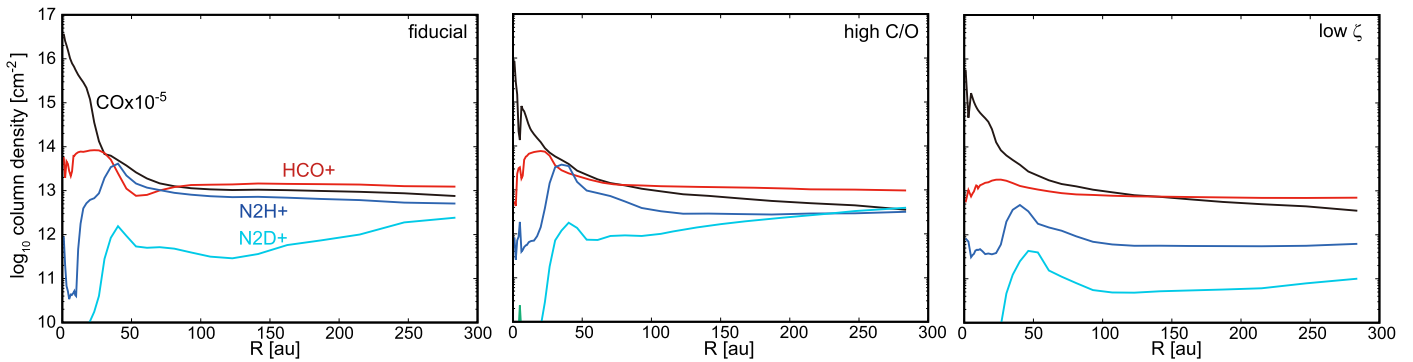
MAPS observations, as well as previous ALMA observations of disks in the past few years, show that detailed physical structure, e.g., size, flaring, and temperature structure, varies significantly among disks (e.g., Law et al. 2021b). While source-specific modeling is desirable, it is out of the scope of the present work. However, we note that the derived abundance and its radial distribution of  $\text{HCO}^+$  have common features; the  $\text{HCO}^+$  abundance is  $\sim 3 \times 10^{-11} - 3 \times 10^{-10}$  at  $\gtrsim 100$  au, while it tends to decrease inward at smaller radii. These features should reflect the basic chemistry of  $\text{HCO}^+$ , which is not very sensitive to the details of the disk structure. Therefore, we compare our results with some template disk models.

We adopt the disk chemistry model of Aikawa et al. (2018); the disk mass is  $1.7 \times 10^{-2} M_{\odot}$ , and the mass of the central star is  $0.5 M_{\odot}$ . Stellar UV and X-ray luminosities are  $10^{31}$  and  $10^{30}$   $\text{erg s}^{-1}$ , respectively. While the dust sedimentation is not considered, the maximum grain size is set to be 1 mm. Since the total gas-to-dust mass ratio is set to be the same as the interstellar value ( $\sim 100$ ), the abundance of small dust grains is reduced compared with the interstellar dust. The 2D ( $R, Z$ ) distributions of the gas number density (i.e., number density of hydrogen nuclei  $n_{\text{H}}$ ) and temperature are shown in Figure 19 in Appendix E. While Aikawa et al. (2018) varied several parameters in the calculation of the chemistry model, we here show three models: their fiducial model, a high-C/O model, and a low- $\zeta$  model, which is newly calculated for the present work. The fiducial model is a static disk model with a CR ionization rate of  $5 \times 10^{-17} \text{ s}^{-1}$ . Two other ionization sources, X-rays and the decay of SLRs, are included in the model with the X-ray spectrum of TW Hya and the ionization rate by SLRs of  $\zeta_{\text{SLR}} = 1 \times 10^{-18} \text{ s}^{-1}$ . The initial molecular

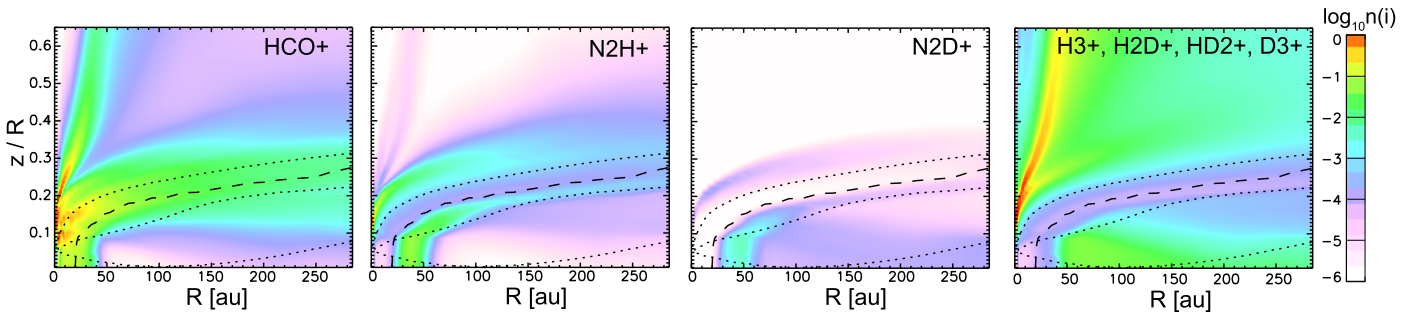
abundance for the disk chemistry is set by calculating the chemical evolution from the molecular cloud formation stage to the collapse of a star-forming core. In the fiducial model, the elemental abundances of C and O are  $7.82 \times 10^{-5}$  and  $1.8 \times 10^{-4}$ , respectively, relative to hydrogen nuclei (i.e., C/O = 0.43). Disk observations in recent years, however, suggest low C/H ratios and high C/O ratios in the gas phase (e.g., Bergin et al. 2014, 2016; Bosman et al. 2021; Zhang et al. 2021). This is likely due to the removal of ice by the sedimentation and radial migration of ice-coated pebbles (Kama et al. 2016; Krijt et al. 2018). Thus, in the high-C/O model,  $\text{H}_2\text{O}$  is completely removed and CO is reduced by one order of magnitude in the initial molecular abundances, which results in a C/O ratio of 1.43. In addition to these two models, we run a low- $\zeta$  model, in which the CR ionization rate is set to zero. Ionization rates by X-ray and SLRs are set to be the same as in the fiducial model, and the initial molecular abundance is the same as the high-C/O model. Since we aim to constrain the ionization rate rather than identifying the main ionization source, the low- $\zeta$  model can simply be considered as a model with a midplane ionization rate of  $\zeta_{\text{mid}} = 10^{-18} \text{ s}^{-1}$ , while  $\zeta_{\text{mid}}$  is  $5 \times 10^{-17} \text{ s}^{-1}$  in the fiducial model and high-C/O model.

While molecular evolution in the disk is calculated up to  $t = 1 \times 10^6$  yr, we compare our observational results with the molecular abundances at  $t = 1 \times 10^5$  yr, which is comparable to the vertical mixing timescale at the radius of several tens of au assuming a  $\alpha$  parameter of  $10^{-3}$  for turbulent mixing (e.g., Aikawa et al. 1996). In gas-grain chemical networks, volatile species tend to be converted to less volatile ices. At  $t = 10^6$  yr, a significant amount of CO and  $\text{N}_2$  is converted to  $\text{CO}_2$ ,  $\text{CH}_3\text{OH}$ , and  $\text{NH}_3$ , which could be an artifact of the static disk assumption (i.e., without mixing or accretion). The desorption rate and thermal diffusion rate (and thus the reaction rate) on the grain surface are very sensitive to temperature. In the static model, in which gas and dust stay at the same position and thus are kept at a constant temperature, only a limited number of species can effectively diffuse and react, which results in an accumulation of specific products. At  $t = 1 \times 10^5$  yr, such accumulations are less significant (see Aikawa et al. 2015, for more details).

