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# Structures

journal homepage: www.elsevier.com/locate/structures

# A review on the shear performance of reinforced concrete (RC) beams strengthened with externally bonded mortar-based composites

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### ARTICLE INFO

Keywords: Reinforced concrete Beam Mortar-based composites Shear Strengthening Retrofitting FRCM FRC ECC UHPFRC

## ABSTRACT

This paper reviews the performance of shear strengthened reinforced concrete (RC) beams with the use of externally bonded mortar-based composite jackets (e.g. FRCM, ECC, UHPFRC). An experimental database was compiled gathering all the known studies in strengthening shear deficient RC beams using innovative mortar-based systems. The role of the RC beams' inherent deficiencies as well as the impact of the design parameters of the alternative jacketing configurations were identified. Existing design models proposed to predict the contribution of the mortar-based composites to the shear strength of RC beams were assessed using the database and conclusions were drawn regarding their accuracy.

### 1. Introduction

Most of the existing reinforced concrete (RC) buildings were designed according to old design standards which often overestimate RC beams' shear strength [1–3]. In addition, poor reinforcement detailing such as insufficient transverse reinforcement (i.e., inadequately anchored, sparse stirrups, smooth bars) and lap-splices in the plastic hinge region increase further their susceptibility by promoting brittle failure modes such as shear failure that may jeopardise the structure's integrity and cause huge property and life losses [1–3]. Furthermore, ageing of materials (e.g. corrosion of the steel reinforcement), the new challenges imposed by climate change accelerate structural deterioration and increase dramatically their susceptibility. Therefore, to maintain the existing building stock, strengthening becomes the only viable solution.

With the development of composite materials, fibre-reinforced polymer (FRP) jacketing has become an effective intervention method in civil engineering projects, and has been widely used to strengthen deficient RC structures worldwide [4]. However, FRP has significant shortcomings mainly related to its epoxy resin matrix, such as the poor performance at high temperatures, non-applicable to wet surfaces, and incompatible with concrete and masonry [5]. To overcome the issues

arising by the use of resins, alternative composite systems have been introduced which retain the advantages of FRP applications but use inorganic (mortar-based) binders instead of resin [6].

Based on the type of textile, various mortar-based composite systems have been developed for the shear strengthening of beams. The term Fibre-Reinforced Cementitious Mortar (FRCM) systems is widely used to include the following systems: (i) TRM (Textile-Reinforced Mortar), in which carbon (CFRCM), glass (GFRCM), basalt (BFRCM) textiles are used [7–9]; (ii) PFRCM (PBO-FRCM), in which Poliparafenilen benzobisoxazole (PBO) textiles are utilised [10]; and (iii) SRG (Steel-Reinforced Grout), in which Ultra-High Tensile Strength Steel (UHTSS) textiles are applied [4,11,12] (Fig. 1).

Gonzalez-Libreros et al. [6] collected the experimental results of 89 externally bonded FRCM shear strengthened RC beams and evaluated the effects of geometry and mechanical properties of beams and strengthening systems. In addition, [6] assessed the efficiency of four analytical models in predicting the shear strength of FRCM strengthened RC beams. According to [6], FRCM systems could improve the shear capacity from 3 % to 195 %, with an average of 55 %, and could also change the failure mode of beams from shear to flexural mode. In addition, the effectiveness of the jacket was affected by parameters such as the strengthening configuration, the compressive strength of the

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https://doi.org/10.1016/j.istruc.2023.105474

Received 11 January 2023; Received in revised form 6 August 2023; Accepted 27 October 2023 Available online 6 November 2023







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Fig. 1. Textiles used in FRCM jacketing applications: (a) carbon; (b) glass; (c) basalt; (d) PBO; (e) steel textiles.

Table 1				
Summary of t	he studies	included i	in the	database.

Reference	SS	$f_c$ (MPa)	a/d	$\rho_w$ (%)	$ ho_f(\%)$	Number of strengthened beams		ode
							Shear	Flexural
[11]	FRCM	34.0	1.6-3.1	0.00	0.19, 0.38	8	8	
[18]	FRC	28.3	2.6	0.12	_	1	1	
[24]	FRC	30.0	1.5, 2.5	0.19	2.00	4	4	
[25]	FRC	26.3	2.3, 3.0	0.00	2.00	3	3	
[26]	FRC	30.0	4.5	0.00	0.00-0.015	4	4	
[4]	FRCM	28.0, 23.0	2.2	0.00	0.08-0.25	9	3	6
[10]	FRCM	39.0	2.4	0.27	0.03	9	9	
[12]	FRCM	34.0	2.8	0.27	0.19, 0.38	8	8	
[14]	FRC	32.4, 36.7	2.8	0.11	0.00 - 1.50	7	7	
[15]	FRC	28.6	1.6	0.89	2.00	2	2	
[16]	FRC	44.8	2.0, 3.0	0	1.50	8	8	
[20]	FRCM	25.8	2.0	0.18	0.12	6	6	
[27]	FRCM	34.0	2.6	0.13	0.15-0.44	8	8	
[28]	FRC	26.6	2.0, 3.0	0	-	4	4	
[29]	FRC	30.0	2.1	0.13	2.0	2	1	1
[30]	FRCM	36.0	2.4	0.27	0.03	4	4	
[31]	FRCM	39.0	2.4	0.27	0.03	1	1	
[9]	FRCM	61.0	3.2	0.00-0.19	-	3	3	
[32]	FRCM	16.8-20.0	1.6-3.6	0.00	0.09-0.60	19	19	
[33]	FRCM	30.0	2.0	0.00, 0.18	0.12, 0.13	6	6	
[34]	FRCM	30.0	1.8	0.00	0.08, 0.13	6	5	1
[35]	FRCM	61.0	1.6	0.00, 0.19	-	2	2	
[36]	FRC	30.0	2.1	0.13	2.0	2	1	1
[13]	FRC	35.0	2.2	0.33	-	3	3	
[23]	FRCM	21.0-25.0	3.3	0.23, 0.33	0.06, 0.36	6	6	
[37]	FRCM	30.0	2.0	0.00	0.06-0.13	15	15	
[38]	FRCM	45.0	2.5	0.00, 0.61	0.02-0.10	6	6	
[8]	FRCM	16.0-18.0	3.2	0.00	1.86-3.80	9	9	
[17]	FRC	24.4-25.2	3.3	0.21	-	5	5	
[39]	FRCM	36.0	3.0	0.00-0.50	1.33, 2.67	6	6	
[40]	FRCM	11.0-20.0	2.3, 2.6	0.00	0.36-0.60	20	19	1
[41]	FRCM	11.0-20.0	1.6	0.00	0.06-0.26	9	10	
[1]	FRCM	38.0	2.2	0.00	-	4	4	
[42]	FRC	26.3	1.8	0.00, 0.30	-	9	9	
Total						218	208	10

matrix relative to the concrete compressive strength and the axial stiffness of the fibre. It was also highlighted that beam's shear strength was improved substantially when the compressive strengths of the matrix and the substrate were similar. Regarding the assessment of existing models to predict the shear strength of the FRCM jacket, it was concluded that the analytical model based on bare fibre characteristics provided more accurate results [6].

Recently, Engineering Cementitious Composites (ECC), Steel Fibre-Reinforced Concrete (SFRC) and Ultra-High Performance Fibre-Reinforced Concrete (UHPFRC) are applied in the form of jackets as externally bonded reinforcement or near surface embedded elements for shear strengthening of deficient RC beams [13–16]. Other hybrid systems developed use FRP grids or welded bar meshes embedded in ECC or other types of cementitious composites like Polymer-Modified Mortar (PMM) or sprayed Polymer-Cement Mortar (PCM) [17,18]. The term ECC-R will be used in the following to describe this last group of hybrid mortar-based composites. To facilitate the descriptions in the following, ECC, UHPFRC, SFRC and ECC-R are collectively referred to as FRC (Fibre Reinforcement Concrete).

Recent studies have confirmed that mortar-based composites system is an effective externally applied reinforcement for RC beams and columns [6,19–22]; however, the studies on the shear behaviour of strengthened RC beams are still limited [23].

In the first part of this paper, a detailed literature review was carried out on the shear performance of RC beams strengthened with mortarbased composite jacketing. A database was compiled and the impact of the design parameters of the beams and the mortar-based composite systems on the shear strength increase was studied. In the second part, existing design models proposed to predict the contribution of the mortar-based composites to the shear strength of RC beams were assessed using the database and conclusions are drawn regarding their accuracy.

### 2. Experimental database

An overview of the studies considered for the development of the



Fig. 2. Variation of  $V_{JAC}/V_{CON}$  as a function of the various mortar-based composite systems.

experimental database is presented in Table 1 (218 beams from 36 experimental studies), including FRCM (TRM, PFRCM, SRG) and FRC (SFRC, UHPFRC, ECC, ECC-R) jacketing systems. The literature is sorted based on the publication year, from the most recent (2020) to the oldest (2014). The data range of the strengthening system (SS), the concrete compressive strength  $(f_c)$ , the shear span ratio (*a/d*), the stirrup

reinforcement ratio ( $\rho_w$ ), the web reinforcement ratio of the textile in FRCM and fibres' volume fraction in FRC ( $\rho_f$ ), as well as the mode of failure as typical parameters influencing shear performance in each literature are also presented in Table 1. The detailed database compiled for the known mortar-based composites is shown in Table A1 of Appendix A.

The database (see Table A1), apart from the details of the beams and the applied mortar-based composites, presents the failure modes observed during testing as well as the shear strength provided by the mortar-based composite jacket  $V_{JAC}$  (=  $V_{RET} - V_{CON}$ ; where  $V_{RET}$  and  $V_{CON}$  are the shear strength of the strengthened and the corresponding reference beam (control beam)). The ratio  $V_{JAC}/V_{CON}$  reflects the contribution of the mortar-based composite on the strength increase of the control beams. In the following, graphs are developed which illustrate the impact of the mechanical and geometrical properties of the strengthened beams on  $V_{JAC}/V_{CON}$ . The data are grouped based on their mode of failure using the classification proposed by [6]. The shear strengthened beams failed in three distinct modes: i) flexural failure where concrete crushing follows the longitudinal steel bar yielding; ii) shear failure where failure is caused by diagonal tension, fabric rupture, etc.; and iii) shear-detachment where shear failure occurs when detachment occurs either between the composite and the beam substrate or within the mortar layer (mostly in the case of multi-layered composite jackets). In some cases, the application of the mortar-based composite jackets (fully wrapped) modified the mode of failure from brittle to ductile flexural failure. The beams that present flexural failure can be considered as the lower bound of the strengthening capacity [6].



Fig. 3. Variation of  $V_{JAC}/V_{CON}$  with (a) a/d, (b)  $f'_c$ , (c)  $\rho_{long}$ , (d)  $\rho_w$ .



Fig. 4. Variation of V<sub>JAC</sub>/V<sub>CON</sub> with (a) jacketing configuration and (b) mechanical anchorage systems.

In general, the addition of mortar-based composite jacketing systems substantially improved the shear behaviour of the RC beams (up to 196 %), as presented in Fig. 2 (The purple curve indicates the percentage of the beams (see the secondary axis) of the database that corresponds to the data related to each abscissa interval). For FRCM systems, the shear strength of RC beam was increased by 61 % on average, 196 % on the maximum and 4 % on the minimum. The average strengthening effect of FRC systems (80 %) was slightly better than that of FRCM system, and the shear strength of RC beam can be increased from 4 % to 190 % in the data collected. There is a large variation of  $V_{JAC}/V_{CON}$  depending on the system applied and the mode of failure (Fig. 2). Most of the beams were strengthened using FRCM systems (72 % of the beams of the database) and among them the CFRCM is the dominant one (36 % of the jacketed beams). SRG and ECC systems were applied equally to 15 % of the beams of the database. The less investigated systems seem to be the UHPFRC (2 %), SFRC (6 %) and ECC-R (5 %) jacketing.

### 2.1. Evaluation of the design parameters of the strengthened RC beams

In this section, the variation of  $V_{JAC}/V_{CON}$  as a function of the design parameters of the beams such as the shear span ratio, a/d, the mean cylindrical concrete compressive strength,  $f_c$ , the longitudinal steel reinforcement ratio,  $\rho_{long}(=A_{sl}/b_wd)$ , and the stirrup reinforcement ratio,  $\rho_w(=A_w/b_ws)$  (where *s* is the stirrups spacing;  $b_w$  is the beam width;  $A_{sl}$  is the sectional area of the tensile reinforcement;  $A_w$  is the sectional area of the stirrups) is presented in Fig. 3.

Most of the tested beams have a shear span ratio, a/d, between 2 and 3 (71 %) which corresponds to the 'shear failure valley', that is, the transition zone between shear compression failure and oblique tension failure [43] (Fig. 3(a)). The variation of  $V_{JAC}/V_{CON}$  as well as the mode of failure seems to be independent from a/d. The variation of  $V_{JAC}/V_{CON}$  with the concrete compressive strength,  $f_c$ , is presented in Fig. 3(b). The highest values of strength increase are observed for  $f_c$  values up to 20 MPa (24 %), which are considered representative of old type construction. As observed in Fig. 3(b), there is a trend the effectiveness of the mortar-based composite systems to decrease as the concrete compressive strength increases.

Regarding the reinforcement detailing of the beams, most of the beams (64 %) have a longitudinal steel reinforcement ratio,  $\rho_{long}$ , higher than 0.02, which in some cases exceed the maximum reinforcement ratio,  $\rho_{max}$ , to avoid flexural failure (Fig. 3(c)). The stirrup reinforcement ratio,  $\rho_w$ , seems to influence the effectiveness of the mortar-based composite jackets (Fig. 3(d)). Excluding the case of  $\rho_w = 0$  (no presence of stirrups in the shear critical region), for  $\rho_w$  values up to 0.0025,

which corresponds to beams strengthened with FRCM systems, the effectiveness of the jacket is reduced with the increase of the shear reinforcement (i.e. closely spaced stirrups). This is mainly attributed to the interaction between the internal and external shear reinforcement [6]. The beams with  $\rho_w$  between 0.0030 and 0.0035 seem not to follow this trend, which mainly corresponds to the beams strengthened with FRC jackets. A detailed analysis on the impact of the external shear reinforcement FRCM system follows in section 2.2.

