

## Research Article

# Application of Fuzzy and Conventional Forecasting Techniques to Predict Energy Consumption in Buildings

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This paper presents the implementation and analysis of two approaches (fuzzy and conventional). Using hourly data from buildings at the University of Granada, we have examined their electricity demand and designed a model to predict energy consumption. Our proposal was conducted with the aid of time series techniques as well as the combination of artificial neural networks and clustering algorithms. Both approaches proved to be suitable for energy modelling although nonfuzzy models provided more variability and less robustness than fuzzy ones. Despite the relatively small difference between fuzzy and nonfuzzy estimates, the results reported in this study show that the fuzzy solution may be useful to enhance and enrich energy predictions.

## 1. Introduction

Electricity is one of the most important inventions science has conferred on humanity. It has become an essential aspect of people's work and day-to-day life. Today, electricity is a pivotal source of energy, and its growing usage worldwide is bringing new challenges in the energy efficiency field. Besides, the recent advances in technology are providing us with a vast amount of information that is not easily treatable for its heterogeneity [1]. Nonetheless, even though our society tends towards more sustainable development, it is not a trivial task to create tools for the accurate treatment and monitoring of energy [2, 3]. Thus, being prepared for the future may be a key to solve energy waste and adequate energy efficiency in our buildings.

Energy consumption forecasting is a critical feature for environmentally friendly buildings as well as an effective strategy to decrease energy consumption and its associated gas emissions along with the resulting economic impact [4, 5]. As a result, energy demand forecasting has been addressed in many scenarios so far [3, 6–9]. Since this problem has in nature historical-oriented data, i.e., we always attempt to find dependencies between past values to model future ones, most of the authors employ time-series

techniques to handle it. Plus, a variant that is gaining in popularity is the combination of fuzzy logic with time-series methods [2, 10–16].

What makes the fuzzy time series suitable for these sorts of problems is its capability to improve the comprehension of the models. That is to say, fuzzy logic provides us with a description of the data in linguistic variables, i.e., by words instead of numerically. Nonetheless, the definition of the fuzzy sets requires introducing a new parameter and, therefore, more complexity to the solution, which is the number of intervals. Originally, some authors defined that the best number of intervals should be seven with a constant length [2, 3]. However, the researchers soon realized that it affected the predictive capacity of the model [17].

Today, these intervals are defined mainly by optimization algorithms. In [18], the authors presented a fuzzy solution for big data using time-series techniques. The authors implemented an automatic clustering algorithm to group the historical data into intervals of different lengths. Their models outperformed classical methods bringing with them several advantages: easy-to-implement, accuracy, and interpretability. Additionally, some authors have incorporated neural networks into their proposals, enhancing, even more, their estimates. Bas et al. [19] employed an artificial neural

network to determine fuzzy relationships to improve the accuracy of the forecasting performance. Cagcag Yolcu and Lam [20] combined a robust approach for fuzzy time series by analysing how the prediction performance of the models is affected by the outliers. Their results were more accurate and robust. It is important to note that the authors of the previous two studies predicted directly using neural networks. This approach will be followed in our study in order to compare our results with the reference series.

Many other approaches have been suggested in the literature to solve energy demand prediction [17], starting with the traditional ARIMA approach [21–24] and moving towards more advanced deep learning techniques [25–31]. Other research works are by Pérez-Chacón et al. [32] with their algorithm to predict big data time series based on a pattern sequence method. They used data from Uruguay’s electricity demand to validate their solution. An interesting COVID-inspired algorithm was proposed by Martínez-Álvarez et al. [33] who used electricity load time series as an application case, showing outstanding performance. Other hybrid algorithms have been proposed by Ruiz et al. [34] in which the authors combine a memetic algorithm with recurrent neural networks to predict energy consumption in public buildings. An ensemble of several predictive models was introduced in [35] where three machine learning algorithms were used (decision trees, gradient boosted trees, and random forest). Their combination successfully outperformed other big data time-series solutions.

We can also mention some applications of fuzzy logic to time series [10, 17–20, 36, 37]. Some research as to a combination of deep learning and fuzzy time series is proposed in [18]. The authors implemented a LSTM-based forecasting model to predict energy consumption. They utilised the fuzzy rules to create preliminary estimates that were used to support the final prediction and to modify the learning process. In [17], we can find another hybrid forecasting system based on fuzzy time series for wind speed estimation. Here, the fuzzy time-series method was used to optimise a multiobjective algorithm to balance the conflict between accuracy and stability. Other similar studies can be cited like the convolutional neural networks of Sadaei et al. [36] or the integration of heuristics for renewable energy forecasting in [38]. Nonetheless, all the authors agree on the same point, the accuracy of the models using fuzzy logic is not good enough, and they use it only as a complement to their solutions.

Following the philosophy of the previous studies, the present work pursues to implement and compare several forecasting techniques to predict energy consumption in public buildings, more specifically, at the University of Granada. What motivates our study is the lack of approaches that exploits the use of fuzzy logic to predict energy consumption. The main advantage of applying fuzzy logic is that it provides us with extra information which can be interpreted as justifying changes in consumption. It may give rules such as «on Monday in the morning, the consumption in summer is low», and opposite to conventional approaches, the latter cannot provide such information. Nonetheless, these fuzzy-oriented models have the drawback

of being less accurate than the numerical ones. This fact is somehow understandable as the fuzzy rules attempt to join information. Therefore, our first goal is to implement a solution using fuzzy systems and optimise them so as to get a comparable precision. To do so, we propose a hybrid method of fuzzy time series and clustering algorithms. The rest of the paper is structured as follows. Section 2 describes the proposed methodology, data used, and its treatment along with the methods applied. Section 3 introduces the experiments conducted. Section 4 gathers the main results obtained in this study. And Section 5 summarises the conclusions attained.

