# HARDWARE IMPLEMENTATION OF A WIRELESS IMPULSIVE SOURCE LOCALIZATION SYSTEM 

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A Thesis Presented to the DEANSHIP OF GRADUATE STUDIES KING FAHD UNIVERSITY OF PETROLEUM \& MINERALS

DHAHRAN, SAUDI ARABIA

In Partial Fulfillment of the Requirements for the Degree of

MASTER OF SCIENCE
In
ELECTRICAL ENGINEERING

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by

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Dhahran, Saudi Arabia

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## DEANSHIP OF GRADUATE STUDIES

This thesis, written by HAIDER ALI under the direction of his thesis adviser and approved by his thesis committee, has been presented to and accepted by the Dean of Graduate Studies, in partial fulfillment of the requirements for the degree of MASTER OF SCIENCE IN ELECTRICAL ENGINEERING.

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Dedicated to my brothers, Uncles and Sir Atta-Ur-Rehman and above all to my late parents who supported me throughout my academic life both morally and financially. I love you all.

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In the name of Allah, the Most Beneficent, the Most Merciful

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# THESIS ABSTRACT 

NAME: Haider Ali<br>TITLE OF STUDY: Hardware Implementation of a Wireless Impulsive Source Localization System<br>MAJOR FIELD: Electrical Engineering<br>DATE OF DEGREE: May 2012

Acoustic source localization systems are becoming an essential part of any modern security system and their accuracy and performance play an important role in the overall structure of such systems. Any acoustic source localization system should be robust enough to work in any real situation like in an indoor or an outdoor environment.

This thesis work focuses on the implementation of an impulsive acoustic source localization system using a new algorithm known as Orthogonal Clustering (OC) by utilizing different wireless signal acquisition hardware and devices. The implementation is carried out using both this new algorithm (i.e. OC) and the conventional Cross Correlation (CC) for comparison purposes. Three different sensor geometries were considered for implementation to observe the effect of the sensor
geometry on the performance of the localization system. Three different wireless hardware systems were used to implement the localization system to verify, compare and analyze the performance of the new algorithm as well as the CC method.

A practical and realistic approach is taken for the implementation of the localization system by implementing it in three-dimensions (3D). To check the consistency and accuracy of the new algorithm as well as of the hardware system the implementation was carried out both in an indoor and outdoor environments. To further verify the consistency of the system in the indoor environment, experiments were carried out both in a less-reverberant environment like the center of a hall and a more-reverberant environment like in a corner of the hall. To analyze the system for computational complexity versus the performance tradeoff the system was implemented for signal acquisition at different sampling rates.

From experiments it was observed that the Pyramid geometry of the sensors was the best among all the geometries accuracy wise. In indoor less-reverberant environment the performance of the OC algorithm was better than the CC algorithm. However, in outdoor environment the CC algorithm produces more accurate results than the OC. Furthermore, the runtime of the CC algorithm (less than a second) is much less than the OC algorithm (more than 10 seconds). The RevoLabs system produces more accurate and consistent results than the VocoPro system.

Keywords: Acoustic Source Localization, Indoor Source Localization, Outdoor Source Localization, Impulsive Acoustics, Wireless Sensor Networks, Commercial off the Shelf Devices

## خلاصة

الاسم: حيدر على

عنوانالرسالة: بناء نظام لاسلكى لتحديد مكان مصادر الاصوات الانفجارية. التخصص: الهنسة الكهريائية


إن إمكانية تحديد مصادر الصوت أصبحت جزء أساسي منه أجهزة الحماية الحيثّة وباتت فاعلية ودقة هذه الإمكانية جزء أساسي من هذه الأجهزة. أجهزة تحديد أماكن الصوت يجب ئب أن تكون فارية على العطل في أي بيئة حققية متل داخل المباني أو خارجها. هذه الرسالة تركز على بناء نظام لتحديد أماكن الأصوات الانفجارية باستخام خوارزمية جديدة تدعى الججموعة المتعامدة (Orthogonal Clustering) وتطبيقها على عدة أجهزة ومعدات لمعالجة وتخزين الإشارات. النطبيق يقارب بين صحة ودقة الخوارزمية الجديدة والخوارزمية المعروفة بفحص الثناتلّ (Cross Correlation). عدة أثكال هندية تمان اعتمادها لثنوزيع الهجسات وأثر ها على دقة تحديد مكان الصوت. ثلاثثة ألجهزة لاسلكية تم استخذامثها لتطبيق النظام علياً وفحص فعاليّتها باستذام الخو ارزميات السابق ذكر ها.

لقّ تم بناء النظام بشكل عطلي لتحديد مكان الصوت بأبعاده الثلاث (3D) للأحقق من صحة النظام

 فحص أثر شدة النزرد في تخزين الإثشارة على صحة ودية تحديد مكان الصوت أيضاً.

من النجارب تم ملاحظة أدق شكل هنسي في تحديد مكان الصوت. هذا الشكل هو الهرم الثناثي الأبعاد (Pyramid) ، في داظل المبنى. كانت أدق النتائج بالستخام خوار ارزمية الهجموعة الـتعامدة.
 الصوت، فقا كانت الدة باستخام خوارزمية فحص الثقاتلّ أسرع بكثير من الهجموعة اللتعامدة بعشر مرات على الأقل. وكان نظام RevoLab اللاسلكي أدق من نظام VocoPro.

## Nomenclature

| Abbrevia |  |
| :---: | :---: |
| AMMSE | Approximate Minimum Mean Square Error |
| AOA | Angle of Arrival |
| CC | Cross Correlation |
| CIR | Channel Impulse Response |
| COTS | Commercial off the Shelf |
| CRLB | Cramer-Rao Lower Bound |
| CS | Compressive Sensing |
| DAQ | Data Acquisition |
| DF | Directivity Factor |
| DFT | Discrete Fourier Transform |
| DI | Directivity Index |
| DOA | Direction of Arrival |
| DTFT | Discrete Time Fourier Transform |
| EDT | Early Decay Time |
| EM | Electromagnetic |
| FPGA | Field Programmable Gate Array |
| FTSP | Flooding Time Synchronization Protocol |
| GCC | Generalized Cross Correlation |
| IASL | Impulsive Acoustic Source Localization |
| IDTFT | Inverse Discrete Time Fourier Transform |


| LS | Least Squares |
| :---: | :---: |
| MAP | Maximum A Posteriori |
| MCU | Microcontroller Unit |
| MMSE | Minimum Mean Square Error |
| MUSIC | Multiple Signal Classification |
| OC | Orthogonal Clustering |
| PHAT | Phase Transform |
| RBS | Reference Broadcast Synchronization |
| RF | Radio Frequency |
| RIR | Room Impulse Response |
| RSS | Received Signal Strength |
| SCOT | Smoothed Coherent Transform |
| SIL | Sound Intensity Level |
| SIMO | Single Input Multiple Output |
| SNR | Signal to Noise Ratio |
| SPL | Sound Pressure Level |
| TDDF | Time Delay Direction Finding algorithm |
| TDE | Time Delay Estimation |
| TDOA | Time Difference of Arrival |
| TPSN | Timing-sync Protocol for Sensor Networks |
| UWB | Ultra Wide-Band |
| WSN | Wireless Sensor Network |

## Notations

| x | Channel Impulse Response |
| :---: | :---: |
| $\epsilon_{C C \_2 D}$ | 2D error for CC algorithm |
| $\epsilon_{O C \_2 D}$ | 2D error for OC algorithm |
| $\epsilon_{C C \_3 D}$ | 3D error for CC algorithm |
| $\epsilon_{O C \_3 D}$ | 3D error for OC algorithm |
| Z | Acoustic Impedance |
| I | Acoustic Intensity or Identity Matrix depending on the context |
| $\alpha_{n}$ | Attenuation factor for path $n$ |
| $\phi$ | Azimuth angle of the source at origin |
| $Z_{0}$ | Characteristic Impedance of an acoustic medium |
| n | Complex White Gaussian Noise |
| $\Phi$ | Design matrix for the Least Squares method |
| $\Psi$ | Dictionary or Sensing matrix |
| $\overrightarrow{\mathbf{k}}$ | Direction of Arrival Vector |
| $\theta$ | Elevation angle of the source at origin |
| $\hat{\mathbf{x}}$ | Estimated channel impulse response |
| $x$ | Estimated source location |
| $\mathbb{E}[x \mid y]$ | Expected value of $x$ given $y$ |
| $f$ | Frequency |
| $\psi_{y_{1} y_{2}}$ | Generalized Cross Spectrum |
| $P$ | Maximum number of clusters |


| $a_{n}$ | Location of microphone $n$ |
| :---: | :---: |
| $\hat{\mathbf{x}}_{\text {MMSE }}$ | MMSE estimate of the CIR |
| $u(k)$ | Noise signal |
| v | Noise vector |
| $b$ | Observation matrix for the Least Squares problem |
| $p$ | Probability of impulses in the CIR |
| $k$ | Propagation Constant |
| $\Gamma$ | Reflection Coefficient |
| $R T_{60}$ | Reverberation Time |
| $x$ | Source location |
| $X_{C C}$ | Source location estimated using CC algorithm |
| $X_{O C}$ | Source location estimated using OC algorithm |
| $s(k)$ | Source signal |
| $\mathcal{S}$ | Sparsity |
| c | Speed of Sound |
| $N$ | The length of the channel impulse response |
| M | The number of rows in the Dictionary Matrix |
| y | The observation vector for OC |
| $\tau_{i j}$ | Time delay between sensor $i$ and $j$ |
| $T D E_{C C}$ | Time Delay Estimated using CC algorithm |
| $T D E_{O C}$ | Time Delay Estimated using OC algorithm |
| $p_{T}$ | Total acoustic pressure at a point |

## $T L$ : Transmission Loss

$\sigma_{x} \quad: \quad$ Variance of the CIR
$\sigma_{i m p}$ : Variance of the impulsive signal
$\sigma_{n} \quad: \quad$ Variance of the noise
$\lambda$ : Wavelength

## CHAPTER 1

## INTRODUCTION

The need of acoustic source localization is growing day by day as an integral part of any modern security system. In particular, localization of sources of impulsive nature in hazardous environments like war, natural catastrophes among others requires the need of robust systems specially designed for this kind of situations. Impulsive acoustic source localization can also be helpful in many commercial applications like shopping malls, conference halls etc. where the location of a burst or a gun shot is to be determined. This work will focus on methods to localize an impulsive acoustic source both in indoor and outdoor environments in three dimensions. A comparison among these methods and their real time implementation and performance will be analyzed and discussed.

This chapter serves as an introduction to the topic of this thesis work. Section 1.1 will discuss the background and a little description about this work while Section 1.2 states the objectives of this thesis work.

### 1.1 Background

Source localization is needed by many applications in engineering and science disciplines [1][2]. Applications ranging from localizing a cell phone user to localizing a sniper fire involves finding the position of the source emanating a signal that can be of electromagnetic or acoustic nature. Increased security issues demand more sophisticated, reliable and robust source localization systems.

Time delay based source localization techniques utilize the time delay that occurs to the signal when it reaches to different sensors at different times. The so called Time Difference of Arrival (TDOA) is the difference in the arrival times of the signal at each sensor. Some algorithms use these TDOA measurements and incorporate them in some mathematical models to directly estimate the source location. These are called TDOA algorithms [3]. Other algorithms take a different approach, they utilize the TDOA information to calculate the Angle of Arrival (AOA) (or Direction of Arrival, DOA) of the signal at each sensor and then utilizing this AOA information they can localize the source. Such algorithms are called AOA algorithms.

Acoustic source localization is becoming an essential technology and its applications are attracting researchers. Localizing the position of the source of gun fire or blast in a war has been studied since World War II [4]. Acoustic source localization systems can be used in malls for security issues or even for daily use, for example, directing the microphone or camera to a certain user in a conference hall or a talk show. Localizing a source that generates an impulsive signal is
equally important and needs the attention of researchers. Impulsive signal source localization systems can be used in military or similar applications.

Although there is plenty of literature available on acoustic source localization, the new technology and advancement in mathematical modeling needs to be incorporated with the existing techniques to take their full advantage to reduce the hardware complexity and energy consumption and enhance the performance of existing systems.

In this work we will use the modern Compressed Sensing (CS) approach to localize impulsive acoustic sources and evaluate its performance. The focus will be on three dimensional source localization using a new algorithm called Orthogonal Clustering (OC) [5] which is a variant of CS. This new algorithm will allow impulsive acoustic source localization by sampling the sensors at reduced rates lower than the Nyquist sampling rate. The work done in [6] already has proved the applicability and feasibility of the algorithm in a two dimensional acoustic source localization environment. Moreover, the algorithm works best (according to the author of [6] in a dense reverberant environment which is the requirement of several practical systems that operate indoors.

In addition, three hardware systems will be used to implement a wireless impulsive acoustic source localization system in 3D. The effect of variations of several parameters on the system performance will be evaluated, such as the indoor and outdoor scenarios, the effect of the number of microphones and the directivity of microphones and sampling rate on the accuracy of the localization system.

Moreover, a performance comparison between a conventional time delay estimation (TDE) technique such as cross correlation (CC) and the new OC based estimation technique will be conducted and the performance of both techniques in the hardware systems implemented will be evaluated for localizing an impulsive acoustic source in 3D.

### 1.2 Thesis Contributions

The major contributions of this thesis are given below:

1. A Commercial off the Shelf (COTS) Wireless Sensor Network (WSN) realizing a wireless localization system of acoustic impulsive sources was configured and tested. Different issues and error sources were identified and verified through a number of experiments to show that the COTS WSN platforms are not suitable for acoustic source localization. Several suggestions were given with examples from the literature to overcome the shortcomings of the existing WSN hardware and software to make them workable for acoustic source localization.
2. A detailed study on the effects of the orthogonal clustering (OC) algorithm parameters on the accuracy of the time delay estimates (TDE) obtained from it in a reverberant environment was conducted. Such a study is the first to appear for this newly developed algorithm.
3. Two different wireless microphone systems were used for acoustic signal
acquisition and integrated with the hybrid algorithm based on the OC TDE method and time difference of arrival (TDOA) 3D localization method for impulsive acoustic source localization. It was observed that the hardware system has a significant contribution in the accuracy of the system.
4. An extensive experimentation and performance study was carried out both in indoor and outdoor environments to analyze and compare the performance of the 3D impulsive acoustic localization system using two different TDE methods one based on OC and the other was based on the well-known cross correlation (CC) method. In the indoor environment, two locations were examined; at the center of the room and at the corner of the room to represent low and high reverberant environments, respectively. This is the first extensive experimentation study to appear comparing OC with other methods for 3D localization.
5. The effects of the microphone geometry, sampling rates and acquisition systems were investigated in details on the accuracy of impulsive acoustic localization system in 3D. Three different microphone array geometries were used to see the effect of geometry structure on the accuracy and performance of both of the OC and CC TDE methods. It was observed that the Pyramid geometry, due to its special structure, was producing the most accurate results while the Rhombus geometry was producing the least accurate results. In addition, it was observed that in indoors the OC produces better results for 4 kHz than CC , while in outdoor the CC was producing better results
than OC at reduced rates.

## CHAPTER 2

## INTRODUCTION TO

## ACOUSTICS

Acoustics is a complete science by itself. Acoustic waves generally behave differently in indoor and outdoor environment and thus a comprehensive study is required in each case. This chapter is devoted to provide basic understanding of acoustics waves and their properties and characteristics. Section 2.1 gives a brief introduction to acoustic waves and discuss various terminologies that are used in acoustics. Indoor acoustics are discussed in Section 2.2 and Section 2.3 provides basics about outdoor acoustics. Finally we conclude the chapter in Section 2.4

### 2.1 Acoustics Basics and Terminologies

Sound is a wave and a wave is a disturbance that propagates through a medium. There are two basic types of waves: longitudinal waves, and transverse waves. Longitudinal waves are waves in which the particle motion in the medium is in
the same direction as the wave is traveling, while transverse waves are waves in which the direction of motion of particles in the medium is normal to the direction of wave.

Acoustic waves (which are longitudinal) are generally pressure variation occurring in the medium due to some vibrating bodies. The total pressure at a point is given by

$$
\begin{equation*}
p_{T}(x, t)=p_{0}(x, t)+p_{1}(x, t) \tag{2.1}
\end{equation*}
$$

where $p_{0}$ represents the ambient pressure of the fluid and $p_{1}$ represents the pressure fluctuation caused by the acoustic field. The types of sounds we encounter cause pressure fluctuations in the range of $10^{-3}-10 P a[4]$.

Another terminology called acoustic intensity $I$ is also used to describe the sound wave energy and it is given by

$$
\begin{equation*}
I=\frac{d P}{d A} \tag{2.2}
\end{equation*}
$$

where $d P$ is the portion of the acoustic power that interacts with the area $d A$ of the detector oriented perpendicular to the direction of the oncoming acoustic wave. The units of acoustic intensity are watts per square meter $\left(W / m^{2}\right)$.

The human ear can generally perceive sound pressures over the range from about $20 \mu P a$ up to about $200 P a$ [4]. Often acoustic intensity is measured with
respective to a reference value as a ratio called the Sound Intensity Level (SIL)

$$
\begin{equation*}
S I L(d B)=10 \log \frac{I}{I_{r e f}} \tag{2.3}
\end{equation*}
$$

where $I$ is the intensity of the sound wave and $I_{r e f}$ is a reference intensity. For the intensity of a sound wave in air, the reference intensity is defined to be $I_{\text {ref }}=$ $10^{-12} \mathrm{~W} / \mathrm{m}^{2}$. Another terminology called Sound Pressure Level (SPL) is also widely used and is defined as

$$
\begin{equation*}
S P L(d B)=20 \log \frac{p}{p_{\text {reff }}} \tag{2.4}
\end{equation*}
$$

where $p$ is the acoustic pressure and $p_{\text {ref }}$ is a reference pressure. For sound in air, the reference pressure is defined as $20 \mu P a$.

Sound waves can also be represented by a sinusoidal equation as shown in Fig. 2.1, e.g.

$$
\begin{equation*}
y(x)=A \sin (k x+\phi), \tag{2.5}
\end{equation*}
$$

where $A$ is the amplitude of wave (i. e., the particle displacement) in the $y$ direction and $k=2 \pi / \lambda$ represents a scaling factor called the wave number. The term $\phi$ is known as the phase shift because it causes a shifting of the wave profile along the $x$-axis (forward for a positive phase shift and backward for a negative phase shift). The $v$ in Fig. 2.1 represents the velocity of the wave in the medium.


Figure 2.1: A Basic Sine Wave

### 2.1.1 Properties of Waves

## Acoustic Impedance

Every medium has an impedance which causes waves to attenuate. For acoustic waves, the impedance $Z$ is defined as the ratio of sound pressure to particle velocity. The unit for impedance is the Rayl, named in honor of Lord Rayleigh. 1 Rayl $=1 \mathrm{~Pa} \mathrm{~s} / \mathrm{m}$. This impedance of the medium is also called the characteristic impedance and usually denoted by $Z_{0}$. In air, the characteristic impedance near room temperature is about, 410 Rayl [4].

Acoustic impedances of media give us a measure of how much energy of a
wave is transmitted into the medium when it travels from one medium to another. When particle velocity and pressure are continuous across the interface between the two media, then the percentage of the energy that is reflected back into the medium is given by

$$
\begin{equation*}
\Gamma=\left(\frac{Z_{2}-Z_{1}}{Z_{2}+Z_{1}}\right)^{2} \tag{2.6}
\end{equation*}
$$

where $Z_{1}$ and $Z_{2}$ are the impedances of the two media and $\Gamma$ is called the reflection coefficient. The fraction of the energy transmitted into the second medium is given by the Transmission Coefficient: $\tau=1-\Gamma$ because $100 \%$ of the energy must be divided between $\tau$ and $\Gamma$.

## Refraction

Refraction is a change of the direction of wave propagation as the wave passes from one medium into another across an interface. Snell's law determines the amount of energy in the reflected and transmitted (refracted) waves. All natural waves obey Snell's law. For acoustic waves the proper form of Snell's law is:

$$
\begin{equation*}
\frac{\sin \left(\theta_{1}\right)}{v_{1}}=\frac{\sin \left(\theta_{2}\right)}{v_{2}} \tag{2.7}
\end{equation*}
$$

where $v_{1}$ is the wave velocity in medium 1 and $v_{2}$ is the wave velocity in medium $2, \theta_{1}$ is the angle that incident wave makes with the normal to boundary between two media in medium one and $\theta_{2}$ is the angle which the transmitted wave makes with the normal to the same boundary in the second medium.

## Reflection

Reflection occurs when a wave travels from one medium into another. If the acoustic impedance of the two media is different, then part of the wave is reflected and some part is transmitted into the medium depending on the acoustic impedances of both media.

## Interference

Interference is a phenomenon that occurs when two (or more) waves add together. Consider two sinusoidal acoustic waves with slightly different frequencies and equal amplitudes that arrive at the same point in space, then using supersposition principle the total pressure in the medium is

$$
\begin{align*}
p_{T}(t) & =A\left[\cos \left(\omega_{1} t\right)+\cos \left(\omega_{2} t\right)\right]  \tag{2.8}\\
& =2 A \cos \left(\frac{\left(\omega_{1}-\omega_{2}\right)}{2} t\right) \cos \left(\frac{\left(\omega_{1}+\omega_{2}\right)}{2} t\right) \tag{2.9}
\end{align*}
$$

Due to the slight difference in frequencies the two waves can be in phase, causing constructive interference and reinforcing one another. Over some period of time, the frequency difference causes the two waves to go out of phase, causing destructive interference (when $\omega_{1} t$ eventually leads $\omega_{2} t$ by $180^{\circ}$ ). The amplitude of the combination will rise and fall in a periodic fashion. This phenomenon is known as the beating of the two waves.

### 2.2 Indoor Acoustics

Walls of a room reflect sound waves which causes the phenomenon of reflection and room resonance. When multiple echoes in a room combine they produce a phenomenon known as reverberation. Indoor applications (as in our application) should take into consideration these important phenomena to accurately extract the desired information from the composite signal captured at a sensor.

### 2.2.1 Sound Absorption and Reverberation

Absorption is useful for reducing echo within a room. The absorption coefficient $\alpha$ is used to measure the amount of absorption that a material incurs. The Absorption coefficient is defined as the ratio of absorbed to incident energy. Absorption coefficients vary with frequency.

Reverberation is described by a parameter known as the reverberation time (denoted as $R T_{60}$ )[4]. Physically, $R T_{60}$ is the time (in seconds) that it takes for a sound source to reduce in sound pressure level (within a room) by a factor of 60 dB after that sound source has been silenced. Mathematically, $R T_{60}$ is given by Sabin's equation:

$$
\begin{equation*}
R T_{60}=0.161 \frac{V}{A} \tag{2.10}
\end{equation*}
$$

where $V$ is the room volume in cubic meters and $A$ is the total absorption of the room's surfaces in metric Sabins. Sabin is the unit of total absorption and one Sabin is defined as the total absorption provided by a one square foot piece of material having an absorption coefficient of $1[4] . R T_{60}$ can be controlled by i)
changing the room size and by ii) changing the absorption properties of the walls.
Another closely related terminology used to describe reverberation is Early Decay Time (EDT) which is actually the time taken by the sound level to drop from 0 dB to $-10 \mathrm{~dB}[4]$ and is given by

$$
\begin{equation*}
E D T=\frac{60 d B}{A(0 \rightarrow-10) d B / S e c} \tag{2.11}
\end{equation*}
$$

where $A$ represents the attenuation rate of the acoustic signal when it decreases from 0 dB to -10 dB sound pressure level.

### 2.2.2 Effects of Room Shapes, and Sound Insulation

Room shapes play an important role in the behavior of acoustic waves inside the room. Different surface structures are used to enhance sound quality inside a hall. Convex surfaces facilitate to diffuse the sound evenly throughout the audience. Concave reflective surfaces focus sound in certain areas and defocus sound from others, causing hot spots where sound is concentrated and dead spots where sound cannot be heard.

The Transmission Coefficient is the ratio of the transmitted to incident sound energy when sound waves encounter a partition or a wall. It is denoted by $\tau$ and ranges from 0 to 1 . A transmission coefficient of 1 implies that all of the sound energy is transmitted through a partition and 0 means complete reflection.

The Transmission Loss is used to describe the sound insulation, measured in
dB and based on transmission coefficient

$$
\begin{equation*}
T L=10 \log \left(\frac{1}{\tau}\right) \tag{2.12}
\end{equation*}
$$

The transmission loss can be loosely defined as the amount of sound reduced by a partition between a sound source and a listener. The complete sound reduction of a partition between two rooms also takes into account the absorptive characteristics of the listener's room, as follows:

$$
\begin{equation*}
S P L_{S}-S P L_{L}=T L+10 \log \left(\frac{A_{L}}{S}\right) \tag{2.13}
\end{equation*}
$$

where $S P L_{S}$ is the average sound pressure level in the room enclosing the sound source, $S P L_{L}$ is the average sound pressure level in the adjacent listener's room, $A_{L}$ is the total absorption in the listener's room, $T_{L}$ is the transmission loss of the partition between the two rooms, and $S$ is the surface area of the partition between the two rooms.

### 2.3 Outdoor Acoustics

Most of the outdoor sound experimentations conducted in 16th and 17th century were concerned about sound speed measurement [1][2]. Besides from interests in prediction and control of noise arising from land and air transport, outdoor acoustics has continued to have extensive military applications in source acquisition, ranging and identification [7]. There are several important parameters regarding
the outdoor acoustic signals which are discussed next.

### 2.3.1 Spreading Losses

When waves travel, their wavefronts spread with distance. The intensity $I$ at a distance $r \mathrm{~m}$ from an isotropic source, which radiates equally in all direction, is given by [2]

$$
\begin{equation*}
I=\frac{P}{4 \pi r^{2}} \tag{2.14}
\end{equation*}
$$

where $P$ is the power of a spherical wavefront of radius $r$. The relationship between sound pressure level $L_{p}$ and sound power $L_{W}$ may be written as

$$
\begin{equation*}
L_{P}=L_{W}-20 \log (r)-11 d B \tag{2.15}
\end{equation*}
$$

For an omnidirectional point sound source, (2.15) shows a reduction of $20 \log 2 d B$, i.e., $6 d B$ per distance doubling in all directions. For a directional source, (2.15) is modified by including the directivity index $(D I)$.

$$
\begin{equation*}
L_{P}=L_{W}+D I-20 \log (r)-11 d B \tag{2.16}
\end{equation*}
$$

The DI is $10 \log (D F) d B$ where $D F$ is the directivity factor given by the ratio of the actual intensity in a given direction to the intensity of an omnidirectional source of the same power output. The directivity factor for a point source on a perfectly reflecting plane is 2 and the directivity index is thus $3 d B$.

### 2.3.2 Atmospheric Absorption

A proportion of sound energy is converted to heat as it travels through the air. There are heat conduction, shear viscosity and molecular relaxation losses [5]. For a plane wave, the pressure $p$ at distance $x$ from a position where the pressure is $p_{0}$ is given by

$$
\begin{equation*}
p=p_{0} e^{-\alpha x / 2} \tag{2.17}
\end{equation*}
$$

The attenuation coefficient $\alpha$ can be calculated using (2.18) to (2.20)

$$
\begin{align*}
\alpha=f^{2}\left[\left(\frac{1.84 \times 10^{-11}}{\left(\frac{T_{0}}{T}\right) 1 / 2 \frac{p_{s}}{p_{0}}}\right)+\left(\frac{T_{0}}{T}\right)^{2.5}\right. & \left(\frac{0.106080 e^{-3352 / T} f_{r, N}}{f^{2}+f_{r, N}^{2}}\right) \\
& \left.+\frac{\left(0.01278 e^{-2239.1 / T} f_{r, O}\right)}{f^{2}+f_{r, O}^{2}} \cdot \frac{N_{P}}{m \cdot a t m}\right] \tag{2.18}
\end{align*}
$$

where $f$ is the frequency, $T$ is the absolute temperature of the atmosphere in degrees Kelvin, $T_{0}=293.15 \mathrm{~K}$ is the reference value of $T\left(20^{\circ} \mathrm{C}\right)$, and $f_{r, N}$ and $f_{r, O}$ are relaxation frequencies associated with the vibration of nitrogen and oxygen molecules respectively and are given by:

$$
\begin{align*}
f_{r, N} & =\frac{p_{s}}{P_{s 0}}\left(\frac{T_{0}}{T}\right)^{1 / 2}\left(9+280 H e^{-4.17\left[\left(\frac{T_{0}}{T}\right)^{1 / s}-1\right]}\right)  \tag{2.19}\\
f_{r, O} & =\frac{p_{s}}{P_{s 0}}\left(24.0+4.04 \times 10^{4} H \frac{0.02+H}{0.391+H}\right) \tag{2.20}
\end{align*}
$$

where $H$ is the percentage molar concentration of water vapor in the atmosphere $=\rho_{s a t} r_{h} p_{0} / p_{s}, r_{h}$ is the relative humidity (\%); $p_{s}$ is the local atmospheric pressure and $p_{0}$ is the reference atmospheric pressure $\left(1 \mathrm{~atm}=1.01325 \times 10^{5} \mathrm{~Pa}\right) ; \rho_{\text {sat }}=$
$10^{C_{\text {sat }}}$, where $C_{\text {sat }}=-6.8346\left(T_{0} / T\right)^{1.261}+4.6151$. These formulae give estimates of the absorption of pure tones to an accuracy of $\pm 10 \%$ for $0.05<H<5,253<$ $T<323, p_{0}<200 k P a$. Outdoor air absorption varies through the day and the year.

### 2.3.3 Ground Effects

Reflection from the ground causes interference with waves above the ground and leads to so called ground effects. A widely used model that is used to investigate the properties of outdoor acoustics makes use of a single parameter, the flow resistivity $\sigma_{e}$, to characterize the ground. Flow resistivity is a terminology that describes the behavior of air when it moves in and out of ground and its unit is Pasmer . The propagation constant $k$ and normalized impedance $Z$ are given, in terms of $\sigma_{e}$, as follows

$$
\begin{align*}
\frac{k}{k_{1}} & =\left[1+0.0978\left(\frac{f}{\sigma_{e}}\right)^{-0.700}-j 0.189\left(\frac{f}{\sigma_{e}}\right)^{-0.595}\right]  \tag{2.21}\\
Z & =\frac{\rho_{1} c_{1}}{\rho c}=1+0.0571\left(\frac{f}{\sigma_{e}}\right)^{-0.754}-j 0.087\left(\frac{f}{\sigma_{e}}\right)^{-0.732} \tag{2.22}
\end{align*}
$$

where $k_{1}$ is the propagation constant within the surface layer, $k$ is the propagation constant in the air, $\rho_{1}, c_{1}$ are the pressure density and sound velocity within the surface layer, $f$ is the frequency of the sound wave and $\rho, c$ are the pressure density and sound velocity in the air.

### 2.3.4 Wind and Temperature Effects on Outdoor Sound

Both wind speed and temperature affect the speed of sound in a region. The speed of sound changes with atmosphere temperature which due to the fact that gases expand and contract with changing temperature. Wind speed directly adds or subtracts from sound speed depending on the direction of wind flow and acoustic waves.

In general, the relationship between the speed of sound profile $c(z)$, temperature profile $T(z)$ and wind speed profile $u(z)$ in the direction of sound propagation $\vec{z}$ is given by

$$
\begin{equation*}
c(z)=c(0) \sqrt{\frac{T(z)+273.15}{273.15}}+u(z) \tag{2.23}
\end{equation*}
$$

where $T$ is in ${ }^{\circ} C$ and $u, c$ are in $m / s$.

### 2.4 Conclusion

Understanding sound waves behavior in the indoor and outdoor environment is essential for acoustic applications such as acoustic source localization. Indoor acoustic applications require an in-depth understanding of sound waves inside a building, room or hall. In this chapter, the characteristics and properties of sound waves inside a building were discussed. The effects of reflections from the walls of the room and reverberations were presented. The effects of room shapes and designs on indoor acoustic waves were also discussed.

In addition, various important outdoor properties like ground effects, spread-
ing losses, and wind and temperature effects on the acoustic signals were discussed.
Atmospheric absorption was also investigated and relevant mathematical expressions were presented.

## CHAPTER 3

# LITERATURE REVIEW ON 

## ACOUSTIC SOURCE

## LOCALIZATION

Localization of acoustic sources uses the same methods and algorithms which are used for radio waves, optical, ultra-wideband (UWB) or any other waves. Certain parameters of the signal like Received Signal Strength (RSS), Time of Arrival (TOA), Angle of Arrival (AOA) or Time Difference of Arrival (TDOA) are used to extract information about the source emanating the signal [3]. This chapter discusses methods of acoustic source localization. Section 3.1 introduces the chapter followed by Section 3.2 which explains the concepts of AOA and TDOA. Section 3.3 provides the mathematical modeling of signals to be processed and Section 3.4 discusses various Time Delay Estimation (TDE) techniques followed by the discussion of Compressive Sensing (CS) based localization schemes in Section 3.5.2.

The chapter is concluded in Section 3.6.

### 3.1 Introduction

In this chapter previous work done by several researchers in the area of acoustic source localization is presented. Different localization techniques will be described with minimal mathematical details to show the concepts. The localization techniques ultimately depend on time delay estimation (TDE) techniques. Almost all the localization techniques require calculating time delays when the sound waves travel from one sensor to another. Thus a detailed discussion on TDE techniques will also be included in this chapter.

### 3.2 Concept of Direction of Arrival (DOA) and Time Difference of Arrival (TDOA)

Two important localization methods that are widely used in literature are Direction of Arrival (DOA) and Time Difference of Arrival (TDOA). The details of both of the methods follow.

### 3.2.1 DOA Technique

Consider Fig. 3.1 in which a sensor array has been shown. The array consists of three sensors which are placed in the far-field of a radiating source. Since the array is in the far-field, the waves coming from the source can be considered as
plane waves.
The normal to the wavefront makes an angle $\theta$ with the axis along which the sensors are placed. The signals received at all sensors are delayed or advanced versions of the signal received at a reference sensor. In Fig. 3.1, the reference sensor is $r_{1}$. The sensors are $d$ distance apart from each sensor on its sides. Now if the signal is received at sensor 1 at $t_{0}$ time, same signal would have already reached at sensor 2 at $\left(t_{0}-d \cos \theta\right)$ time [8]. Therefore, the time difference (or time delay) between the two sensors is given by

$$
\begin{equation*}
\tau_{21}=\frac{d \cos (\theta)}{c} \tag{3.1}
\end{equation*}
$$

where $c$ is the sound velocity in air. If $\tau_{21}$ is known and $\theta$ ranges from $0^{\circ}$ to $180^{\circ}$ then $\theta$ can be uniquely determined [8]. To find the angle of arrival $\theta$ we need to find the time difference $\tau_{21}$. This time difference is also known as time-difference-of-arrival (TDOA) and the process of finding angle $\theta$ is known as Direction of Arrival (DOA) estimation (in some references it is also known as Angle of Arrival, AOA) [3]).

To formally develop a mathematical model we proceed as follows based on methods described in [9].

Suppose there are $M$ sensors placed in the far field of a wideband source. Let $\overrightarrow{\mathbf{r}_{i}}$ denotes the location of the $i$ th sensor. $\overrightarrow{\mathbf{r}_{i}}$ is 3 -dimensional $\left(\overrightarrow{\mathbf{r}_{i}}=\left[x_{i}, y_{i}, z_{i}\right]\right)$ for a 3D array or 2-dimensional $\left(\overrightarrow{\mathbf{r}_{i}}=\left[x_{i}, y_{i}\right]\right)$ for a 2D array. The azimuth and elevation angle of the source are denoted by $\phi$ and $\theta$ respectively. If $\tau_{j 1}$ represents


Figure 3.1: Sensor array in the far-field of a radiating source
the TDOA between the reference sensor 1 and any sensor $j$ then we can define a vector as

$$
\begin{equation*}
\vec{\tau}=\left[\tau_{21}, \tau_{31}, \ldots, \tau_{M 1}\right]^{T} ; \quad \tau_{j 1}=\tau_{j}-\tau_{1} \tag{3.2}
\end{equation*}
$$

and accordingly we can define the DOA vector for the far field signal as

$$
\overrightarrow{\mathbf{k}}=\left[\begin{array}{c}
k_{x}  \tag{3.3}\\
k_{y} \\
k_{z}
\end{array}\right]=\left[\begin{array}{c}
\sin (\theta) \cos (\phi) \\
\sin (\theta) \sin (\phi) \\
\cos (\theta)
\end{array}\right]
$$

Now from Fig. 3.1 we see the TDOA between sensor 1 and 2 is given by (3.1) which is actually the projection of distance $d$ between sensor 1 and 2 along the direction of the signal from the source divided by the sound speed. Generalizing
this concept we can write

$$
\vec{\tau}=-\frac{\mathbf{R} \overrightarrow{\mathbf{k}}}{c} ; \quad \mathbf{R}=\left[\begin{array}{c}
\vec{r}_{2}-\vec{r}_{1}  \tag{3.4}\\
\vdots \\
\vec{r}_{M}-\vec{r}_{1}
\end{array}\right]
$$

where $\mathbf{R}$ is the matrix whose rows are the distance difference between the reference sensor 1 and all other sensors. Thus if we know the $\vec{\tau}$ and we already know $c$ and $\mathbf{R}$ we can estimate $\overrightarrow{\mathbf{k}}$ using Least Squares (LS) as the system is over-determined for $M>3$ in 2D case and for $M>4$ in 3 D case. The LS solution for $\overrightarrow{\mathbf{k}}$ is given by [10]

$$
\begin{align*}
\overrightarrow{\mathbf{k}} & =\underset{\vec{k}}{\operatorname{ArgMin}}\left\{\left(\frac{\mathbf{R} \overrightarrow{\mathbf{k}}}{c}+\hat{\vec{\tau}}\right)^{T} \Lambda_{\tau}^{-1}\left(\frac{\mathbf{R} \overrightarrow{\mathbf{k}}}{c}+\hat{\vec{\tau}}\right)\right\}  \tag{3.5}\\
& =-c\left(\mathbf{R}^{T} \Lambda_{\tau}^{-1} \mathbf{R}\right) \mathbf{R}^{T} \Lambda_{\tau}^{-1} \hat{\vec{\tau}}=-c \mathbf{B} \hat{\vec{\tau}} \tag{3.6}
\end{align*}
$$

which is a simple multiplication between $c$, the delay vector and and a data independent matrix B. After estimating the DOA vector $\overrightarrow{\mathbf{k}}$ we can find $\phi$ and $\theta$ by expressing $\overrightarrow{\mathbf{k}}$ in Polar coordinates. For 2D case:

$$
\begin{equation*}
\hat{\phi}=\cos ^{-1}\left(\hat{k}_{x}\right) \tag{3.7}
\end{equation*}
$$

For 3D case [9]:

$$
\begin{align*}
& \hat{\phi}=\tan ^{-1}\left(\frac{\hat{k}_{y}}{\hat{k}_{x}}\right)  \tag{3.8}\\
& \hat{\theta}=\cos ^{-1}\left(\hat{k}_{z}\right)=\cos ^{-1}\left(\left(1-\left(\hat{k}_{x}^{2}+\hat{k}_{y}^{2}\right)\right)^{1 / 2}\right) \tag{3.9}
\end{align*}
$$

For the 3D case (3.3) produces three nonlinear equations with two unknowns which is again a LS problem and its solution is given by [9]

$$
\begin{equation*}
(\hat{\phi}, \hat{\theta})=\underset{\hat{\phi}, \hat{\theta}}{\operatorname{ArgMin}}\left\{\left(\hat{\overrightarrow{\mathbf{k}}}-\overrightarrow{\mathbf{k}}(\hat{\phi}, \hat{\theta})^{T}\right) \Lambda_{k}^{-1}(\hat{\overrightarrow{\mathbf{k}}}-\overrightarrow{\mathbf{k}}(\hat{\phi}, \hat{\theta}))\right\} \tag{3.10}
\end{equation*}
$$

where $\Lambda_{k}^{-1}$ is the covariance matrix of $\hat{\overrightarrow{\mathbf{k}}}$. Berdugo et al [9] propose another suboptimal close-form estimate given by

$$
\begin{align*}
& \hat{\phi}=\tan ^{-1}\left(\frac{\hat{k}_{y}}{\hat{k}_{x}}\right),  \tag{3.11}\\
& \hat{\theta}=\tan ^{-1}\left(\frac{\left(\hat{k}_{x}^{2}+\hat{k}_{y}^{2}\right)^{1 / 2}}{\hat{k}_{z}}\right) \tag{3.12}
\end{align*}
$$

which they have shown to be asymptotically efficient. Moreover, they claim that following certain geometrical constraints for the sensor arrangements, the closed form in (3.11) and (3.12) achieves the Cramér-Rao Lower Bound (CRLB).

### 3.2.2 TDOA Technique

Fig. 3.2 displays a scenario where there are three sensors (mics) placed on the vertices of an equilateral triangle. Mic 1 is taken as the reference and is placed at the origin of the Coordinate system. The locations of microphone 1, 2, and 3 are $\left(x_{1}, y_{1}\right),\left(x_{2}, y_{2}\right),\left(x_{3}, y_{3}\right)$ respectively. The unknown source location is $(x, y)$. The TDOA between references $i$ and $j$ (i.e., $t_{i}-t_{j}$ ) may be used to obtain the distance difference, which may be written as

$$
\begin{align*}
d_{i j} & =d_{i}-d_{j}=c\left(t_{i}-t_{0}\right)-c\left(t_{j}-t_{0}\right)  \tag{3.13}\\
& =c\left(t_{i}-t_{j}\right), \quad i=1,2,3, \quad j=1,2,3, \quad i \neq j \tag{3.14}
\end{align*}
$$

where $t_{0}$ is the time of flight of wave from the source to the reference sensor. $\left(t_{i}-t_{j}\right)$ corresponds to the TDOA between microphone $i$ and $j$. This TDOA can be found by using TDE techniques discussed in Section 3.4. From (3.14)

$$
\begin{equation*}
d_{i}=d_{i j}+d_{j} \tag{3.15}
\end{equation*}
$$

Applying (3.15) to microphones 1 and 2 and squaring both sides,

$$
\begin{align*}
d_{2}^{2} & =\left(d_{21}+d_{1}\right)^{2}=\left(x_{2}-x\right)^{2}+\left(y_{2}-y\right)^{2}  \tag{3.16}\\
& =x_{2}^{2}-2 x_{2} x+y_{2}^{2}-2 y_{2} y+d_{1}^{2} \tag{3.17}
\end{align*}
$$



Figure 3.2: Sensor array in the far-field of a radiating source

Rearranging (3.17), we get

$$
\begin{equation*}
\left(d_{21}^{2}-x_{2}^{2}-y_{2}^{2}\right)+2 d_{21} d_{1}=-2 x_{2} x-2 y_{2} y \tag{3.18}
\end{equation*}
$$

Similarly for mic 1 and 3, we can derive,

$$
\begin{equation*}
\left(d_{31}^{2}-x_{3}^{2}-y_{3}^{2}\right)+2 d_{31} d_{1}=-2 x_{3} x-2 y_{3} y \tag{3.19}
\end{equation*}
$$

Equations (3.18) and (3.19) correspond to hyperbollas which represent the possible source locations corresponding to $\tau_{21}$ and $\tau_{31}$ respectively. We can solve
these nonlinear equations through a computer program e.g. MATLAB to find the actual source locations. Thus the main task is to estimate the correct TDOA and then we can estimate the source locations easily. Note that both AOA and TDOA methods require the TDOAs among the sensors, the difference is in the way of estimating source location from these TDOAs.

We can generalize this approach for $N$ sensors for the 3D case. Suppose there is an array consisting of $N+1$ sensors placed in a three dimensional space. Let $a_{n}$ be the location of the $n$th sensor (a $3 \times 1$ vector, $\vec{a}_{n}=x \vec{a}_{x}+y \vec{a}_{y}+z \vec{a}_{z}$ ). For simplicity we assume that one of the sensors is located at origin and we use this sensor as the reference for the remaining sensors. Let $\mathbf{x}$ denote the source location and $d_{n}$ denote the distance corresponding to the TDOA between sensor $n$ and the reference sensor, then

$$
\begin{equation*}
d_{n}=\left\|a_{n}-\mathbf{x}\right\|-\|\mathbf{x}\|, \quad n=1, \cdots, N \tag{3.20}
\end{equation*}
$$

where $\|\cdot\|$ denotes the Euclidean norm. Equation (3.20) can be written as [11]

$$
\begin{equation*}
\left\|a_{n}-\mathbf{x}\right\|^{2}=\left\|d_{n}+\mathbf{x}\right\|^{2} \tag{3.21}
\end{equation*}
$$

which upon simplifying produces the following system of equations in the unknown x,

$$
\begin{equation*}
d_{n}\|\mathbf{x}\|+a_{n}^{T} \mathbf{x}=b_{n}, n=1, \cdots, N \tag{3.22}
\end{equation*}
$$

where

$$
\begin{equation*}
b_{n}=\frac{\left\|a_{n}\right\|^{2}-d_{n}^{2}}{2} \tag{3.23}
\end{equation*}
$$

If we define the following as

$$
y=\left[\begin{array}{c}
\|\mathbf{x}\|  \tag{3.24}\\
\mathbf{x}
\end{array}\right] ; \quad \phi=\left[\begin{array}{cc}
d_{1} & a_{1}^{T} \\
\vdots & \vdots \\
d_{N} & a_{N}^{T}
\end{array}\right] ; \quad b=\left[\begin{array}{c}
b_{1} \\
\vdots \\
b_{N}
\end{array}\right]
$$

then (3.22) can be written as

$$
\begin{equation*}
\boldsymbol{\Phi} y=b \tag{3.25}
\end{equation*}
$$

We will be using more than four sensors to improve the TDOA uncertainty, in which case, (3.25) becomes over-determined and can be solved using the LS method. The LS solution of (3.25) is given by

$$
\begin{equation*}
\hat{y}=\left(\boldsymbol{\Phi}^{T} \boldsymbol{\Phi}\right)^{-1} \boldsymbol{\Phi}^{T} b \tag{3.26}
\end{equation*}
$$

Then the corresponding LS estimate of source location is given by

$$
\hat{x}=\left[\begin{array}{ll}
\mathbf{0} & \mathbf{I} \tag{3.27}
\end{array}\right] \hat{y}
$$

Note that the last three columns of $\boldsymbol{\Phi}$ consist of the coordinates of the sensors locations. If all the sensors are in a plane, then $\mathbf{\Phi}$ will become singular (one column will be zero) or almost singular and the solution to (3.26) will become
impossible. To avoid such a situation we arrange the sensors in such a way that the resulting array covers the three dimensions. We discuss the geometries in detail in Chapter 5.

### 3.3 Signal Models

Depending on the environment we may have different signal models. The possible signal models, in our case, are given below.

### 3.3.1 Single Source Free Field Model

Suppose there is only one source radiating sound waves in an anechoic environment (open or outdoor environment). An array of $N$ microphones is placed in that environment. If we choose microphone 1 as the reference, the signal received at the $n$th microphone can be written as [8][12]

$$
\begin{align*}
y_{n}(k) & =\alpha_{n} s\left(k-t-\tau_{n 1}\right)+v_{n}(k)  \tag{3.28}\\
& =\alpha_{n} s\left(k-t-\mathcal{F}_{n}(\tau)\right)+v_{n}(k)  \tag{3.29}\\
& =x_{n}(k)+v_{n}(k), n=1,2, \ldots, N \tag{3.30}
\end{align*}
$$

where $\alpha_{n}(n=1,2, \ldots, N)$ are the attenuation factors, $s(k)$ is the unknown source signal, $t$ is the propagation time from source to reference mic $1, v_{n}(k)$ is an additive noise signal at the $n$th sensor (assumed to be uncorrelated with the source signal and other mics' noise), and $\tau_{n 1}=\mathcal{F}_{n}(\tau)$ is the TDOA between sensor 1 and
$n$ and $\tau$ is the TDOA between sensors 1 and 2 . For $n=3, \ldots, N$ the function $\mathcal{F}_{n}$ depends on $\tau$ as well as on the geometry of the array.