### 2.2. Evaluation of the design parameters of FRCM jacketing systems

### 2.2.1. Strengthening configuration

The database contains 164 collected beams strengthened by FRCM systems (Table A1 - [1,4,8-12,20,23,27,30-35,37-41]). The variation of  $V_{JAC}/V_{CON}$  as a function of FRCM jacket configuration is presented in Fig. 4(a). Regarding the notation given to the alternative jackets, "F" and "U" stand for the fully wrapped and U-shaped jackets, respectively, whereas "SB" for the side bonded. "C" and "S" correspond to continuous textiles and textile strips, respectively. "A" indicates the presence of a mechanical anchorage system. U-shaped jackets were applied to 74 % of the strengthened beams from which 12 % and 48 % used continuous textiles with and without mechanical anchorage, respectively. The rest used textile strips with (8 %) and without mechanical anchorage (6 %). Side bonded jackets with continuous textiles and textiles strips were applied to 14 % and 8 % of the database beams, respectively. By excluding the fully wrapped beams (4%), in general the U-shaped FRCM jackets seem to be more effective when compared to the side bonded ones. As observed in Fig. 4(a), the most common mode of failure is shear detachment (49 %), which was observed even in the beams that mechanical anchorage was used (23 %).

systems mechanical anchorage 40 The used in [4,8,10,23,27,30,31,37,40,41] out of 164 beams of the database for the application of the FRCM jackets are the following: i) metallic (steel or aluminium) anchors; ii) FRCM/FRP insertion anchors; iii) near surface mounted (NSM) anchors; and iv) horizontal FRCM laminate anchors. Details about the aforementioned mechanical anchorage systems can be found in [44]. Fig. 4(b) presents the relationship between the failure modes of the strengthened beams when the mechanical anchorage systems were adopted. For U-wrapped strengthened beams, except for NSM anchors, the other three methods can improve the adhesion between the FRCM system and the concrete surface. Metallic (steel or aluminium) anchors are an effective method to prevent debonding of the system significantly, but [38] illustrated that it is ineffective in preventing the fibre from sliding in the matrix. No detachment failure mode can be found for FRCM/FRP insertion and horizontal FRCM laminate anchors.



Fig. 5. Failure modes: (a) shear-fibre rupture; (b) shear-detachment.

In the research carried by [8], T-beams strengthened with the 2-layered carbon TRM jacket using FRCM/FRP insertion anchors had similar behaviour to the 4-layered carbon TRM jacketed beams without anchorage system, thus demonstrating the need of using anchorage systems in providing a more cost-effective strengthening solution. However, according to Baggio et al. [6], the use FRCM/FRP insertion anchors in U-shaped FRCM jacketed rectangular beams increased strength by only 3 % compared with beams without anchors. As observed by [16] the lack of effectiveness of such an anchorage system may be related to the fact that the anchors are intended to restrain outof-plane peeling of the composite and do not restrain the in-plane fibre slippage. Moreover, [6] demonstrated that although beams with and without anchors exhibited diagonal tension shear failure, the presence of anchors slightly changed the inclination of shear cracks around the anchors. In the collected data, only 50 % of the samples with NSM anchorage prevented detachment. It is worth noting that all these detached NSM anchorage samples refer to the U-shaped strip configuration. However, [30] demonstrated that NSM system was still effective compared with the non-anchored ones, since they had higher shear capacity and delayed the occurrence of detachment. The failure mode observed was the gradual crack's development, leading eventually to jacket debonding. In the case of side-bonded jacketing, metallic anchors could not prevent the detachment of the jackets (Fig. 4(b)).

# 2.2.2. Failure modes

The failure modes of the FRCM shear strengthened beams included in the database for the different jacketing configurations are presented in Fig. 4(a). Additionally, Fig. 5 illustrates the typical failure modes attributed to fibre rupture or detachment of the jacket.

<u>Fully wrapped beams</u>: In most cases, failure occurred due to fibre rupture. Although debonding is most likely to happen first, shear capacity is controlled by the rupture of the textile [4,40]. The fully wrapped configuration creates a larger contact area and bonding strength between the jacket and substrate, enhancing the interface friction and transfer of frictional forces between the strengthening system and concrete. Furthermore, the fully wrapped configuration creates a tight wrapping layer that serves as a protective barrier for the concrete surface, reducing the risk of surface delamination and damage. These factors make the mortar-based composite jacket less prone to premature detachment and increase the likelihood of transforming the beam's response from shear to flexural failure. In case of shear failure, noticeable diagonal cracks can be observed on the jacket, especially near the supports and load application points, with fibre rupture commonly occurring at the crack initiation location at the bottom of the beam [46]. Fig. 5(a) illustrates a typical shear failure mode caused by fibre rupture.

U-wrapped beams: Most U-wrapped beams without mechanical anchorage systems failed due to detachment of the composite, which can be further classified as follows: (a) detachment of the textile from the jacket-beam interface accompanied by the peeling of the beam's cover; (b) complete extraction of some fibres in the textile; (c) detachment of the jacket itself accompanied by the detachment of the mortar-fabric/ mortar layers or the delaminated or slipped multi-layer textiles. Fig. 5 (b) illustrates the potential detachment mode in this failure scenario, with the left side presenting the frontal view and the right side showing the top view. It is worth noting that in this failure mode, shear diagonal cracks on beams can be observed after the jacket is removed. In general, the detachment of mortar-based composite jacketing does not affect the concrete surface of RC beams [4,8,12], but a few researchers mention that the concrete cover peels off [5,39]. In addition, [37] observed that fibre slippage was more likely to occur in fabrics with higher density since the closely spaced fibres may prevent the uninhibited flow of the mortar, leading thus to a reduced bond quality. The beams failing in this mode often demonstrate significantly constrained ductility [46]. Another key failure mode similar to that of a fully wrapped reinforcement configuration is the rupture of the fibre [27,41]; this appears to be more common in systems with anchors. In the case of U-wrapped jackets with anchors, there is another failure mode in which the anchorage is separated or the surrounding area of the anchorage is damaged [8,10]. This phenomenon is also common in FRP systems [45].

Side bonded beams: Detachment was the mode of failure observed for the side bonded beams. Almost all specimens had 45° diagonal cracks at the load location when failure occurred [20,37]. [37] observed the following detachment patterns: (i) longitudinal stripping of the jacket at the top; (ii) debonding of the jacket in the vertical direction, that is, the detachment along with the whole depth of the beam at the load position; (iii) longitudinal peeling of mortar-based composite system at the bottom; and (iv) the peeling of the jacket in the inclined direction, which is more common on the inclined mortar-based composite system strips. Based on the data collected, anchoring does not have a significant impact on the failure mode of side bonded jackets. Therefore, to avoid premature detachment of the strengthened beams, certain design codes for externally bonded FRP composite materials design prohibit using



Fig. 6. Variation of  $V_{JAC}/V_{CON}$  with (a)  $\varepsilon_{fu}$ , (b)  $\rho_f$ , (c)  $E_f \rho_f$ , (d)  $E_s \rho_w/E_f \rho_f$  (e)  $\rho_{cm}$ , (f)  $f'_{cm}/f'_c$ 

side bonded jackets [46]. Based on the review, this approach may need to be adopted also for the case of FRCM systems.

In addition to the influence of the strengthening configuration on the failure mode, the reinforcement ratio of longitudinal and transverse bars ( $\rho_{long}$  and  $\rho_w$ ) in the beam also has an impact. As shown in Fig. 3(c) and (d), increasing  $\rho_{long}$  and  $\rho_w$  leads to a slight decrease in the probability of detachment of the strengthening jacket. This decrease can be attributed to the fact that a higher reinforcement ratio enhances the load transfer mechanisms within the beam, thereby reducing localized stress concentrations. This improved load transfer capacity reduces the strain and stress on the strengthening jacket, thereby reducing the risk of detachment. Furthermore, a higher  $\rho_{long}$  and  $\rho_w$  contributes to better control of

deflection and crack development in the beam, which enhances the overall structural integrity and limiting concrete's cover peeling. The reduced deflection also mitigates the discrepancy in load displacement response between the strengthening system and the substrate, thereby further preventing detachment.

# 2.2.3. Evaluation of the design parameters of the FRCM system

The variation of  $V_{JAC}/V_{CON}$  with the nominal ultimate strain of the textiles as provided by the manufacturer ( $\varepsilon_{fu}$ ), the web reinforcement ratio of the textile ( $\rho_f$ ), the axial rigidity of the textile ( $E_f\rho_f$ ), the FRCM reinforcement ratio ( $\rho_{cm}$ ), and  $f'_{cm}/f'_c$  (where  $f'_{cm}$  is cementitious matrix compressive strength) is depicted in Fig. 6. The web reinforcement ratio



Fig. 7. Variation of  $V_{JAC}/V_{CON}$  with (a) fibre type, (b) volume fraction of fibres, and (c) jacketing configuration and (d). $b_{w,FRC}/b'_{w}$ 

 $(\rho_f)$  and the FRCM reinforcement ratio  $(\rho_{cm})$  are defined as follows [6]:

$$p_f = 2nt_f w_f / b_w s_f \tag{1}$$

$$\rho_{cm} = 2t_{cm} w_f / b_w s_f \tag{2}$$

where *n* is the number of textile layers applied;  $t_f$  is the thickness of the textile;  $t_{cm}(=(n+1)t_m)$  is the total thickness of the FRCM composite ( $t_m$  is the nominal thickness of a single mortar layer); $w_f$  is the width of FRCM strips; and  $s_f$  is the longitudinal distance of FRCM strips (if the textiles are applied as continuous, then  $w_f = s_f = 1$ ).

Regarding  $\varepsilon_{fu}$ , apart from glass and basalt fibre, the rest of the materials have two or more different values for  $\varepsilon_{fu}$ . Most of the beams (53 %) were strengthened with textiles that had  $\varepsilon_{fu}$  in the range of 1.5–2.0 % (Fig. 6(a)). 87 % of the strengthened beams had a web reinforcement ratio  $\rho_f <$  0.0045 and 48 % had  $\rho_f <$  0.0015 (Fig. 6(b)). The variation of  $V_{JAC}/V_{CON}$  seems not to be directly related to the amount of web reinforcement confirming similar observations made in other studies [52–54]. The increase of  $\rho_f$  has a slight impact on the CFRCM jacket shear strength (average :  $V_{JAC}/V_{CON} = 0.86$ ), a significant impact on the and GFRCM strength Bjacket shear (average :  $V_{JAC}/V_{CON}$  = 1.10and0.69) and almost no effect on the PFRCM and SRG (*average* :  $V_{JAC}/V_{CON} = 0.25$  and 0.62).

The interaction between internal transverse steel reinforcement (stirrups) and the externally bonded FRCM jackets has not been studied in detail. Similar to the approach adopted for FRP jacketing [47], the ratio of the axial stiffness of the transverse steel reinforcement to that of the FRCM composite ( $E_S \rho_W / E_f \rho_f$ ; where  $E_f \rho_f$ , is axial rigidity of the

textile index of FRCM composites;  $E_f$  is the elastic modulus of the textile fibres in GPa;  $E_s$  is the elastic modulus of steel reinforcement) is used to evaluate the interaction between stirrups and the FRCM system. In Fig. 6 (c) and (d), the relationship between  $E_f \rho_f$  and  $E_S \rho_W / E_f \rho_f$  with  $V_{JAC} / V_{CON}$ is presented, respectively. The  $E_f \rho_f$ , which expresses the axial rigidity of the textile, for most of the jackets lies between 0.052 and 1 (89 % of the beams). For similar axial rigidity values, the PFRCM system seems less effective than the rest of the FRCM systems (C-, G-, BFRCM and SRG). When internal shear reinforcement is present (Fig. 6(d)), the increase of  $E_S \rho_W / E_f \rho_f$  (i.e., more stirrups for the beam) renders the contribution of the FRCM system less effective. Using the experimental data shown in Fig. 6(d), and after applying exponential curve fitting to the data (51 beams), the following empirical expression is derived:

$$V_{FRCM}/V_{CON} = 0.383 \left( E_s \rho_w / E_f \rho_f \right)^{-0.3}$$
(3)

Eq. (3) should be treated with caution since it is based on a limited amount of data.

Regarding the FRCM reinforcement ratio, most of the specimens (79%) receive  $\rho_{cm}$  values between 0.06 and 0.18 (Fig. 6(e)). In general, the increase of  $\rho_{cm}$  leads to increased shear capacity for the beams. This is attributed to the fact that an increase in  $\rho_{cm}$  corresponds to an increase in the thickness of the FRCM mortar, which increases the cross-sectional area (especially the width) of the RC beam, thereby improving the shear capacity of the beam. The impact of the cementitious matrix compressive strength,  $f_{cm}^{\prime}$ , on  $V_{JAC}/V_{CON}$  is presented in Fig. 6(f). 91% of the studies used  $f_{cm}/f_c^{\prime}$  between 0.5 and 2.5. As observed in the Fig. 6(f),

#### Table 2

Analytical models for the shear strength contribution of the FRCM jacket based on fibre properties.

Reference	V <sub>FRCM</sub>
Model 1 [51]; Model 2	$V_{FRCM} = 2nt_f h_f rac{w_f}{s_f} arepsilon_{eff} E_f(\cot  heta + \cot lpha) sin lpha V_{FRCM} = 2nt_f h_f rac{w_f}{s_f} arepsilon_{eff} E_f; \  heta = 0$
[52]*	$45^{0}; \alpha = 90^{0}$
	For [51]: $\varepsilon_{eff} = 0.5\varepsilon_{fu}$
	For [52]: For fully wrapped: $\varepsilon_{eff} = 0.035 \left(\frac{f_c^{2/3}}{\rho_f E_f}\right)^{0.65} \varepsilon_{fu}$
	<u>2</u> 0.55
	For side bonding or U-wrapped: $\varepsilon_{eff} = 0.020 \left( \frac{f_c^3}{\rho_f E_f} \right)  \varepsilon_{fu}$
	Experimental value of effective strain: $e_{eff}^{exp} = \frac{V_{FRCM}^{exp}}{2nt_f h_f (w_f/s_f) E_f}$
Model 3 [7]	$V_{FRCM} = 2nt_f b_w h_f rac{W_f}{s_f} f_{fed}(cot heta sin lpha + cos lpha);$
	$V_{FRCM} = 2nt_f b_w h_f rac{w_f}{s_f} f_{fed}; \ \theta = 45^0; a = 90^0; f_{fed} = D_f f_{fed,max} f_{fed,max} =$
	$8.67 eta_l eta_w \sqrt{rac{1000\sqrt{f_c}}{nt_f}}; eta_l = egin{cases} 1, \lambda \geq 1 \ \sin\left(rac{\pi\lambda}{2} ight), \lambda < 1 \end{cases}; eta_w =$
	$\sqrt{rac{2-w_f/(s_f sinlpha)}{1+w_f/(s_f sinlpha)}}$
	$D_{f} = \left\{ rac{2}{\pi \lambda} igg( rac{1 - \cos\left(rac{\pi \lambda}{2} ight)}{\sin\left(rac{\pi \lambda}{2} ight)} igg), \lambda \leq 1  ight.; \lambda = L_{max}/L_{e}$
	$1-rac{\pi-2}{\pi\lambda},\lambda>1$
	$L_{max} = \begin{cases} h_f/sin\alpha, \text{for U-wrapped jackets} \\ h_f/2sin\alpha, \text{for side bonding jackets} \end{cases}; L_e = 15 \sqrt{\frac{1000nt_f}{\sqrt{f_c}}}$
	$h_{fe} = z_b - z_t;  z_b = h_f - (h - d_{fb});  z_t = d_{ft}$

\* *n* is the number of textile layers applied;  $t_f$  is the thickness of fibre sheets;  $h_f$  is the effective depth of the jacket taken as 0.9d;  $w_f$  is the width of FRCM strips;  $s_f$  is the longitudinal distance of FRCM strips;  $\varepsilon_{eff}$  is the fibre effective strain;  $E_f$  is the elastic modulus of the fabric;  $\alpha$  is the angle between the fibres and the beam axis perpendicular to the shear force;  $\theta$  is the angle between the concrete compression strut and the beam axis perpendicular to the shear force.