Figure 9 shows the abundances of CO,  $\text{HCO}^+$ , and electrons relative to hydrogen nuclei, in the low- $\zeta$  model. The abundances in the other models are shown in Figure 19 in Appendix E. We can see that CO and  $\text{HCO}^+$  are mostly cospatial and that the observed features are reproduced; the  $\text{HCO}^+/\text{CO}$  abundance ratio is  $\sim 10^{-5} - 10^{-4}$ , and the  $\text{HCO}^+$  abundance is  $\sim 10^{-10}$  in the lower part of the CO-rich layer, where the density is higher. In Figure 9, the dashed line



**Figure 10.** Column densities of CO (multiplied by  $10^{-5}$ ),  $\text{HCO}^+$ ,  $\text{N}_2\text{H}^+$ , and  $\text{N}_2\text{D}^+$  in the fiducial model (left), high-C/O model (middle), and low- $\zeta$  model (right).



**Figure 11.** The absolute abundances (number densities) of  $\text{HCO}^+$ ,  $\text{N}_2\text{H}^+$ ,  $\text{N}_2\text{D}^+$ , and  $\text{H}_3^+$  (and its deuterated isotopomers) relative to hydrogen nuclei in the low- $\zeta$  model. The dashed line depicts the CO snow surface, and the dotted lines depict the position where the X-ray ionization rate is  $5 \times 10^{-17}$  (the upper dotted line),  $1 \times 10^{-18}$  (the middle dotted line), and  $1 \times 10^{-19} \text{ s}^{-1}$  (the lower dotted line).

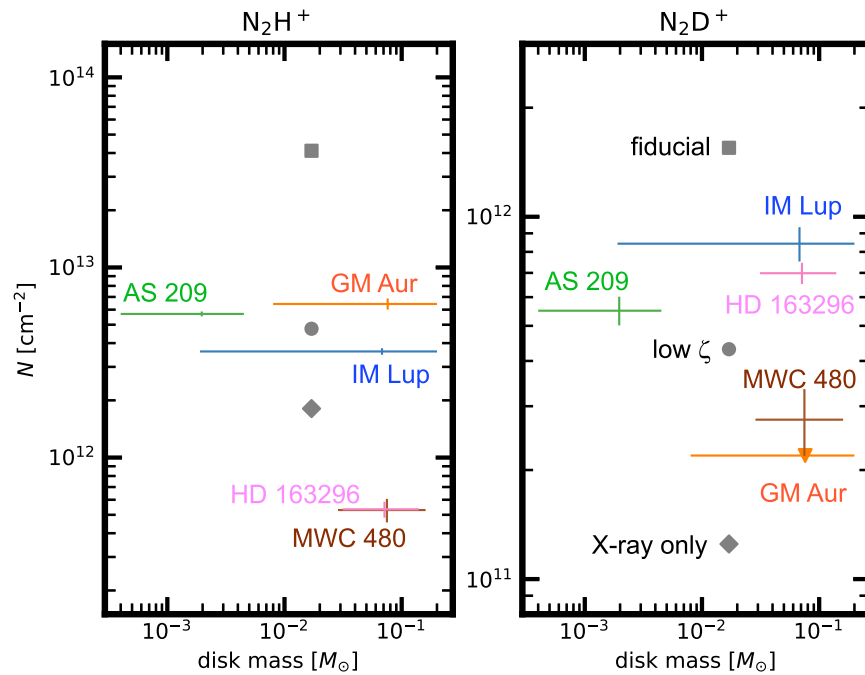
depicts the CO snow surface, and the dotted lines depict the position where the X-ray ionization rate is  $5 \times 10^{-17}$  (upper),  $1 \times 10^{-18}$  (middle), and  $1 \times 10^{-19} \text{ s}^{-1}$  (lower). We note that the dashed line and dotted lines are roughly parallel at radii  $>50$  au, probably because both parameters are controlled by the radiation transfer from the central star (i.e., stellar irradiation and X-rays). Inside the CO snow line (where the dashed line crosses the midplane), CO is indeed abundant near the midplane, although its abundance is reduced by an order of magnitude compared to the initial value ( $\sim 10^{-5}$ ) owing to the conversion to less volatile species such as  $\text{CO}_2$  ice. In this region, the  $\text{HCO}^+/\text{CO}$  abundance ratio is less than  $10^{-5}$  in the low- $\zeta$  model, which is also consistent with the observations. Comparing the  $\text{HCO}^+$  and the electron abundances, we can see that the former is slightly lower than the latter even in the layers where the  $\text{HCO}^+$  abundance peaks. This means that the ionization degree is actually higher than the  $\text{HCO}^+$  abundance; atomic ions are relatively abundant even in the CO-rich layer in the model.

Figure 10 shows the radial profiles of the column densities of CO (multiplied by  $10^{-5}$ ),  $\text{HCO}^+$ ,  $\text{N}_2\text{H}^+$ , and  $\text{N}_2\text{D}^+$  in the three models. As references, 2D distributions of absolute abundances (i.e., number densities) of major molecular ions in the low- $\zeta$  model are shown in Figure 11. Similar plots for the other two disk models are shown in Figure 20 in Appendix E. The column densities in the models are almost constant outside  $\sim 100$  au, while the observed values decline outward. This discrepancy might arise because the model gas density is not exponentially tapered, but simply follows a power law up to a radius of 284 au. We thus only compare the model column densities inside  $\sim 200$  au with the observed values. In all three models, the radial profile of the column density ratio  $N(\text{HCO}^+)/N(\text{CO})$  is similar to those in Figure 7;  $N(\text{HCO}^+)/N(\text{CO})$  is nearly constant ( $\sim 10^{-5}$ )

but declines toward the disk center inside a certain radius, which corresponds to the CO snow line in the disk models.

Figure 10 shows that at radii outside the CO snow line ( $\sim 20$  au in the template model) the  $\text{HCO}^+$  column density is not sensitive to  $\zeta_{\text{mid}}$ , since the contribution of the X-ray ionized region is significant in the CO-rich layer there (see Figures 11 and 20). Inside the CO snow line, the CO-rich layer extends to the midplane. The  $\text{HCO}^+$  column density and the gas column density ratio  $N(\text{HCO}^+)/N(\text{CO})$  around and inside the CO snow line are thus more sensitive to  $\zeta_{\text{mid}}$ .<sup>27</sup> The peak value of the  $\text{HCO}^+$  column density is lower in the low- $\zeta$  model than in the models with  $\zeta_{\text{mid}} = 5 \times 10^{-17} \text{ s}^{-1}$  by a factor of 4.6 (fiducial model) and 4.2 (high-C/O model). The column density ratio of  $\text{HCO}^+/\text{CO}$  at the  $\text{HCO}^+$  column density peak is also lower in the low- $\zeta$  model accordingly. Around the CO snow lines predicted from the thermochemical model of Zhang et al. (2021), the  $\text{HCO}^+$  column density derived from the observation is  $\gtrsim 10^{14} \text{ cm}^{-2}$  with the column density ratio of  $\text{HCO}^+/\text{CO} \sim 10^{-5}$  in our targeted disks, as in our fiducial model or high-C/O model, except for those around IM Lup and MWC 480. It may suggest  $\zeta_{\text{mid}} \sim 10^{-17} \text{ s}^{-1}$  around the CO snow line. We note, however, that the  $\text{HCO}^+$  column density would also depend on the total gas column density, which is not varied in the set of template models shown here. While the mass of the template disk model is within the range of estimated values for GM Aur and IM Lup, AS 209 is less massive and the disks around the Herbig Ae stars are more massive (Zhang et al. 2021) (see Section 4.4). Source-specific models are needed for further comparison.

<sup>27</sup> We note that the absolute abundance of  $\text{HCO}^+$  in the midplane is high even at radii slightly outside the CO snow line. For  $\text{HCO}^+$  to be the abundant ion, CO does not need to fully sublimate to the gas phase (Aikawa et al. 2015).