## 2. Methodology

This section is pivotal to properly understand the rest of the study along with the decisions made throughout this research. As a general overview of the steps followed in this research, we can examine Figure 1. First, we obtain the energy information directly from the meters, which may present missing values, errors, or other problems. After that, we cleaned, processed, and selected the data we planned to use for comparison. Since our first aim was to compare the fuzzy implementations with the conventional ones, we carried out the nonfuzzy predictions and tested several parameters and granularities so as to get an advance of the estimates’ behaviour. Then, we selected the appropriate granularity and settled several considerations and applied the fuzzy approach. Both, fuzzy and nonfuzzy results were stored for a final comparison and analysis. Finally, we draw some interesting conclusions from our results altogether.

*2.1. Dataset.* First of all, prior to defining the bulk of our methodology, it is important to know the data we are training with. The time series in hand belongs to meters from the University of Granada. The measurements were taken on an hourly basis and are expressed in kWh. Most of the series comprises 5 years of data, from 2013 to 2018. Some present slightly smaller sizes owing to the date of installation of the metering systems and therefore the start of the sample collection.

Our data consist of a set of meters. Each device measures several buildings. Accordingly, the time series and building distribution are exposed in Table 1. For privacy reasons, the name of the buildings is not shown.

We selected the series according to the quality of the data. We utilised 10 series out of 20 available. What motivated this decision was the quality of the data and the likeliness of the series. In other words, the sheer number of missing values in some cases was excessively high, and as an objective criterion, we discarded the ones with the higher absence of data. Besides, it also prevented biased results by the imputation of missing values.

In many cases, empty registers can be found in the middle of the series presenting more than 6 months of empty records, with some exceptions such as the one displayed in Figure 2. The figure represents the energy

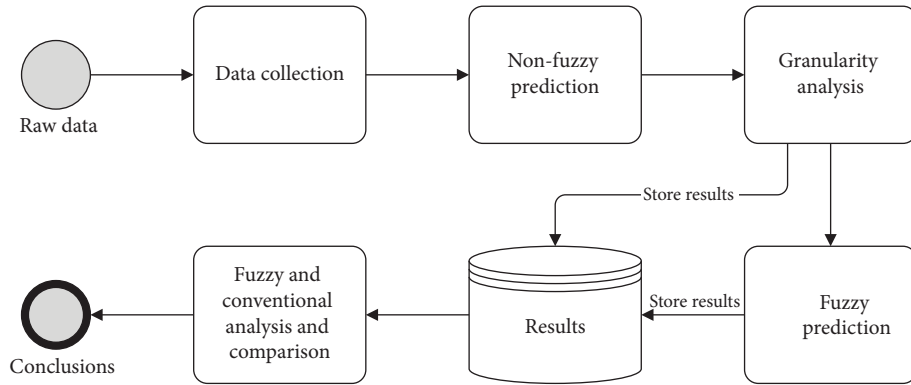


FIGURE 1: General scheme of the proposed methodology.

TABLE 1: Buildings’ description of the database.

Building	Meters available	Meters used
B1	4	2
B2	5	4
B3	4	1
B4	7	3

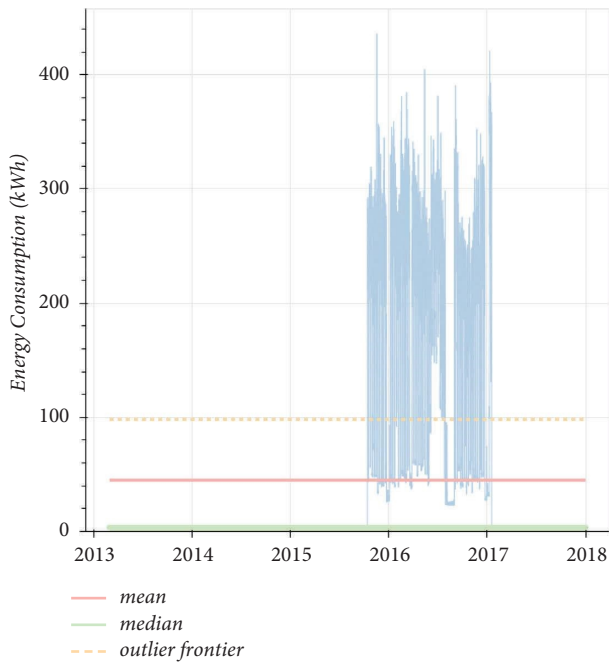


FIGURE 2: Example of discarded time-series, representing the mean (red), median (green), and the outlier region (dotted orange) of the consumption (blue).

consumption of one of the buildings during the morning period. It can easily be seen that the motive of our choice is that, from 2013 to 2017, we do not have any relevant information except for a little more than a year. It is rather straightforward to see how the outlier frontier was not adjusted properly as most of the consumption is outside. Also, the lack of registers with a correct record makes the mean and median well below the actual value. Opposite to this, we have Figure 3.

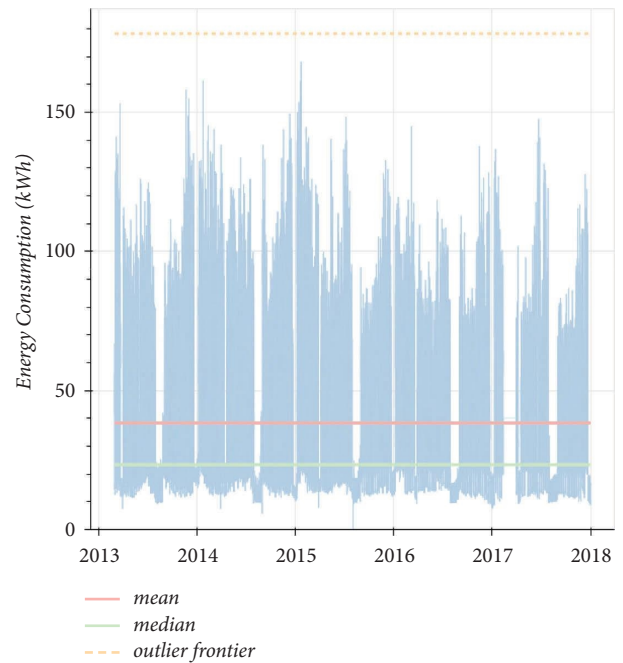


FIGURE 3: Example of one of the energy time series chosen.