\*\*  $D_f$  is the stress distribution coefficient;  $f_{fed,max}$  is the maximum design stress of the jackets;  $\beta_l$  and  $\beta_w$  reflect the effect of the effective bond length and the concrete width ratio of the jacket;  $\lambda$  is the maximum bond length parameter;  $L_{max}$ and  $L_e$  are the available bond length and the effective bond length respectively;  $z_b$  and  $z z_t$  are the co-ordinates of the top and bottom ends of the effective FRCM;  $d_{fb}$  is the distance from the compression face to the top edge of the FRCM;  $d_{ft}$  is the distance from the compression face to the lower edge of the jacket.

there is not direct correlation between  $f'_{cm}/f'_c$  to  $V_{JAC}/V_{CON}$ .

### 2.3. Evaluation of the design parameters of FRC jacketing systems

The database presented in Table A1 contains 54 collected beams strengthened by the FRC (ECC, ECC-R, SFRC and UHPFRC) systems [13–18,24–26,28,29,36,42]. Fig. 7(a) and (b) present the variation of  $V_{JAC}/V_{CON}$  with the fibre type and the fibres' volume fraction. Since some studies do not provide information on the specific fibre types and volume fractions, only the specimens for which full details are provided are presented in Fig. 7(a) and (b) (46 and 31 beams were used in Fig. 7 (a) and (b), respectively). Most FRC systems use steel fibres (57 %), followed by PVA and PE fibres (28 % and 15 %, respectively). A smaller percentage of FRC jacketed beams, especially in the cases that steel or PVA fibres are used, fails due to detachment compared with FRCM strengthened beams. [48] demonstrated that the FRC system can offer a better bonding effect with the beam surface to prevent the occurrence of partial detachment. As seen in Fig. 7(a), the shear strength increases for PE, PVA and steel fibre systems ranges between 5 % and 88 %, 10 % to

### Table 3

Analytical models for the shear strength contribution of the FRCM jacket based on FRCM composite properties.

	Reference	V <sub>FRCM</sub>
Experimental value of effective strain: $\varepsilon_{eff}^{exp} = \frac{V_{FRCM}^{exp}}{nA_f E_{FRCM} d}$ Model 5 [54] $V_{FRCM} = k_e \varepsilon_{eff} E_{FRCM} \rho_f b_w d(\cot\theta + \cot a) sina;$ $v_{FRCM} = k_e \varepsilon_{eff} E_{FRCM} \rho_f b_w d; \theta = 45^{\circ}; a = 90^{\circ};$ $\varepsilon_{eff} = \frac{f_{fdd}}{E_{FRCM}} \left[ 1 - \frac{1}{3} \frac{l_e sina}{\min(0.9d; h_f)} \right]; f_{fdd} = \frac{0.24}{\gamma_{fd} \sqrt{\gamma_c}} \sqrt{\frac{E_{FRCM} k_b} \sqrt{f_{ck} f_{cm}}},$ $f_{cam}^{\prime} = 0.30 f_{ck}^{\prime 2/3} k_b = \left( \frac{2 - w_f / b}{1 - w_f / 400} \right)^{0.5}; l_e = \left( \frac{E_{FRCM} t_f}{2 f_{cam}} \right)^{0.5}; k_e = 0.5$ $b = \begin{cases} s_f, forstrips \\ 0.9 dsin(\theta + \alpha) / sin\alpha, for continous; \end{cases}$ Experimental value of effective strain: $\varepsilon_{eff}^{exp} = \frac{V_{FRCM}^{exp}}{k_e E_{FRCM} \rho_f b_w d}$ Model 6 [37] $V_{FRCM} = F_z (V_m + V_f);$ $*** F_z = \frac{Nw_f}{a} V_m = 2(0.17 \sqrt{f_{cm}} t_m d); V_f = 2nA_f f_{fv} df_{fv} = E_{FRCM} \varepsilon_{eff};$ $\varepsilon_{eff} = \varepsilon_{FRCM} \le 0.004$ Experimental value of effective strain: $\varepsilon_{eff}^{exp} = \frac{(V_{FRCM}^{exp} / F_z - V_m)}{2nA_f E_{FRCM} df_z}$	Model 4 [53]*	$egin{aligned} V_{FRCM} &= nA_f f_{f\nu} h_f; \ A_f &= 2t_f w_f / s_f; f_{f u} &= E_{FRCM} arepsilon_{eff};  arepsilon_{eff} = arepsilon_{FRCM} \leq 0.004 \end{aligned}$
		Experimental value of effective strain: $e_{eff}^{exp} = \frac{V_{FRCM}^{exp}}{nA_f E_{FRCM} d}$
** $V_{FRCM} = k_{e} \varepsilon_{eff} E_{FRCM} \rho_{f} b_{w} d; \theta = 45^{\circ}; \alpha = 90^{\circ};$ $\varepsilon_{eff} = \frac{f_{fdd}}{E_{FRCM}} \left[ 1 - \frac{1}{3} \frac{l_{e} sin\alpha}{\min(0.9d; h_{f})} \right]; f_{fdd} = \frac{0.24}{r_{fd}\sqrt{r_{c}}} \sqrt{\frac{E_{FRCM} k_{b} \sqrt{f_{ck} f_{cm}}}{t_{f}}};$ $f'_{ctm} = 0.30 f'_{ck}^{2/3} k_{b} = \left( \frac{2 - w_{f} / b}{1 - w_{f} / 400} \right)^{0.5}; l_{e} = \left( \frac{E_{FRCM} t_{f}}{2 f_{ctm}} \right)^{0.5}; k_{e} = 0.5$ $b = \begin{cases} s_{f}, forstrips\\ 0.9dsin(\theta + \alpha) / sin\alpha, forcontinous; \end{cases}$ Experimental value of effective strain: $\varepsilon_{eff}^{exp} = \frac{V_{FRCM}^{exp}}{k_{e} E_{FRCM} \rho_{f} b_{w} d}$ Model 6 [37] $V_{FRCM} = F_{z} (V_{m} + V_{f});$ $F_{z} = \frac{Nw_{f}}{a} V_{m} = 2(0.17 \sqrt{f_{cm}} t_{m} d); V_{f} = 2nA_{f} f_{fv} df_{fv} = E_{FRCM} \varepsilon_{eff};$ $\varepsilon_{eff} = \varepsilon_{FRCM} \leq 0.004$ Experimental value of effective strain: $\varepsilon_{eff}^{exp} = \frac{(V_{FRCM}^{exp} / F_{z} - V_{m})}{2nA_{f} E_{FRCM} d}$	Model 5 [54]	$V_{FRCM} = k_e \varepsilon_{eff} E_{FRCM} \rho_f b_w d(\cot\theta + \cot\alpha) \sin\alpha;$
$\begin{split} \varepsilon_{eff} &= \frac{f_{fdd}}{E_{FRCM}} \left[ 1 - \frac{1}{3} \frac{l_e sin\alpha}{\min(0.9d; h_f)} \right]; f_{fdd} &= \frac{0.24}{\gamma_{fd} \sqrt{\tau_c}} \sqrt{\frac{E_{FRCM} k_b \sqrt{f_{cd} f_{cm}}}{t_f}}; \\ f'_{ctm} &= 0.30 f'_{ck}^{2/3} k_b = \left( \frac{2 - w_f / b}{1 - w_f / 400} \right)^{0.5}; l_e = \left( \frac{E_{FRCM} k_f}{2f_{cm}} \right)^{0.5}; k_e = 0.5 \\ b &= \left\{ \frac{s_f, forstrips}{0.9 dsin(\theta + \alpha) / sin\alpha, for continous}; \right. \\ \text{Experimental value of effective strain:} \varepsilon_{eff}^{exp} &= \frac{V_{FRCM}^{exp}}{k_e E_{FRCM} \rho_f b_w d} \\ \text{Model 6 [37]} & V_{FRCM} = F_z (V_m + V_f); \\ \kappa^{***} & F_z &= \frac{N w_f}{a} V_m = 2(0.17 \sqrt{f_{cm}} t_m d); V_f = 2nA_f f_{fv} df_{fv} = E_{FRCM} \varepsilon_{eff}; \\ \varepsilon_{eff} &= \varepsilon_{FRCM} \leq 0.004 \\ \text{Experimental value of effective strain:} \varepsilon_{eff}^{exp} &= \frac{(V_{FRCM}^{exp} / F_z - V_m)}{2nA_f E_{FRCM} dd} \end{split}$	**	$V_{FRCM} = k_e \varepsilon_{eff} E_{FRCM} \rho_f b_w d; \ \theta = 45^0; \alpha = 90^0;$
$\begin{aligned} f'_{ctm} &= 0.30f'_{ck}^{2/3}k_b = \left(\frac{2-w_f/b}{1-w_f/400}\right)^{0.5}; l_e = \left(\frac{E_{FRCM}t_f}{2f_{ctm}}\right)^{0.5}; k_e = 0.5\\ b &= \begin{cases} s_f, forstrips\\ 0.9dsin(\theta+\alpha)/sina, forcontinous; \end{cases}\\ \text{Experimental value of effective strain:} \varepsilon_{eff}^{exp} &= \frac{V_{FRCM}^{exp}}{k_e E_{FRCM}\rho_f b_w d}\\ \text{Model 6 [37]} & V_{FRCM} = F_z(V_m + V_f);\\ *** & F_z &= \frac{Nw_f}{a}V_m = 2(0.17\sqrt{f_{cm}}t_m d); V_f = 2nA_f f_{fv} df_{fv} = E_{FRCM}\varepsilon_{eff};\\ \varepsilon_{eff} &= \varepsilon_{FRCM} \leq 0.004\\ \text{Experimental value of effective strain:} \varepsilon_{eff}^{exp} &= \frac{(V_{FRCM}^{exp}/F_z - V_m)}{2nA_f E_{FRCM} d} \end{aligned}$		$arepsilon_{eff} = rac{f_{fdd}}{E_{FRCM}} \left[ 1 - rac{1}{3} rac{l_e sin lpha}{\min(0.9d; h_f)}  ight]; f_{fdd} = rac{0.24}{\gamma_{fd}\sqrt{\gamma_c}} \sqrt{rac{E_{FRCM} k_b \sqrt{f_{ck} f_{ctm}}}{t_f}};$
$b = \begin{cases} s_{f}, forstrips\\ 0.9dsin(\theta + \alpha)/sin\alpha, forcontinous; \end{cases}$ Experimental value of effective strain: $\varepsilon_{eff}^{exp} = \frac{V_{FRCM}^{exp}}{k_e E_{FRCM} \rho_f b_w d}$ Model 6 [37] *** $V_{FRCM} = F_z (V_m + V_f);$ $F_z = \frac{Nw_f}{a} V_m = 2(0.17 \sqrt{f_{cm}} t_m d); V_f = 2nA_f f_{fy} df_{fy} = E_{FRCM} \varepsilon_{eff};$ $\varepsilon_{eff} = \varepsilon_{FRCM} \le 0.004$ Experimental value of effective strain: $\varepsilon_{eff}^{exp} = \frac{(V_{FRCM}^{exp}/F_z - V_m)}{2nA_f E_{FRCM} d}$		$f'_{ctm} = 0.30 f_{ck}^{2/3} k_b = \left(\frac{2 - w_f/b}{1 - w_f/400}\right)^{0.5}; l_e = \left(\frac{E_{FRCM} t_f}{2f_{ctm}}\right)^{0.5}; k_e = 0.5$
Experimental value of effective strain: $\varepsilon_{eff}^{exp} = \frac{V_{FRCM}^{exp}}{k_e E_{FRCM} \rho_f b_w d}$ Model 6 [37] $V_{FRCM} = F_z (V_m + V_f);$ $F_z = \frac{Nw_f}{a} V_m = 2(0.17 \sqrt{f_{cm}} t_m d); V_f = 2nA_f f_{fv} df_{fv} = E_{FRCM} \varepsilon_{eff};$ $\varepsilon_{eff} = \varepsilon_{FRCM} \le 0.004$ Experimental value of effective strain: $\varepsilon_{eff}^{exp} = \frac{(V_{FRCM}^{exp}/F_z - V_m)}{2nA_f E_{FRCM} d}$		$b = \begin{cases} s_f, for strips \\ 0.9 dsin(\theta + \alpha)/sin\alpha, for continous; \end{cases}$
Model 6 [37] $V_{FRCM} = F_z(V_m + V_f);$ $F_z = \frac{Nw_f}{a}V_m = 2(0.17\sqrt{f_{cm}}t_m d); V_f = 2nA_f f_{fv} df_{fv} = E_{FRCM}\varepsilon_{eff};$ $\varepsilon_{eff} = \varepsilon_{FRCM} \le 0.004$ Experimental value of effective strain: $\varepsilon_{eff}^{exp} = \frac{(V_{FRCM}^{exp}/F_z - V_m)}{2nA_f E_{FRCM} d}$		Experimental value of effective strain: $\varepsilon_{eff}^{exp} = \frac{V_{FRCM}^{exp}}{k_e E_{FRCM} \rho_f b_w d}$
*** $F_{z} = \frac{Nw_{f}}{a} V_{m} = 2(0.17 \sqrt{f_{cm}} t_{m} d); V_{f} = 2nA_{f}f_{fv}df_{fv} = E_{FRCM}\varepsilon_{eff};$ $\varepsilon_{eff} = \varepsilon_{FRCM} \leq 0.004$ Experimental value of effective strain: $\varepsilon_{eff}^{exp} = \frac{(V_{FRCM}^{exp}/F_{z} - V_{m})}{2nA_{f}E_{FRCM}d}$	Model 6 [37]	$V_{FRCM} = F_z(V_m + V_f);$
$arepsilon_{eff} = arepsilon_{FRCM} \le 0.004$ Experimental value of effective strain: $arepsilon_{eff}^{exp} = rac{\left(V_{FRCM}^{exp}/F_z - V_m ight)}{2nA_f E_{FRCM} d}$	***	$F_z = rac{Nw_f}{a}V_m = 2ig(0.17\sqrt{f_{cm}}t_m dig); V_f = 2nA_f f_{fv} df_{fv} = E_{FRCM}arepsilon_{eff};$
Experimental value of effective strain: $\epsilon_{e\!f\!f}^{exp} = rac{\left(V_{FRCM}^{ex}/F_z - V_m ight)}{2nA_f E_{FRCM} d}$		$arepsilon_{eff} = arepsilon_{FRCM} \leq 0.004$
		Experimental value of effective strain: $e_{eff}^{exp} = rac{(V_{FRCM}^{exp}/F_z - V_m)}{2nA_f E_{FRCM} d}$

\*  $A_f$  is area of mesh reinforcement by unit width;  $f_{fv}$  is design tensile strength of the FRCM system.