**Figure 12.** The  $\text{N}_2\text{H}^+$  and  $\text{N}_2\text{D}^+$  column densities as a function of disk mass. For each disk, a mass range adopted from Zhang et al. (2021) is shown as the horizontal error bar. The column densities correspond to the peak values, with the error bars indicating the 16th and 84th percentiles. For  $\text{N}_2\text{D}^+$  in GM Aur, we instead plot the 99.85th percentile at  $\sim 100$  au as an upper limit. Predictions from the template models are shown by the gray points.

#### 4.4. Ionization Rate Traced by $\text{N}_2\text{H}^+$ and $\text{N}_2\text{D}^+$

The template disk models (Figures 10, 11, and 20) indicate that, in contrast to  $\text{HCO}^+$ , the column densities of  $\text{N}_2\text{H}^+$  and  $\text{N}_2\text{D}^+$  are more sensitive to the ionization rate below the CO snow surface, where these molecular ions are relatively abundant. In the cold midplane,  $\text{H}_3^+$  and its deuterated isotopomers are the most abundant ions, but  $\text{H}_3^+$  and  $\text{D}_3^+$  are not observable at radio wavelengths, and  $\text{H}_2\text{D}^+$  and  $\text{HD}_2^+$  are not detected so far, possibly due to unfavorable o/p ratios (e.g., Chapillon et al. 2011). Figure 20 shows that among the observable molecular ions,  $\text{N}_2\text{D}^+$  is the best proxy of deuterated  $\text{H}_3^+$  and thus the best probe of ionization rate in the midplane. Although its abundance is lower than the sum of  $\text{H}_3^+$  and its deuterated isotopomers, the gas above the CO snow surface does not significantly contribute to its column density in our template disk models. In the template disk models, the  $\text{N}_2\text{H}^+$  and  $\text{N}_2\text{D}^+$  column densities have a peak around  $R \sim 50$  au, where these molecular ions are abundant in the midplane (see also Qi et al. 2019). This indicates that  $\zeta_{\text{mid}}$  could be best investigated by their peak column densities, especially by the  $\text{N}_2\text{D}^+$  column density.

The column densities of  $\text{N}_2\text{H}^+$  and  $\text{N}_2\text{D}^+$  in our target disks are derived by Cataldi et al. (2021) and are plotted in Figure 8. As expected from the template disk models, these column densities have a peak outside the CO snow line, except for GM Aur, for which the  $\text{N}_2\text{H}^+$  column density is the highest at the innermost radial grid. The value at the innermost grid could, however, be overestimated, since these column densities are derived by assuming a fixed excitation temperature of 20 K. When the excitation temperature is set to be the same as the midplane temperature of the thermochemical model of Zhang et al. (2021), the  $\text{N}_2\text{H}^+$  column density has a peak ( $\sim 10^{13} \text{ cm}^{-2}$ ) around  $R \sim 100$  au (Cataldi et al. 2021).

Unlike  $\text{HCO}^+$ , the distributions of  $\text{N}_2\text{H}^+$  and  $\text{N}_2\text{D}^+$  are expected to anticorrelate with that of CO. We thus consider their column densities rather than the column density ratio to CO.

In Figure 12, we plot the peak  $\text{N}_2\text{H}^+$  and  $\text{N}_2\text{D}^+$  column densities derived by Cataldi et al. (2021) versus disk mass to see whether there is any trend. For each disk, a range of possible masses is shown, extending from the minimum masses to the best-fit mass given in Tables 3 and 2 of Zhang et al. (2021), respectively. While the estimated disk masses of IM Lup, GM Aur, HD 163296, and MWC 480 overlap with each other,<sup>28</sup> their  $\text{N}_2\text{H}^+$  and  $\text{N}_2\text{D}^+$  peak column densities vary, which indicates that the midplane ionization rate varies among the disks. The gray squares and circles depict the peak column densities around  $R \sim 50$  au in the fiducial model and low- $\zeta$  model, respectively. The gray diamonds show the values in the model with X-ray ionization only, i.e., the midplane ionization rate is  $\lesssim 10^{-19} \text{ s}^{-1}$ . The peak column densities of the high-C/O model are not plotted but are similar to those of the fiducial model.

The  $\text{N}_2\text{H}^+$  column densities of IM Lup, GM Aur, and AS 209 indicate  $\zeta_{\text{mid}} \sim 10^{-18} \text{ s}^{-1}$ . For MWC 480 and HD 163296, the  $\text{N}_2\text{H}^+$  column density is lower than that of the X-ray-only model, which indicates that the X-ray ionization is less effective in these disks than in our template models. We note that a fraction of  $\text{N}_2\text{H}^+$  exists in the layer with relatively high X-ray ionization rate ( $\gtrsim 5 \times 10^{-17} \text{ s}^{-1}$ ), which sets the floor value of the  $\text{N}_2\text{H}^+$  column density in our template models. For MWC 480, the low  $\text{N}_2\text{H}^+$  column density is consistent with its soft X-ray spectrum and relatively low  $\text{HCO}^+$  column density. An alternative explanation for the variety of  $\text{N}_2\text{H}^+$  column density would be the temperature structure in the disk. The column density of  $\text{N}_2\text{H}^+$  should be lower if the midplane layer of the low temperature ( $\lesssim 20$  K) is thinner (Qi et al. 2019). This could be the case for the MWC 480 disk, in which both  $\text{N}_2\text{H}^+$  and  $\text{N}_2\text{D}^+$  column densities are

<sup>28</sup> Fedele et al. (2018) reproduced their 1.3 mm dust continuum image with a disk model with a dust mass of  $3.5 \times 10^{-4} M_{\odot}$ . If the gas-to-dust mass ratio is 100, the disk mass of AS 209 is also similar to the disk mass of IM Lup and GM Aur.

low. HD 163296, on the other hand, has relatively high column density of  $N_2D^+$ , which indicates that there is plenty of cold gas in the midplane (see below).

The  $N_2D^+$  peak column densities of IM Lup, AS 209, and HD 163296 are similar to or slightly larger than the value from the low- $\zeta$  model, which suggests  $\zeta_{\text{mid}} \gtrsim 10^{-18} \text{ s}^{-1}$ . In the HD 163296 disk, the peak  $N_2D^+$  column density is relatively high, while the low  $N_2H^+$  column density indicates lower X-ray ionization rate than the template models. The midplane ionization rate, which is better traced by  $N_2D^+$ , would thus be set by SLRs or high-energy particles. In GM Aur, on the other hand, the upper limit of  $N_2D^+$  column density indicates a low ionization rate ( $<10^{-18} \text{ s}^{-1}$ ) in the midplane.

Finally, we note that the  $N_2H^+$  and  $N_2D^+$  column densities depend not only on  $\zeta_{\text{mid}}$  but also on other parameters such as the vertical temperature distribution and the disk mass (Cleeves et al. 2014; Qi et al. 2019). Source-specific models are needed to estimate the midplane ionization rate more quantitatively for each object.

## 5. Conclusions

We observed and analyzed  $HCO^+ J=1-0$  and  $H^{13}CO^+ J=1-0$  lines toward the protoplanetary disks around IM Lup, GM Aur, AS 209, HD 163296, and MWC 480.  $H^{13}CO^+ J=1-0$  was detected in all five disks, while  $H^{13}CO^+ J=1-0$  was detected ( $S/N > 6\sigma$ ) toward GM Aur and HD 163296 and tentatively detected ( $S/N > 3\sigma$ ) toward the other disks by a matched filter analysis in the  $u$ - $v$  plane. The disk-integrated flux of  $H^{13}CO^+ J=1-0$  is also above  $3\sigma$  in IM Lup, GM Aur, and HD 163296.