As we mentioned before, our data are collected hourly and consequently, we split the series into three-time slots: morning, between 8 h and 15 h; evening, from 16 h to 22 h; and night, starting at 22 h until 6 h. Those intervals were chosen according to the morning and afternoon shifts, taking into account the classes. An example has been already presented in Figure 2 with the morning series of the building. Another representative series we selected is depicted in Figure 3. In this case, in contrast to Figure 2, we can appreciate a more normalised behaviour in consumption. Most of the records were properly collected with some exceptions (see the first month of 2017).

2.2. Data Preparation. After describing the data we are using, we must mention how we preprocessed the data for our models. The data used for our workflow are made of 10 energy time series on an hourly basis from meters at the University of Granada. These data were transformed into

five different series whose prediction could be interesting: (1) hourly (actual data), (2) morning [8, 15]h, (3) evening [16, 22]h, (4) night [23, 7]h, and (5) daily (accumulated consumption).

In doing this, we created a 5-element decomposition of each series and thus a set of 50 sets of data. We will apply a fuzzy treatment to each of these new series with the clustering algorithms. They will be used in the forecasting stage as well. Furthermore, it will generate a fuzzy time series for each clustering method. In other words, 150 fuzzy series are to be added to the 50 previously created. As a result, we obtained 200 time-series for each forecasting method.

*2.3. Methods Applied.* The current section introduces all the methods we have applied to the aforementioned data already prepared. In this work, we implemented two well-known machine learning techniques, multilayer perceptron (MLP) and long short-term memory (LSTM) neural networks, along with three clustering methods, namely,  $k$ -Means (kM), density-based spatial clustering of applications with noise (DBSCAN, DB in short), and hierarchical clustering (HC). The two first methods were used as a predictor in both fuzzy and conventional approaches, and the other three were used to define the number of intervals for the fuzzy sets using the triangular membership function.

MLP is a type of feed-forward neural network. Its structure is mainly composed of three layers: input, hidden, and output layer. The input takes the data to be processed, and the hidden layers get the results from the previous layer and pass the information to the output layer. Each layer has several neurons that use an activation function so as to move the computations onward through a particular value (or weight) between two neurons. In this case, the information is processed in a forward fashion, i.e., from input to output [3].

On the other side, we adopted the LSTM. In contrast to the MLP, where the data flow from back to front, LSTM has recurrent connections allowing them to move the information back and forth. In this way, feedback from other layers is provided [17]. The choice to employ this model was based not only on the wide range of successful applications [26, 34, 39, 40] but also on its great flexibility and adaptation when solving problems.

The first algorithm we implemented for procuring the fuzzy variables was kM [18]. This is one of the most popular techniques based on dividing the data into  $k$  groups. An iterative procedure assigns randomly  $k$  points as centres (or centroids). Then, each sample is linked to a particular group that minimises the error. Once all the points have been associated with a cluster, it recalculates new centroids as the mean of the member points. This process is iteratively repeated until certain stop criteria are fulfilled.

The second clustering algorithm is DB [36] that, as its name indicates, is based on the detection of communities via density features. The definition of community has two parameters: the number of instances and  $\epsilon$ , being the latter the distance needed to be considered in the vicinity of one cluster. This feature is rather interesting as those points far enough from all the centres are considered outliers.

Lastly, we implemented agglomerative or hierarchical clustering (HC) [38]. In this technique, a distance metric is defined, first of all, as being plausible a metric with a cluster-cluster or cluster-sample basis. In this way, all the points are isolated and they progressively come together to the closest cluster/sample creating new groups. Conceptually, it builds a tree-based structure where the leaves represent the initial data and each branch a specific cluster.

For the fuzzification process, we implemented a Sugeno-based inference system. It has multiple inputs and just one output. In our implementation of the inference system, the ANNs act as a black box generating functions to the related inputs with outputs instead of using directly the interpretable rules. Besides, we will be able to prevent the defuzzification phase through the ANNs which leads us to a more flexible approach. We utilised a triangular membership function like the one displayed in Figure 4. This function allows us to get the membership degree to each of the fuzzy sets. To this end, it is needed to know the limits and the central point that will define each fuzzy set. For instance, the limits in the red set are 0 and 60 kWh and the central point is 20.

Then, having a time series  $t_{1,n}$  of  $n$  values and a set  $C$  of  $m$  centroids, we can define a triangular function for each  $c \in C$ . In doing so, we will obtain a matrix  $t_{m,n}$  with the membership degrees of each centroid.

We should thoroughly take the number of lags  $l$  (previous values for prediction) of the time series as this will turn the original series into  $l \cdot m$  columns to be predicted, thereby increasing the complexity of the problem.

These functions are defined by the centroid (e.g.,  $k$ -Means) or by the mean of each cluster (e.g., DBScan). The points that are not in the min and max of the distribution were classified as outliers. The edges were built as follows. The cluster with the smallest values starts at 0 or the minimum value of the cluster minus the standard deviation. In the case of the cluster with the biggest values, it ends in the value of the biggest value plus a standard deviation. In doing this, we prevented the appearance of undetected outliers in which their membership degrees were 0 and had a very high (or low) consumption while they remained undetected. The outliers amongst clusters were eliminated by maximising the Silhouette coefficient. The outliers were processed the same way in all the implemented algorithms. They were detected by enlarging the edges of the distribution function or when they fall into two different membership functions.

