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An interpretable multi-stage forecasting framework for energy consumption and CO₂ emissions for the transportation sector

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Abstract:

The transportation sector is deemed one of the primary sources of energy consumption and greenhouse gases throughout the world. To realise and design sustainable transport, it is imperative to comprehend relationships and evaluate interactions among a set of variables, which may influence transport energy consumption and CO₂ emissions. Unlike recent published papers, this study strives to achieve a balance between machine learning (ML) model accuracy and model interpretability using the Shapley additive explanation (SHAP) method for forecasting the energy consumption and CO₂ emissions in the UK's transportation sector. To this end, this paper proposes an interpretable multi-stage forecasting framework to simultaneously maximise the ML model accuracy and determine the relationship between the predictions and the influential variables by revealing the contribution of each variable to the predictions. For the UK's transportation sector, the experimental results indicate that road carbon intensity is found to be the most contributing variable to both energy consumption and CO₂ emissions predictions. Unlike other studies, population and GDP per capita are found to be uninfluential variables. The proposed multi-stage forecasting framework may assist policymakers in making more informed energy decisions and establishing more accurate investment.

Keywords: Energy consumption forecasting, CO_2 emissions forecasting, Transportation sector, Machine learning, Feature selection.

1 Introduction

1.1 Background

Over the last decades, energy consumption (EngCons) and carbon dioxide emissions (CO₂E) challenges have been the primary issues for policymakers. This was because of the impact of energy usage on national economic growth as well as the impact of carbon on human health. In parallel with economic and social enhancements, energy demand has risen worldwide. Correspondingly, the rapidly increasing level of the human population, socioeconomic improvement, urbanization, and scientific developments have cumulatively led to an increase in worldwide EngCons and CO₂E in numerous sectors [1, 2]. The world CO₂E for different transportation sectors is provided in Figure 1. Although CO₂E is increasing until 2025, they will continue to decrease dramatically until 2070.

In the United Kingdom (UK), almost all transportation sectors must decarbonize to fulfill the economywide net-zero commitment. Due to a continual increase throughout vehicle kilometers traveled, transportation CO₂ peaked in 2007, 8.4% greater compared to 1990. Since then, emissions through the transportation sector have dropped back to around 1990 levels up till 2019, primarily due to enhancements in new vehicle energy efficiency and reduced transportation growth compared to prior years due to a dip following the 2008/2009 recession [3]. According to the Energy Stats [4], although in 2020 the UK government observed significant falls in energy usage for almost all vehicle forms, with the most considerable reduction in buses and automobiles transport remains the most significant part of energy usage throughout the UK.

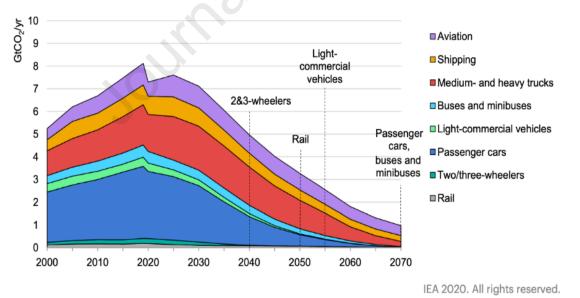


Figure 1. World CO₂E for different transportation modes [5].

A range of machine learning (ML) models can be utilized to estimate EngCons and CO₂E, including multiple linear regression (MLR) [6, 7], logistic regression [8], generalized linear models [9], time series analysis [10, 11], artificial neural networks (ANN) [12-14], deep learning [15-17], support vector machine (SVM) [18, 19], decision tree, random forest (RF) [20, 21], hybrid methods [22, 23], to name

a few. Despite extensive research having been conducted using ML models to forecast EngCons and CO_2E , it is noticed that limited attention has been focused on the transport sector of the UK. For instance, Piecyk and McKinnon [24] conducted a study in 2010 to forecast the carbon footprint of road freight transport in 2020, factors affecting freight transport demand, truck fuel consumption and related CO_2E were discussed. However, their research only focused on part of the transport sector and is now out-of-date, which diminishes the value of their research for policymakers in decision-making. Logan et al. [25] conducted a similar study where they estimated the energy demand of road transport including cars, buses and trains. The energy consumption of the transport sector failed to meet the needs of UK Transport Vision 2050 [26].

Furthermore, as review of literature indicates, previous studies have explored forecasting the EngCons and/or CO₂E, which preselected a small number of features without any strong justification and rationale on how and why those set of features are selected. Because of a small number of preselected features, unlike many studies in other energy forecasting domains, no study has employed FS methods to select the combination of features which can lead to high accuracy of ML models. In addition, only one study [27] has used interpretable ML to forecast the EngCons and CO₂E to determine the influential variables. Therefore, as one of the most crucial needs, the transportation sector is calling for an interpretable multi-stage framework to accurately forecast the EngCons and CO₂E and to systematically evaluate the effects of different types of features.

1.2 Novelty and contributions

The novelty and contributions of this study in comparison with recently published works in forecasting EngCons and CO_2E in transportation sector can be concluded as follows:

- This study considers multi-source data in the UK's transportation sector by integrating three categories of variables (features) including socioeconomic, transportation- and energy-related variables. Neither of published papers used a large list of input features and performed correlation and multicollinearity analyses to remove highly correlated features to provide an appropriate subset of features for interpretability of black-box ML models. All previous works preselected a small number of features without any strong justification and rationale on how and why those set of features are selected.
- Previous studies in the literature used neither filter/embedded methods to select the input features holding strong relationship with the EngCons and CO₂E, nor wrapper methods to select the features which can lead to high accuracy of ML models. This study introduces a novel voting scheme for feature selection (FS), which combines both filter and embedded paradigms, which has not been studied before in the EngCons context.

• The other contribution is to propose an interpretable ML-based forecasting framework, which is depicted in Fig 2. The proposed generalised framework integrates multi-stage FS procedure with ML models to simultaneously achieve more accurate forecasts and more reliable interpretation of black-box ML models using Shapley additive explanation (SHAP) analysis proposed by Lundberg et al. [61]. SHAP is a method employed for interpreting the output of ML models, which is briefly described in Section 3.7. Although the SHAP analysis has recently found applications in energy-related fields [27-29], more work is required to demonstrate the practicality and usefulness of SHAP analysis in interpretable ML models for forecasting EngCons and CO₂E. To the best of our knowledge, this study is the second work in EngCons context (the first study is Aras and Van [30], however, they overlooked the fact that investigation of multicollinearity in their study is crucial) that applies the SHAP analysis to forecast the EngCons and CO₂E to determine the influential variables contributing to the predictive performance.

It is worth mentioning that the proposed methodology is designed for any ML-based forecasting problems, in which simultaneously selecting as few features as possible for interpretability of ML models (or any other reasons) and achieving an acceptable model accuracy are desired. Multiple stages of FS procedure are so insightful on how different features are influencing and interacting with each other.

This paper is organised as follows. Section 2 reviews literature of the existing study regarding EngCons and CO₂E. Section 3 introduces the forecasting framework according to the integrated multi-stage FS methods and ML models. In Section 4, the case study and experimental settings are described. In Section 5, the analyses of experimental results are described along with Shapley Analysis to demonstrate the usefulness and benefits of the proposed framework. Section 6 briefly presents some noticeable discussion and lastly, concluding statements are provided in Section 7.

2 Literature review

2.1 Feature selection for energy forecasting

Multivariate ML-based forecasting models work based on selecting a set of potentially influencing features. As it is discussed in Section 2.2 only Wang et al. [31] used FS method for forecasting CO₂E and EngCons in transportation sector which in contrast to previous studies that have typically chosen a limited number of key features, such as population, GDP, and total number of vehicles, without providing a clear rationale or justification for their selection.

An appropriate FS procedure is crucial in forecasting CO₂E and EngCons. A summary of a few recent studies considering the FS methods in different energy fields is provided as follows. Jurado et al. [32] compared several ML techniques for energy prediction inside houses. They suggested a hybrid strategy that combines FS methods using soft computing and ML models, i.e., fuzzy, RF, and ANN. Feng et al. [33] developed a method for wind prediction using the ML approach. A FS structure was established to identify the most appropriate inputs for the ML approach. An organised FS method for establishing house energy prediction was suggested by Zhang and Wen [34].

The power usage of appliances was forecasted by Moldovan and Slowik [35] utilizing binary grey wolf optimization, in which the best features were selected utilizing the RF, KNN, decision tree, and extra tree methods. Qiao et al. [36] suggested a framework for house energy usage forecasting, depending on FS techniques. Lv and Wang [37] offered an efficient short-term wind speed prediction model by taking into account the impact of several meteorological variables. The filter-wrapper method integrating K-medoid clustering was developed to choose crucial meteorological elements. In the above papers, experimental results indicated that the ML models utilizing the FS methods typically have greater generalization and precision than those without FS.

2.2 ML for energy forecasting

Over the past few years, many forecasting models have been developed to predict EngCons and CO2E in different sectors. In this section, we briefly review the papers which investigated ML-based forecasting in the transportation sector in recent years. Readers can refer to [2,38] to study more references. Wang et al. [39] developed an ML model for transportation emissions utilizing the SVM, GPR, and ANN algorithms. Sahraei et al. [40] forecasted transportation energy usage utilizing the multivariate adaptive regression splines (MARS) method for 45 years after 1975 in Turkey.

Li et al. [41] utilised an ML model to predict Australia's vehicle gasoline usage utilizing an autoregressive and structural method. The outcomes of a prediction regarding gasoline usage for 2019-2020 demonstrate the outstanding prediction performance of the ML model. Ağbulut [2] utilised three ML models, i.e., ANN, SVM, and deep learning to predict transport energy usage and CO2E. Results showed that CO2E and energy usage through the transport sector will rise by almost 3.4 times more by 2050 than today. Sahraei and Çodur [23] suggested hybrid methods, ANN-PSO, ANN-Simulated Annealing, and ANN-GA, for a precise optimization of the input parameters regarding forecasting the energy usage during 1975-2019 throughout Turkey.