We derived the  $HCO^+$  column density by fitting the azimuthally averaged spectra of  $HCO^+$  and  $H^{13}CO^+$  simultaneously for radial bins of half the beam FWHM. In all five disks, the  $HCO^+$  column density increases inward but becomes flat or drops toward the center inside a radius of  $R \sim 100$  au. The column density ratio of  $N(HCO^+)/N(CO)$  is about  $10^{-5}$ – $10^{-4}$  at  $R \gtrsim 100$  au, except for the MWC 480 disk, in which the column density ratio is  $<10^{-5}$  at  $R \lesssim 200$  au.

We derived the  $HCO^+$  abundance in the warm CO-rich layer, where  $HCO^+$  is expected to be the dominant molecular ion, via the column density ratio  $N(HCO^+)/N(CO)$  using the radial profiles of CO column density and CO depletion factor from Zhang et al. (2021). Beyond  $\sim 100$  au, the derived  $HCO^+$  abundance ranges from  $3 \times 10^{-11}$  to  $3 \times 10^{-10}$  in the IM Lup, GM Aur, and HD 163296 disks. The  $HCO^+$  abundance is lower in MWC 480, possibly due to the lack of high-energy ( $>$  a few keV) X-rays. The  $HCO^+$  abundance tends to decline toward the disk center for  $R \lesssim 100$  au. This can be explained by the lower ionization degree in denser gas, especially inside the CO snow line, where the CO-rich layer is in the midplane.

We find a hint of a correlation between the  $HCO^+$  abundance and the gap carved by a putative planet in AS 209: the  $HCO^+$  abundance exceeds  $10^{-9}$  at  $R \sim 50$ – $150$  au, where the CO column density is depressed. This region seems to correspond to the gas gap, where ionization would be more efficient. In HD 163296, the  $HCO^+$  abundance shows a shallow bump at 100–150 au, which coincides with the radius of DCO<sup>+</sup> enhancement found by Flaherty et al. (2017). This feature could also be related to the enhanced ionization around a gas gap. In MWC 480, the  $HCO^+$  column density has a local maximum at  $\sim 76$  au, which coincides with the local depression of CO and the gap seen in the dust continuum.

Finally, we compared the column densities of  $HCO^+$ ,  $N_2H^+$ , and  $N_2D^+$  with those of template disk models: a fiducial disk model with a midplane ionization rate  $\zeta_{\text{mid}}$  of  $5 \times 10^{-17} \text{ s}^{-1}$ , a model with CO and  $H_2O$  depletion, and a model with  $\zeta_{\text{mid}} = 1 \times 10^{-18} \text{ s}^{-1}$ . The almost constant  $HCO^+$  abundance at  $R \gtrsim 100$  au is explained by X-ray ionization in the CO-rich layer. The decline of the  $HCO^+$  abundance at the inner radii, on the other hand, can be explained by CO sublimation inside the CO snow line; the CO-rich layer then extends to the midplane, where the ionization degree is low owing to high density. While the estimated disk mass ranges of IM Lup, GM Aur, HD 163296, and MWC 480 overlap with each other, their peak column densities of  $N_2H^+$  and  $N_2D^+$  vary, which may indicate that the midplane ionization rate varies among disks. The peak  $N_2D^+$  column density suggests a midplane ionization rate of  $\gtrsim 10^{-18} \text{ s}^{-1}$  for IM Lup, AS 209, and HD 163296, while the upper limit of  $N_2D^+$  column density indicates that it is  $<10^{-18} \text{ s}^{-1}$  for GM Aur. The peak column density of  $N_2H^+$  is lower in MWC 480 than in other disks, which is consistent with its soft X-ray spectrum and relatively low  $HCO^+$  column density. Alternatively, the low column densities of  $N_2H^+$  and  $N_2D^+$  in the MWC 480 disk could be due to its warmer temperature, i.e., the cold midplane layer is thinner than in other disks. Source-specific models are needed for further evaluation of the midplane ionization rate.

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Facility: ALMA.

*Software:* Astropy (Astropy Collaboration et al. 2013; Price-Whelan et al. 2018), bettermoments (Teague & Foreman-Mackey 2018), CASA (McMullin et al. 2007), emcee (Foreman-Mackey et al. 2013), gofish (Teague 2019), matplotlib (Hunter 2007), NumPy (van der Walt et al. 2011), pythonradex (<https://github.com/gica3618/pythonradex>), SciPy (Virtanen et al. 2020), SPECTCOL (VAMDC Consortium, <http://www.vamdc.org>), VISIBLE (Loomis et al. 2018).

## Appendix A

### Hybrid Zeroth-moment Maps with a $0''.5$ Beam

While we used the data cubes tapered to a circular  $0''.3$  beam for the analysis, faint emission is better recognized in images with lower spatial resolution. Since Band 3 lines tend to be fainter than Band 6 lines, the MAPS collaboration also produced the data cube tapered to a circular  $0''.5$  beam for Band 3 lines (Öberg et al. 2021; Czekala et al. 2021). Figure 13 shows the hybrid zeroth-moment maps of the  $J = 1 - 0$  lines of  $\text{HCO}^+$  and  $\text{H}^{13}\text{CO}^+$  tapered to a circular  $0''.5$  beam. All maps were produced by combining a Keplerian mask and a smoothed  $0\sigma$ -clip mask (Law et al. 2021a).

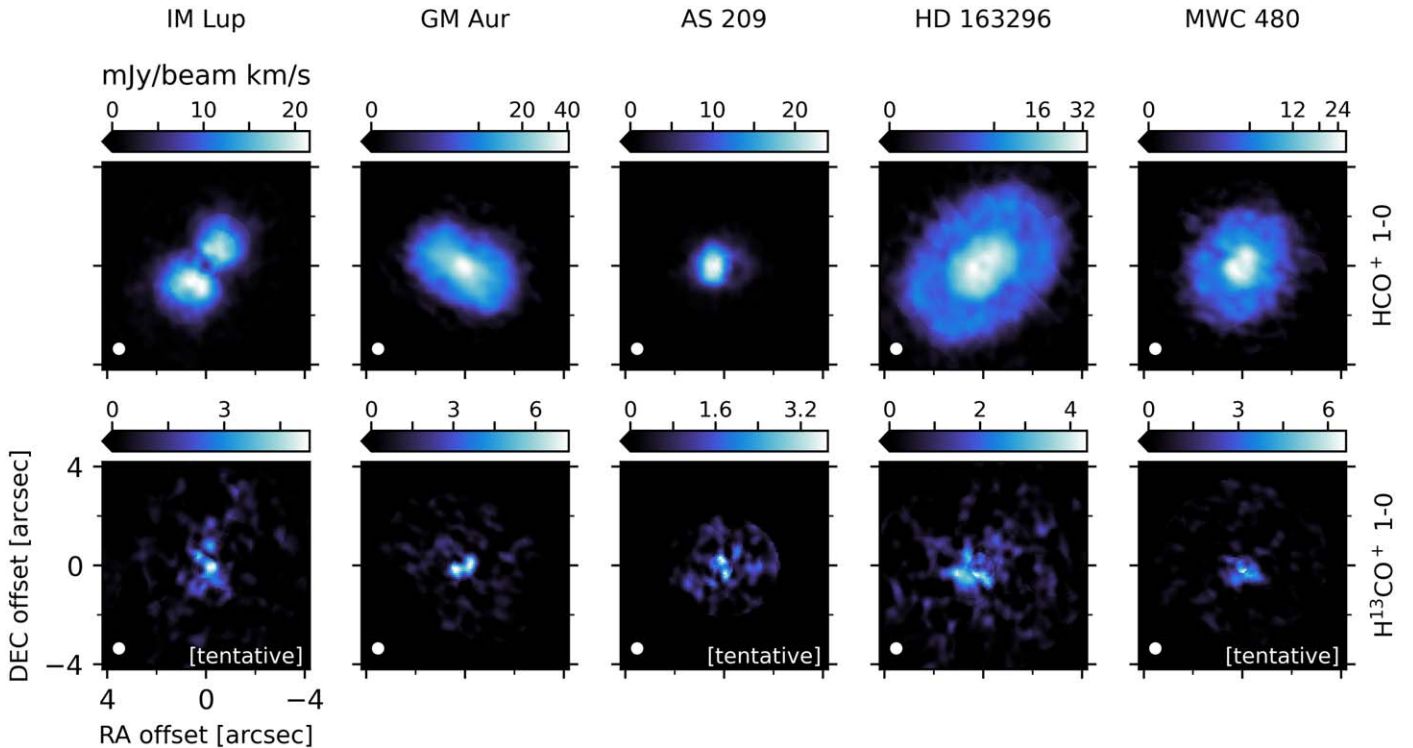


Figure 13. Same as Figure 2, but for images tapered to a circular  $0''.5$  beam.