### 3.3.2 Single Source Reverberant Model

Real environments are not free from objects, there are always objects causing reflections and reverberations (indoor case). Consider there is a single source in a reverberant model. This scenario can be modeled as single-input multiple-output (SIMO) system. The $n$th sensor signal at time $k$ can be given by [8][12]

$$
\begin{align*}
y_{n}(k) & =g_{n} * s(k)+v_{n}(k),  \tag{3.31}\\
& =x_{n}(k)+v_{n}(k), n=1,2, \ldots, N \tag{3.32}
\end{align*}
$$

where $g_{n}$ is the channel impulse response from the source to mic $n$. Equation (3.31) can also be written in a matrix form as

$$
\begin{equation*}
\mathbf{y}_{n}=\mathbf{G}_{n} s(k)+\mathbf{v}_{n}(k), n=1,2, \ldots, N \tag{3.33}
\end{equation*}
$$

where

$$
\begin{align*}
\mathbf{y}_{n}(k) & =\left[\begin{array}{ccccc}
y_{n}(k) & y_{n}(k-1) & \ldots & y_{n}(k-L+1)
\end{array}\right]^{T},  \tag{3.34}\\
\mathbf{G} & =\left[\begin{array}{ccccc}
g_{n, 0} & \ldots & g_{n, L-1} & \ldots & 0 \\
\vdots & \ddots & \ddots & \ddots & \vdots \\
0 & \ldots & g_{n, 0} & \ldots & g_{n, L-1}
\end{array}\right] \tag{3.35}
\end{align*}
$$

$$
\begin{align*}
s(k) & =\left[\begin{array}{lllll}
s(k) & s(k-1) & \ldots & s(k-L+1) & \ldots \\
s(k-2 L+2)
\end{array}\right]^{T}  \tag{3.36}\\
\mathbf{v}_{n}(k) & =\left[\begin{array}{lll}
v_{n}(k) & \ldots & v_{n}(k-L+1)
\end{array}\right]^{T} \tag{3.37}
\end{align*}
$$

and $L$ is the length of the longest channel impulse response of the SIMO system. The TDOA $\tau$ is an implicit or hidden parameter in this model.

### 3.4 Time Delay Estimation (TDE) Techniques

As we discussed earlier, the main task that every position localization technique needs to perform is to estimate the TDOA among the sensors. There are various algorithms which are used for this purpose. Every algorithm and technique has its own benefits, drawbacks, scenarios, and applications. We will discuss the most widely used TDE techniques in the following subsections.

### 3.4.1 Generalized Cross-Correlation Techniques

The generalized cross-correlation (GCC) method [8][12][13] is the most widely used method for estimating time delay. GCC assumes the free field model and considers only two microphones. TDOA is found by choosing a delay that maximizes the cross-correlation function of the two mics' signals.

$$
\begin{equation*}
\hat{\tau}^{G C C}=\arg \max _{\tau} r_{y_{1} y_{2}}^{G C C}(p) \tag{3.38}
\end{equation*}
$$

where

$$
\begin{align*}
r_{y_{1} y_{2}}^{G C C}(p) & =F^{-1}\left[\psi_{y_{1} y_{2}}(f)\right]  \tag{3.39}\\
& =\int_{-\infty}^{\infty} \psi_{y_{1} y_{2}}(f) e^{j 2 \pi f p} d f=\int_{-\infty}^{\infty} \vartheta(f) \phi_{y_{1} y_{2}}(f) e^{j 2 \pi f p} d f \tag{3.40}
\end{align*}
$$

is the GCC function, and $F^{-1}[\cdot]$ is the inverse discrete-time Fourier transform (IDTFT),

$$
\begin{equation*}
\phi_{y_{1} y_{2}}(f)=E\left[Y_{1}(f) Y_{2}^{*}(f)\right] \tag{3.41}
\end{equation*}
$$

is the cross-spectrum with $Y_{n}(f)=\sum_{k} y_{n}(k) e^{-j 2 \pi f k}, n=1,2, \vartheta(f)$ is a frequencydomain weighting function, and

$$
\begin{equation*}
\psi_{y_{1} y_{2}}(f)=\vartheta(f) \phi_{y_{1} y_{2}}(f) \tag{3.42}
\end{equation*}
$$

is the generalized cross-spectrum and $E[\cdot]$ represents the expectation operation.

## Classical Cross-Correlation

By setting $\vartheta(f)=1$, the GCC expression simplifies to simple cross-correlation function [8][12][13]. The free-field signal model was given in (3.28). Taking its Discrete Fourier Transform (DFT), we get

$$
\begin{equation*}
Y_{n}(f)=\alpha_{n} S(f) e^{-j 2 \pi f\left[t-\mathcal{F}_{n}(t)\right]}+V_{n}(f), n=1,2 . \tag{3.43}
\end{equation*}
$$

Substituting (3.43) into (3.42) and assuming that all noise signals are uncorrelated with each other and with source signals; we get expression for the cross-correlation function

$$
\begin{equation*}
\psi_{y_{1} y_{2}}^{C C}(f)=\alpha_{1} \alpha_{2} e^{-j 2 \pi f \tau} E\left[|S(f)|^{2}\right] \tag{3.44}
\end{equation*}
$$

which is dependent on the source signal.

## Smoothed Coherent Transform

Often the microphone signal is smoothed out to reduce fluctuation effects on TDOA by using

$$
\begin{equation*}
\vartheta(f)=\frac{1}{\sqrt{E\left[\left|Y_{1}(f)\right|^{2}\right] E\left[\left|Y_{2}(f)\right|^{2}\right]}} \tag{3.45}
\end{equation*}
$$

which gives the so-called Smoothed COherence Transform (SCOT) [8][12][13]. Substituting (3.45) and (3.43) into (3.42), we get the expression for SCOT crossspectrum

$$
\begin{align*}
\psi_{y_{1} y_{2}}^{S C O T}(f) & =\frac{\alpha_{1} \alpha_{2} e^{-j 2 \pi f \tau} E\left[|S(f)|^{2}\right]}{\sqrt{E\left[\left|Y_{1}(f)\right|^{2}\right] E\left[\left|Y_{2}(f)\right|^{2}\right]}}  \tag{3.46}\\
& =\frac{e^{-j 2 \pi f \tau}}{\sqrt{\left(1+\frac{1}{S N R_{1}(f)}\right) \cdot\left(1+\frac{1}{S N R_{2}(f)}\right)}} \tag{3.47}
\end{align*}
$$

where

$$
\begin{equation*}
S N R_{n}(f)=\frac{\alpha_{n}^{2} E\left[|S(f)|^{2}\right]}{E\left[\left|V_{n}(f)\right|^{2}\right]}, n=1,2 \tag{3.48}
\end{equation*}
$$

In case the SNRs are the same at both microphones, then

$$
\begin{equation*}
\psi_{y_{1} y_{2}}^{S C O T}(f)=\left[\frac{S N R(f)}{1+S N R(f)}\right] \cdot e^{-j 2 \pi f \tau} \tag{3.49}
\end{equation*}
$$

Equation (3.49) means that the SCOT performance depends on the SNR and so in return, the TDOA estimate will vary with SNR . With $S N R \gg 1$,

$$
\begin{equation*}
\psi_{y_{1} y_{2}}^{S C O T}(f) \approx e^{-j 2 \pi f \tau} \tag{3.50}
\end{equation*}
$$

Thus the SCOT produces good results when noise levels are quite low.

## The Phase Transform

If we set

$$
\begin{equation*}
\vartheta(f)=\frac{1}{\left|\phi_{y_{1} y_{2}}(f)\right|} \tag{3.51}
\end{equation*}
$$

in (3.40) we get the phase transform (PHAT) method which takes only phase of (3.40) in to consideration. The generalized cross-spectrum becomes

$$
\begin{equation*}
\psi_{y_{1} y_{2}}^{P H A T}(f)=e^{-j 2 \pi f \tau}, \tag{3.52}
\end{equation*}
$$

Substituting (3.52) in (3.40), we get the following GCC function:

$$
r_{y_{1} y_{2}}^{P H A T}(p)=\int_{-\infty}^{\infty} e^{j 2 \pi f(p-\tau)} d f=\left\{\begin{array}{rr}
\infty, & p=\tau  \tag{3.53}\\
0, & \text { otherwise }
\end{array}\right.
$$

### 3.4.2 Eigenvector-Based Techniques

These techniques take advantage of the usage of multiple microphones (more than 2) [8][12]. We assume the single-source free-field model in (3.28) with $N$ microphones. Further we assume that the array is in the far-field, all attenuation factors $\alpha_{n}=1$ and noise signals are mutually independent Gaussian random processes with the same variance. We will discuss two methods within this category.

## Narrowband MUSIC

Transforming (3.28) into frequency domain, we get [8][12]

$$
\begin{equation*}
Y_{n}(f)=X_{n}(f)+V_{n}(f)=S(f) e^{-j 2 \pi\left[t+\mathcal{F}_{n}(\tau)\right] f}+V_{n}(f) \tag{3.54}
\end{equation*}
$$

where $Y_{n}(f), X_{n}(f), V_{n}(f)$, and $S(f)$ are the DTFT of $y_{n}(k), x_{n}(k), v_{n}(k)$, and $s(k)$ respectively. We define a frequency-domain vector as:

$$
\mathbf{y}=\left[\begin{array}{llll}
Y_{1}(f) & Y_{2}(f) & \ldots & Y_{n}(f) \tag{3.55}
\end{array}\right]^{T}
$$

Substituting (3.54) into (3.55), we get

$$
\begin{align*}
\mathbf{y} & =\mathbf{x}+\mathbf{v}  \tag{3.56}\\
& =\varsigma(\tau) S(f) e^{-j 2 \pi f t}+\mathbf{v} \tag{3.57}
\end{align*}
$$

where

$$
\varsigma(\tau)=\left[\begin{array}{llll}
e^{-j 2 \pi \mathcal{F}_{1}(\tau) f} & e^{-j 2 \pi \mathcal{F}_{2}(\tau) f} & \ldots & e^{-j 2 \pi \mathcal{F}_{N}(\tau) f} \tag{3.58}
\end{array}\right]^{T}
$$

and $\mathbf{v}$ is defined similarl to $\mathbf{y}$. The output covariance matrix is given by

$$
\begin{equation*}
R_{y}=E\left(\mathbf{y y}^{H}\right)=R_{X}+\sigma_{v}^{2} I \tag{3.59}
\end{equation*}
$$

where

$$
\begin{equation*}
R_{X}=\sigma_{S}^{2} \varsigma(\tau) \varsigma^{H}(\tau) \tag{3.60}
\end{equation*}
$$

And $\sigma_{S}^{2}=E\left[|S(f)|^{2}\right]$ and $\sigma_{V}^{2}=E\left[\left|V_{1}(f)\right|^{2}\right]=\ldots=E\left[\left|V_{N}(f)\right|^{2}\right]$ are the signal and noise variances respectively. After performing eigenvalue decomposition of $R_{y}$, we obtain

$$
\begin{equation*}
\mathbf{R}_{\mathbf{Y}}=\mathbf{B} \boldsymbol{\Lambda} \mathbf{B}^{\mathbf{H}} \tag{3.61}
\end{equation*}
$$

where

$$
\begin{align*}
\boldsymbol{\Lambda} & =\operatorname{diag}\left[\begin{array}{llll}
\lambda_{Y, 1} & \lambda_{Y, 2} & \ldots & \lambda_{Y, N}
\end{array}\right]  \tag{3.62}\\
& =\operatorname{diag}\left[\begin{array}{lllll}
\lambda_{Y, 1}+\sigma_{v}^{2} & \sigma_{v}^{2} & \ldots & \sigma_{v}^{2}
\end{array}\right] \tag{3.63}
\end{align*}
$$

is a diagonal matrix consisting of the eigenvalues of $\mathbf{R}_{\mathbf{Y}}$,

$$
\mathbf{B}=\left[\begin{array}{llll}
b_{1} & b_{2} & \ldots & b_{N} \tag{3.64}
\end{array}\right],
$$

$\mathbf{b}_{\mathbf{n}}$ is the eigenvector associated with the eigenvalue $\lambda_{Y, n}$, and $\lambda_{Y, 1}$ is the only non-zero positive eigenvalue of $R_{Y}$. For $n \geq 2$

$$
\begin{equation*}
\mathbf{R}_{\mathbf{Y}} \mathbf{b}_{\mathbf{n}}=\left[\sigma_{s}^{2} \varsigma(\tau) \varsigma^{H}(\tau)+\sigma_{v}^{2} \mathbf{I}\right] \mathbf{b}_{\mathbf{n}} \tag{3.65}
\end{equation*}
$$

From (3.64) and (3.65), it is also found that

$$
\begin{equation*}
\sigma_{S}^{2} \varsigma(\tau) \varsigma^{H}(\tau) \mathbf{b}_{\mathbf{n}}=0 \tag{3.66}
\end{equation*}
$$

which is equivalent to

$$
\begin{equation*}
\varsigma^{H}(\tau) \mathbf{b}_{\mathbf{n}}=0 \tag{3.67}
\end{equation*}
$$

or

$$
\begin{equation*}
\mathbf{b}_{\mathbf{n}}{ }^{H} \varsigma(\tau)=0 \tag{3.68}
\end{equation*}
$$

It means that the eigenvectors associated with the $N-1$ lowest eigenvalues of $\mathbf{R}_{\mathbf{Y}}$ are orthogonal to the vector corresponding to the actual TDOA. The following cost function can be used to find TDOA $\tau$. The function $p=\tau$ maximizes this cost function:

$$
\begin{equation*}
J_{M U S I C}(p)=\frac{1}{\sum_{n=2}^{N}\left|b_{n}^{H} \varsigma(p)\right|^{2}} \tag{3.69}
\end{equation*}
$$

where MUSIC stands for MUltiple SIgnal Classification.

## Broadband MUSIC

Since the speech signal is non-stationary thus the narrowband MUSIC algorithm does not produce good results. One straight forward solution to this problem is to change cost function of (3.69) such that it covers all the sound frequency range. But this will degrade the delay estimation performance because the peak will not be well-defined due to a broadband signal. Another approach uses spatial correlation concepts and this is discussed in detail in [8].

### 3.5 Localization Schemes

### 3.5.1 Conventional Localization Schemes

In [9], a new algorithm has been developed for direction finding of the incoming acoustic wave. The algorithm finds the azimuth and elevation angles directly from the estimated time delays between the array elements. The algorithm offers computational simplicity as it utilizes the linear relationship between the time delay vector and the DOA vector in Cartesian coordinates. Numerical and experimental results were given to demonstrate the performance of the Time Delay Direction Finding (TDDF) algorithm. The experimental results with a 7 microphone array have shown that in an anechoic chamber the average TDDF azimuth error was about 1.5 degrees, while in a regular room the average error was about 5 degrees. In [14], a distributed acoustic passive localization method using Wireless Sensor Network (WSN) has been proposed. Based on the time difference of arrival
(TDOA) from each participating WSN nodes in clusters, the base station calculates the azimuth angle and pitch angle, then using the geometrical information along with these TDOA estimates, the source location is found.

In [15], the authors localized the acoustic source using a WSN by utilizing the measured signal quantities like RSS, AOA and TDOA. For each of these quantities, an appropriate weighted LS criterion function was developed that was used for sound source localization. The authors claim that their work provides improvement of the localization accuracy for low SNR.

In [16], the authors propose a WSN based acoustics source localization and tracking system. The sensor board used in WSN was accompanied by a Xilinx Spartan-3L FPGA for powerful signal processing. The nodes were sparsely deployed. Each node, due to a powerful local signal processor, was able to estimate DOA locally and send it to a base station. Due to the widely distributed sensing and the novel sensor fusion technique, the method can handle multiple measurement errors prevalent in reverberant environments. Furthermore, the paper also describes the DOA estimation algorithm and the applied middleware services for coordinated sensing and communication introduces the sensor fusion algorithm and presents a detailed error analysis.

### 3.5.2 Localization Schemes Utilizing CS and Orthogonal Clustering algorithms

Although CS is finding applications in a wide range of areas in signal processing, it has not been widely used for acoustic source localization. The limited literature that can be found in regard to source localization using CS is mostly based on simulations. Especially, most of the researchers focused on electromagnetic (EM) source localization [17].

In [18], the author uses spatial CS for direction of arrival estimation. Utilizing the spatial scarcity of the sensor array and spatial orientation diversity, the author claims that his approach addresses challenging array signal processing problems such as left-right ambiguity and poor estimation performance at end-fire. However, the results are totally based on simulation and no practical implementation has been considered.

Exploiting spatial and signal scarcity, the authors in [19] develop a Bayesian framework for the localization problem. The authors also discuss 1-bit CS to reduce the amount of inter-sensor communications by transmitting only the intrinsic timing information. They also develop an algorithm for bearing estimation using a network of sensors. However, like most of the work in literature the CS approach towards localization problem has been considered only in simulation. It is, therefore, necessary to investigate the performance of CS theory in practical hardware based systems.

The conventional localization schemes estimate the TDOA directly from the
received signal at the sensors by cross-correlation or other TDE techniques. We can also use the channel impulse response concept to estimate the TDOA between the signals received at different sensors. But in this case the TDOA is hidden and estimation techniques are used to estimate the channel impulse response first.

The Orthogonal Clustering (OC) algorithm [5] basically estimates the Room Impulse Response (RIR) from the received signals at sensors. The TDOA can then be found by finding the time difference between the Direct Line of Sight (DLOS) component of the RIR. The details of how the algorithm works are given in chapter 5 and this method is used in the hardware implementation of the Impulsive Acoustic Source Localization (IASL) system proposed in this work. The main advantages of OC algorithm are:

1. It utilizes the a priory statistical information of the signal: sparsity (there are limited number of reflections of the signal), structure of the matrices of the mathematical models etc.
2. The algorithm does not need sampling of sensors at Nyquist rate, it can produce good results at sub-Nyquist sampling rate [5][6]
3. Subsampling reduces the power consumption of the sensors, especially in the case of the wireless mics which run on batteries.
4. Reduced computational complexity.

More details about the algorithm will be given in chapter 5 .

### 3.6 Conclusion

Acoustic source localization is basically a three step process; i) sound data acquisition from sensors array ii) estimating time delay from captured signals and iii) finding source location from time delays using localization algorithms. This chapter introduced all of these steps. The concepts of DOA and TDOA were explained at the beginning of the chapter. Signal models for different scenarios were developed to properly implement source localization in different environments. Several Time Delay Estimation (TDE) techniques were also discussed and relevant mathematical expressions were derived. At the end of the chapter an overview of acoustic source localization literature was presented by describing the results, techniques and relevant applications found in literature.

## CHAPTER 4

## WIRELESS SENSOR

## NETWORK BASED SOLUTION

## AND ISSUES

### 4.1 Introduction

Wireless Sensor Networks (WSN) research has focused mainly on implementing applications which use sensors that read slowly varying physical phenomena such as temperature, light, pressures etc. Moreover, the devices in the network (wireless sensor nodes) themselves are low power. Accordingly the software environments (operating system for operating these devices, software drivers etc.) are also designed keeping in mind the low power capabilities of the nodes.

TinyOS is a lightweight operating system specifically designed for low-power wireless sensors [20]. TinyOS is an open source operating system and it has gone
through evaluation of several versions. Its latest version is TinyOS 2.1.1 [21].
One of the objectives of the thesis is to investigate acoustic source localization in open environments and WSN is a natural choice for this purpose because of its several properties like good range (about 300meters), being active wireless devices (the node can perform operation on samples), low power consumption compared to other technologies, fine networking among nodes and many more. However, developing a WSN for acoustic application is not an easy task and we faced several issues during the development which will be discussed shortly. In literature, there is almost no material available that discusses issues in the TinyOS for commercial off the shelf (COTS) wireless sensor nodes (WSN) platforms in regard with high processing applications [22].

In this chapter, we present an analysis of the performance of TinyOS 2.x for an application that involve high sampling of the sensors, saving of the samples in local flash memory of the nodes and after completion of the sampling process reading back these samples from flash and forwarding it to the sink node. This application involves the implementation of several components and their relevant interfaces.

We use Crossbow's IRIS [23] nodes, MIB520 programmer and sink [23] and MTS300 sensorboards [24] to implement our application. The IRIS nodes have 4Mbit flash memory [25].

### 4.2 Related Work

The acoustic source localization research is not new and a good literature is available in this area. Successful attempts have also been made to implement acoustic source localization using WSN. Acoustic source localization is high processing application and require higher sampling rate (at least 8 kHz ) than what is provided by the available hardware and/or software environment for WSN. Therefore, the researchers use other ways such as attaching additional hardware, editing the existing software modules or writing new software modules etc. to cope with the issues that may be faced during acoustic application development.

In [26], the authors present a custom designed sensorboard that can be used with zigbee enabled nodes for multi-channel data processing. The sensorboard was designed using FPGA and it can be used with Telos-B and MICAz/MICA2 motes [27]. A microphone can be attached to the sensorboard for acoustic applications. This sensorboard relieves the motes from the burden of high processing that is needed for acoustic applications.

Gyula Simon, Miklós Maróti et al. present in [28] a WSN based counter sniper system in which they localize a sniper. They also use their custom designed sensorboards based on FPGA to carry out the processing of acoustic signals as the sensor nodes they use (UC Berkeley's Mica2 nodes [27]) are not capable of carrying out these high processing tasks using the standard TinyOS library components.

In [29], a software based approach was chosen to cope with the limitation of WSN for high processing applications. The authors wrote their own components
rather than using standard TinyOS components to implement high sampling of the microphones of Mica2. By utilizing the ADC's free running mode of ATMega128 MCU and intelligently using the flash memory of the mote the authors were able to achieve a sampling rate of 17.723 kHz . This shows that the hardware itself is capable of sampling the sensors at high rate but the software environment i.e. TinyOS is not fully utilizing it. We will explain it more in Section 4.7.

### 4.3 High Level Structure of the Application

Now we will present the high level structure of our application. Fig. 4.1 depicts a scenario of our application. There are three IRIS motes with MTS300 sensorboards (MTS300 not shown in the Fig. 4.1) and a sink node which is also an IRIS mote connected to MIB520 gateway. The gateway is then connected to the PC through USB connection.

Our objective is to sample the microphones attached to every node at the same time and transfer that samples from nodes to PC. So this can be achieved in the following way.

1. All the nodes in the network should be strictly synchronized.
2. Then we send a command from sink node to all the nodes to start sampling for a certain number of samples
3. The nodes upon receiving this command start sampling and store the samples in their local flash memory.
4. Upon completion of sampling the nodes read back stored samples from flash and send them to the sink.
5. The sink forwards these received packets to the PC.

Every node in the network runs the same application except the sink node which has its own dedicated application developed for it. The details of application development and underlying structure are given in Section 4.5. But before that we would like to give a brief introduction to TinyOS 2.x.


Figure 4.1: An example Wireless Sensor Network

### 4.4 TinyOS 2.x for WSN

"TinyOS is a lightweight operating system specifically designed for low-power wireless sensors" [20]. TinyOS is an open source operating system; a large community from all over the world contributes to its development. The website www.tinyos.net is the official website of TinyOS and provides almost all the necessary information for TinyOS like its source files, instructions for downloading TinyOS environment, tutorials, example application and much more.

TinyOS is written in nesC language (a dialect of C programming language) and features a component-based architecture, which enables rapid innovation and implementation while minimizing code size as required by the severe memory constraints inherent in sensor networks. TinyOS uses the concepts of components and interfaces. Components are different files which perform specific tasks while interfaces are communication link among different components. Interfaces carry commands and events from one component to another.

A component has two types: i) Module and ii) Configuration. Modules implement programming logic while configurations connect components into larger abstractions. A component uses three computational concepts: i) commands, ii) events, and iii) tasks. Commands and events provide the mechanism of communication among components while tasks are used to express intra-component concurrency. A command from a component is a request to another component to use its services. An event is a signal from the provider of a service to the user about the completion of the request made by the user previously. For exam-
ple, a component may request the sampling of a sensor to corresponding provider of the service. Once the request (sampling of the sensor) has been completed the provider signals an event to the user along with the sampled data and other information.

For illustration purpose an example structure of an application called BlinkC is shown in Fig. 4.2. Fig. 4.2 is identical to a figure generated by nesdoc -a tool of TinyOS which generates documentation for an application. In nesdoc diagrams, a single box is a module and a double box is a configuration. Dashed border lines denote that a component is a generic while solid border lines indicate that a component is singleton [20]. A generic component can be instantiated multiple times in an application and every instantiation is an independent copy of the component being instantiated. Singleton components are single components and are only one instance. If multiple configuration wire to a singleton component they all will use the same single copy of that component. In Fig. 4.2, TimerMilliC is a generic component and has been instantiated three times in BlinkC application while LedsC is a singleton component.

### 4.5 Acoustic Signal Acquisition Implementation

As was discussed in Section 4.3, our application consists of several steps i.e. i) sampling of the microphone ii) writing to/reading from flash memory iii) transferring data from motes to the sink wirelessly and iv) forwarding data from the sink to the PC through serial communication. We will now discuss the development


Figure 4.2: Block Diagram representation of a TinyOS application
of these steps one by one.

### 4.5.1 Synchronization

Our application requires the nodes to be strictly synchronized network-wide and the synchronization error should be in the order of micro seconds. There are several synchronization algorithms available for WSN but we have consulted the most popular ones. These are:

1. Reference Broadcast Synchronization (RBS) [30][31]
2. Timing-sync Protocol for Sensor Networks (TPSN) [32]
3. Flooding Time Synchronization Protocol (FTSP) [33]

In the RBS, a reference message is broadcasted. The receivers record their local time when receiving the reference broadcast and exchange the recorded times with each other. The main advantage of RBS is that it eliminates transmitter-side non-determinism. The disadvantage of the approach is that additional message exchange is necessary to communicate the local time-stamps between the nodes. The TPSN algorithm first creates a spanning tree of the network and then performs pairwise synchronization along the edges. Each node gets synchronized by exchanging two synchronization messages with its reference node one level higher in the hierarchy. The TPSN achieves two times better performance than RBS. The problem with TPSN is that it does not estimate the clock drift of nodes, which limits its accuracy.

We chose FTSP for network synchronization because of the following reasons:

1. It eliminates the shortcoming of the RBS and TPSN.
2. It achieves better performance than both of them with less synchronization error
3. Its implementation for TinyOS 2.x is already available [34].

The FTSP algorithm works by flooding several broadcast messages to the network from a beacon or root node elected by the nodes in the network. The nodes in the network receive these messages from root node, calculate the difference in the local and global (root's) time and then convert its local time to global time using the information of local clock drift and skew. FTSP uses MAC-layer time-stamping and error compensation techniques to achieve synchronization. It
is mentioned in [33] that FTSP achieves good synchronization and a maximum error of 4 microseconds can occur. However, as will be explained later in Section 4.6, this little error is achieved in an ideal scenario when there is no other processing going on the motes.

### 4.5.2 Sampling

The IRIS motes do not have any sensors embedded on it. Separate sensorboards are attached to it. We are using MTS300 sensorboard. This board has three sensors: microphone, temperature and a light sensor and a sounder device used to create a 4 kHz sound wave.

MTS300 carries a Panasonic WM-62A omnidirectional microphone [35]. The microphone circuitry consists of a tone detector, a multiplexer, a preamplifier, an anti-aliasing filter, a digital potentiometer and a bi-quad active filter. There are two output choices out of the circuitry: a raw microphone signal or the tone detector output. The LM567 CMOS Tone Detector IC detects a 4 kHz signal and outputs 1. If 4 kHz signal was not detected a 0 is outputted. 4 kHz tone can be generated by the sounder present on the sensorboard. We are using the raw microphone signal output for our application.

TinyOS 2.x provides a general purpose interface -ReadStream- for reading/sampling a sensor. The lower layers then provide its implementation for different sensors. For microphone ReadStream is provided by MicReadStreamP and MicStreamC components.

The microphone first needs to be powered on before its use. So after the completion of system initialization, we power on the microphone circuitry by using SplitControl interface. SplitControl interface for microphone is implemented by MicP component.

Unfortunately ReadStream is implemented using the single-sample mode of the ADC in combination with a microsecond alarm. It means that ADC free running mode is off and we can't achieve higher rates with this interface. During our experimentation we've found that we can attain approximately 4.9 kHz sampling rate with other processing turned off. Off course, it is not enough sampling rate for an audio signal. As the anti-aliasing filter of the microphone circuitry is a bandpass filter with cutoff frequencies 159 Hz and 6.4 kHz we need to sample the mic at a rate greater than or equal to 12.8 kHz . One way of achieving higher sampling rate is to sample the microphone in ADC free-running mode [36] by writing our own hardware specific code. Since our objective was to check the performance of TinyOS 2.x standard interfaces and components for high sampling applications like ours we did not continue with our own code development and continued with the standard interfaces and components.

We cannot send data with higher sampling rate directly through radio because of the limited bandwidth of the radio channels and the overhead in communication protocols. So we need to store the sampled data into the Flash memory of the mote as it is sampled. After completing the sampling of mic we then read the data back from the mote and send it to the BaseStation through radio.

### 4.5.3 Flash Reading/Writing

IRIS motes have a 4-Mbit serial flash (Atmel's AT45DB041) [25] for storing data, measurements, and other user-defined information.

TinyOS 2.x implements the storage tasks through one of three abstractions: i) small objects, ii) circular/linear logs and iii) large objects [37][38]. TinyOS 2.x also provides interfaces to abstract the underlying storage services and components that provide these interfaces.

Since our application deals with large amount of data, we use the large object abstraction. The interfaces BlockRead and BlockWrite are used for this abstraction to read and write data to the flash. These interfaces are provided by the BlockStrogeC component. We use these interfaces for reading and writing to flash to check its performance.

### 4.5.4 Radio communication

Radio communication uses different interfaces to carry out multiple tasks. In our code we used these interfaces: i) AMSend, for sending radio messages to a single node or to the network, ii) Receive, for receiving packets from the network, iii) Packet, for accessing payload of the radio packet and iv) AMPacket, for setting packet destination address in case of the unicast communication.

The radio packet consists of a header, footer and a payload area. The header and footer are system defined and usually need not to be edited. The payload area is where the user can put the data. The data can directly be put into the payload
or for consistency and convenience structures can be used to organize the data inside the payload. We use our own structure given in Fig. 4.3 to transfer our information among the motes. There are two structures: i) moteStruct: which is used by the nodes in the network to transmit their packets to the sink and ii) baseStruct: which is used by the sink to transmit its packets to the network.

The packet length of radio message can be defined by using specific lines in the Makefile of the application. In our case the total packet length including the overhead was 65 bytes due to the fact that we added extra fields for better management of the network as will be explained in Section 4.5.6. The default packet size of TinyOS 2.x is 28 bytes

```
typedef nx_struct moteStruct {
    nx_uint16_t src_addr;
    nx_uint8_t is_synced;
    nx_uint8_t state;
    nx_uint32_t time_stamp;
    nx_uint32_t start_time;
    nx_uint32_t sampling_time;
    nx_uint32_t stop_time;
    nx_uint16_t reading[BUF_READ];
} moteStruct;
typedef nx_struct baseStruct {
    nx_uint16_t nodeid;
        nx_uint16_t cmd;
}baseStruct;
```

Figure 4.3: User-defined structure for the payload of radio packet

### 4.5.5 Serial communication and MATLAB interfacing

The next stage is to deliver the packets from the sink that it received from network to the PC over the USB link. MIB520 uses FTDI FT2232C to use USB port as virtual COM port [23]. After installing the required drivers we can access the MIB520 as serial port in the PC.

We then access the virtual COM port in MATLAB to get the binary data from the port. The data need to be parsed into packets and their corresponding fields. We wrote MATLAB programs to convert binary data into packets and extracted specific fields from these packets. As is shown in Fig. 4-3 every field of the packet contain specific data and a careful coding is required to successfully extract the required information out of the received binary data from serial port.

### 4.5.6 Overall Structure of the Application

After discussing individual components of our model we are now able to discuss the application itself. The network consists of a single sink node and multiple data acquisition nodes. The sink node requires its own special code to properly manage the network and transmit/receive packets to/from the network and to/from the PC. We call this application as BaseStation and from now on we will refer to the sink node, alternatively, by BaseStation. The BaseStation is our modified version of the standard BaseStation application that can be found in /tos/apps directory of the TinyOS 2.x standard distribution. The original BaseStation only works as a repeater, whatever packet it receives from the network it forwards it to the

PC and vice versa. Our modified version is an intelligent BaseStation, it does not forward every packet to PC until it was intended and also it manages the network's status by issuing certain commands to the nodes.

All the nodes besides the sink node run an application that is different from the BaseStation and this application will be called the sync. All the nodes (except the sink) have the same sync application installed onto them. We will refer to these nodes as sync, alternatively, onward.

We have designed the sync and BaseStation applications such that both of them interact with each other in a command-response manner. We define a set of commands which are known to the BaseStation and all the nodes in the network. The BaseStation sends the commands in the cmd field of its structure (baseStruct) while the motes respond to these commands by sending their status in the state field of their structure (moteStruct). We define these commands and responses as enum constants as given in Fig. 4.4.

First we will discuss the BaseStation side story. Upon booting the BaseStation broadcasts a message with the REBOOT state in the cmd field to the network to indicate that it has booted and all the nodes need to reboot as well. After this it does nothing and waits to receive any radio packet forwarded to it. The nodes reboot and once they have booted successfully they send the state BOOTED in response to indicate that they have booted in their state field of their packet.

The command DO_NOTHING indicates that this broadcast message is a synchronization message and does not contain any command. The BaseStation uses
this state to broadcast synch messages when it receives request from nodes for synch messages transmission when they boot. The synch messages are then periodically sent to the network.

The command IS_SYNCED is used to ask nodes in the network about their synchronization status when needed. The BaseStation then waits for the nodes' response about their status. When a node becomes synchronized it sends the status NO_DATA in its state field with is_synced field set to 1 to the BaseStation. When the BaseStation receives the synchronization confirmation from all the nodes in the network it stops sending synch messages and then issues START_SAMPLE command to the nodes to start sampling of the microphone sensors attached to

```
enum{ //commands for basestation cmd
    DO_NOTHING = 1,
    IS_SYNCED =2,
    START_SAMPLE = 3,
    START_TX = 4,
    REBOOT = 5,
};
enum{ // response statuses for motes state
        NO_DATA = 10,
        DATA_START = 11,
        DATA_STOP = 12,
        SAMPLE_DONE = 13,
        REBOOTED = 14,
};
```

Figure 4.4: Commands and states for BaseStation and nodes respectively
them. After sampling, all the motes inform the BaseStation about the completion of sampling and storing data in local flash tasks which in return issues the START_TX command to the first node only using unicast communication.

The first node reads the data from flash which it has previously stored and transmits it to the BaseStation only. Note that all the motes communicate with BaseStationon on peer-to-peer basis. Only BaseStation broadcast certain messages when needed. Also the communication among BaseStation and motes is based on best effort approach. No acknowledgement of communication is carried out to save power as the data length is quite large (32bytes). When the first node successfully completes the transmission of data it sends DATA_STOP status to BaseStation to indicate end-of-data. BaseStation then issues the START_TX command to the second node. The second node transmits data and informs BaseStation about completion. The BaseStation then sends START_TX commands to the third node which also transmits it data and so on. The BaseStation is programmed such that it forwards only those packets to PC which contains microphone readings, all other messages are not forwarded to PC.

Now we will discuss the sync's side story. Fig. 4.5 gives the flowchart description of the sync application that is installed on every node in the network except the sink node.

NO_DATA is used to exchange signaling information like synchronization status, reboot status, sample done status and several others. We define two different message_t variables (buffers more accurately) in the application: AMsignal


Figure 4.5: The structure of sync application
for transmitting signaling messages and AMdata for transmitting packets which contain microphone data. The data packet containing DATA_START state is transmitted using AMdata buffer. All other packets containing one of the remaining states are transmitted using AMsignal buffer. Two AM types are used: AM_BASESTRUCT (equals to 7) for receiving packets from BaseStation and AM_MOTESTRUCT (equals to 6) for sending packets to BaseStation. This strategy avoids inter-mote communication and all motes communicate with BaseStation only and the network congestion is reduced.

As will be explained in Section 4.6, TinyOS uses the concept of tasks and split-phase operation. Several tasks may be running in parallel in the system in split-phase operation sense and their completion is arbitrary depending on the application. Therefore, in the Fig. 4.5 we have represented these tasks in separate small flowcharts. There are four small flowcharts for the events of ReadStream.bufferDone (corresponding to the interface for reading sensor), BlockWrite.writeDone, BlockRead.readDone (corresponding to interfaces for writing and reading form flash memory) and AMSend.sendDone (corresponding to interface for sending radio packets to the network) besides the main application flowchart. Their interaction with the main flowchart is shown by a page-reference (like Back and Read).

The application when booted calls AMControl.start command to start the radio hardware of the node. After its successful start the application then starts the microphone hardware. After that the flash erase operation is carried out because
as in mentioned [37][38] an erase is necessary before writing to the flash memory of the node. After that the node sends the BOOTED state to the BaseStation in the state field. The node then waits for the radio packets from the BaseStation.

When a radio packet is received the node checks the payload for certain commands issued by BaseStation. The cmd may contain one of five possible commands of Fig. 4.4. If the cmd is REBOOT it means the BaseStation wants the nodes to be reset. So the node reset itself using the Reset interface.

If the cmd is DO_NOTHING it means this packet is a synchronization message. The node using FTSP algorithm converts its local clock to global time of BaseStation and updates a variable is_synced and sends the radio packet to the BaseStation. The is_synced may be TRUE or FALSE depending on the return value of GlobalTime.local2Global function. TRUE means node is synchronized to the BaseStation and FALSE means not synchronized.

As was discussed in this section previously the BaseStation sends synch messages periodically until all nodes become synchronized. If the cmd in the received message is START_SAMPLE it means that all the nodes are synchronized and the BaseStation wants all the nodes to start sampling of the microphone. So the node posts four buffers for sampling and then calls the ReadStream interface.

When the ReadStream fills the first buffer it signals the ReadStream.bufferDone event after which the application writes the sampled data to the flash using BlockWrite.write interface. After successful writing to flash the BlockWrite.writeDone event is signaled. The application then checks whether
the required number of samples have been read from mic if yes it issues BlockWrite.sync command to the flash to sync the data it has written recently otherwise it again posts buffer to ReadStream interface. Sync is required for data to be stored permanently on flash otherwise the data will be lost after power off [38].

The application also notes down the time when first sample is read and the time when last sample is written to flash. This time difference is then used to calculate average sampling rate of the microphone.

After successful sampling operation, the node sends SAMPLE_DONE status to the BaseStation to indicate that it has finished sampling. When the BaseStation receive SAMPLE_DONE status from all nodes it issues START_TX command to the node1.

So if the cmd in the received message from BaseStation contains START_TX it means that the node needs to send all the mic data it has recently stored in the flash. The application keeps the records of number of messages it sends so that it sends the required number of messages. This number depends on the data. For example, in our application we have 16384 samples and we send 16 samples per message so there are total $16384 / 16=1024$ messages to be sent. Once all the data have been sent the node then sends a message with the state of DATA_STOP. The BaseStation can recognize this state. The BaseStation then sends START_TX command to the next node, for example, node \# 2 and so on. Similarly all the nodes in the network send their mic readings one by one to the BaseStation which forwards it to the PC on serial port.

### 4.6 Results and Discussion

In this section we will discuss different experimentations we carried out and the analysis based on them.

### 4.6.1 Error Souces and Uncertainties

During the development we faced several issues. These will be discussed one by one but let's first discuss the split-phase operation of TinyOS which is the main cause of these issues (in the scenario of this specific application only).

## Split-phase Operation in TinyOS 2.x

"Hardware is almost always split-phase rather than blocking" [20]. Split-phase operation means that the request for an operation is completed immediately (for example, request for reading a sensor attached to ADC) but actual completion of the operation takes sometime depending on the hardware resources. The completion of actual operation is signaled later by a separate call back.

Now the software may be required to operate either in synchronous mode or split-phase. For proper implementation the software and hardware behavior must be the same. So the solution is to either make the reading interface split-phase or make the ADC synchronous. TinyOS takes the former approach [20]. Rather than making everything synchronous through threads, operations that are split-phase in hardware are split-phase in software as well. This means that many common operations, such as sampling sensors and sending packets, are split-phase. Almost
all the interfaces we use in the applications are split-phase. As we will see in the coming sections, this split-phase operation is very unfavorable to applications which sample the sensors at high rate and require that the nodes should be strictly synchronized.

## Uncertainties in Sampling

The most critical interface is ReadStream. The ReadStream interface's design is based on Read interface which works on the principle of reading only one sample at a time and signaling back this sample to the application. The Read interface does not have the capability to read ADC continuously and hence the ReadStream interface which uses it encounters a great deal of delay of arbitrary nature between any two consecutive samples. This reduces not only the sampling rate but also affect the continuity of the sampling. Since the sample interval is arbitrary, the samples from different motes are not strictly concurrent even if their local clocks are synchronized and therefore they don't correspond to the same physical event.

This issue is very critical for our application. Our application requires that all the readings from all the nodes should correspond to the same real time happening. So using the TinyOS 2.x standard distribution ReadStream interface we cannot achieve real time concurrent sampling for all nodes.

The second problem is with achieving higher sampling rate. Using ReadStream we were able to achieve only 4.9 kHz average sampling rate. Obviously this sampling rate is not enough for audio signal processing. The literature says that we can achieve higher sampling rate by sampling ADC in free running mode but
that would mean modifying several components of TinyOS standard distribution along with their interfaces at different levels of abstraction. This proves that there is a need of enhancing TinyOS interfaces and components to accommodate high sampling rate applications.

## Uncertainties in Flash Reading/Writing

Now the problems is that both the read and write interfaces (BlockRead and BlockWrite) for the flash are split-phase and so all the issues faced in sampling operation are faced in this scenario as well.

Since every ADC has a limited buffer which contains the recent reading, we need to extract data from this buffer and store it in the flash before the ADC start sampling the next reading. This means that we have to empty the buffer and write the data to flash in a time period less than or equal to the sampling interval of the microphone otherwise the ADC will overwrite the buffer with the new reading and the old reading will be lost. This requires that write interface of the flash should be able to write the data synchronously and fast enough for successful sampling. However, as we mentioned that BlockWrite interface (and all other interfaces of flash memory) are split phase and thus the writing operation is not synchronous or continuous. Instead it is arbitrary and the time interval between any two writing operations is also arbitrary. This creates problem for the ADC to successfully deliver a synchronous high rate read operation.

This situation is explained in Fig. 4.6. The sampling interval is denoted by $t_{s}$ and is arbitrary. Let's assume that $t_{s}$ is between time $t_{0}$ and $t_{1}$. Similarly $t_{w}$
represents the flash writing time and let's assume this time is between $t_{2}$ and $t_{3}$. Now for every single sampling/writing operation the total time taken $t_{s w}$ is given by

$$
\begin{equation*}
t_{0}+t_{2}<t_{s w}<t_{1}+t_{3} \tag{4.1}
\end{equation*}
$$

Equation (4.1) signifies the fact that for every node the interval $t_{s w}$ is not constant and hence the sampling/writing operation takes arbitrary time for every node.


Figure 4.6: Analyzing the arbitrariness of ReadStream and BlockWrite

## Synchronization Issues

We also faced problems in achieving strict synchronization among the motes. To analyze how the synchronization works and whether the selected synchronization scheme (FTSP [33]) will achieve the goal we performed certain experiments:

1. Time stamping different events in the application
2. Changing the number of synch messages sent per second to the network
3. Changing the total number of samples to be read

We used a modified version of the sync application discussed in Section 4.5. The number of samples to be read was 16384. We time-stamped the message arrival time for START_SAMPLE command from BaseStation to check whether all the motes receive the command at the same time. Then we start sampling and note down the local clock value when the first sampling buffer is signaled to see the timing of the first buffer completion at each node. We also note down the local time when the last sampling buffer is signaled.

Literature for FTSP [33] says that at least one synch message from beacon to the network is required for proper synchronization. However, as we will show the synchronization is also heavily dependent on the local processing on the mote. So to check the performance we played with the synch message period i.e. the number of synch messages sent to network per second from beacon.

The motes were placed next to each other. The experiment was performed to check the timing of different events so there was no audio source because we are not interested in the signal itself. Fig. 4.7 shows the output of two experiments, the first experiment was done with sync message period of 1second and the second experiment was done with sync message period of 500 mSec i.e. two messages/second.

As can be seen from Fig. 4.7 a and 4.7 b, the average sampling frequency decreases from 3.0 kHz to 2.4 kHz when the number of synch messages are increased from 1 to $2 / \mathrm{sec}$. This is because in the second case the local MCU of the mote has to do extra processing (receiving extra message and performing synchroniza-
tion tasks twice a second compared to once in the first case) which disturb the process of sampling the microphone. This issues arise from the fact that MCU is sequential by nature, the parallelism of TinyOS is only in software sense.

```
Sampling Frequency of Mote1=3072.917883
Sampling Frequency of Mote1=3059.176090
Sampling Frequency of Mote1 = 3082.023747
Mote1: START_SAMPLE cmd arrival from BS Time Stamp = 1823
Mote2: START_SAMPLE cmd arrival from BS Time Stamp = 1823
Mote3: START_SAMPLE cmd arrival from BS Time Stamp = 1823
Mote1: Time of 1st sample = 2774815
Mote2: Time of 1st sample =2775712
Mote3: Time of 1st sample = 3663319
Time Difference in Mote 1 & 2 =-897 uSec
Time Difference in Mote 2 & 3=-887607 uSec
Time Difference in Mote 3 & 1=888504 uSec
Mote1: Time of last sample = 6118176
Mote2: Time of last sample =6137625
Mote3: Time of last sample = 7006283
Time Difference in Mote 1 & 2 = -19449 uSec
Time Difference in Mote 2 & 3 = -868658 uSec
Time Difference in Mote 3 & 1=888107 uSec
```

(a)

```
Sampling Frequency of Mote1=2457.516704
Sampling Frequency of Mote1=2446.188940
Sampling Frequency of Mote1=2443.109647
Mote1: START_SAMPLE cmd arrival from BS Time Stamp = 1318
Mote2: START_SAMPLE cmd arrival from BS Time Stamp = 1318
Mote3: START_SAMPLE cmd arrival from BS Time Stamp = 1318
Mote1: Time of 1st sample = 2320246
Mote2: Time of 1st sample = 2320244
Mote3: Time of 1st sample =2316661
Time Difference in Mote 1 & 2 = 2 uSec
Time Difference in Mote 2 & 3=3583 uSec
Time Difference in Mote 3 & 1 = -3585 uSec
Mote1: Time of last sample = 5664560
Mote2: Time of last sample = 5684902
Mote3: Time of last sample =5686335
Time Difference in Mote 1 & 2 = -20342 uSec
Time Difference in Mote 2 & 3 = -1433 uSec
Time Difference in Mote 3 & 1=21775 uSec
Fs=2.4487e+003
```

(b)

Figure 4.7: Analyzing the effect of no. of sync message/s on synchronization, (a) 1000 mSec case, (b) 500 mSec case.

Looking at Fig. 4.7a and 4.7 b , we observe that all motes are strictly synchronized at the time when they receive the START_SAMPLE command from BaseStation because the time stamp for this message reception is the same on all motes. However, the time for the first sample buffer event is not the same for all motes. This may be due to two reasons:

1. The local times of the motes are no longer synchronized because of the clock drift
2. Sample done event was not signaled at the same time because of the arbitrary nature of ReadStream interface on all motes.

We call this situation as uncertainty because we don't know the real reason of the problem. So we have two uncertainties here: i) synchronization uncertainty and ii) sampling uncertainty.

Fig. 4.7 clearly shows that in case (b) the time difference of sample buffer done event is less compared to case (a) both for the first sample and the last sample buffer. This verifies that the more the number of synch messages/second sent to the network the more it gets synchronized. However we cannot increase the number of synch messages more than $2 /$ seconds because it heavily disturbs other processing going on the local MCU of the motes as is evident in Fig. 4.7 for the sampling frequency that has decreased due to increase in number of sync messages per second.

We performed another experiment playing with the total number of samples to be taken from microphone while keeping the sync message period constant (1
second). We performed the experiment for two cases: i) 4096 samples ii) 8192 samples. Fig. 4.8 shows the results of these experiments.

Here in this case as well, the motes are strictly synchronized when they receive START_SAMPLE command from BaseStation. The arbitrariness of sample done event remains but there are two things to be noted:

1. The average sampling frequency reduces as the numbers of samples reduce. It is 1.5 kHz for case (a) and 2.1 kHz for case (b)
2. The time difference for the last sampling buffer done event is more in case (b) than case (a) which clarifies that since in case (a) the number of samples is less and hence it takes less time and hence little clock drift is observed as compared to case (b) where there are more samples (double the no. in case (a)) to be read which take more time and hence the clock drift occurring in this time is more.