Three ML algorithms were developed by Li et al. [42], including gradient boosting regression (GBR), SVM, and ordinary least squares regression, to predict transport CO₂E. More recently, Javanmard et al. [38] employed a hybrid approach integrating a multi-objective mathematical model with MLs to predict energy demand and CO₂E in the transportation sector of Canada. Korkmaz [43] developed black widow optimization and bezier search differential evolution methods to calculate the transport energy usage throughout Turkey. More recently, a hybrid RF-SVR and response surface method were carried out by Khajavi and Rastgoo [44] to forecast CO₂E for 30 important towns throughout China.

Given the concentration of this study, Table 1 summarises key information from prior studies from all over the world forecasting energy demand and CO_2E in the transportation sector. In the case of the FS methods (wrapper, filter, and embedded), we could not find any study to utilise the FS methods except for Wang et al. [31], which used stepwise linear regression to select most significant variables. In addition, based on authors' review of literature only [2,38] considered both energy demand and CO_2E as target variables.

| _ | Target | | _ | | Feature selection | n | | Applied Models | |
|-------|----------------------------|----------------|----------------------------|--------------------------|---------------------|---------|---|---------------------------------|---|
| Paper | Variable(s) | Field | Country | Timeframe | Filter/ Embedded | Wrapper | ML | Mathematical | Hybrid |
| [2] | Energy and CO ₂ | Transport | Turkey | 1970-2016 | No | No | ANN, SVM, DL | - | - |
| [22] | Energy | Transport | Jordan | 1985-2009 | No | No | - | - | Neuro-Fuzzy Inference System ANN-GA, |
| [23] | Energy | Transport | Turkey | 1975-2019 | No | No | - | - | ANN-SA, and ANN-PSO |
| [31] | CO_2 | Transport | China | 1980-2014 | Yes | No | BPNN, GPR, SVM | - | PSO-SVM |
| [45] | Energy | Transport | Thailand | 1989-2008 | No | No | ANN | - | - |
| [40] | Energy | Transport | Turkey | 1975-2019 | No | No | multivariate adaptive regression splines | - | - |
| [41] | Energy | Automobile | Australia | 1974-2019 (Quarterly) | No | No | Autoregressive and structural model | - | - |
| [42] | CO ₂ | Transport | Top 30 Emitting Nations | 2005-2014 | No | No | OLS, SVM, GBR ARIMA, | - | - |
| [38] | Energy and CO ₂ | Transport | Canada | 1990-2019 | No | No | ARFIMA, SARIMA, GARCH, MIDAS, SVR | - | - |
| [43] | Energy | Transport | Turkey | 2000-2017 | No | No | Bezier search differential evolution and black widow optimization | - | - |
| [44] | CO ₂ | Road Transport | China | 2006-2015 | No | No | - | - | Hybrid RF-SVR, and response surface |
| [46] | CO ₂ | Road Transport | UK | 2010-2014 | No | No | - | Basic Estimations to 2050 | - |
| [47] | non-methane | Road Transport | EU Nations | 2004-2016 | No | No | SVR, RLR | - | Kernel grey model |

Table1. Summary of the primary studies in predicting energy demand and CO_2E in the transportation sector.

| [48] | CO ₂ | Transport | Pakistan | 1971-2014 | No | No | - | Autoregressive | |
|---------------|----------------------------|----------------|----------|--------------------|-----|-----|---|------------------------------------|--|
| [49] | CO ₂ | Transport | China | 2015 (3 months) | No | No | ANN, gaussian naive bayes, linear and logistic regression, stacked deep belief networks | | |
| [50] | CO ₂ | Land transport | Cyprus | 2010-2016 | No | No | - | Environmentally extended input- | |
| [51] | Energy | Transport | Turkey | 1975-2016 | No | No | ANN | output analysis | |
| Prseent study | Energy and CO ₂ | Transport | UK | 1990-2019 | Yes | Yes | ANN, RF, LSTM, SVM, MLR, LSBoost, GPR | | |
| | | | | ournal | 210 | | | | |

3. Research methodology

3.1 Overall procedure of proposed forecasting framework

Figure 2 provides a conceptual framework of our proposed method for forecasting EngCons and CO₂E. The primary goal of the proposed integrated multi-stage FS and ML method is to leverage the benefits of FS to identify the most influential features while mitigating multicollinearity, and to identify a subset of features able to achieve an appropriate balance between accuracy of ML models and their interpretability power.

The architecture of our proposed method involves multiple stages: i) pre-processing operations, (ii) correlation analysis of variables, (iii) filter and embedded FS methods, (iv) multicollinearity analysis, (v) integrated wrapper FS and ML models, (vi) selecting the best ML models with the highest accuracy, and finally (vii) performing Shapley analysis to determine the contributions of variables.

First, the raw data was collected and processed by removing noise, correcting the data inconsistencies, and integrating them into a homogeneous dataset. The other stages are described in some details as follows. In any ML study, some potentially important features can be automatically selected and added to the feature list based on the domain knowledge as depicted in Figure 2.

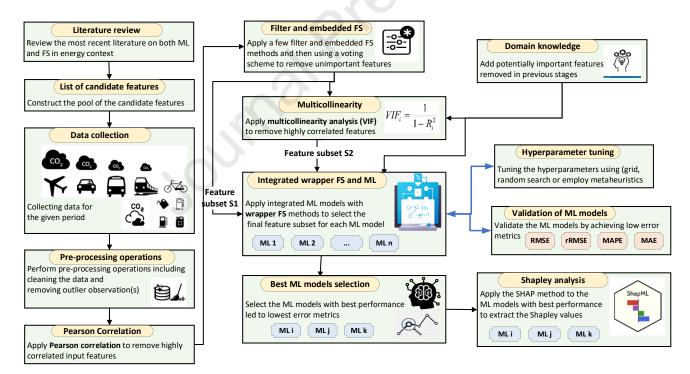


Figure 2. The conceptual framework of the integrated FS and ML based forecasting framework.

3.2 Pairwise Pearson correlation

For each input feature (IF), the Pearson correlation coefficient r_{ij} of this feature (*i*) with each of the other input features (*j*) along with its corresponding significance value p_{ij} (*i* and $j \in Set_{IF}$) are calculated. If the absolute value of correlation coefficient r_{ij} for each pair of input features is greater than correlation threshold value T_u (in this study $T_u = 0.95$) with significant confidence ($p_{ij} < a$, *a* is significance level), only one highly collinear feature will be selected, while the remaining features will be excluded from the candidate pool to avoid redundancy.

3.3 Filter and embedded FS methods

3.3.1 Maximum Relevance and Minimum Redundancy (mRMR)

The mRMR is a filter FS algorithm to rank input features based on their relevance to the output feature and simultaneously discard redundant input features [52]. Mutual information (MI) is employed to quantify both the relevance and redundancy of mRMR. The following describes MI:

$$I(X,Y) = \iint p(x,y) \log \frac{p(x,y)}{p(x)p(y)} \tag{1}$$

where X, Y are vectors, p(x, y) is the joint probabilistic density, p(x) and p(y) are the marginal probabilistic densities, respectively.

Assuming a feature set S with $m(x_i, i \in (1, m))$ features, then Max-Relevance represents a feature subset that jointly has the largest relevance to the output variable y:

$$maxD(S,y), D = \frac{1}{|S|} \sum_{x_i \in S} I(x_i, y)$$
(2)

For defining redundant features, Minimum Redundancy is implemented using Max-Relevance's possible redundancy. :

$$minR(S), \ R = \frac{1}{|S|^2} \sum_{x_i, x_j \in S} I(x_i, x_j)$$
(3)

An incremental search method is then employed to find the optimal solution that can satisfy the above two constraints. Assuming that there already have a feature set S_{m-1} , the task is to determine the *mth* feature from $\{X - S_{m-1}\}$

$$max_{x_j \in X - S_{m-1}} [I(x_j, y) - \frac{1}{m-1} \sum_{x_i \in S_{m-1}} I(x_i, x_j)]$$
(4)

3.3.2 Random Forest

Random Forest (RF) is an ensemble technique that combines a predetermined number of decision trees. It employs information gain or Gini impurity as the criteria for splitting each node across all trees [53]. Nodes with the highest impurity reduction are usually found at the start of decision trees, while nodes

with the lowest impurity reduction are typically located towards the end. Therefore, by selectively pruning branches at a specific node, it is feasible to create a subset of the most significant features.

3.3.3 Boruta FS

Boruta is a wrapper algorithm that utilises an RF to identify pertinent features associated with output labels while discarding irrelevant features that may occasionally exhibit significance due to chance [54]. A detailed procedure for BFS is iterated below:

- Randomise the feature set by creating shadow copies (shadow features) of all features and combining them with the original features to create an extended feature set.
- Establish an RF model for the expanded feature set and assess the feature's importance (the average reduced accuracy Z value). The larger the Z value, the more significant the trait. Z-max denotes the maximum Z value of the shadow feature.
- During each iteration, if the feature's Z value is larger than Z-max, the feature is deemed essential and is retained. Otherwise, the feature will be considered trivial and eliminated from the feature list.
- The preceding approach terminates when all features are either verified or rejected or when the maximum number of BFS iterations is achieved.

3.3.4 Voting scheme in FS

One of the challenges in FS is to determine the most appropriate FS method(s) for a particular set of data due to the fact that each FS method has its own logic based on a statistical measure to calculate the relative importance of features, which may lead to different subsets of selected features. In other words, a feature may be deemed important in one method but not in another.