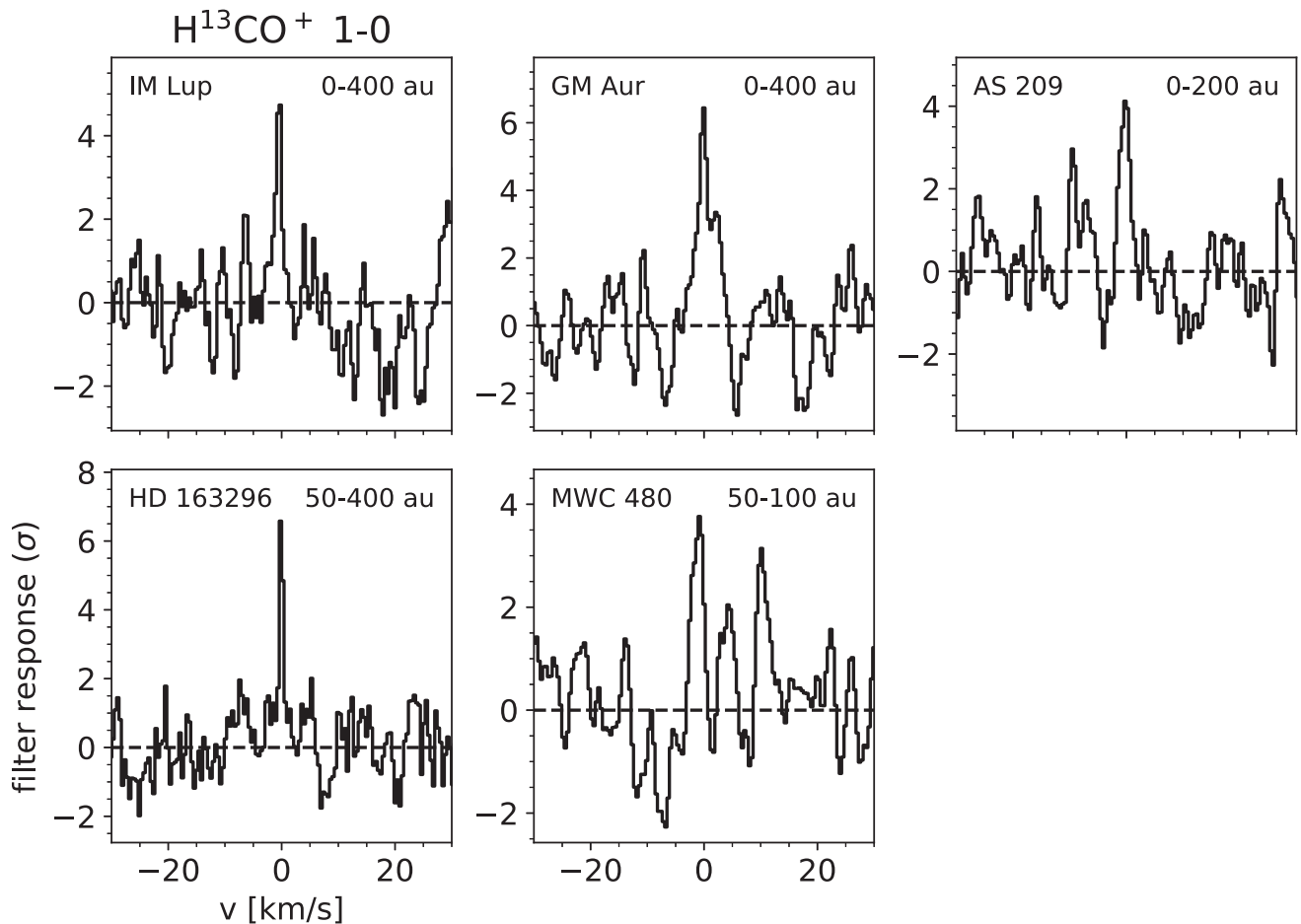
## Appendix B

### Matched Filter Analysis and Disk-integrated Spectra for $\text{H}^{13}\text{CO}^+ J=1-0$

The  $J=1-0$  line of  $\text{H}^{13}\text{CO}^+$  is not clearly seen in our zeroth-moment maps (Figure 2), radial emission profiles (Figure 3), or azimuthally averaged spectra (Figure 16). To test whether the line is detected, we applied a matched filter analysis in the  $u$ - $v$  plane (Loomis et al. 2018; see also Czekala et al. 2021). We calculate the visibilities of a Keplerian disk model, which are then cross-correlated with the observed visibilities to produce a response for each channel of the data. The response spectrum is then divided by the rms of the response spectrum at signal-free regions. Since we do not know the radial distribution of the emission, we computed the filter response for a series of Keplerian disk models with varying radial extents to find the Keplerian model that maximizes the

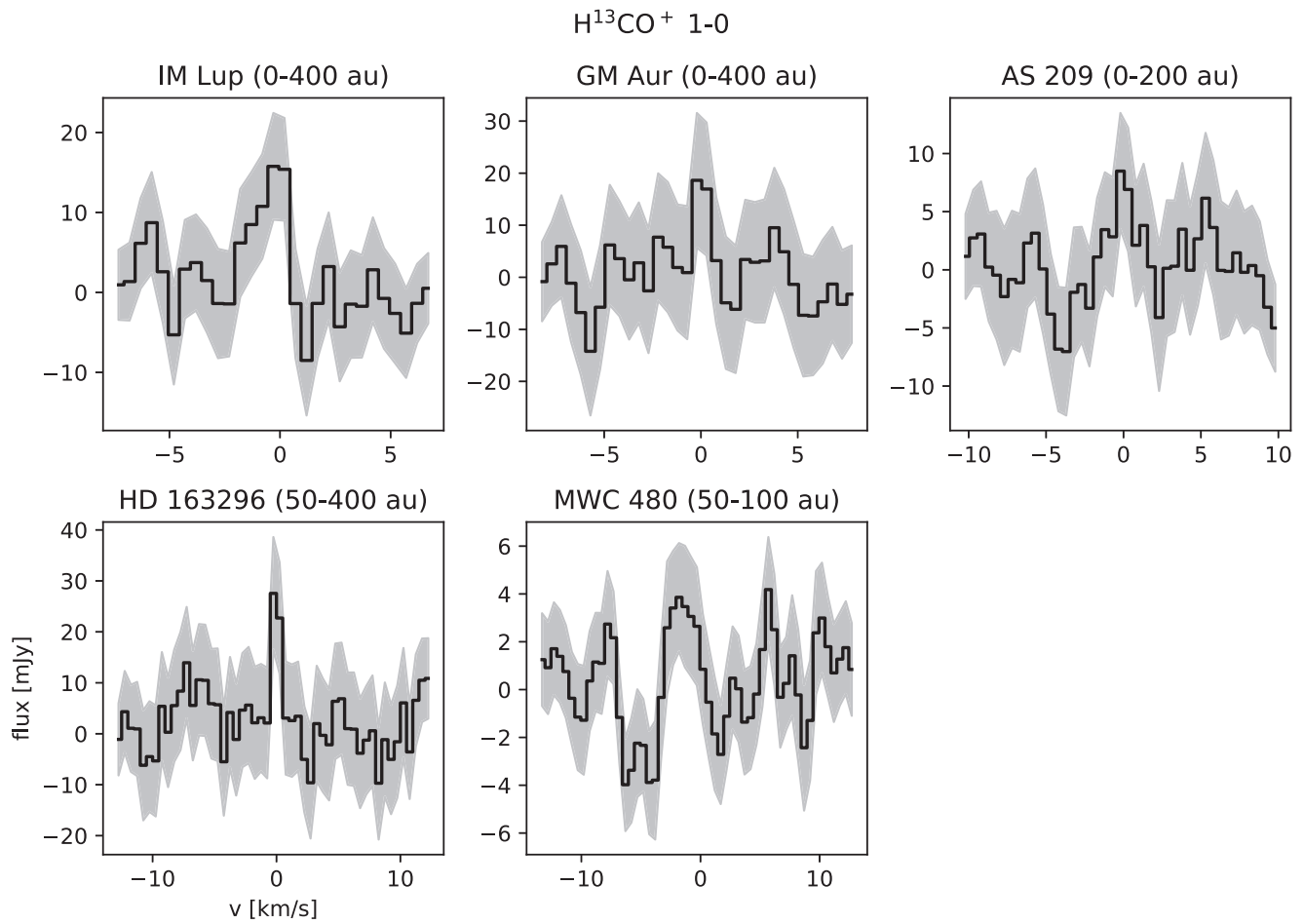
S/N at the systemic velocity. Figure 14 shows the matched filter responses with the maximum S/N, while the radial extent of the corresponding Keplerian disk models is shown in the figure and also listed in Table 2. We note that the radial extent of the Keplerian disk model roughly represents the radial extent of the emission.  $\text{H}^{13}\text{CO}^+ J=1-0$  is detected with an S/N above  $6\sigma$  for GM Aur and HD 163296. The line is tentatively detected with an S/N above  $3\sigma$  for IM Lup, AS 209, and MWC 480.