So as the time elapses, due to clock drifts, the local clocks of the motes get more and more un-synchronized.

These experiments confirm that the FTSP algorithm was not able to synchronize the network in our case and the synchronization depends on several parameters. The local clocks behavior is also arbitrary due to the inherent drift in the clock.

## Uncertainties in Radio and Serial Communication

We encountered the following problems in radio and serial communication:

```
Sampling Frequency of Mote1 = 1508.338994
Sampling Frequency of Mote1=1505.173328
Sampling Frequency of Mote1 = 1504.135432
Mote1: START_SAMPLE cmd arrival from BS Time Stamp = 1318
Mote2: START_SAMPLE cmd arrival from BS Time Stamp = 1318
Mote3: START_SAMPLE cmd arrival from BS Time Stamp = 1318
Mote1: Time of 1st sample = 2320247
Mote2: Time of 1st sample = 2320313
Mote3: Time of 1st sample = 2316663
Time Difference in Mote 1 & 2 = -66 uSec
Time Difference in Mote 2 & 3=3650 uSec
Time Difference in Mote 3 & 1= -3584 uSec
Mote1: Time of last sample = 3118601
Mote2: Time of last sample =3121741
Mote3: Time of last sample =3118880
Time Difference in Mote 1 & 2 = -3140 uSec
Time Difference in Mote 2 & 3=2861 uSec
Time Difference in Mote 3 & 1=279 uSec
```

(a)

```
Sampling Frequency of Mote1 = 2145.595489
Sampling Frequency of Mote1=2135.533437
Sampling Frequency of Mote1 = 2134.508167
Mote1: START_SAMPLE cmd arrival from BS Time Stamp = 1319
Mote2: START_SAMPLE cmd arrival from BS Time Stamp = 1319
Mote3: START_SAMPLE cmd arrival from BS Time Stamp = 1319
Mote1: Time of 1st sample = 2295104
Mote2: Time of 1st sample =2295102
Mote3: Time of 1st sample =2291450
Time Difference in Mote 1 & 2 = 2 uSec
Time Difference in Mote 2 & 3=3652 uSec
Time Difference in Mote 3 & 1= -3654 uSec
Mote1: Time of last sample =3969020
Mote2: Time of last sample = 3981714
Mote3: Time of last sample =3978948
Time Difference in Mote 1 & 2 = -12694 uSec
Time Difference in Mote 2 & 3=2766 uSec
Time Difference in Mote 3&1=9928 uSec
```

(b)

Figure 4.8: Analyzing the effect of no. of samples on synchronization, (a) 4096 samples case, (b) 8192 samples case

1. Radio packet loss (about $20 \%$ )
2. Radio packet length variations
3. Serial packet length variations

The radio packet loss is a serious issue. We can lose critical data such as impulsive peak corresponding to the gunfire because of its short duration. A peak may be contained in 2 or 3 packets only because of the low sampling frequency and $20 \%$ loss is "enough" to lose this peak.

The second issue is the packet length variation. The received packet at PC does not have a constant length. The length varies by a few bytes but this also complicates the programming at the PC. The issues may be due to two reasons:

1. The length of packet varies because of the local clock drifts at the transmitting node and receiving node (BaseStation)
2. The length of packet varies because of local clock drift in the BaseStation relative to PC clock.

Now this situation is also arbitrary and uncertain. So this is another uncertainty adding to the issues we are facing in our application. The problem of packet length variation can be solved by padding (truncating) in the case of short (long) packets.

## Joint Uncertainty

The uncertainties discussed in previous subsections $1-5$ contribute to a joint uncertainty that makes the task of debugging and application analysis difficult. It drastically affects our application being sensitive to synchronization, sampling and communication.

It is to be noted that these uncertainties come from the split-phase design
of the interfaces and components of the TinyOS. One can develop his/her own interfaces and components directly accessing the hardware and taking care of minute details. For example for continuous sampling we can take advantage of the free running mode of ATMega1281 microcontroller [36]. In free running mode the MCU constantly samples the sensor and updates its buffer. The user has to take care of taking the data out of the register. Similarly for fast flash reading/writing hardware specific code can be written. In [29] the authors have written their own code for microphone sampling, flash reading/writing and other services. They were able to achieve a sampling rate of 17.73 kHz and a good synchronization among the motes by modifying the FTSP algorithm and incorporating some other techniques from the literature. The authors, however, did not share their code as it is proprietary.

### 4.6.2 An Example Experiment

Fig. 4.9 shows a configuration of three sensor nodes placed on a line 50 cm apart from each other. The nodes were programmed with the sync application of Section 4.5. Fig. 4.10 shows the plotted sampled data that was sampled from the three motes. The audio source was an unloaded toy gun. The gun was fired at node 1.

The data peak which represents the shot occurs for node 1 at sample time 6356, for node 2 at sample time 7024 and for node 3 at sample time 6487. All the nodes are sampling at an approximate average sampling rate of 4.9 kHz . Using this sampling rate we can convert the peak sample time to real time. These are


Figure 4.9: Nodes configuration for the experiment, (a) Front View, (b) Side View. given by

$$
\begin{align*}
t_{1} & =\frac{6356}{4.9 k S P S}=1.297 s, t_{2}=\frac{7024}{4.9 k S P S}=1.433 \mathrm{~s} \\
t_{3} & =\frac{6487}{4.9 k S P S}=1.323 \mathrm{~s} \tag{4.2}
\end{align*}
$$

while $t_{1}, t_{2}, t_{3}$ represent the peak time for node 1,2 and 3 respectively.

Clearly the timings are invalid because a distance of 50 cm corresponds to a time delay of $\frac{50 \mathrm{~cm}}{340 \mathrm{~m} / \mathrm{s}}=1.47 \mathrm{mSec}$ while the time difference of arrival at each node for the gunshot is in the order of hundreds of milliseconds.

This strange behavior of the motes can be explained by the following reasons:

1. The local clocks of all nodes are not synchronized to each other.
2. Several packets were lost in the radio/serial communication and the peaks do not correspond to the same value of the signal but to different peaks in the same signal at different times. Note that the experiment was performed in a hall so the echoes may correspond to the peaks as well.
3. The data were not properly written to /read from flash. For example, some of the data were overwritten because of fast sampling compared to slow writing of the flash.
4. The data were overwritten in the ADC buffer by the ADC before the application was able to extract data out of the buffer and write it to the flash.

So any or all of the uncertainty discussed in Section 4.6.1 may contribute to the erroneous results of the experiment. This shows that the standard TinyOS interfaces and their relevant components are not suitable for applications which involve high sampling rate, strict synchronization and fast data storage and trans-




Figure 4.10: Results for the experiment conducted in Fig. 4.9
fer. Instead, one needs to change the existing system code of TinyOS or develop his/her own code entirely from the hardware level to operating system level to achieve the accuracy needed.

### 4.7 Conclusion

In this chapter we presented the development of a WSN for impulsive acoustic source localization and the issues encountered during the development process. The development was totally based on using the TinyOS 2.x standard interfaces and components.

Five error sources were identified that can significantly degrade the WSN performance if not handled in a custom way. The effect of each of these error sources was verified through a specific experiment and the development of specific applications. Several recommendations were given to overcome such errors.

## CHAPTER 5

## THE ORTHOGONAL

## CLUSTERING ALGORITHM

## AND EXPERIMENTAL SETUP

In this chapter we will discuss the Orthogonal Clustering (OC) algorithm that we will use for our acoustic source localization application as well as the hardware system and TDOA geometries. Section 5.1 describes the steps that are involved in the OC algorithm for TDE. Section 5.2 describes in detail the TDOA geometries we are using to analyze and compare the performance of the OC and CC TDE methods. We discuss the hardware system used to carry out the experiments in Section 5.3.

### 5.1 The Orthogonal Clustering (OC) Algorithm

In this section we describe the main steps that are involved in the OC method for TDE estimation. We will only give the important mathematical expressions of the algorithm and will not go into the mathematical detail of the algorithm as it has already been explained very well in [5] and [6].

### 5.1.1 Problem Development

Suppose there are $N$ sensors and they are placed in a Cartesian Coordinate system. An impulsive acoustic source generates a signal in the same system. Every sensor will capture the signal. Let sensor 0 be the reference sensor for all other sensors. The signal received at a particular sensor will be an advanced or delayed version of the signal received at the sensor 0. If the size of the Cartesian Coordinate system is $X \times Y$, where $X$ (in meters) is the maximum size of $x$-axis and $Y$ (in meters) is that of $y$-axis, then the maximum time difference between the signals of any two sensors $j$ and $i$ that can be observed will be

$$
\begin{equation*}
\tau_{j i}=\frac{\sqrt{X^{2}+Y^{2}}}{c} \tag{5.1}
\end{equation*}
$$

where $c$ is the speed of the sound wave. We can formulate this scenario into a matrix notation. Let $\Psi$ be an $M \times N$ matrix and each column of the $\Psi$ represents the delayed version of the original signal. Column 1 represents the zero-delay signal (at time 0) as shown in Fig. 5.1, column 2 represents the signal delayed by
one sample and so on. $N$ is the length of the signal (e.g., 16000 samples) and $M$ is the expected number of delays. We keep $M=16000$ to accommodate a time delay up to 1 second (at 16 kHz sampling rate) which is enough for our application (in our application the delays are not more than few milliseconds). The $\boldsymbol{\Psi}$ matrix is called the Dictionary or Sensing matrix. Let y be the observed signal we captured at a sensor then we can write,

$$
\begin{equation*}
\mathbf{y}=\Psi_{x}+\mathbf{n} \tag{5.2}
\end{equation*}
$$

where $\mathbf{x}$ is a vector representing the Channel Impulse Response (CIR) of the environment (indoor or outdoor) and $\mathbf{n}$ is the complex additive white Gaussian noise. Since we are assuming a single acoustic source, $\mathbf{x}$ will be a sparse vector and will have few nonzero values corresponding to the original signal and its reflections. We call this number of nonzero values as the Sparsity or the Support of the $\mathbf{x}$ and represent it by $\mathcal{S}$.

The Dictionary matrix $\Psi$ has a structure (resembling that of a Toeplitz matrix) and this information can be utilized to reduce computational complexity to find $\mathbf{x}$. The authors in [5] established an algorithm which they denote as Orthogonal Clustering (OC). They utilize the CS knowledge and the structure of $\Psi$ along with other a priori statistical information to efficiently estimate the CIR while reducing the computational burden on the processing system. The next subsection describes the algorithm in details.


Figure 5.1: Problem formulation for OC

### 5.1.2 The OC Algorithm

The $\mathbf{x}$ in (5.2) is modeled as $\mathbf{x}=\mathbf{x}_{\mathbf{B}} \odot \mathbf{x}_{\mathbf{G}}$, where $\odot$ represent element by element multiplication. $\mathbf{x}_{\mathbf{B}}$ is a random process whose elements are independent and identically distributed (iid) with Bernoulli distribution and those of $\mathbf{x}_{\mathbf{G}}$ are also iid but with some unknown zero mean distribution. If $\mathbf{x}$ has sparsity $\mathcal{S}$ then (5.2) can be written as

$$
\begin{equation*}
\mathbf{y}=\mathbf{\Psi}_{\mathcal{S}} \mathbf{x}_{\mathcal{S}}+\mathbf{n} \tag{5.3}
\end{equation*}
$$

where $\Psi_{\mathcal{S}}$ is the sub-matrix formed by only those columns corresponding to nonzero values of $\mathbf{x}$ i.e. $\left\{\psi_{i}: i \in \mathcal{S}\right\}$. The Minimum Mean Square Estimate (MMSE) of $\mathbf{x}$ given the observation $\mathbf{y}$ is given by [5]

$$
\begin{equation*}
\hat{\mathbf{x}}_{M M S E}=\mathbb{E}[\mathbf{x} \mid \mathbf{y}]=\sum_{\mathcal{S}} p(\mathcal{S} \mid \mathbf{y}) \mathbb{E}[\mathbf{x} \mid \mathbf{y}, \mathcal{S}] \tag{5.4}
\end{equation*}
$$

where $\mathbb{E}[\mathbf{x} \mid \mathbf{y}, \mathcal{S}]$ is simply the linear MMSE of $\mathbf{x}$ given $\mathbf{y}$ if $\mathbf{x}$ conditioned on its support is Gaussian [5][6] i.e.

$$
\begin{equation*}
\mathbf{x}_{\mathcal{S}}=\sigma_{x}^{2} \mathbf{\Psi}_{\mathcal{S}}^{H} \Sigma_{\mathcal{S}}^{-1} \mathbf{y} \tag{5.5}
\end{equation*}
$$

where

$$
\begin{equation*}
\Sigma_{\mathcal{S}}=\frac{1}{\sigma_{n}^{2}} \mathbb{E}\left[\mathbf{y} \mathbf{y}^{H} \mid \mathcal{S}\right]=\mathbf{I}_{M}+\frac{\sigma_{x}^{2}}{\sigma_{n}^{2}} \mathbf{\Psi}_{\mathcal{S}} \boldsymbol{\Psi}_{\mathcal{S}}^{H} \tag{5.6}
\end{equation*}
$$

where $\sigma_{n}, \sigma_{x}$ are the variances of $\mathbf{x}$ and the noise respectively and $H$ represents the complex conjugate transpose. If $\mathbf{x} \mid \mathcal{S}$ is non-Gaussian then the Best Linear Unbiased Estimate of $\mathbf{x}$ is

$$
\begin{equation*}
\mathbf{x}_{\mathcal{S}}=\left(\mathbf{\Psi}_{\mathcal{S}}^{H} \mathbf{\Psi}_{\mathcal{S}}\right)^{-1} \mathbf{\Psi}_{\mathcal{S}}^{H} \mathbf{y} \tag{5.7}
\end{equation*}
$$

$p(\mathcal{S} \mid \mathbf{y})$ is calculated using Bayes rule [5]

$$
\begin{equation*}
p(\mathcal{S} \mid \mathbf{y})=\frac{p(\mathbf{y} \mid \mathcal{S}) p(\mathcal{S})}{\Sigma_{\mathcal{S}} p(\mathbf{y} \mid \mathcal{S}) p(\mathcal{S})} \tag{5.8}
\end{equation*}
$$

The expressions for the two unknowns i.e. $p(\mathbf{y} \mid \mathcal{S})$ and $p(\mathcal{S})$ are given in [5]. The MMSE formulation in the case when the $p(\mathcal{S} \mid \mathbf{x})$ is unknown and the Maximum A Posteriori (MAP) estimate of $\mathbf{x}$ have also been covered in [6] in detail. Since we are using the MMSE estimate of $\mathbf{x}$ in our application we will not discuss the MAP estimation of $\mathbf{x}$.

Now let $\mathcal{S}$ be the support of $\mathbf{x}$ then (5.3) can be written as [5][6]

$$
\mathbf{y}=\left[\begin{array}{llll}
\Psi_{\mathcal{S}_{1}} & \mathbf{\Psi}_{\mathcal{S}_{2}} & \ldots & \Psi_{\mathcal{S}_{P}}
\end{array}\right]\left[\begin{array}{c}
\mathbf{x}_{1}  \tag{5.9}\\
\mathbf{x}_{2} \\
\vdots \\
\mathbf{x}_{P}
\end{array}\right]+\mathbf{n}
$$

where $P$ is the maximum number of clusters formed from the columns of $\Psi$ because of orthogonality (or semi-orthogonality as the authors in [5] call it) among them due to the structure of the matrix. $\mathcal{S}$ is the support set corresponding to the $i$ th cluster(with $i=1,2, \ldots, P)$. This clustering allows us to write (5.4) as
$\hat{\mathbf{x}}_{\text {AMMSE }}$ means approximate MMSE of $\mathbf{x}$. Equation (5.10) means that $\hat{\mathbf{x}}_{\text {AMMSE }}$ can be calculated in a divide-and-conquer manner by separately evaluating each cluster either in parallel, if possible, or one by one which reduces the computation burden on a processing platform considerably.


Figure 5.2: Flowchart of the OC algorithm showing the main steps

Now we describe the steps that the OC algorithm takes to estimate $\hat{\mathbf{x}}_{M M S E}$. Fig. 5.2 shows these steps in the form of a flow chart. We discuss these steps next in detail.

## Step1: Determining Dominant Position

The first step of the algorithm is to find the dominant support of $\hat{\mathbf{x}}$ and this can be achieved by correlating the observation vector $\mathbf{y}$ with the sensing matrix $\Psi$ in (5.2). This will give us an initial guess of the sparsity of $\hat{\mathbf{x}}$.

## Step2: Forming Semi-orthogonal Clusters

The vector of $N$ correlations obtained from Step1 can help us create clusters. First an index $i_{1}$ is selected that corresponds to the largest correlation and a cluster of size $L$ is formed around it. The value of $L$ is selected according to a correlation tolerance $\epsilon$. Then another cluster is formed around the next largest correlation with index $i_{2}$ and so on until a total $P$ non-overlapping clusters are formed. If two clusters are overlapping then they are combined into one big cluster.

## Step3: Finding the Dominant Support and their Likelihood

The next step is to find the maximum possible support size $P_{c}$ in a cluster $i$ of size $L_{i}$ for each of the $P$ clusters formed in Step 2. This is done by finding the likelihood for all supports of size $\ell=1,2, \ldots, P_{c} . P_{c}$ is calculated by the following formula [5]

$$
\begin{equation*}
P_{c}=\left\lceil\operatorname{erfc}^{-1}\left(10^{-2}\right) \sqrt{2 L_{i} p(1-p)}+L_{i} p\right\rceil \tag{5.11}
\end{equation*}
$$

where $p$ is the probability of success for Binomial Distribution $B(L, p)$ and $\lceil\cdot\rceil$ is the Ceil function which maps its argument to the smallest following integer. Each cluster is processed independently because of the semi-orthogonality between them.

## Step4: Finding $\mathbb{E}[\mathbf{x} \mid \mathbf{y}]$

After we have the dominant supports and their likelihood then we can find $\mathbb{E}[\mathbf{x} \mid \mathbf{y}]$ using (5.5) or (5.7) for each size of the support.

## Step5: Evaluating the Estimate of x

Finally using (5.4) we can find the $\hat{\mathbf{x}}_{M M S E}$ as we have all the necessary components determined.

After developing the mathematical model now we are ready to move ahead with the implementation of the algorithm. Section 5.2 discusses the TDOA geometries in different scenarios we have developed for implementing the impulsive acoustic source localization system using CC and OC methods for TDE.

### 5.2 Experimental Scenarios and Sensors Geometries

Fig 5.3 shows the experimental scenarios that we are taking into consideration for the implementation of our application. Broadly there are two scenarios: i) Indoor experiments and ii) Outdoor experiments. There are two different wireless sound acquisition systems: i) RevoLabs ${ }^{\circledR}$. Wireless HD Microphone System and ii) VocoPro ${ }^{\circledR}$ UHF8800 Wireless Microphone System. Three different TDOA geometries were considered to analyze not only the performance of OC/CC but also the effect of geometry on the efficiency of a source localization system. Furthermore, we considered two different scenarios in indoor experiments i.e. i) experimenting in the center of the hall and ii) experimenting in a corner of the hall to see the effect of reverberation and reflections on the performance of the system. Note that in Fig 5.3 we display three sampling rates i.e. $4 \mathrm{kHz}, 8 \mathrm{kHz}$ and 16 kHz but the

OC algorithm could not be run for the 16 kHz case due to its huge requirement of the PC memory. The available PC were not able to run the OC algorithm. Now we will discuss the sensor geometries in Section 5.2.1.


Figure 5.3: Different Scenarios Considered in the Experimentation

### 5.2.1 TDOA Geometries

In this section we discuss the sensor geometries to be used in the experimentations. There are three different geometries and they are discussed next.

## Pyramid Geometry

Fig. 5.4 shows the Pyramid geometry of five microphones. One of the microphones is at origin and has been taken as a reference for the remaining microphones. One of the sensors is on the $z$-axis (elevated) and the remaining three sensors are in the $x y$-plane at an angle of $120^{\circ}$ from each other. Although the array size can be scaled up or down but we have kept the sensors positions as follows to restrict the array to a $2 \times 2 \times 2 m^{3}$ space:
mic $0=a_{0}=(0,0,0), \quad$ mic1 $=a_{1}=(2,0,0)$,
$m i c 2=a_{2}=\left(2 \cos 120^{\circ}, 2 \sin 120^{\circ}, 0\right), \quad m i c 3=a_{3}=\left(2 \cos 240^{\circ}, 2 \sin 240^{\circ}, 0\right)$,
$\operatorname{mic4}=a_{4}=(0,0,0.72)$

Note that in the practical implementation (Fig 5.4c) the array ground was considered at 89 cm height from the real ground to avoid reflections from the ground and other effects of the ground as was discussed in Section 2.3.3.

To select source positions for the experimentation we selected locations which cover some important areas of the geometry. Since the geometry is symmetric around the origin, the results of these points will represent other areas of the geometry as well.

(a)

(b)

(c)

Figure 5.4: TDOA Pyramid Geometry with VocoPro System. (a) Pyramid Geometry 3D plot (b) Pyramid Geometry 2D plot (c) Pyramid Geometry, Indoor Experiment with VocoPro System

Fig. 5.5 shows the source locations (shown as green dots) that we have selected for our experimentation. These points will be used in all our experiments both in
indoor and outdoor scenarios. Table 5.1 shows these source locations with their description and mathematical representation.


Figure 5.5: Selection of source locations of Pyramid geometry for experimentation

Table 5.1: Source locations for Pyramid geometry experiments

| Source <br> Location | $\begin{aligned} & \left(\cos 60^{\circ},\right. \\ & \left.\sin 60^{\circ}, 0.5\right) \\ & =(0.5,0.866,0.5) \end{aligned}$ | $(0,0,1)$ | $\begin{aligned} & \left(2.5 \cos 60^{\circ}\right. \\ & \left.2.5 \sin 60^{\circ}, 0\right) \\ & =(1.25,2.16,0) \end{aligned}$ | $\begin{aligned} & \left(2 \cos 60^{\circ},\right. \\ & \left.2 \sin 60^{\circ}, 0\right) \\ & =(1,1.73,0) \end{aligned}$ | $(2.5,0,0)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Description | In-between mic1 and 2 inside the array at height of 0.5 m at $60^{\circ}$ | Above the center of the array | In-between mic1 \& 2, outside the array | In-between mic1 $\& 2$ on the circle inscribing the array. | Along the line (outside array) passing through mic1 and center of the array |

## Circular Geometry

Fig. 5.6 shows the arrangement of microphones which form a shape of circle when viewed from top. We cannot place all the sensors on a planer circle as then the $\Phi$ matrix discussed in Section 3.2.2 will become singular and no solution can be
found. The sensor (microphone) locations are:

$$
\begin{aligned}
& a_{0}=(0,0,0), \quad a_{1}=\left(r \cos 60^{\circ}, r \sin 60^{\circ}, 0.5\right) \\
& a_{2}=\left(r \cos 120^{\circ}, r \sin 120^{\circ}, 0\right), \quad a_{3}=\left(r \cos 180^{\circ}, r \sin 180^{\circ}, 0.5\right), \\
& a_{4}=\left(r \cos 240^{\circ}, r \sin 240^{\circ}, 0\right), \quad a_{5}=\left(r \cos 300^{\circ}, r \sin 300^{\circ}, 0.5\right)
\end{aligned}
$$

where $r=1.5 m$ is the radius of the circle. Since one of the microphones should be at the origin to satisfy the equations we developed in Section 3.2.2, we shifted the array along the $x$-axis by $-r$ such that mic0 would be at the origin and the array would be in two quadrants, in this case, it is in quadrant 2 and 3.

Note that in the practical implementation (Fig 5.6c) the array ground was considered at 89 cm height from the real ground to avoid reflections from the ground and other effects of the ground as was discussed in Section 2.3.3.

To select the source positions for the experimentation we selected locations which cover the important areas of the geometry. Fig. 5.7 shows the source locations (shown as green dots) that we have selected for our experimentation. These points will be used in all our experiments both in indoor and outdoor scenarios. Table 5.2 shows the source locations with their description and mathematical representation.

(a)

(b)

(c)

Figure 5.6: TDOA Circular Geometry with RevoLabs System. (a) Circular Geometry 3D plot (b) Circular Geometry 2D plot (c) Circular Geometry, Indoor Experiment with RevoLabs System

Table 5.2: Source locations for Circular geometry experiments

| Source Location | $\left(r \cos 30^{\circ}-r\right.$, <br> $\left.r \sin 30^{\circ}, 0\right)$ | $\left(r \cos 30^{\circ}-r\right.$, <br> $\left.r \sin 30^{\circ}, 1\right)$ | $(-2 r, 0,0)$ | $(-2 r, 0,0.5)$ | $(-3 r, 0,0)$ | $\left(2 r \cos 180^{\circ}-r\right.$, <br> $\left.2 r \sin 180^{\circ}, 0\right)$ | $\left(2 r \cos 60^{\circ}-r\right.$, <br> $\left.2 r \sin 60^{\circ}, 0.5\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Value | $(-0.2,0.7500,0)$ | $(-0.2,0.7500,1)$ | $(-3,0,0)$ | $(-3,0,0.5)$ | $(-4.5,0,0)$ | $(0,2.6,0.5)$ | $(0,2.6,1)$ |
| Description | In-between mic0 and <br> 1 on the <br> circumference at <br> height of 0 m |  <br> 2, outside the array <br> at height of 1 m | In-between <br> mic1 \& 2, <br> inside the <br> array at <br> height of 0 m | Along the line <br> (outside array) <br> passing through <br> mic1 and center of <br> the array at height <br> 0.5 m | Along the line <br> (inside array) <br> passing through <br> mic1 and center of <br> the array at height <br> 0 m | In-between mic0 <br> and 1 on the <br> circumference at <br> height of 0.5 m | Along the line (outside <br> array) passing through <br> mic1 and center of the <br> array at height of 1 m |



Figure 5.7: Selection of source locations of Circular geometry for experimentation

## Rhombus Geometry

This geometry is a modified version of the Pyramid geometry. We added an extra sensor to the bottom of the array and elevated them by 0.5 m while mic0 remained at the origin. The array converts to a rhombus after this modification as shown
in Fig. 5.8. The sensor (microphone)locations are:

$$
\begin{aligned}
& a_{0}=(0,0,0), \quad a_{1}=(1.5,0,0.5), \quad a_{2}=(0,1.5,0.5), \\
& a_{3}=(-1.5,0,0.5), a_{4}=(0,-1.5,0.5), a_{5}=(0,0,1)
\end{aligned}
$$

Note that in the practical implementation (Fig 5.8c) the array ground was considered at 39 cm height from the real ground to avoid reflections from the ground and other effects of the ground as was discussed in Section 2.3.3. This elevation of 39 cm for Rhombus geometry is half of the elevation we chose for Pyramid and Circular geometries because of the limited height of the microphone stands. Here the base of the geometry is $a_{0}$ while the highest sensor $a_{5}$ is at elevation of $1 m$ from the base of the geometry. As we will see in Chapter 6 and 7 this reduced elevation of the Rhombus geometry has significant effect on the accuracy of the geometry.

To select the source positions for the experimentation we selected locations which cover the important areas of the geometry. Fig. 5.9 shows the source locations (shown as green dots) that we have selected for our experimentation. These points will be used in all our experiments both in indoor and outdoor scenarios. Table 5.3 shows the source locations with their description and mathematical representation.

(a)

(b)

(c)

Figure 5.8: TDOA Rhombus Geometry with RevoLabs System. (a) Rhombus Geometry 3D plot (b) Rhombus Geometry 2D plot (c) Rhombus Geometry, Indoor Experiment with RevoLabs System

Table 5.3: Source locations for Rhombus geometry experiments

| Source Location | $(2 \mathrm{r}, 0, \mathrm{~h})$ | $(2 \mathrm{r}, 0,2 \mathrm{~h})$ | $\left(2 r \cos 45^{\circ}\right.$, <br> $\left.2 r \sin 45^{\circ}, 2 h\right)$ | $\left(2 r \cos 75^{\circ}\right.$, <br> $\left.2 r \sin 75^{\circ}, h\right)$ | $\left(2 r \cos 88^{\circ}\right.$, <br> $\left.2 r \sin 88^{\circ}, h\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Value | $(3,0,0.5)$ | $(3,0,1)$ | $(2.12,2.12,1.00)$ | $(0.77,2.89,0.5)$ | $(0.10,2.99,0.5)$ |
| Description | On the line <br> passing through <br> mic1 and center <br> of the array at <br> height $0.5 m$ | On the line <br> passing through <br> mic1 and center of <br> the array at height <br> 1m | In-between mic1 <br> and 2 outside the <br> circumference on <br> which mics ly. | At angle of 75 <br> between mic1 \& 2. | At angle of $88^{\circ}$ <br> between mic1 \& 2. |



Figure 5.9: Selection of source locations of Rhombus geometry for experimentation

### 5.3 Hardware Systems

As discussed in Chapter 4 we tried to implement our acoustic source localization system on WSN but because of the issues encountered and the HW limitations we could not continue with that implementations. To verify the OC algorithm and compare its performance with CC TDE method we chose two different wireless
microphone systems for signal acquisition in the indoor and outdoor environments. Both of these systems are for commercial use like in meeting rooms, music concerts etc. These hardware systems are discussed next.

### 5.3.1 RevoLabs ${ }^{\circledR}$ Wireless HD Microphone System

This is an 8 -channel wireless microphone system (shown in Fig. 5.10) with advanced features. Its specifications are [39]:

1. Audio Bandwidth: $50 \mathrm{~Hz}-20 \mathrm{kHz}$
2. Radio Frequency: $1.88-1.90 \mathrm{GHz}$
3. Ethernet - RJ45
4. Rechargeable batteries powered microphones, battery life $=8$ hours.
5. Range of Operation: $300 \mathrm{ft} .=91 \mathrm{~m}$.
6. Impervious to RF interference due to RF Armor technology.
7. Omni-directional wireless microphones

The basestation provides the output through a Mini Phoenix Connector for each channel (mic).

### 5.3.2 VocoPro ${ }^{\circledR}$ UHF8800 Wireless Microphone System

UHF-8800 [40] is an 8-channel wireless microphone system that is produced by VocoPro ${ }^{\circledR}$. The system consists of a receiver basestation and 8 microphones as

Executive HD Omni-
directional Wireless Microphone


Figure 5.10: RevoLabs HD Wireless Microphone System
shown in Fig. 5.11. Its features are:

1. UHF Band Operation
2. 8 XLR Microphone Outputs
3. Frequency bands of the 8 channels: $\mathrm{M}=656.825 \mathrm{MHz}, \mathrm{N}=685.96 \mathrm{MHz}$, $\mathrm{O}=694.11 \mathrm{MHz}, \mathrm{P}=629.40 \mathrm{MHz}, \mathrm{Q}=676.74 \mathrm{MHz}, \mathrm{R}=614.15 \mathrm{MHz}, \mathrm{S}$ $=619.12 \mathrm{MHz}$.
4. Receiver's Frequency Response: $40 \mathrm{~Hz}-16 \mathrm{kHz}$.
5. Receiver's Max. Output Level: Balanced: 0-400mV, Unbalanced: 0 200mV
6. Receiver's spurious rejection: 75 dB typical


Figure 5.11: VocoPro UHF8800 Wireless Microphone System
7. Transmitter Power: 30 mV
8. Transmitter Spurious Emission: $<40 \mathrm{~dB}$ (with carrier)
9. Transmitter Battery Voltage: Two AA 1.5 V , Battery Life: 12 hours

The microphones of this system are directional and are specifically designed for vocals thus their sensitivity is quite low than RevoLabs microphones. This feature has special effects on the experimentation and the results as we will discuss in Chapter 6 and 7 in detail.

### 5.3.3 Data Acquisition Setup

The VocoPro system provides output through XLR balanced audio jacks while the RevoLabs system provides output through Mini Phoenix connectors. For both


Figure 5.12: MCC's DaqBoard/2000 Data Acquisition PCI Card
of the systems a data acquisition (DAQ) device is needed that converts analog signals to digital and presents the data in an acceptable form to the processing environment like MATLAB. For this purpose we use two different DAQ systems: i) DaqBoard/2000 along with DBK202 [41] and ii) USB1608FS USB based DAQ card [42]. Both of the boards are from Measurement Computing Corporation $\left(\mathrm{MCC}^{\circledR}\right)$.

The DaqBoard/2000 (shown in Fig. 5.12 is fully support by MATLAB and we can acquire data directly from the board. The maximum sampling frequency of the board is 200 kHz accumulative for all channels. A maximum of 16 single-ended analog/digital channels can be sampled. Additional hardware can be attached to the P4 connector through the CA-195 cable for ease of signal acquisition, for example, we are using DBK202 [41] adapter (shown in Fig. 5.13).

The DaqBoard/2000 can be attached to a PC having a PCI expansion card


Figure 5.13: MCC's DBK202 Expansion Card
only. Thus it cannot be connected to a laptop limiting its mobility. Furthermore, we tested the DabBoard/2000 for data acquisition and we found that there is heavy coupling between adjacent channels. Fig. 5.14 shows such a test in which we connected the output of a microphone of RevoLabs system to channel 0 of the DaqBoard. All other channels of the DaqBoard were open and no signals were connected to them. Fig. 5.14 clearlys shows that there is coupling between channel 0 and 1. Besides that the DaqBoard adds an unwanted bias to the signals deteriorating the shape of the signal which affects the results of the TDE algorithms.

We decided to use USB1608FS DAQ shown in Fig. 5.15 from the same company. We tested it and there were no issues found which were found in the case of DaqBoard. Furthermore, the USB1608FS DAQ is a USB device and small in size which can easily be connected to a laptop and thus very portable, especially helpful in outdoor experiments. USB1608FS can support up to 16 single-ended analog channels with 100 kHz maximum sampling rate for all channels accumulative. Since we are using a maximum of six microphones in our experiments we can easily sample each mic at 16 kHz sampling rate which is enough for our


Figure 5.14: Signal acquired from DaqBoard/2000 with channel 0 connected to a microphone and channel 1-7 unconnected to any signal but are open.
application.


Figure 5.15: MCC's USB1608FS USB Data Acquisition Board

The next step was to connect the outputs of RevoLabs and VocoPro bases-
tations to USB1608FS properly. As was mentioned earlier, the output of the RevoLabs system is provided through Mini Phoenix connectors. We connected the signal and ground wire of the Mini Phoenix to USB1608FS directly as shown in Fig. 5.16a while for the VocoPro system we have to use two additional connectors: first an XLR to standard Audio Jack and then Audio Jack to 3.5 mm 5-pin Stereo Jack (SJ-3535NGS) converter produced by Digikey. Fig. 5.16b shows the connection of UHF8800 connections to USB1608FS. After setting up successfully the hardware system and TDOA geometries in MATLAB we headed towards experimentations and the detailed results are given in Chapter 6 and 7.

### 5.3.4 Computing Platform

Because of the extensive amount of experiments and their evaluation we needed to use several computers to process the data using the OC algorithm. There were two kinds of computers:

1. Dell ${ }^{\circledR}$ 's Precision T1500 with the following specifications:

- Processor: Intel ${ }^{\circledR}$ Core $^{T M}$ i7
- Memory (RAM): 8 GB
- Operating System: Microsoft ${ }^{\circledR}$ Windows 7

2. Dell ${ }^{\circledR}$ 's Precision T1500 with the following specifications:

- Processor: Intel ${ }^{\circledR}$ Core $^{T M}$ i5
- Memory (RAM): 4 GB


Figure 5.16: USB1608FS connection to: a) RevoLabs system (b) VocoPro system

- Operating System: Microsoft ${ }^{\circledR}$ Windows 7

We will refer to the first computer as Fast Computer and to the second one as Slow Computer in our results in the rest of this thesis.

### 5.4 Conclusions

In this chapter we introduced the OC algorithm and its detailed steps. All the experimental scenarios were described in detail and the TDOA geometries that we will be using in our indoor and outdoor experiments were presented. Moreover, the target locations we have chosen for our experimentation were also explained. The data acquisition setup including the wireless microphone systems, data acquisition boards and the processing platforms were illustrated and their features were highlighted.

## CHAPTER 6

## INDOOR EXPERIMENTS AND

## RESULTS

In this chapter we discuss and present the detailed analysis and results of the indoor experimentation conducted.There are several scenarios for indoor experimentation. We draw a part of Fig. 5.3 again here in Fig. 6.1 to show the indoor experimentation scenarios investigated in this chapter.

Before discussing the experimental results, it is better to first simulate the TDOA geometries for the source locations specified in Section 5.2.1 in order to compare them with experimental results. We provide the parametric analysis of the OC algorithm in Section 6.1. Section 6.2 discusses the indoor experiments and results using RevoLabs wireless microphone system while Section 6.3 discusses the indoor experiments and results using VocoPro wireless microphone system. Section 6.4 concludes this chapter.


Figure 6.1: Indoor experiments scenarios

Note that in Fig. 6.1 we show the 16 kHz case but we were not able to run the OC algorithm on the available PCs due to the huge amount of memory required for OC for the case of 16 kHz sampling rate. The signals were acquired at 16 kHz sampling rate only for the Dictionary matrix $(\Psi)$ development.

### 6.1 Parametric Analysis of the OC Algorithm

In this section we want to analyze the variation effects of different parameters on the results of the OC algorithm. The parameters investigated are:

1. The Dictionary matrix $\Psi$
2. The index of CIR used to calculate the TDOA
3. The Probability of nonzero values $(p)$ in the CIR
4. Signal Variance ( $\sigma_{i m p}$ )
5. Noise Variance $\left(N_{0}\right)$

We chose the Pyramid geometry discussed in Section 5.2.1 for this analysis (we chose this geometry randomly as we could choose any other). Pyramid geometry has fives sensors (numbered from $0-4$ ). The case of indoor experiment in the center of the hall was taken and the sampling rate for signal capture was 8 kHz . We used RevoLabs HD Wireless Microphone System for acoustic signal acquisition with Measurement Computing (MCC) USB1608FS data acquisition card.

Now we will discuss these parametric analysis one by one in the following pages.

### 6.1.1 Effect of $\Psi$ on the results

The Dictionary matrix $\Psi$ plays very important role in the accuracy of the results of the OC algorithm. In this section we will show that the algorithm is very sensitive to the $\Psi$ which limits the practicality of the algorithm. As was discussed in Section 5.1.1 the $\Psi$ columns consist of delayed versions of a signal. We captured five different signals at different locations and scenarios at 16 kHz and developed $\Psi$ from them. Then using the Pyramid geometry and the experimental setup described in chapter 5 we conducted several experiments to see the effect of $\Psi$ on the results. It is to be noted that we captured the signal at 16 kHz for Dictionary building but when we carried out the experiment for localization we used 8 kHz thus we downsample the $\Psi$ to 8 kHz for successful operation of the algorithm. The results are discussed next.

## $\Psi$ Based on a Signal Captured in a Big Hall $\left(\Psi_{0}\right)$

We used the $\Psi$ matrix based on a signal captured in the middle of a big hall (whose dimensions were larger than $10 \times 15 \mathrm{~m}^{2}$ ) thus there were almost no reverberations. This $\Psi$ was adapted from [6]. Table 6.1 gives details of the results when we run the algorithm using this Dictionary. The top row of Table 6.1 represents the source locations we discussed in Section 5.2.1. TDE ${ }_{O C}$ is Time Delay Estimate (TDE) using Orthogonal Clustering (OC) algorithm and $X_{O C}$ is the source location estimate using OC. MSE stands for Mean Square Error ( $\epsilon$ ) which
is calculated using

$$
\begin{equation*}
\epsilon_{O C}=\sqrt{\left(x_{s}-x_{s}^{o c}\right)^{2}+\left(y_{s}-y_{s}^{o c}\right)^{2}+\left(z_{s}-z_{s}^{o c}\right)^{2}} \tag{6.1}
\end{equation*}
$$

and $\tau_{i j}$ is the time delay between mic $i$ and $j$.
Table 6.1: Results for 8 kHz case of Triangular geometry when array was placed in the center of the hall using $\Psi_{0}$. All the measurements are in meters

| Source <br> Location | $(0.5,0.866,0.5)$ | $(0,0,1)$ | $\begin{gathered} \left(2.5 \cos 60^{\circ}, 2.5 \sin 60^{\circ},\right. \\ 0)=(1.25,2.16,0) \end{gathered}$ | $\begin{gathered} \left(2 \cos 60^{\circ}, 2 \sin 60^{\circ}, 0\right)= \\ (1,1.73,0) \end{gathered}$ | $(2.5,0,0)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Description | In-between micl and 2 inside the array at height of 0.5 m at $60^{\circ}$ | Above the center of the array | In-between mic $1 \& 2$, outside the array | In-between mic $1 \& 2$ on the circle inscribing the array. | Along the line (outside array) passing through micl and center of the array |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}\right. \end{gathered}$ | $\begin{aligned} & (0.0020,0.0020, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{array}{lr} (0.0036, & 0.0036, \\ 0.0036, & -0.0021) \end{array}$ | $\begin{array}{cc} (-0.0006, & -0.0006, \\ 0.0059, & 0.0003) \end{array}$ | $\begin{array}{cc} (0, \quad 0.0000,0.0059 \\ 0.0004) \end{array}$ | $\left(\begin{array}{cc} (-0.0059, & 0.0041, \quad 0.0041, \\ 0.0003) \end{array}\right.$ |
| $\begin{aligned} & T D E_{O C} \\ & \left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c}\right. \end{aligned}$ | $\begin{array}{cc} (0.0019, & 0.0006 \\ 0.0040, & -0.0009) \end{array}$ | $\begin{array}{lr} (0.0031, & 0.0018 \\ 0.0046, & -0.0008) \end{array}$ | $\begin{array}{cc} (-0.0010, & -0.0005, \\ 0.0041, & -0.0014) \end{array}$ | $\begin{array}{cc} (0.0047, & 0.0011, \\ 0.0071, & 0.0024) \end{array}$ | $\left.\begin{array}{cc} (-0.0018, & 0.0030, \\ 0.0020 \end{array}\right)$ |
| $\begin{aligned} & X_{O C} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (0.1990,0.9873, \\ 1.2052) \end{gathered}$ | $\begin{gathered} (0.0562, \quad 0.6572 \\ 0.7559) \end{gathered}$ | $\begin{gathered} (1.9129,2.7945, \\ 3.8052) \end{gathered}$ | $\begin{gathered} (0.0395,1.0509, \\ -0.5213) \end{gathered}$ | $\begin{gathered} (2.2769,-0.5339 \\ -4.2958) \end{gathered}$ |
| MSE for OC | 0.7763 | 0.7033 | 3.9143 | 1.2867 | 4.3346 |
| Run Time (Sec) | 38.345 | 35.4579 | 44.5371 | 66.0748 | 39.8441 |

## $\Psi$ Based on a Signal Captured in a relatively Small Hall with Source

 being Near a Wall $\left(\Psi_{1}\right)$The signal that was used to build this Dictionary was captured from an unloaded gunshot at 16 kHz ; the sensor was 3 m away from the wall. The source was 160 cm away from the sensor and in the same plane in which the sensor was lying. Fig. 6.2 shows the plot of the captured signal. Table 6.2 displays the results when the $\Psi_{1}$ was used.


Figure 6.2: Indoor Unloaded Gunshot at 16 kHz near the wall captured using RevoLabs System

Table 6.2: Results for the case of $\Psi_{1}$

| Source <br> Location | $(0.5,0.866,0.5)$ | $(0,0,1)$ | $\begin{gathered} \left(2.5 \cos 60^{\circ}, 2.5 \sin 60^{\circ},\right. \\ 0)=(1.25,2.16,0) \end{gathered}$ | $\begin{gathered} \left(2 \cos 60^{\circ}, 2 \sin 60^{\circ}, 0\right)= \\ (1,1.73,0) \end{gathered}$ | $(2.5,0,0)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Description | In-between mic1 and 2 inside the array at height of 0.5 m at $60^{\circ}$ | Above the center of the array | In-between mic $1 \& 2$, outside the array | In-between mic1 \& 2 on the circle inscribing the array. | Along the line (outside array) passing through mic1 and center of the array |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{4}\right. \end{gathered}$ | $\begin{aligned} & (0.0020,0.0020, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{array}{lr} (0.0036, & 0.0036, \\ 0.0036, & -0.0021) \end{array}$ | $\begin{array}{cc} (-0.0006, & -0.0006 \\ 0.0059, & 0.0003) \end{array}$ | $\begin{gathered} (0, \quad 0.0000, \quad 0.0059, \\ 0.0004) \end{gathered}$ | $(-0.0059,0.0041,0.0041,0.0003)$ |
| $\begin{aligned} & T D E_{O C} \\ & \left(\tau_{\mathbf{1 0}}^{o c}, \tau_{\mathbf{2 0}}^{o c}, \boldsymbol{\tau}_{\mathbf{3 0}}^{o c}, \boldsymbol{\tau}_{\mathbf{4}}^{o}\right. \end{aligned}$ | $\begin{array}{ll} (0.0016, & 0.0010, \\ 0.0054, & -0.0011) \end{array}$ | $\begin{array}{cc} (0.0006, & -0.0010, \\ 0.0018, & -0.0049) \end{array}$ | $\begin{array}{cc} (-0.0030, & -0.0027, \\ 0.0014, & 0.0001) \end{array}$ | $\begin{array}{cc} (-0.0009, & -0.0001, \\ 0.0041, & -0.0027) \end{array}$ | $(-0.0015,0.0021,0.0027,-0.0008)$ |
| $\begin{aligned} & X_{O c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | (0.5053, 1.1157, 1.0630) | $\begin{gathered} (-0.3164,3.3499 \\ 26.7301) \end{gathered}$ | $\begin{gathered} (-0.9516,-1.4374, \\ 0.5545) \end{gathered}$ | $\begin{gathered} (1.6739,2.2354, \\ 5.8290) \end{gathered}$ | $\begin{gathered} (2.0843,0.3273, \\ 1.9111) \end{gathered}$ |
| MSE for OC | 0.6160 | 25.9492 | 4.2539 | 5.8895 | 1.9830 |
| $\begin{gathered} \hline \text { OC Time } \\ (\mathrm{Sec}) \end{gathered}$ | 57.2618 | 48.4149 | 88.6293 | 49.1725 | 42.1681 |

## $\Psi$ Based on a Signal Captured in a relatively Small Hall with source being in the middle of the hall and near the sensor $\left(\Psi_{2}\right)$

The signal shown in Fig. 6.3 for this Dictionary was captured in the same hall and same equipment was used as in the previous subsection but this time the source was in the middle of the hall. The source was at 10 cm height just right on top of the sensor. Please note the effect of the source being near the sensor. There are more peaks in this case than the case of $\Psi_{1}$. Table 6.3 shows the results when $\Psi_{2}$ was used with the OC algorithm.