In the proposed methodology, three different FS methods, including two filter FS methods (mRMR and Boruta) and one embedded FS method (RF) were applied to select the most important features. However, both filter and embedded methods have their own drawbacks; filter methods ignore the dependency among input features and embedded methods heavily rely on ML models. To overcome such issue, a voting scheme was proposed, when an FS method *m* picks the feature *f*, it assigns the vote V_{mf} (*no* = 0 or *yes* = 1) for that feature. In the end, the voting scheme calculates the total "*yes*" votes for each feature, i.e., total vote $V_f = \sum_m V_{fm}$, and then a subset of features with the total vote V_f greater than or equal to the total vote threshold value V_T (provided by ML practitioner depending on the problem) are selected.

3.4 Multicollinearity analysis

Multicollinearity refers to the correlation between input features in ML applications, which typically does not impact the performance of the ML models. However, it may significantly distort the interpretability of the model and develop a biased insight of feature importance. For instance, during

training process, a ML method such as Lasso Regression may assign a large weight to one arbitrary representative of a group of highly correlated features and fully omit the rest ones, despite similar information these features represent. A misleading interpretation may therefore be obtained due to multicollinearity. To mitigate adverse impact of multicollinearity on interpretation of ML, variance inflation factor (VIF) [55, 56] was introduced in the study for removing highly correlated features.

3.5 ML models

3.5.1 Support vector machine (SVM)

SVM is a model for binary classification that functions based on the principle of separating hyperplanes [57]. This approach guarantees the determination of the hyperplane that can effectively partition the training datasets under the largest geometric interval. A Kernel function is incorporated into SVM to facilitate the mapping of input spaces onto a feature space of high dimensionality through a non-linear transformation, which ultimately results in the establishment of a linear decision boundary within the transformed space.

3.5.2 Gaussian process regression (GPR)

The GPR model is a supervised machine-learning algorithm that operates on probabilistic principles [58]. It leverages prior knowledge to generate predictions and provides measures of uncertainty. Assuming a training set $\mathcal{D} = (X, y) = \{(X_i, y_i) | i = 1, ..., N\}$, where X is denotes an input vector and y denotes an output or target variable. When given a new input X*, the corresponding output \hat{y}^* can be expressed as

$$\hat{y}^* = K(X^*, X)K(X, X)^{-1}y$$
(5)

The derivation process is as follows, assuming:

$$\begin{bmatrix} y\\ y^* \end{bmatrix} \sim \mathcal{N}(0, \begin{bmatrix} K(X,X) & K(X,X^*)\\ K(X^*,X) & K(X^*,X^*) \end{bmatrix})$$
(6)

According to the conditional distribution property of the multidimensional Gaussian distribution:

$$y^* | y \sim \mathcal{N}(K(X^*, X)K(X, X)^{-1}y, K(X^*, X^*) - K(X^*, X)K(X, X)^{-1}K(X, X^*))$$
(7)

Finally, $p(\hat{y}^*|y)$ is able to achieve its maximum when $\hat{y}^* = K(X^*, X)K(X, X)^{-1}y$.

3.5.3 Long short-term memory (LSTM) networks

Long Short-Term Memory (LSTM) networks are sequential neural networks that address the vanishing gradient of Recurrent Neural Networks [59] by introducing the concept of cell states and bring four interacting layers and gate units as shown in Figure 3.

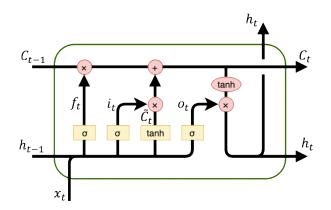


Figure 3. Schematic diagram of an LSTM.

The self-connected memory cell C_t is the key feature of LSTMs, enabling gradients to flow across long sequences. LSTMs use 3 sigmoid gates (forgetting, input, and output) to manage cell state information.:

$$\sigma(x) = \frac{1}{1 + e^{-x}} \tag{8}$$

Forgetting gate f_t determines the specific information to discard from the cell state based on h_{t-1} and x_t , and update the cell state C_{t-1} (i.e., 0: discard, 1: remain).

$$f_t = \sigma \big(W_f \cdot [h_{t-1}, x_t] + b_f \big) \tag{9}$$

The input gate i_t and a *tanh* layer are then developed to control new information stored in the new cell:

$$i_{t} = \sigma(W_{i} \cdot [h_{t-1}, x_{t}] + b_{i})$$
(10)

$$\tilde{C}_t = tanh(W_C \cdot [h_{t-1}, x_t] + b_C)$$
(11)

the new cell state C_t can be updated:

$$C_t = f_t \cdot C_{t-1} + i_t \cdot \widetilde{C}_t \tag{12}$$

Finally, the output gate o_t uses the current input and the previous output to decide what parts of the cell state to output, and a *tanh* function is established to calculate the current state.

$$o_t = \sigma(W_0[h_{t-1}, x_t] + b_0)$$
(13)

$$h_t = o_t \cdot \tanh(C_t) \tag{14}$$

In Equations (8)-(14), the matrices W_f , W_i and W_o are the recurrent weighting metrics; b_f , b_i , b_c and b_o are the corresponding bias vectors.

3.5.4 Linear regression (LR)

LR measures the relationship between a target variable and a given set of input variables [60]. Assuming there are *m* input variables:

$$Y = \beta_0 + cX_1 + \beta_2 X_2 + \dots + \beta_m X_m + \varepsilon$$
⁽¹⁵⁾

where β_0 is the constant term and β_1 to β_m are the coefficients associated with the input variables. ε is the random error. Note that the m^{th} regression coefficient β_m represents the expected change in Y per unit change in the m^{th} input variable x_m , assuming $E(\varepsilon) = 0$, $\beta_m = \frac{\partial E(Y)}{\partial X_m}$.

3.5.5 Gradient tree boosting with least squares (LSBoost)

LSBoost is a meta learning method that comprises a specific number of weak tree-learners [61]. The algorithm initiates by sequentially training individual weak learners in the form of decision trees, and subsequently fits the residual of errors to attain improved performance. The LSBoost approach employs the least squares as the criterion for loss.

Assuming the training set $\{(x_i, y_i)\}_{i=1}^n$, a loss function $L(y, F) = \frac{(y-F)^2}{2}$ and regression function $F_m(x), (F_0(x) = \overline{y})$, where m is the number of iterations. For each iteration,

$$\tilde{y}_i = y_i - F_{m-1}(x_i)$$
, for $i = 1, 2, ..., N$ (16)

$$(\rho_m, \alpha_m) = \arg\min_{\rho, \alpha} \sum_{i=1}^{N} [\widetilde{y}_i - \rho h(x_i; \alpha)]^2$$
(17)

$$F_m(x) = F_{m-1}(x) + \rho_m h((x; \alpha_m))$$
(18)

where $h(x_i; \alpha)$ is a parameterised function of input variables x_i that characterised by parameter α_m , ρ_m is a successive increment/step/boost of LSBoost.

3.5.6 Multi-layer Perceptron (MLP)

A multilayer perceptron is a fully connected feedforward artificial neural network (ANN) containing at least three layers of nodes: an input layer, a hidden layer, and an output layer [62]. Assuming an input layer consisting of a set of neurons $\{x_i | x_1, x_2, ..., x_m\}$, each neuron in the hidden

layer is linearly weighted to sum the values from the input layer:

$$v_i = \omega_{i1} x_1 + \omega_{i2} x_2 + \dots + \omega_{im} x_m \tag{19}$$

Where v_i is the weighted sum of the input connections of hidden node i, ω_{im} is the weight between hidden node i and input x_m .

Then, the weighted summation is applied to a nonlinear activation function, typically a hyperbolic tan function or sigmoid function:

$$y(v_i) = \tanh(v_i) \quad \text{or} \quad y(v_i) = (1 + e^{-v_i})^{-1}$$
(20)

The learning process in the MPL is carried out through backpropagation by changing the weights after all data is processed.

Assuming an error in an output node j in the nth data point $e_j(n) = y_j(n) - \overline{y}_j(n)$, where y is the actual value and \overline{y} is the calculated value. The node weights can be adjusted based on the least mean squares algorithm to minimise the error in the entire output as described:

$$\mathcal{E}(n) = \frac{1}{2} \sum_{j} e_j^2(n) \tag{21}$$

According to gradient descent, the change in each weight is:

$$\Delta \omega_{ji}(n) = -\eta \frac{\partial \mathcal{E}(n)}{\partial v_j(n)} \bar{y}_j(n)$$
(22)

Where \bar{y}_j is the output of the previous neuron and η is the learning rate, then the derivative can be described with Equation (25):

$$-\frac{\partial \mathcal{E}(n)}{\partial v_j(n)} = \phi'\left(v_j(n)\right) \sum_k -\frac{\partial \mathcal{E}(n)}{\partial v_k(n)} \omega_{jk}(n)$$
(23)

Where ϕ' is the derivative of the activation function. The derivative depends on the change in weights of the *k*th nodes, which represent the output layer.

3.6 Wrapper FS

SIFE [63] is an efficient wrapper-based evolutionary algorithm with set-inspired operations and fuzzy granulation for both high-dimensional and low-dimensional FS problems. To improve its search policy, SIFE uses a three-parent crossover approach based on set-theoretic concepts such as 'union' and 'intersection'. Fuzzy granulation is also integrated into SIFE, which aids in population initialization and elite steps. It helps in generating a diverse population throughout generations and acts as a surrogate strategy to avoid additional fitness evaluations. This approach aims to achieve a fast and reasonable balance between exploration and exploitation in its problem encoding and search operation, while

reducing computational costs. SIFE is adopted in this research because of its high capability of handling both high-dimensional and low-dimensional search space.