\*\*  $k_e$  is the "effectiveness coefficient", take 0.5;  $f_{fdd}$  is debonding strength;  $f_{ck}$  is concrete characteristic cylindrical strength;  $f'_{ctm}$  is average tensile strength of concrete;  $\gamma_{fd}$  and  $\gamma_c$  are partial safety factor, which are taken as 1 in this chapter;  $k_b$  is the geometric coefficient;  $l_e$  is optimal bond length.

\*\*\*  $V_m$  and  $V_f$  are shear strength contribution from textile and mortar, respectively;  $F_z$  is the ratio of the total length of the strengthened zone to the critical shear span; N is number of FRCM strips; a is the length of shear critical span.

89~% and 15~% to 187~%, respectively. Most studies use a volume fraction of fibres between 1.5 and 2.0 % (83~% of the samples in Fig. 7 (b)). Although the number of specimens is small, it seems that there is a trend between the increase in strength as the volume fraction of fibres increases.

Fig. 7(c) shows the variation of  $V_{JAC}/V_{CON}$  with the type of jacketing configuration. The most common strengthening configuration in FRC system is side bonding (SB), which accounts for 65 % of the beams, whereas 8 % correspond to one side bonding and the rest (57 %) to two side bonding. SB (two sides) jackets have a greater potential to improve shear strength, and  $V_{JAC}/V_{CON}$  increase by up to187%, while for SB (one side) jackets, the strength increased ranges between 33 % and 124 %. For U-wrapped beams (35 % of the samples),  $V_{JAC}/V_{CON}$  ranges from 13 to 157 %.

The impact of the ratio of the width of the jacket to the width of the beam,  $b_{w,FRC}/b_w$ , on  $V_{JAC}/V_{CON}$  is presented in Fig. 7(d). The term  $b_{w,FRC}$  refers to the width of the mortar-based composite jacket, which corresponds to the total width of the two sides. 64 % of the studies used  $b_{w,FRC}/b_w$  between 0.2 and 0.6. Detachment failure is observed for  $b_{w,FRC}/b_w$  less than 0.4. Due to the limited number of data and the large dispersion of the results no solid conclusions can be drawn about the impact of  $b_{w,FRC}$  on the shear strength increase.

# 3. Shear resistance of beams retrofitted with mortar-based composites

### 3.1. Analytical models for FRCM jacketing systems

The total shear strength of FRCM strengthened RC beams ( $V_{shear}$ ) comprises shear strength contributions from concrete ( $V_C$ ), steel stirrups ( $V_s$ ) and FRCM jacket ( $V_{FRCM}$ ) [49]:

### Table 4

Results of the assessment of the analytical models 1-6 based on the selected statistical indices.

Туре	Formula	Failure mode	Number	$v_{FRCM}^{exp}/v_{FRC}^{pred}$	l M		$v_{FRCM}^{pred}/v_{FRCM}^{exp}$	<sub>M</sub> -1
				μ	SD	COV	MAE	RMSE
Fibre-properties- based	Model 1 [51]	No detachment	20	0.60	0.35	0.58	1.22	1.58
		Detachment	75	0.84	1.06	1.26	1.95	3.21
		Total	95	0.79	0.96	1.19	1.80	2.95
	Model 2 [52]	No detachment	20	1.19	0.82	0.69	0.49	0.54
		Detachment	75	3.12	2.02	0.65	0.67	0.93
		Total	95	2.71	1.98	0.73	0.64	0.87
	Model 3 [7]	No detachment	20	0.58	0.19	0.32	0.99	1.16
		Detachment	75	0.70	0.41	0.59	1.09	1.68
		Total	95	0.67	0.38	0.57	1.09	1.60
Composite-properties-based	Model 4 [53]	No detachment	14	2.12	2.80	1.32	1.00	2.01
		Detachment	45	2.61	1.30	0.50	0.54	0.58
		Total	59	2.50	2.05	0.83	0.65	1.10
	Model 5 [54]	No detachment	14	1.78	0.87	0.49	1.08	2.54
		Detachment	45	2.36	0.90	0.38	0.52	0.56
		Total	59	2.22	0.91	0.41	0.65	1.33
	Model 6 [37]	No detachment	14	1.05	2.80	2.67	1.43	3.32
		Detachment	45	1.61	0.93	0.58	0.60	0.74
		Total 59		1.47	2.05	1.39	0.79	1.74



Fig. 8. Comparison between experimental,  $v_{FRCM}^{exp}$ , and predicted,  $v_{FRCM}^{pred}$ , shear strength for: (a) Model 1; (b) Model 2; (c) Model 3.

 $V_{shear} = V_C + V_s + V_{FRCM} \le V_{Rd,max}$ 

(4)

 $V_{shear}$  shall not exceed the shear limit value ( $V_{Rd,max}),$  which corresponds

to the crushing of diagonal compression columns in the web of the member [49].

According to EC2 [49] and ACI 318[50], the shear strength



Fig. 9.  $\varepsilon_{eff}^{exp}$  versus  $\varepsilon_{eff}^{pred}$ : (a) Model 1, (b) Model 2; Normalized experimental effective strain,  $\varepsilon_{eff}^{exp}/\varepsilon_{fu}$  versus  $\rho_f E_f / f_c^{2/3}$ : (c) Model 1, (d) Model 2.

contribution from concrete  $(V_C)$  is:

$$V_{c}^{EC2} = 0.12k (100\rho_{long} f_{c}^{\prime})^{1/3} b_{w} d$$

$$\geq 0.035k^{3/2} f_{c}^{\prime 2/3} b_{w} d$$
(5)

$$V_C^{ACI} = 0.167 \sqrt{f'_c b_w d} \tag{6}$$

where  $f'_c$  is the concrete compressive strength,  $b_w$  is the width of the cross-section, d is the depth of the cross-section,  $\rho_{long}$  is the area ratio of the tensile reinforcement, and  $k = 1 + \sqrt{(200/d)} \le 2.0$  (with d in mm) is a factor that considers the size effect. According to EC2 [49], the shear strength contribution from stirrup ( $V_s$ ) can be calculated as:

$$V_s = \frac{A_w}{s} z f_{ywd} \tag{7}$$

where  $f_{ywd}$  is the design yield strength of the shear reinforcement,  $A_w$  is the shear reinforcement area, z = 0.9d is the inner lever arm, and *s* is the stirrup spacing.

The shear strength contribution of the FRCM jacket,  $V_{FRCM}$ , can be calculated using the analytical models presented in Tables 2 and 3. The models presented in Table 2 are based on the fibre properties [7,51,52], whereas the models of Table 3 are based on the FRCM composite properties [37,53,54]. The analytical models were implemented in the database presented in Table A1. For all the beams of the database, the angle between the concrete compression strut and the beam axis is perpendicular to the shear force is considered  $\theta = 45^{\circ}$ , whereas the

angle between the fibres and the beam axis is perpendicular to the shear force in all the applications is  $\alpha = 90^{0}$ . In addition, the expression for the each model's experimental value of the effective strain ( $\varepsilon_{eff}^{exp}$ ) that is calculated from the experimental shear strength appears in Tables 2 and 3, except for Model 3 which does not depend on  $\varepsilon_{eff}^{exp}$ . Due to limitations imposed by the analytical models, the strengthened beams with anchorage systems and/or flexural failure are not considered in the analysis [6,7,51,52].

The experimental and the predicted normalised shear stress of the FRCM jacketing system,  $v_{FRCM}^{exp}$  and  $v_{FRCM}^{pred}$ , are calculated from:

$$v_{FRCM}^{exp} = \frac{V_{FRCM}^{exp}}{b_w df'_c}; v_{FRCM}^{pred} = \frac{V_{FRCM}^{pred}}{b_w df'_c}$$
(8)

where  $V_{FRCM}^{exp}$  (=  $V_{JAC}$ see Table A) is the experimental shear strength provided by FRCM jackets;  $V_{FRCM}^{pred}$  is predicted the shear strength provided by FRCM jacket which is calculated by the different models.

# 3.1.1. Assessment of the analytical models for FRCM jacketing systems

The accuracy of the six models in predicting the shear strength of the composite system is assessed using the following statistical indices: the Average Value ( $\mu$ ), Standard Deviation (SD) and Coefficient of Variation (COV) of  $v_{FRCM}^{exp}/v_{FRCM}^{pred}$ , Mean Absolute Error (MAE) and Root Mean Square Error (RMSE) between  $v_{FRCM}^{exp}$  and  $v_{FRCM}^{pred}$ . The calculated  $\mu$ , SD, COV, RMSE, and MAE values for the models are presented in Table 4. COV, MAE and RMSE are calculated as follows:



Fig. 10. Comparison between experimental,  $v_{RCM}^{exp}$  and predicted,  $v_{RCM}^{pred}$ , shear strength for: (a) Model 4; (b) Model 5; (c) Model 6.

$$COV = \frac{SD}{\mu}$$
(9)

$$MAE = \frac{\sum_{i=1}^{x} \left| v_{FRCM}^{pred} / v_{FRCM}^{exp} - 1 \right|}{N}$$
(10)

$$RMSE = \sqrt{\frac{\sum_{i=1}^{x} \left( v_{FRCM}^{pred} / v_{FRCM}^{exp} - 1 \right)^{2}}{N}}$$
(11)

3.1.1.1. Models based on fibre properties. Triantafillou and Papanicolaou proposed Model 1 [51] for fully wrapped rectangular beams firstly, which was later extended to include U-wrapped beams [6]. However, Model 1 did not consider the impact of jacket detachment on shear performance. To address this, Escrig et al. [52] improved Model 2, which incorporated different expressions for  $\epsilon_{\textit{eff}}$  depending on the presence of the jacket's detachment. In addition, Tetta and Triantafillou [7] proposed Model 3, which eliminated the need for the fibre elastic modulus Ef in the formula. This modification overcame the difficulty of selecting an appropriate elastic modulus value when predicting the shear strength provided by FRCM. Fig. 8 illustrates the relationship between  $v_{FRCM}^{pred}$  and  $v_{FRCM}^{exp}$  obtained by Models 1 [51], 2 [52], and 3 [7]. As illustrated in Fig. 8(a), the shear strength contribution of the FRCM system in Model 1 is overestimated ( $\mu = 0.79$ , SD = 0.96, COV = 1.19, Table 4), regardless of whether the strengthening beam fails or not due to the detachment of the FRCM jacket, which would lead to an unsafe situation in shear design. Moreover, the MAE and RMSE of this mode are

the largest of all models, reaching 1.80 and 2.95, respectively. For Model 2, the average  $v_{FRCM}^{exp}/v_{FRCM}^{pred}$  ratio, SD, and COV are 2.71, 1.98, and 0.73, respectively (Table 4). In contrast to Model 1, Model 2 underestimates the shear contribution of FRCM jacketing for both modes of failure (Fig. 8(b)). This implies that the structure is safe, however the design is not efficient leading to waste of materials and higher cost. Considering the average value of  $v_{FRCM}^{exp}/v_{FRCM}^{pred}$  for the two modes of failure (1.19, 3.12 for detachment and non-detachment failure, respectively), in case detachment Model 2 is less accurate. The average value of  $v_{FRCM}^{exp}/v_{FRCM}^{pred}$  for Model 3 is the smallest (0.67) among the 3 models, leading to an overestimation of the Strength which is unconservative. However, the predicted values for the CFRCM strengthened beams that failed due to detachment are very close to the experimental ones (Fig. 8(c)).

Fig. 9 presents the experimental value of the fibre effective strain  $\varepsilon_{eff}^{exp}$  versus the predicted value of strain  $\varepsilon_{eff}^{pred}$ , as well as the normalized experimental value of effective strain  $\varepsilon_{eff}^{exp}/\varepsilon_{fu}$  versus  $\rho_f E_f / f_c^{2/3}$ , for Models 1 and 2. Model 3 is not included since it is not based on  $\varepsilon_{eff}$ . Regarding  $\varepsilon_{eff}^{exp}$  versus  $\varepsilon_{eff}^{pred}$ , the effective strain of most beams in Model 1 is underestimated (Fig. 9(a)), which implies that  $\varepsilon_{eff}$  should be larger than 0.5  $\varepsilon_{fu}$ . Although Model 2 used more detailed equations for  $\varepsilon_{eff}$ , the predicted values of effective strain are underestimated. Therefore, further improvement of the formulae for the effective strain prediction is required. As shown in Fig. 9(c) for Model 1,  $\varepsilon_{eff}^{exp}/\varepsilon_{fu}$  has a remarkably decreasing trend as  $\rho_f E_f / f_c^{2/3}$  increases. However, the direct relationship



**Fig. 11.**  $\varepsilon_{eff}^{exp}$  verse  $\varepsilon_{eff}^{pred}$ : (a) Model 4, (b) Model 5, (c) Model 6; Normalized experimental effective strain,  $\varepsilon_{eff}^{exp} / \varepsilon_{fu}$ , versus  $\rho_f E_{FRCM} / f_c^{2/3}$ : (d) Model 4, (e) Model 5, (f) Model 6.

between the two variables is not clear due the large dispersion of the results. The trend in Model 2 between  $\rho_f E_f / f_c^{2/3}$  and  $\varepsilon_{eff}^{exp} / \varepsilon_{fu}$  compared to that of Model 1 seems to be more consistent (Fig. 9(d)), especially in the case of detachment failure. As observed in both graphs in Fig. 9(c) and (d), for a small number of beams (6.3 % and 5.2 % in Model 1 and 2, respectively)  $\varepsilon_{eff}^{exp} / \varepsilon_{fu}$  exceeds 1, which implies that the effective strain is larger than the rupture strain which is not realistic since  $\varepsilon_{eff}^{exp}$  should be a portion of  $\varepsilon_{fu}$ . This is attributed to the fact that  $\varepsilon_{eff}^{exp}$  is not measured but it

results after the implementation of Models 1 and 2 for  $V_{FRCM}^{exp}(=V_{JAC}$ see Table A).