In Figure 15 we show the shifted and azimuthally averaged, disk-integrated  $\text{H}^{13}\text{CO}^+ J=1-0$  spectrum of each disk. The radial extent of the region over which we averaged is the same as for the matched filter. The disk-integrated spectra also point toward a detection in GM Aur and HD 163296, although at lower significance than the matched filter. In summary, we detect  $\text{H}^{13}\text{CO}^+ J=1-0$  toward GM Aur and IM Lup and tentatively detect it toward the other three disks.



**Figure 14.** Matched filter response for  $\text{H}^{13}\text{CO}^+ J=1-0$ . For each disk, we chose the Keplerian mask with the radius that maximized the S/N. The radial extent of that model is indicated in the upper right corner of each panel. The y-axis is in units of the noise in the filter response.

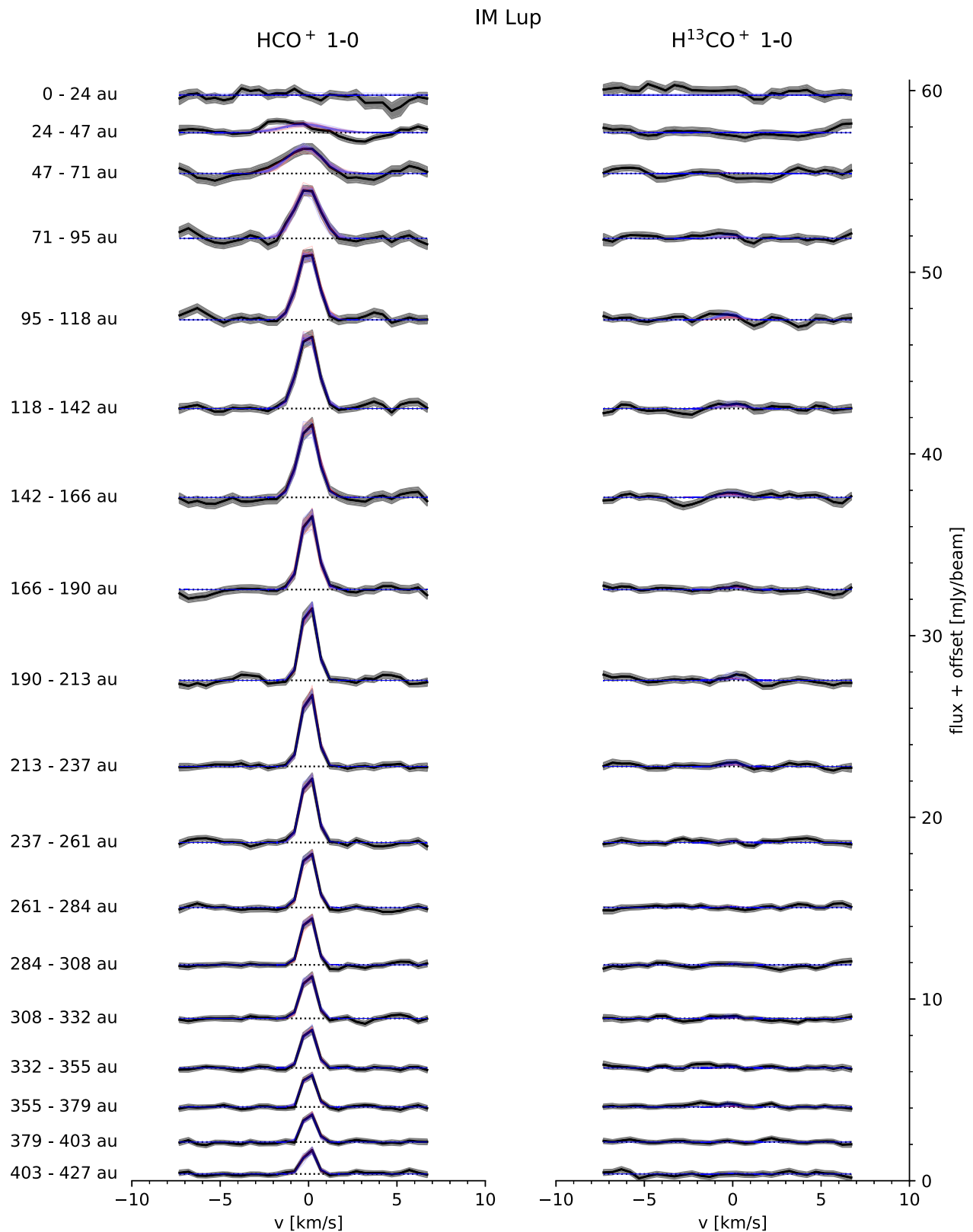




**Figure 15.** Disk-integrated spectra (over the radial range indicated in the title of each panel) of  $\text{H}^{13}\text{CO}^+ J = 1 - 0$ . The spectrum at each spatial location of the data cube was shifted to the systemic velocity prior to integration. The shaded region corresponds to the  $1\sigma$  error.

### Appendix C Azimuthally Averaged Spectra

Figure 16 shows the azimuthally averaged spectra of  $\text{HCO}^+$  and  $\text{H}^{13}\text{CO}^+ J = 1 - 0$ , together with model spectra from the MCMC fits.



**Figure 16.** The black curves show azimuthally averaged spectra for IM Lup. Spectra are vertically offset for clarity. The shaded region marks the  $1\sigma$  error. The horizontal dotted line marks the zero flux level. For each spectrum, we show 20 randomly selected model spectra from the MCMC with the blue curves ( $T_{\text{ex}}$  as free parameter) and the red curves ( $T_{\text{ex}}$  fixed to 30 K). The selection probability of each model was set proportional to its posterior probability. Most of the time, the model spectra overlap closely, so that only the blue curves are visible.