3.7 ML interpretation by SHAP method

As black-box ML models have long been criticised for lacking interpretability. In the context of decision-making, stakeholders and policy makers prioritise quantitative analysis of the correlation between input and target variables over the predictive accuracy of ML models.

Shapley Additive Explanations (SHAP) is an approach employed for interpreting the output of ML models [64]. The classical Shapley value from game theory is used by SHAP method to establish a connection between the optimal credit allocation and the local explanation. SHAP operates by decomposing the output of an ML model into the sums of the impacts of individual features which facilitates the comprehension of the significance of individual features and benefits decision-making. In order to compute SHAP value, a linear explanation model is utilised as an interpretable approximation to a ML model [65]:

$$g(z') = \phi_0 + \sum_{i=1}^{M} \phi_i z_i'$$
(24)

where $z' \in \{0,1\}^M$ represents whether a feature is used to estimate the output variable, *M* is the number of input features, ϕ_i is the SHAP value of the *i*th feature, and ϕ_0 is the mean value of the output variable. The SHAP value assesses feature importance by comparing model prediction performance with and without each feature in feature combinations:

$$\phi_i = \sum_{S \subseteq z'\{i\}} \frac{|S|!(M-|S|-1)}{M!} [f_x(S \cup \{i\}) - f_x(S)]$$
(25)

where S is the set of non-zero z', and $f_x(S) = E[|f(x)x_S|]$ is the expected outcome of the model f(x) subjected to S.

4 Experimental setting

The study utilises the MATLAB software to implement the ML algorithms and wrapper FS. All experiments for filter and embedded FS, SHAP analysis and producing heatmap are coded in Python.

4.1 Data

The case of this study is based on the EngCons and CO_2E in the UK's transportation sector in the time interval of 1990-2019. The year 2020 was not considered in this study, because this observation is detected as an outlier for some features due to the Covid Pandemic. The EngCons and CO_2E of the UK's transportation sector is illustrated in Figure 4, where similar pattern as bimodal distribution chart

in EngCons and CO_2E is observed. The initial growth trajectory encountered an avalanche of decline in 2008 which persisted until 2013 when it reached its lowest point, the same as in 1990. After a brief fouryear increase in EngCons and CO_2E levels, they began a second decline in 2017 and beyond.

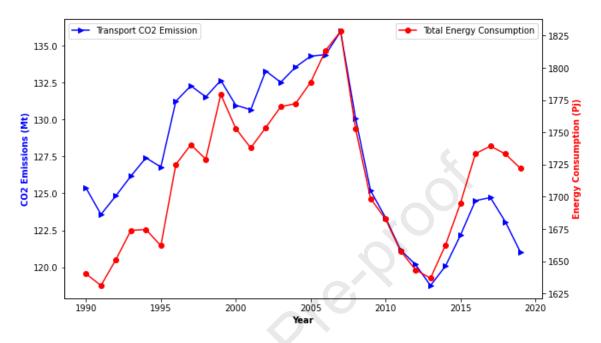


Figure 4. EngCons and CO₂E in the transportation sector in the UK (1990-2019).

Table 2 presents the list of 24 variables (features) along with their corresponding abbreviations, which include 22 input variables and two target variables, EngCons and CO₂. Based on the intensive review of existing literature, a wide range of input variables in three categories including socioeconomic, transportation and energy-related factors are considered. Socioeconomic factors include GDP per capita, population, gasoline price and unemployment rate which indicate the strong relationship between the EngCons and CO_2E in literature. To consider urbanization level of the UK, urban population rate is added to the list.

For transportation category, we considered three main modes of transportation including air, rail, and road transportation, and each mode comprising passenger and freight transportation. Furthermore, energy intensity in transport, renewable and waste energy in transport, share of electric vehicles and road carbon intensity which could have significant influence on EngCons and CO₂E are considered. For energy category, a few energy-related variables considered in other studies, which may have relationships with EngCons and CO₂E in transport are added to the list.

The data was collected from the UK Department for Transport (www.gov.uk/government/ organisations/department-for-transport), UK Office for National Statistics (www.ons.gov.uk/economy/ environmentalaccounts), and International Energy Agency (World Energy Balances Highlights) https://www.iea.org/data-and-statistics/data-product/world-energy-balances-highlights. The descriptive statistics of the 24 features considered for transport EngCons and CO₂E is presented in Table A1.

| Feature | Abbreviation | Feature | Abbreviation |
|---------------------------------------|--------------|---------------------------------|--------------|
| CO ₂ E in transport | CO_2 | Unemployment rate | UR |
| EngCons in transport | EC-Trans | Gasoline price | GP |
| Oil Products consumption in transport | OP-Trans | Total public energy RD&D budget | R&D |
| Total EngCons in all sectors | EC-All | Net energy imports | NEI |
| Total energy supply | TES | Road carbon intensity | RCI |
| Population | POP | Air passengers | AP |
| Urban population rate | UPR | Air fright | AF |
| Energy intensity in transport | EI | Rail passengers | RP |
| GDP per capita | GDP | New road vehicle registrations | NVR |
| Total final Electricity consumption | EC-Elec | Total licensed road vehicles | TV |
| Renewable & Waste by Transport | RW-Trans | Average road vehicle milage | AVM |
| Share of electric vehicles | SEV | Total road vehicle milage | TVM |

Table 2. Twenty-four features and their corresponding abbreviation.

4.2 Hyperparameter setting of MLs

Optimising hyperparameters is crucial for MLs resulting in promising performance. A pilot study was conducted to manually tune the parameters to assess the impact of FS methods on ML model performance and evaluate the influence of different features on EngCons and CO₂E. The best values of hyperparameters found in the pilot experiments for seven ML models are presented in Table 3.

| ML Model | Parameter name | Parameter value |
|-----------|--|--|
| MLR RF | Maximum number splits Pruning Number of trees | - 10 Off 7 |
| LS-Boost | Maximum number splits Pruning Number of trees Learning rate | 12 Off 7 0.3 |
| MLP | Number of hidden layers Number of neurons Learning method Activation function | 1 10 Levenberg-Marquardt Sigmoid |
| LSTM | Number of LSTM layers Number of hidden units Maximum epoch | 1 20 100 |
| SVR-RBF | Box constraint I Gamma (γ) | 100 1 |
| GPR | Explicit basis Prediction method | Linear Subset of regressors approximation |

Table 3. The summary of hyperparameters for the ML models.

4.3 Evaluation metrics

[1

To develop a comprehension of the model performance in terms of the EngCons and CO2E of transportation sector, the following evaluation metrics are included: root mean square error (RMSE), relative root mean square error (rRMSE), mean absolute error (MAE), mean absolute percentage error (MAPE).

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (y_i - p_i)^2}$$
(26)

$$rRMSE = \sqrt{\frac{\frac{1}{n}\sum_{i=1}^{n}(y_{i}-p_{i})^{2}}{\sum_{i=1}^{n}(p_{i})^{2}}}$$

$$MAE = \frac{1}{n}\sum_{i=1}^{n}|y_{i}-p_{i}|$$

$$MAPE = \frac{1}{n}\sum_{i=1}^{n}\left|\frac{y_{i}-p_{i}}{y_{i}}\right|$$
(27)
(28)
(29)

where y_i is the actual value and p_i is the predicted value.

5. Results and analysis

5.1 Primary correlation analysis

Since all 22 input variables are continuous numerical, Pearson correlation coefficients with two-tailed test were computed among them. The correlation results indicate that some correlation values were both statistically significant with a = .01 and greater than predefined correlation threshold .95.

The correlation between population and urban population rate was found to be extremely high, r(28)=+1. The variables rail passengers and air passengers were found to be extremely positively correlated with population with r(28)=.99 and r(28)=.98, respectively. Energy intensity is extremely negatively correlated with population, r(28)=-.98. It is interesting to note that gasoline price has very strong positive correlation with GDP per capita, r(28)=.93. Total number of licensed road vehicles has very strong positive correlation with population, r(28)=.95, but our domain knowledge recommended us not to remove TV.

Correlation analysis of target variables indicated that EC-Trans(t) and CO2(t) have very strong positive correlation of r(28)= .84. Renewable and waste energy in transport and share of electric vehicles have slight or very weak negative correlation with EC-Trans(t), but moderate negative correlation with CO2(t). The correlation values of EC-Trans(t) and CO2(t) with their corresponding next year values, i.e. EC-Trans(t+1) and CO2(t+1), are r(27)= .86 and r(27)= .91, respectively.

5.2 Intermediate results

After removing extremely correlated input features, voting scheme was implemented in a conservative manner with total vote threshold value V_T of 1. In fact, features were discarded only if they be deemed

not important in all 3 FS methods. The selected feature subsets for EC-Trans(t+1) and CO2(t+1) were listed in Tables 4 and 5.

In this study, regarding that population and GDP per capita variables are found to be important in all similar studies, domain knowledge recommended adding these two variables to the selected list of features after they were removed in the voting scheme.

| FS Method | CO2(t) | EC- Trans(t) | OP- Trans | EC- All | TES | R&D | UR | RCI | NVR | TV | Total count |
|--------------|--------|-----------------|--------------|------------|-----|-----|----|-----|-----|----|-------------|
| mRMR | ٠ | • | ٠ | ٠ | 0 | 0 | • | ٠ | ٠ | ٠ | 8 |
| Boruta | • | • | • | • | • | 0 | • | • | • | 0 | 8 |
| RF | • | • | • | • | 0 | • | • | • | • | 0 | 8 |
| Score | 3 | 3 | 3 | 3 | 1 | 1 | 3 | 3 | 3 | 1 | 10 |

Table 4. Result of FS voting scheme for EC-Trans(t+1).