Finally, the representation of the proposed workflow is depicted in Figure 5. First, the data are treated by the clustering algorithm in the fuzzification process providing the membership degrees and then the news information is given to the forecasting model so as to obtain the predicted value after defuzzification. The use of the proposed forecasting models allows us to decide as to which output will be provided, the fuzzy representation or the numerical one as is shown in the figure. Bearing in mind that the defuzzification phase is not as important as the fuzzification part of the implementation of our Sugeno-type inference system, this stage is implicitly included in the ANNs that translate the membership values into a straight prediction.

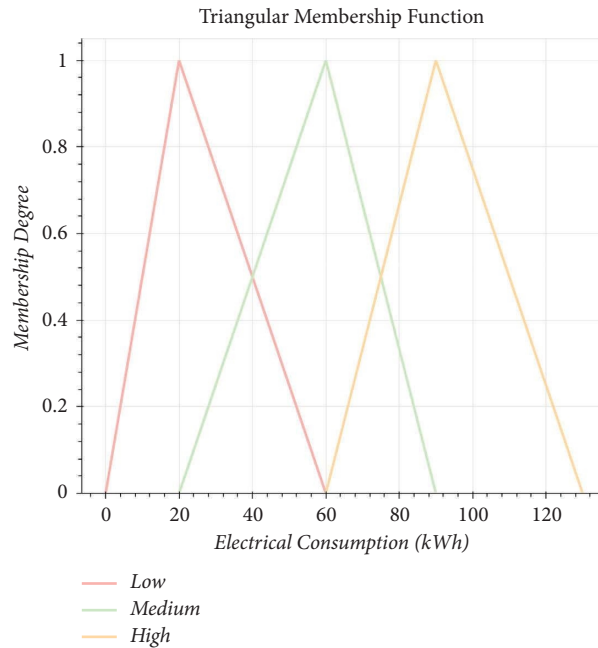


FIGURE 4: Triangular membership function for the three energy consumptions (high, medium, and low).

### 3. Experiments

The experiments conducted in this study are detailed in the following paragraphs to provide a proper understanding of the technologies adopted and the design of the trials.

This research project has been entirely developed in Python 3.7. We employed four widely used libraries, namely, Scikit-Learn, Keras, Pandas, and Bokeh. Scikit-Learn was used to implement MLP and the clustering algorithms, DB, HC, and kM. LSTM was implemented in Keras. Pandas was used to manipulate our data and process the information. Finally, Bokeh was utilised as a means for depicting our results.

We designed our experiments in several stages as can be seen in Figure 6. The first is data collection and clustering analysis based on the Silhouette coefficient. Second, we predicted the entire series and analysed the nonfuzzy approaches and their results. It was examined both daily and hourly granularities. Third, we studied the performance of the fuzzy-based solutions. Finally, we contrasted both fuzzy and conventional solutions.

### 4. Results

The results obtained from the prediction of the 200 time-series generated are presented in this section and discussed in the next one. They will be analysed according to the forecasting method used. For simplicity reasons, we will introduce a summary of the most remarkable outcomes; otherwise, it would make it difficult for the reader to follow the discussion.

As we can deduce from Figure 5, the first experiments we designed were in the fuzzification part. We had to set a number of clusters so as to get how many functions we will use in the next stage. We selected the Silhouette coefficient

and selected the best values accordingly. Interestingly, in nearly none of the tests, the best number of clusters surpassed three. We skip these results considering them of no great significance as they do not provide much further information to the reader. We will discuss this fact in the next section. Having said that, let us introduce the most remarkable experiments we thought out.

Since we intend to compare two approaches, a fuzzy-based solution and the numerical one (or the nonfuzzy approach), we present Table 2 first, which gather the results for the entire series on both a daily and an hourly basis.

In view of the fact that the fuzzy table with all the models and experiments would be too large, we are going to split its content into different tables and highlight the most significant results. Table 3 compares the clustering methods we applied when using the MLP neural network. We implemented three clustering algorithms, DBScan (DB), hierarchical clustering (HC), and  $k$ -Means (kM).

As an example of the prediction performed by one of the models, we can see Figure 7. We do not put all the series together (the two models, LSTM and MLP) in order to make it easy to discern what is happening. Although some of them follow the trend of the original time-series, others cannot fit that well. In this piece of series, it is interesting to see how it is not clear to tell from the figure whether DB is the algorithm with the highest error, but mathematically it is.

Similarly, we conducted the same experiments but using LSTM. We can see the metrics obtained in Table 4.

Table 5 presents the results obtained after adjusting our models with the hourly time series. We compared the three clustering algorithms, DB, HC, and kM as well.

As we mentioned before, we do not want to make it difficult for readers to follow our study; for this reason, we will skip some results and we will go straight to the