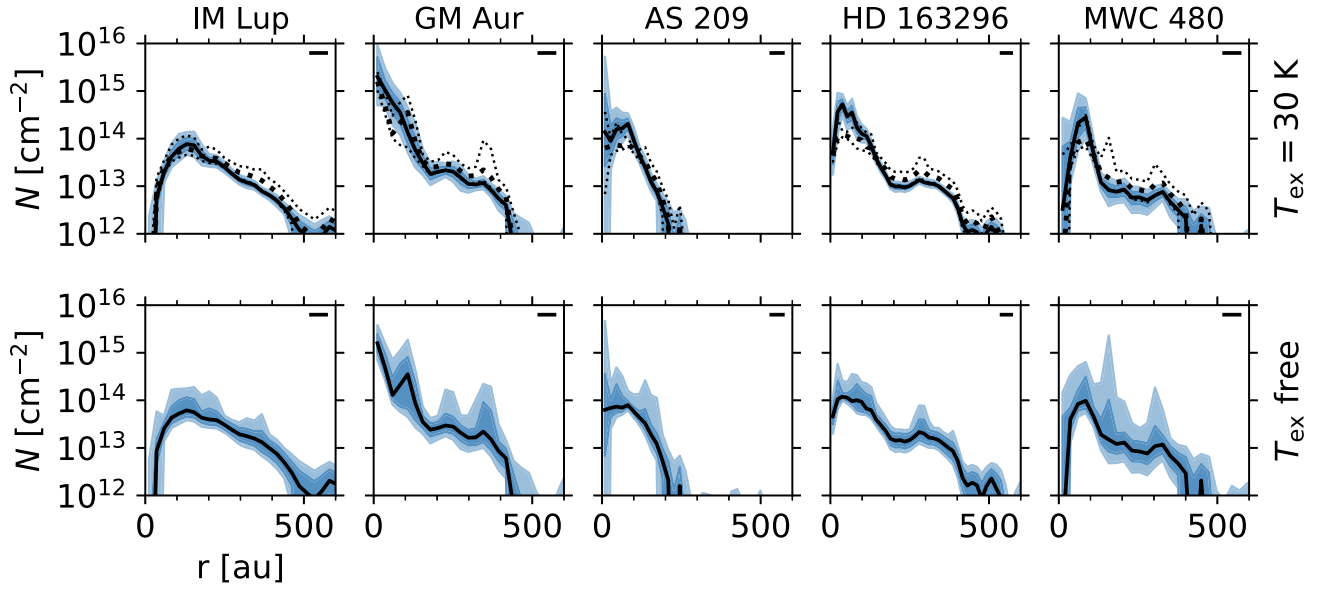
(The complete figure set (7 images) is available.)

### Appendix D

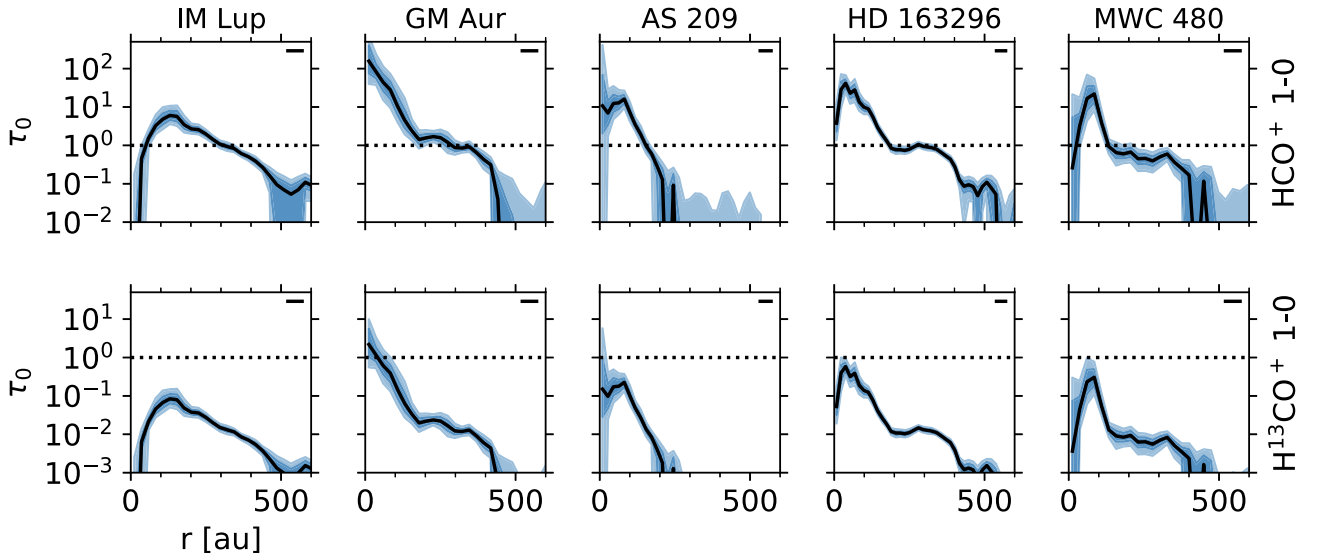
#### Dependence of $\text{HCO}^+$ Column Density on Assumed Excitation Temperature

In our fiducial fits, the excitation temperature is a free parameter. In order to explore the dependence of our results on the excitation

temperature, we performed additional fits where the excitation temperature is fixed to 30 K. Figure 17 displays a comparison of the column density profiles derived from the different fits. The comparison is discussed in Section 3.2. Figure 18 shows the optical depth profiles derived assuming  $T_{\text{ex}} = 30$  K.



**Figure 17.** The column density of  $\text{HCO}^+$  assuming an excitation temperature of 30 K (top row) and for our fiducial fits where  $T_{\text{ex}}$  is a free parameter (bottom row). The black solid lines mark the median, while the shading encompasses the regions from the 16th to 84th percentile and from the 2.3th to 97.7th percentile, respectively. To ease comparison, in the top panel, the thick and thin black dotted lines mark the median and the 16th and 84th percentiles of the fits where  $T_{\text{ex}}$  is a free parameter.