In summary, Model 1 [51] consistently overestimates the shear strength contribution, regardless of whether the FRCM jacket is detached or not. It has the highest Mean Absolute Error (MAE) and Root Mean Square Error (RMSE) values compared to the other two models, indicating a significant deviation from experimental results. Model 3 [7] also tends to overestimate the strength, but the difference between the predicted and tested results is less pronounced compared to Model 1. On the other hand, Model 2 [52] underestimates the shear contribution of

### Table 5

# Analytical models to predict ... VFRC

	Formula
Model 7	$V_{FRC} = \frac{2}{z} f_{cLFRC} \left(\frac{a}{z}\right)^{0.25} b_{w,FRC} d_{FRC}$
[55]*	$3^{\prime\prime}$ (d)
Model 8	$f_{\rm res}$ ( $f_{\rm res}$ ) ] <sup>1/3</sup>
[56]**	$V_{FRC} = 0.18 b_{w,FRC} d_{FRC} k \left[ 100  ho_{long} \left( 1 + 7.5 \frac{f_{FURK}}{f_{ct,FRC}} \right) f'_{c,FRC}  ight]$
Model 9	$V_{rec} = V_{rec} + V_{crec} = \frac{0.18\sqrt{f_{c,FRC}}b_{w,FRC}d_{FRC}}{(f_{vd,FRC}/\tan\alpha)b_{w,FRC}z}$
[57]***	$\mathbf{v}_{FRC} = \mathbf{v}_{c,FRC} + \mathbf{v}_{f,FRC} = \gamma_b + \gamma_b$

\*Where  $f_{ct,FRC}$  is the tensile strength of FRC jacket, taken as  $0.3 f_{c,FRC}^{2/3}$ ;  $f_{c,FRC}$  is the compressive strength of FRC jacket;  $b_{w,FRC}$  is the width of the jacket;  $d_{FRC}$  is the effective depth of the jacket;

\*\*k is the is the size effect factor, taken as  $1 + \sqrt{200/d_{FRC}} \le 2.0$ ;  $f_{Fluk}$  is the characteristic value of the final residual tensile strength of FRC obtained from the crack opening (1.5 mm), and  $f_{Fluk}/f_{ct,FRC}$  would be taken as 0.62 [58]; \*\*\*where  $V_{c,FRC}$  is shear strength contributions from concrete in FRC;  $V_{f,FRC}$  is

shear strength contributions from fibre in FRC; Where  $f_{vd,FRC} = 0.3 f_{c,FRC}^{2/3} / \gamma_c$  is the design average tensile strength perpendicular to diagonal cracks.

### Table 6

Results of the assessment of the analytical Models 7–9 based on the selected statistical indices.

Model	Number	$v_{FRC}^{exp}/v_{FR}^{pr}$	red RC	$v_{FRC}^{pred}/v_{FR}^{exp}$	$v_{\scriptscriptstyle FRC}^{pred}/v_{\scriptscriptstyle FRC}^{exp}-1$					
		μ SD C		COV	MAE	RMSE				
Model 7 [55]	39	1.11	0.84	0.76	1.20	1.86				
Model 8 [56]	39	1.63	1.11	0.68	0.63	0.82				
Model 9 [61]	39	1.13	0.85	0.75	1.10	1.61				

FRCM. However, its prediction results are inaccurate, as both the MAE and RMSE values are larger than those of Model 2. This implies that the structure designed by Model 2 [52] is considered safe, but the design is inefficient, resulting in unnecessary material waste and higher costs.

3.1.1.2. Models based on FRCM composite properties. Since many of the studies included in the database do not provide information on the elastic modulus of the FRCM composite, only 59 beams from the database are used to compare the experimental,  $v_{FRCM}^{exp}$ , with the predicted shear stress values,  $v_{FRCM}^{pred}$ , using Models 4–6 (Table 3) as shown in Fig. 10.

Model 4 is provided by ACI 549.4R-13 [53], which is only standard considering the shear strength contribution of continuous FRCM Uwrapped or fully wrapped systems. However, it is based on very few experimental tests, and the guidelines also point out that these equations need further validation [6]. As observed in Table 3, Model 4 reaches average  $\nu_{FRCM}^{exp}/\nu_{FRCM}^{pred}$  ratio (µ) of 2.50, SD of 2.05, and COV of 0.83. Fig. 10(a) demonstrates that Model 4 underestimates the predicted shear strength. This may be attributed to the low value of the effective strain of the fibre considered (limited to  $\epsilon_{e\!f\!f}^{pred}=0.004,$  see also Fig. 11(a) where  $\varepsilon_{eff}^{exp}$  is compared to  $\varepsilon_{eff}^{pred}$ ). Model 6 proposed by [37] also considers  $\varepsilon_{\it eff}^{\it pred}=$  0.004, and they think the shear strength provided by FRCM system can be calculated by summarizing the contribution of the textile and the associated mortar. Model 6 has an average  $v_{FRCM}^{exp}/v_{FRCM}^{pred}$  ratio ( $\mu$ ) of 1.48, SD of 2.05 and COV 1.39. As seen in Fig. 10(c), in most of the cases the model underestimates the shear strength of the strengthened beams. Model 5 [54] was first used in the design of the FRP system based on the experimental response of U-wrapped beams. In case of the FRCM systems, the tensile stress distribution along the shear cracks in the FRCM reinforced material is uneven and locally high due to the brittle behaviour of the mortar-based composite material. Meanwhile, tensile

stress may allow partial failure before the entire cement composite material fails. Consequently, the efficiency of FRCM jackets is lower than that of FRP jackets, and in Model 5 this is considered by introducing the "effectiveness coefficient"  $k_e$  which is taken equal to 0.5 [21,51]. Model 5 has an average  $v_{FRCM}^{exp}/v_{FRCM}^{pred}$  ratio ( $\mu$ ) of 2.22, SD of 0.91 and COV of 0.41. From Fig. 10(b), it seems that Model 5 has a similar behaviour with Models 4 and 6.

Fig. 11 depicts the experimental value of the fibre effective strain,  $\varepsilon_{eff}^{exp}$ , versus the predicted value,  $\varepsilon_{eff}^{pred}$ , as well as the normalized experimental value of effective strain  $\varepsilon_{eff}^{exp}/\varepsilon_{fu}$  versus  $\rho_f E_f/f_c^{2/3}$  for Models 4, 5, and 6. Fig. 11(d-f) suggests similar to Models 1 and 2 that,  $\varepsilon_{eff}^{exp}/\varepsilon_{fu}$  decreases with the increase of  $\rho_f E_{FRCM}/f_c^{2/3}$ .  $\varepsilon_{eff}^{exp}/\varepsilon_{fu}$  is almost always greater than 0.25 and  $\rho_f E_{FRCM}/f_c^{2/3}$  is less than 0.05 for nearly all nondetachment failed beams. The high consistency of these models verifies that  $\rho_f E_{FRCM}/f_c^{2/3}$  has an influence on  $\varepsilon_{eff}$ , which is also affected by the failure mode of the beam. The strengthened beams with  $\varepsilon_{eff}^{exp}/\varepsilon_{fu} > 1$  correspond to 8.4 %, 55.9 % and 22.0 % (5, 33 and 13 beams) in case of Models 4, 5, and 6. As discussed in section 3.1.1.1,  $\varepsilon_{eff}^{exp}$  is not measured but it is defined after implementing Models 4, 5, and 6 for  $V_{FRCM}^{exp}(=V_{JAC}$  see Table A).

When  $v_{FRCM}^{exp}$  is less than 0.5, Figs. 10 and 11 highlight that Models 4, 5, and 6, which are based on the properties of the composite material, outperform Models 1, 2, and 3, which rely on fiber properties. This is particularly evident when the detachment failure occurs. However, when considering the entire range, Models 4, 5, and 6 do not exhibit a significant advantage over Models 1, 2, and 3 in terms of MAE and RMSE. Consequently, the existing models are unable to provide accurate predictions for the shear strength contribution of FRCM.

# 3.2. Analytical models for FRC jacketing systems

The total shear strength of fibre-reinforced-cement system strengthened RC beams ( $V_{shear}$ ) comprises shear strength contributions from concrete ( $V_C$ ), steel stirrups ( $V_S$ ) and FRC jacket ( $V_{FRC}$ ):

$$V_{shear} = V_C + V_s + V_{FRC} \tag{12}$$

 $V_{FRC}$  is calculated according to ACI [57], *fib* Model Code [58] and the Japan Society of Civil Engineers [59] design codes that are presented in Table 5. The same models were adopted by Yin et al. [56]. In case of Models 7 and 8,  $V_C$  is defined by Eqs. (5) and (6), respectively, whereas  $V_s$  is defined according to Eq. (7). For Model 8,  $V_c$  is given by [60]:

$$V_c = \beta_d \beta_p \beta_n f_{vcd} b_w d / \gamma_b \tag{13}$$

where  $f_{vd,FRC} = 0.3 f_{c,FRC}^{2/3} / \gamma_c$  is the design average tensile strength perpendicular to diagonal cracks;  $f_{vcd} = 0.2 \sqrt{f_c}$ ;  $\beta_d = \sqrt[4]{\frac{1000}{d}} \le 1.5$ ;  $\beta_p = \sqrt[3]{100\rho_{long}} \le 1.5$ ;  $\beta_n = 1$  for the member without axial compressive force.

The experimental and the predicted normalised shear stress of the FRC jacketing system,  $v_{FRC}^{exp}$  and  $v_{FRC}^{pred}$ , are calculated from:

$$v_{FRC}^{exp} = \frac{V_{FRC}^{exp}}{b_w df_c'}; v_{FRC}^{pred} = \frac{V_{FRC}^{pred}}{b_w df_c'}$$
(13)

where  $V_{FRC}^{exp}$  (=  $V_{JAC}$  see Table A) is the experimental shear strength provided by FRC jackets;  $V_{FRC}^{pred}$  is predicted the shear strength provided by FRCM jacket which is calculated by Models 7–9.

In the case of the ECC-R jacketed beams (13 specimens), Models 7–9 (Table 5) cannot be used to assess this system [59,60]. Additionally, due to missing information the beams of studies [15,29,36] were not used. In total 39 beams were used to calculate  $\mu$ , SD, COV of  $\gamma_{FRC}^{exp}/\gamma_{FRC}^{pred}$  as well as



Fig. 12. Comparison between experimental,  $v_{FRC}^{exp}$  and predicted,  $v_{FRC}^{pred}$ , shear strength for: (a) Model 7; (b) Model 8; (c) Model 9.

MAE, RMSE of  $v_{FRC}^{pred} - v_{FRC}^{exp}$  as presented in Table 6. Fig. 12 illustrates the relationship between  $v_{FRC}^{pred}$  and  $v_{FRC}^{exp}$  for Models 7–9.

Each of Models 7 [55], 8 [56] and 9 [57] rely on a different parameter to assess the shear strength contributed by the FRC system. Specifically, Model 7 considers the influence of the shear span ratio, Model 8 introduces the characteristic value of the final residual tensile strength of the FRC obtained by considering a crack opening equal to 1.5 mm, and Model 9 considers that the shear strength of the FRC comprises the shear strength of concrete and the shear strength of the fibres. Even though  $\mu$  is larger than 1 in all models, still there is a certain number of beams where  $v_{FRC}^{exp} < v_{FRC}^{pred}$  (Model 7: 20 beams, Model 8: 16 beams, Model 9: 18, Fig. 12). Models 7 and 9 seem to be equivalent. However, the dispersion is high in all models, leaving much room for the development of more reliable formulas for the various FRC strengthening systems.

# 4. Conclusions

This paper presents a review on the shear strengthening of existing RC beams with mortar-based composites. Experimental data from 36 studies were collected and an experimental database that comprises 218 RC beams was compiled. 164 beams were retrofitted using FRCM systems and 54 beams using alternative mortar-based composites. The impact of the design parameters of the beams and the mortar-based composite systems on the shear strength increase was thoroughly presented and discussed. The various failure modes of the strengthened beams were classified. Furthermore, existing design models proposed to predict the contribution of the mortar-based composites to the shear

strength of RC beams were assessed using the database. The main conclusions drawn are the following:

- Experimental evidence has demonstrated that the strengthening effect of the externally applied mortar-based composites is higher when the concrete compressive strength  $f_c' < 30 MPa$  and it reduces as the internal shear reinforcement ( $\rho_w$ ) increases. It seems that the presence of the externally bonded system limits the strain of the internal shear links preventing them from reaching their yielding strength.
- Mortar-based composites is an effective system in increasing the shear capacity of deficient RC beams. When FRCM jacketing is applied, shear strength of RC beams increased from 4 % to 196 % (61 % on average), whereas in case of FRC systems from 4 % to 190 % (by 80 % on average).
- Carbon textiles are the most popular among the textiles used in FRCM (CFRCM) systems (>50 % of the beams were jacketed with carbon textiles) reaching a shear strength increase up to 196 %. For similar axial rigidity values, PFRCM systems are less effective. The average  $V_{JAC}/V_{CON}$  for the B-, C- G-, PFRCM and SRG jackets is 110 %, 86 %, 69 %, 25 %, and 62 %, respectively. SRG, C- and BFRCM exhibit similar shear strength enhancement capacity.
- U-shaped jacketing is the most popular configuration (74 % of the beams) with the failure mode observed being detachment of the jacket. In general, the alternative anchorage systems discussed herein effectively prevented detachment of the FRCM jacketing system, however near surface mounted (NSM) anchors seem to be less effective. In case of side bonded beams, the anchorage systems

Table A1Database of mortar-based composite systems.