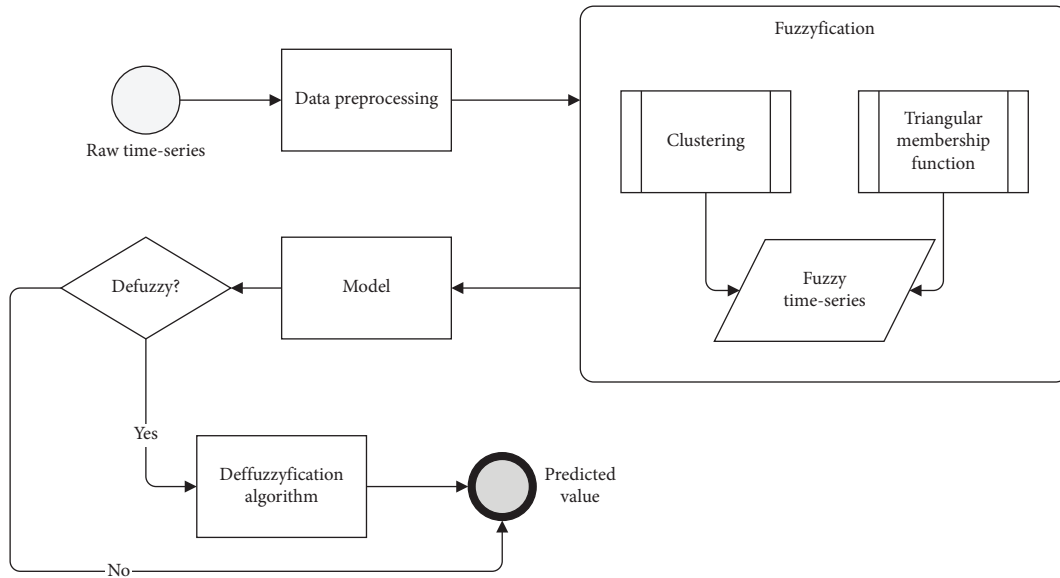


FIGURE 5: General overview of the hybrid fuzzy logic and clustering model.

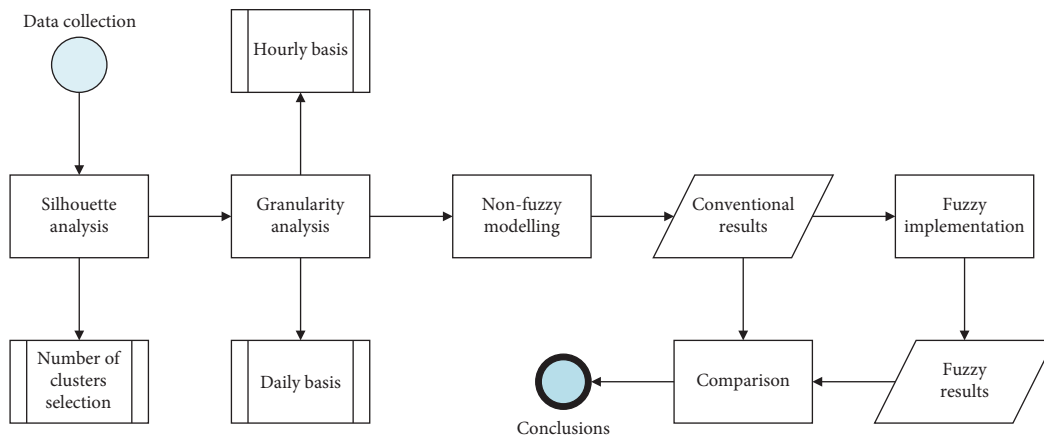


FIGURE 6: Flowchart of the experimentation carried out.

comparison table between fuzzy and nonfuzzy approaches. Since MLP has shown better error, Table 6 gathers the results with this model and compares the best results of the fuzzy solution versus the one without fuzzy logic applied.

As an illustrative example of the predictions, Figure 8 shows both conventional (blue series) and fuzzy solutions in the same graph. This chart presents the evolution of consumption on a daily basis.

## 5. Discussion

This section brings together the most significant results we achieved from our experiments. As we mentioned in the second paragraph of the previous section, we would like to point out that the number of clusters was chosen by maximizing the Silhouette coefficient and selecting the most appropriate value accordingly. Each cluster stands for a membership function of its own. Most of the experiments we carried out provided three as the optimal value although

there were some experiments in which the number of clusters exceeded three according to our selection criteria. Having this into consideration, the tags in our univariate time-series define a linguistic variable. For the three-cluster case, we would have «low», «medium», and «high» consumption. Similarly, given five clusters, we tagged them as «very low», «low», «medium», «high», and «very high» consumption. Knowing that the linguistic variables given to each of the electricity meters were based on their consumption as the use of each building differs, it was reasonable to assume that the variables should behave uniformly in our scenario, not adding much information on their own by the name.

Then, we have to comment on some important aspects of Table 2. The table puts together the results of our models for both daily and hourly granularities. From the table, we can draw some conclusions. The first one is that virtually all the experiments revealed MLP as the best predictor in both granularities. Nevertheless, according to the MAE, only 6 out of 20 LSTM turned out to be better than MLP in the daily

TABLE 2: Comparison between LSTM and MLP models without using the fuzzy approach using the entire series.

Meter	Model	Daily			Hourly		
		RMSE	MAE	$R^2$	RMSE	MAE	$R^2$
M1	LSTM	146.1452	64.1385	0.7411	5.3348	<b>1.4093</b>	0.9177
	MLP	<b>125.4831</b>	<b>56.3078</b>	<b>0.8092</b>	<b>5.1306</b>	1.5869	<b>0.9239</b>
M2	LSTM	223.3225	<b>88.8834</b>	0.5515	10.9791	<b>1.6636</b>	0.8495
	MLP	<b>138.0524</b>	<b>59.2156</b>	<b>0.8286</b>	<b>10.6464</b>	2.9834	<b>0.8584</b>
M3	LSTM	190.5074	87.7230	0.4206	<b>4.6348</b>	<b>1.0642</b>	<b>0.9345</b>
	MLP	<b>143.4906</b>	<b>51.9965</b>	<b>0.6713</b>	4.7567	1.4236	0.9311
M4	LSTM	804.5589	<b>170.6163</b>	0.5776	11.1949	<b>2.2656</b>	0.9827
	MLP	<b>666.6745</b>	190.1642	<b>0.7100</b>	<b>10.1513</b>	2.6782	<b>0.9858</b>
M5	LSTM	447.4029	<b>104.5444</b>	0.5214	6.7374	1.0369	0.9766
	MLP	<b>379.0906</b>	111.1212	<b>0.6564</b>	<b>6.7014</b>	<b>0.9829</b>	<b>0.9769</b>
M6	LSTM	218.1491	50.4770	0.5603	5.0652	<b>0.6833</b>	0.9541
	MLP	<b>179.5734</b>	<b>50.0577</b>	<b>0.7020</b>	<b>4.8017</b>	1.0286	<b>0.9588</b>
M7	LSTM	232.0006	<b>61.1003</b>	0.7551	8.1263	<b>0.6860</b>	0.9419
	MLP	<b>202.1236</b>	66.4395	<b>0.8141</b>	<b>7.8352</b>	1.2313	<b>0.9460</b>
M8	LSTM	98.5282	<b>24.3363</b>	0.7554	4.3384	<b>0.5955</b>	0.9164
	MLP	<b>89.2251</b>	32.0510	<b>0.7994</b>	<b>4.0838</b>	0.8277	<b>0.9259</b>
M9	LSTM	78.9721	<b>30.2903</b>	0.8466	4.2556	<b>1.5538</b>	0.8912
	MLP	<b>69.3567</b>	31.2242	<b>0.8817</b>	<b>4.1723</b>	1.7256	<b>0.8954</b>
M10	LSTM	213.9082	<b>52.9707</b>	0.7196	5.7286	<b>1.0394</b>	0.9535
	MLP	<b>163.2353</b>	63.7221	<b>0.8367</b>	<b>5.5033</b>	1.3785	<b>0.9571</b>