Figure 6.3: Indoor Unloaded Gunshot at 16 kHz using RevoLabs System when Source was in the middle of the hall and near the sensor

Table 6.3: Results for the case of $\Psi_{2}$

| Source <br> Location | $(0.5,0.866,0.5)$ | $(\mathbf{0}, \mathbf{0}, \mathbf{1})$ | $\begin{gathered} \left(2.5 \cos 60^{\circ},\right. \\ \left.2.5 \sin 60^{\circ}, 0\right)=(1.25, \\ 2.16,0) \end{gathered}$ | $\begin{gathered} \left(2 \cos 60^{\circ}, 2 \sin 60^{\circ}, 0\right)= \\ (1,1.73,0) \end{gathered}$ | $(2.5,0,0)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Description | In-between micl and 2 inside the array at height of 0.5 m at $60^{\circ}$ | Above the center of the array | In-between mic1 \& 2, outside the array | In-between mic1 \& 2 on the circle inscribing the array. | Along the line (outside array) passing through micl and center of the array |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30},\right. \end{gathered}$ | $\begin{array}{cc} (0.0020, & 0.0020, \\ 0.0057, & -0.0003) \end{array}$ | $\begin{array}{cc} (0.0036, & 0.0036, \\ 0.0036, & -0.0021) \end{array}$ | $\begin{array}{cc} (-0.0006, & -0.0006, \\ 0.0059, & 0.0003) \end{array}$ | $\begin{gathered} (0,0.0000, \quad 0.0059, \\ 0.0004) \end{gathered}$ | $\left(-0.0059, \begin{array}{cc} 0.0041, & 0.0041, \\ 0.0003 \end{array}\right)$ |
| $\begin{aligned} & \text { TDE }{ }_{o C} \\ & \left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c},\right. \end{aligned}$ | $\begin{array}{cc} (0.0049, & 0 \\ 0.0073, & 0.0027) \end{array}$ | (0.0076, 0.0027, <br> $0.0106, \quad 0.0049$ ) | $\begin{array}{cc} (0.0056, & 0.0027, \\ 0.0094, & 0.0039 \end{array}$ | $\begin{array}{cc} (-0.0005, & 0.0001, \\ 0.0031, & 0.0018) \end{array}$ | $\left(-0.0015, \begin{array}{cc} 0.0015, & 0.0025, \\ 0.0032 \end{array}\right)$ |
| $\begin{aligned} & X_{O c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (-0.0061,1.1512, \\ -0.7474) \end{gathered}$ | $\begin{gathered} (0.1045,1.2895, \\ -0.1541) \end{gathered}$ | $\begin{gathered} (0.2989,1.1953, \\ -0.4373) \end{gathered}$ | $\begin{gathered} (1.4855,1.8696, \\ -4.6764) \end{gathered}$ | $\begin{gathered} (2.5486,0.6878, \\ -10.1994) \end{gathered}$ |
| MSE for OC | 1.3760 | 1.7337 | 1.4236 | 4.7036 | 10.2227 |
| OC Time (Sec) | 61.1333 | 58.7058 | 53.7054 | 48.9618 | 205.5077 |

## $\Psi$ Based on a Signal Captured Outdoor when Source was Far from the

Sensor $\left(\Psi_{3}\right)$

The signal that was used to build the $\Psi_{3}$ was captured from an unloaded gunshot at 16 kHz ; the sensor was placed in an outdoor environment. The source was 2 m away from the sensor and in the same plane in which the sensor was lying.

Fig. 6.4 shows the plot of the captured signal. Table 6.4 displays the results when $\Psi_{3}$ was used on the data for Triangular geometry for 8 kHz case and array being in the center of the hall.

Table 6.4: Results for the case of $\Psi_{3}$

| Source <br> Location | $(0.5,0.866,0.5)$ | $(0,0,1)$ | $\begin{gathered} \left(2.5 \cos 60^{\circ}, 2.5 \sin 60^{\circ},\right. \\ 0)=(1.25,2.16,0) \end{gathered}$ | $\begin{gathered} \left(2 \cos 60^{\circ}, 2 \sin 60^{\circ}, 0\right)=(1, \\ 1.73,0) \end{gathered}$ | $(\mathbf{2 . 5}, \mathbf{0}, 0)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Description | In-between micl and 2 inside the array at height of 0.5 m at $60^{\circ}$ | Above the center of the array | In-between mic $1 \& 2$, outside the array | In-between micl \& 2 on the circle inscribing the array. | Along the line (outside array) passing through micl and center of the array |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{4}\right. \end{gathered}$ | $\begin{array}{ll} (0.0020, & 0.0020, \\ 0.0057, & -0.0003 \end{array}$ | $\begin{array}{cc} (0.0036, & 0.0036, \\ 0.0036, & -0.0021) \end{array}$ | $\begin{array}{cc} (-0.0006, & -0.0006, \\ 0.0059, & 0.0003) \end{array}$ | $\begin{gathered} (0, \quad 0.0000, \quad 0.0059, \\ 0.0004) \end{gathered}$ | (-0.0059, 0.0041, 0.0041, 0.0003) |
| $\begin{aligned} & \text { TDE }{ }_{O C} \\ & \left(\boldsymbol{\tau}_{\mathbf{1 0}}^{o c}, \boldsymbol{\tau}_{\mathbf{2 0}}^{o c}, \boldsymbol{\tau}_{\mathbf{3 0}}^{o c}, \boldsymbol{\tau}_{4}^{o}\right. \end{aligned}$ | $\begin{array}{cc} (0.0040, & 0.0016, \\ 0.0057, & 0.0003) \end{array}$ | $\begin{array}{cr} (0.0026, & 0.0004, \\ 0.0050, & -0.0013) \end{array}$ | $\begin{array}{cc} (-0.0004, & -0.0006, \\ 0.0040, & 0.0022) \end{array}$ | $\begin{array}{cc} (0.0004, & -0.0003, \\ 0.0044, & 0.0013) \end{array}$ | $(-0.0027,0.0022,0.0032,0.0010)$ |
| $\begin{aligned} & X_{O C} \\ & \left(\boldsymbol{x}_{s}^{o c}, \boldsymbol{y}_{s}^{o c}, \boldsymbol{Z}_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (0.0081,0.8229, \\ 0.2631) \end{gathered}$ | $\begin{gathered} (0.1202,1.1071, \\ 1.1349) \end{gathered}$ | $\begin{gathered} (1.3112,2.5055, \\ -5.3011) \end{gathered}$ | $\begin{gathered} (0.7925,1.7668, \\ -1.6489) \end{gathered}$ | $\begin{gathered} (3.1113,0.5809, \\ -2.0737) \end{gathered}$ |
| MSE for OC | 0.5477 | 1.1218 | 5.3127 | 1.6623 | 2.2386 |
| OC Time (Sec) | 47.5013 | 43.8546 | 49.3129 | 60.1322 | 40.7117 |



Figure 6.4: Outdoor Unloaded Gunshot at 16 kHz using RevoLabs System when Source was Far from the Sensor

## $\Psi$ Based on a Signal Captured Outdoor when Source was Near the

 Sensor $\left(\Psi_{4}\right)$$\Psi_{4}$ was built using a signal captured outdoor using same environment and equipment as in the previous section but this time the source was 10 cm away from the sensor and in the same plane in which the sensor was lying. Fig. 6.5 shows the plot of the captured signal and Table 6.5 shows the results when we used $\Psi_{4}$ with the OC algorithm.


Figure 6.5: Outdoor Unloaded Gunshot at 16 kHz using RevoLabs System when Source was near to the Sensor

Table 6.5: Results for the case of $\Psi_{4}$

| Source Location | $(0.5,0.866,0.5)$ | $(0,0,1)$ | $\begin{gathered} \left(2.5 \cos 60^{\circ}, 2.5 \sin 60^{\circ}, 0\right) \\ =(1.25,2.16,0) \end{gathered}$ | $\begin{gathered} \left(2 \cos 60^{\circ}, 2 \sin 60^{\circ}, 0\right)=(1, \\ 1.73,0) \end{gathered}$ | $(2.5,0,0)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Description | In-between mic 1 and 2 inside the array at height of 0.5 m at $60^{\circ}$ | Above the center of the array | In-between micl \& 2, outside the array | In-between mic $1 \& 2$ on the circle inscribing the array. | Along the line (outside array) passing through mic1 and center of the array |
| $\begin{gathered} \text { Exact TDs } \\ \left(\boldsymbol{\tau}_{10}, \tau_{20}, \tau_{30}, \tau_{4}\right. \end{gathered}$ | $\begin{array}{lr} (0.0020, & 0.0020, \\ 0.0057, & -0.0003) \end{array}$ | $\begin{array}{lr} (0.0036, & 0.0036, \\ 0.0036, & -0.0021) \end{array}$ | $\begin{array}{cc} (-0.0006, & -0.0006, \\ 0.0059, & 0.0003) \end{array}$ | $\begin{gathered} (0, \quad 0.0000, \quad 0.0059, \\ 0.0004) \end{gathered}$ | $(-0.0059, \quad 0.0041, \quad 0.0041,0.0003)$ |
| $\begin{aligned} & \text { TDE } E_{O C} \\ & \left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c}, \tau_{4}^{o}\right. \end{aligned}$ | $\begin{array}{lr} (0.0059, & 0.0011, \\ 0.0088, & -0.0003) \end{array}$ | $\begin{array}{cc} (0.0025, & 0.0043, \\ 0.0051, & -0.0010) \end{array}$ | $\begin{array}{cc} (0.0008, & -0.0019, \\ 0.0027, & -0.0011) \end{array}$ | $\left(\begin{array}{lll} (0.0043, & 0.0037, & 0.0095, \\ 0.0047) \end{array}\right.$ | $(-0.0035,0.0015,0.0022,-0.0001)$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (0.0945,1.1874, \\ 0.3441) \end{gathered}$ | $\begin{gathered} (0.4955,0.2023, \\ 0.6396) \end{gathered}$ | $\begin{gathered} (-0.2456,4.4444 \\ 5.3807) \end{gathered}$ | $\begin{gathered} (0.6083,1.1694, \\ -1.0467) \end{gathered}$ | $\begin{gathered} (34.7310,4.2639 \\ 3.7402) \end{gathered}$ |
| MSE for OC | 0.5404 | 0.6453 | 6.0338 | 1.2503 | 32.7262 |
| OC Time (Sec) | 60.4040 | 52.9025 | 55.8619 | 48.4347 | 62.7220 |

## Selection of Preferred $\Psi$

Looking at the results in Table 6.1 to 6.5 we observe that other than the two specific source locations $(1.25,2.16,0)$ and $(2.5,0,0)$ the Dictionary $\Psi_{4}$ has the least error for OC compared to other dictionaries. The least runtime on averages is observed for $\Psi_{0}$ but its MSE is more than the $\Psi_{4}$ in for three out of five source
locations ( $60 \%$ ). Thus we will use this Dictionary onward in our experiments.

### 6.1.2 The index of CIR used to calculate the TDOA

We carried out an experiment to decide how to calculate correct TDOA for OC algorithm. The values of different parameters of the algorithm were: $N_{0}=1.5 \times$ $10^{-4}, \sigma_{i m p}=1, p=5$ which were chosen based on the experimental readings. We chose two different conditions for index selection for the purpose of TDOA calculation:

1. Using the index of first nonzero value of CIR to calculate TDOA
2. Using the index of maximum value of CIR to calculate TDOA

Table 6.6 shows the results when we used both the aforementioned conditions along with the comments in the last column. For three out of five source locations the choice of index of the maximum amplitude produces more correct results compared to the choice of index of first nonzero value of the CIR.

Table 6.6: Index choice for TDOA calculation

| Source Location | Exact TDOA | TDOA based on Maximum Amplitude | TDOA based on first nonzero value | Comments |
| :---: | :---: | :---: | :---: | :---: |
| (0.5, 0.866, 0.5) | $\begin{aligned} & \hline(0.0020,0.0020, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{gathered} (0.005,0.0011, \\ 0.0088,-0.0003) \end{gathered}$ | $\begin{array}{cc} \hline(0.0022, & 0.0011, \\ 0.0056, & -0.00025) \end{array}$ | First nonzero based TDOA is more correct compared to the Max. Amp case |
| $(0,0,1)$ | $\begin{array}{ll} \hline(0.0036, & 0.0036, \\ 0.0036, & -0.0021) \end{array}$ | $\begin{array}{cc} \hline(0.0025, & 0.0043, \\ 0.0051, & -0.0010) \end{array}$ | $\begin{array}{ll} \hline(0.0027, & -0.0034, \\ 0.0053, & -0.0010) \end{array}$ | Max. Amp based TDOA is more correct compared to the First Nonzero case |
| (1.25, 2.16, 0) | $\begin{array}{cc} \hline(-0.0006, & -0.0006, \\ 0.0059, & 0.0003) \end{array}$ | $\begin{array}{ll} \hline(0.0008, & -0.0019, \\ 0.0027, & -0.0011) \end{array}$ | $\begin{array}{cc} \hline(0.0075, & 0.0047, \\ 0.0094, & 0.0056) \end{array}$ | Max. Amp based TDOA is more correct compared to the First Nonzero case |
| (1, 1.73, 0) | $\begin{array}{cc} \hline(0, & 0.0000, \\ 0.0059, & 0.0004) \end{array}$ | $\begin{array}{ll} \hline(0.0043, & 0.0037, \\ 0.0095, & 0.0047) \end{array}$ | $\begin{array}{cc} \hline(0.0032, & 0.0029, \\ 0.0044, & -0.0035) \end{array}$ | Max. Amp based TDOA is more correct compared to the First Nonzero case |
| $(2.5,0,0)$ | $\begin{gathered} (-0.0059, \\ 0.00041, \\ 0.0041, \\ \hline \end{gathered}$ | $\begin{array}{ll} \hline(-0.0035, & 0.0015, \\ 0.0022, & -0.0001) \end{array}$ | $\begin{array}{cc} \hline(-0.0043, & 0.0016, \\ 0.0025, & 0) \end{array}$ | First nonzero based TDOA is more correct compared to the Max. Amp case |

### 6.1.3 Effect of Probability of Impulses ( $p$ )

We conducted another experiment which deals with the probability of impulses in a CIR signal $(p)$ which is equal to the expected non-zero values in the CIR divided by the length of the CIR. We used index of maximum value of CIR for TDOA calculation. Other parameters were kept as follows:

$$
\sigma_{i m p}=0.5, N_{0}=1.5 \times 10^{-4}, c=340 \mathrm{~m} / \mathrm{s}
$$

where $c=340 \mathrm{~m} / \mathrm{s}$ is the speed of sound, $N_{0}$ is the noise variance and $\sigma_{i m p}$ is the variance of the source signal. We chose the values of $p$ in the range of $3-15$ as it covers the expected number of reflections for both of the indoor and outdoor experimentation. The speed of sound (c), in our case, is constant because during our experimentation the temperature range was $15-25{ }^{\circ} \mathrm{C}$ which corresponds to the speed of sound in the range $340.31-346.18 \mathrm{~m} / \mathrm{s}$. Using this range of the speed of sound the time delay for 1 m distance is almost constant and is equal to 0.0029 seconds. So we can safely choose $c=340 \mathrm{~m} / \mathrm{s}$. Table 6.7 shows the results which tell us that changing the value of $p$ has no effect on the results at all. Instead it increases the run time for the algorithm significantly. In other words, the algorithm does not care about what value of $p$ we provide to it, it looks for the presence of the dictionary signal (of which $\Psi$ is made of) or its reflected version in the signal of a sensor.

Table 6.7: Effect of change in $p$ on the results of the algorithm

| $p$ | Source <br> Location | Description | Exact TDs $\left(\boldsymbol{\tau}_{10}, \boldsymbol{\tau}_{20}, \boldsymbol{\tau}_{30}, \boldsymbol{\tau}_{40}\right)$ | $\begin{aligned} & T D E_{c c} \\ & \left(\tau_{10}^{c}, \tau_{20}^{c c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{aligned} & T D E_{O C} \\ & \left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c}, \tau_{40}^{o c}\right) \end{aligned}$ | $\begin{aligned} & X_{C c} \\ & \left(x_{s}^{\tau c}, y_{s}^{c c}, z_{s}^{c c}\right) \end{aligned}$ | $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{aligned} & \text { MSE } \\ & \text { for CC } \end{aligned}$ | $\begin{aligned} & \text { MSE } \\ & \text { for OC } \end{aligned}$ | CC <br> Time <br> (Sec) | $\underset{(\mathrm{Sec})}{\mathrm{OC} \text { Time }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3 | $\begin{gathered} (0.5, \\ 0.866, \\ 0.5) \end{gathered}$ | In-between mic1 and 2 inside the array at height of 0.5 m at $60^{\circ}$ | $\begin{aligned} & (0.0020, \\ & 0.0020,0.0057, \\ & -0.0003) \end{aligned}$ | $\begin{gathered} (0.0045,0.0024, \\ 0.0085,0.0001) \end{gathered}$ | $\begin{aligned} & (0.0024,0.0011, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{gathered} (0.3669 \\ 1.1491, \\ 0.3550) \end{gathered}$ | $\begin{gathered} (0.3633, \\ 1.0631, \\ 0.4935) \end{gathered}$ | 0.3448 | 0.2400 | 0.0354 | 41.0290 |
| 5 | $\begin{gathered} (0.5, \\ 0.866, \\ 0.5) \end{gathered}$ | In-between mic1 and 2 inside the array at height of 0.5 m at $60^{\circ}$ | $\begin{gathered} (0.0020, \\ 0.0020,0.0057, \\ -0.0003) \end{gathered}$ | $\left.\begin{array}{ll} (0.0045, & 0.0024, \\ 0.0085, & 0.0001 \end{array}\right)$ | $\begin{aligned} & (0.0024,0.0011, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{gathered} (0.3669 \\ 1.1491, \\ 0.3550) \end{gathered}$ | $\begin{gathered} (0.3633 \\ 1.0631, \\ 0.4935) \end{gathered}$ | 0.3448 | 0.2400 | 0.0351 | 64.6451 |
| 8 | $\begin{gathered} (0.5, \\ 0.866, \\ 0.5) \end{gathered}$ | In-between micl and 2 inside the array at height of 0.5 m at $60^{\circ}$ | $\begin{gathered} (0.0020, \\ 0.0020,0.0057, \\ -0.0003) \end{gathered}$ | $\begin{aligned} & (0.0045,0.0024, \\ & 0.0085,0.0001) \end{aligned}$ | $\begin{aligned} & (0.0024,0.0011, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{gathered} (0.3669 \\ 1.1491, \\ 0.3550) \end{gathered}$ | $\begin{gathered} (0.3633 \\ 1.0631, \\ 0.4935) \end{gathered}$ | 0.3448 | 0.2400 | 0.0813 | $\begin{gathered} 2158.5= \\ 35 \text { minut } \\ \text { es } 58 \\ \text { seconds } \end{gathered}$ |
| 10 | $\begin{gathered} (0.5, \\ 0.866, \\ 0.5) \end{gathered}$ | In-between micl and 2 inside the array at height of 0.5 m at $60^{\circ}$ | $\begin{aligned} & (0.0020, \\ & 0.0020,0.0057, \\ & -0.0003) \end{aligned}$ | $\begin{aligned} & (0.0045,0.0024, \\ & 0.0085,0.0001) \end{aligned}$ | $\begin{aligned} & (0.0024,0.0011, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{gathered} (0.3669 \\ 1.1491, \\ 0.3550) \end{gathered}$ | $\begin{gathered} (0.3633 \\ 1.0631, \\ 0.4935) \end{gathered}$ | 0.3448 | 0.2400 | 0.2134 | $\begin{gathered} 899.135 \\ 4= \\ 14 \text { minut } \\ \text { es } 8 \\ \text { seconds } \end{gathered}$ |
| 15 | $\begin{gathered} (0.5, \\ 0.866, \\ 0.5) \end{gathered}$ | In-between mic1 and 2 inside the array at height of 0.5 m at $60^{\circ}$ | $\begin{aligned} & (0.0020, \\ & 0.0020,0.0057, \\ & -0.0003) \end{aligned}$ | $\begin{aligned} & (0.0045,0.0024, \\ & 0.0085,0.0001) \end{aligned}$ | $\begin{aligned} & (0.0024,0.0011, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{gathered} (0.3669 \\ 1.1491, \\ 0.3550) \end{gathered}$ | $\begin{gathered} (0.3633, \\ 1.0631, \\ 0.4935) \end{gathered}$ | 0.3448 | 0.2400 | 0.1903 | $\begin{gathered} 7661.2= \\ 2 \mathrm{hrs} \\ 7 \text { minutes } \\ 41 \\ \text { seconds } \end{gathered}$ |

### 6.1.4 Signal Variance ( $\sigma_{i m p}$ )

Now we will investigate the effects of variation in signal variance ( $\sigma_{i m p}$ ) on the results of the algorithm using the same signals and $\Psi$ matrix as in Section 6.1.1. We used index of maximum absolute value of CIR for TDOA calculation. Other parameters were kept as follows:

$$
\begin{equation*}
p=5, N_{0}=1.5 \times 10^{-4}, c=340 \mathrm{~m} / \mathrm{s} \tag{6.2}
\end{equation*}
$$

We kept the range of signal variance from 0.3 to 2.0 volts because during experimentation we found out that the signal peak amplitude was in this range.

Table 6.8 shows the results for different values of $\sigma_{i m p}$. As can be seen form Table 6.8 changing the value of $\sigma_{i m p}$ has no effect on the results at all and we can choose any value we want. In fact, the results defend on the source signal, the Dictionary matrix and sampling rate. We will choose $\sigma_{i m p}=1$ as it is favorable for normalized signals.

Table 6.8: Effect of change in $\sigma_{i m p}$ on the results of the algorithm

| $\sigma_{\text {imp }}$ | Source <br> Location | Description | Exact TDs $\left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right)$ | $\begin{aligned} & T D E_{c c} \\ & \left(\tau_{10}^{c c}, \tau_{20}^{c c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{aligned} & T D E_{o c} \\ & \left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c}, \tau_{40}^{o c}\right) \end{aligned}$ | $\begin{aligned} & X_{c c} \\ & \left(x_{s}^{c c}, y_{s}^{c c}, \boldsymbol{Z}_{s}^{c c}\right) \end{aligned}$ | $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{aligned} & \text { MSE } \\ & \text { for CC } \end{aligned}$ | $\begin{aligned} & \text { MSE } \\ & \text { for OC } \end{aligned}$ | CC <br> Time <br> (Sec) | $\underset{(\mathrm{Sec})}{\text { OC Time }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.3 | $\begin{gathered} (0.5, \\ 0.866, \\ 0.5) \end{gathered}$ | In-between mic1 and 2 inside the array at height of 0.5 m at $60^{\circ}$ | $\begin{gathered} (0.0020,0.0020, \\ 0.005,-0.0003) \end{gathered}$ | $\begin{gathered} (0.0045,0.0024, \\ 0.0085,0.0001) \end{gathered}$ | $\begin{aligned} & (0.0024,0.0011, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{gathered} (0.3669 \\ 1.1491, \\ 0.3550) \end{gathered}$ | $\begin{gathered} (0.3633 \\ 1.0631, \\ 0.4935) \end{gathered}$ | 0.3448 | 0.2400 | 0.0644 | 63.3623 |
| 0.8 | $\begin{gathered} (0.5, \\ 0.866, \\ 0.5) \end{gathered}$ | In-between micl and 2 inside the array at height of 0.5 m at $60^{\circ}$ | $\begin{gathered} (0.0020,0.0020, \\ 0.0057,-0.0003) \end{gathered}$ | $\begin{gathered} (0.0045,0.0024, \\ 0.0085,0.0001) \end{gathered}$ | $\begin{aligned} & (0.0024,0.0011, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{gathered} (0.3669 \\ 1.1491 \\ 0.3550) \end{gathered}$ | $\begin{gathered} (0.3633 \\ 1.0631, \\ 0.4935) \end{gathered}$ | 0.3448 | 0.2400 | 0.0606 | 59.1333 |
| 1.0 | $\begin{gathered} (0.5, \\ 0.866, \\ 0.5) \end{gathered}$ | In-between mic1 and 2 inside the array at height of 0.5 m at $60^{\circ}$ | $\begin{gathered} (0.0020,0.0020, \\ 0.0057,-0.0003) \end{gathered}$ | $\begin{gathered} (0.0045,0.0024, \\ 0.0085,0.0001) \end{gathered}$ | $\begin{aligned} & (0.0024,0.0011, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{gathered} (0.3669 \\ 1.1491 \\ 0.3550) \end{gathered}$ | $\begin{gathered} (0.3633 \\ 1.0631, \\ 0.4935) \end{gathered}$ | 0.3448 | 0.2400 | 0.0458 | 60.0819 |
| 1.5 | $\begin{gathered} (0.5, \\ 0.866, \\ 0.5) \end{gathered}$ | In-between mic1 and 2 inside the array at height of 0.5 m at $60^{\circ}$ | $\begin{aligned} & (0.0020,0.0020, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{aligned} & (0.0045,0.0024, \\ & 0.0085,0.0001) \end{aligned}$ | $\begin{aligned} & (0.0024,0.0011, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{gathered} (0.3669 \\ 1.1491 \\ 0.3550) \end{gathered}$ | $\begin{gathered} (0.3633 \\ 1.0631, \\ 0.4935) \end{gathered}$ | 0.3448 | 0.2400 | 0.0351 | 58.2630 |
| 2.0 | $\begin{gathered} (0.5, \\ 0.866, \\ 0.5) \end{gathered}$ | In-between micl and 2 inside the array at height of 0.5 m at $60^{\circ}$ | $\begin{gathered} (0.0020,0.0020, \\ 0.0057,-0.0003) \end{gathered}$ | $\begin{aligned} & (0.0045,0.0024, \\ & 0.0085,0.0001) \end{aligned}$ | $\begin{aligned} & (0.0024,0.0011, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{gathered} (0.3669 \\ 1.1491 \\ 0.3550) \end{gathered}$ | $\begin{gathered} (0.3633 \\ 1.0631, \\ 0.4935) \end{gathered}$ | 0.3448 | 0.2400 | 0.0359 | 58.6135 |

### 6.1.5 Noise Variance $\left(N_{0}\right)$

Looking at the results of previous subsections we can safely choose $p=5, \sigma_{i m p}=$ $1, c=340 \mathrm{~m} / \mathrm{s}$ without causing any effect to the results of the algorithm. We used index of first nonzero value of CIR for TDOA calculation. Now we will investigate the effect of variations in the variance of noise on the results of the algorithm.

After analyzing all the signals we captured both indoor and outdoor we found out that the noise level was in the range of -0.04 to 0.04 volts (these values represent the maximum and minimum noise level) which when normalized w.r.t. the peak of the signal reduces to -0.003 to 0.003 volts. Now we will select a range of $0.005-0.09$ volts for signal noise level to see its effect on the output of the algorithm.

We will use the same signals and dictionary matrix which we used in the previous subsections. Table 6.9 shows the results when we varied the value of $N_{0}$.

Table 6.9: Effect of change in $N_{0}$ on the results of the algorithm

| $N_{0}$ | Source <br> Location | Description | Exact TDs $\left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right)$ | $\begin{aligned} & T D E_{C c} \\ & \left(\tau_{10}^{c}, \tau_{20}^{\tau c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{aligned} & T D E_{o c} \\ & \left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c}, \tau_{40}^{o c}\right) \end{aligned}$ | $\begin{aligned} & X_{c c} \\ & \left(x_{s}^{c c}, y_{s}^{c c}, Z_{s}^{c c}\right) \end{aligned}$ | $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} \text { MSE } \\ \text { for } \mathbf{C C} \end{gathered}$ | $\begin{aligned} & \text { MSE } \\ & \text { for OC } \end{aligned}$ | CC <br> Time <br> (Sec) | $\begin{aligned} & \text { OC Time } \\ & \text { (Sec) } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.005 | $\begin{gathered} (0.5, \\ 0.866, \\ 0.5) \end{gathered}$ | In-between mic1 and 2 inside the array at height of 0.5 m at $60^{\circ}$ | $\begin{aligned} & (0.0020,0.0020, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{aligned} & (0.0045,0.0024, \\ & 0.0085,0.0001) \end{aligned}$ | $\begin{aligned} & (0.0024,0.0011, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{gathered} (0.3669 \\ 1.1491 \\ 0.3550) \end{gathered}$ | $\begin{gathered} (0.3633 \\ 1.0631, \\ 0.4935) \end{gathered}$ | 0.3448 | 0.2400 | 0.0355 | 80.6391 |
| 0.01 | $\begin{gathered} (0.5, \\ 0.866, \\ 0.5) \end{gathered}$ | In-between mic1 and 2 inside the array at height of 0.5 m at $60^{\circ}$ | $\begin{aligned} & (0.0020,0.0020, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{gathered} (0.0045,0.0024, \\ 0.0085,0.0001) \end{gathered}$ | $\begin{aligned} & (0.0059,0.0011, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{gathered} (0.3669 \\ 1.1491, \\ 0.3550) \end{gathered}$ | $\begin{gathered} (-0.4631 \\ 0.7422, \\ 0.4100) \end{gathered}$ | 0.3448 | 0.9752 | 0.0861 | 87.9956 |
| 0.03 | $\begin{gathered} (0.5, \\ 0.866, \\ 0.5) \end{gathered}$ | In-between mic1 and 2 inside the array at height of 0.5 m at $60^{\circ}$ | $\begin{aligned} & (0.0020,0.0020, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{gathered} (0.0045,0.0024, \\ 0.0085,0.0001) \end{gathered}$ | $\begin{aligned} & (0.0059,0.0011, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{gathered} (0.3669 \\ 1.1491, \\ 0.3550) \end{gathered}$ | $\begin{gathered} (-0.4631, \\ 0.7422, \\ 0.4100) \end{gathered}$ | 0.3448 | 0.9752 | 0.0357 | $\begin{gathered} 144.469 \\ 2 \end{gathered}$ |
| 0.05 | $\begin{gathered} (0.5, \\ 0.866, \\ 0.5) \end{gathered}$ | In-between mic1 and 2 inside the array at height of 0.5 m at $60^{\circ}$ | $\begin{gathered} (0.0020, \\ 0.0020,0.0057, \\ -0.0003) \end{gathered}$ | $\begin{gathered} (0.0045,0.0024, \\ 0.0085,0.0001) \end{gathered}$ | $\begin{aligned} & (0.0059,0.0011, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{gathered} (0.3669 \\ 1.1491, \\ 0.3550) \end{gathered}$ | $\begin{gathered} (-0.4631, \\ 0.7422, \\ 0.4100) \end{gathered}$ | 0.3448 | 0.9752 | 0.4645 | 66.9509 |
| 0.09 | $\begin{gathered} (0.5, \\ 0.866, \\ 0.5) \end{gathered}$ | In-between mic1 and 2 inside the array at height of 0.5 m at $60^{\circ}$ | $\begin{aligned} & (0.0020,0.0020, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{gathered} (0.0045,0.0024, \\ 0.0085,0.0001) \end{gathered}$ | $\begin{aligned} & (0.0059,0.0011, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{gathered} (0.3669 \\ 1.1491, \\ 0.3550) \end{gathered}$ | $\begin{array}{r} (-0.4631, \\ 0.7422, \\ 0.4100) \end{array}$ | 0.3448 | 0.9752 | 0.2364 | 66.9509 |

Looking at the results in Table 6.9 it is clear that increasing the noise level has great effect on the results. However, one trend is clear that after crossing a
certain threshold in $N_{0}$ the results stay the same. We tried different values of $N_{0}$ below 0.005 (which we did not include in the report because of space limitations) and we got the same results as for 0.005 case. Similarly for $N_{0}$ above 0.09 we got the same results as for the case of 0.09 .

### 6.1.6 Conclusion of This Section

Since $p$ and $\sigma_{i m p}$ has no significant effect on the results of the OC algorithm we can safely choose them as $p=5, \sigma_{i m p}=1$ to cover their most expected values. As was discussed in Subsection 6.1.1 the best Dictionary in our case is $\Psi_{4}$ thus we will use it onward in our experiments. As was discussed in Subsection 6.1.5 any value below 0.005 for $N_{0}$ produce the same results as 0.005 thus we choose to keep $N_{0}=1.5 \times 10^{-4}$ which produce good results. Also based on the results in Subsection 6.1.2 the selection of index of maximum amplitude produce efficient results. This finding was also observed by the author of [6] in his work and thus in our coming experiments we use this index for time delay calculation.

### 6.2 Results using RevoLabs Wireless Microphone System

In this section we discuss in detail the indoor experiments we conducted using RevoLabs system and their results and analysis. As there are three different geometries and each geometry has different scenarios thus we need to organize
the discussion in subsections. Subsections 6.2.1, 6.2.2 and 6.2.3 discuss the results for Pyramid, Circular and Rhombus geometries in indoor environment using RevoLabs System, respectively. To save space we will not discuss the observation of individual scenario. The observations for all the indoor scenarios using RevoLab system will be discussed in detailed in subsection 6.2.4. It is to be noted that we used an unloaded toy gunshot for all the experiments using RevoLabs system.

### 6.2.1 Pyramid Geometry Experiments and Results

In this section we discuss the results for the Pyramid geometry obtained using RevoLabs wireless microphone system. We are using the geometry with the source locations discussed in Section 5.2.1.

There are several experimental scenarios as was shown in Fig. 6.1. The results are organized with respect to the sampling rate and follow next.

## Results for 8 kHz Case

Fig. 6.6 shows the experimental setup for the Pyramid geometry in the indoor environment. Fig. 6.6a shows the case when the array of microphones was placed in the center of the hall which represents a less-reverberant environment. Fig. 6.6b shows the case when array was placed in a corner of the hall which represents a more-reverberant environment. Note that the radius of geometry in Fig. 6.6a is small compared to Fig. 6.6b which we used to analyze the effects of the geometry size and here it is given only to show the experimental scenario.

Table 6.10 shows the results we obtained for the case when the array was
placed in the center of the hall where $\epsilon_{C C}$ represents the 3 D error for CC method.

(a)

(b)

Figure 6.6: Indoor Pyramid Geometry Setup Using RevoLabs System, (a) Indoor Pyramid Geometry in the Center of the Hall using RevoLabs System, (b) Indoor Pyramid Geometry in a Corner of the Hall using RevoLabs System.

Fig. 7.4 shows the plot of the original source locations and the estimated source locations using CC and OC algorithms. Fig. 6.7a shows the 2D plot of $x, y$-coordinates of the estimated source locations for the less-reverberant case

Table 6.10: Pyramid indoor results using RevoLabs at 8 kHz for the case when the array was placed in the center of the hall. Fast Machine was used.

| Source Location | (0.5, 0.866, 0.5) | $\begin{gathered} \left(2 \cos 60^{\circ}, 2 \sin 60^{\circ}, 0\right)= \\ (1,1.73,0) \end{gathered}$ | $\begin{gathered} \left(2.5 \cos 60^{\circ}, 2.5 \sin 60^{\circ}, 0\right) \\ =(1.25,2.16,0) \end{gathered}$ | $(\mathbf{0}, \mathbf{0}, \mathbf{1})$ | (2.5, 0, 0) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Description | In-between $a_{1}$ and $a_{2}$ inside the array at height of 0.5 m at $60^{\circ}$ | In-between $a_{1}$ \& $a_{2}$ on the circle inscribing the array. | In-between $a_{1} \& a_{2}$, outside the array | Above the center of the array | Along the line (outside array) passing through $a_{1}$ and center of the array |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | $\begin{aligned} & (0.0020,0.0020, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{gathered} (0,0.0000,0.0059, \\ 0.0004) \end{gathered}$ | $\begin{gathered} (-0.0006,-0.0006, \\ 0.0059,0.0003) \end{gathered}$ | $\begin{aligned} & (0.0036,0.0036, \\ & 0.0036,-0.0021) \end{aligned}$ | $\begin{gathered} (-0.0059,0.0041, \\ 0.0041,0.0003) \end{gathered}$ |
| $\begin{aligned} & T D E_{c c} \\ & \left(\tau_{10}^{c c},,_{20}^{c c}, \tau_{30}^{c c},,_{40}^{c c}\right) \end{aligned}$ | $\begin{gathered} (0.0045,0.0024, \\ 0.0085,0.0001) \end{gathered}$ | $\begin{aligned} & (0.0075,0.0046, \\ & 0.0073,-0.0021) \end{aligned}$ | $\begin{gathered} (-0.0019,-0.0018 \\ 0.0076,-0.0018) \end{gathered}$ | $\begin{aligned} & (0.0075,0.0046, \\ & 0.0073,-0.0021) \end{aligned}$ | $\begin{gathered} (-0.0064,0.0044, \\ 0.0056,0.0118) \end{gathered}$ |
| $\begin{aligned} & \text { TDE } E_{o c} \\ & \left(\tau_{10}^{o c}, \tau_{20}, \tau_{30}^{o c}, \tau_{40}^{o c}\right) \end{aligned}$ | $\begin{aligned} & (0.0059,0.0011, \\ & 0.0088,-0.0003) \end{aligned}$ | $\begin{aligned} & (0.0013,0.0015, \\ & 0.0070,0.0012) \end{aligned}$ | $\begin{gathered} (0.0010,-0.0011, \\ 0.0062,0.0005) \end{gathered}$ | $\begin{aligned} & (0.0025,0.0043, \\ & 0.0051,-0.0010) \end{aligned}$ | $\begin{gathered} (-0.0049,0.0035, \\ 0.0035,0.0010) \end{gathered}$ |
| $\begin{aligned} & X_{c c} \\ & \left(x_{s}^{c c}, y_{s}^{c c}, Z_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (0.3669,1.1491, \\ 0.3550) \end{gathered}$ | $\begin{gathered} (-0.3303,0.4604, \\ -0.2349) \end{gathered}$ | $\begin{gathered} (1.4279,2.4476, \\ 1.4870) \end{gathered}$ | $\begin{gathered} (-0.3303,0.4604, \\ -0.2349) \end{gathered}$ | $\begin{gathered} (0.4549,0.2798, \\ -13.9459) \end{gathered}$ |
| $\begin{aligned} & \hline X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, \boldsymbol{Z}_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (0.0982,1.1934, \\ 0.3381) \end{gathered}$ | $\begin{gathered} (0.7562,1.2564, \\ -0.2556) \end{gathered}$ | $\begin{gathered} (0.6719,1.8823, \\ -0.0756) \end{gathered}$ | $\begin{gathered} (0.4972,0.1850, \\ 0.6376) \end{gathered}$ | (4.0349, 0, -1.8341) |
| $\epsilon_{\text {cc }}$ | 0.3448 | 1.3587 | 1.5249 | 1.3587 | 14.0978 |
| $\epsilon_{o c, 3 D}$ | 0.5430 | 0.5909 | 0.6458 | 0.6425 | 2.3916 |
| $\epsilon_{o C_{2} 2 \mathrm{D}}$ | 0.5183 | 0.5327 | 0.6414 | 0.5305 | 1.5349 |
| Time for CC (Sec) | 0.0677 | 0.0334 | 0.0354 | 0.0348 | 0.0347 |
| Time for OC (Sec) | 62.0450 | 48.0434 | 55.2455 | 52.6566 | 121.6402 |

while Fig. 6.7b shows the same for the more-reverberant case. The height of the source positions are separately plotted in the form of bargraph. Fig. 6.7c and 6.7d shows the bargraphs of the heights for the less- and more-reverberant cases respectively.


Figure 6.7: Pyramid Geometry Source Locations Estimated by CC and OC at 8 kHz Indoor using RevoLabs system, (a) Source Locations estimated in the less-reverberant case, only the $x, y$ coordinates are shown, (b) Source Locations estimated in the more-reverberant case,, only the $x, y$ coordinates are shown, (c) Height Estimate for the less-reverberant case, (d) Height Estimate for the more-reverberant case

Table 6.11 shows the results we obtained for the case when the array was
placed in a corner of the hall.

Table 6.11: Pyramid indoor results using RevoLabs at 8 kHz for the case when the array was placed in a corner of the hall. Fast Machine was used.

| Source Location | (0.5, 0.866, 0.5) | $\begin{gathered} \left(2 \cos 60^{\circ}, 2 \sin 60^{\circ}, 0\right)= \\ (1,1.73,0) \end{gathered}$ | $(\mathbf{0}, \mathbf{0}, \mathbf{1})$ | (2.5, 0, 0) | $(-4,4,0)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Description | In-between $a_{1}$ and $a_{2}$ inside the array at height of 0.5 m at $60^{\circ}$ | In-between $a_{1}$ \& $a_{2}$ on the circle inscribing the array. | Above the center of the array | Along the line (outside array) passing through $a_{1}$ and center of the array | On the line through $a_{2}$ and origin outside the array |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | $\begin{aligned} & (0.0020,0.0020, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{gathered} (0,0.0016,0.0058, \\ 0.0005) \end{gathered}$ | $\begin{aligned} & (0.0036,0.0036, \\ & 0.0036,-0.0021) \end{aligned}$ | $\begin{gathered} (-0.0059,0.0041, \\ 0.0041,0.0003) \end{gathered}$ | $\begin{gathered} (0.0046,-0.0056, \\ 0.0024,0.0001) \end{gathered}$ |
| $\begin{aligned} & \text { TDE } E_{c c} \\ & \left(\tau_{10}^{c c}, \tau_{20}^{c c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{aligned} & (0.0041,0.0060, \\ & 0.0104,-0.0009) \end{aligned}$ | $\begin{gathered} (-0.0021,-0.0008, \\ 0.0032,-0.0043) \end{gathered}$ | $\begin{aligned} & (0.0066,0.0080, \\ & 0.0061,-0.0018) \end{aligned}$ | $\begin{gathered} (-0.0180,0.0073, \\ -0.0056,0.0009) \end{gathered}$ | $\begin{aligned} & (0.0060,-0.0041, \\ & 0.0031,-0.0019) \end{aligned}$ |
| $\begin{aligned} & T D E_{o c} \\ & \left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c}, \tau_{40}^{o c}\right) \end{aligned}$ | $\begin{aligned} & (0.0030,0.0031, \\ & 0.0080,-0.0007) \end{aligned}$ | $\begin{gathered} (0.00010,0.0023, \\ 0.0060,0.0010) \end{gathered}$ | $\begin{aligned} & (0.0045,0.0043, \\ & 0.0045,-0.0009) \end{aligned}$ | $\begin{gathered} (4.0336,-0.1112, \\ -1.6068) \end{gathered}$ | $\begin{gathered} (0.0050,-0.0040, \\ 0.0030,0.0008) \end{gathered}$ |
| $\begin{aligned} & X_{c c} \\ & \left(x_{s}^{x c}, y_{s}^{c c}, z_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (0.8388,0.9929 \\ 0.1037) \end{gathered}$ | $\begin{gathered} (15.3081,15.8584 \\ 79.1244) \end{gathered}$ | $\begin{gathered} (0.1154,-0.3792, \\ -0.1675) \end{gathered}$ | $\begin{gathered} (1.3065,-4.3425 \\ -1.0072) \end{gathered}$ | $\begin{gathered} (-1.4631,0.8716 \\ 1.3128) \end{gathered}$ |
| $\begin{aligned} & \hline X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (0.6096,1.0304, \\ 0.4051) \end{gathered}$ | $\begin{gathered} (0.9782,0.9718, \\ -0.3176) \end{gathered}$ | $\begin{gathered} (-0.0234,0.0406, \\ 0.5384) \\ \hline \end{gathered}$ | $\begin{gathered} (4.0336,-0.1112, \\ -1.6068) \end{gathered}$ | $\begin{gathered} (-1.6662,1.4543, \\ -0.5553) \end{gathered}$ |
| $\epsilon_{c c}$ | 0.5366 | 81.7377 | 1.2329 | 4.6148 | 4.2363 |
| $\epsilon_{\text {OC }}{ }^{\text {c }}$ D | 0.2192 | 0.8223 | 0.4639 | 2.2240 | 3.4979 |
| $\epsilon_{o C_{2} 2 \mathrm{D}}$ | 0.1976 | 0.7585 | 0.0469 | 1.5376 | 3.4535 |
| Time for CC (Sec) | 0.0356 | 0.0349 | 0.0355 | 0.0346 | 0.1918 |
| Time for OC (Sec) | 315.4692 | 352.7878 | 56.6916 | 134.9118 | 609.6994 |

## Results for 4 kHz Case

The same experimental setup was used (shown in Fig. 6.6) as that for the case of 8 kHz . Table 6.12 shows the results we obtained for the case when the array was placed in the center of the hall while Table 6.13 shows the results for the case when the array was placed in a corner of the hall.

Using the results from Table 6.12 and 6.13 we plot the actual and estimated $x, y$ coordinates of the source locations in Fig. 6.8a and Fig. 6.8b for the case of less-reverberant (center of hall) and more-reverberant (corner of hall) scenarios respectively. Fig. 6.8c and Fig. 6.8d compares the estimate of source height obtained using CC and OC with the actual heights.

Table 6.12: Pyramid indoor results using RevoLabs at 4 kHz for the case when the array was placed in the center of the hall. Slow Machine was used.

| Source Location | (0.5, 0.866, 0.5) | $\begin{gathered} \left(2 \cos 60^{\circ}, 2 \sin 60^{\circ}, 0\right)= \\ (1,1.73,0) \end{gathered}$ | $\begin{gathered} \left(2.5 \cos 60^{\circ}, 2.5 \sin 60^{\circ},\right. \\ 0)=(1.25,2.16,0) \end{gathered}$ | $(\mathbf{0}, \mathbf{0}, \mathbf{1})$ | (2.5, 0, 0) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Description | In-between $a_{1}$ and $a_{2}$ inside the array at height of 0.5 m at $60^{\circ}$ | In-between $a_{1} \& a_{2}$ on the circle inscribing the array. | In-between $a_{1}$ \& $a_{2}$, outside the array | Above the center of the array | Along the line (outside array) passing through $a_{1}$ and center of the array |
| $\begin{gathered} \text { Exact TDs } \\ \left(\boldsymbol{\tau}_{10}, \boldsymbol{\tau}_{20}, \tau_{30}, \boldsymbol{\tau}_{40}\right) \end{gathered}$ | $\begin{aligned} & (0.0020,0.0020, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{gathered} (0,0.0000,0.0059, \\ 0.0004) \end{gathered}$ | $\begin{gathered} (-0.0006,-0.0006, \\ 0.0059,0.0003) \end{gathered}$ | $\begin{aligned} & (0.0036,0.0036, \\ & 0.0036,-0.0021) \end{aligned}$ | $\begin{gathered} (-0.0059,0.0041, \\ 0.0041,0.0003) \end{gathered}$ |
| $\begin{aligned} & \hline \boldsymbol{T D E} E_{c c} \\ & \left(\tau_{10}^{c c}, \tau_{20}^{c c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{aligned} & (0.0025,0.005, \\ & 0.0120,0.0005) \end{aligned}$ | $\begin{gathered} (0.0013,0.0003, \\ 0.0063,0.0015) \end{gathered}$ | $\begin{gathered} (-0.0177,0.0003, \\ 0.0080,-0.0145) \end{gathered}$ | $\begin{aligned} & (0.0060,0.0090, \\ & 0.0032,-0.0005) \end{aligned}$ | $\begin{gathered} \hline(-0.0067,0.0037, \\ 0.0070,0.0013) \end{gathered}$ |
| $\begin{aligned} & \text { TDE } E_{o c} \\ & \left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c}, \tau_{40}^{o c}\right) \end{aligned}$ | $\begin{gathered} (0.0043,0.0010, \\ 0.0071,0.0009) \end{gathered}$ | $\begin{gathered} (0.0010,0.0009, \\ 0.0071,0.0015) \end{gathered}$ | $\begin{gathered} (-0.0017,-0.0021, \\ 0.0078,0.0010) \end{gathered}$ | $\begin{aligned} & (0.0046,0.0028, \\ & 0.0048,-0.0041) \end{aligned}$ | $\begin{gathered} (-0.0049,0.0063, \\ 0.0051,0.0009) \end{gathered}$ |
| $\begin{aligned} & \boldsymbol{X}_{c c} \\ & \left(x_{s}^{c c}, y_{s}^{c c}, \boldsymbol{z}_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (1.0841,1.5576, \\ 0.4870) \end{gathered}$ | $\begin{gathered} (0.6606,1.4661, \\ -0.8013) \end{gathered}$ | $\begin{gathered} \hline 6.7612,4.8144, \\ 17.2162) \end{gathered}$ | $\begin{gathered} (0.1853,-1.0504, \\ 0.2877) \end{gathered}$ | $\begin{gathered} (-0.5518,0.5176, \\ 0.3555) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (0.1258,1.1027, \\ 0.0974) \end{gathered}$ | $\begin{gathered} (0.8055,1.4205, \\ -0.5108) \end{gathered}$ | $\begin{gathered} (1.3545,2.4144, \\ -0.4361) \end{gathered}$ | $\begin{array}{rr} (-0.1756, & 0.3952, \\ 0.4071) \end{array}$ | $\begin{gathered} (0.6132,-0.2717, \\ 0.1383) \end{gathered}$ |
| $\epsilon_{c c}$ | $0.9054$ | $0.9094$ | $18.2706$ | 1.2826 | $3.1157$ |
| $\epsilon_{o c, 3 D}$ | $0.5984$ | 0.6281 | 0.5156 | 0.7339 | $1.9113$ |
| $\epsilon_{o C, 2 D}$ | 0.4428 | 0.3655 | 0.2751 | 0.4325 | 1.9062 |
| Time for CC (Sec) | 0.0346 | 0.0344 | 0.0344 | 0.0327 | 0.0346 |
| Time for OC (Sec) | 21.1277 | 13.9726 | 13.0115 | 10.9131 | 14.2258 |

Table 6.13: Pyramid indoor results using RevoLabs at 4 kHz for the case when the array was placed in a corner of the hall. Slow Machine was used.

| Source Location | $(0.5,0.866,0.5)$ | $\left(2 \cos 60^{\circ}, 2 \sin 60^{\circ}\right.$, $0)=(1,1.73,0)$ | $(0,0,1)$ | $(2.5,0,0)$ | $(-4,4,0)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Description | In-between $a_{1}$ and $a_{2}$ inside the array at height of 0.5 m at $60^{\circ}$ | In-between $a_{1}$ \& $a_{2}$ on the circle inscribing the array. | Above the center of the array | Along the line (outside array) passing through $a_{1}$ and center of the array | On the line through $a_{2}$ and origin outside the array |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | $\begin{aligned} & (0.0020,0.0020, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{gathered} (0,0.0000, \\ 0.0059, \quad 0.0004) \end{gathered}$ | $\begin{aligned} & (0.0036,0.0036, \\ & 0.0036,-0.0021) \end{aligned}$ | $\begin{gathered} (-0.0059,0.0041, \\ 0.0041,0.0003) \end{gathered}$ | $\begin{gathered} (0.0046,-0.0056,0.0024, \\ 0.0001) \end{gathered}$ |
| $\begin{aligned} & \text { TDE } E_{C C} \\ & \left(\tau_{10}^{c c}, \tau_{20}^{c c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{gathered} (0.0110,0.0022, \text {, } \\ 0.0107,0.0005) \end{gathered}$ | $\begin{aligned} & (0.0060,0.0090, \\ & 0.0032,-0.0005) \end{aligned}$ | $\begin{gathered} (-0.0005,0.0005, \\ 0.0177,0.0010) \end{gathered}$ | $\begin{gathered} (-0.0043,-0.0077, \\ 0.0047,0.0015) \end{gathered}$ | $\begin{gathered} (0.0070,-0.0018, \\ 0.0057,-0.0003) \end{gathered}$ |
| $\begin{aligned} & T D E_{O C} \\ & \left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c}, \tau_{40}^{o c}\right) \end{aligned}$ | $\begin{aligned} & (0.0049,0.0045, \\ & 0.0076,-0.0023) \end{aligned}$ | $\begin{gathered} (0.0013,0.0011, \\ 0.0071,0.0015) \end{gathered}$ | $\begin{gathered} (0.0039,0.0032, \\ 0.0041,0.0034) \end{gathered}$ | $\begin{gathered} (-0.0041,0.0057, \\ 0.0052,0.0011) \end{gathered}$ | $\begin{gathered} (0.0034,-0.0039,0.0027, \\ 0.0015) \end{gathered}$ |
| $\begin{aligned} & X_{C c} \\ & \left(x_{s}^{c c}, \boldsymbol{y}_{s}^{c c}, z_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (-0.6810,1.0194 \\ 0.5692) \end{gathered}$ | $\begin{gathered} (0.1853,-1.0504, \\ 0.2877) \end{gathered}$ | $\begin{gathered} (0.8204,1.8191, \\ 1.2374) \end{gathered}$ | $\begin{gathered} (0.4252,-0.7154, \\ 0.2312) \end{gathered}$ | $\begin{gathered} (-0.7597,0.7131, \\ 0.3891) \end{gathered}$ |
| $\begin{aligned} & X_{O C} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (0.2912,0.6313, \\ -0.0453) \end{gathered}$ | $\begin{gathered} (0.7515,1.3531, \\ -0.4607) \end{gathered}$ | $\begin{gathered} (-0.0589,0.1921, \\ -2.0679) \end{gathered}$ | $\begin{gathered} (0.9928,-0.1246, \\ -0.0938) \end{gathered}$ | $\begin{gathered} (-2.4492,3.3591, \\ -3.6382) \end{gathered}$ |
| $\epsilon_{\text {cc }}$ | 1.1929 | 1.2826 | 1.2536 | 2.2069 | 4.6319 |
| $\epsilon_{O C \_3 D}$ | 0.6293 | 0.6450 | 3.0745 | 1.5153 | 4.0065 |
| $\epsilon_{\text {OC_2D }}$ | 0.3141 | 0.4515 | 0.2010 | 1.5124 | 1.6780 |
| Time for CC (Sec) | 0.0346 | 0.0344 | 0.0327 | 0.0346 | 0.0326 |
| $\begin{gathered} \hline \text { Time for } \mathrm{OC} \\ \text { (Sec) } \end{gathered}$ | 21.1277 | 13.9726 | 10.9131 | 14.2258 | 17.4918 |



Figure 6.8: Pyramid Geometry Source Locations Estimated by CC and OC at 4 kHz Indoor using RevoLabs system, (a) Source Locations estimated in the less-reverberant case, only the $x, y$ coordinates are shown, (b) Source Locations estimated in the more-reverberant case,, only the $x, y$ coordinates are shown, (c) Height Estimate for the less-reverberant case, (d) Height Estimate for the more-reverberant case.