15

Ref.	Name	Beam de	etails						Mortar-based system details													Test Results		
		Shape	$b_w$	d	a/d	f'c	$\rho_{long}$	$\rho_w$	SC	TYPE	Anchors	t <sub>cf</sub>	εfu	$E_f$	n	$\rho_f^*$	t <sub>cm</sub>	f'cm	Efrcm	$\rho_{cm}$	FM	VJAC	V <sub>JAC</sub> /V <sub>CON</sub>	
			mm	mm		MPa	%	%						GPa	-		mm	MPa	GPa			kN		
[11]	BS1-L	R	180	334	3.1	34	2.6	0.00	U	S	_	0.084	0.0150	190	2	0.0019	12	50	NR	0.133	SH	73.1	0.87	
	BS1-H	R	180	334	3.1	34	2.6	0.00	U	S	-	0.169	0.0150	190	2	0.0038	12	50	NR	0.133	SH	103.7	1.23	
	BS-L	R	180	334	2.6	34	2.6	0.00	U	S	-	0.084	0.0150	190	2	0.0019	12	50	NR	0.133	SH	125.5	1.12	
	BS-H	R	180	334	2.6	34	2.6	0.00	U	S	-	0.169	0.0150	190	2	0.0038	12	50	NR	0.133	SH	148.8	1.33	
	BS3-L	R	180	334	2.1	34	2.6	0.00	U	S	_	0.084	0.0150	190	2	0.0019	12	50	NR	0.133	SH	122.9	0.66	
	BS3-H	R	180	334	2.1	34	2.6	0.00	U	S	_	0.169	0.0150	190	2	0.0038	12	50	NR	0.133	SH	139.7	0.75	
	BS4-L	R	180	334	1.6	34	2.6	0.00	U	S	_	0.084	0.0150	190	2	0.0019	12	50	NR	0.133	SH	59.0	0.20	
	BS4-H	R	180	334	1.6	34	2.6	0.00	U	S	_	0.169	0.0150	190	2	0.0038	12	50	NR	0.133	SH	91.3	0.32	
[18]	BGS	R	200	423	2.6	28.3	4.75	0.12	SB(T)	E-N-M	_	_	_	_	_	_	20	36.7	_	_	SH	13.50	0.04	
[24]	S/d1 551	R	150	280	1.5	30.0	3 50	0.12	SB(T)	E DE						0.02	10	128			SH	27.10	0.01	
[27]	S/d1.551	D	150	200	1.5	30.0	3.50	0.19	SB(T)	E DE	_	_	_	_	_	0.02	10	120	_	_	SH	51.20	0.10	
	5/U1.552	л р	150	200	1.5	20.0	3.50	0.19	SD(I)	E-PE	-	-	-	-	-	0.02	10	120	-	-	51	22.20	0.18	
	5/02.551	R	150	280	2.5	30.0	3.50	0.19	SD(1)	E-PE	-	-	-	-	-	0.02	10	128	-	-	511	22.20	0.13	
5051	5/02.552	R	150	280	2.5	30.0	3.50	0.19	SB(1)	E-PE	-	-	-	-	-	0.02	10	128	-	-	SH	39.95	0.24	
[25]	a-N-E-Cast	R	150	265	2.3	26.3	2.37	0.00	SB(T)	E-PE	-	-	-	-	-	0.02	20	25	-	-	SH	16.81	0.77	
	b-B-E-Cast	R	150	265	2.3	26.3	2.37	0.00	SB(T)	E-PE-R	-	-	-	-	-	0.02	20	25	-	-	SH	19.13	0.88	
	c-N-E-Cast	R	150	265	3.0	26.3	2.37	0.00	SB(T)	E-PE	-	-	-	-	-	0.02	20	25	-	-	SH	11.29	0.51	
[26]	R 0.44-NS-F0	R	150	156	4.5	30.0	0.97	0.00	U	E-N	-	-	-	-	-	0.0	50	-	-	-	SH	4.00	0.15	
	R 0.44-NS-F0.5	R	150	156	4.5	30.0	0.97	0.00	U	E-N	-	-	-	-	-	0.005	50	-	-	-	SH	5.00	0.19	
	R 0.44-NS-F1.0	R	150	156	4.5	30.0	0.97	0.00	U	E-N	-	-	-	-	-	0.01	50	-	-	-	SH	11.50	0.44	
	R 0.44-NS-F1.5	R	150	156	4.5	30.0	0.97	0.00	U	E-N	-	-	-	-	-	0.015	50	-	-	-	SH	31.50	1.21	
[4]	AUH1	R	200	270	2.2	28	0.4	0.00	U	S	-	0.254	0.0150	190	1	0.0025	7	55	25	0.070	F	13.1	0.28	
	AUML1	R	200	270	2.2	28	0.4	0.00	U	S	YES	0.084	0.0150	190	1	0.0008	7	55	25	0.070	F	16.3	0.34	
	AFL1	R	200	270	2.2	28	0.4	0.00	F	S	_	0.084	0.0150	190	1	0.0008	7	55	25	0.070	F	18.1	0.38	
	AFH1	R	200	270	2.2	28	0.4	0.00	F	S	_	0.254	0.0150	190	1	0.0025	7	55	25	0.070	F	13.6	0.29	
	BUL1	R	200	270	2.2	23	1.5	0.00	U	S	_	0.084	0.0150	190	1	0.0008	7	55	25	0.070	SH	71.9	1.05	
	BUL2	R	200	270	2.2	23	1.5	0.00	U	s	_	0.084	0.0150	190	2	0.0017	10	55	25	0 1 0 0	SH	68.3	1.00	
	BUMI 1	R	200	270	2.2	23	1.5	0.00	U	S	VES	0.004	0.0150	100	1	0.0017	7	55	25	0.100	SH	77.7	1.00	
	BEI 1	D	200	270	2.2	23	1.5	0.00	E	s	115	0.004	0.0150	100	1	0.0000	7	55	25	0.070	E	77.5	1.14	
	DFLI	л р	200	270	2.2	23	1.5	0.00	г Г	5	-	0.004	0.0150	190	1	0.0008	10	55	25	0.070	г	100.1	1.13	
51.03	DFTI	ĸ	200	2/0	2.2	23	1.5	0.00	F T	5	-	0.084	0.0150	190	2	0.0017	10	55	25	0.100	F	109.1	1.60	
[10]	B_P1	T	150	335	2.4	39	3.1	0.27	U	PBO	YES	0.046	0.0215	270	1	0.0003	8	30	NR	0.060	SH	17.9	0.09	
	B_P2	Т	150	335	2.4	39	3.1	0.27	U	РВО	YES	0.046	0.0215	270	1	0.0003	8	30	NR	0.060	SH	44.7	0.23	
	B_P3	Т	150	335	2.4	39	3.1	0.27	U	РВО	YES	0.046	0.0215	270	1	0.0003	8	30	NR	0.060	SH	33.7	0.17	
	B_WS1	Т	150	335	2.4	39	3.1	0.27	U	PBO	YES	0.046	0.0215	270	1	0.0003	8	30	NR	0.060	SH	38.1	0.19	
	B_WS2	Т	150	335	2.4	39	3.1	0.27	U	PBO	YES	0.046	0.0215	270	1	0.0003	8	30	NR	0.060	SH	41.5	0.21	
	B_WS3	Т	150	335	2.4	39	3.1	0.27	U	PBO	YES	0.046	0.0215	270	1	0.0003	8	30	NR	0.060	SH	37.8	0.19	
	B_W1	Т	150	335	2.4	39	3.1	0.27	U	PBO	YES	0.046	0.0215	270	1	0.0003	8	30	NR	0.060	SH	54.5	0.27	
	B_W2	Т	150	335	2.4	39	3.1	0.27	U	PBO	YES	0.046	0.0215	270	1	0.0003	8	30	NR	0.060	SH	39.1	0.20	
	B_W3	Т	150	335	2.4	39	3.1	0.27	U	PBO	YES	0.046	0.0215	270	1	0.0003	8	30	NR	0.060	SH	30.7	0.15	
[12]	B1-U-L	Т	180	335	2.8	34	4.1	0.00	U	S	_	0.084	0.0150	190	2	0.0019	12	50	20	0.133	SH	86.4	0.71	
	B1-U-H	Т	180	335	2.8	34	4.1	0.00	U	S	_	0.169	0.0150	190	2	0.0038	12	50	20	0.133	SH	79.2	0.65	
	B1-S-L	Т	180	335	2.8	34	4.1	0.00	SB	S	_	0.084	0.0150	190	2	0.0019	12	50	20	0.133	SH	60.8	0.50	
	B1-S-H	Т	180	335	2.8	34	4.1	0.00	SB	S	_	0.169	0.0150	190	2	0.0038	12	50	20	0.133	SH	51.2	0.42	
	B2-U-L	т	180	335	2.8	34	4 1	0.10	U	s	_	0.084	0.0150	190	2	0.0019	12	50	20	0.133	SH	60.8	0.36	
	B2-U-L	т	180	335	2.0	34	4 1	0.10	U	s	_	0.004	0.0150	100	2	0.0019	12	50	20	0.133	SU	42 5	0.26	
	D2-U-11 D2 II I	т	100	333 225	2.0	24	4.1	0.10	U	s	-	0.109	0.0150	100	2	0.0030	12	50	20	0.133	SH CU	42.0	0.20	
	DJ-U-L	1	180	335	2.8	34	4.1	0.21	U	5	-	0.084	0.0150	190	2	0.0019	12	50	20	0.133	SH	43.9	0.22	
	в3-U-Н	Т	180	335	2.8	34	4.1	0.21	U	S	-	0.169	0.0150	190	2	0.0038	12	50	20	0.133	SH	19.7	0.10	
[14]	0F-8D12	R	150	250	2.8	32.4	2.62	0.11	SB(T)	E-S	YES	-	-	-	-	0.0	10	56.8	-	-	SH	48.80	0.90	
	1F-8D12	R	150	250	2.8	36.7	2.62	0.11	SB(T)	E-S	YES	-	-	-	-	1.0	10	69.7	-	-	SH	45.90	0.85	
	1.5F-8D12	R	150	250	2.8	32.4	2.62	0.11	SB(T)	E-S	YES	-	-	-	-	1.5	10	60.8	-	-	SH	57.15	1.05	
	1.5F-4D12	R	150	250	2.8	36.7	2.62	0.11	SB(T)	E-S	YES	-	-	-	-	1.5	10	60.8	-	-	SH	55.30	1.02	
	1.5F-6D12	R	150	250	2.8	36.7	2.62	0.11	SB(T)	E-S	YES	-	-	-	-	1.5	10	60.8	-	-	SH	47.20	0.87	

(continued on next page)

Ref.	Name	Beam details							Mortar-based system details												Test Results			
		Shape	b <sub>w</sub>	d	a/d	f'c	$\rho_{long}$	$\rho_w$	SC	TYPE	Anchors	t <sub>cf</sub>	efu	$E_{f}$	n	$\rho_f^*$	t <sub>cm</sub>	f'cm	Efrem	$\rho_{cm}$	FM	VIAC	VIAC /VCON	
						MPa	06	0%				-5	-)	GPa	-	<u> </u>		MDo	GPa			LN		
			111111	111111		MPa	90	70						GPa			111111	MPa	GPa			KIN		
	1.5F-6D10	R	150	250	2.8	36.7	2.62	0.11	SB(T)	E-S	YES	-	-	-	-	1.5	10	60.8	-	-	SH	46.90	0.87	
[1][]	1.5F-8D10	R	150	250	2.8	36.7	2.62	0.11	SB(T)	E-S	YES	-	-	-	-	1.5	10	60.8	-	-	SH	54.70	1.01	
[15]	EJ-UK	R	150	124	1.0	28.0	1.22	0.89	U CD(T)	E-5	-	-	-	-	-	2.0	50	110	-	-	511	-3.03	-	
[16]	EJ-0/K	r D	150	257	2.0	20.0	2.10	0.09	SB(T)	E-5 E DVA	-	-	-	-	-	2.0	20	110	-	-	SH SH	-1.20	-	
[10]	SA 20 3	D	150	257	2.0	11.0	1.04	0.00	SB(T)	E DVA	-	-	-	-	_	1.5	20	44.0	-	-	SII SU	16.00	0.39	
	SR-20-2	R	150	252.5	2.0	44.8	2.50	0.00	SB(T)	E-PVA E-DVA	_	_	_	_	_	1.5	20	44.8	_	_	SH	52 50	0.53	
	SB-20-2 SB-20-3	R	150	252.5	3.0	44.8	2.59	0.00	SB(T)	E-PVA	_	_	_	_	_	1.5	20	44.8	_	_	SH	12 50	0.20	
	SA-40-2	R	150	257	2.0	44.8	1.04	0.00	SB(T)	E-PVA	_	_	_	_	_	1.5	40	44.8	_	_	SH	27.00	0.40	
	SA-40-3	R	150	257	3.0	44.8	1.04	0.00	SB(T)	E-PVA	_	_	_	_	_	1.5	40	44.8	_	_	SH	17.50	0.41	
	SB-40-2	R	150	252.5	2.0	44.8	2.59	0.00	SB(T)	E-PVA	_	_	_	_	_	1.5	40	44.8	_	_	SH	82.50	0.89	
	SB-40-3	R	150	252.5	3.0	44.8	2.59	0.00	SB(T)	E-PVA	_	_	_	_	_	1.5	40	44.8	_	_	SH	13.00	0.21	
[20]	E-C-A	R	150	280	2	25.8	1.4	0.18	SB	С	_	0.047	0.018	240	3	0.0012	20	20	NR	0.175	SH	36.9	0.40	
	E-G-A	R	150	280	2	25.8	1.4	0.18	SB	G	_	0.047	0.0325	80	3	0.0012	20	40	NR	0.175	SH	20.0	0.22	
	E-P-A	R	150	280	2	25.8	1.4	0.18	SB	PBO	_	0.046	0.0215	270	3	0.0012	20	30	NR	0.175	SH	23.4	0.25	
	E-C-UA	R	150	280	2	25.8	1.4	0.18	SB	С	-	0.047	0.018	240	3	0.0012	20	20	NR	0.175	SH	35.5	0.36	
	E-G-UA	R	150	280	2	25.8	1.4	0.18	SB	G	-	0.047	0.0325	80	3	0.0012	20	40	NR	0.175	SH	16.3	0.17	
	E-P-UA	R	150	280	2	25.8	1.4	0.18	SB	PBO	-	0.046	0.0215	270	3	0.0012	20	30	NR	0.175	SH	26.3	0.27	
[27]	Bi10-GM1-A	R	150	270	2.6	34	2.8	0.13	U	С	YES	0.110	0.0180	242	1	0.0015	6	43.4	NR	0.080	SH	57.5	0.68	
	Bi10-GM1	R	150	270	2.6	34	2.8	0.13	U	С	-	0.110	0.0180	242	1	0.0015	6	43.4	NR	0.080	SH	40.0	0.47	
	Bi7-GM1-A	R	150	270	2.6	34	2.8	0.13	U	С	YES	0.110	0.0180	242	1	0.0015	6	43.4	NR	0.080	SH	72.5	0.85	
	Bi7-GM1	R	150	270	2.6	34	2.8	0.13	U	С	-	0.110	0.0180	242	1	0.0015	6	43.4	NR	0.080	SH	60.0	0.71	
	Bi10-GM2-A	R	150	270	2.6	34	2.8	0.13	U	С	YES	0.110	0.0180	242	2	0.0029	9	43.4	NR	0.120	SH	107.5	1.26	
	Bi10-GM2	R	150	270	2.6	34	2.8	0.13	U	С	-	0.110	0.0180	242	2	0.0029	9	43.4	NR	0.120	SH	90.0	1.06	
	Bi10-GM3	R	150	270	2.6	34	2.8	0.13	U	С	-	0.110	0.0180	242	3	0.0044	12	43.4	NR	0.160	SH	30.0	0.35	
50.03	Uni10-GM1	R	150	270	2.6	34	2.8	0.13	U	С	-	0.110	0.0180	242	1	0.0015	6	43.4	NR	0.080	SH	95.0	1.12	
[28]	S-20-2	R	150	257	2.0	26.6	0.82	0.00	SB(T)	E-N	-	-	-	-	-	-	20	56	-	-	SH	57.00	0.84	
	S-20-3	R	150	257	3.0	26.6	0.82	0.00	SB(T)	E-N	-	-	-	-	-	-	20	56	-	-	SH	16.00	0.38	
	S-40-2	R	150	257	2.0	26.6	0.68	0.00	SB(T)	E-N	-	-	-	-	-	-	40	56	-	-	SH	27.00	0.40	
[20]	5-40-3 ST 15 D	K D	150	257	3.0	20.0	0.68	0.00	SB(1)	E-IN E-C	- VEC	-	-	-	-	-	40	50 12E 4	-	-	SH	1/.50	0.41	
[29]	51-15-R ST 25 D	К D	150	250	2.1	20.0	1.30	0.13	SD SP(T)	E-5 E 6	I ES	-	-	-	-	2.0	20	135.4	-	-	F C	108.00 69 E	1.88	
[20]	B D100 B7	т	150	230	2.1	30.0	2.1	0.13	3D(1)	DBO	163	-	-	- 270	1	2.0	30 9	20	- ND	-	S SU	11.0	0.05	
[30]	B P100_BZ	т	150	335	2.4	36	3.1	0.27	U	PBO	- VFS	0.040	0.0215	270	1	0.0003	8	30	NR	0.053	SH	27.3	0.03	
	B P100_1	т	150	335	2.4	36	3.1	0.27	U	PBO	VES	0.040	0.0215	270	1	0.0003	8	30	NR	0.053	SH	27.3	0.12	
	B P100 3	Ť	150	335	2.4	36	3.1	0.27	U	PBO	YES	0.046	0.0215	270	1	0.0003	8	30	NR	0.053	SH	22.8	0.10	
[31]	B1	T	150	335	2.4	39	3.1	0.27	U	PBO	YES	0.046	0.0215	270	1	0.0003	8	30	NR	0.048	SH	36.9	0.16	
[9]	S0-CM	R	250	317	3.2	61	3.7	0.00	SB	C	-	0.128	0.0160	230	1	NR	8	58	21	0.064	SH	125.6	0.87	
	S50-CM	R	250	317	3.2	61	3.7	0.11	SB	C	_	0.128	0.0160	230	1	NR	8	58	21	0.064	SH	79.2	0.30	
	S150-CM	R	250	317	3.2	61	3.7	0.19	SB	С	_	0.128	0.0160	230	1	NR	8	58	21	0.064	SH	78.5	0.26	
[32]	CL1	R	102	177	2.6	20	2.2	0.00	U	С	_	0.062	0.0079	225	1	0.0012	4	38.7	NR	0.078	SH	28.9	0.97	
	CL1_strips	R	102	177	2.6	17	2.2	0.00	U	С	_	0.062	0.0079	225	2	0.0009	6	38.7	NR	0.090	SH	33.7	1.13	
	CH1	R	102	177	2.6	20	2.2	0.00	U	С	_	0.095	0.0079	225	1	0.0019	4	31.1	NR	0.078	SH	15.1	0.51	
	CH1_CL1	R	102	177	2.6	17	2.2	0.00	U	С	-	0.079	0.0079	225	2	0.0031	6	38.7	NR	0.118	SH	37.6	1.27	
	CH2	R	102	177	2.6	20	2.2	0.00	U	С	-	0.095	0.0079	225	2	0.0037	6	31.1	NR	0.118	SH	39.2	1.32	
	CL3	R	102	177	2.6	18	2.2	0.00	U	С	-	0.062	0.0079	225	3	0.0036	8	35.5	NR	0.157	SH	37.9	1.28	
	CH2_CH1	R	102	177	2.6	17	2.2	0.00	U	С	-	0.079	0.0079	225	3	0.0049	8	38.7	NR	0.157	SH	44.4	1.49	
	CH3	R	102	177	2.6	19	2.2	0.00	U	С	-	0.095	0.0079	225	3	0.0056	8	26.9	NR	0.157	SH	45.4	1.53	
	CH3_CL1	R	102	177	2.6	17	2.2	0.00	U	С	-	0.079	0.0079	225	4	0.0068	10	38.7	NR	0.196	SH	48.5	1.63	
	G1	R	102	177	2.6	17	2.2	0.00	U	G	-	0.044	0.0166	74	1	0.0009	4	35.5	NR	0.078	SH	12.2	0.41	
	G3	R	102	177	2.6	17	2.2	0.00	U	G	-	0.044	0.0166	74	3	0.0026	8	35.5	NR	0.157	SH	37.0	1.25	
	G7	R	102	177	2.6	17	2.2	0.00	U	G	-	0.044	0.0166	74	7	0.0060	16	38.7	NR	0.314	SH	53.0	1.78	