Table 5. Result of FS voting scheme for CO2(t+1).

| FS Method | CO2(t) | EC- Trans(t) | OP- Trans | EC- All | TES | RW- Trans | R&D | NEI | RCI | AVM | GP | POP | Total count |
|--------------|--------|-----------------|--------------|------------|-----|--------------|-----|-----|-----|-----|----|-----|-------------|
| mRMR | • | • | • | • | • | • | • | • | • | 0 | 0 | • | 10 |
| Boruta | • | 0 | • | • | • | • | • | • | • | • | • | 0 | 10 |
| RF | • | ٠ | • | • | • | • | • | • | ٠ | • | 0 | 0 | 10 |
| Score | 3 | 2 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 2 | 1 | 1 | 12 |

The correlations between selected features and EC-Trans(t) and CO2(t) were presented in Figures 5 and 6 where significant correlative features were detected, which confirms the need for multicollinearity analysis.

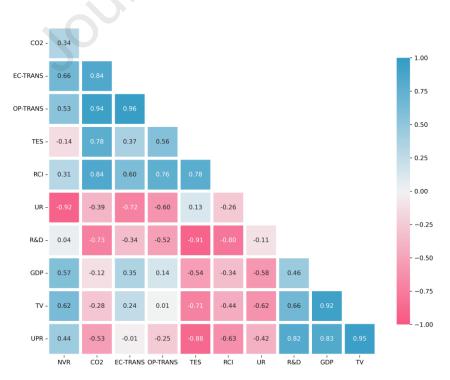


Figure 5. The heatmap of correlation coefficient for EC-Trans(t).

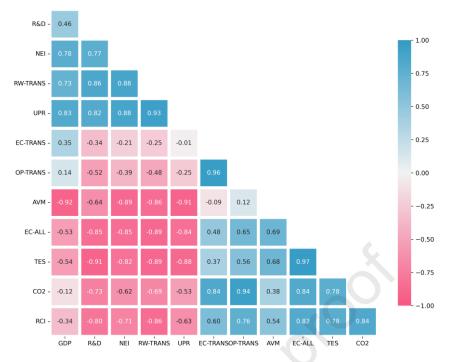


Figure 6. The heatmap of correlation coefficient for CO2(t).

5.3 Multicollinearity analysis

Multicollinearity analysis was performed to model the relationship between 12 selected features and EC-Trans(t+1), and between 13 selected features and CO2(t+1) as presented in Tables 4 and 5, respectively. The Multicollinearity analyses indicate that two regression models have severe multicollinearity for some of the features. For both EC-Trans(t+1) and CO2(t+1) regression models, the features with the highest VIF are iteratively removed until the VIF for each feature becomes less than 10. In EC-Trans(t+1) regression model, the OP-Trans, CO2(t), TES, POP and TV were respectively removed, whereas in CO2(t+1) regression model, OP-Trans, R&W-Trans, TES, POP, AVM and GDP were respectively removed.

Each selected feature subset, before and after multicollinearity analysis (called S1 and S2, respectively, as shown in Figure 2), underwent the final wrapper FS method (SIFE) to produce the final feature subsets as listed in Tables 6 and 7. More specific, for both EC-Trans(t+1) and CO2(t+1), the number of selected features by ML models based on S1 varied significantly while constantly for subset S2. On the other hand, intersections in FS were noticed despite individual preference of ML models in determining the crucial features. For EC-Trans(t+1), NVR and TV are extra two features deemed as the most influential features by all ML models in S1 followed by GDP. In S2, NVR and OP-Trans are determined as important features. For CO2(t+1), in S1, AVM, GP, and RCI was determined significant for 7, 6 and 5 times, respectively. When it comes to S2, 4 features including GP, RCI, EC-Trans and OP-Trans were selected multiple times (i.e., 7, 7, 6 and 6 times) by ML models.

It's important to note that unlike similar studies where population and GDP are key driving variables, in the UK's transportation sector only GDP is selected as influential variable for forecasting EC-

Trans(t+1). The possible reason for this observation could be due to fact that although in all countries, particularly developing countries, population and GDP are key driving factors of EngCon and CO2E, these two measures are significantly harnessed in the UK and they have been decreasing since 2017 as depicted in Figure 4.

| | | | | | | | Selecte | d featu | res | | | | | |
|-------------------|--------------|--------|--------------|------------|------|-----|---------|---------|-----|------|------|-----|-----------------|--------------------------|
| Feature subset | ML models | CO2(t) | OP- Trans | EC- All | TES | R&D | UR | RCI | NVR | TV | POP | GDP | EC- Trans(t) | Number of features |
| | LSBoost | 0 | • | • | 0 | • | 0 | 0 | • | • | 0 | • | • | 7 |
| | MPL | • | • | • | 0 | 0 | 0 | 0 | • | • | 0 | • | • | 7 |
| | SVR | 0 | 0 | 0 | 0 | 0 | 0 | • | • | • | • | 0 | • | 5 |
| S1 | GPR | 0 | 0 | 0 | 0 | 0 | • | 0 | • | • | 0 | 0 | • | 4 |
| 51 | LR | 0 | 0 | 0 | 0 | 0 | • | • | • | • | 0 | • | • | 6 |
| | RF | 0 | • | • | • | • | • | • | • | • | • | • | • | 11 |
| | LSTM | 0 | • | 0 | 0 | 0 | 0 | • | • | • | 0 | • | • | 6 |
| | Score | 1 | 4 | 3 | 1 | 2 | 3 | 4 | 7 | 7 | 2 | 5 | 7 | 46 |
| | LSBoost | | | • | | • | • | 0 | • | | | 0 | • | 5 |
| | MPL | | | • | | 0 | • | 0 | | | | • | • | 5 |
| | SVR | | | • | | 0 | 0 | 0 | • | | | • | ٠ | 4 |
| S2 | GPR | N/A | N/A | • | N/A | 0 | • | 0 | • | N/A | N/A | 0 | ٠ | 4 |
| 32 | LR | 1N/A | 1N/A | • | 1N/A | 0 | • | • | • | 1N/A | 1N/A | 0 | • | 5 |
| | RF | | | • |] | 0 | 0 | • | • | | | • | • | 5 |
| | LSTM | | | 0 |] | 0 | 0 | • | • | | | • | • | 5 |
| | Score | | | 6 |] | 1 | 4 | 3 | 7 | | | 4 | 7 | 32 |

Table 6. Selected feature subsets with the ML models for forecasting EC-Trans(t+1).

Note: N/A indicates the feature is excluded in S2

Table 7. Selected feature subsets with the ML models for forecasting CO₂(t+1).

| Easture | ML | | | | | | Selec | ted feat | tures | | | | | | Number |
|-------------------|---------|-----------------|--------------|------------|------|--------------|-------|----------|-------|------|----|------|------|--------|----------------|
| Feature subset | models | EC- Trans(t) | OP- Trans | EC- All | TES | RW- Trans | R&D | NEI | RCI | AVM | GP | POP | GDP | CO2(t) | of features |
| | LSBoost | 0 | • | 0 | 0 | • | 0 | 0 | 0 | • | 0 | 0 | 0 | ٠ | 4 |
| | MPL | • | 0 | 0 | 0 | 0 | • | 0 | • | • | ٠ | 0 | • | • | 7 |
| | SVR | 0 | 0 | • | 0 | 0 | 0 | • | • | • | • | 0 | 0 | • | 6 |
| S 1 | GPR | 0 | 0 | 0 | 0 | 0 | • | 0 | 0 | • | • | 0 | 0 | • | 4 |
| 51 | LR | • | 0 | • | 0 | 0 | • | 0 | • | • | • | 0 | • | • | 8 |
| | RF | 0 | • | • | 0 | • | 0 | 0 | • | • | • | 0 | 0 | • | 7 |
| | LSTM | • | • | 0 | • | 0 | • | • | • | • | • | • | • | • | 11 |
| | Score | 3 | 3 | 3 | 1 | 2 | 4 | 2 | 5 | 7 | 6 | 1 | 3 | 7 | 47 |
| | LSBoost | • | | • | | | 0 | 0 | • | | ٠ | | | • | 5 |
| | MPL | • | | • | | | 0 | • | • | | ٠ | | | • | 6 |
| | SVR | 0 | | • | | | 0 | • | • | | ٠ | | | • | 5 |
| 62 | GPR | • | N/A | 0 | N/A | N/A | • | • | • | N/A | • | N/A | N/A | • | 6 |
| S2 | LR | • | IN/A | • | IN/A | 1N/A | • | 0 | • | IN/A | • | IN/A | IN/A | • | 6 |
| | RF | • | | • | | | • | 0 | • | | ٠ | | | • | 6 |
| | LSTM | • | | | | 0 | • | • | 1 [| ٠ | | | • | 6 | |
| | Score | 6 | | 6 | | | 3 | 4 | 7 | | 7 | | | 7 | 40 |

Note: N/A indicates the feature is excluded in S2

5.4 Final results

The performance of ML models in terms of *RMSE*, *rRMSE*, *MAPE* and *MAE* metrics for forecasting EC-Trans(t+1) and CO2(t+1) based on S1 and S2 feature subsets are listed in Tables 8 and 9 as well as

Figures 8 and 9, respectively. As shown in the tables and figures, the performance metrics share a similar pattern in both EC-Trans(t+1) and CO2(t+1) forecasts. In general, a better performance was observed when the ML models were treated with more features. The performance of some ML models was relatively constant or even improved with a reduced number of features. For example, GPR indicated an increase in all metrics in EC-Trans(t+1) despite fewer input features. Similar results were shown in SVR-RBF and LSTM regarding CO_2E prediction. Among all employed ML models, SVR-RBF and RF indicated the best performance throughout all feature subsets and prediction tasks even with fewer features compared with other ML models.