Bold value represents the best value between the two rows of each model.

one and 9 in the other set of experiments. However, we can see how the  $R^2$  metric provides a much worse value in those cases. Additionally, the difference between RMSE and the MAE in such tests resulted to be higher than MLP's which gives us the hint that MLP is having more robust estimates. It is remarkable to note that both models enhanced their predictions in terms of the  $R^2$  metric when working with the hourly data. This can be a result of the amount of data available in such a case.

Taking into account the errors made by the predictive models and both granularities, the next step is to implement the clustering methods. Thus, Tables 3 and 4 compare each clustering algorithm using MLP and LSTM, respectively. From Table 3 we might discard the use of DB as it did not attain the best adjustment in any case. Furthermore, DB got the third position according to all the metrics we used. Regarding HC and kM, they achieved very similar results. However, HC outperforms kM in 60% of the cases for the RMSE and  $R^2$  metrics, and only for the MAE, they obtained 50% each. And what stands out in Table 4 is that DB maintains its last position and only in M6 outperformed its rivals which had a quite low  $R^2$ . In this case, 5 out of 10 tests

give HC the best performance by RMSE and  $R^2$ , and the remaining 4 were for the kM algorithm. The most interesting aspect of Table 4 is that 7 out of 10 kM's MAE were better than HC's, of which 4 repeated their behaviour from the MLP model (meters 2, 5, 7, and 8; see Table 3).

Next, we have to pay attention to Table 5 which has the metrics once trained our predictive models using the hourly time-series. A closer inspection of the table shows a significant improvement in the DB algorithm. In addition to this, all the metrics have been enhanced in all the cases. In fact, now DB has the best scores in 8 out of 10 predictions according to RMSE and  $R^2$  and 5 out of 10 with the MAE metric. The rest of them is distributed as follows: HC obtained the best RMSE and  $R^2$  in M3 and the best MAE in M5; kM was the best for M2 according to the three metrics, and it was the best rank in M7, M8, and M10 for the MAE. These results reveal not only DB as the best clustering algorithm but also a general improvement in the accuracy of the predictions and better robustness using more data. Bear in mind that the table utilised the hourly time series, and therefore the models have more information to work with, and this has to be the reason for this improvement.

TABLE 3: Comparison of the different clustering techniques for the fuzzy-oriented approach with MLP on a daily basis.

Meter	Method	RMSE	MAE	$R^2$
M1	DB	177.7155	120.7909	0.6172
	HC	<b>144.8932</b>	<b>73.3900</b>	<b>0.7456</b>
	kM	147.2462	77.8078	0.7372
M2	DB	229.1446	119.5351	0.5278
	HC	182.6804	80.4405	0.6999
	kM	<b>162.8930</b>	<b>77.9993</b>	<b>0.7614</b>
M3	DB	190.1826	104.0214	0.4226
	HC	<b>153.1764</b>	<b>77.6672</b>	<b>0.6254</b>
	kM	168.7235	94.0590	0.5455
M4	DB	855.2163	313.5884	0.5228
	HC	<b>676.5370</b>	<b>210.2765</b>	<b>0.7014</b>
	kM	727.3272	235.0870	0.6548
M5	DB	416.8174	129.1178	0.5846
	HC	390.0882	134.7437	0.6362
	kM	<b>383.4103</b>	<b>124.1867</b>	<b>0.6485</b>
M6	DB	225.7441	85.4364	0.5291
	HC	<b>177.9789</b>	<b>66.9214</b>	<b>0.7073</b>
	kM	194.6913	93.9808	0.6498
M7	DB	338.4739	166.1670	0.4788
	HC	224.2768	82.0394	0.7712
	kM	<b>213.3479</b>	<b>74.5784</b>	<b>0.7929</b>
M8	DB	136.1172	81.3379	0.5331
	HC	<b>95.7162</b>	34.4682	<b>0.7691</b>
	kM	96.7354	<b>28.9196</b>	0.7642
M9	DB	114.5623	57.0771	0.6771
	HC	75.4612	32.1241	0.8599
	kM	<b>71.2364</b>	<b>29.4829</b>	<b>0.8752</b>
M10	DB	259.4291	114.6123	0.5876
	HC	<b>171.0675</b>	<b>75.5993</b>	<b>0.8207</b>
	kM	191.8339	97.0186	0.7745

Bold value represents the best value among the three rows of each method. DB is DBScan, HC is hierarchical clustering, and kM is  $k$ -Means.