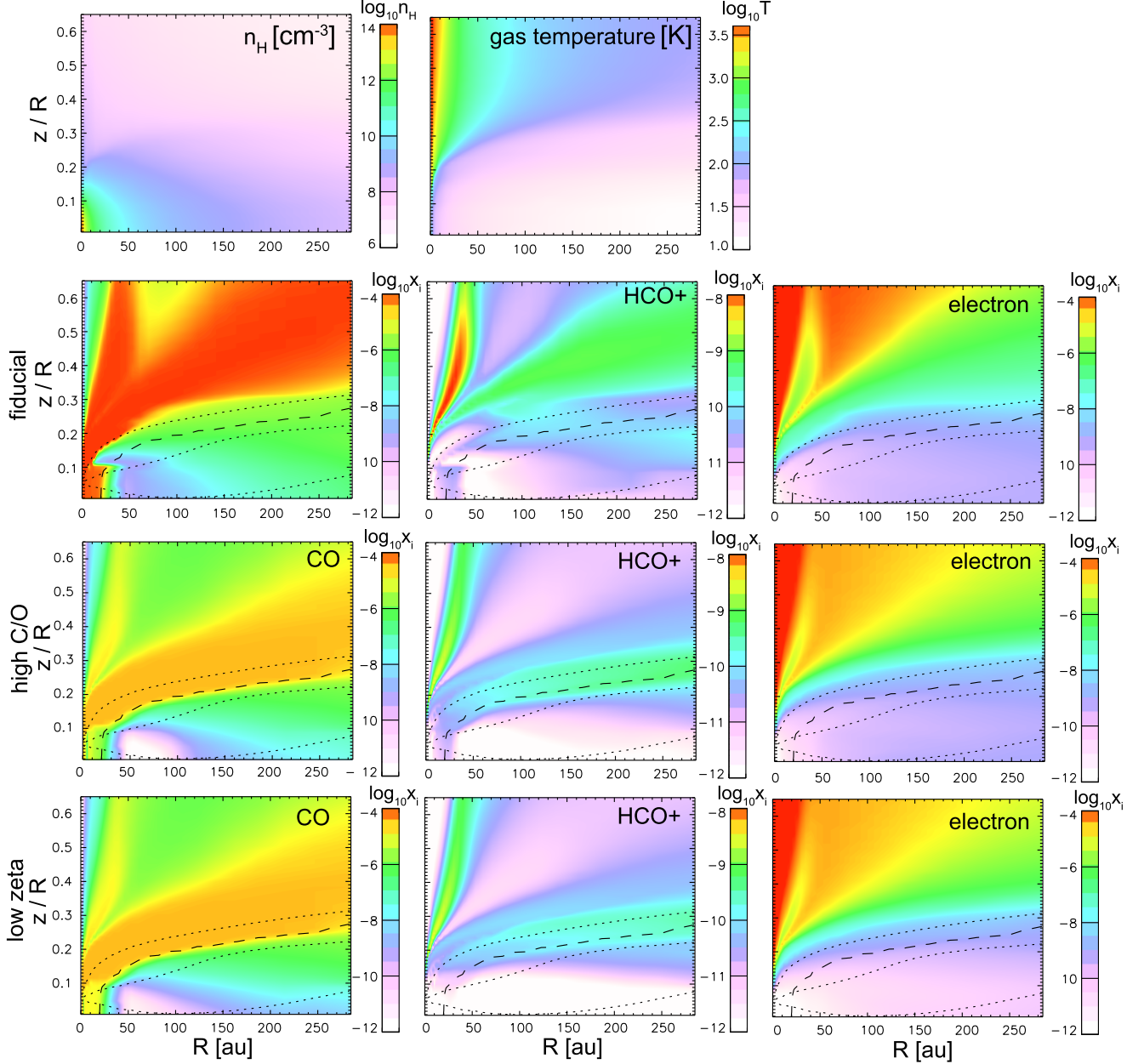
**Figure 18.** Optical depth profiles of  $\text{HCO}^+$  ( $J = 1 - 0$ ) and  $\text{H}^{13}\text{CO}^+$  ( $J = 1 - 0$ ) derived from fitting azimuthally averaged spectra assuming  $T_{\text{ex}} = 30$  K. The black lines mark the median, while the shading encompasses the regions from the 16th to 84th percentile and from the 2.3th to 97.7th percentile, respectively.

### Appendix E Template Disk Chemistry Models

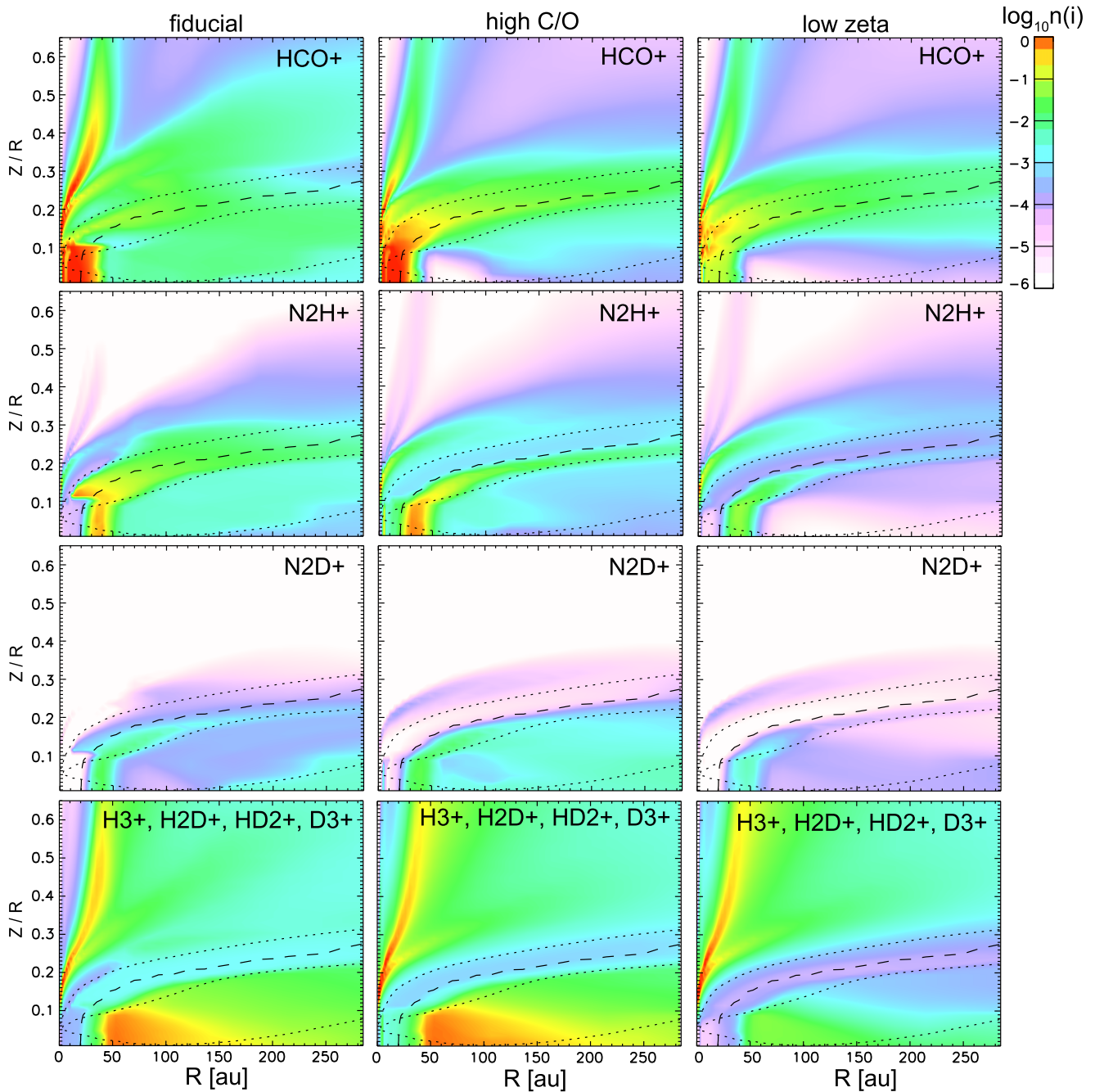
The top panels in Figure 19 show the 2D ( $R, Z$ ) distributions of the number of hydrogen nuclei and gas temperature in the template disk model. The panels in the second row show the abundances of gaseous CO,  $\text{HCO}^+$ , and electrons relative to hydrogen nuclei in the fiducial model. The panels in the third

and fourth rows are for the high-C/O model and the low- $\zeta$  model, respectively.

Figure 20 shows the absolute abundances (i.e., number density) of  $\text{HCO}^+$  (top row),  $\text{N}_2\text{H}^+$  (second row),  $\text{N}_2\text{D}^+$  (third row), and  $\text{H}_3^+$  and its deuterated isotopomers (fourth row) in the fiducial model (left), the high-C/O model (middle), and the low- $\zeta$  model (right).



**Figure 19.** Number density of hydrogen nuclei ( $n_{\text{H}}$ ) and gas temperature of the template disk model are shown in the top row. Furthermore, we show the abundances of CO (left column),  $\text{HCO}^+$  (middle column), and electrons (right column) relative to hydrogen nuclei in the fiducial model (second row), the CO-depleted model (third row), and the model without CR ionization (low- $\zeta$  model; bottom row).



**Figure 20.** Absolute abundance (i.e., number density in units of  $\text{cm}^{-3}$ ) of major molecular ions in the fiducial disk model (left column), high-C/O model (middle column), and low- $\zeta$  model (right column).

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