| | | | Me | etrics | | Nubmer |
|------------|----------------------|--------|-------|--------|--------|----------------|
| Dataset | ML models | RMSE | rRMSE | MAPE | MAE | of features |
| | LSBoost | 14.805 | 0.864 | 0.806 | 13.770 | 7 |
| | MLP | 17.160 | 1.000 | 0.864 | 14.903 | 7 |
| | <mark>SVR-RBF</mark> | 6.769 | 0.395 | 0.338 | 5.833 | 5 |
| S1 | GPR | 21.131 | 1.233 | 1.148 | 19.647 | 4 |
| | LR | 13.847 | 0.808 | 0.633 | 10.876 | 6 |
| | RF | 10.881 | 0.635 | 0.488 | 8.404 | 11 |
| | LSTM | 38.311 | 2.235 | 2.129 | 36.575 | 6 |
| Average | | 17.558 | 1.024 | 0.915 | 15.715 | 6.571 |
| | LSBoost | 23.668 | 1.381 | 1.092 | 18.763 | 7 |
| | MLP | 33.500 | 1.954 | 1.569 | 27.036 | 5 |
| | <mark>SVR-RBF</mark> | 8.357 | 0.488 | 0.340 | 5.880 | 4 |
| S2 | GPR | 19.561 | 1.141 | 0.849 | 14.666 | 4 |
| | LR | 26.552 | 1.549 | 1.375 | 23.675 | 5 |
| | RF | 17.159 | 1.000 | 0.702 | 12.079 | 5 |
| | LSTM | 40.154 | 2.342 | 2.248 | 38.649 | 6 |
| Average | | 24.136 | 1.408 | 1.168 | 20.109 | 5.143 |
| | LSBoost | 59.9% | 59.8% | 35.5% | 36.3% | 0.0% |
| | MLP | 95.2% | 95.4% | 81.6% | 81.4% | -28.6% |
| | <mark>SVR-RBF</mark> | 23.5% | 23.5% | 0.6% | 0.8% | -20% |
| Difference | GPR | -7.4% | -7.5% | -26.0% | -25.4% | 0.0% |
| | LR | 91.8% | 91.7% | 117.2% | 117.7% | -16.7% |
| | RF | 57.7% | 57.5% | 43.9% | 43.7% | -54.5% |
| | LSTM | 4.8% | 4.8% | 5.6% | 5.7% | 0.0% |
| Average | | 37.5% | 37.4% | 27.6% | 27.9% | -21.7% |

Table 8. ML performance for forecasting EC-Trans(t+1) with S1 and S2 feature sets.

Table 9. ML performance for forecasting CO2(t+1) with S1 and S2 feature sets.

| Deterat | | Metrics | Number | | | |
|---------|-----------|---------|--------|------|-----|----------|
| Dataset | ML models | RMSE | rRMSE | MAPE | MAE | of |
| | | KNISE | IKIMSE | MAPE | MAE | features |

| | LSBoost | 1.180 | 0.962 | 0.876 | 1.072 | 4 |
|------------|----------------------|-------|-------|-------|-------|--------|
| | MLP | 1.011 | 0.825 | 0.693 | 0.849 | 7 |
| | SVR-RBF | 1.16 | 0.946 | 0.734 | 0.902 | 6 |
| S 1 | GPR | 1.197 | 0.977 | 0.867 | 1.068 | 4 |
| | LR | 1.426 | 1.163 | 0.837 | 1.031 | 8 |
| | RF | 1.311 | 1.069 | 0.976 | 1.197 | 7 |
| | LSTM | 1.920 | 1.566 | 1.368 | 1.682 | 11 |
| Average | | 1.315 | 1.073 | 0.907 | 1.114 | 6.714 |
| | LSBoost | 1.412 | 1.152 | 0.919 | 1.132 | 5 |
| | MLP | 1.901 | 1.554 | 1.377 | 1.690 | 6 |
| | <mark>SVR-RBF</mark> | 1.126 | 0.918 | 0.751 | 0.925 | 5 |
| S2 | GPR | 2.041 | 1.665 | 1.378 | 1.688 | 6 |
| | LR | 1.484 | 1.211 | 0.876 | 1.079 | 6 |
| | RF | 1.867 | 1.523 | 1.203 | 1.483 | 6 |
| | LSTM | 1.787 | 1.458 | 1.278 | 1.570 | 6 |
| Average | | 1.660 | 1.354 | 1.112 | 1.367 | 5.714 |
| | LSBoost | 19.7% | 19.8% | 4.9% | 5.6% | 25.0% |
| | MLP | 88.0% | 88.4% | 98.7% | 99.1% | -14.3% |
| | SVR-RBF | -2.9% | -3.0% | 2.3% | 2.5% | -16.7% |
| Difference | GPR | 70.5% | 70.4% | 58.9% | 58.1% | 50.0% |
| | LR | 4.1% | 4.1% | 4.7% | 4.7% | -25.0% |
| | RF | 42.4% | 42.5% | 23.3% | 23.9% | -14.3% |
| | LSTM | -6.9% | -6.9% | -6.6% | -6.7% | -45.5% |
| Average | | 26.2% | 26.3% | 22.5% | 22.6% | -14.9% |
| | | | | | | |

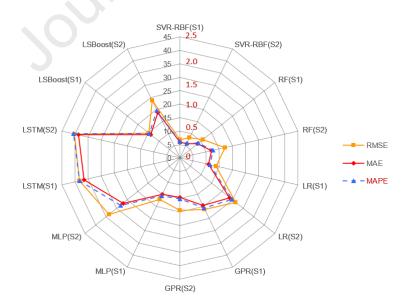


Figure 7. Performance of the ML models in forecasting EC-Trans(t+1).

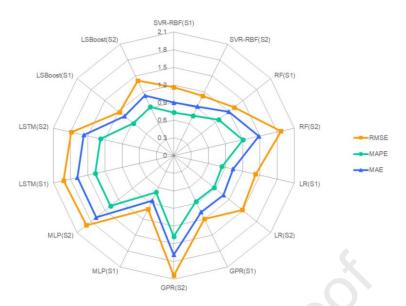


Figure 8. Performance of the ML models in forecasting CO2(t+1).

Figures 10 and 11 illustrate the detailed training and testing performances of SVR-RBF using feature subsets S1 and S2 for forecasting EC-Trans(t+1) and CO2(t+1), respectively. It is noticed that there was only a marginal decrease in *rRMSE* when utilising a smaller feature subset. Specifically, S2 had one less feature than S1 for both EngCons and CO₂E. This result indicates that the FS procedure proposed in the study was successful in reducing the dimension of the feature set while preserving the most pertinent information. In addition, the evaluation of SVR-RBF on the test set exhibits a negligible diminution in its performance as compared to that on the training set, which indicates slight overfitting issue.

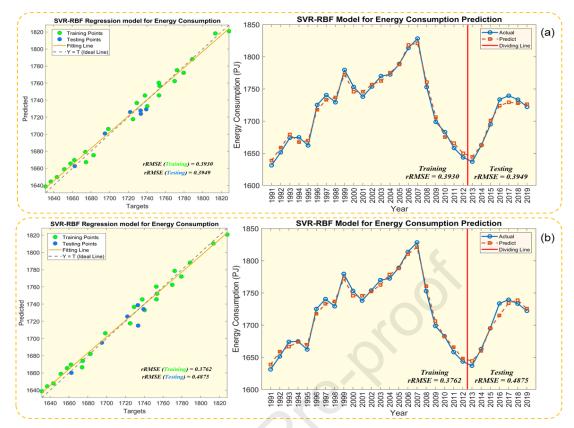


Figure 10. Performance of SVR-RBF in forecasting EC-Trans(t+1) based on (a) S1 and (b) S2 feature subsets.

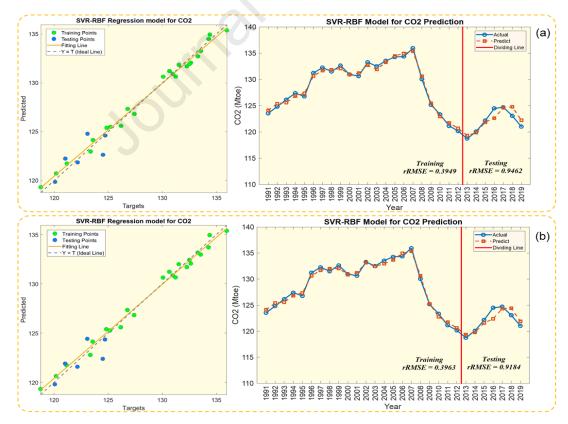


Figure 11. Performance of SVR-RBF in forecasting CO2(t+1) based on (a) S1 and (b) S2 feature subsets.

5.5 SHAP analysis

The SHAP method was utilised to enhance the interpretability of ML models and examine the impact of input features on model output. Figures 12 to 14 summarised the SHAP values of the final determined features (i.e., S2 feature set) and their quantified contribution towards EC-Trans(t+1) and CO2(t+1)using SVR-RBF and RF, respectively. The SHAP graphs in Figures 12-15 (a) display each input feature as a vertical bar on the x-axis, indicating its SHAP value and contribution to the models' output. SHAP values can be positive or negative, indicating whether a feature increased or decreased the model output. The SHAP values magnitude signifies the effect's intensity. The colour of each bar denotes the feature value in relation to the mean predicted value in the dataset. Blue signifies low values or negative effects, while red signifies high values or positive effects. The colour scheme aids in interpreting feature contributions and understanding the relationship between their values and the model's predictions. A simplified version of SHAP values were depicted in Figures 12-15 (b) which summarise the overall importance of each feature. In this study, the SHAP method was employed for interpreting SVR-RBF and RF in predicting EngCons and CO₂E, respectively. As shown in Figures 12 and 13, EC-trans played a significant role in EngCons while NVR, GDP and EC-All indicated a similar importance. In addition, it is observed that a higher value of EC-Trans and NVR led to a positive SHAP value and vice versa. Such association was not detected in GDP and EC-All. In terms of CO2E, RCI contributed a significant higher proportion than any other features (i.e., CO₂, EC-All, GP and NEI). Similarly, association between a higher value of RCI, CO₂ and a positive SHAP value is obtained and vice versa. For forecasting EC-Trans(t+1) based on RF, RCI, EC-Trans ranked top 2 and were significantly more important than the other 3 features. The relations between positive SHAP value and the higher value of RCI, EC-Trans and NVR is also notice in the Figure 14. UR however suggested an opposite result where a higher value is associated with negative SHAP value. While for CO₂E prediction, RCI was also regarded as the most critical feature, followed by CO2(t) and R&D. Similar associations are seen between greater RCI, CO2(t) values and positive SHAP values, and vice versa. An opposite result is detected in R&D.