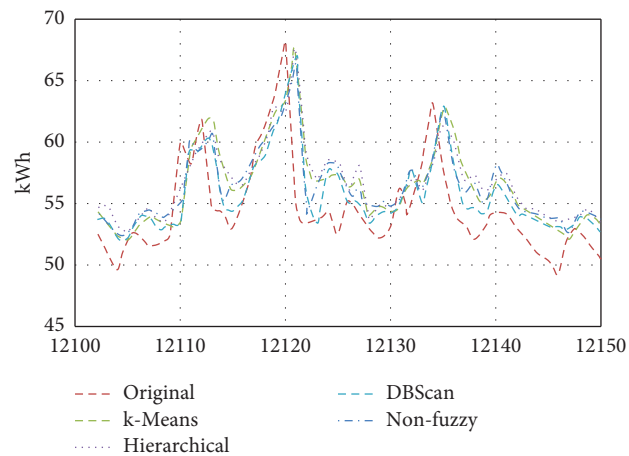


FIGURE 7: Example of the hourly prediction performed by the MLP of one of the meters. Comparison of the different clustering methods along with the conventional model.



TABLE 4: Comparison of the different clustering techniques for the fuzzy-oriented approach with LSTM on a daily basis.

Meter	Method	RMSE	MAE	$R^2$
M1	DB	204.6027	94.4456	0.4926
	HC	<b>195.5054</b>	<b>92.9729</b>	<b>0.5367</b>
	kM	216.1003	109.9226	0.4340
M2	DB	409.9392	307.3953	-0.5111
	HC	280.1156	121.2162	0.2944
	kM	<b>252.8798</b>	<b>92.4339</b>	<b>0.4250</b>
M3	DB	275.5571	117.3078	-0.2122
	HC	<b>211.3214</b>	<b>92.0701</b>	<b>0.2871</b>
	kM	222.4379	107.1479	0.2101
M4	DB	1319.6981	654.4967	-0.1363
	HC	978.9773	214.1039	0.3747
	kM	<b>960.4926</b>	<b>191.4649</b>	<b>0.3981</b>
M5	DB	544.9214	154.6821	0.2901
	HC	<b>511.4943</b>	114.9144	<b>0.3745</b>
	kM	511.5907	<b>95.2821</b>	0.3743
M6	DB	<b>232.0024</b>	59.7434	<b>0.5026</b>
	HC	269.5572	64.4206	0.3286
	kM	253.0153	<b>55.5814</b>	0.4085
M7	DB	425.5167	166.9462	0.1762
	HC	<b>286.3125</b>	98.4231	<b>0.6270</b>
	kM	296.6960	<b>95.4022</b>	0.5995
M8	DB	170.7479	41.8688	0.2653
	HC	117.1675	29.4378	0.6541
	kM	<b>115.5324</b>	<b>28.0488</b>	<b>0.6637</b>
M9	DB	207.3880	134.1462	-0.0581
	HC	155.0012	<b>41.3702</b>	0.4089
	kM	<b>128.7002</b>	45.2480	<b>0.5925</b>
M10	DB	337.4693	87.3844	0.3022
	HC	<b>251.8003</b>	85.1934	<b>0.6115</b>
	kM	274.7407	<b>84.9319</b>	0.5375

Bold value represents the best value among the three rows of each method. DB is DBScan, HC is hierarchical clustering, and kM is  $k$ -Means.

The results shown in Table 6 indicate that both approaches turned out to be very accurate as virtually all of them achieved over 0.9 in  $R^2$ . Further analysis of these predictions shows that the fuzzy approach gives better results in 50% of the cases by MAE and in 4 cases by RMSE and  $R^2$ . Nonetheless, it is interesting to note that we can find slight differences between them. The biggest difference of  $R^2$  was 0.006 for the M2, the tiniest with 0.00004 for the M4, and on average of 0.002.

Finally, as an illustrative example of the predictions, we may take a look at Figure 8. As we can see, there is a weekly pattern. There are two points, the lowest ones that correspond to the weekends, and therefore it is normal that they were lower than the rest. In any case,

TABLE 5: Comparison of the different clustering techniques for the fuzzy-oriented approach with MLP on an hourly basis.

Meter	Method	RMSE	MAE	$R^2$
M1	DB	<b>5.1093</b>	<b>1.6630</b>	<b>0.9245</b>
	HC	5.3902	1.8563	0.9160
	kM	5.2176	1.8483	0.9213
M2	DB	10.8719	2.5343	0.8524
	HC	10.9243	2.7631	0.8510
	kM	<b>10.6448</b>	<b>2.3971</b>	<b>0.8585</b>
M3	DB	4.6532	<b>0.9554</b>	0.9340
	HC	<b>4.6407</b>	1.3267	<b>0.9344</b>
	kM	4.9519	1.3331	0.9253
M4	DB	<b>10.1662</b>	<b>2.3978</b>	<b>0.9857</b>
	HC	11.5014	2.7697	0.9817
	kM	10.9031	2.7014	0.9836
M5	DB	<b>6.8727</b>	1.6164	<b>0.9757</b>
	HC	6.9378	<b>1.3631</b>	0.9752
	kM	7.2575	1.4105	0.9729
M6	DB	<b>4.6280</b>	<b>0.8201</b>	<b>0.9617</b>
	HC	4.6956	0.9210	0.9606
	kM	4.9537	1.2178	0.9561
M7	DB	<b>7.9172</b>	1.3358	<b>0.9448</b>
	HC	7.9193	1.7544	0.9448
	kM	7.9968	<b>1.1567</b>	0.9437
M8	DB	<b>4.1679</b>	1.1607	<b>0.9228</b>
	HC	4.2259	0.9397	0.9207
	kM	4.1785	<b>0.7979</b>	0.9224
M9	DB	<b>4.1845</b>	<b>1.6167</b>	<b>0.8948</b>
	HC	4.2176	1.6730	0.8931
	kM	4.2386	1.7501	0.8921
M10	DB	<b>5.5571</b>	1.3467	<b>0.9563</b>
	HC	5.8465	1.6683	0.9516
	kM	5.6554	<b>1.2593</b>	0.9547

Bold value represents the best value among the three rows of each method. DB is DBScan, HC is hierarchical clustering, and kM is  $k$ -Means.

what should attract our attention is that certain patterns in this series are well predicted and they follow the evolution adequately. However, intentionally, we show two weeks (the last part of the graph) where the consumption is slightly different. On this occasion, the models struggled to follow the trend at first, but they promptly adjust the prediction in a better way. The most significant aspect of Figure 8 we would like to highlight is that the fuzzy-oriented solutions managed to fit the curves properly which is essential for our solution.