### 6.2.2 Circular Geometry Experiments and Results

This section experiments use the circular geometry with the source locations discussed in Section 5.2.1. The values of different parameters of the OC algorithm were the same as were decided in Section 6.1.6.

There are two different experimental scenarios i.e. i). experimenting in the center of the hall and ii). experimenting in a corner of the hall. We call the first scenario as less-reverberant case and the second as more-reverberant case due to reflections from the wall. Two different sampling rates of 8 kHz and 4 kHz were used during experiments. The results for all these scenarios follows.

## Results for the 8 kHz Case

Fig. 6.9 shows the experimental setup for the Circular geometry in indoor environment. Fig. 6.9a shows the case when array was placed in the center of the hall while Fig. 6.9b shows the case when array was placed in a corner of the hall.

Table 6.14 shows the results for the center of the hall case while Table 6.15 shows the results for the corner of the hall case. We plot the $x, y$ coordinates of the actual and estimated source locations for the less-reverberant case in Fig. 6.10a and Fig. 6.10b plots the $x, y$ coordinates for the more-reverberant case.


Figure 6.9: Indoor Circular Geometry Setup Using RevoLabs System, (a) Indoor Circular Geometry in the Center of the Hall using RevoLabs System, (b) Indoor Circular Geometry in a Corner of the Hall using RevoLabs System.

Note that in the case of array being in the corner of the hall, one source location $(-4.5,0,0)$ was crossing the dimension of the room thus it was not possible to test it. Fig. 6.10c and Fig. 6.10d show the bargraphs for the height of source locations for the case of less- and more-reverberant scenarios respectively.


Figure 6.10: Circular Geometry Source Locations Estimated by CC and OC at 8 kHz Indoor using RevoLabs system, (a) Source Locations estimated in the less-reverberant case, only the $x, y$ coordinates are shown, (b) Source Locations estimated in the more-reverberant case,, only the $x, y$ coordinates are shown, (c) Height Estimate for the less-reverberant case, (d) Height Estimate for the more-reverberant case

Table 6.14: Circular indoor results using RevoLabs at 8 kHz for the case when the array was placed in the center of the hall. Fast Machine was used.

| Source Location | $\left(r \cos 30^{\circ}-r, r \sin 30^{\circ}\right.$ <br> ,0) | $\left(r \cos 30^{\circ}-r, r \sin 30^{\circ}\right.$ <br> ,1) | (-2r, 0,0 ) | $(-2 r, 0,0.5)$ | (-3r, 0, 0) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Value | (-0.2 0.7500, 0) | (-0.2, 0.7500, 1) | $(-3,0,0)$ | $(-3,0,0.5)$ | $(-4.5,0,0)$ |
| Description | In-between mic0 and 1 on the circumference at height of 0 m | In-between mic0 and 1 on the circumference at height of 1 m | At mic3 with zero height | At mic3 with 0.5 m height | Along the line (outside array) passing through mic3 and center of the array at height 0 m |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | $\begin{gathered} \hline(0.0004, \\ 0.0064,0.0040, \\ 0.0041) \end{gathered}$ | $\begin{gathered} (-0.0010, \quad 0.0032, \\ 0.0049,0.0053 \\ 0.0027) \end{gathered}$ | $\begin{gathered} (-0.0010,-0.0044, \\ -0.0074,-0.0044, \\ -0.0010) \end{gathered}$ | $\begin{gathered} (-0.0013,-0.0043, \\ -0.0089,-0.0043, \\ 0.0013) \end{gathered}$ | $\begin{gathered} (-0.0015,-0.0056, \\ -0.0086,-0.0056,- \\ 0.0015) \end{gathered}$ |
| $\begin{aligned} & T D E_{c c} \\ & \left(\tau_{10}^{c c}, \tau_{20}^{\tau c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{gathered} (0.0020, \\ 0.0049, \\ 0.0113, \\ 0.0079 \\ 0.0092) \end{gathered}$ | $\begin{array}{cc} (0.0013, & 0.0041, \\ 0.0119, & 0.0079, \\ 0.0045) \end{array}$ | $\begin{gathered} (0.0015,-0.0071, \\ -0.0069,-0.0056, \\ 0.0018) \end{gathered}$ | $\begin{gathered} (-0.0021,-0.0014, \\ -0.0064, \\ -0.0022, \\ 0.0056) \end{gathered}$ | $\begin{array}{cc} (0.0029, & 0.0010, \\ -0.0061, & -0.0065, \\ 0.0005) \end{array}$ |
| $\begin{aligned} & T D E_{O C} \\ & \left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c}, \tau_{40}^{o c}\right) \end{aligned}$ | $\begin{gathered} \hline(0.0014,0.0033, \\ 0.0057,0.0056, \\ 0.0035) \end{gathered}$ | $\begin{gathered} (-0.0007,0.0024, \\ 0.0041,0.0043, \\ 0.0024) \end{gathered}$ | $\begin{gathered} (-0.0013,-0.0047, \\ -0.0063,-0.0038 \\ -0.0015) \end{gathered}$ | $\begin{gathered} (-0.0003,-0.0031,- \\ 0.0078,-0.0037,- \\ 0.0017) \end{gathered}$ | $\begin{gathered} (0.0089,0.0024,- \\ 0.0036,-0.0030, \\ 0.0014) \end{gathered}$ |
| $\begin{aligned} & X_{C C} \\ & \left(x_{s}^{c c}, y_{s}^{c c}, \boldsymbol{Z}_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (-1.1901,0.5856 \\ -1.4665) \end{gathered}$ | $\begin{gathered} (-5.1927,-1.6669, \\ 3.6153) \end{gathered}$ | $\begin{gathered} (-1.0795,-0.1313, \\ 0.0051) \end{gathered}$ | $\begin{gathered} (-1.3075,0.3541,- \\ 2.1072) \end{gathered}$ | $\begin{gathered} (-1.3625,-0.1550,- \\ 0.6050) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (-0.6310,0.4794, \\ -0.0879) \end{gathered}$ | $\begin{gathered} (-0.6365,0.5531, \\ 0.5337) \end{gathered}$ | $\begin{gathered} (-2.7991,0.0512 \\ 0.5282) \end{gathered}$ | $\begin{gathered} (-2.3801 \\ -0.2262, .2893) \end{gathered}$ | $\begin{gathered} (-1.2150,-0.0819,- \\ 1.188) \end{gathered}$ |
| $\epsilon_{c c}$ [ $3 D$ | 1.7771 | 6.1325 | 1.9250 | 3.1284 | 3.1991 |
| $\epsilon_{c c-2 D}$ | 1.0036 | 5.5469 | 1.9250 | 1.7291 | 3.1414 |
| $\epsilon_{O C_{-} 3 D}$ | 0.5165 | 0.6684 | 0.5675 | 0.6927 | 3.4943 |
| $\epsilon_{O C-2 D}$ | 0.5089 | 0.4789 | 0.2074 | 0.6599 | 3.2860 |
| Time for CC <br> (Sec) | 0.2172 | 0.1406 | 0.1597 | 1.3229 | 0.1470 |
| Time for OC <br> (Sec) | 46.6671 | 50.7984 | 50.2909 | 53.5083 | 45.1788 |

Table 6.15: Circular indoor results using RevoLabs at 8 kHz for the case when the array was placed in a corner of the hall. Fast Machine was used.

| Source Location | $\left(r \cos 30^{\circ}-r, r \sin 30^{\circ}, 0\right)$ | $\left(r \cos 30^{\circ}-r, r \sin 30^{\circ}, 1\right)$ | $(-2 r, 0,0)$ | ( $-2 r, 0,0.5$ ) |
| :---: | :---: | :---: | :---: | :---: |
| Value | (-0.2 0.7500, 0) | (-0.2, 0.7500, 1) | (-3, 0, 0) | (-3, 0, 0.5) |
| Description | In-between mic0 and 1 on the circumference at height of 0 m | In-between mic 0 and 1 on the circumference at height of 1 m | At mic3 with zero height | At mic3 with 0.5 m height |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | $\begin{gathered} (0.0004,0.0040,0.0064, \\ 0.0062,0.0041) \end{gathered}$ | $\begin{gathered} (-0.0010, \quad 0.0032,0.0049, \\ 0.0053, \quad 0.0027) \end{gathered}$ | $\begin{gathered} (-0.0010,-0.0044,-0.0074, \\ -0.0044,-0.0010) \end{gathered}$ | $\begin{gathered} (-0.0013,-0.0043,-0.0089, \\ -0.0043,-0.0013) \end{gathered}$ |
| $\begin{aligned} & T D E_{C C} \\ & \left(\tau_{10}^{\tau c}, \tau_{20}^{c c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{gathered} (0.0022,0.0098,0.0116 \\ 0.0145,0.0040) \end{gathered}$ | $\begin{gathered} (-0.0041,0.0027,0.0077 \\ 0.0083, \quad 0.0134) \end{gathered}$ | $\begin{gathered} (0.0010,-0.0051,-0.0045, \\ -0.0003,0.0039) \end{gathered}$ | $\begin{gathered} (0.0044, \quad-0.0069, \quad-0.0074, \\ -0.0029, \quad 0.0070) \end{gathered}$ |
| $\begin{aligned} & T D E_{o c} \\ & \left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c}, \tau_{40}^{o c}\right) \end{aligned}$ | $\begin{gathered} (0.0008,0.0026,0.0051, \\ 0.0048,0.0038) \end{gathered}$ | $\begin{gathered} (-0.0005,0.0021,0.0038, \\ 0.0041,0.0024) \end{gathered}$ | $\begin{gathered} (-0.0015,-0.0047,-0.0059, \\ -0.0035,-0.0014) \end{gathered}$ | $\begin{gathered} (-0.0005,-0.0029,-0.0068, \\ -0.0034,-0.0015) \end{gathered}$ |
| $\begin{aligned} & X_{C C} \\ & \left(x_{s}^{c c}, y_{s}^{c c}, X_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (-1.9743,0.3453, \\ 2.8836) \end{gathered}$ | $\begin{gathered} (-2.2941,-0.1232, \\ -5.3467) \end{gathered}$ | $\begin{gathered} (-1.3421,0.0204, \\ -0.6997) \end{gathered}$ | $\begin{gathered} (-0.7989, \quad-0.1164, \\ -2.3374) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (-0.7621,0.5498 \\ -0.5106) \end{gathered}$ | $\begin{gathered} (-0.6702,0.5848 \\ 0.3978) \end{gathered}$ | $\begin{gathered} (-2.5398,0.0998, \\ 0.6096) \end{gathered}$ | $\begin{gathered} (-2.2858, \\ -0.1586,0.4016) \end{gathered}$ |
| $\epsilon_{c c}$ 3D | 3.4098 | 6.7400 | 1.7997 | 3.5930 |
| $\epsilon_{\text {cc_ } 2 \mathrm{D}}$ | 1.8198 | 2.2688 | 1.6581 | 2.2041 |
|  | 0.7853 | 0.7817 | 0.7703 | 0.7381 |
| $\epsilon_{O C-2 D}$ | 0.5967 | 0.4984 | 0.4709 | 0.7316 |
| Time for CC <br> (Sec) | 0.2172 | 0.1406 | 0.1597 | 1.3229 |
| Time for OC <br> (Sec) | 46.6671 | 50.7984 | 50.2909 | 53.5083 |

## Results for the 4 kHz Case

The same experimental setup was used (shown in Fig. 6.9) as that for the case of 8 kHz . Table 6.16 shows the results we obtained for the less reverberant environment and Table 6.17 shows the results for the case when the array was placed in a corner of the hall which represents an indoor more-reverberant environment.

Table 6.16: Circular indoor results using RevoLabs at 4 kHz for the case when the array was placed in the center of the hall. Slow Machine was used.

| Source <br> Location | $\begin{gathered} \left(r \cos 30^{\circ}-r,\right. \\ \left.r \sin 30^{\circ}, 0\right) \end{gathered}$ | $\begin{gathered} \left(r \cos 30^{\circ}-r,\right. \\ \left.r \sin 30^{\circ}, 1\right) \end{gathered}$ | $(-2 r, 0,0)$ | $(-2 r, 0,0.5)$ | $(-3 \mathrm{r}, 0,0)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Value | (-0.2 0.7500, 0) | (-0.2, 0.7500, 1) | (-3, 0, 0) | (-3, 0, 0.5) | (-4.5, 0, 0) |
| Description | In-between mic0 and 1 on the circumference at height of 0 m | In-between mic0 and 1 on the circumference at height of 1 m | At mic3 with zero height | At mic3 with 0.5 m height | Along the line (outside array) passing through mic3 and center of the array at height 0m |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | (0.0004, 0.0040, 0.0064, 0.0062, 0.0041 ) | $\begin{gathered} (-0.0010, \\ 0.0049, \quad 0.0032, \\ 0.0027) \end{gathered}$ | $\begin{array}{cc} \hline(-0.0010, & -0.0044, \\ -0.0074, & -0.0044, \\ -0.0010) \end{array}$ | $\begin{array}{cc} \hline(-0.0013, & -0.0043, \\ -0.0089, & -0.0043, \\ -0.0013) \end{array}$ | $\begin{array}{cc} \hline(-0.0015, & -0.0056, \\ -0.0086, & -0.0056, \\ -0.0015) \end{array}$ |
| $\begin{aligned} & T D E_{C C} \\ & \left(\tau_{10}^{c c}, \tau_{20}^{c c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{gathered} (0,0.0125, \\ 0.0092,0.0055, \\ 0.0118) \\ \hline \end{gathered}$ | $(0.0018$, 0.0032, <br> 0.0073, 0.0047, <br> $0.0083)$  | $\begin{gathered} (0.0040,-0.0013, \\ -0.0045,-0.0020, \\ 0.0047) \end{gathered}$ | $\begin{gathered} (0.0040,-0.0013, \\ -0.0045,-0.0020, \\ 0.0047) \\ \hline \end{gathered}$ | $\begin{array}{cc} (0.0010, & 0.0047, \\ -0.0063, & -0.0065, \\ 0.0005) \end{array}$ |
| $\begin{aligned} & T D E_{O C} \\ & \left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c}, \tau_{40}^{o c}\right. \end{aligned}$ | (0, -0.0013, 0.0053, 0.0013, -0.0008) | $\begin{array}{cc} (0.2500, & -0.7500, \\ 0.2500, & 0.2500 \\ 0.7500) \\ \hline \end{array}$ | $\begin{gathered} (0.0018,-0.0020, \\ -0.0030,-0.0005, \\ -0.0003) \\ \hline \end{gathered}$ | $\begin{gathered} (0.0018,-0.0020, \\ -0.0030,-0.0005, \\ -0.0003) \\ \hline \end{gathered}$ | $\begin{array}{cc} (-0.0003, & 0.0010, \\ -0.0015, & -0.0013, \\ 0.0050) \end{array}$ |
| $\begin{aligned} & X_{C c} \\ & \left(x_{s}^{c c}, y_{s}^{c c}, z_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (-2.3313,-0.6064 \\ 0.4805) \end{gathered}$ | $\begin{gathered} (-1.8464,0.1032 \\ 0.0713) \end{gathered}$ | $\begin{gathered} (-1.4135,0.1001 \\ -1.7072) \end{gathered}$ | $\begin{gathered} (-1.4135,0.1001, \\ -1.7072) \end{gathered}$ | $\begin{gathered} (-0.7240,0.0093, \\ 1.3066) \end{gathered}$ |
| $\begin{aligned} & X_{O C} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, \boldsymbol{Z}_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (-0.9155,0.1295 \\ -0.0934) \end{gathered}$ | $\begin{gathered} (-1.5528,0.1499 \\ -0.3683) \end{gathered}$ | $\begin{gathered} (-1.7876,-0.1206, \\ -0.3870) \end{gathered}$ | $\begin{gathered} (-1.7876,-0.1206 \\ -0.3870) \end{gathered}$ | $\begin{gathered} (-1.4542,0.1771 \\ -0.2648) \end{gathered}$ |
| $\epsilon_{\text {cc_ } 3 D}$ | 2.5716 | 1.9978 | 2.3327 | 2.7201 | 3.9957 |
| $\epsilon_{c c \_2 D}$ | 2.5263 | 1.7689 | 1.5897 | 1.5897 | 3.7760 |
| $\epsilon_{\text {OC_3 }}{ }_{\text {c }}$ | 0.9517 | 2.0156 | 1.2784 | 1.5071 | 3.0625 |
| $\epsilon_{\text {OC_2 }}$ | 0.9471 | 1.4799 | 1.2184 | 1.2184 | 3.0510 |
| Time for CC <br> (Sec) | 0.0522 | 0.0454 | 0.0457 | 0.0456 | 0.0468 |
| Time for OC <br> (Sec) | 21.1344 | 17.5049 | 20.8175 | 20.7418 | 17.8947 |

We plot the $x, y$ coordinates of the actual and estimated source locations for the less-reverberant case in Fig. 6.11a and Fig. 6.11b plots the $x, y$ coordinates for the more-reverberant case. Fig. 6.11c and Fig. 6.11d plots the bargraphs for

Table 6.17: Circular indoor results using RevoLabs at 4 kHz for the case when the array was placed in a corner of the hall. Slow Machine was used.

| Source Location | $\left(r \cos 30^{\circ}-r, r \sin 30^{\circ}, 0\right)$ | $\left(r \cos 30^{\circ}-r, r \sin 30^{\circ}, 1\right)$ | $(-2 r, 0,0)$ | (-2r, 0, 0.5) |
| :---: | :---: | :---: | :---: | :---: |
| Value | (-0.2 0.7500, 0) | (-0.2, 0.7500, 1) | (-3, 0, 0) | (-3, 0, 0.5) |
| Description | In-between mic0 and 1 on the circumference at height of 0 m | In-between mic0 and 1 on the circumference at height of 1 m | At mic3 with zero height | At mic3 with 0.5 m height |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | $\begin{gathered} (0.0004,0.0040,0.0064, \\ 0.0062,0.0041) \end{gathered}$ | $\begin{gathered} (-0.0010,0.0032, \quad 0.0049 \\ 0.0053, \\ 0.0027) \end{gathered}$ | $\begin{gathered} (-0.0010,-0.0044,-0.0074 \\ -0.0044, \quad-0.0010) \end{gathered}$ | $\begin{gathered} (-0.0013,-0.0043,-0.0089 \\ -0.0043,-0.0013) \end{gathered}$ |
| $\begin{aligned} & T D E_{C c} \\ & \left(\tau_{10}^{c c}, \tau_{20}^{c c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{gathered} (0.0047,0.0147,0.0115, \\ 0.0187,0.0085) \end{gathered}$ | $\begin{gathered} (0.0008,-0.0020,0.0100, \\ 0.0057,-0.0010) \end{gathered}$ | $\begin{gathered} (0.0010, \quad 0.0005,-0.0077, \\ -0.0035, \quad 0.0088) \end{gathered}$ | $\begin{gathered} (-0.0005,-0.0053,-0.0115, \\ -0.0063, \quad 0.0053) \end{gathered}$ |
| $\begin{aligned} & \text { TDE }{ }_{o c} \\ & \left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c}, \tau_{40}^{o c}\right) \end{aligned}$ | $\begin{gathered} (0.0022,0.0035,0.0027, \\ 0.0060,0.0020) \end{gathered}$ | $\begin{gathered} (-0.0015,0.0027, \quad 0, \\ 0.0010,0.0015) \end{gathered}$ | $\begin{gathered} (0.0010,-0.0010,-0.0013, \\ -0.0008, \quad 0.0018) \end{gathered}$ | $\begin{gathered} (0.0005,-0.0032,-0.0027, \\ -0.0032, \quad-0.0008) \end{gathered}$ |
| $\begin{aligned} & X_{c c} \\ & \left(x_{s}^{c c}, y_{s}^{c c}, \boldsymbol{Z}_{s}^{c c}\right) \end{aligned}$ | (-1.4518, 0.5873, 7.7525) | $(-1.2221,-0.1445,-0.1691)$ | $(-1.1253,0.9294,-3.8466)$ | (-1.5333, 0.8111, -4.1501) |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | (-0.7377, 0.3325, -0.0450) | (-1.1163, 0.0331, 1.1544) | (-1.7843, 0.1202, -1.4160) | (-2.0937, -0.1438, -0.6772) |
| $\epsilon_{c c, 3 D}$ | 7.8546 | 1.7922 | 4.3789 | 4.9430 |
| $\epsilon_{c c-2 D}$ | 1.2624 | 1.3583 | 2.0925 | 1.6761 |
| $\epsilon_{o c}$ 3D | 0.6823 | 1.1736 | 1.8701 | 1.4926 |
| $\epsilon_{\text {OC_2D }}$ | 0.6808 | 1.1634 | 1.2216 | 0.9177 |
| Time for CC <br> (Sec) | 0.0464 | 0.0472 | 0.0465 | 0.0543 |
| Time for OC <br> (Sec) | 26.0555 | 22.3360 | 22.8007 | 18.6865 |

the height of source locations for the case of less- and more-reverberant scenarios respectively.


Figure 6.11: Circular Geometry Source Locations Estimated by CC and OC at 4 kHz Indoor using RevoLabs system, (a) Source Locations estimated in the less-reverberant case, only the $x, y$ coordinates are shown, (b) Source Locations estimated in the more-reverberant case,, only the $x, y$ coordinates are shown, (c) Height Estimate for the less-reverberant case, (d) Height Estimate for the more-reverberant case

### 6.2.3 Rhombus Geometry Experiments and Results

Now we will discuss the Rhombus geometry results in indoor environment. We are using the geometry with the source locations discussed in Section 5.2.1. The values of different parameters of the OC algorithm were the same as were decided in Section 6.1.

(b)

Figure 6.12: Indoor Rhombus Geometry Experimental Setup Using RevoLabs System, (a) Indoor Rhombus Geometry in the Center of the Hall using RevoLabs System, (b) Indoor Rhombus Geometry in a Corner of the Hall using RevoLabs System.

Like Pyramid and Circular geometries there are two different experimental scenarios i.e. i) experimenting in the center of the hall and ii) experimenting in a corner of the hall. The experimental setup for these scenarios is shown in Fig. 6.12. Fig. 6.12a shows the case of array placed in the center of hall while Fig. 6.12 b shows the case of array placed in a corner of the hall.

Two different sampling rates of 8 kHz and 4 kHz were used during experiments. We also captured signals at 16 kHz sampling rate but we could not run the OC algorithm for this case as the memory required for OC algorithm is quite large (our system had 8 gigabyte RAM and still it was not able to run the MATLAB code). CC can be run for 16 kHz rate but then we would not be able to compare it with OC and that is why we did not runt it for 16 kHz . The results for all these scenarios follow next.

## Results for the Case of 8 kHz

We run the OC algorithm for the experimental signals captured at 8 kHz . The results for the case of array being in the center of the hall are given in Table 6.18 while Table 6.19 shows the results for the case of array placed in a corner of the hall.

We plot the $x, y$ coordinates of the actual and estimated source locations for the less-reverberant case in Fig. 6.13a and Fig. 6.13b plots the $x, y$ coordinates for the more-reverberant case. Fig. 6.13c and Fig. 6.13d plots the bargraphs for the height of source locations for the case of less- and more-reverberant scenarios respectively.


Figure 6.13: Rhombus Geometry Source Locations Estimated by CC and OC at 8 kHz Indoor using RevoLabs system, (a) Source Locations estimated in the less-reverberant case, only the $x, y$ coordinates are shown, (b) Source Locations estimated in the more-reverberant case,, only the $x, y$ coordinates are shown, (c) Height Estimate for the less-reverberant case, (d) Height Estimate for the more-reverberant case.

Table 6.18: Rhombus indoor results using RevoLabs at 8 kHz for the case when the array was placed in the center of the hall. Fast Machine was used.

| Source Location | (2r, 0, h) | ( $\mathbf{r}, \mathbf{0}, 2 \mathrm{~h}$ ) | $\begin{aligned} & \left(2 r \cos 45^{\circ},\right. \\ & \left.2 r \sin 45^{\circ}, 2 h\right) \end{aligned}$ | $\begin{aligned} & \left(2 r \cos 75^{\circ},\right. \\ & \left.2 r \sin 75^{\circ}, h\right) \end{aligned}$ | $\begin{aligned} & \left(2 r \cos 88^{\circ},\right. \\ & \left.2 r \sin 88^{\circ}, h\right) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Value | (3, 0, 0.5) | (3, 0, 1) | (2.12, 2.12, 1.00) | (0.77, 2.89, 0.5) | (0.10, 2.99, 0.5) |
| Description | On the line passing through mic1 and center of the array at height of 0.5 m | On the line passing through micl and center of the array at height of 1 m | In-between mic 1 and 2 outside the circumference on which mics lye. | At angle of $75^{\circ}$ between mic 1 and 2 | At angle of $88^{\circ}$ between mic 1 and 2 |
| $\begin{gathered} \text { Exact TDs } \\ \left(\boldsymbol{\tau}_{10}, \boldsymbol{\tau}_{\mathbf{2 0}}, \boldsymbol{\tau}_{\mathbf{3 0}}, \boldsymbol{\tau}_{40}\right) \end{gathered}$ | $\left.\begin{array}{cc} (-0.0045, & 0.0009 \\ 0.0043, & 0, \\ \hline \end{array}\right)$ | $\begin{gathered} (-0.0047, \quad 0.0007, \\ 0.0040,-0.0002, \\ 0.0005) \\ \hline \end{gathered}$ | $\begin{gathered} (-0.0026,-0.0026, \\ 0.0031,0.0007, \\ 0.0005) \\ \hline \end{gathered}$ | $\begin{array}{cc} \hline(-0.0002, & -0.0042, \\ 0.0019, & 0.0013, \\ 0) \end{array}$ | $\begin{array}{cc} (0.0008, & -0.0045, \\ 0.0011, & 0.0013, \\ 0) \end{array}$ |
| $\begin{aligned} & \boldsymbol{T D E} E_{c c} \\ & \left(\boldsymbol{\tau}_{10}^{c c}, \boldsymbol{\tau}_{20}^{c c}, \boldsymbol{\tau}_{30}^{c \epsilon}, \boldsymbol{\tau}_{40}^{c \mathrm{c}}\right) \end{aligned}$ | $\begin{array}{cc} (0.0001, & -0.0014, \\ 0.0016, & 0.0015, \\ 0.0011) \end{array}$ | $\begin{array}{cc} (-0.0037, & 0.0011, \\ 0.0092, & 0.0001, \\ 0.0008) \end{array}$ | $\begin{gathered} (-0.0016,-0.0025, \\ 0.0066,0.0041, \\ 0.0040) \end{gathered}$ | $\begin{array}{ccc} \hline 0.0026, & -0.0034, & - \\ 0.0019, & 0.0022, & - \\ 0.0027) \end{array}$ | $\begin{gathered} (0,-0.0009, \\ 0.0113, \quad 0.0036, \\ 0.0039) \end{gathered}$ |
| $\begin{aligned} & T D E_{o c} \\ & \left(\boldsymbol{\tau}_{10}^{o c}, \boldsymbol{\tau}_{20}^{o o}, \boldsymbol{\tau}_{30}^{o c}, \boldsymbol{\tau}_{40}^{o g}\right) \end{aligned}$ | $\begin{gathered} \hline(-0.0003,0.0005, \\ 0.0036,0.0009, \\ 0.0011) \end{gathered}$ | $\begin{gathered} \hline-0.0012,0.0013, \\ 0.0030, \\ -0.0009,-0.0020) \end{gathered}$ | $\begin{gathered} (-0.0026,-0.0032, \\ 0.0029,0.0012,- \\ 0.009) \end{gathered}$ | $\begin{gathered} (-0.0009,-0.0100, \\ 0.0030,0.0020, \\ 0.0005) \end{gathered}$ | $\begin{gathered} \hline(0.0015,-0.00030, \\ 0.0029,0.0036 \\ 0.0010) \end{gathered}$ |
| $\begin{aligned} & X_{c c} \\ & \left(x_{s}, y_{s}^{c c}, z_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (1.3348,4.0596,- \\ 2.5483) \end{gathered}$ | $\begin{gathered} (-2.1503,0.9416, \\ 1.2194) \end{gathered}$ | $\begin{gathered} (0.9136,0.9012,- \\ 0.6042) \end{gathered}$ | $\begin{gathered} (-0.4036,0.7654, \\ 0.7835) \end{gathered}$ | $\begin{gathered} (0.1023,-0.4085, \\ 2.2758) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (1.0140,0.6643,- \\ 0.1714) \end{gathered}$ | $\begin{gathered} (0.7455,0.0120, \\ 1.1372) \end{gathered}$ | $\begin{gathered} (1.0907,1.4063, \\ 1.0142) \end{gathered}$ | $\begin{gathered} (1.4865,3.8414,- \\ 0.1101) \end{gathered}$ | $\begin{gathered} (0.1592,0.8330, \\ 0.4595) \end{gathered}$ |
| $\epsilon_{\text {cc } \text { c } 3 \mathrm{D}}$ | 5.3428 | 5.2403 | 2.3483 | 2.4437 | 3.8345 |
| $\epsilon_{\text {cce } 2 \mathrm{D}}$ | 4.3878 | 5.2357 | 1.7149 | 2.4272 | 3.3985 |
|  | 2.1991 | 2.2587 | 1.2526 | 1.3382 | 2.1461 |
| $\epsilon_{\text {Oc. } 2 \mathrm{D}}$ | 2.0941 | 2.2545 | 1.2525 | 1.1910 | 2.1457 |
| $\begin{aligned} & \text { Time for CC } \\ & \text { (Sec) } \end{aligned}$ | 0.0977 | 0.2304 | 0.0985 | 0.0446 | 0.2216 |
| Time for OC (Sec) | 191.6126 | 309.6996 | 62.0895 | 56.1844 | 83.4175 |

Table 6.19: Rhombus indoor results using RevoLabs at 8 kHz for the case when the array was placed in a corner of the hall. Fast Machine was used.

| Source Location | (2r, 0, h) | ( $\mathbf{2 r}, \mathbf{0}, 2 \mathrm{~h}$ ) | $\begin{aligned} & \left(2 r \cos 45^{\circ},\right. \\ & \left.2 r \sin 45^{\circ}, 2 h\right) \end{aligned}$ | $\begin{aligned} & \left(2 r \cos 75^{\circ},\right. \\ & \left.2 r \sin 75^{\circ}, h\right) \end{aligned}$ | $\begin{aligned} & \left(2 r \cos 88^{\circ},\right. \\ & \left.-2 r \sin 88^{\circ}, h\right) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Value | (3, 0, 0.5) | (3, 0, 1) | (2.12, 2.12, 1.00) | (0.77, 2.89, 0.5) | (0.10, -2.99, 0.5) |
| Description | On the line passing through mic 1 and center of the array at height of 0.5 m | On the line passing through mic 1 and center of the array at height of 1 m | In-between mic 1 and 2 outside the circumference on which mics lye. | At angle of $75^{\circ}$ between mic 1 and 2 | At angle of $88^{\circ}$ between mic 1 and 2 |
| $\begin{gathered} \text { Exact TDs } \\ \left(\boldsymbol{\tau}_{10}, \boldsymbol{\tau}_{20}, \boldsymbol{\tau}_{30}, \boldsymbol{\tau}_{40}\right) \end{gathered}$ | $\left.\begin{array}{cc} (-0.0045, & 0.0009, \\ 0.0043, & 0, \end{array} 0\right)$ | $\begin{gathered} \hline(-0.0047, \quad 0.0007, \\ 0.0040,-0.0002, \\ -0.0005) \\ \hline \end{gathered}$ | $\begin{array}{cc} \hline(-0.0026, & -0.0026, \\ 0.0031, & 0.0007, \\ -0.0005) \\ \hline \end{array}$ | $\begin{array}{cc} \hline(-0.0002, & -0.0042, \\ 0.0019, & 0.0013, \\ 0) & \\ \hline \end{array}$ | $\begin{array}{cc} (0.0008, & -0.0045, \\ 0.0011, & 0.0013, \\ 0) \end{array}$ |
| $\begin{aligned} & \boldsymbol{T D E} E_{c c} \\ & \left(\boldsymbol{\tau}_{10}^{c c}, \boldsymbol{\tau}_{20}^{c c}, \boldsymbol{\tau}_{30}^{c c}, \boldsymbol{\tau}_{40}^{c c}\right) \end{aligned}$ | $(-0.0029$, $0.0140, \quad 0.0003$, $0.0031)$ | $(-0.0032,0.0024$, $0.0061, \quad 0.0001$, $0.0005)$ | $\begin{array}{cc} (0.0035, & -0.0044, \\ 0.0063, & 0.0034, \\ -0.0116) \end{array}$ | $\begin{array}{cc} \hline(-0.0109, & -0.0079, \\ -0.0010, & 0.0076, \\ -0.0050) \end{array}$ | $\begin{array}{cc} \hline 0.0021, & 0.0101, \\ 0.0049, & -0.0024, \\ 0.0031) \end{array}$ |
|  | $(-0.0006$,  <br> -0.0026, 0.0010, <br> -0.0018, $-0.0006)$ | $(0.0020$, 0.0008, <br> 0.0069, 0.0026, <br> $0.0006)$  | $\begin{array}{cc} (-0.0004, & -0.0013, \\ 0.0036, & 0.0024, \\ 0.0004) \end{array}$ | $(0.0020$, 0.0019, <br> 0.0029, 0.0074, <br> $0.0026)$  | $\begin{array}{cc} \hline 0.0026, & -0.0021, \\ 0.0054, & 0.0049, \\ 0.0043) \end{array}$ |
| $\begin{aligned} & \hline X_{c c} \\ & \left(x_{s}^{\tau c}, y_{s}^{c c},,_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (-1.1178,-0.1888, \\ 2.0933) \end{gathered}$ | $\begin{gathered} (-0.4590,0.7892, \\ 0.7679) \end{gathered}$ | $\begin{gathered} (0.8369,1.9320, \\ -3.0544) \end{gathered}$ | $\begin{gathered} (-2.6302,-0.8123, \\ -3.3523) \end{gathered}$ | $\begin{gathered} (0.8101,-5.4995, \\ -2.1443) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (0.1703,0.5928, \\ 1.3107) \end{gathered}$ | $\begin{gathered} (0.6552, \quad 0.6313, \\ 0.6028) \end{gathered}$ | $\begin{gathered} (0.6115,0.9707, \\ 0.3603) \end{gathered}$ | $\begin{gathered} (-0.0445,0.6594, \\ 1.9767) \end{gathered}$ | $\begin{gathered} (0.6103,1.5906, \\ -1.5742) \end{gathered}$ |
| $\epsilon_{c c, 3 D}$ | 4.4194 | 3.5555 | 4.2567 | 6.3921 | 3.7140 |
| $\epsilon_{c c .2 D}$ | 4.1221 | 3.5479 | 1.2968 | 5.1009 | 2.6080 |
| $\epsilon_{\text {Oc }}{ }_{\text {c } 3 \mathrm{D}}$ | 3.0027 | 2.4606 | 2.0014 | 2.7964 | 2.5536 |
| $\epsilon_{\text {OC.2D }}$ | 2.8912 | 2.4283 | 1.8964 | 2.3747 | 1.4895 |
| $\begin{aligned} & \text { Time for } \mathrm{CC} \\ & \text { (Sec) } \end{aligned}$ | 0.0370 | 0.0370 | 0.0355 | 0.0369 | 0.0369 |
| Time for $\mathbf{O C}$ (Sec) | 67.6747 | 62.1999 | 70.1450 | 369.7572 | 50.6591 |

## Results for the Case of 4 kHz

For the 4 kHz the same experimental setup was used as for the 8 kHz case shown
in Fig. 6.12. The results for the case of array being in the center of the hall are
given in Table 6.20 while Table 6.21 shows the results for the case of array placed
in a corner of the hall.
Table 6.20: Rhombus indoor results using RevoLabs at 4 kHz for the case when the array was placed in the center of the hall. Slow Machine was used.

| Source Location | (2r, 0, h) | (2r, 0, 2h) | $\begin{aligned} & \left(2 r \cos 45^{\circ},\right. \\ & \left.2 r \sin 45^{\circ}, 2 h\right) \end{aligned}$ | $\begin{aligned} & \left(2 r \cos 75^{\circ},\right. \\ & \left.2 r \sin 75^{\circ}, h\right) \end{aligned}$ | $\begin{aligned} & \left(2 r \cos 88^{\circ},\right. \\ & \left.2 r \sin 88^{\circ}, h\right) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Value | (3, 0, 0.5) | (3, 0, 1) | (2.12, 2.12, 1.00) | (0.77, 2.89, 0.5) | (0.10, 2.99, 0.5) |
| Description | On the line passing through mic 1 and center of the array at height of 0.5 m | On the line passing through mic 1 and center of the array at height of 1 m | In-between mic 1 and 2 outside the circumference on which mics lye. | At angle of $75^{\circ}$ between mic 1 and 2 | At angle of $88^{\circ}$ between mic 1 and 2 |
| $\begin{gathered} \text { Exact TDs } \\ \left(\boldsymbol{\tau}_{10}, \boldsymbol{\tau}_{\mathbf{2 0}}, \boldsymbol{\tau}_{\mathbf{3 0}}, \boldsymbol{\tau}_{\mathbf{4 0}}\right) \end{gathered}$ | $\begin{array}{lll} (-0.0045, & 0.0009, \\ 0.0043, & 0, & 0) \end{array}$ | $\begin{gathered} -0.0047,0.0007, \\ 0.0040,-0.0002,- \\ 0.0005) \end{gathered}$ | $\begin{gathered} \left(-0.0026,{ }^{-0.0026,}\right. \\ 0.0031,0.0007,- \\ 0.0005) \end{gathered}$ | $\begin{aligned} & (-0.0002, \\ & 0.0019,0.0042, \\ & 0) \\ & 0.0013, \end{aligned}$ | $\begin{aligned} & \begin{array}{l} (0.0008, \\ 0.0011, \\ 0.00045, \\ 0.0013, \end{array} \\ & \hline \end{aligned}$ |
| $\begin{aligned} & T D E_{c c} \\ & \left(\boldsymbol{\tau}_{10}^{c c}, \boldsymbol{\tau}_{20}^{c c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{gathered} (-0.0003, \quad 0.0095, \\ 0.0080 . \quad 0.0045, \\ 0.0027) \end{gathered}$ | $\begin{gathered} (0.0015, \\ 0.0080,-0.00018, \\ 0.0018) \end{gathered}$ | $\begin{gathered} (-0.0010, \quad 0.0005, \\ 0.0063, \quad 0.0037, \\ 0.0040) \end{gathered}$ | $\begin{gathered} \hline(0.0018,-0.0027, \\ -0.0022,-0.0022, \\ -0.0018) \end{gathered}$ | $\begin{gathered} (0.0103, \quad 0.0008, \\ -0.0010, \quad 0.0063, \\ 0.0013) \end{gathered}$ |
| $\begin{aligned} & \text { TDE }{ }_{o c} \\ & \left(\boldsymbol{\tau}_{10}^{o c}, \boldsymbol{\tau}_{20}^{o c}, \boldsymbol{\tau}_{30}^{o c}, \tau_{40}^{o c}\right) \end{aligned}$ | $\begin{array}{cc} (-0.0027, & -0.0018, \\ 0.0027, & -0.0020, \end{array}$ <br> 0 ) | $(0.0003$, 0.0025, 0.0008, 0.0003, | $\begin{gathered} \hline 0.0005, r \\ 0.0037, \quad 0.0020, \\ 0.0037) \end{gathered}$ | $\begin{gathered} \hline(-0.0010,-0.0037, \\ -0.0013,-0.0015, \\ -0.0027) \end{gathered}$ | $\begin{gathered} \hline 0.0055,-0.0010, \\ 0.0030,0.0020, \\ 0.0022) \end{gathered}$ |
| $\begin{aligned} & \boldsymbol{X}_{c c} \\ & \left(\boldsymbol{x}_{s}^{c c}, \boldsymbol{y}_{s}^{c c}, \boldsymbol{Z}_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (0.2274,-0.6758, \\ 1.1663) \end{gathered}$ | $\begin{gathered} (0.7030, \quad 0.6986, \\ 0.7819) \end{gathered}$ | $\begin{gathered} (1.2434, \quad 1.1928, \\ -1.2197) \end{gathered}$ | $\begin{gathered} (-0.3748,0.5857, \\ 1.4128) \end{gathered}$ | $\begin{gathered} (-0.4298, \quad 0.6130, \\ 0.9153) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (0.1469,0.5171, \\ 0.8753) \end{gathered}$ | $\begin{gathered} (-0.1002, \\ 0.6371, \quad 1.2008) \end{gathered}$ | $\begin{gathered} (1.0207,1.4610, \\ -2.1807) \end{gathered}$ | $\begin{gathered} (-0.0481, \quad 1.0586 \\ 2.7918) \end{gathered}$ | $\begin{gathered} (-0.3984, \quad 0.6275, \\ 0.3538) \end{gathered}$ |
| $\epsilon_{\text {cc }{ }_{\text {c }} \text { D }}$ | 2.9305 | 2.4108 | 2.5603 | 2.7301 | 2.4705 |
| $\epsilon_{\text {cc. } 2 \mathrm{D}}$ | 2.8538 | 2.4009 | 1.2760 | 2.5730 | 2.4354 |
| $\epsilon_{\text {oc }}{ }_{\text {c } 3 \mathrm{D}}$ | 2.9237 | 3.1713 | 3.4292 | 3.0456 | 2.4189 |
| $\epsilon_{\text {OC.2D }}$ | 2.8995 | 3.1650 | 1.2817 | 2.0058 | 2.4145 |
| Time for $\mathbf{C C}$ (Sec) | 0.0464 | 0.1200 | 0.8762 | 0.0481 | 0.0528 |
| $\begin{aligned} & \text { Time for } \mathrm{OC} \\ & \text { (Sec) } \end{aligned}$ | 51.0664 | 198.7423 | 143.7500 | 246.7433 | 177.3496 |

Table 6.21: Rhombus indoor results using RevoLabs at 4 kHz for the case when the array was placed in a corner of the hall. Slow Machine was used.

| Source Location | (2r, 0, h) | ( $2 \mathrm{r}, 0,2 \mathrm{~h}$ ) | $\begin{aligned} & \left(2 r \cos 45^{\circ},\right. \\ & \left.2 r \sin 45^{\circ}, 2 h\right) \end{aligned}$ | $\begin{aligned} & \left(2 r \cos 75^{\circ},\right. \\ & \left.2 r \sin 75^{\circ}, h\right) \end{aligned}$ | $\begin{aligned} & \left(2 r \cos 88^{\circ},\right. \\ & \left.2 r \sin \left(\pi+88^{\circ}\right), h\right) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Value | (3, 0, 0.5) | (3, 0, 1) | (2.12, 2.12, 1.00) | (0.77, 2.99, 0.5) | (0.10, -2.99, 0.5) |
| Description | On the line passing through mic1 and center of the array at height of 0.5 m | On the line passing through mic 1 and center of the array at height of 1 m | In-between mic1 and 2 outside the circumference on which mics lye. | At angle of $75^{\circ}$ <br> between mic 1 and 2 | At angle of $88^{\circ}$ between mic4 and 5 |
| $\begin{gathered} \text { Exact TDs } \\ \left(\boldsymbol{\tau}_{10}, \boldsymbol{\tau}_{20}, \boldsymbol{\tau}_{30}, \boldsymbol{\tau}_{40}\right) \end{gathered}$ | $\left.\begin{array}{c} (-0.0045, \\ 0.0009, \\ 0.0043, \end{array} \quad 0, \quad 0\right)$ | $\begin{gathered} (-0.0047,0.0007,0.0040, \\ -0.0002,-0.0005) \end{gathered}$ | $\begin{gathered} (-0.0026,-0.0026,0.0031, \\ 0.0007,-0.0005) \end{gathered}$ | $\begin{array}{cc} \hline(-0.0001, & -0.0043, \\ 0.0018, & 0.0013, \end{array}$ | $\begin{array}{cc} \hline(0.0008, & 0.0043, \\ 0.0011, & -0.0016, \end{array}$ |
|  | $\begin{gathered} (0.0018,0.0110,0.0168, \\ 0.0075, \quad 0.0035) \end{gathered}$ | $\begin{gathered} (-0.0040,0.0045,0.0113, \\ 0.0008, \quad 0.0043) \end{gathered}$ | (0.0018, 0.0010, $0.0053,0.0040,0.0015)$ | (-0.0045, -0.0100, <br> $0.0065,0.0095,-0.0055)$ | $\begin{array}{cc} \hline 0.0035, & -0.0053, \\ 0.0182, & -0.0168, \\ 0.0010) \end{array}$ |
| $\begin{aligned} & T D E_{o c} \\ & \left(\boldsymbol{\tau}_{10}^{a}, \boldsymbol{\tau}_{20}^{a}, \boldsymbol{\tau}_{30}^{a c}, \boldsymbol{\tau}_{40}^{a}\right) \end{aligned}$ | $\begin{array}{ccc} (0, & 0.0020, & 0.0043, \\ 0.0030, & 0.0035) \end{array}$ | (-0.0013, -0.0008, 0.0020, -0.0030, -0.0027) | (-0.0005, 0.0022, <br> $0.0035,0.0015,0.0022$, | (0.0010, -0.0020, -$0.0005,-0.0040,-0.0032)$ | $(0.0025,-0.0020,-$ $0.0018,-0.0043,-$ $0.0035)$ |
| $\begin{aligned} & X_{c c} \\ & \left(x_{s}^{c c}, y_{s}^{c c}, Z_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (1.4493,0.5969, \\ 2.6610) \end{gathered}$ | (-6.2309, 2.9453, 6.2661) | $\begin{gathered} (0.4504, \quad 0.7719, \\ 0.3735) \end{gathered}$ | $\begin{gathered} (-1.3827,-4.9766,- \\ 3.2025) \end{gathered}$ | $\begin{gathered} \text { (6.9532, } 4.8568, \\ -9.5040) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (0.6940, \quad 0.6608, \\ -0.7102) \end{gathered}$ | $\begin{gathered} (0.4880, \quad 0.4083, \\ 1.5759) \end{gathered}$ | $\begin{gathered} (1.3885,-0.0381, \\ -1.6142) \end{gathered}$ | $\begin{gathered} (-0.2182, \quad 0.5655, \\ 1.7190) \end{gathered}$ | $\begin{gathered} (-0.5450, \quad 0.6186, \\ 1.3547) \end{gathered}$ |
| $\epsilon_{\text {cc } \text { c } 3 D}$ | 2.7260 | 11.0280 | 2.2355 | 9.0448 | 14.4437 |
| $\epsilon_{\text {cc- } 2 \mathrm{D}}$ | 1.6616 | 9.6894 | 2.1460 | 8.2523 | 10.4182 |
| $\epsilon_{\text {Oc_ } 3 \mathrm{D}}$ | 2.6868 | 2.6093 | 3.4679 | 2.8881 | 3.7641 |
| $\epsilon_{\text {OC.2D }}$ | 2.3988 | 2.5450 | 2.2787 | 2.6182 | 3.6658 |
| $\begin{aligned} & \text { Time for CC } \\ & \text { (Sec) } \end{aligned}$ | 0.1255 | 1.1706 | 1.1435 | 0.2140 | 2.4819 |
| $\begin{aligned} & \text { Time for OC } \\ & \text { (Sec) } \end{aligned}$ | 283.6486 | 111.0679 | 110.458 | 710.8866 | 279.8250 |

We plot the $x, y$ coordinates of the actual and estimated source locations for
the less-reverberant case in Fig. 6.14a and Fig. 6.14b plots the $x, y$ coordinates for the more-reverberant case.