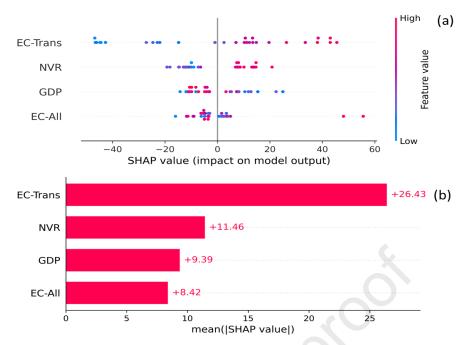


Fig. 12. The Shapley analysis for SVR-RBF for forecasting EC-Trans(t+1). (a) SHAP summary plot with S2 features, (b) The average contributions of the S2 features.

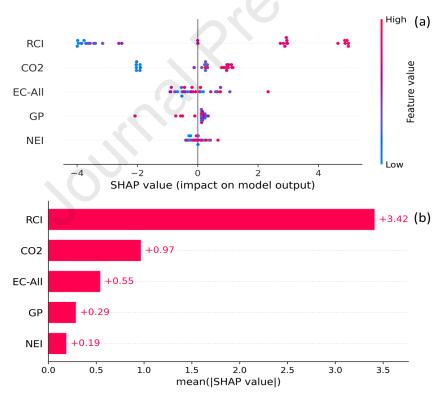


Fig. 13. The Shapley analysis for SVR-RBF for forecasting CO2(t+1). (a) SHAP summary plot with S2 features, (b) The average contributions of the S2 features.



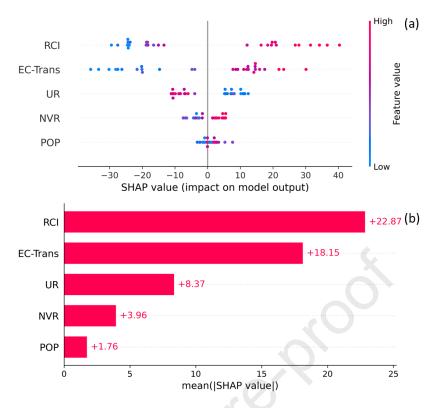


Figure 14. The Shapley analysis of RF for forecasting EC-Trans(t+1). (a) SHAP summary plot with S2 features, (b) The average contributions of the S2 features.

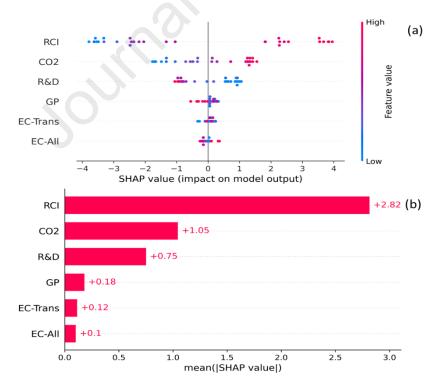


Fig. 15. The Shapley analysis of RF for forecasting CO2(t+1). (a) SHAP summary plot with S2 features, (b) The average contributions of the S2 features.

6. Noticeable discussions and limitations

A few noticeable points and limitations have been figured out in this study which are worth revealing for future similar studies. The dataset comprises a small size of 30 observations in the 1990-2019 period with 24 features, thereby such a small sample size leads to some challenges for MLs such as overfitting and the presence of random effects, which may negatively disturb the generalisation capability of ML models. To minimise the adverse impact caused by a small sample size, multiple FS stages within the forecasting framework was proposed to select the most related features and the feature space was therefore significantly reduced from initial 22 input features to less than 10 features. The risk of sparse matrix was then avoided.

Wrapper and embedded FS methods are both ML-based approaches. However, as previously mentioned, the issue of overfitting can hinder MLs from producing the most representative subset of features. In the context of filter methods, it is possible for two features to present a strong correlation based solely on numerical values, but this correlation may not essentially hold true. Therefore, in this paper, we proposed a voting mechanism to achieve a common agreement from three popular FS methods (i.e., mRMR, Boruta and RF). The preference of individual feature selection methods was mitigated to a greater extent.

It has been observed that most ML models exhibit a decrease in performance because of reducing the dimensionality of the feature set. This is comprehensible as the removed feature(s) may still possess a nuanced amount of valuable information but were excluded due to significant multicollinearity. The potential influence of the limited scope of the included data on this matter should not be underestimated. In comparison to high dimension datasets, such as gene analysis, low dimension dataset is less prone to containing redundant or irrelevant variables. However, this does not imply that the proposed FS methods were incapable of handling low-dimensional data, as suggested by SVR-RBF methods. In fact, a superior performance was achieved even with a reduced number of features. Also, it is important to note that despite a compromise in forecasting accuracy, the proposed framework retains the most related features for EngCons in transport sector, in which policymakers can benefit more from correct and accurate conclusion rather than accurate prediction but contain misleading information.

Lastly in all studies, GDP and population were selected as key driving variables for forecasting EC-Trans(t) and CO2(t), but in this study neither GDP nor population are found as influential variables in the UK's transportation sector, possibly because the trend of both EngCons and CO₂E are rapidly decreasing in the UK.

7. Conclusions and future research

A sustainable transport system necessitates a comprehension of the associations between transport EngCons and CO_2E , and their contributing factors, which also facilitates achieving promising performance of MLs in forecasting. To this end, this paper proposes an interpretable multi-stage forecasting framework to quantify EngCons and CO_2E in the UK's transport sector and identifying the

most relevant factors based on 22 initial input features from multisource including socioeconomic, transportation- and energy-related variables. Unlike recent published papers that solely focused on achieving the best prediction accuracy, the proposed framework also integrated interpretable ML methods to simultaneously maximise the forecasting accuracy and to determine the relationship between the forecasts and the influential variables using the SHAP method.

The contributions of this paper are as follows:

- To the best of our knowledge, this study is the first attempt, which employed a large list of input features and performed correlation and multicollinearity analyses to remove highly correlated features to provide an appropriate subset of features for interpretability of black-box ML models.
- This study introduces a novel voting scheme for feature selection (FS), which combines both filter and embedded paradigms, which has not been studied before in the EngCons context.
- This study is the second work in EngCons context (the first study is [30]) that applies the SHAP analysis to forecast the EngCons and CO2E to determine the influential variables.

The results indicate that the proposed multi-stage FS framework was able to improve the quality of data by removing potentially irrelevant and redundant features, in which average *rRMSE* and average *MAPE* of 1.024 and 0.915 for forecasting EC-Trans(t+1), and average *rRMSE* and average *MAPE* of 1.073 and 0.907 for forecasting CO2(t+1) with S1 feature subsets are achived. The selected best ML model varies depending on the feature subset examined. Overall, in both S1 and S2 feature subsets SVR-RBF and LSTM have the best and the weakest performance.

Shapley analysis for UK's transport EngCons and CO₂E forecasting indicates that road carbon intensity is the most significant factor associated with both EngCons and CO₂E. Unlike similar studies where population and GDP are key driving variables, Shapley analysis reveals that only GDP is selected as contributing variable for forecasting EC-Trans(t+1).

In 2020 the United Nations Economic Commission for Europe recommended that countries investigate the possibility of reporting quarterly GHG emissions data as part of climate change statistics [63]. There are solid methodologies for estimating GHG emissions on an annual basis and a few countries currently strived to develop statistical methodologies to compile quarterly time series emissions. Thus, for future researchers are encouraged to use quarterly GHG emissions data, rather than annual observations in which ML models avoid facing challenges with small sample size.