Having discussed the results obtained, it can be said that both approaches are shown to be suitable to solve this problem as both of them received the best score in half of the cases.

TABLE 6: Comparison between fuzzy and nonfuzzy approaches.

Meter	Approach	RMSE	MAE	$R^2$
M1	Fuzzy	<b>5.1093</b>	1.6630	<b>0.9245</b>
	Nonfuzzy	5.1306	<b>1.5869</b>	0.9239
M2	Fuzzy	10.8719	<b>2.5343</b>	0.8524
	Nonfuzzy	<b>10.6464</b>	2.9834	<b>0.8584</b>
M3	Fuzzy	<b>4.6532</b>	<b>0.9554</b>	<b>0.9340</b>
	Nonfuzzy	4.7567	1.4236	0.9311
M4	Fuzzy	10.1662	<b>2.3978</b>	0.9857
	Nonfuzzy	<b>10.1513</b>	2.6782	<b>0.9858</b>
M5	Fuzzy	6.8727	1.6164	0.9757
	Nonfuzzy	<b>6.7014</b>	<b>0.9829</b>	<b>0.9769</b>
M6	Fuzzy	<b>4.6280</b>	<b>0.8201</b>	<b>0.9617</b>
	Nonfuzzy	4.8017	1.0286	0.9588
M7	Fuzzy	7.9172	1.3358	0.9448
	Nonfuzzy	<b>7.8352</b>	<b>1.2313</b>	<b>0.9460</b>
M8	Fuzzy	4.1679	1.1607	0.9228
	Nonfuzzy	<b>4.0838</b>	<b>0.8277</b>	<b>0.9259</b>
M9	Fuzzy	4.1845	<b>1.6167</b>	0.8948
	Nonfuzzy	<b>4.1723</b>	1.7256	<b>0.8954</b>
M10	Fuzzy	<b>5.5033</b>	1.3785	<b>0.9571</b>
	Nonfuzzy	5.5571	<b>1.3467</b>	0.9563

Bold values represent the best approach for each metric; that is to say, for each column (metric), we compare the two approaches (fuzzy and nonfuzzy), and the best is highlighted in bold.

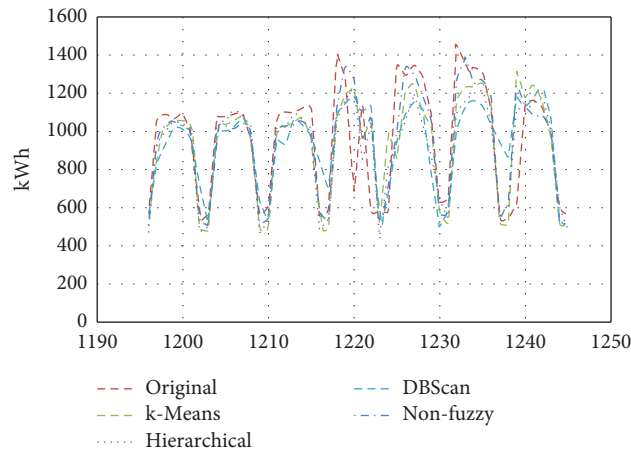


FIGURE 8: Illustrative example of a daily prediction using MLP. Comparison between fuzzy and nonfuzzy models.

## 6. Conclusions

In the course of this research, we implemented and compared several fuzzy and nonfuzzy time-series methods. Apart from the effectiveness shown in previous studies, the fuzzy time series offers extra utility as they provide us with,

not only a single value but an interval in which the objective value is expected to be. This can be translated into a piece of enriching information as there are many scenarios where absolute certainties are uncommon, but trends and approximations have higher importance, as is the case of energy efficiency.

The methods implemented have shown great flexibility during the whole process, from the creation of the fuzzy sets to the final prediction. One of the limitations we should mention is that this flexibility turns into a higher computational cost as several tests should be done prior to deciding some of the parameters. The second drawback is a fuzzy representation of the series leading to a loss in terms of accuracy, and we should balance whether this loss pays off or not depending on the problem to solve. Although the fuzzy models did not achieve the lowest error in all the cases, they managed to maintain higher robustness compared with the numerical ones. Furthermore, those cases in which the fuzzy approaches ranked below presented a slight difference in terms of error, i.e., both predictions were, in all cases, quite similar.

Finally, we would like to highlight the overall performance of the DBScan algorithm against the other clustering algorithms. It is a surprising finding that this method achieved such good results in spite of not being mentioned in the literature by previous authors.

The studied models have demonstrated to have the capability to predict energy consumption at the University of Granada and its buildings. However, as future work, we propose a method for optimal parameters search along with the modification and experimentation with different membership functions. Additionally, we propose the use of density clustering and mean-shift algorithms that may offer good results in these kinds of problems.

## Acronyms

DB:	Density-based spatial clustering of applications with noise
HC:	Hierarchical clustering
kM:	$k$ -Means
LSTM:	Long short-term memory
MAE:	Mean absolute error
MLP:	Multilayer perceptron
RMSE:	Root mean square error.

## Data Availability

The data used in this study are not available for public access due to privacy policies. We are committed to safeguarding the privacy and confidentiality of the organizations involved in this research. Sharing the data, even in an anonymized form, would risk violating these privacy commitments and could compromise the trust and confidentiality of our data sources.

## Conflicts of Interest

The authors declare that there are no conflicts of interest.

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