Figure 6.14: Rhombus Geometry Source Locations Estimated by CC and OC at 4 kHz Indoor using RevoLabs system, (a) Source Locations estimated in the less-reverberant case, only the $x, y$ coordinates are shown, (b) Source Locations estimated in the more-reverberant case,, only the $x, y$ coordinates are shown, (c) Height Estimate for the less-reverberant case, (d) Height Estimate for the more-reverberant case.

Fig. 6.14c and Fig. 6.14d plots the bargraphs for the height of source locations
for the case of less- and more-reverberant scenarios respectively.

### 6.2.4 Observations for the Experiments using RevoLabs System

Looking at the results in subsections 6.2.1 to 6.2 .3 we can find the numerical facts about the results. We present these numerical facts in subsection 6.2.4 and then based on these numerical facts we deduce the observations and present them in subsection 6.2.4

## Numerical Facts

1. For the Pyramid 8 kHz , less-reverberant case: $80 \%$ of the time OC produces more correct results than CC by a factor of at least 2.3 i.e. OC 3D-MSE $\left(\epsilon_{O C \_3 D}\right)$ is at least 2.3 times less than CC 3D-MSE $\left(\epsilon_{C C \_3 D}\right)$ for $80 \%$ of the source locations. The runtime for OC is at least 900 times more than the runtime for CC.
2. For the Pyramid 8 kHz , more-reverberant case: $100 \%$ of the time OC produces more correct results than CC by a factor of at least 1.21. The runtime for OC is at least 1000 times more than the runtime for CC.
3. For the Pyramid 4 kHz , less-reverberant case: $100 \%$ of the time OC produces more correct results than CC by a factor of at least 1.44. The runtime for OC is at least 300 times more than the runtime for CC.
4. For the Pyramid 4 kHz , more-reverberant case: $80 \%$ of the time OC produces more correct results than CC by a factor of at least 1.15. The runtime for OC is at least 300 times more than the runtime for CC.
5. For the Circular 8 kHz , less-reverberant case: $80 \%$ of the time OC produces more correct results than CC by a factor of at least 3.44. The runtime for OC is at least 200 times more than the runtime for CC .
6. For the Circular 8 kHz , more-reverberant case: $100 \%$ of the time OC produces more correct results than CC by a factor of at least 2.33 . The runtime for OC is at least 200 times more than the runtime for CC.
7. For the Circular 4 kHz , less-reverberant case: $80 \%$ of the time OC produces more correct results than CC by a factor of at least 1.3. The runtime for OC is at least 380 times more than the runtime for CC.
8. For the Circular 4 kHz , more-reverberant case: $100 \%$ of the time OC produces more correct results than CC by a factor of at least 1.52. The runtime for OC is at least 340 times more than the runtime for CC.
9. For the Rhombus 8 kHz , less-reverberant case: $100 \%$ of the time OC produces more correct results than CC by a factor of at least 1.78. The runtime for OC is at least 600 times more than the runtime for CC .
10. For the Rhombus 8 kHz , more-reverberant case: $100 \%$ of the time OC produces more correct results than CC by a factor of at least 1.44. The runtime for OC is at least 1300 times more than the runtime for CC.
11. For the Rhombus 4 kHz , less-reverberant case: $60 \%$ of the time CC produces more correct results than OC by a factor of at least 1.115. The runtime for OC is at least 1100 times more than the runtime for CC.
12. For the Rhombus 4 kHz , more-reverberant case: $80 \%$ of the time OC produces more correct results than CC by a factor of at least 1.014. The runtime for OC is at least 90 times more than the runtime for CC.

## Indoor RevoLabs Experiments Observations

Looking at the numerical facts in subsection 6.2 .4 we can make the following observations for the experiments carried out indoor using RevoLabs system.

1. $80 \%$ of the time OC produces better results for the Pyramid geometry for the less reverberant case by a factor of at least 1.44 while $100 \%$ times for the more-reverberant case by a factor of at least 1.15 than the CC. But this accuracy comes at the cost of at least 300 times more runtime taken by OC than CC both for the less- and more-reverberant environments.
2. $80 \%$ of the time OC produces better results for the Circular geometry for the less reverberant case by a factor of at least 1.3 while $100 \%$ times for the more-reverberant case by a factor of at least 1.52 than the CC. But this accuracy comes at the cost of at least 200 times more runtime taken by OC than CC both for the less- and more-reverberant environments.
3. At least $70 \%$ of the time OC produces better results for the Rhombus geometry for the less reverberant case by a factor of at least 1.78 while at least
$80 \%$ of the time for the more-reverberant case by a factor of at least 1.014 than the CC. But this accuracy comes at the cost of at least 600 times more runtime taken by OC than CC for the less-reverberant case and at least 90 times more runtime by OC than CC for the more-reverberant case.
4. The Rhombus geometry produces the least accurate results with a minimum $\epsilon_{O C \_3 D}$ of value 1.25 m among the three geometries while the Pyramid geometry produces the most accurate results with a minimum $\epsilon_{O C \_3 D}$ of value 0.21 m . The Circular is in-between Rhombus and Pyramid, accuracy-wise, with a minimum $\epsilon_{O C \_3 D}$ of value 0.51 m .
5. The 8 kHz case is taking at least 2 times more runtime for OC than 4 kHz case for all the geometries.
6. The OC algorithm is taking at least 90 times more runtime than CC for all the cases of indoor experimentation using RevoLabs.
7. $100 \%$ of the time the OC produces more accurate results than CC in the more-reverberant environment for all the indoor experimental scenarios using RevoLabs while at least $70 \%$ of the time in the less-reverberant environment for all indoor experimental scenarios. This shows that as the reverberation increases the performance of both OC and CC decreases because of the signal shape distortion due to increased reverberations. However, CC is more disturbed by the reverberation than OC.

### 6.3 Results using VocoPro Wireless Microphone

## System

This section discusses the indoor experiments and their results and analysis for the Pyramid, Circular and Rhombus geometries using VocoPro Wireless Microphone System. It is to be noted that the sensitivity of VocoPro microphones were very week because of its specific design for vocals [40] and we could not capture the unloaded toy gunshot thus we used a loaded toy gunshot for these experiments. However the loaded gunshot signal has different shape and characteristics which affect the results significantly as we will see in the coming pages.

Fig. 6.15 shows a sample loaded shot captured at 16 kHz using VocoPro system in the indoor environment. It is to be noted that the maximum balanced output level of the VocoPro system is 400 mV [40] which gets attenuated upon traveling from the base station of VocoPro to the PC through several connectors as was shown in section 5.3.2 thus we had to magnify the signal by a multiplicative factor of 100 in MATLAB. First we will present the results in both tabular and plotted forms and then we will discuss the observations for all the scenarios in subsection 6.3.4 for the VocoPro system.


Figure 6.15: A sample unloaded gunshot acquired using VocoPro system at 16 kHz , amplified 100 times in MATLAB

### 6.3.1 Pyramid Geometry Experiments and Results

We discuss the results for the Pyramid geometry experiments in indoor environment using VocoPro system in this section. We conducted the experiments at 8 kHz and 4 kHz sampling rate. Fig. 6.16 shows the experimental setup for Pyramid geometry using VocoPro system indoors. Fig. 6.16a shows the experimental setup for the case of array placed in the center of the hall while Fig. 6.16b shows the experimental setup for the case of array placed in a corner of the hall. The VocoPro microphones are directional and thus can capture the sound waves coming perpendicularly (or at angles around $90^{\circ}$ ). We kept the mics standing upward rather than directing it to a specific locations for all the source locations and experiments for the sake of consistency.


Figure 6.16: Indoor Pyramid Geometry Experimental Setup Using VocoPro System, (a) Indoor Pyramid Geometry in the Center of the Hall using VocoPro System, (b) Indoor Pyramid Geometry in a Corner of the Hall using VocoPro System

For each sampling rate there are two different scenarios i) experimentation in the center of the hall and ii). experimentation in the corner of the hall. We divide the discussion further into two subsections w.r.t. to the sampling rate as follows.

## Results for 8 kHz Sampling Rate

Table 6.22 shows the results for 8 kHz when the array was placed in the center of the hall while Table 6.23 shows the results for 8 kHz but this time the array was placed in a corner of the hall.

Table 6.22: Pyramid indoor results using VocoPro System at 8 kHz for the case when the array was placed in the center of the hall. Fast Machine was used.

| Source Location | ( $0.5,0.866,0.5)$ | $(\mathbf{0}, \mathbf{0}, \mathbf{1})$ | $\begin{gathered} \left(2.5 \cos 60^{\circ}, 2.5 \sin 60^{\circ}, 0\right)= \\ (1.25,2.16,0) \end{gathered}$ | $\begin{gathered} \left(2 \cos 60^{\circ}, 2 \sin 60^{\circ}, 0\right)= \\ (1,1.73,0) \end{gathered}$ | (2.5, 0, 0) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Description | In-between $a_{1}$ and $a_{2}$ inside the array at height of 0.5 m at $60^{\circ}$ | Above the center of the array | In-between $a_{1} \& a_{2}$, outside the array | In-between $a_{1} \& a_{2}$ on the circle inscribing the array. | Along the line (outside array) passing through $a_{1}$ and center of the array |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | $\begin{aligned} & (0.0020,0.0020, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{aligned} & (0.0036,0.0036, \\ & 0.0036,-0.0021) \end{aligned}$ | $\begin{gathered} (-0.0006,-0.0006, \\ 0.0059,0.0003) \end{gathered}$ | $\begin{gathered} (0,0.0000,0.0059, \\ 0.0004) \end{gathered}$ | $\begin{gathered} (-0.0059,0.0041, \\ 0.0041,0.0003) \end{gathered}$ |
| $\begin{aligned} & \text { TDE } E_{c c} \\ & \left(\tau_{10}^{c c}, \tau_{20}^{c c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{array}{lr} (0.0005, & 0.0066, \\ 0.0035, & -0.0011) \end{array}$ | $\begin{array}{cc} (0.0088, & -0.0070, \\ 0.0019, & -0.0008) \end{array}$ | $\begin{array}{cc} (-0.0013, & 0.0096, \\ 0.0041, & -0.0019) \end{array}$ | $\begin{array}{cc} (0.0004 & 0.0061, \\ 0.0013, & 0) \end{array}$ | $\begin{array}{ll} (-0.0054, & 0.0087, \\ 0.0034, & 0.0024) \end{array}$ |
| $\begin{aligned} & \text { TDE } E_{o c} \\ & \left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c}, \tau_{40}^{o c}\right) \end{aligned}$ | (0.0043, 0.0064, <br> $0.0010, \quad 0.0018)$ | $\begin{array}{lr} (0.0029, & 0.0021, \\ 0.0032, & -0.0020) \end{array}$ | $\begin{array}{ll} (-0.0063, & -0.0085, \\ -0.0059, & -0.0020) \end{array}$ | $\begin{array}{cc} (0.0015, & -0.0048, \\ -0.0014, & 0.0044) \end{array}$ | $\begin{array}{cc} (-0.0030, & -0.0061, \\ 0.0037, & 0.0069) \end{array}$ |
| $\begin{aligned} & \hline X_{c c} \\ & \left(x_{s}^{c c}, y_{s}^{c c}, \boldsymbol{Z}_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (0.9277,-0.7554, \\ 0.6606) \end{gathered}$ | $\begin{gathered} (0.5659,-1.8107, \\ -0.1469) \end{gathered}$ | $\begin{gathered} (0.9304,-1.2065, \\ -0.0141) \end{gathered}$ | $\begin{gathered} (0.8994,-1.2575 \\ 0.3600) \end{gathered}$ | $\begin{gathered} (-0.1363,-0.9037, \\ 0.2600) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, \boldsymbol{z}_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (0.0051,-1.0006, \\ -0.4356) \end{gathered}$ | $\begin{gathered} (-0.0683,0.2780 \\ 1.6199) \end{gathered}$ | $\begin{gathered} (0.2307,-0.5347, \\ 0.3720) \end{gathered}$ | $\begin{gathered} (1.6411,-1.2758, \\ 4.5593) \end{gathered}$ | $\begin{gathered} (0.0350,-1.7220, \\ 1.0418) \end{gathered}$ |
| $\epsilon_{c c, 3 D}$ | 1.6845 | 2.2168 | 3.3817 | 3.0108 | 2.8801 |
| $\epsilon_{c c, 2 D}$ | 1.6769 | 1.8970 | 3.3817 | 2.9892 | 2.8684 |
| $\epsilon_{o c .3 D}$ | 2.1458 | 0.6828 | 2.9050 | 5.4985 | 3.7326 |
| $\epsilon_{o C-2 D}$ | 1.9311 | 0.2863 | 2.8810 | 3.0734 | 3.5843 |
| Time for CC (Sec) | 0.0555 | 0.0337 | 0.1205 | 0.0342 | 0.0347 |
| Time for OC(Sec) | 46.5581 | 49.8827 | 48.7259 | 39.8475 | 40.3569 |

Next we plot the $x, y$ coordinates of the actual and estimated source locations for the less-reverberant case in Fig. 6.17a and Fig. 6.17b plots the $x, y$ coordinates for the more-reverberant case. Fig. 6.17c and Fig. 6.17d plots the bargraphs for the height of source locations for the case of less- and more-reverberant scenarios respectively.


Figure 6.17: Pyramid Geometry Source Locations Estimated by CC and OC at 8 kHz Indoor using VocoPro system, (a) Source Locations estimated in the less-reverberant case, only the $x, y$ coordinates are shown, (b) Source Locations estimated in the more-reverberant case,, only the $x, y$ coordinates are shown, (c) Height Estimate for the less-reverberant case, (d)Height Estimate for the morereverberant case.

Table 6.23: Pyramid indoor results using VocoPro System at 8 kHz for the case when the array was placed in a corner of the hall. Fast Machine was used.

| Source Location | ( $0.5,0.866,0.5)$ | $(\mathbf{0}, \mathbf{0}, \mathbf{1})$ | (1.25, 2.16, 0) | $\begin{gathered} \left(2 \cos 60^{\circ}, 2 \sin 60^{\circ}, 0\right)= \\ (1,1.73,0) \end{gathered}$ | (-2.5, 0, 0) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Description | In-between $a_{1}$ and $a_{2}$ inside the array at height of 0.5 m at $60^{\circ}$ | Above the center of the array | On the line through $a_{2}$ and origin outside the array | In-between $a_{1} \& a_{2}$ on the circle inscribing the array. | Along the line (outside array) passing in-between $a_{2}, a_{3}$ and center of the array |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | $\begin{aligned} & (0.0020,0.0020, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{aligned} & (0.0036,0.0036, \\ & 0.0036,-0.0021) \end{aligned}$ | $\begin{gathered} (0.0046,-0.0056, \\ 0.0024,0.0001) \end{gathered}$ | $\begin{gathered} (0,0.0016,0.0058, \\ 0.0005) \end{gathered}$ | $\begin{gathered} (-0.0059,0.0041, \\ 0.0041,0.0003) \end{gathered}$ |
| $\begin{aligned} & \hline T D E_{c c} \\ & \left(\tau_{10}^{c c}, \tau_{20}^{c c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{array}{cc} (0.0011, & -0.0093, \\ 0.0032, & -0.0014) \end{array}$ | $\begin{array}{lr} (0.0011, & 0.0051, \\ 0.0034, & -0.0014) \end{array}$ | $(-0.0003$, -0.0316, <br> -0.0003, $0.0014)$ | $\begin{array}{cc} (0.0006, & -0.0079, \\ 0.0059, & -0.0021) \end{array}$ | $(0.0066$, -0.0014, <br> 0.0051, $0.0039)$ |
| $\begin{aligned} & \text { TDE } E_{o C} \\ & \left(\tau_{10}^{o c},,_{20}^{o c}, \tau_{30}^{o c}, \tau_{40}^{o c}\right) \end{aligned}$ | $\begin{array}{cc} (0.0026, & -0.0025, \\ 0.0050, & 0.0019) \end{array}$ | $\begin{array}{lr} (0.0025, & 0.0043, \\ 0.0005, & -0.0049) \end{array}$ | $\begin{array}{cc} (-0.0035, & -0.0055, \\ 0.0054, & 0.0025) \end{array}$ | $\begin{array}{cc} (-0.0027, & -0.0033, \\ 0.0021, & -0.0030) \end{array}$ | $\begin{array}{cc} (0.0059, & -0.0010, \\ 0.0020, & -0.0010) \end{array}$ |
| $\begin{aligned} & X_{c c} \\ & \left(\boldsymbol{x}_{s}^{c c}, y_{s}^{c c}, \boldsymbol{z}_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (1.0023,-1.5170, \\ 0.0708) \end{gathered}$ | $\begin{gathered} (0.7497,-0.4332, \\ 0.9639) \end{gathered}$ | $\begin{gathered} (1.1998, \\ -2.8720) \\ -2.0781, \end{gathered}$ | $\begin{gathered} (1.0667,-1.4845, \\ -0.7438) \end{gathered}$ | $\begin{gathered} (-0.8566, \quad 0.7411, \\ -1.8421) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (-0.1648,1.9273, \\ -1.8976) \end{gathered}$ | $\begin{gathered} (0.0393,-0.9889 \\ 2.6795) \end{gathered}$ | $\begin{gathered} (-0.2585,-1.6453 \\ 1.6529) \end{gathered}$ | $\begin{gathered} (-0.8356,-1.9845 \\ -5.3778) \end{gathered}$ | $\begin{gathered} (-1.5875,0.5143, \\ 1.0243) \end{gathered}$ |
| $\epsilon_{c c, 3 D}$ | 2.4729 | 1.4020 | 5.1198 | 3.3001 | 2.5775 |
| $\epsilon_{c c, 2 D}$ | 2.4353 | 1.3230 | 4.2384 | 3.2152 | 1.8028 |
| $\epsilon_{o c, 3 D}$ | 2.7050 | 2.8989 | 4.4145 | 6.7888 | 1.4651 |
| $\epsilon_{O C .2 D}$ | 1.2523 | 1.9113 | 4.0934 | 4.1433 | 1.0475 |
| Time for CC (Sec) | 0.0345 | 1.3950 | 0.0411 | 0.0605 | 0.0336 |
| Time for $\mathrm{OC}(\mathbf{S e c})$ | 52.7992 | 38.9396 | 31.9275 | 50.4358 | 47.8197 |

## Results for 4 kHz Sampling Rate

Table 6.24 shows the results for 4 kHz when the array was placed in the center of the hall while Table 6.25 shows the results for 4 kHz but this time the array was placed in a corner of the hall.

Next we plot the $x, y$ coordinates of the actual and estimated source locations for the less-reverberant case in Fig. 6.18a and Fig. 6.18b plots the $x, y$ coordinates for the more-reverberant case. Fig. 6.18c and Fig. 6.18d plots the bargraphs for the height of source locations for the case of less- and more-reverberant scenarios respectively.

Table 6.24: Pyramid indoor results using VocoPro System at 4 kHz for the case when the array was placed in the center of the hall. Slow Machine was used.

| Source Location | (0.5, 0.866, 0.5) | $(\mathbf{0}, \mathbf{0}, \mathbf{1})$ | $\begin{gathered} \left(2.5 \cos 60^{\circ}, 2.5 \sin 60^{\circ}, 0\right)= \\ (1.25,2.16,0) \end{gathered}$ | $\begin{gathered} \left(2 \cos 60^{\circ}, 2 \sin 60^{\circ}, 0\right)= \\ (1,1.73,0) \end{gathered}$ | (2.5, 0, 0) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Description | In-between $a_{1}$ and $a_{2}$ inside the array at height of 0.5 m at $60^{\circ}$ | Above the center of the array | In-between $a_{1} \& a_{2}$, outside the array | In-between $a_{1} \& a_{2}$ on the circle inscribing the array. | Along the line (outside array) passing through $a_{1}$ and center of the array |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | $\begin{aligned} & (0.0020,0.0020, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{aligned} & (0.0036,0.0036, \\ & 0.0036,-0.0021) \end{aligned}$ | $\begin{gathered} (-0.0006,-0.0006, \\ 0.0059,0.0003) \end{gathered}$ | $\begin{gathered} (0,0.0000,0.0059 \\ 0.0004) \end{gathered}$ | $\begin{gathered} (-0.0059,0.0041, \\ 0.0041,0.0003) \end{gathered}$ |
| $\begin{aligned} & \text { TDE } E_{c c} \\ & \left(\tau_{10}^{c c}, \tau_{20}^{c c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{array}{lr} (0.0005, & 0.0122, \\ 0.0070, & -0.0022) \end{array}$ | $\begin{array}{ll} (0.0027, & -0.0028, \\ -0.0057, & -0.0027) \end{array}$ | $\begin{array}{cc} (-0.0060, & 0.0003, \\ 0.0018, & 0) \end{array}$ | $(0.0055$, 0.0020, <br> 0.0037, $0.0037)$ | $\begin{array}{cc} (-0.0043, & 0.0217, \\ 0.0018, & -0.0037) \end{array}$ |
| $\begin{aligned} & \text { TDE }{ }_{o c} \\ & \left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c}, \tau_{40}^{o c}\right) \end{aligned}$ | $\begin{array}{cc} (0.0067, & 0.0075, \\ 0.0030, & 0.0067) \end{array}$ | $\begin{array}{cc} (-0.0008, & 0.0012, \\ 0.0047, & 0.0027) \end{array}$ | $\begin{array}{cc} (-0.0043, & -0.0057, \\ 0.0013, & -0.0003) \end{array}$ | $\begin{array}{cc} (0.0065, & 0.0050, \\ 0.0018, & -0.0057) \end{array}$ | $(0.0030$ 0.0205, <br> -0.0015, $0.0043)$ |
| $\begin{aligned} & \boldsymbol{X}_{c c} \\ & \left(x_{s}^{c c}, \boldsymbol{y}_{s}^{c c}, \boldsymbol{Z}_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (1.0619, \\ -0.8738) \\ -0.2506, \end{gathered}$ | $\begin{gathered} (1.5452, \quad 0.8800, \\ -2.3249) \end{gathered}$ | $\begin{gathered} (-2.9071, \quad-0.3612, \\ 0.3600) \end{gathered}$ | $\begin{gathered} (-0.6671,0.3032, \\ -2.2206) \end{gathered}$ | $\begin{gathered} (-2.0128,-1.0747, \\ -6.8739) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (-0.2260,-0.7607, \\ -3.0456) \end{gathered}$ | $\begin{gathered} (1.3425,1.2565, \\ -3.6098) \end{gathered}$ | $\begin{gathered} (-0.2648,-1.2004 \\ 0.2112) \end{gathered}$ | $\begin{gathered} (-0.6916,-0.4968, \\ -1.1020) \end{gathered}$ | $\begin{gathered} (2.0313,-1.5068, \\ 3.9919) \end{gathered}$ |
| $\epsilon_{c c, 3 D}$ | 2.5852 | 3.7706 | 4.8752 | 3.1219 | 8.2928 |
| $\epsilon_{c c, 2 D}$ | 2.1899 | 1.7782 | 4.8619 | 2.1943 | 4.6390 |
| $\epsilon_{o c, 3 D}$ | 3.9680 | 4.9630 | 3.6921 | 3.0058 | 4.2925 |
| $\epsilon_{o c .2 D}$ | 1.7814 | 1.8388 | 3.6861 | 2.7965 | 1.5780 |
| Time for CC (Sec) | 0.0773 | 0.0445 | 0.0442 | 0.0440 | 0.0436 |
| Time for OC (Sec) | 15.5273 | 21.3783 | 20.4861 | 15.9091 | 16.9983 |

Table 6.25: Pyramid indoor results using VocoPro System at 4 kHz for the case when the array was placed in a corner of the hall. Slow Machine was used.

| Source Location | (0.5, 0.866, 0.5) | $(0,0,1)$ | (1.25, 2.16, 0) | $\begin{gathered} \left(2 \cos 60^{\circ}, 2 \sin 60^{\circ}, 0\right)= \\ (1,1.73,0) \end{gathered}$ | (-2.5, 0, 0) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Description | In-between $a_{1}$ and $a_{2}$ inside the array at height of 0.5 m at $60^{\circ}$ | Above the center of the array | On the line through $a_{2}$ and origin outside the array | In-between $a_{1} \& a_{2}$ on the circle inscribing the array. | Along the line (outside array) passing in-between $a_{2}, a_{3}$ and center of the array |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | $\begin{aligned} & (0.0020,0.0020, \\ & 0.0057,-0.0003) \end{aligned}$ | $\begin{aligned} & (0.0036,0.0036, \\ & 0.0036,-0.0021) \end{aligned}$ | $\begin{gathered} (0.0046,-0.0056, \\ 0.0024,0.0001) \end{gathered}$ | $\begin{gathered} (0,0.0000,0.0059 \\ 0.0004) \end{gathered}$ | $\begin{gathered} (-0.0059,0.0041, \\ 0.0041,0.0003) \end{gathered}$ |
| $\begin{aligned} & T D E_{c c} \\ & \left(\tau_{10}^{\tau c}, \tau_{20}^{c c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{array}{cc} (-0.0047, & 0.0020, \\ 0.0123, & -0.0015) \end{array}$ | $\begin{array}{lr} (0.0022, & 0.0075, \\ 0.0040, & -0.0008) \end{array}$ | $\begin{array}{lr} (0.0018, & 0.0085, \\ 0.0065, & -0.0053) \end{array}$ | $\begin{array}{cc} (0.0003, & -0.0040, \\ 0.0053, & 0.0035) \end{array}$ | $\begin{array}{cc} (-0.0018, & 0.0095, \\ 0.0040, & 0.0028) \end{array}$ |
| $\begin{aligned} & T D E_{o C} \\ & \left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c},,_{40}^{o c}\right) \end{aligned}$ | $\begin{array}{cc} \hline(0.0022, & -0.0097, \\ 0.0017, & 0.0008) \end{array}$ | $\begin{array}{cc} (0.0035, & 0.0063, \\ 0.0013, & 0.0070) \end{array}$ | $\begin{array}{ll} (0.0003, & -0.0083, \\ -0.0008, & -0.0027) \end{array}$ | $\begin{array}{cc} (-0.0013, & 0.0023, \\ 0.0022, & 0.0047) \end{array}$ | $\begin{array}{cc} (0.0050, & 0.0063, \\ 0.0063, & 0) \end{array}$ |
| $\begin{aligned} & X_{c c} \\ & \left(x_{s}^{c c}, y_{s}^{c c}, \boldsymbol{Z}_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (-0.6794,1.1405, \\ -0.7435) \end{gathered}$ | $\begin{gathered} (0.7361,-0.7855 \\ 0.4339) \end{gathered}$ | $\begin{gathered} (0.9495,-0.4729, \\ -2.2479) \end{gathered}$ | $\begin{gathered} (0.6743,5.9845, \\ -11.0942) \end{gathered}$ | $\begin{gathered} (0.8811,-1.1943, \\ -0.1602) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (0.8819,-1.5868 \\ 0.3306) \end{gathered}$ | $\begin{gathered} (0.1887,-1.0112, \\ -6.1138) \end{gathered}$ | $\begin{gathered} (1.0311,-1.6249, \\ -1.0673) \end{gathered}$ | $\begin{gathered} (2.0311,-0.0555, \\ -12.2592) \end{gathered}$ | (0.2822, 0, 0.3600) |
| $\epsilon_{c c, 3 D}$ | 1.7357 | 1.2163 | 3.4750 | 11.8865 | 3.5894 |
| $\epsilon_{\text {cc_ } 2 \mathrm{D}}$ | 1.2109 | 1.0765 | 2.6500 | 4.2670 | 3.5858 |
| $\epsilon_{o c .3 D}$ | 2.4882 | 7.1878 | 3.9386 | 12.4314 | 2.8054 |
| $\epsilon_{O C .2 D}$ | 2.4824 | 1.0286 | 3.7913 | 2.0618 | 2.7822 |
| Time for CC (Sec) | 0.0444 | 0.0433 | 0.0437 | 0.0438 | 0.0435 |
| Time for OC (Sec) | 15.9668 | 20.9052 | 17.2456 | 19.4981 | 16.0384 |

### 6.3.2 Circular Geometry Experiments and Results

Now we will present the experiments we conducted and their results for the Circular geometry using VocoPro system. We conducted the experiments at 8 kHz


Figure 6.18: Pyramid Geometry Source Locations Estimated by CC and OC at 4 kHz Indoor using VocoPro system, (a) Source Locations estimated in the less-reverberant case, only the $x, y$ coordinates are shown, (b) Source Locations estimated in the more-reverberant case,, only the $x, y$ coordinates are shown, (c) Height Estimate for the less-reverberant case, (d) Height Estimate for the more-reverberant case.
and 4 kHz sampling rate. Fig. 6.19 shows the experimental setup for Pyramid geometry using VocoPro system indoor. Fig. 6.19a shows the experimental setup for the case of array placed in the center of the hall while Fig. 6.19b shows the experimental setup for the case of array placed in a corner of the hall.


Figure 6.19: Indoor Circular Geometry Experimental Setup Using VocoPro System, (a) Indoor Circular Geometry in the Center of the Hall using VocoPro System, (b) Indoor Circular Geometry in a Corner of the Hall using VocoPro System.

For each sampling rate there are two different scenarios i) experimentation in the center of the hall and ii). experimentation in a corner of the hall. We divide the discussion further into two subsections w.r.t. to the sampling rate as follows.

## Results for 8 kHz Sampling Rate

Table 6.26 shows the results for 8 kHz when the array was placed in the center of the hall while Table 6.27 shows the results for 8 kHz when the array was placed in a corner of the hall.

Table 6.26: Circular indoor results using VocoPro System at 8 kHz for the case when the array was placed in the center of the hall. Fast Machine was used.

| Source Location | $\left(r \cos 30^{\circ}-r, r \sin 30^{\circ}\right.$ <br> ,0) | $\begin{gathered} \left(r \cos 30^{\circ}-r,\right. \\ \left.r \sin 30^{\circ}, 1\right) \end{gathered}$ | (-2r, 0,0 ) | ( $-2 r, 0,0.5$ ) | (-3r, 0, 0) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Value | (-0.2 0.7500, 0) | (-0.2, 0.7500, 1) | $(-3,0,0)$ | (-3, 0, 0.5) | (-4.5, 0, 0) |
| Description | In-between mic0 and 1 on the circumference at height of 0 m | In-between mic0 and 1 on the circumference at height of 1 m | At mic3 with zero height | At mic3 with 0.5 m height | Along the line (outside array) passing through mic3 and center of the array at height 0 m |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | (0.0004, 0.0040, $0.0064, \quad 0.0062$, 0.0041 ) | $\begin{array}{cc} \hline(-0.0010, & 0.0032, \\ 0.0049, & 0.0053, \\ 0.0027) \\ \hline \end{array}$ | (-0.0010, -0.0044, $-0.0074,-0.0044$, -0.0010) | (-0.0013, -0.0043, $-0.0089,-0.0043$, -0.0013 ) | (-0.0015, -0.0056, $-0.0086,-0.0056$, -0.0015) |
| $\begin{aligned} & T D E_{c c} \\ & \left(\tau_{10}^{c c}, \tau_{20}^{c c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{array}{cc} (0.0080, & -0.0005, \\ 0.0187, & 0.0213, \\ 0.0135) \end{array}$ | $\begin{array}{cc} \hline(0.0415, & 0.0001, \\ 0.0150, & -0.0065, \\ -0.0050) \end{array}$ | $\begin{array}{cc} \hline(-0.0076, & -0.0049, \\ 0.0030, & 0.0051, \\ 0.0001) \end{array}$ | $\begin{array}{cc} (0.0085, & -0.0043, \\ -0.0074, & 0.0001, \\ -0.0155) \end{array}$ | $\begin{array}{cc} \hline(-0.0018, & -0.0206, \\ -0.0040, & -0.0182, \\ -0.0020) \end{array}$ |
| TDE ${ }_{\text {oc }}$ <br> $\left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c}, \tau_{40}^{o c}\right)$ | $\begin{array}{cc} \hline(0.0139, & 0.0039, \\ 0.0226, & 0.0279, \\ 0.0119) \end{array}$ | $\begin{array}{cc} \hline(0.0035, & -0.0069, \\ -0.0146, & -0.0141, \\ -0.0203) \end{array}$ | $\begin{array}{cc} \hline(-0.0086, & -0.0077, \\ -0.0095, & -0.0016, \\ -0.0100) \end{array}$ | $\begin{array}{cc} (0.0073, & 0.0081, \\ 0.0018, & 0.0070, \\ 0.0090) \end{array}$ | $\begin{array}{cc} \hline(-0.0009, & -0.0098, \\ -0.0037, & -0.0053, \\ 0.0035) \end{array}$ |
| $\begin{aligned} & \boldsymbol{X}_{c c} \\ & \left(x_{s}^{c c}, \boldsymbol{y}_{s}^{c c}, \boldsymbol{z}_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (-0.6085,0.3906, \\ 10.3074) \end{gathered}$ | $\begin{gathered} (-1.6646,7.4002, \\ 10.4321) \end{gathered}$ | $\begin{gathered} (-0.9197,0.3618, \\ 0.2642) \end{gathered}$ | $\begin{gathered} (-2.3683,0.3564, \\ -13.1643) \end{gathered}$ | $\begin{gathered} (-2.3994,-0.5120, \\ 3.0382) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (-2.3367,0.8083, \\ 19.2068) \end{gathered}$ | $\begin{gathered} (-3.0968,0.4411, \\ -9.1498) \end{gathered}$ | $\begin{gathered} (-1.7063, \quad 0.1253, \\ -0.7380) \end{gathered}$ | $\begin{gathered} (-1.7280,0.0656, \\ 0.4371) \end{gathered}$ | $\begin{gathered} (-4.3159,1.6332, \\ -8.2502) \end{gathered}$ |
| $\epsilon_{\text {cc } 3 \text { c }}$ | 10.3217 | 11.6334 | 2.1280 | 13.6835 | 3.7290 |
| $\epsilon_{c c-2 D}$ | 0.5441 | 6.8095 | 2.1115 | 0.7253 | 2.1621 |
| $\epsilon_{o c, 3 D}$ | 19.3253 | 10.5596 | 1.4947 | 1.2753 | 8.4124 |
| $\epsilon_{O C-2 D}$ | 2.1375 | 2.9133 | 1.2998 | 1.2737 | 1.6436 |
| Time for CC (Sec) | 0.1326 | 0.2568 | 0.1437 | 0.1364 | 0.1340 |
| Time for OC (Sec) | 34.5292 | 37.2538 | 35.9664 | 38.5995 | 39.6390 |

Next we plot the $x, y$ coordinates of the actual and estimated source locations for the less-reverberant case in Fig. 6.20a and Fig. 6.20b plots the $x, y$ coordinates for the more-reverberant case. Fig. 6.20c and Fig. 6.20d plots the bargraphs for the height of source locations for the case of less- and more-reverberant scenarios respectively.


Figure 6.20: Circular Geometry Source Locations Estimated by CC and OC at 8 kHz Indoor using VocoPro system, (a) Source Locations estimated in the less-reverberant case, only the $x, y$ coordinates are shown, (b) Source Locations estimated in the more-reverberant case,, only the $x, y$ coordinates are shown, (c) Height Estimate for the less-reverberant case, (d) Height Estimate for the more-reverberant case

Table 6.27: Circular indoor results using VocoPro System at 8 kHz for the case when the array was placed in a corner of the hall. Fast Machine was used.

| Source Location | $\begin{gathered} \left(r \cos 30^{\circ}-r, r \sin 30^{\circ}\right. \\ , 0) \end{gathered}$ | $\begin{gathered} \left(r \cos 30^{\circ}-r,\right. \\ \left.r \sin 30^{\circ}, 1\right) \end{gathered}$ | (-2r, 0,0$)$ | (-2r, 0, 0.5) | (-3r, 0, 0) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Value | (-0.2 0.7500, 0) | (-0.2, 0.7500, 1) | $(-3,0,0)$ | (-3, 0, 0.5) | $(-4.5,0,0)$ |
| Description | In-between mic0 and 1 on the circumference at height of 0 m | In-between mic0 and 1 on the circumference at height of 1 m | At mic3 with zero height | At mic3 with 0.5 m height | Along the line (outside array) passing through mic3 and center of the array at height 0 m |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | $\begin{array}{cc} \hline(0.0004, & 0.0040, \\ 0.0064, & 0.0062, \\ 0.0041) \\ \hline \end{array}$ | $\begin{array}{cc} \hline(-0.0010, & 0.0032, \\ 0.0049, & 0.0053, \\ 0.0027) \\ \hline \end{array}$ | $\begin{array}{cc} (-0.0010, & -0.0044, \\ -0.0074,-0.0044, \\ -0.0010) \\ \hline \end{array}$ | $\begin{array}{cc} \hline(-0.0013, & -0.0043, \\ -0.0089, & -0.0043, \\ -0.0013) \\ \hline \end{array}$ | $(-0.0015,-0.0056$, $-0.0086,-0.0056$ -0.0015 ) |
| $\begin{aligned} & T D E_{c c} \\ & \left(\tau_{10}^{c c}, \tau_{20}^{c c}, \tau_{30}^{c c},,_{40}^{c c t}\right) \end{aligned}$ | $\begin{array}{cc} \hline(0.0043, & 0.0009, \\ 0.0067, & 0.0056, \\ -0.0025) \end{array}$ | $\begin{array}{cc} \hline(0.0005, & 0.0025, \\ 0.0031, & 0.0077, \\ 0.0005) \end{array}$ | $\begin{array}{cc} \hline(-0.0014, & -0.0054, \\ -0.0008, & 0.0010, \\ -0.0037) \end{array}$ | $\begin{array}{cc} \hline(0.0005, & -0.0150, \\ -0.0036, & 0.0019, \\ -0.0094) \end{array}$ | $\begin{gathered} \hline-0.0016, \quad-0.0115, \\ -0.0092,-0.0054, \\ -0.0034) \end{gathered}$ |
| $\begin{aligned} & T D E_{o c} \\ & \left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c},,_{40}^{o c}\right) \end{aligned}$ | $\begin{array}{cc} (-0.0174, & -0.0248, \\ -0.0181, & -0.0133, \\ -0.0081) \end{array}$ | $\begin{array}{cc} \hline(-0.0036, & 0.0003, \\ -0.0030, & -0.0030, \\ -0.0009) \end{array}$ | $\begin{array}{cc} \hline(0.0022, & -0.0011, \\ 0.0027, & -0.0031, \\ 0.0043) \end{array}$ | $\begin{array}{cc} \hline(-0.0049, & -0.0027, \\ -0.0018, & 0.0010, \\ -0.0005) \end{array}$ | $\begin{array}{cc} (-0.0064, & -0.0145, \\ -0.0120, & -0.0105, \\ -0.0050) \end{array}$ |
| $\begin{aligned} & X_{c c} \\ & \left(x_{s}, y_{s}^{c c}, z_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (-1.3727,0.3006, \\ -0.7569) \end{gathered}$ | $\begin{gathered} (-1.9563,0.0145, \\ 0.0753) \end{gathered}$ | $\begin{gathered} (-1.4084,0.0421, \\ 0.9923) \end{gathered}$ | $\begin{gathered} (-1.0281,-0.5055, \\ 3.8458) \end{gathered}$ | $\begin{gathered} \hline(-2.1488, \\ -0.4130,1.6808) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (-0.6978,-3.0374, \\ 8.2110) \end{gathered}$ | $\begin{gathered} (-1.5110,-0.0580, \\ 0.3634) \end{gathered}$ | $\begin{gathered} (-1.4462,0.2392, \\ -0.9877) \end{gathered}$ | $\begin{gathered} (-1.5661,0.4255, \\ 1.3173) \end{gathered}$ | $\begin{gathered} (-0.4923, \quad-0.6927, \\ 4.1383) \end{gathered}$ |
| $\epsilon_{\text {cc. } 3 D}$ | 1.4663 | 2.1168 | 1.8760 | 3.9164 | 2.9195 |
| $\epsilon_{c c, 2 D}$ | 1.2558 | 1.9041 | 1.5921 | 2.0356 | 2.3872 |
| $\epsilon_{\text {oc }{ }_{\text {c } 3 D} \text { d }}$ | 9.0561 | 1.6665 | 1.8566 | 1.7044 | 5.8023 |
| $\epsilon_{o c, 2 D}$ | 3.8200 | 1.5401 | 1.5721 | 1.4957 | 4.0672 |
| Time for $\mathbf{C C}(\mathbf{S e c})$ | 0.1373 | 0.1368 | 0.1373 | 0.3102 | 0.6309 |
| Time for OC (Sec) | 41.3691 | 39.6792 | 47.3056 | 48.1760 | 44.0392 |

## Results for 4 kHz Sampling Rate

Table 6.28 shows the results for 4 kHz when the array was placed in the center of the hall while Table 6.29 shows the results for 4 kHz when the array was placed in a corner of the hall. Next we plot the $x, y$ coordinates of the actual and estimated source locations for the less-reverberant case in Fig. 6.21a and Fig. 6.21b plots the $x, y$ coordinates for the more-reverberant case. Fig. 6.21c and Fig. 6.21d plots the bargraphs for the height of source locations for the case of less- and morereverberant scenarios respectively.