Ref.	Name	Beam details							Mortar-based system details												Test Results		
		Shape	$b_w$	d	a/d	f'c	$\rho_{long}$	$\rho_w$	SC	TYPE	Anchors	t <sub>cf</sub>	єfu	$E_{f}$	n	$\rho_f^*$	t <sub>cm</sub>	f'cm	Efrcm	$\rho_{cm}$	FM	VIAC	V <sub>JAC</sub> /V <sub>CON</sub>
						MPa	06	0%					-)	GPa	-	<u> </u>		MDo	<u>CPa</u>			kN	
			100			IVIF a	70	70						Gra				IVIF a	Gra			KIN	
	B1 B2	R	102	177	2.6	20	2.2	0.00	U	В	-	0.037	0.0183	89 80	1	0.0007	4	33.3	NR	0.078	SH	14.4 36.1	0.48
	B7	R	102	177	2.0	20	2.2	0.00	U	B	_	0.037	0.0183	89	7	0.0022	16	35.5	NR	0.137	SH	47.9	1.22
	CL1 1 6	R	102	177	1.6	19	2.2	0.00	U	C	_	0.057	0.0100	225	1	0.00012	4	33.3	NR	0.014	SH	26.1	0.40
	CL3.1.6	R	102	177	1.0	19	2.2	0.00	U	C	_	0.062	0.0079	225	3	0.0012	8	33.3	NR	0.070	SH	40.2	0.61
	CL1 3.6	R	102	177	3.6	19	2.2	0.00	U	C	_	0.062	0.0079	225	1	0.0012	4	33.3	NR	0.107	SH	29.4	1 15
	CL3 3.6	R	102	177	3.6	19	2.2	0.00	U	C	_	0.062	0.0079	225	3	0.0036	8	33.3	NR	0.157	SH	39.6	1.55
[33]	C0	R	150	280	2.0	30	1.4	0.00	U	C	_	0.047	0.0180	240	2	0.0013	9	20	NR	0.120	SH	56.8	0.77
[00]	PO	R	150	280	2.0	30	1.4	0.00	U	PBO	_	0.045	0.0215	270	2	0.0012	12	40	NR	0.160	SH	46.2	0.63
	GO	R	150	280	2.0	30	1.4	0.00	U	G	_	0.047	0.0325	80	2	0.0013	15	22	NR	0.200	SH	49.7	0.67
	C1	R	150	280	2.0	30	1.4	0.18	U	C	_	0.047	0.0180	240	2	0.0013	9	20	NR	0.120	SH	46.9	0.47
	P1	R	150	280	2.0	30	1.4	0.18	U	PBO	_	0.045	0.0215	270	2	0.0012	12	40	NR	0.160	SH	29.1	0.29
	G1	R	150	280	2.0	30	1.4	0.18	U	G	_	0.047	0.0325	80	2	0.0013	15	22	NR	0.200	SH	38.3	0.38
[34]	C_Full	R	150	296	1.8	30	1.3	0.00	U	С	_	0.047	0.0180	240	2	0.0013	13	20	NR	0.173	F	75.3	1.02
	CIntermittent	R	150	296	1.8	30	1.3	0.00	U	С	_	0.047	0.0180	240	2	0.0008	13	20	NR	0.114	SH	52.6	0.71
	P_Full	R	150	296	1.8	30	1.3	0.00	U	PBO	_	0.045	0.0215	270	2	0.0012	13	30	NR	0.173	SH	33.4	0.45
	P_Intermittent	R	150	296	1.8	30	1.3	0.00	U	PBO	-	0.045	0.0215	270	2	0.0008	13	30	NR	0.114	SH	24.2	0.33
	G_Full	R	150	296	1.8	30	1.3	0.00	U	G	-	0.047	0.0325	80	2	0.0013	13	40	NR	0.173	SH	45.5	0.62
	G_Intermittent	R	150	296	1.8	30	1.3	0.00	U	G	-	0.047	0.0325	80	2	0.0008	13	40	NR	0.114	SH	23.4	0.32
[35]	S0-CM	R	250	311	1.6	61	3.8	0.00	SB	С	-	0.128	0.0160	234.5	1	NR	8	58	NR	0.064	SH	136.5	0.23
	S50-CM	R	250	311	1.6	61	3.8	0.09	SB	С	_	0.128	0.0160	234.5	1	NR	8	58	NR	0.064	SH	106.3	0.16
[36]	ST-1S	R	150	250	2.1	30.0	1.36	0.13	SB	E-S	_	-	-	-	-	2.0	30	135.4	-	-	SH	19.00	0.33
	ST-2S	R	150	250	2.1	30.0	1.36	0.13	SB(T)	E-S	-	-	-	-	-	2.0	60	135.4	-	-	F	83.00	1.44
[13]	В	R	150	267	2.2	35.0	2.35	0.33	SB	E-N	-	-	-	-	-	-	20	72.60	-	-	SH	43.60	1.00
	С	R	150	267	2.2	35.0	2.35	0.33	SB	E-N	-	-	-	-	-	-	20	30.20	-	-	SH	45.34	1.04
	D	R	150	267	2.2	35.0	2.35	0.33	SB	E-N-R	-	-	-	-	-	-	20	30.20	-	-	SH	54.06	1.24
[23]	S1-FRCM-F3-UA	R	150	230	3.3	23	6.1	0.23	U	С	YES	0.047	0.0180	240	1	0.0006	8	45.2	NR	0.107	SH	29.9	0.26
	S1-FRCM-F4-UN	R	150	230	3.3	21	6.1	0.23	U	S	-	0.047	0.0160	190	1	0.0006	8	45.2	NR	0.107	SH	34.5	0.30
	S1-FRCM-F4-UA	R	150	230	3.3	21	6.1	0.23	U	S	YES	0.047	0.0160	190	1	0.0006	8	45.2	NR	0.107	SH	34.9	0.30
	S-FRCM-F3-UN	R	150	230	3.3	25	6.1	0.33	U	С	-	0.270	0.0180	240	1	0.0036	8	45.2	NR	0.107	SH	24.3	0.19
	S-FRCM-F4-UN	R	150	230	3.3	21	6.1	0.33	U	S	-	0.270	0.0160	190	1	0.0036	8	45.2	NR	0.107	SH	17.5	0.13
50.00	S-FRCM-F4-UA	R	150	230	3.3	21	6.1	0.33	U	S	YES	0.270	0.0160	190	1	0.0036	8	45.2	NR	0.107	SH	31.3	0.24
[37]	C-F-90	R	150	280	2.0	30	1.4	0.00	SB	C	-	0.047	0.0180	240	2	0.0013	12	20	NR	0.160	SH	75.1	1.02
	C-I-90	R	150	280	2.0	30	1.4	0.00	SB	C	-	0.047	0.0180	240	2	0.0008	12	20	NR	0.105	SH	52.3	0.71
	C-I-45	К D	150	280	2.0	30	1.4	0.00	SB	C	-	0.047	0.0180	240	2	0.0007	12	20	NR	0.083	SH	33./	0.46
	C-I-90-A	К D	150	280	2.0	30	1.4	0.00	SD	C	I ES	0.047	0.0180	240	2	0.0008	12	20	NR	0.105	5H 6H	26.2	0.73
	C-I-45-A D E 00	К D	150	280	2.0	30 20	1.4	0.00	SD		125	0.047	0.0180	240	2	0.0007	12	20	NR	0.085	5H 6H	30.3 22.6	0.49
	P_I_90	R	150	280	2.0	30	1.4	0.00	SB	PBO	_	0.045	0.0215	270	∠ 2	0.0012	12	30	NR	0.100	SH	23.0	0.32
	P_I_45	R	150	280	2.0	30	1.4	0.00	SB	PBO	_	0.045	0.0215	270	2	0.0008	12	30	NR	0.103	SH	20.9	0.52
	P_I_90_Δ	R	150	280	2.0	30	1.4	0.00	SB	PBO	VFS	0.045	0.0215	270	2	0.0000	12	30	NR	0.005	SH	25.4	0.34
	P_I_45_A	R	150	280	2.0	30	1.4	0.00	SB	PBO	VFS	0.045	0.0215	270	2	0.0006	12	30	NR	0.103	SH	40.5	0.55
	G_F_90	R	150	280	2.0	30	1.1	0.00	SB	G	-	0.047	0.0210	80	2	0.0013	12	40	NR	0.000	SH	45.4	0.61
	G_I_90	R	150	280	2.0	30	1.1	0.00	SB	G	_	0.047	0.0325	80	2	0.0008	12	40	NR	0.105	SH	23.4	0.32
	G-I-45	R	150	280	2.0	30	1.4	0.00	SB	G	_	0.047	0.0325	80	2	0.0007	12	40	NR	0.083	SH	-7.1	-9.60
	G-I-90-A	R	150	280	2.0	30	1.4	0.00	SB	G	YES	0.047	0.0325	80	2	0.0008	12	40	NR	0.105	SH	30.5	0.41
	G-I-45-A	R	150	280	2.0	30	1.4	0.00	SB	G	YES	0.047	0.0325	80	2	0.0007	12	40	NR	0.083	SH	12.8	0.17
[38]	BA-S-1	R	203	275	2.5	45	12.0	0.61	U	PBO	_	0.050	0.0120	270	1	0.0002	6	38	NR	0.030	SH	29.5	0.18
21112	BA-S-4	R	203	275	2.5	45	12.0	0.61	U	PBO	_	0.050	0.0120	270	4	0.0010	15	38	NR	0.074	SH	29.5	0.18
	BA-C-4	R	203	275	2.5	45	12.0	0.61	U	PBO	_	0.050	0.0120	270	4	0.0020	15	38	NR	0.148	SH	51.0	0.31
	BB-S-1	R	203	275	2.5	45	12.0	0.00	U	PBO	_	0.050	0.0120	270	1	0.0002	6	38	NR	0.030	SH	-12.5	-0.11
	BB-S-4	R	203	275	2.5	45	12.0	0.00	U	PBO	_	0.050	0.0120	270	4	0.0010	15	38	NR	0.074	SH	4.0	0.04
																						(continued	on next page)