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Appendix A

 Table A1. Descriptive statistics for the full features

| Feature Abbreviation | Unit | Mean | Std | Min | Max |
|----------------------|-----------------------|----------|---------|----------|----------|
| CO2 | Mtoe | 127.39 | 5.09 | 118.76 | 135.96 |
| EC-Trans | PJ | 1716.13 | 54.84 | 1631.21 | 1828.29 |
| OP-Trans | PJ | 1675.92 | 61.87 | 1577.97 | 1798.86 |
| EC-All | PJ | 5861.52 | 394.87 | 5144.19 | 6341.47 |
| TES | PJ | 8625.08 | 741.32 | 7145.14 | 9449.86 |
| POP | Million | 8.90 | 9.80 | 2.00 | 9.00 |
| UPR | % | 80.20 | 1.87 | 78.11 | 83.65 |
| EI | MJ/pkm | 144.04 | 31.99 | 94.13 | 190.43 |
| GDP | USD | 34816.21 | 10197.2 | 18389.02 | 50653.26 |
| EC-Elec | PJ | 1130.26 | 76.32 | 987.96 | 1255.23 |
| RW-Trans | PJ | 18.79 | 22.54 | 0.00 | 68.90 |
| SEV | % | 0.47 | 0.81 | 0.00 | 3.30 |
| UR | % | 6.54 | 1.82 | 3.80 | 10.40 |
| GP | USD | 1.41 | 0.46 | 0.80 | 2.20 |
| R&D | USD | 419.23 | 358.78 | 69.90 | 1290.15 |
| NEI | PJ | 971.17 | 1991.90 | -2014.40 | 4026.40 |
| RCI | gCO2/MJ | 70.80 | 0.57 | 69.30 | 71.60 |
| AP | Million | 91.32 | 34.34 | 42.86 | 165.39 |
| AF | Million tone | 5702.52 | 847.88 | 3825.40 | 7618.10 |
| RP | Million | 1169.33 | 354.97 | 735 | 1744 |
| NVR | Thousand | 2714.65 | 402.78 | 1901.80 | 3295.96 |
| TV | Million | 31345.42 | 4606.01 | 24511.00 | 38682.70 |
| AVM | 1000 miles | 9.65 | 0.59 | 8.90 | 10.53 |
| TVM | Billion vehicle miles | 295.88 | 26.28 | 241.00 | 338.60 |

| Symbol | Description | | | | | | | |
|-----------------------------|---|--|--|--|--|--|--|--|
| Ι | Mutual information | | | | | | | |
| р | Joint probabilistic density | | | | | | | |
| S | Data set | | | | | | | |
| maxD | Max-Relevance | | | | | | | |
| minR | Minimum-Redundancy | | | | | | | |
| <i>x</i> , <i>X</i> | Input feature, input vector | | | | | | | |
| V_{mf} | Whether select feature or not | | | | | | | |
| V_T | The total vote threshold value | | | | | | | |
| ${\cal D}$ | Training dataset | | | | | | | |
| y, <i>y</i> ̄, <i>ỹ/p</i> | Actual, average actual and predicted target | | | | | | | |
| 2.6 | variable | | | | | | | |
| \mathcal{N} | Gaussian distribution | | | | | | | |
| σ() | Sigmoid function | | | | | | | |
| f_t | Forgetting gate | | | | | | | |
| <i>C</i> () | Cell state | | | | | | | |
| i_t | Input gate | | | | | | | |
| O_t | Output gate | | | | | | | |
| h () | Hidden state | | | | | | | |
| W_f, W_i, W_o | Recurrent weighting metrics | | | | | | | |
| b_{f} , bi, b_{o} | Bias vectors | | | | | | | |
| $\beta_1, \beta_2, \beta_m$ | Coefficients | | | | | | | |
| 3 | Random error | | | | | | | |
| E | Expectation function | | | | | | | |
| L | Loss function | | | | | | | |
| a_m, p_m | Increment/step/boost of LSBoost | | | | | | | |
| η | Learning rate of ANN | | | | | | | |
| ϕ' | The derivative of the activation function | | | | | | | |
| ω | Weights of ANN nodes | | | | | | | |
| ϕ | SHAP value | | | | | | | |
| ϕ_{O} | The mean value of the output variable | | | | | | | |

Nomenclature

| FS Method | CO2(t) | EC- Trans(t) | OP- Trans | EC- All | TES | R&D | UR | RCI | NVR | TV | Total count |
|--------------|--------|-----------------|--------------|------------|-----|-----|----|-----|-----|----|-------------|
| mRMR | • | • | • | • | 0 | 0 | • | • | • | • | 8 |
| Boruta | • | • | • | • | • | 0 | • | • | • | 0 | 8 |
| RF | ٠ | • | ٠ | ٠ | 0 | ٠ | ٠ | ٠ | • | 0 | 8 |
| Score | 3 | 3 | 3 | 3 | 1 | 1 | 3 | 3 | 3 | 1 | 10 |

Table 4. Result of FS voting scheme for EC-Trans(t+1).

Table 5. Result of FS voting scheme for CO2(t+1).

| FS Method | CO2(t) | EC- Trans(t) | OP- Trans | EC- All | TES | RW- Trans | R&D | NEI | RCI | AVM | GP | POP | Total count |
|--------------|--------|-----------------|--------------|------------|-----|--------------|-----|-----|-----|-----|----|-----|----------------|
| mRMR | • | • | • | • | • | • | • | • | • | 0 | 0 | • | 10 |
| Boruta | • | 0 | • | • | • | • | • | • | • | • | • | 0 | 10 |
| RF | • | • | • | • | • | • | • | • | | • | 0 | 0 | 10 |
| Score | 3 | 2 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 2 | 1 | 1 | 12 |

Table 6. Selected feature subsets with the ML models for forecasting EC-Trans(t+1).

| | | | | | | S | Selecte | d featu | res | | | | | |
|-------------------|--------------|--------|--------------|------------|------|-----|---------|---------|-----|------|-----|-----|-----------------|--------------------------|
| Feature subset | ML models | CO2(t) | OP- Trans | EC- All | TES | R&D | UR | RCI | NVR | TV | POP | GDP | EC- Trans(t) | Number of features |
| | LSBoost | 0 | • | • | 0 | • | 0 | 0 | ٠ | • | 0 | • | • | 7 |
| | MPL | • | • | • | 0 | 0 | 0 | 0 | • | • | 0 | • | • | 7 |
| | SVR | 0 | 0 | 0 | 0 | 0 | 0 | • | • | • | • | 0 | • | 5 |
| S1 | GPR | 0 | 0 | 0 | 0 | 0 | • | 0 | • | • | 0 | 0 | ٠ | 4 |
| 51 | LR | 0 | 0 | 0 | 0 | 0 | • | • | • | • | 0 | • | ٠ | 6 |
| | RF | 0 | ٠ | • | • | • | • | • | • | • | ٠ | • | ٠ | 11 |
| | LSTM | 0 | • | 0 | 0 | 0 | 0 | • | • | • | 0 | • | ٠ | 6 |
| | Score | 1 | 4 | 3 | 1 | 2 | 3 | 4 | 7 | 7 | 2 | 5 | 7 | 46 |
| | LSBoost | | | • | | • | • | 0 | • | - | | 0 | • | 5 |
| | MPL | | \mathbf{O} | • | | 0 | • | 0 | • | | N/A | • | • | 5 |
| | SVR | | | • | | 0 | 0 | 0 | • | | | • | ٠ | 4 |
| S2 | GPR | NT/A | NT/A | • | NT/A | 0 | • | 0 | • | NT/A | | 0 | • | 4 |
| 52 | LR | N/A | N/A | • | N/A | 0 | • | • | • | N/A | | 0 | ٠ | 5 |
| | RF | | | • | | 0 | 0 | • | • | | | • | • | 5 |
| | LSTM | | | 0 | | 0 | 0 | • | • | | | • | • | 5 |
| | Score | | | 6 | | 1 | 4 | 3 | 7 | | | 4 | 7 | 32 |

Note: N/A indicates the feature is excluded in S2

| Feature subset | ML | | Selected features | | | | | | | | | | | | | |
|-------------------|---------|-----------------|-------------------|------------|------|--------------|-----|-----|-----|-----|----|-----|------|--------|----------------|--|
| | models | EC- Trans(t) | OP- Trans | EC- All | TES | RW- Trans | R&D | NEI | RCI | AVM | GP | POP | GDP | CO2(t) | of features | |
| | LSBoost | 0 | • | 0 | 0 | • | 0 | 0 | 0 | • | 0 | 0 | 0 | ٠ | 4 | |
| | MPL | • | 0 | 0 | 0 | 0 | • | 0 | • | • | • | 0 | • | ٠ | 7 | |
| | SVR | 0 | 0 | • | 0 | 0 | 0 | • | • | • | • | 0 | 0 | ٠ | 6 | |
| C1 | GPR | 0 | 0 | 0 | 0 | 0 | • | 0 | 0 | • | • | 0 | 0 | ٠ | 4 | |
| S1 | LR | • | 0 | • | 0 | 0 | • | 0 | • | • | • | 0 | • | ٠ | 8 | |
| | RF | 0 | • | • | 0 | • | 0 | 0 | • | • | • | 0 | 0 | • | 7 | |
| | LSTM | • | • | 0 | • | 0 | • | • | • | • | • | • | • | • | 11 | |
| | Score | 3 | 3 | 3 | 1 | 2 | 4 | 2 | 5 | 7 | 6 | 1 | 3 | 7 | 47 | |
| | LSBoost | • | N/A | • | - | | 0 | 0 | • | N/A | • | | | • | 5 | |
| | MPL | • | | • | | | 0 | • | • | | | | | • | 6 | |
| | SVR | 0 | | • | | | 0 | • | • | | • | | 27/4 | ٠ | 5 | |
| G2 | GPR | • | | 0 | NT/A | | • | • | • | | • | | | • | 6 | |
| S2 | LR | • | | ٠ | N/A | N/A | ٠ | 0 | • | | • | N/A | N/A | ٠ | 6 | |
| | RF | • | | ٠ | | | ٠ | 0 | ٠ | | • | 1 | | ٠ | 6 | |
| | LSTM | • | | ٠ | | | 0 | ٠ | • | | • | 1 | | ٠ | 6 | |
| | Score | 6 | | 6 | 1 | | 3 | 4 | 7 | | 7 | 1 | | 7 | 40 | |

| Table 7. Selected feature subsets with the ML models for forecasting CC | $_{2}(t+1).$ |
|---|--------------|
|---|--------------|

Note: N/A indicates the feature is excluded in S2

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Highlights:

- An interpretable multi-stage forecasting framework is proposed.
- The drivers of energy consumption and CO2 emissions in UK's transport sector are identified.
- A comprehensive comparison between different machine learning models is carried out.
- The impacts of feature selection methods on machine learning models are investigated.

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Declaration of interests

☑ The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

□ The authors declare the following financial interests/personal relationships which may be considered as potential competing interests:

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