Table 6.28: Circular indoor results using VocoPro System at 4 kHz for the case when the array was placed in the center of the hall. Slow Machine was used.

| Source Location | $\begin{gathered} \left(r \cos 30^{\circ}-r, r \sin 30^{\circ}\right. \\ , 0) \end{gathered}$ | $\begin{gathered} \left(r \cos 30^{\circ}-r\right) \\ \left.r \sin 30^{\circ}, 1\right) \end{gathered}$ | ( $-2 r, 0,0$ ) | ( $-2 r, 0,0.5$ ) | (-3r, 0, 0) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Value | (-0.2 0.7500, 0) | (-0.2, 0.7500, 1) | $(-3,0,0)$ | (-3, 0, 0.5) | (-4.5, 0, 0) |
| Description | In-between mic0 and 1 on the circumference at height of Om | In-between mic0 and 1 on the circumference at height of 1 m | At mic3 with zero height | At mic3 with 0.5 m height | Along the line (outside array) passing through mic3 and center of the array at height 0 m |
| $\begin{gathered} \text { Exact TDs } \\ \left(\boldsymbol{\tau}_{\mathbf{1 0}}, \boldsymbol{\tau}_{\mathbf{2 0}}, \boldsymbol{\tau}_{30}, \boldsymbol{\tau}_{40}\right) \end{gathered}$ | (0.0004, 0.0040 , $0.0064, \quad 0.0062$, 0.0041 ) | $\begin{array}{cc} \hline(-0.0010, & 0.0032, \\ 0.0049, & 0.0053, \\ 0.0027) \end{array}$ | $\begin{array}{cc} \hline(-0.0010, & -0.0044, \\ -0.0074, & -0.0044, \\ -0.0010) \end{array}$ | $\begin{array}{cc} \hline(-0.0013, & -0.0043, \\ -0.0089, & -0.0043, \\ -0.0013) \end{array}$ | $\begin{array}{cc} (-0.0015, & -0.0056, \\ -0.0086,-0.0056, \\ -0.0015) \end{array}$ |
| $\begin{aligned} & \text { TDE } \boldsymbol{L E}_{c c} \\ & \left(\boldsymbol{\tau}_{10}^{c c}, \boldsymbol{\tau}_{20}^{c c}, \boldsymbol{\tau}_{30}^{c c}, \boldsymbol{\tau}_{40}^{c c}\right) \end{aligned}$ | $\begin{array}{cc} (0.0138, & -0.0005, \\ 0.0275, & 0.0143, \\ 0.0135) \end{array}$ | $\begin{array}{cc} (0.0073, & -0.0018, \\ 0.0150, & 0.0092, \\ -0.0035) \end{array}$ | $\begin{array}{cc} (-0.0177, & 0.0090, \\ -0.0187, & 0.0088, \\ -0.0103) \end{array}$ | $\begin{array}{cc} (0.0027, & -0.0165, \\ -0.0013, & 0.0020, \\ -0.0155) \end{array}$ | $\begin{array}{cc} (-0.0018, & -0.0063, \\ -0.0040, & -0.0210, \\ -0.0190) \end{array}$ |
|  | $\begin{array}{cc} (-0.0065, & -0.0103 \\ 0, & -0.0027, \\ \hline \end{array}$ | $\begin{array}{cc} (0.0060, & -0.0053, \\ 0.0005, & -0.0035, \\ -0.0035) \end{array}$ | $\begin{array}{cc} (0.0053, & 0.0022, \\ 0.0005, & 0.0015, \\ -0.0005) \end{array}$ | $\begin{array}{cc} (-0.0013, & 0.0032, \\ -0.0018, & -0.0035, \\ -0.0008) \end{array}$ | $(0.0040$, -0.0 .0020, -0.0025, $-0.0010)$ |
| $\begin{aligned} & \boldsymbol{X}_{c c} \\ & \left(\boldsymbol{x}_{s}^{c c}, \boldsymbol{y}_{s}^{c c}, \boldsymbol{z}_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (-2.5373,-2.6683, \\ 17.1077) \end{gathered}$ | $\begin{gathered} (-0.7246, \quad 0.4459, \\ -2.5209) \end{gathered}$ | $\begin{gathered} (2.0021,-1.7679, \\ -5.1883) \end{gathered}$ | $\begin{gathered} (-1.2263,-0.3539, \\ -0.4450) \end{gathered}$ | $\begin{gathered} (-2.3751,1.3301, \\ 2.0626) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (-1.3268, \\ 1.7133) \end{gathered}$ | $\begin{gathered} (-1.3995,-0.5600, \\ -1.4857) \end{gathered}$ | $\begin{gathered} (-1.6317,0.0083 \\ -0.2654) \end{gathered}$ | $\begin{gathered} (-1.2684,-0.0024, \\ 0.7657) \end{gathered}$ | $\begin{gathered} (-1.3953,-0.1486, \\ -0.3003) \end{gathered}$ |
| $\epsilon_{\text {cc, } 3 \mathrm{D}}$ | 17.6017 | 3.5728 | 7.4206 | 2.0407 | 3.2463 |
| $\epsilon_{\text {cc } 2 \text { 2 }}$ | 4.1410 | 0.6064 | 5.3053 | 1.8087 | 2.5069 |
|  | 2.3983 | 3.0551 | 1.3939 | 1.7518 | 3.1227 |
| $\epsilon_{\text {OC.2D }}$ | 1.6781 | 1.7762 | 1.3684 | 1.7316 | 3.1082 |
| Time for CC (Sec) | 0.0469 | 0.0464 | 0.0544 | 0.0463 | 0.0464 |
| Time for OC (Sec) | 20.6177 | 20.5589 | 23.5458 | 19.9169 | 19.9744 |

Table 6.29: Circular indoor results using VocoPro System at 4 kHz for the case when the array was placed in a corner of the hall. Slow Machine was used.

| Source Location | $\begin{gathered} \left(r \cos 30^{\circ}-r, r \sin 30^{\circ}\right. \\ , 0) \end{gathered}$ | $\begin{gathered} \left(r \cos 30^{\circ}-r,\right. \\ \left.r \sin 30^{\circ}, 1\right) \end{gathered}$ | ( $-2 r, 0,0$ ) | (-2r, 0, 0.5) | (-3r, 0, 0) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Value | (-0.2 0.7500, 0) | (-0.2, 0.7500, 1) | $(-3,0,0)$ | (-3, 0, 0.5) | (-4.5, 0, 0) |
| Description | In-between mic0 and 1 on the circumference at height of 0 m | In-between mic0 and 1 on the circumference at height of 1 m | At mic3 with zero height | At mic3 with 0.5 m height | Along the line (outside array) passing through mic3 and center of the array at height 0 m |
| $\begin{gathered} \text { Exact TDs } \\ \left(\boldsymbol{\tau}_{10}, \boldsymbol{\tau}_{\mathbf{2 0}}, \boldsymbol{\tau}_{\mathbf{3},}, \boldsymbol{\tau}_{40}\right) \end{gathered}$ | $\begin{array}{cc} \hline 0.0004, & 0.0040, \\ 0.0064, & 0.0062, \\ 0.0041) \end{array}$ | $\begin{array}{cc} \hline(0.0010, & 0.0032, \\ 0.0049, & 0.0053, \\ 0.0027) \end{array}$ | $\begin{array}{cc} \hline(-0.0010, & -0.0044, \\ -0.0074, & -0.0044, \\ -0.0010) \\ \hline \end{array}$ | $\begin{array}{cc} \hline(-0.0013, & -0.0043, \\ -0.0089, & -0.0043, \\ -0.0013) \\ \hline \end{array}$ | $\begin{gathered} (-0.0015,-0.0056, \\ -0.0086,-0.0056, \\ -0.0015) \end{gathered}$ |
| $\begin{aligned} & \left(\boldsymbol{\tau}_{10}^{c c}, \boldsymbol{\tau}_{20}^{\tau c}, \tau_{30}^{c c}, \boldsymbol{\tau}_{40}^{c c}\right) \end{aligned}$ | $\begin{array}{cc} \hline(-0.0003, & 0.0010, \\ 0.0053, & 0.0133, \\ 0.0083) \end{array}$ | $\begin{array}{cc} (0.0010, & 0.0040, \\ 0.0037, & 0.0107, \\ 0.0088) \end{array}$ | $\begin{array}{cc} \hline(-0.0065, & -0.0123, \\ -0.0008, & 0.0022, \\ -0.0032) \end{array}$ | $\begin{array}{cc} \hline(-0.0032, & -0.0047, \\ -0.0083, & 0.0032, \\ -0.0113) \end{array}$ | $\begin{gathered} (-0.0085, \quad-0.0182, \\ -0.0150, \quad-0.0037, \\ -0.0098) \end{gathered}$ |
| $\begin{aligned} & T D E_{o c} \\ & \left(\boldsymbol{\tau}_{10}^{o \sigma}, \boldsymbol{\tau}_{20}^{o c}, \boldsymbol{\tau}_{30}^{o c}, \boldsymbol{\tau}_{40}^{o c}\right) \end{aligned}$ | $(0.0003$, -0.0025, <br> -0.0018, -0.0020, <br> $-0.0013)$  | $(0.0105$, 0.0067, 0.0050, 0.0080, $0.0065)$ | $\begin{array}{cc} \hline(-0.0003, & -0.0060, \\ -0.0005, & -0.0032, \\ -0.0015) \end{array}$ | $\begin{array}{cc} (-0.0103, & -0.0083, \\ -0.0075, & -0.0107, \\ -0.0060) \end{array}$ | $\begin{array}{cc} \hline(-0.0025, & -0.0065, \\ -0.0050, & -0.0047, \\ -0.0030) \end{array}$ |
| $\begin{aligned} & X_{c c} \\ & \left(x_{s}^{c c}, y_{s}^{c c}, \boldsymbol{z}_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (-2.4871,-1.5054, \\ 2.8999) \end{gathered}$ | $\begin{gathered} (-1.7952, \quad 0.2691, \\ 1.2486) \end{gathered}$ | $\begin{gathered} (-0.9251, \quad 0.1646, \\ 4.2830) \end{gathered}$ | $\begin{gathered} (-1.3503, \quad 1.1569, \\ -0.2270) \end{gathered}$ | $\begin{gathered} (-1.9940, \quad-0.4931, \\ 8.0051) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (-1.5003,-0.0329 \\ 0.3026) \end{gathered}$ | $\begin{gathered} (-2.0237,-0.2316, \\ 0.6986) \end{gathered}$ | $\begin{gathered} (-1.5202,-0.1695, \\ 0.5537) \end{gathered}$ | $\begin{gathered} (-1.9196,-0.0118, \\ 2.1073) \end{gathered}$ | $\begin{gathered} (-1.4343, \quad-0.1125, \\ 1.1040) \end{gathered}$ |
| $\epsilon_{\text {cc, } 3 \mathrm{D}}$ | 4.3275 | 1.6845 | 4.7620 | 2.1421 | 8.4026 |
| $\epsilon_{\text {cc. } 2 \mathrm{D}}$ | 3.2121 | 1.6661 | 2.0815 | 2.0149 | 2.5541 |
|  | 1.5476 | 2.0930 | 1.5891 | 1.9367 | 3.2604 |
| $\epsilon_{\text {OC.2D }}$ | 1.5178 | 2.0711 | 1.4895 | 1.0804 | 3.0677 |
| Time for CC (Sec) | 1.5178 | 0.0468 | 0.0470 | 0.0473 | 0.0462 |
| Time for OC (Sec) | 18.2064 | 21.4984 | 21.2012 | 16.9659 | 26.7784 |



Figure 6.21: Circular Geometry Source Locations Estimated by CC and OC at 4 kHz Indoor using VocoPro system, (a) Source Locations estimated in the less-reverberant case, only the $x, y$ coordinates are shown, (b) Source Locations estimated in the more-reverberant case,, only the $x, y$ coordinates are shown, (c) Height Estimate for the less-reverberant case, (d) Height Estimate for the more-reverberant case.

### 6.3.3 Rhombus Geometry Experiments and Results

In this section we will discuss the experiments we conducted and their results for the Rhombus geometry using VocoPro system. We conducted the experiments at 8 kHz and 4 kHz sampling rate. Fig. 6.22 shows the experimental setup for Rhombus geometry using VocoPro system indoor.

(a)

(b)

Figure 6.22: Indoor Rhombus Geometry Experimental Setup Using VocoPro System, (a) Indoor Rhombus Geometry in the Center of the Hall using VocoPro System, (b) Indoor Rhombus Geometry in a Corner of the Hall using VocoPro System.

Fig. 6.22a shows the experimental setup for the case of array placed in the center of the hall while Fig. 6.22b shows the experimental setup for the case of array placed in a corner of the hall.

For each sampling rate there are two different scenarios i) experimentation in the center of the hall and ii). experimentation in a corner of the hall. We divide the discussion further into two subsections w.r.t. to the sampling rate as follows.

## Results for 8 kHz Sampling Rate

Table 6.30 shows the results for 8 kHz when the array was placed in the center of the hall while Table 6.31 shows the results for 8 kHz when the array was placed in a corner of the hall.

Table 6.30: Rhombus indoor results using VocoPro System at 8 kHz for the case when the array was placed in the center of the hall. Fast Machine was used.

| Source Location | $\begin{gathered} \left(r \cos 30^{\circ}-r, r \sin 30^{\circ}\right. \\ , 0) \end{gathered}$ | $\begin{gathered} \left(r \cos 30^{\circ}-r\right. \\ \left.r \sin 30^{\circ}, 1\right) \end{gathered}$ | (-2r, 0,0$)$ | ( $-2 r, 0,0.5$ ) | (-3r, 0, 0) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Value | (-0.2 0.7500, 0) | (-0.2, 0.7500, 1) | $(-3,0,0)$ | (-3, 0, 0.5) | (-4.5, 0, 0) |
| Description | In-between mic0 and 1 on the circumference at height of 0 m | In-between mic0 and 1 on the circumference at height of 1 m | At mic3 with zero height | At mic3 with 0.5 m height | Along the line (outside array) passing through mic3 and center of the array at height 0 m |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | $\begin{array}{cc} \hline(0.0004, & 0.0040, \\ 0.0064, & 0.0062, \\ 0.0041) \end{array}$ | $\begin{array}{cc} \hline(-0.0010, & 0.0032, \\ 0.0049, & 0.0053, \\ 0.0027) \end{array}$ | $\begin{array}{cc} (-0.0010, & -0.0044, \\ -0.0074, & -0.0044, \\ -0.0010) \end{array}$ | $\begin{array}{cc} (-0.0013, & -0.0043, \\ -0.0089, & -0.0043, \\ -0.0013) \end{array}$ | $\begin{array}{cc} (-0.0015, & -0.0056, \\ -0.0086, & -0.0056, \\ -0.0015) \end{array}$ |
| $\begin{aligned} & T D E_{c c} \\ & \left(\tau_{10}^{\tau c}, \tau_{20}^{c c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{array}{cc} \hline(0.0080, & -0.0005, \\ 0.0187, & 0.0213, \\ 0.0135) \end{array}$ | $\begin{array}{cc} \hline(0.0415, & 0.0001, \\ 0.0150, & -0.0065, \\ -0.0050) \end{array}$ | $\begin{array}{cc} \hline(-0.0076, & -0.0049, \\ 0.0030, & 0.0051, \\ 0.0001) \end{array}$ | $\begin{array}{cc} \hline(0.0085, & -0.0043, \\ -0.0074, & 0.0001, \\ -0.0155) \end{array}$ | $\begin{array}{cc} (-0.0018, & -0.0206, \\ -0.0040, & -0.0182, \\ -0.0020) \end{array}$ |
| $\begin{aligned} & \operatorname{TDE}_{o c} \\ & \left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c},,_{40}^{o c}\right) \end{aligned}$ | $\begin{array}{cc} \hline(0.0139, & 0.0039, \\ 0.0226, & 0.0279, \\ 0.0119) \end{array}$ | $\begin{array}{cc} \hline(0.0035, & -0.0069, \\ -0.0146, & -0.0141, \\ -0.0203) \end{array}$ | $\begin{array}{cc} \hline(-0.0086, & -0.0077, \\ -0.0095, & -0.0016, \\ -0.0100) \end{array}$ | $\begin{array}{cc} \hline(0.0073, & 0.0081, \\ 0.0018, & 0.0070, \\ 0.0090) \end{array}$ | $\begin{array}{cc} (-0.0009, & -0.0098, \\ -0.0037, & -0.0053, \\ 0.0035) \end{array}$ |
| $\begin{aligned} & \boldsymbol{X}_{c c} \\ & \left(x_{s}^{c c}, y_{s}^{c c}, \boldsymbol{z}_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (-0.6085,0.3906, \\ 10.3074) \end{gathered}$ | $\begin{gathered} (-1.6646,7.4002, \\ 10.4321) \end{gathered}$ | $\begin{gathered} (-0.9197, \quad 0.3618, \\ 0.2642) \end{gathered}$ | $\begin{gathered} (-2.3683,0.3564, \\ -13.1643) \end{gathered}$ | $\begin{gathered} (-2.3994,-0.5120, \\ 3.0382) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (-2.3367,0.8083, \\ 19.2068) \end{gathered}$ | $\begin{gathered} (-3.0968,0.4411, \\ -9.1498) \end{gathered}$ | $\begin{gathered} (-1.7063,0.1253, \\ -0.7380) \end{gathered}$ | $\begin{gathered} (-1.7280,0.0656, \\ 0.4371) \end{gathered}$ | $\begin{gathered} (-4.3159,1.6332, \\ -8.2502) \end{gathered}$ |
| $\epsilon_{c c, 3 D}$ | 10.3217 | 11.6334 | 2.1280 | 13.6835 | 3.7290 |
| $\epsilon_{c c-2 D}$ | 0.5441 | 6.8095 | 2.1115 | 0.7253 | 2.1621 |
| $\epsilon_{o c .3 D}$ | 19.3253 | 10.5596 | 1.4947 | 1.2753 | 8.4124 |
| $\epsilon_{o c .2 D}$ | 2.1375 | 2.9133 | 1.2998 | 1.2737 | 1.6436 |
| Time for CC (Sec) | 0.1326 | 0.2568 | 0.1437 | 0.1364 | 0.1340 |
| Time for OC (Sec) | 34.5292 | 37.2538 | 35.9664 | 38.5995 | 39.6390 |

Table 6.31: Rhombus indoor results using VocoPro System at 8 kHz for the case when the array was placed in a corner of the hall. Fast Machine was used.

| Source Location | $\begin{gathered} \left(r \cos 30^{\circ}-r, r \sin 30^{\circ}\right. \\ , 0) \end{gathered}$ | $\begin{gathered} \left(r \cos 30^{\circ}-r,\right. \\ \left.r \sin 30^{\circ}, 1\right) \end{gathered}$ | (-2r, 0,0$)$ | ( $-2 r, 0,0.5$ ) | (-3r, 0, 0) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Value | (-0.2 0.7500, 0) | (-0.2, 0.7500, 1) | $(-3,0,0)$ | $(-3,0,0.5)$ | (-4.5, 0, 0) |
| Description | In-between mic0 and 1 on the circumference at height of 0 m | In-between mic0 and 1 on the circumference at height of 1 m | At mic3 with zero height | At mic3 with 0.5 m height | Along the line (outside array) passing through mic3 and center of the array at height 0 m |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | $\begin{array}{cc} \hline(0.0004, & 0.0040, \\ 0.0064, & 0.0062, \\ 0.0041) \\ \hline \end{array}$ | $\begin{array}{cc} (-0.0010, & 0.0032, \\ 0.0049, & 0.0053, \\ 0.0027) \end{array}$ | $\begin{array}{cc} (-0.0010, & -0.0044, \\ -0.0074, & -0.0044, \\ -0.0010) \end{array}$ | (-0.0013, -0.0043, $-0.0089,-0.0043$, -0.0013 ) | $\begin{array}{cc} (-0.0015, & -0.0056, \\ -0.0086, & -0.0056 \\ -0.0015) \end{array}$ |
| $\begin{aligned} & T D E_{c c} \\ & \left(\tau_{10}^{c c}, \tau_{20}^{c c}, \tau_{30}^{c c},,_{40}^{c c}\right) \end{aligned}$ | $(0.0043$, 0.0009, <br> 0.0067, 0.0056, <br> $-0.0025)$  | $\begin{array}{cc} \hline(0.0005, & 0.0025, \\ 0.0031, & 0.0077, \\ 0.0005) \end{array}$ | $\begin{gathered} (-0.0014, \\ -0.0054, \\ -0.0008, \\ 0.0010, \\ -0.0037) \end{gathered}$ | $\begin{array}{cc} \hline(0.0005, & -0.0150, \\ -0.0036, & 0.0019, \\ -0.0094) \end{array}$ | $\begin{array}{cc} \hline(-0.0016, & -0.0115, \\ -0.0092, & -0.0054, \\ -0.0034) \end{array}$ |
| $\begin{aligned} & T D E_{o c} \\ & \left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c},,_{40}^{o c}\right) \end{aligned}$ | $\begin{array}{cc} (-0.0174, & -0.0248, \\ -0.0181, & -0.0133, \\ -0.0081) \end{array}$ | $\begin{array}{cc} \hline(-0.0036, & 0.0003, \\ -0.0030, & -0.0030, \\ -0.0009) \end{array}$ | $\begin{array}{cc} \hline(0.0022, & -0.0011, \\ 0.0027, & -0.0031, \\ 0.0043) \end{array}$ | $\begin{array}{cc} (-0.0049, & -0.0027, \\ -0.0018, & 0.0010, \\ -0.0005) \end{array}$ | $\begin{array}{cc} (-0.0064, & -0.0145, \\ -0.0120, & -0.0105, \\ -0.0050) \end{array}$ |
| $\begin{aligned} & X_{c c} \\ & \left(x_{s}^{c c}, y_{s}^{c c}, \boldsymbol{z}_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (-1.3727,0.3006, \\ -0.7569) \end{gathered}$ | $\begin{gathered} (-1.9563,0.0145, \\ 0.0753) \end{gathered}$ | $\begin{gathered} (-1.4084,0.0421, \\ 0.9923) \end{gathered}$ | $\begin{gathered} (-1.0281,-0.5055, \\ 3.8458) \end{gathered}$ | $\begin{gathered} (-2.1488, \\ -0.4130,1.6808) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (-0.6978,-3.0374, \\ 8.2110) \end{gathered}$ | $\begin{gathered} (-1.5110,-0.0580, \\ 0.3634) \end{gathered}$ | $\begin{gathered} (-1.4462,0.2392, \\ -0.9877) \end{gathered}$ | $\begin{gathered} (-1.5661,0.4255, \\ 1.3173) \end{gathered}$ | $\begin{gathered} (-0.4923, \quad-0.6927, \\ 4.1383) \end{gathered}$ |
| $\epsilon_{\text {cc } \text { c } 3 D}$ | 1.4663 | 2.1168 | 1.8760 | 3.9164 | 2.9195 |
| $\epsilon_{c c, 2 D}$ | 1.2558 | 1.9041 | 1.5921 | 2.0356 | 2.3872 |
| $\epsilon_{\text {OC. } 3 D}$ | 9.0561 | 1.6665 | 1.8566 | 1.7044 | 5.8023 |
| $\epsilon_{O C-2 D}$ | 3.8200 | 1.5401 | 1.5721 | 1.4957 | 4.0672 |
| Time for CC (Sec) | 0.1373 | 0.1368 | 0.1373 | 0.3102 | 0.6309 |
| Time for OC (Sec) | 41.3691 | 39.6792 | 47.3056 | 48.1760 | 44.0392 |

Next we plot the $x, y$ coordinates of the actual and estimated source locations for the less-reverberant case in Fig. 6.23a and Fig. 6.23b plots the $x, y$ coordinates for the more-reverberant case. Fig. 6.23c and Fig. 6.23d plots the bargraphs for the height of source locations for the case of less- and more-reverberant scenarios respectively.


Figure 6.23: Rhombus Geometry Source Locations Estimated by CC and OC at 8 kHz Indoor using VocoPro system, (a) Source Locations estimated in the less-reverberant case, only the $x, y$ coordinates are shown, (b) Source Locations estimated in the more-reverberant case,, only the $x, y$ coordinates are shown, (c) Height Estimate for the less-reverberant case, (d) Height Estimate for the more-reverberant case

## Results for 4 kHz Sampling Rate

Table 6.32 shows the results for 4 kHz when the array was placed in the center of the hall while Table 6.33 shows the results for 4 kHz when the array was placed in a corner of the hall.

Next we plot the $x, y$ coordinates of the actual and estimated source locations for the less-reverberant case in Fig. 6.24a and Fig. 6.24b plots the $x, y$ coordinates for the more-reverberant case. Fig. 6.24c and Fig. 6.24d plots the bargraphs for the height of source locations for the case of less- and more-reverberant scenarios respectively.

Table 6.32: Rhombus indoor results using VocoPro System at 4 kHz for the case when the array was placed in the center of the hall. Slow Machine was used.

| Source Location | (2r, 0, h) | ( $2 \mathrm{r}, \mathbf{0 , 2 h )}$ | $\begin{aligned} & \left(2 r \cos 45^{\circ},\right. \\ & \left.2 r \sin 45^{\circ}, 2 h\right) \end{aligned}$ | $\begin{aligned} & \left(2 r \cos 75^{\circ},\right. \\ & \left.2 r \sin 75^{\circ}, h\right) \end{aligned}$ | $\begin{aligned} & \left(2 r \cos 88^{\circ},\right. \\ & \left.2 r \sin 88^{\circ}, h\right) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Value | $(3,0,0.5)$ | $(3,0,1)$ | (2.12, 2.12, 1.00) | (0.77, 2.89, 0.5) | (0.10, 2.99, 0.5) |
| Description | On the line passing through micl and center of the array at height of 0.5 m | On the line passing through mic1 and center of the array at height of 1 m | In-between micl and 2 outside the circumference on which mics lye. | At angle of $75^{\circ}$ between mic 1 and 2 | At angle of $88^{\circ}$ between mic1 and 2 |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | $\begin{array}{ccc} (-0.0045, & 0.0009, \\ 0.0043, & 0, & 0) \end{array}$ | (-0.0047, 0.0007, $0.0040, \quad-0.0002$, -0.0005 ) | $\begin{array}{cc} (-0.0026, & -0.0026, \\ 0.0031, & 0.0007, \\ -0.0005) \end{array}$ | $\begin{array}{cl} \hline(-0.0002, & -0.0042, \\ 0.0019, & 0.0013, \\ 0) \end{array}$ | (0.0008, -0.0045, <br> $0.0011,0.0013$, <br> 0) |
| $\begin{aligned} & T D E_{c c} \\ & \left(\tau_{10}^{c c}, \tau_{20}^{c}, \tau_{30}^{c c},,_{40}^{c c}\right) \end{aligned}$ | $\begin{array}{cc} (-0.0018, & -0.0071, \\ 0.0061, & 0.0011, \\ 0.0016) \end{array}$ | $\begin{array}{cc} \hline(-0.0003, & -0.0065, \\ -0.0005, & 0.0057, \\ -0.0103) \end{array}$ | $\begin{array}{cc} (0.0075, & -0.0065, \\ -0.0032, & 0.0047, \\ -0.0057) \end{array}$ | $\begin{array}{cc} \hline(-0.0005, & 0.0037, \\ -0.0060, & 0.0127, \\ -0.0138) \end{array}$ | $\begin{array}{cc} \hline(0.0008, & 0.0003, \\ 0.0037, & 0.0053, \\ 0.0035) \end{array}$ |
| $\begin{aligned} & T D E_{o c} \\ & \left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c},,_{40}^{o c}\right) \end{aligned}$ | $\begin{array}{cc} (0.0083, & -0.0103, \\ -0.0022, & 0.0013, \\ -0.0015) \end{array}$ | $\begin{array}{cc} (0.0008, & -0.0080, \\ -0.0057, & 0.0175, \\ 0.0013) \end{array}$ | $\begin{array}{cc} \hline(0.0077, & -0.0030, \\ 0.0025, & 0.0158, \\ 0.0043) \end{array}$ | $\begin{array}{cc} \hline(0.0030, & -0.0030, \\ 0.0030, & 0.0035, \\ 0.0138) \end{array}$ | $(0.0010$, 0.0013, <br> -0.0027, 0.0065, <br> $0.0025)$  |
| $\begin{aligned} & X_{c c} \\ & \left(x_{s}^{c c}, y_{s}^{c c}, z_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (11.7638,-10.4075, \\ -9.9372) \end{gathered}$ | $\begin{gathered} (-0.0224,1.5024, \\ -1.5358) \end{gathered}$ | $\begin{gathered} (-0.7715,-0.3331, \\ -1.5925) \end{gathered}$ | $\begin{gathered} (0.9106,3.8096, \\ -8.7717) \end{gathered}$ | $\begin{gathered} (0.6780, \quad 0.6066, \\ 0.7956) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{x_{s}^{c},}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (-0.8176,-3.5090, \\ -0.7050) \end{gathered}$ | $\begin{gathered} (3.0570,-7.1134, \\ -0.8894) \end{gathered}$ | $\begin{gathered} (0.9054,-3.3654, \\ 5.6364) \end{gathered}$ | $\begin{gathered} (0, \\ \hline \\ 6.4 .7682, \end{gathered}$ | $\begin{gathered} (0.6080,0.6820, \\ 1.2015) \end{gathered}$ |
| $\epsilon_{c c, 3 D}$ | 12.9342 | 4.2217 | 4.5934 | 9.3182 | 2.4703 |
| $\epsilon_{c c-2 D}$ | 15.2357 | 3.3752 | 3.7919 | 0.9303 | 2.4525 |
| $\epsilon_{o c .3 D}$ | 5.3234 | 7.3603 | 7.2843 | 8.9378 | 2.4651 |
| $\epsilon_{o C-2 D}$ | 5.1853 | 7.1137 | 5.6182 | 6.7026 | 2.3632 |
| Time for CC (Sec) | 0.3846 | 0.2279 | 0.0690 | 0.0451 | 0.0768 |
| Time for OC (Sec) | 63.4931 | 27.2423 | 24.4149 | 118.6396 | 27.8298 |



Figure 6.24: Rhombus Geometry Source Locations Estimated by CC and OC at 4 kHz Indoor using VocoPro system, (a) Source Locations estimated in the less-reverberant case, only the $x, y$ coordinates are shown, (b) Source Locations estimated in the more-reverberant case,, only the $x, y$ coordinates are shown, (c) Height Estimate for the less-reverberant case, (d) Height Estimate for the more-reverberant case

Table 6.33: Rhombus indoor results using VocoPro System at 4 kHz for the case when the array was placed in a corner of the hall. Slow Machine was used.

| Source Location | (2r, 0, h) | ( $\mathbf{2 r}, \mathbf{0 , 2 h ) ~}$ | $\begin{aligned} & \left(2 r \cos 45^{\circ},\right. \\ & \left.2 r \sin 45^{\circ}, 2 h\right) \end{aligned}$ | $\begin{aligned} & \left(2 r \cos 75^{\circ},\right. \\ & \left.2 r \sin \left(\pi+75^{\circ}\right), h\right) \end{aligned}$ | $\begin{aligned} & \left(2 r \cos 88^{\circ},\right. \\ & \left.2 r \sin \left(\pi+88^{\circ}\right), h\right) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Value | (3, 0, 0.5) | $(3,0,1)$ | (2.12, 2.12, 1.00) | (0.77, -2.99, 0.5) | (0.10, -2.99, 0.5) |
| Description | On the line passing through mic1 and center of the array at height of 0.5 m | On the line passing through mic1 and center of the array at height of 1 m | In-between micl and 2 outside the circumference on which mics lye. | At angle of $255^{\circ}$ between mic 3 and 4 | At angle of $268^{\circ}$ between mic3 and 4 |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | $\begin{array}{lll} (-0.0045, & 0.0009 \\ 0.0043, & 0, & 0 \end{array}$ | $\begin{array}{cc} (-0.0047, & 0.0007, \\ 0.0040, & -0.0002, \\ -0.0005) \end{array}$ | $\begin{array}{cc} (-0.0026, & -0.0026, \\ 0.0031, & 0.0007, \\ -0.0005) \end{array}$ | $\begin{array}{cc} (-0.0002, & 0.0042, \\ 0.0019, & -0.0015, \\ 0) \end{array}$ | $\begin{array}{cc} (0.0008, & 0.0043, \\ 0.0011, & -0.0016, \\ 0) \end{array}$ |
| $\begin{aligned} & T D E_{c c} \\ & \left(\tau_{10}^{c c}, \tau_{20}^{c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{array}{cc} \hline(-0.0113, & 0.0050, \\ -0.0085, & -0.0018, \\ 0.0055) \end{array}$ | $\begin{array}{cc} \hline(0.0055, & 0.0125, \\ 0.0095, & 0.0190, \\ 0.0060) \end{array}$ | $\begin{array}{cc} \hline(-0.0027, & -0.0110, \\ 0.0135, & 0.0022, \\ 0.0043) \end{array}$ | $\begin{array}{cc} \hline(0.0013, & 0.0110, \\ -0.0018, & 0.0032, \\ 0.0015) \end{array}$ | $\begin{array}{cc} \hline(-0.0027, & -0.0150, \\ -0.0022, & 0.0055, \\ -0.0060) \end{array}$ |
| $\begin{aligned} & T D E_{o c} \\ & \left(\tau_{10}^{o c}, \tau_{20}^{o,}, \tau_{30}^{o c},,_{40}^{o c}\right) \end{aligned}$ | $\begin{array}{cc} (0.0043, & -0.0018, \\ -0.0015, & 0.0005, \\ -0.0013) \end{array}$ | $\begin{array}{cc} \hline(0.0013, & 0.0020, \\ -0.0113, & 0.0065, \\ 0.0070) \end{array}$ | $\begin{array}{cc} \hline(0.0035, & -0.0012, \\ 0.0050, & 0.0090, \\ 0.0030) \end{array}$ | $\begin{gathered} (0,-0.0053,-0.0047, \\ -0.0025, \\ 0.0003) \end{gathered}$ | $\begin{array}{cc} \hline(0.0043, & 0.0008, \\ -0.0005, & -0.0003, \\ 0.0013) \end{array}$ |
| $\begin{aligned} & X_{c c} \\ & \left(x_{s}^{c c}, y_{s}^{c c}, z_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (-0.7541,-0.7443, \\ -2.2780) \end{gathered}$ | $\begin{gathered} (-0.3730, \quad 2.2572, \\ 7.2009) \end{gathered}$ | $\begin{gathered} (0.8201,-6.5767, \\ -0.9456) \end{gathered}$ | $\begin{gathered} (0.5112,-0.7912, \\ 1.4346) \end{gathered}$ | $\begin{gathered} (-0.2282,-16.3172, \\ -6.7394) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{c o}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (-0.7384, \quad 0.7084, \\ 0.7430) \end{gathered}$ | $\begin{gathered} (1.8774,1.7742, \\ -3.5569) \end{gathered}$ | $\begin{gathered} (0.0001,-0.0609, \\ 2.0105) \end{gathered}$ | $\begin{gathered} (0.3849,-0.2167, \\ 0.5821) \end{gathered}$ | $\begin{gathered} (-0.6696, \\ 0.4858, \\ 0.4619) \end{gathered}$ |
| $\epsilon_{c c, 3 D}$ | 4.7291 | 7.4110 | 9.0060 | 2.3120 | 15.1701 |
| $\epsilon_{c c-2 D}$ | 3.8272 | 4.0586 | 8.7934 | 2.1146 | 13.3313 |
| $\epsilon_{\text {OC } 3 \text { d }}$ | 3.8127 | 5.0173 | 3.2049 | 2.7022 | 3.5602 |
| $\epsilon_{\text {OC.2D }}$ | 3.8050 | 2.0995 | 3.0414 | 2.7009 | 3.5599 |
| Time for CC (Sec) | 0.0448 | 0.0438 | 0.0365 | 0.0354 | 0.0364 |
| Time for OC (Sec) | 24.3726 | 25.3826 | 26.8228 | 33.1654 | 25.2192 |

### 6.3.4 Observations for the Experiments using VocoPro

## System

Looking at the results in subsections 6.3.1 to 6.3 .3 we can find the numerical facts about the results for the VocoPro system. We present these numerical facts in subsection 6.3.4 and then based on these numerical facts we deduce the observations and present them in subsection 6.3.4

## Numerical Facts

1. For the Pyramid 8 kHz , less-reverberant case: $80 \%$ of the time CC produces more correct results than OC by a factor of at least 1.27 i.e. CC 3D-MSE $\left(\epsilon_{C C \_3 D}\right)$ is at least 1.27 times less than OC 3D-MSE ( $\left.\epsilon_{O C \_3 D}\right)$ for $80 \%$ of the source locations. The runtime for OC is at least 1160 times more than the runtime for CC .
2. For the Pyramid 8 kHz , more-reverberant case: $80 \%$ of the time CC produces more correct results than OC by a factor of at least 1.09. The runtime for OC is at least 750 times more than the runtime for CC.
3. For the Pyramid 4 kHz , less-reverberant case: $60 \%$ of the time OC produces more correct results than CC by a factor of at least 1.04. The runtime for OC is at least 200 times more than the runtime for CC.
4. For the Pyramid 4 kHz , more-reverberant case: $80 \%$ of the time CC produces more correct results than OC by a factor of at least 1.13. The runtime for OC is at least 300 times more than the runtime for CC.
5. For the Circular 8 kHz , less-reverberant case: $60 \%$ of the time OC produces more correct results than CC by a factor of at least 1.102. The runtime for OC is at least 260 times more than the runtime for CC.
6. For the Circular 8 kHz , more-reverberant case: $60 \%$ of the time OC produces more correct results than CC by a factor of at least 1.01. The runtime for OC is at least 280 times more than the runtime for CC.
7. For the Circular 4 kHz , less-reverberant case: $100 \%$ of the time OC produces more correct results than CC by a factor of at least 1.04. The runtime for OC is at least 430 times more than the runtime for CC.
8. For the Circular 4 kHz , more-reverberant case: $80 \%$ of the time OC produces more correct results than CC by a factor of at least 1.106. The runtime for OC is at least 350 times more than the runtime for CC.
9. For the Rhombus 8 kHz , less-reverberant case: $60 \%$ of the time OC produces more correct results than CC by a factor of at least 1.102. The runtime for OC is at least 260 times more than the runtime for CC.
10. For the Rhombus 8 kHz , more-reverberant case: $60 \%$ of the time OC produces more correct results than CC by a factor of at least 1.01. The runtime for OC is at least 300 times more than the runtime for CC.
11. For the Rhombus 4 kHz , less-reverberant case: $60 \%$ of the time CC produces more correct results than OC by a factor of at least 1.004. The runtime for OC is at least 350 times more than the runtime for CC.
12. For the Rhombus 4 kHz , more-reverberant case: $80 \%$ of the time OC produces more correct results than CC by a factor of at least 1.24. The runtime for OC is at least 540 times more than the runtime for CC.

## Indoor VocoPro Experiments Observations

Looking at the numerical facts in subsection 6.3 .4 we can make the following observations for the experiments carried out indoor using VocoPro system.

1. $70 \%$ of the time CC produces better results for the Pyramid geometry for the less reverberant case by a factor of at least 1.04 while $80 \%$ times for the more-reverberant case by a factor of at least 1.09 than the OC. The OC still takes more time than CC, at least 200 times more than CC both for lessand more-reverberant cases.
2. $80 \%$ of the time OC produces better results for the Circular geometry for the less reverberant case by a factor of at least 1.04 while $70 \%$ times for the more-reverberant case by a factor of at least 1.01 than the CC. But this accuracy comes at the cost of at least 260 times more runtime taken by OC than CC both for the less- and more-reverberant environments.
3. $60 \%$ of the time OC produces better results for the Rhombus geometry for the less reverberant case by a factor of at least 1.004 while at least $70 \%$ of the time for the more-reverberant case by a factor of at least 1.01 than the CC. But this accuracy comes at the cost of at least 260 times more runtime taken by OC than CC for the less-reverberant case and at least 300 times more runtime by OC than CC for the more-reverberant case.
4. The Rhombus geometry produces the least accurate results with a minimum $\epsilon_{O C \_3 D}$ of value 1.27 m among the three geometries while the Pyramid ge-
ometry produces the most accurate results with a minimum $\epsilon_{O C \_3 D}$ of value 0.68 m . The Circular is in-between Rhombus and Pyramid, accuracy-wise, with a minimum $\epsilon_{O C \_3 D}$ of value 1.25 m .
5. The 8 kHz case is taking at least 2 times more runtime for OC than 4 kHz case for all the geometries
6. The OC algorithm is taking at least 200 times more runtime than CC for all the cases of indoor experimentation using VocoPro.
7. At least $70 \%$ of the time the OC produces more accurate results than CC in the less- and more-reverberant environment for all the indoor experimental scenarios using VocoPro system.

### 6.4 Conclusion

An extensive experimentation and analysis was carried out for the indoor 3D geometries using two different hardware systems in this chapter. Two different sampling rate i.e. 4 kHz and 8 kHz were used during experimentation to compare the results of the OC algorithm with the classical CC TDE techniques. Several scenarios for the experimentation were considered which may be encountered during practical situations. Three different geometries were considered to see the effect of the geometry on the performance of the OC algorithm. Further more, in Pyramid geometry five sensors were used while in the remaining two geometries six sensors were used. A parametric analysis of the OC algorithm was also
conducted to see the variation in the results of the algorithm due to variation in various parameters. Specifically it was shown that the OC algorithm is sensitive to the signal shape.

It was observed that the Pyramid geometry produces best results among the three geometries with a minimum 3D-MSE OC error of 0.21 m when using the RevoLabs system . This verifies that the structure of the geometry is more important than the number of sensors. The Rhombus geometry provides the least accurate results with a minimum 3D-MSE OC error of 1.25 m . The OC algorithm was producing at least $70 \%$ of the times better results than CC for the RevoLabs system with a runtime tradeoff of up to 90 times more than that of CC. With VocoPro system the OC algorithm was producing at least $70 \%$ of the times better results than CC with a runtime tradeoff of up to 200 times more than that of CC.

The VocoPro system produces at least four times erroneous results compared to the RevoLabs system. Thus the signal acquisition hardware plays an important role in the source localization system.

## CHAPTER 7

## OUTDOOR EXPERIMENTS

## AND RESULTS

In this chapter we discuss in detail the experiments we conducted in an outdoor environment and their results and analysis. Section 7.1 gives the details of the experimental scenarios we are considering and the environment details. Section 7.2 discuss in detail the experiments conducted using the RevoLabs Wireless Microphone System and their results while section 7.3 discuss the experiments and their results conducted using VocoPro Wireless Microphone System. Section 7.5 concludes this chapter.

### 7.1 Experimental Scenarios

Fig. 7.1 shows the satellite image of the outdoor location where we conducted all our outdoor experiments. This image was taken using Google ${ }^{T M}$ Earth [43] software, version 6.1.0 in April 2012. The red solid line in Fig. 7.1 provides the
distances of the nearby buildings and trees from the center of the spot where experiments took place. These distances are long enough such that there is no reverberation observed in the signals we captured. However, the reflections from the walls of the nearby buildings still exist, specifically in the case of loaded gunfire.


Figure 7.1: Satellite image of the outdoor experimental environment

Fig. 7.2 shows all the experimental scenarios in the form of block diagram. Note that there is no center- or wall-version of the experiment as we did in the indoor experiments. Also Fig. 7.2 shows only two sampling rates i.e. 4 kHz and 8 kHz although we acquired the signals at 16 kHz as well. This is because the OC algorithm could not be run on the PCs we have because of the large amount of memory required for the case of 16 kHz , hence we did not include it in Fig. 7.2.


Figure 7.2: Outdoor experimental scenarios

### 7.2 Results using RevoLabs System

In this section we discuss in detail the outdoor experiments we conducted using the RevoLabs system and their results and analysis. As there are three different geometries and each geometry has different scenarios we need to organize the discussion in the following subsections. Subsections 7.2.1, 7.2.2 and 7.2.3 discuss the results for Pyramid, Circular and Rhombus geometries in outdoor environment using RevoLabs System respectively. The observations and discussion are given in subsection 7.2.4. It is to be noted that we used an unloaded toy gunshot for all the experiments using the RevoLabs system.

### 7.2.1 Pyramid Geometry Experiments and Results

In this section we discuss the results for the Pyramid geometry obtained using the RevoLabs wireless microphone system. We are using the geometry with the source locations discussed in Section 5.2.1. Fig. 7.3 shows the experimental setup of the Pyramid geometry using the RevoLabs system. Note that we carried out all our experiments during night to avoid the daily life noise and disturbances although a practical system would require to work in any situation. This is because we wanted to assess the OC algorithm performance and compare it with CC results without the results being affected by the environmental factors.


Figure 7.3: Pyramid geometry using RevoLabs system outdoor

There are several experimental scenarios as was shown in Fig. 7.2. The results
are organized with respect to the sampling rate and follow next.

## Results for the 8 kHz Case

Table 7.1 shows the results we obtained for the case of 8 kHz . Using the results from Table 7.1 we plot the $x, y$ coordinates of the estimated source locations in Fig. 7.5a while Fig. 7.4b plots the bargraph for the $z$-coordinate of the estimated source locations along with the actual source locations.

Table 7.1: Pyramid Outdoor results using RevoLabs at 8kHz. Fast Machine was used.

| Source Location | $\begin{gathered} \left(\cos 60^{\circ}, \sin 60^{\circ}, 0.5\right) \\ =(0.5,0.866,0.5) \end{gathered}$ | $\begin{gathered} \left(2 \cos 60^{\circ}, 2 \sin 60^{\circ}, 0\right)=(1, \\ 1.73,0) \end{gathered}$ | $\begin{gathered} \left(2.5 \cos 60^{\circ}, 2.5 \sin 60^{\circ}, 0\right)= \\ (1.25,2.16,0) \end{gathered}$ | $(0,0,1)$ | $(2.5,0,0)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Description | In-between $a_{1}$ and $a_{2}$ inside the array at height of 0.5 m at $60^{\circ}$ | In-between $a_{1} \& a_{2}$ on the circle inscribing the array. | In-between $a_{1} \& a_{2}$, outside the array | Above the center of the array | Along the line (outside array) passing through $a_{1}$ and center of the array |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | $\begin{array}{lr} (0.0020, & 0.0020 \\ 0.0057, & -0.0003) \end{array}$ | $\begin{gathered} (0, \quad 0.0000, \quad 0.0059, \\ 0.0004) \end{gathered}$ | $\begin{array}{cc} (-0.0006, & -0.0006 \\ 0.0059, & 0.0003) \end{array}$ | $\begin{array}{cc} (0.0036, & 0.0036, \\ 0.0036, & -0.0021) \end{array}$ | $\begin{array}{cc} (-0.0059, & 0.0041, \\ 0.0041, & 0.0003) \end{array}$ |
| $\begin{aligned} & T D E_{C C} \\ & \left(\tau_{10}^{c c}, \tau_{20}^{c c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{array}{cc} (0.0037, & 0.0015, \\ 0.0084, & 0) \end{array}$ | $\begin{array}{cc} (0.0019, & -0.0008, \\ 0.0073, & 0.0006) \end{array}$ | $\begin{array}{cc} (-0.0009, & -0.0008, \\ 0.0064, & -0.0001) \end{array}$ | $\begin{array}{lr} (0.0047, & 0.0085, \\ 0.0053, & -0.0024) \end{array}$ | $\begin{array}{cc} (-0.0040, & 0.0049 \\ 0.0083, & 0.0004) \end{array}$ |
| TDE ${ }_{\text {oc }}$ <br> $\left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c}, \tau_{40}^{o c}\right)$ | $\begin{array}{lr} (0.0026, & 0.0024, \\ 0.0045, & -0.0015) \end{array}$ | $\begin{array}{ll} (0.0011, & 0.0005, \\ 0.0046, & 0.0016) \end{array}$ | $\begin{array}{rr} (-0.0018, & -0.0015, \\ 0.0072, & 0) \end{array}$ | $\begin{array}{ll} (0.0026, & 0.0021, \\ 0.0022, & 0.0001) \end{array}$ | $\begin{array}{cc} (-0.0013, & 0.0004, \\ 0.0019, & -0.0021) \end{array}$ |
| $\begin{aligned} & X_{c c} \\ & \left(x_{s}^{c c}, \boldsymbol{y}_{s}^{c c}, z_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (0.4683,1.2863 \\ 0.3600) \end{gathered}$ | $\begin{gathered} (0.5932,1.6194 \\ 0.0461) \end{gathered}$ | $\begin{gathered} (1.3071,2.2164 \\ 0.4894) \end{gathered}$ | $\begin{gathered} (0.4857,-0.6912, \\ -0.2842) \end{gathered}$ | $\begin{gathered} (0.4866, \quad 0.7143 \\ 0.3620) \end{gathered}$ |
| $\begin{aligned} & X_{O C} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (0.2428,0.5038 \\ 1.0798) \end{gathered}$ | $\begin{gathered} (0.5426, \quad 1.2436, \\ -1.5405) \end{gathered}$ | $\begin{gathered} (1.5263,2.5573, \\ 0.3600) \end{gathered}$ | $\begin{gathered} (-0.1457,0.0351, \\ 0.2335) \end{gathered}$ | $\begin{gathered} (4.5163,2.5238 \\ 16.8156) \end{gathered}$ |
| $\epsilon_{\text {cc_ } 3 D}$ | 0.4441 | 0.4241 | 0.4959 | 1.5371 | 2.1668 |
| $\epsilon_{c c \_2 D}$ | 0.4215 | 0.4215 | 0.0802 | 0.8448 | 2.1363 |
| $\epsilon_{O C}$ [ 3 D | 0.7304 | 1.6790 | 0.6032 | 0.7810 | 17.1230 |
| $\epsilon_{O C-2 D}$ | 0.4443 | 0.6677 | 0.4840 | 0.1498 | 3.2303 |
| Time for CC (Sec) | 0.0345 | 0.0351 | 0.0350 | 0.0351 | 0.0343 |
| Time for OC (Sec) | 61.4610 | 66.5716 | 62.8896 | 45.6164 | 38.9513 |



Figure 7.4: Pyramid Geometry Source Locations Estimated by CC and OC at 8 kHz Outdoor using RevoLabs system, (a) The $x, y$ coordinates of estimated source Locations, (b) The $z$ coordinate of the estimated source locations.

## Results for the 4 kHz Case

Table 7.2 shows the results we obtained for the case of 4 kHz . Using the results from Table 7.2 we plot the $x, y$ coordinates of the estimated source locations in Fig. 7.5a while Fig. 7.5b plots the bargraph for the $z$-coordinate of the estimated source locations along with the actual source locations.