Ref.	Name	Beam de	etails						Mortar	-based system	1 details										Test	Results	
		Shape	<i>b</i>	đ	a/d	f'.	01	0	SC	TYPE	Anchors	t.c	-6-	Ec	n	0.0*	t	f'	<i>E</i>	0	FM	Viac	VIAC /VCON
		<u>onape</u>	<u> </u>		<u>u</u> / u	<u> </u>	Piong	PW				-0	ЕJU		_	PJ		<i>J cm</i>	-jrcm	PCM		• JAC	·JAC / · CON
			mm	mm		MPa	%	%						GPa			mm	MPa	GPa			kN	
	BB-C-1	R	203	275	2.5	45	12.0	0.00	U	PBO	-	0.050	0.0120	270	1	0.0005	6	38	NR	0.059	SH	23.5	0.21
[8]	CH2	Т	200	385	2.3	18	3.2	0.00	U	С	-	0.950	0.0079	225	2	0.0190	6	37.4	NR	0.060	SH	47.0	0.38
	CL3	Т	200	385	2.3	16	3.2	0.00	U	С	-	0.620	0.0079	225	3	0.0186	8	35.8	NR	0.080	SH	57.6	0.47
	CH4	Т	200	385	2.3	16	3.2	0.00	U	C	-	0.950	0.0079	225	4	0.0380	10	36.1	NR	0.100	SH	96.5	0.78
	G/	T	200	385	2.3	18	3.2	0.00	U	G	-	0.440	0.0166	74	7	0.0308	16	33.7	NR	0.160	SH	94.2	0.77
	CH2_A100	I T	200	385	2.3	17	3.2	0.00	U	C	YES	0.950	0.0079	225	2	0.0190	0	34.5	NR	0.060	SH	112.5	0.91
	CL3_AI00	T	200	383 20E	2.3	17	3.Z	0.00	U	C	IES VEC	0.020	0.0079	223	3	0.0180	8 10	37.9	NR.	0.080	5H 6H	114.0	0.93
	CH4_A30 CH4_A100	Т	200	385	2.3	17	3.2	0.00	U	C	VES	0.950	0.0079	225	4	0.0380	10	33.4	NR	0.100	SH	237.5	1.20
	G7 A100	т	200	385	2.3	17	3.2	0.00	U	G	VES	0.930	0.0075	74	7	0.0308	16	37.4	NR	0.160	SH	107.2	0.87
[17]	B-E	R	250	300	3.3	24.4	0.99	0.00	U	E-PVA	_	-	_	_	_	-	40	63.2	_	_	SH	13.50	0.10
1273	B-M-6	R	250	300	3.3	25.2	0.99	0.21	U	E-PVA-R	_	_	_	_	_	_	40	28.1	_	_	SH	21.00	0.16
	B-M-1	R	250	300	3.3	25.0	0.99	0.21	U	E-PVA-R	_	_	_	_	_	_	40	62	_	_	SH	45.90	0.35
	B-E-6	R	250	300	3.3	24.5	0.99	0.21	U	E-PVA-R	_	_	_	_	_	_	40	49.6	_	_	SH	28.00	0.21
	B-E-1	R	250	300	3.3	24.9	0.99	0.21	U	E-PVA-R	_	_	_	_	_	_	40	53.4	_	_	SH	36.90	0.28
[39]	S0- FRCM-1	R	150	250	3.0	36	5.0	0.00	SB	С	-	1.000	0.0160	230	1	0.0133	12	74	22	0.160	SH	66.5	1.10
	S0- FRCM-2	R	150	250	3.0	36	5.0	0.00	SB	С	-	1.000	0.0160	230	2	0.0267	18	74	22	0.240	SH	87.2	1.45
	S1- FRCM-1	R	150	250	3.0	36	5.0	0.25	SB	С	-	1.000	0.0160	230	1	0.0133	12	74	22	0.160	SH	68.4	0.64
	S1- FRCM-2	R	150	250	3.0	36	5.0	0.25	SB	С	-	1.000	0.0160	230	2	0.0267	18	74	22	0.240	SH	72.1	0.67
	S- FRCM-1	R	150	250	3.0	36	5.0	0.50	SB	С	-	1.000	0.0160	230	1	0.0133	12	74	22	0.160	SH	67.6	0.51
	S- FRCM-2	R	150	250	3.0	36	5.0	0.50	SB	С	-	1.000	0.0160	230	2	0.0267	18	74	22	0.240	SH	73.6	0.55
[40]	SB_MCH2_20	R	102	177	2.6	19	2.2	0.00	SB	С	-	0.095	0.0079	225	2	0.0037	6	28.2	NR	0.118	SH	21.0	0.70
	SB_MCH2_150	R	102	177	2.6	19	2.2	0.00	SB	С	-	0.095	0.0079	225	2	0.0037	6	16.2	NR	0.118	SH	11.0	0.37
	SB_MCH3_20	R	102	177	2.6	19	2.2	0.00	SB	C	-	0.095	0.0079	225	3	0.0056	8	26.9	NR	0.157	SH	33.0	1.11
	SB_MCH3_150	R	102	177	2.6	19	2.2	0.00	SB	C	-	0.095	0.0079	225	3	0.0056	8	16.2	NR	0.15/	SH	17.0	0.57
	UW_MCH2_20	К D	102	177	2.0	20	2.2	0.00	U	C	-	0.095	0.0079	220	2	0.0037	6	31.1	NR.	0.118	5H 6H	39.0	1.31
	UW_MCH2_150	R	102	177	2.0	19	2.2	0.00	U	C	_	0.095	0.0079	225	3	0.0037	8	26.9	NR	0.110	SH	20.0 45.0	1.51
	UW MCH3 150	R	102	177	2.0	19	2.2	0.00	U	C	_	0.095	0.0079	225	3	0.0056	8	16.2	NR	0.157	SH	25.0	0.84
	UW MCH3 100	R	102	177	2.6	18	2.2	0.00	U	C	_	0.095	0.0079	225	3	0.0056	8	17.3	NR	0.157	SH	45.0	1.51
	UW MCH3 250	R	102	177	2.6	18	2.2	0.00	U	C	_	0.095	0.0079	225	3	0.0056	8	17	NR	0.157	SH	29.0	0.97
	UW_MCL3_20	R	102	177	2.6	18	2.2	0.00	U	С	_	0.062	0.0079	225	3	0.0036	8	38.7	NR	0.157	SH	38.0	1.28
	UW_MCL3_150	R	102	177	2.6	18	2.2	0.00	U	С	_	0.062	0.0079	225	3	0.0036	8	16.2	NR	0.157	SH	25.0	0.84
	UW_MG7_20	R	102	177	2.6	17	2.2	0.00	U	G	-	0.044	0.0166	74	7	0.0060	16	35.5	NR	0.314	SH	53.0	1.78
	UW_MG7_150	R	102	177	2.6	18	2.2	0.00	U	G	-	0.044	0.0166	74	7	0.0060	16	16.2	NR	0.314	SH	27.0	0.91
	FW_MCH2_20	R	102	177	2.6	19	2.2	0.00	F	С	-	0.095	0.0079	225	2	0.0037	6	28.2	NR	0.118	F	58.0	1.95
	FW_MCH2_150	R	102	177	2.6	19	2.2	0.00	F	С	-	0.095	0.0079	225	2	0.0037	6	16.2	NR	0.118	SH	48.0	1.61
	CH4_20	Т	200	385	2.3	12	3.2	0.00	U	С	-	0.095	0.0079	225	4	0.0038	10	36.1	NR	0.100	SH	95.0	0.76
	CH4_150	Т	200	385	2.3	12	3.2	0.00	U	С	-	0.095	0.0079	225	4	0.0038	10	22.9	NR	0.100	SH	66.0	0.53
	CH4_A100_20	Т	200	385	2.3	11	3.2	0.00	U	С	Yes	0.095	0.0079	225	4	0.0038	10	33.4	NR	0.100	SH	236.0	1.90
5 4 3 3	CH4_A100_150	Т	200	385	2.3	12	3.2	0.00	U	С	Yes	0.095	0.0079	225	4	0.0038	10	19.3	NR	0.100	SH	119.0	0.96
[41]		T	150	320	2.5	18	1.6	0.00	U	C	-	0.048	0.0180	225	1	0.0006	4	21.8	NR	0.053	SH	10.6	0.18
	LZ	I T	150	320	2.5	19	1.0	0.00	U	C	-	0.048	0.0180	225	2	0.0013	6	21.8	NR	0.080	SH	13.4	0.24
	H1 H2	I T	150	320	2.5	20	1.0	0.00	U	C	-	0.096	0.0180	225	2	0.0013	4	21.8	NR. ND	0.055	5П СЦ	24.2	0.42
	L2A15ha	т	150	320	2.5	20	1.0	0.00	U	C	YES	0.048	0.0180	225	∠ 2	0.0020	6	21.0	NR	0.080	SH	59.7	1.04
	L2A10	Ť	150	320	2.5	11	1.6	0.00	U	C	YES	0.048	0.0180	225	2	0.0013	6	21.0	NR	0.080	SH	85.7	1.96
	H1A15	T	150	320	2.5	12	1.6	0.00	U	C	YES	0.096	0.0180	225	1	0.0013	4	21.8	NR	0.053	SH	54.7	1.25
	H2A10	Т	150	320	2.5	12	1.6	0.00	Ū	C	YES	0.096	0.0180	225	2	0.0026	6	21.8	NR	0.080	SH	51.6	1.18
	H2A10	Т	150	320	2.5	12	1.6	0.00	U	С	YES	0.096	0.0180	225	2	0.0026	6	21.8	NR	0.080	SH	52.1	0.91
[1]	SB-CT1	R	150	300	3.3	38	2.2	0.00	SB	С	_	0.128	0.0160	230	1	NR	7	58	NR	0.093	SH	16.0	0.26
	UW-CT1	R	150	300	3.3	38	2.2	0.00	U	С	-	0.128	0.0160	230	1	NR	7	58	NR	0.093	SH	14.1	0.23

Ref.	Name	Beam c	letails						Morta	tr-based syste	m details										Test R	esults	
		Shape	$b_w$	q	a/d	$f_c$	$\rho_{long}$	ρw	SC	TYPE	Anchors	$t_{cf}$	nfэ	$E_f$	u	$\rho f^*$	$t_{cm}$	$f_{cm}$	$E_{frcm}$	$\rho_{cm}$	FM	$V_{JAC}$	V <sub>JAC</sub> /V <sub>CON</sub>
			mm	шш		MPa	%	%						GPa			mm	MPa	GPa			kN	
	SB-CT2	R	150	300	3.3	38	2.2	0.00	SB	C	I	0.128	0.0160	230	1	NR	7	58	NR	0.093	HS	60.9	0.99
	UW-CT2	R	150	300	3.3	38	2.2	0.00	Ŋ	U	I	0.128	0.0160	230	1	NR	7	58	NR	0.093	HS	64.9	1.05
[42]	1	R	150	231	1.7	26.3	1.74	0.30	Ŋ	E-S	I	I	I	I	I	I	30	26.3	I	I	HS	64.65	1.11
	2	R	150	231	1.7	26.3	1.74	0.30	n	E-S	I	I	I	I	I	I	30	26.3	I	I	HS	84.40	1.45
	ŝ	R	150	231	1.7	26.3	1.74	0.00	n	E-S	I	I	I	I	I	I	30	26.3	I	I	ΗS	28.40	0.49
	7	R	150	231	1.7	26.3	1.74	0.30	n	E-S	I	I	I	I	I	I	30	85.7	I	I	ΗS	81.20	1.40
	8	R	150	231	1.7	26.3	1.74	0.30	n	E-S	I	I	I	I	I	I	30	85.7	I	I	SH	80.05	1.38
	6	R	150	231	1.7	26.3	1.74	0.00	n	E-S	I	I	I	I	I	I	30	85.7	I	I	HS	18.30	0.32
	13	R	150	231	1.7	26.3	1.74	0.30	n	E-S	I	I	I	I	I	I	30	95.3	I	I	HS	73.15	1.26
	14	R	150	231	1.7	26.3	1.74	0.30	n	E-S	I	I	I	I	I	I	30	95.3	I	I	HS	90.95	1.57
	15	R	150	231	1.7	26.3	1.74	0.00	Ŋ	E-S	I					I	30	95.3	I	I	HS	67.95	1.17
Note: 1	. 'SC' is jacket's	strengther	ning co	nfiguratio	., î., :uo	– U wra	pped, 'F'	– Fully	wrapp	ed, 'SB' – Si	de bonding	(one side	, (SB(T))	– Side b	guibno	3 (two sic	les).	te che		1	4 5 77		the Ghan Chief

Table A1 (continued)

j Type: B' - BFRCM, 'G' - CFRCM, 'BO' - PBOFRCM, 'S' - SRG, 'E-N' - FRC (unknown fibre) without mesh/grid, 'E-N-R' - FRC (unknown fibre) with mesh/grid, 'E-PC' - FRC (PE fib mesh/grid, 'E-PVA' - RC (PVA fibre) without mesh/grid, 'E-VA+R' - FRC (PVA fibre) with mesh/grid, 'E-S' - FRC (steel fibre) without mesh/grid, 'E-S' - FRC (steel fi FM' is failure mode: 'F' – flexural failure, 'SH' – shear failure.

 $f_c$  is cylinder compression strength. If the specimen uses cube compression strength, it shall be converted according to [62].

fraction of fibre in mortar in ECC. refers to the volume and it in FRCM, textile ratio of the Regarding  $\rho_b$ , it refers to the fibre reinforcement

seem not to be effective even in the case of anchors and the failure mode observed is detachment. In cases where fully wrapped jackets were applied the failure mode changed from shear to flexural and fibre rupture was the observed mode of failure.

- The increase of FRCM reinforcement ratio, ρ<sub>cm</sub>, leads to increased shear capacity for the strengthened beams, since the cross-sectional area (especially the width) of the RC beam is increased, thereby improving the shear capacity of the beam.
- In most of the FRC jacketed beams (74 %) no textiles (or grids) are used. The types of fibres used are PE, PVA, and steel up to 2 % fibre volume fraction.
- For the prediction of the shear strength contribution by the FRCM system, Triantafillou and Papanicolaou [51, Model 1], Escrig et al. [52, Model 2], and Tetta et al. [7, Model 3] models are based on fibre properties, whereas ACI [53, Model 4], Ombres [54, Model 5], and Younis et al. [37, Model 6] models are based on FRCM composite properties (effective strain and elastic modulus). The comparison of the average  $V_{FRCM}^{exp}/V_{FRCM}^{pred}$  among the six models indicates that all the models except Triantafillou and Papanicolaou [51, Model 1] and Tetta et al. [7, Model 3] models underestimate the predicted shear strength provided by FRCM jacketing which is conservative. The models seem to perform less effectively for beams that failed by detachment. The dispersion of  $V_{FRCM}^{exp}/V_{FRCM}^{pred}$  is the lowest for Triantafillou and Papanicolaou [51, Model 1] and Tetta et al. [7, Model 3] models.
- ACI 544 [55, Model 7], fib [56, Model 8], and Japan Society of Civil Engineers [61, Model 9] models were implemented to a limited number of FRC jacketed beams and based on the average values of  $V_{FRCM}^{exp}/V_{FRCM}^{pred}$  the shear strength is underestimated. The dispersion of  $V_{FRCM}^{exp}/V_{FRCM}^{pred}$  is very similar between the models. The data used are limited and further work is needed in the direction of generating experimental data and the development of reliable formulae.

The conclusions drawn from this review rely on the sampling presented in the compiled database in Appendix A. To verify the main observations made, future experimental studies, especially concerning FRC jacketing, are necessary to provide additional data. Several areas that require further investigation have been identified, including understanding the interaction between the internal shear reinforcement and the externally applied mortar-based composite jacket. Effective anchorage systems to prevent detachment of U-wrapped jacketed beams also need development. Defining the limiting effective strain of the fibre is crucial for improving existing models predicting the shear strength contribution of FRCM jackets. Moreover, there are gaps in existing studies on shear performance of RC beams strengthened with externally bonded mortar-based composites, necessitating more research and experimental testing on basalt-FRCM to validate its mechanical properties and potential in strengthening RC beams. A deeper understanding of the bond behaviour and load transfer mechanisms between internal shear reinforcement and the external jacket is essential for reliable design guidelines. Innovative anchorage solutions must be explored and evaluated to ensure the long-term durability and effectiveness of the strengthening system.

Moreover, existing predictive models for shear strength contribution of jackets lack accuracy, as they do not adequately consider critical factors such as the shear span-to-depth ratio and the mortar thickness. These factors have been observed to significantly influence the effectiveness of strengthening. Additionally, advancing the field of RC beam strengthening using FRCM composites requires a precise definition of the limiting effective strain of fibers. This parameter, which relates to the strain at which fiber detachment occurs, has a substantial impact on the overall performance of the FRCM jacket. Developing a reliable definition based on rupture strain or detachment failure strain of the textile reinforcement will enable the creation of more precise and reliable predictive models.

# **Declaration of Competing Interest**

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

### Appendix A.

Table A1.

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# X. Liu and G.E. Thermou

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