Table 7.2: Pyramid Outdoor results using RevoLabs at 4kHz. Slow Machine was used.

| Source Location | $\begin{gathered} \left(\cos 60^{\circ}, \sin 60^{\circ}, 0.5\right) \\ =(0.5,0.866,0.5) \end{gathered}$ | $\begin{gathered} \left(2 \cos 60^{\circ}, 2 \sin 60^{\circ}, 0\right)=(1, \\ 1.73,0) \end{gathered}$ | $\begin{gathered} \left(2.5 \cos 60^{\circ}, 2.5 \sin 60^{\circ}, 0\right)= \\ (1.25,2.16,0) \end{gathered}$ | (0,0,1) | (2.5, 0, 0) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Description | In-between $a_{1}$ and $a_{2}$ inside the array at height of 0.5 m at $60^{\circ}$ | In-between $a_{1} \& a_{2}$ on the circle inscribing the array. | In-between $a_{1} \& a_{2}$, outside the array | Above the center of the array | Along the line (outside array) passing through $a_{1}$ and center of the array |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | $\begin{array}{lr} (0.0020, & 0.0020, \\ 0.0057, & -0.0003) \end{array}$ | $\begin{array}{cc} (0, & 0.0000, \\ 0.0004) \end{array}$ | $\begin{array}{cl} (-0.0006, & -0.0006, \\ 0.0059, & 0.0003) \end{array}$ | $\begin{array}{lr} (0.0036, & 0.0036, \\ 0.0036, & -0.0021) \end{array}$ | $\begin{array}{cc} (-0.0059, & 0.0041, \\ 0.0041, & 0.0003) \end{array}$ |
| TDE ${ }_{\text {cC }}$ <br> $\left(\tau_{10}^{c c}, \tau_{20}^{c c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right)$ | $\begin{array}{cc} (0.0035, & -0.0015, \\ 0.0077, & 0) \end{array}$ | $\begin{array}{lr} (0.0032, & 0.0018, \\ 0.0073, & -0.0010) \end{array}$ | $\begin{array}{cc} (0.0013, & -0.0020, \\ 0.0075, & 0.0003) \end{array}$ | $\begin{array}{ll} (0.0047, & 0.0085, \\ 0.0053, & 0.0010 \end{array}$ | $\begin{array}{cc} (-0.0043, & 0.0057, \\ 0.0083, & -0.0015) \end{array}$ |
| TDE ${ }_{\text {oc }}$ <br> $\left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c},,_{40}^{o c}\right)$ | $\begin{array}{cc} (0.0030, & -0.0015, \\ 0.0022, & 0.0008) \end{array}$ | $\begin{array}{cc} (-0.0022, & -0.0027, \\ -0.0008, & 0) \end{array}$ | $\begin{array}{ll} (-0.0035, & -0.0015, \\ -0.0008, & -0.0027) \end{array}$ | $\begin{array}{cc} (-0.0010, & 0.0045, \\ 0.0018, & -0.0008) \end{array}$ | $\begin{array}{lr} (-0.0040, & 0.0008, \\ -0.0010, & -0.0030) \end{array}$ |
| $\begin{aligned} & \hline X_{c c} \\ & \left(x_{s}^{c c}, y_{s}^{c c}, z_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (0.3426,1.4275, \\ 0.3600) \end{gathered}$ | $\begin{gathered} (0.4063,1.1077, \\ 0.5262) \end{gathered}$ | $\begin{gathered} (0.7301,1.8580, \\ 0.2301) \end{gathered}$ | $\begin{gathered} (0.4857,-0.6912, \\ 0.3603) \end{gathered}$ | $\begin{gathered} (0.2842, \quad 0.5182, \\ -0.0106) \end{gathered}$ |
| $\begin{aligned} & \hline X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (-1.2830, \quad 1.5068, \\ -1.0899) \end{gathered}$ | $\begin{gathered} (-0.1711,-0.6427, \\ 0.3600) \end{gathered}$ | $\begin{gathered} (-0.9151,-0.2213, \\ -3.6543) \end{gathered}$ | $\begin{gathered} (1.4036,-0.9580, \\ 1.2697) \end{gathered}$ | $\begin{gathered} (-1.8082,0.5998 \\ -5.2496) \end{gathered}$ |
| $\epsilon_{c c, 3 D}$ | 0.5998 | 1.0083 | 0.6438 | 1.0597 | 2.2756 |
| $\epsilon_{c c .2 D}$ | 0.5832 | 0.8600 | 0.6013 | 0.8448 | 2.2756 |
| $\epsilon_{o c .3 D}$ | 2.4733 | 2.6704 | 4.8695 | 1.7207 | 6.8176 |
| $\epsilon_{O C .2 D}$ | 1.8946 | 2.6460 | 3.2184 | 1.6994 | 4.3498 |
| Time for CC (Sec) | 0.4294 | 0.0427 | 0.0433 | 0.0429 | 0.0426 |
| Time for OC (Sec) | 16.2785 | 19.5867 | 20.3712 | 22.0094 | 19.8440 |



Figure 7.5: Pyramid Geometry Source Locations Estimated by CC and OC at 4 kHz Outdoor using RevoLabs system, (a) The $x, y$ coordinates of estimated source Locations, (b) The $z$ coordinate of the estimated source locations.

### 7.2.2 Circular Geometry Experiments and Results

In this section we discuss the results for the Circular geometry obtained using RevoLabs wireless microphone system. We are using the geometry with the source locations discussed in Section 5.2.1. Fig. 7.6 shows the experimental setup of the Circular geometry using RevoLabs system which was also conducted during night.


Figure 7.6: Circular geometry using RevoLabs system outdoor

There are several experimental scenarios as was shown in Fig. 7.2. The results are organized with respect to the sampling rate and follows next.

## Results for the 8 kHz Case

Table 7.3 shows the results we obtained for the case of 8 kHz . Using the results from Table 7.3 we plot the $x, y$ coordinates of the estimated source locations in Fig. 7.7a while Fig. 7.7b plots the bargraph for the $z$-coordinate of the estimated source locations along with the actual source locations.

Table 7.3: Circular Outdoor results using RevoLabs at 8 kHz . Fast Machine was used.

| Source Location | $\begin{gathered} \left(r \cos 30^{\circ}-r\right. \\ \left.r \sin 30^{\circ}, 0\right) \end{gathered}$ | $\left(r \cos 30^{\circ}-r, r \sin 30^{\circ}, 1\right)$ | $(-2 r, 0,0)$ | (-2r, 0, 0.5) | (-3r, 0, 0) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Value | (-0.2 0.7500, 0) | (-0.2, 0.7500, 1) | (-3, 0, 0) | $(-3,0,0.5)$ | (-4.5, 0, 0) |
| Description | In-between mic0 and $1\left(a_{0}, a_{1}\right)$ on the circumference at height of 0 m | In-between mic0 and 1 ( $a_{0}, a_{1}$ ) on the circumference at height of 1 m | At mic3 ( $a_{3}$ ) with zero height | At mic3 $\left(a_{3}\right)$ with 0.5 m height | Along the line (outside array) passing through mic3 ( $a_{3}$ ) and center of the array at height 0m |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | $\begin{array}{cc} (0.0004, & 0.0040, \\ 0.0064, & 0.0062, \\ 0.0041) \end{array}$ | $\begin{array}{cc} \hline(-0.0010, & 0.0032, \\ 0.0049, & 0.0053, \\ 0.0027) \end{array}$ | $\begin{array}{cc} (-0.0010, & -0.0044, \\ -0.0074, & -0.0044, \\ -0.0010) \end{array}$ | $\begin{array}{cc} \hline(-0.0013, & -0.0043, \\ -0.0089, & -0.0043, \\ -0.0013) \end{array}$ | $\begin{array}{cc} (-0.0015, & -0.0056, \\ -0.0086, & -0.0056, \\ -0.0015) \end{array}$ |
| $\begin{aligned} & T D E_{c c} \\ & \left(\tau_{10}^{c c}, \tau_{20}^{c c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{array}{cc} \hline(0.0014, & 0.0067, \\ 0.0079, & 0.0074, \\ 0.0048) \end{array}$ | $\begin{array}{cc} \hline(-0.0033, & 0.0050 \\ 0.0070, & 0.0064, \\ 0.0040) \end{array}$ | $\begin{array}{cc} \hline(-0.0014, & -0.0038, \\ -0.0057, & -0.0029, \\ -0.0012) \end{array}$ | $\begin{array}{cc} \hline(-0.0010, & -0.0033, \\ -0.0069, & -0.0033, \\ -0.0018) \end{array}$ | $\begin{array}{cc} \hline(0.0006, & -0.0043, \\ -0.0044, & -0.0034, \\ -0.0006) \end{array}$ |
| $\begin{aligned} & T D E_{o c} \\ & \left(\tau_{10}^{o c}, \boldsymbol{\tau}_{20}^{o c}, \tau_{30}^{o c}, \tau_{40}^{o c}\right) \end{aligned}$ | $\begin{array}{cc} \hline 0.0009, & 0.0049, \\ 0.0069, & 0.0066, \\ 0.0038) \end{array}$ | $\begin{array}{cc} (-0.0029, & 0.0031, \\ 0.0050, & 0.0055, \\ 0.0035) \end{array}$ | $\begin{array}{cc} (-0.0006, & -0.0035, \\ -0.0062, & -0.0035, \\ -0.0013) \end{array}$ | $\begin{array}{cc} \hline(-0.0009, & -0.0030, \\ -0.0075, & -0.0038, \\ -0.0010) \end{array}$ | $\begin{array}{ccc} (0.0008, & -0.0010 \\ -0.0019, & 0, & 0.0019) \end{array}$ |
| $\begin{aligned} & X_{c c} \\ & \left(x_{s}^{c c}, y_{s}^{c c}, \boldsymbol{X}_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (-0.5055,0.2660, \\ 0.7977) \end{gathered}$ | $\begin{gathered} (-0.3900, \quad 0.3906, \\ 0.1767) \end{gathered}$ | $\begin{gathered} (-2.6153,0.1293, \\ 0.8050) \end{gathered}$ | $\begin{gathered} (-2.4742,-0.1079, \\ 0.9082) \end{gathered}$ | $\begin{gathered} (-1.4648,-0.0894, \\ 0.2004) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{\left.x_{s}^{c}, y_{s}^{o c}, z_{s}^{o c}\right)}\right. \end{aligned}$ | $\begin{gathered} (0.1202, \quad 0.6295, \\ 0.4137) \end{gathered}$ | $\begin{gathered} (-0.5272, \quad 0.7006, \\ 0.4647) \end{gathered}$ | $\begin{gathered} (-2.3847, \\ 0.2354) \end{gathered}$ | $\begin{gathered} (-2.3921,-0.0745, \\ 0.2974) \end{gathered}$ | $\begin{gathered} (-1.4908, \\ -0.0295, \\ -0.0245) \end{gathered}$ |
| $\epsilon_{c c, 3 D}$ | 0.9818 | 0.9181 | 0.9015 | 0.6743 | 3.0431 |
| $\epsilon_{\text {cc-2 }}{ }^{\text {d }}$ | 0.5723 | 0.4065 | 0.4059 | 0.5367 | 3.0365 |
| $\epsilon_{o C, 3 D}$ | 0.5368 | 0.6293 | 0.6649 | 0.6451 | 3.0095 |
| $\epsilon_{O C, 2 D}$ | 0.3421 | 0.3309 | 0.6218 | 0.6125 | 3.0094 |
| Time for CC (Sec) | 0.2126 | 0.2356 | 0.1413 | 0.1381 | 0.1543 |
| Time for OC (Sec) | 56.1228 | 55.1528 | 65.5428 | 77.7755 | 62.7603 |



Figure 7.7: Circular Geometry Source Locations Estimated by CC and OC at 8 kHz Outdoor using RevoLabs system, (a) The $x, y$ coordinates of estimated source Locations, (b) The $z$ coordinate of the estimated source locations.

## Results for the 4 kHz Case

Table 7.4 shows the results we obtained for the case of 4 kHz . Using the results from Table 7.4 we plot the $x, y$ coordinates of the estimated source locations in Fig. 7.8a while Fig. 7.8b plots the bargraph for the $z$-coordinate of the estimated source locations along with the actual source locations.

Table 7.4: Circular Outdoor results using RevoLabs at 4kHz. Slow Machine was used.

| Source Location | $\begin{gathered} \left(r \cos 30^{\circ}-r,\right. \\ \left.r \sin 30^{\circ}, 0\right) \end{gathered}$ | $\left(r \cos 30^{\circ}-r, r \sin 30^{\circ}, 1\right)$ | $(-2 r, 0,0)$ | $(-2 r, 0,0.5)$ | $(-3 \mathrm{r}, 0,0)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Value | (-0.2 0.7500, 0) | (-0.2, 0.7500, 1) | $(-3,0,0)$ | $(-3,0,0.5)$ | $(-4.5,0,0)$ |
| Description | In-between mic0 and $1\left(a_{0}, a_{1}\right)$ on the circumference at height of 0 m | In-between mic0 and 1 ( $a_{0}, a_{1}$ ) on the circumference at height of 1 m | At mic3 $\left(a_{3}\right)$ with zero height | At mic3 $\left(a_{3}\right)$ with 0.5 m height | Along the line (outside array) passing through $\operatorname{mic} 3\left(a_{3}\right)$ and center of the array at height 0m |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | (0.0004, 0.0040 , $0.0064, \quad 0.0062$, 0.0041) | $(-0.0010, \quad 0.0032, \quad 0.0049$, $0.0053, \quad 0.0027)$ | (-0.0010, -0.0044, - <br> $0.0074,-0.0044,-0.0010)$ | $(-0.0013,-0.0043,-0.0089$, $-0.0043,-0.0013)$ | $(-0.0015,-0.0056$, - <br> $0.0086,-0.0056,-0.0015)$ |
| $\begin{aligned} & T D E_{C C} \\ & \left(\tau_{10}^{c c}, \tau_{20}^{c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{array}{cc} \hline 0.0035, & 0.0057, \\ 0.0107, & 0.0065, \\ 0.0057) \end{array}$ | (0.0037, 0.0057, 0.0098, $0.0065, \quad 0.0065)$ | $(-0.0003, \quad 0.0047, \quad 0.0070$, $0.0020, \quad 0.0020)$ | $(-0.0013, \quad 0.0008,0.0020$, $-0.0022,-0.0020)$ | (0.0008, -0.0050, -0.0037, $-0.0008, \quad 0.0030)$ |
| $\begin{aligned} & T D E_{o c} \\ & \left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c}, \tau_{40}^{o o}\right) \end{aligned}$ | $(-0.0020$, 0.0010, <br> 0.0003, -0.0008, <br> $0.0010)$  | (0.0032, $0.0008, ~ 0.0047$, $0.0010, \quad 0.0037)$ | (0.0005, -0.0008, -0.0003, $0.0010,-0.0020)$ | $\begin{gathered} (0.0027,-0.0003, \quad 0.0005, \\ 0, \quad 0.0018) \end{gathered}$ | (0.0027, -0.0020, -0.0005, $0.0005, \quad 0.0030)$ |
| $\begin{aligned} & X_{c c} \\ & \left(x_{s}^{c c}, y_{s}^{c c}, Z_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (-1.3972,0.0751, \\ 0.3319) \end{gathered}$ | $\begin{gathered} (0.5197,0.6436, \\ -4.0344) \end{gathered}$ | $\begin{gathered} (-1.7170,-0.1214, \\ 0.0566) \end{gathered}$ | $\begin{gathered} (-1.4342, \quad 0.0593, \\ 0.0996) \end{gathered}$ | $\begin{gathered} \hline(-1.4167,-0.0022, \\ -0.4103) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, \boldsymbol{z}_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} \hline(-1.4983,-0.0303, \\ 0.0877) \end{gathered}$ | $\begin{gathered} \hline(-1.9887,-0.1471, \\ 7.3279) \end{gathered}$ | $\begin{gathered} \hline(-1.4932, \quad 0.0392, \\ 0.1637) \end{gathered}$ | $\begin{gathered} (-1.4878,-0.0238, \\ 0.4896) \end{gathered}$ | $\begin{gathered} (-1.4308,-0.0933, \\ 0.2569) \end{gathered}$ |
| $\epsilon_{\text {cc, } 3 \mathrm{D}}$ | 1.4139 | 5.0867 | 1.2900 | 1.6173 | 3.1105 |
| $\epsilon_{c c, 2 D}$ | 1.3744 | 0.7276 | 1.2888 | 1.5669 | 3.0833 |
| $\epsilon_{O C, 3 D}$ | 1.5173 | 6.6367 | 1.5161 | 1.5124 | 3.0814 |
| $\epsilon_{o c .2 D}$ | 1.5147 | 2.0011 | 1.5073 | 1.5124 | 3.0706 |
| Time for CC (Sec) | 0.0462 | 0.0462 | 0.0474 | 0.0455 | 0.0452 |
| Time for OC (Sec) | 26.6654 | 21.1501 | 23.5461 | 23.4298 | 29.4686 |



Figure 7.8: Circular Geometry Source Locations Estimated by CC and OC at 4 kHz Outdoor using RevoLabs system, (a) The $x, y$ coordinates of estimated source Locations, (b) The $z$ coordinate of the estimated source locations.

### 7.2.3 Rhombus Geometry Experiments and Results

In this section we discuss the results for the Rhombus geometry obtained using the RevoLabs wireless microphone system. We are using the geometry with the source locations discussed in Section 5.2.1.

There are several experimental scenarios as was shown in Fig. 7.2. The results are organized with respect to the sampling rate and follow next.

## Results for the 8 kHz Case

Table 7.5 shows the results we obtained for the case of 8 kHz . Using the results from Table 7.5 we plot the $x, y$ coordinates of the estimated source locations in Fig. 7.9a while Fig. 7.9b plots the bargraph for the $z$-coordinate of the estimated source locations along with the actual source locations.


Figure 7.9: Rhombus Geometry Source Locations Estimated by CC and OC at 8 kHz Outdoor using RevoLabs system, (a) The $x, y$ coordinates of estimated source Locations, (b) The $z$ coordinate of the estimated source locations.

Table 7.5: Rhombus Outdoor results using RevoLabs at 8 kHz . Fast Machine was used.

| Source Location | ( $2 \mathrm{r}, 0, \mathrm{~h}$ ) | ( $2 \mathrm{r}, \mathbf{0}, 2 \mathrm{~h}$ ) | $\begin{aligned} & \left(2 r \cos 45^{\circ},\right. \\ & \left.2 r \sin 45^{\circ}, 2 h\right) \end{aligned}$ | $\begin{aligned} & \left(2 r \cos 75^{\circ},\right. \\ & \left.2 r \sin 75^{\circ}, h\right) \end{aligned}$ | $\begin{aligned} & \left(2 r \cos 88^{\circ},\right. \\ & \left.2 r \sin 88^{\circ}, h\right) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Value | ( $3,0,0.5$ ) | $(3,0,1)$ | (2.12, 2.12, 1.00) | (0.77, 2.89, 0.5) | (0.10, 2.99, 0.5) |
| Description | On the line passing through micl $\left(a_{1}\right)$ and center of the array at height of 0.5 m | On the line passing through micl $\left(a_{1}\right)$ and center of the array at height of 1 m | In-between mic1 $\left(a_{1}\right)$ and $2\left(a_{2}\right)$ outside the circumference on which mics lye. | At angle of $75^{\circ}$ between micl $\left(a_{1}\right)$ and $2\left(a_{2}\right)$ | At angle of $88^{\circ}$ between mic1 $\left(a_{1}\right)$ and $2\left(a_{2}\right)$ |
| Exact TDs $\left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right)$ | $\left.\begin{array}{ll} (-0.0045, & 0.0009 \\ 0.0043, & 0, \\ 0 \end{array}\right)$ | $\begin{array}{cc} (-0.0047, \quad 0.0007, \\ 0.0040,-0.0002, \\ -0.0005) \end{array}$ | $\begin{array}{cc} (-0.0026, & -0.0026, \\ 0.0031, & 0.0007, \\ -0.0005) \end{array}$ | $\begin{array}{cc} (-0.0002, & -0.0042 \\ 0.0019, & 0.0013 \\ 0) \end{array}$ | $\begin{array}{cc} (0.0008, & -0.0045 \\ 0.0011, & 0.0013 \\ 0) \end{array}$ |
| $\begin{aligned} & T D E_{C C} \\ & \left(\tau_{10}^{c c}, \tau_{20}^{c c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{array}{cc} (-0.0039, & 0.0006 \\ 0.0049, & 0.0005 \\ 0.0007) \end{array}$ | $\begin{array}{cc} \hline(-0.0018, & 0.0001, \\ 0.0035, & 0.0009 \\ -0.0009) \end{array}$ | $\begin{array}{cc} \hline(0.0032, & -0.0014, \\ -0.0024, & 0.0025, \\ 0.0015) \end{array}$ | $\begin{gathered} \hline(0.0008, \\ 0.0 .0011, \\ 0.0045, \quad 0.0050 \\ 0.0015) \end{gathered}$ | $\begin{array}{cc} \hline(0.0039, & 0.0001, \\ 0.0036, & 0.0040, \\ 0.0024) \end{array}$ |
| $\begin{aligned} & T D E_{o c} \\ & \left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c}, \tau_{40}^{o c}\right) \end{aligned}$ | $\begin{array}{cc} \hline(-0.0041, & 0.0013, \\ 0.0054, & 0.0011, \\ 0.0014) \end{array}$ | $\begin{array}{cc} \hline(-0.0038, & 0.0003, \\ 0.0038, & 0.0001, \\ -0.0003) \end{array}$ | $\begin{array}{cc} \hline(-0.0020, & -0.0016, \\ 0.0030, & 0.0019, \\ -0.0047) \end{array}$ | $\begin{gathered} \hline(0.0003, \\ 0.0 .0004, \\ 0.0020) \end{gathered}$ | $\begin{array}{cc} \hline(0.0015, & 0.0004, \\ 0.0018, & 0.0020, \\ 0.0009) \end{array}$ |
| $\begin{aligned} & X_{C c} \\ & \left(x_{s}^{c c}, y_{s}^{c c}, z_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (1.4432, \quad 0.5489, \\ 0.1431) \end{gathered}$ | $\begin{gathered} \hline(0.8066, \quad 0.6000, \\ 0.7603) \end{gathered}$ | $\begin{gathered} (0.6966,-0.1342, \\ 1.3825) \end{gathered}$ | $\begin{gathered} (0.2166, \quad 0.5760 \\ 0.7554) \end{gathered}$ | $\begin{gathered} (-0.0419,0.9498, \\ -0.0743) \end{gathered}$ |
| $\begin{aligned} & X_{O C} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (2.5922, \quad 0.4034, \\ -0.8218) \end{gathered}$ | $\begin{gathered} (2.2121, \quad 0.4030 \\ 0.7716) \end{gathered}$ | $\begin{gathered} (0.6110, \quad 0.9208 \\ 0.7297) \end{gathered}$ | $\begin{gathered} (-0.7522,-1.4986, \\ 5.1090) \end{gathered}$ | $\begin{gathered} (0.0536, \quad 0.8116 \\ 0.0479) \end{gathered}$ |
| $\epsilon_{c c \_3 D}$ | 1.6888 | 2.2866 | 2.6933 | 2.3930 | 2.1242 |
| $\epsilon_{\text {cc_ } 2 \mathrm{D}}$ | 1.6507 | 2.2740 | 2.6660 | 2.3793 | 2.0451 |
| $\epsilon_{O C+3 D}$ | 1.4409 | 0.9139 | 1.9464 | 6.5436 | 2.2253 |
| $\epsilon_{\text {OC_2 }}$ | 0.5736 | 0.8849 | 1.9275 | 4.6451 | 2.1789 |
| Time for CC (Sec) | 0.0372 | 0.0376 | 0.0372 | 0.0374 | 0.0373 |
| Time for OC (Sec) | 56.8121 | 49.8612 | 54.3802 | 48.8363 | 48.1199 |

## Results for the 4 kHz Case

Table 7.6 shows the results we obtained for the case of 4 kHz . Using the results from Table 7.6 we plot the $x, y$ coordinates of the estimated source locations in Fig. 7.10a while Fig. 7.10b plots the bargraph for the $z$-coordinate of the estimated source locations along with the actual source locations.

Table 7.6: Rhombus Outdoor results using RevoLabs at 4kHz. Slow Machine was used.

| Source Location | ( $2 \mathrm{r}, \mathbf{0}, \mathrm{h}$ ) | ( $2 \mathrm{r}, \mathbf{0 , 2 h ) ~}$ | $\begin{aligned} & \left(2 r \cos 45^{\circ},\right. \\ & \left.2 r \sin 45^{\circ}, 2 h\right) \end{aligned}$ | $\begin{aligned} & \left(2 r \cos 75^{\circ},\right. \\ & \left.2 r \sin 75^{\circ}, h\right) \end{aligned}$ | $\begin{aligned} & \left(2 r \cos 88^{\circ},\right. \\ & \left.2 r \sin 88^{\circ}, h\right) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Value | $(3,0,0.5)$ | $(3,0,1)$ | (2.12, 2.12, 1.00) | (0.77, 2.89, 0.5) | (0.10, 2.99, 0.5) |
| Description | On the line passing through mic1 $\left(a_{1}\right)$ and center of the array at height of 0.5 m | On the line passing through mic1 $\left(a_{1}\right)$ and center of the array at height of 1 m | In-between mic1 $\left(a_{1}\right)$ and $2\left(a_{2}\right)$ outside the circumference on which mics lye. | At angle of $75^{\circ}$ between mic $1\left(a_{1}\right)$ and $2\left(a_{2}\right)$ | At angle of $88^{\circ}$ between mic $1\left(a_{1}\right)$ and $2\left(a_{2}\right)$ |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | $\left.\begin{array}{cc} (-0.0045, & 0.0009, \\ 0.0043, & 0, \end{array}\right)$ | $\begin{array}{cc} (-0.0047, & 0.0007, \\ 0.0040, & -0.0002, \\ -0.0005) \end{array}$ | $\begin{array}{cc} (-0.0026, & -0.0026, \\ 0.0031, & 0.0007, \\ -0.0005) \end{array}$ | $\begin{gathered} (-0.0002, \quad-0.0042, \\ 0.0019, \quad 0.0013, \quad 0) \end{gathered}$ | $\begin{array}{cc} (0.0008, & -0.0045, \\ 0.0011, & 0.0013, \\ 0) \end{array}$ |
| $\begin{aligned} & T D E_{c c} \\ & \left(\tau_{10}^{\tau c}, \tau_{20}^{c c}, \tau_{30}^{c c},,_{40}^{c c}\right) \end{aligned}$ | $\begin{gathered} (-0.0032, \quad 0.0045, \\ 0.0065,0.0030 \\ 0.0022) \end{gathered}$ | $\begin{array}{cc} \hline(-0.0013, & 0.0050, \\ 0.0067, & 0.0035, \\ 0.0018) \end{array}$ | $\begin{array}{cc} (-0.0032, & -0.1645, \\ -0.0015, & 0.0008, \\ 0.0015) \end{array}$ | $\begin{array}{cc} \hline(0.0045, & -0.0010, \\ 0.0045, & 0.0037, \\ 0.0015) \end{array}$ | $\begin{array}{cc} \hline(0.0027, & -0.0003, \\ 0.0037, & 0.0040, \\ 0.0013) \end{array}$ |
| $\begin{aligned} & T D E_{o c} \\ & \left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c},,_{40}^{o c}\right) \end{aligned}$ | $\begin{array}{cc} \hline(-0.0005, & 0.0010, \\ 0.0022, & 0.0013, \\ 0.0020) \end{array}$ | $\begin{array}{cc} \hline(-0.0045, & -0.0003, \\ -0.0010, & -0.0018, \\ -0.0010) \end{array}$ | $(0.0010$, 0.0020, <br> 0.0013, 0.0008, <br> $0.0013)$  | $\begin{array}{cc} \hline(0.0015, & -0.0003, \\ 0.0027, & 0.0018, \\ 0.0005) \end{array}$ | $\begin{array}{cc} \hline(-0.0025, & -0.0003, \\ -0.0013, & -0.0025, \\ -0.0037) \end{array}$ |
| $\begin{aligned} & X_{c c} \\ & \left(x_{s}^{c c}, y_{s}^{c c}, z_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (0.2340, \quad 0.2875, \\ 0.2877) \end{gathered}$ | $\begin{gathered} (0.3801,0.2485, \\ 0.6474) \end{gathered}$ | $\begin{gathered} (5.4664,14.6437, \\ 5.3962) \end{gathered}$ | (0, 0.7082, 0.3440) | $\begin{gathered} (0.1391,0.8598, \\ 0.3126) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (-1.7069,0.4012, \\ 4.8467) \end{gathered}$ | $\begin{gathered} (-0.5855,0.7196, \\ 0.2520) \end{gathered}$ | $\begin{gathered} (0.1301,-0.6510, \\ -1.4182) \end{gathered}$ | $\begin{gathered} (0.2525,0.8673, \\ 0.2308) \end{gathered}$ | $\begin{gathered} (-0.0305,0.5173, \\ 1.0128) \end{gathered}$ |
| $\epsilon_{c c, 3 D}$ | 2.7890 | 2.6552 | 13.6882 | 2.3189 | 2.1388 |
| $\epsilon_{c c, 2 D}$ | 2.7809 | 2.6317 | 12.9631 | 2.3137 | 2.1305 |
| $\epsilon_{O C, 3 D}$ | 6.4195 | 3.7327 | 4.1816 | 2.1052 | 2.5287 |
| $\epsilon_{O C-2 D}$ | 4.7239 | 3.6570 | 3.4115 | 2.0879 | 2.4762 |
| Time for CC (Sec) | 0.0506 | 0.0522 | 0.0456 | 0.0452 | 0.0450 |
| Time for OC(Sec) | 25.4932 | 24.1869 | 23.6965 | 23.7874 | 24.1993 |



Figure 7.10: Rhombus Geometry Source Locations Estimated by CC and OC at 4 kHz Outdoor using RevoLabs system, (a) The $x, y$ coordinates of estimated source Locations, (b) The $z$-coordinate of the estimated source locations.

### 7.2.4 Observation for RevoLabs Outdoor Experiments

Looking at the results in subsections 7.2.1 to 7.2.3 we can find the numerical facts about the results. We present these numerical facts in subsection 7.2.4 and then based on these numerical facts we deduce the observations and present them in subsection 7.2.4

## Numerical Facts

1. In outdoor experiments using RevoLabs system the CC produces more accurate results than OC for the Pyramid Geometry. $80 \%$ of the time the CC produce more accurate results for the Pyramid geometry by a factor of at least 1.21 than CC i.e. CC 3D-MSE $\left(\epsilon_{C C \_3 D}\right)$ is at least 1.21 times less than OC 3D-MSE $\left(\epsilon_{O C \_3 D}\right)$ at 8 kHz . For 4 kHz case $100 \%$ of the times CC produce more accurate results than OC by a minimum factor of 1.63 . The runtime for OC is at least 37 times more than the runtime for CC .
2. For Circular geometry 8 kHz case, the OC produces more accurate results than CC $100 \%$ of the times by a minimum factor of 1.003 while for the 4 kHz case CC produces better results than OC by a minimum factor of $1.00760 \%$ of the times. The minimum runtime for OC is at least 230 times more than CC runtime.
3. For Rhombus geometry 8 kHz case, the OC produces more accurate results than CC $60 \%$ of the times by a minimum factor of 1.16 while for the 4 kHz case CC produces better results than OC by a minimum factor of $1.1860 \%$
of the times. The minimum runtime for OC is at least 230 times more than CC runtime.

## Outdoor RevoLabs Experiments Observations

Looking at the numerical facts in subsection 7.2 .4 we can make the following observations for the experiments carried out outdoor using RevoLabs system.

1. The CC is producing the best results for Pyramid geometry in outdoor using RevoLabs system with a minimum 3D-MSE $\epsilon_{C C-3 D}$ of 0.4215 m and minimum 2D error of 0.08 m .
2. The OC produces better results for the Circular in 8 kHz case $100 \%$ of the times and for the Pyramid $60 \%$ of the times respectively. However for the case of 4 kHz CC produces better results than OC $60 \%$ of the times. It means the OC efficiency decreases as the sampling rate is decreased.
3. Overall the CC produces better results $66 \%$ of the times in all the outdoor cases using RevoLabs and the OC is better only $34 \%$ of the times. The accuracy of CC in outdoors is due to the fact that because of the absence of reverberations and nearby reflections there is no signal shape distortion among the signals received at all microphones. Thus their correlation with each other is better than the indoor environment.

### 7.3 Results using VocoPro System

In this section we discuss in detail the outdoor experiments we conducted using the VocoPro system and their results and analysis. As there are three different geometries and each geometry has different scenarios we need to organize the discussion in subsections. Subsections 7.3.1, 7.3.2 and 7.3.3 discuss the results for Pyramid, Circular and Rhombus geometries in outdoor environment using the VocoPro System. The observations are given in subsection 7.3.4. It is to be noted that we used a loaded toy gunshot for all the experiments using the VocoPro system.

### 7.3.1 Pyramid Geometry Experiments and Results

In this section we discuss the results for the Pyramid geometry obtained using the VocoPro wireless microphone system. We are using the geometry with the source locations discussed in Section 5.2.1. Fig. 7.11 shows the experimental setup of the Pyramid geometry using the VocoPro system. Like for the case of the RevoLabs system we conducted all outdoor experiments during night.


Figure 7.11: Pyramid geometry using VocoPro system outdoor

There are several experimental scenarios as was shown in Fig. 7.2. The results are organized with respect to the sampling rate and follow next.

## Results for the 8 kHz Case

Table 7.7 shows the results we obtained for the case of 8 kHz . Using the results from Table 7.7 we plot the $x, y$ coordinates of the estimated source locations in Fig. 7.12a while Fig. 7.12b plots the bargraph for the $z$-coordinate of the estimated source locations along with the actual source locations.

Table 7.7: Pyramid Outdoor results using VocoPro at 8 kHz . Fast Machine was used.

| Source Location | $\begin{gathered} \left(\cos 60^{\circ}, \sin 60^{\circ}, 0.5\right) \\ =(0.5,0.866,0.5) \end{gathered}$ | $\begin{gathered} \left(2 \cos 60^{\circ}, 2 \sin 60^{\circ}, 0\right)=(1, \\ 1.73,0) \end{gathered}$ | $\begin{gathered} \left(2.5 \cos 60^{\circ}, 2.5 \sin 60^{\circ}, 0\right)= \\ (1.25,2.16,0) \end{gathered}$ | (0,0,1) | (2.5, 0, 0) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Description | In-between $a_{1}$ and $a_{2}$ inside the array at height of 0.5 m at $60^{\circ}$ | In-between $a_{1} \& a_{2}$ on the circle inscribing the array. | In-between $a_{1} \& a_{2}$, outside the array | Above the center of the array | Along the line (outside array) passing through $a_{1}$ and center of the array |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | $\begin{array}{cc} (0.0020, & 0.0020, \\ 0.0057, & -0.0003) \end{array}$ | $\begin{array}{cc} (0, & 0.0000, \\ 0.0059, & 0.0004) \end{array}$ | $\begin{array}{cl} (-0.0006, & -0.0006, \\ 0.0059, & 0.0003) \end{array}$ | $\begin{array}{lr} (0.0036, & 0.0036, \\ 0.0036, & -0.0021) \end{array}$ | $(-0.0059$, 0.0041, <br> 0.0041, $0.0003)$ |
| $\begin{aligned} & T D E_{c c} \\ & \left(\tau_{10}^{c c}, \tau_{20}^{c c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{array}{lr} (0.0013, & 0.0008, \\ 0.0053, & -0.0005) \end{array}$ | $\begin{array}{cc} (-0.0008, & -0.0005, \\ 0.0049, & -0.0008) \end{array}$ | $\begin{array}{cc} (0.0008, & -0.0005, \\ 0.0057, & 0.0001) \end{array}$ | (0.0084, 0.0018, $-0.0075, \quad 0)$ | $\begin{array}{cc} (-0.0171, & 0.0031, \\ 0.0041, & 0.0001) \end{array}$ |
| TDE ${ }_{\text {oc }}$ <br> $\left(\tau_{10}^{o c}, v_{20}^{o c},,_{30}^{o c}, \tau_{40}^{o c}\right)$ | $\begin{array}{cc} (0.0049, & 0.0006, \\ 0.0019, & 0.0011) \end{array}$ | $\begin{array}{cc} (0.0049, & 0.0006, \\ 0.0019, & 0.0011) \end{array}$ | $\begin{array}{cc} (0.0037, & 0.0015, \\ 0.0084, & 0) \end{array}$ | $\begin{array}{cc} (0.0005, & 0.0008, \\ 0.0014, & 0.0005) \end{array}$ | $\begin{array}{cc} (-0.0029, & 0.0046, \\ 0.0022, & 0.0009) \end{array}$ |
| $\begin{aligned} & X_{c c} \\ & \left(x_{s}^{c}, y_{s}^{c c}, z_{s}^{c c}\right. \end{aligned}$ | $\begin{gathered} (0.5855,1.2181, \\ 0.7503) \end{gathered}$ | $\begin{gathered} (1.4575,2.3525, \\ 1.6308) \end{gathered}$ | $\begin{gathered} (0.7311,1.7629, \\ 0.2418) \end{gathered}$ | $\begin{gathered} (1.3204,2.3928, \\ 0.3600) \end{gathered}$ | $\begin{gathered} (3.3621,0.4863, \\ 0.1390) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{\left.x_{s}^{c}, y_{s}^{o c}, z_{s}^{o c}\right)}\right. \end{aligned}$ | $\begin{gathered} (-1.1449, \quad 0.2765, \\ -9.5272) \end{gathered}$ | $\begin{gathered} (-1.1449, \\ -0.6420) \\ -2.65, \end{gathered}$ | $\begin{gathered} (0.4683,1.2863, \\ 0.3600) \end{gathered}$ | $\begin{gathered} (0.4525, \\ -1.1609) \\ -3964, \end{gathered}$ | $\begin{gathered} (2.2483,-0.9849, \\ -0.9906) \end{gathered}$ |
| $\epsilon_{\text {cc, } 3 D}$ | 0.4404 | 1.8045 | 0.6967 | 2.8069 | 0.9995 |
| $\epsilon_{\text {cc-2 }}{ }^{\text {d }}$ | 0.3624 | 0.7725 | 0.6534 | 2.7329 | 0.9898 |
| $\epsilon_{\text {OC } 3 D}$ | 2.0875 | 2.6694 | 1.2264 | 2.2431 | 1.4194 |
| $\epsilon_{O C, 2 D}$ | 1.7474 | 2.5910 | 1.1724 | 0.6015 | 1.0165 |
| Time for CC (Sec) | 0.0350 | 0.0349 | 0.0338 | 0.0348 | 0.0352 |
| Time for OC (Sec) | 36.9219 | 40.2083 | 45.6537 | 38.7338 | 39.9076 |



Figure 7.12: Pyramid Geometry Source Locations Estimated by CC and OC at 8 kHz Outdoor using VocoPro system, (a) The $x, y$ coordinates of estimated source Locations, (b) The $z$ coordinate of the estimated source locations.

## Results for the 4 kHz Case

Table 7.8 shows the results we obtained for the case of 4 kHz . Using the results from Table 7.8 we plot the $x, y$ coordinates of the estimated source locations in Fig. 7.13a while Fig. 7.13b plots the bargraph for the $z$-coordinate of the estimated source locations along with the actual source locations.

Table 7.8: Pyramid Outdoor results using VocoPro at 4kHz. Slow Machine was used.

| Source Location | $\begin{gathered} \left(\cos 60^{\circ}, \sin 60^{\circ}, 0.5\right) \\ =(0.5,0.866,0.5) \end{gathered}$ | $\begin{gathered} \left(2 \cos 60^{\circ}, 2 \sin 60^{\circ}, 0\right)=(1, \\ 1.73,0) \end{gathered}$ | $\begin{gathered} \left(2.5 \cos 60^{\circ}, 2.5 \sin 60^{\circ}, 0\right)= \\ (1.25,2.16,0) \end{gathered}$ | $(0,0,1)$ | $(2.5,0,0)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Description | In-between $a_{1}$ and $a_{2}$ inside the array at height of 0.5 m at $60^{\circ}$ | In-between $a_{1} \& a_{2}$ on the circle inscribing the array. | In-between $a_{1} \& a_{2}$, outside the array | Above the center of the array | Along the line (outside array) passing through $a_{1}$ and center of the array |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | $\begin{array}{lr} (0.0020, & 0.0020, \\ 0.0057, & -0.0003) \end{array}$ | $\begin{array}{cc} (0, & 0.0000 \\ 0.0059, & 0.0004) \end{array}$ | $\begin{array}{cc} (-0.0006, & -0.0006, \\ 0.0059, & 0.0003) \end{array}$ | $\begin{array}{lr} (0.0036, & 0.0036, \\ 0.0036, & -0.0021) \end{array}$ | $\begin{array}{cc} (-0.0059, & 0.0041, \\ 0.0041, & 0.0003) \end{array}$ |
| $\begin{aligned} & T D E_{C c} \\ & \left(\tau_{10}^{c c}, \tau_{20}^{c c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{array}{ll} (0.0010, & 0.0035, \\ 0.0035, & 0.0013) \end{array}$ | $\begin{array}{cc} (-0.0015, & -0.0003 \\ 0.0047, & 0.0013) \end{array}$ | $\begin{array}{cc} (-0.0005, & -0.0018 \\ 0.0057, & 0.0008) \end{array}$ | $\begin{array}{cc} (-0.0035, & 0.0018, \\ 0.0018, & 0) \end{array}$ | $\begin{array}{cc} (-0.0018, & 0.0027, \\ 0.0070, & 0.0005) \end{array}$ |
| $\begin{aligned} & T D E_{o c} \\ & \left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c}, \tau_{40}^{o c}\right) \end{aligned}$ | $\begin{array}{cc} (0.0035, & 0.0027, \\ 0.0040, & 0.0011) \end{array}$ | $\begin{array}{ll} (0.0093, & 0.0032, \\ 0.0005, & 0.0030) \end{array}$ | $\begin{array}{cc} (0.0030, & 0.0022, \\ 0.0040, & 0.0013) \end{array}$ | $\begin{array}{lr} (0.0050, & 0.0020, \\ 0.0003, & -0.0035) \end{array}$ | $\begin{array}{cc} (0.0057, & 0.0035, \\ 0.0022, & 0) \end{array}$ |
| $\begin{aligned} & X_{c c} \\ & \left(x_{s}^{c c}, y_{s}^{c c}, z_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (0.6882, \quad 0, \\ -0.7972) \end{gathered}$ | $\begin{gathered} (2.0755,2.5704, \\ -2.4056) \end{gathered}$ | $\begin{gathered} (1.2712,2.9115, \\ -0.8451) \end{gathered}$ | (0.1250, $0,0.3600)$ | $\begin{gathered} (1.1979,1.0981 \\ 0.1150) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(\boldsymbol{x}_{s}^{o c}, y_{s}^{o c}, \boldsymbol{Z}_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (-0.0310,0.2905, \\ -0.3281) \end{gathered}$ | $\begin{gathered} (-1.6407,-0.1903 \\ -0.4890) \end{gathered}$ | $\begin{gathered} (0.0428, \\ -0.4277 \\ -0.6147) \end{gathered}$ | $\begin{gathered} (-1.2015,-0.3556, \\ 2.2524) \end{gathered}$ | $\begin{gathered} (-0.7225,-0.2268, \\ 0.3600) \end{gathered}$ |
| $\epsilon_{c c}$ 3 ${ }^{\text {d }}$ | 1.5710 | 2.7659 | 1.1311 | 0.6521 | 1.7072 |
| $\epsilon_{c c}$ 2D | 0.8862 | 1.3649 | 0.7518 | 0.1250 | 1.7033 |
| $\epsilon_{O C}$ 3D | 1.1397 | 3.3015 | 2.1991 | 1.7716 | 3.2505 |
| $\epsilon_{O C_{-} 2 D}$ | 0.7830 | 3.2651 | 2.1114 | 1.2530 | 3.2305 |
| Time for CC (Sec) | 0.0496 | 0.0428 | 0.0433 | 0.0424 | 0.0435 |
| Time for OC (Sec) | 22.3595 | 21.4214 | 23.2750 | 21.1390 | 20.1693 |



Figure 7.13: Pyramid Geometry Source Locations Estimated by CC and OC at 4 kHz Outdoor using VocoPro system, (a) The $x, y$ coordinates of estimated source Locations, (b) The $z$ coordinate of the estimated source locations.

### 7.3.2 Circular Geometry Experiments and Results

In this section we discuss the results for the Circular geometry obtained using the
VocoPro wireless microphone system. We are using the geometry with the source locations discussed in Section 5.2.1. Fig. 7.14 shows the experimental setup of the Circular geometry using the VocoPro system.


Figure 7.14: Circular geometry using VocoPro system outdoor

There are several experimental scenarios as was shown in Fig. 7.2. The results are organized with respect to the sampling rate and follow next.

## Results for the 8 kHz Case

Table 7.9 shows the results we obtained for the case of 8 kHz . Using the results from Table 7.9 we plot the $x, y$ coordinates of the estimated source locations in Fig. 7.15a while Fig. 7.15b plots the bargraph for the $z$-coordinate of the estimated source locations along with the actual source locations.

Table 7.9: Circular Outdoor results using VocoPro at 8 kHz . Fast Machine was used.

| Source Location | $\begin{gathered} \left(r \cos 30^{\circ}-r,\right. \\ \left.r \sin 30^{\circ}, 0\right) \end{gathered}$ | $\left(r \cos 30^{\circ}-r, r \sin 30^{\circ}, 1\right)$ | $(-2 r, 0,0)$ | $(-2 r, 0,0.5)$ | (-3r, 0, 0) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Value | (-0.2 0.7500, 0) | (-0.2, 0.7500, 1) | $(-3,0,0)$ | $(-3,0,0.5)$ | $(-4.5,0,0)$ |
| Description | In-between mic0 and $1\left(a_{0}, a_{1}\right)$ on the circumference at height of 0 m | In-between mic0 and 1 ( $a_{0}, a_{1}$ ) on the circumference at height of 1 m | At mic3 $\left(a_{3}\right)$ with zero height | At mic3 $\left(a_{3}\right)$ with 0.5 m height | Along the line (outside array) passing through $\operatorname{mic} 3\left(a_{3}\right)$ and center of the array at height 0m |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | $\begin{array}{cc} (0.0004, & 0.0040, \\ 0.0064, & 0.0062, \\ 0.0041) \end{array}$ | $\begin{array}{cc} (-0.0010, & 0.0032, \\ 0.0049, & 0.0053 \\ 0.0027) \end{array}$ | $\begin{gathered} (-0.0010,-0.0044, \\ -0.0074,-0.0044, \\ -0.0010) \end{gathered}$ | $\begin{gathered} (-0.0013,-0.0043, \\ -0.0089,-0.0043, \\ -0.0013) \\ \hline \end{gathered}$ | (0.0015, -0.0056, -0.0086, -0.0056, -0.0015) |
| $\begin{aligned} & T D E_{c c} \\ & \left(\tau_{10}^{c}, \tau_{20}^{\tau c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{array}{cc} (0.0019, & 0.0044, \\ 0.0073, & 0.0060, \\ 0.0060) \end{array}$ | $\begin{array}{cc} \hline(0.0019, & 0.0020, \\ 0.0064, & 0.0081, \\ 0.0081) \end{array}$ | $\begin{array}{cc} \hline(0.0036, & 0.0025, \\ 0.0046, & 0.0003, \\ 0.0003) \end{array}$ | $\begin{array}{cc} \hline(0.0045, & 0.0016, \\ 0.0047, & 0.0035, \\ 0.0035) \end{array}$ | $\begin{array}{cc} (-0.0009, & -0.0044, \\ -0.0075, & -0.0044, \\ -0.0044) \end{array}$ |
| $\begin{aligned} & T D E_{o c} \\ & \left(\tau_{10}^{o o}, \tau_{20}^{o c}, \tau_{30}^{o c}, \tau_{40}^{o c}\right) \end{aligned}$ | $\begin{array}{cc} (-0.0009, & 0.0004) \\ 0.0035, & 0.0018 \\ 0.0018) \end{array}$ | $\begin{array}{cc} \hline(-0.0014, & 0.0037, \\ -0.0003, & 0.0005, \\ 0.0005) \end{array}$ | $\begin{array}{cc} \hline(0.0080, & 0.0004, \\ 0.0047, & 0.0011, \\ 0.0011) \end{array}$ | $\begin{array}{cc} \hline(-0.0014, & 0.0275, \\ 0.0025, & 0.0018, \\ 0.0018) \end{array}$ | $\begin{gathered} \hline(0.0011, \\ -0.00015, \\ -0.0153) \end{gathered}$ |
| $\begin{aligned} & X_{C c} \\ & \left(x_{s}^{c c}, y_{s}^{c c}, X_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (-0.9180, \quad 0.4587, \\ -0.7832) \end{gathered}$ | $\begin{gathered} (-1.6279,0.2979, \\ 0.6046) \end{gathered}$ | $\begin{gathered} (-1.6998,0.2942, \\ 0.9796) \end{gathered}$ | $\begin{gathered} (-1.5159,-0.0180, \\ -0.1070) \end{gathered}$ | $\begin{gathered} (-1.6632,-0.0749, \\ 0.3504) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (-1.5437, \quad-0.0977, \\ 0.0817) \end{gathered}$ | $\begin{gathered} (-1.4843,-0.1294 \\ 0.0833) \end{gathered}$ | $\begin{gathered} (-1.6858,-0.0987, \\ 0.8628) \end{gathered}$ | $\begin{gathered} (-2.2585,-1.5381, \\ 0.5801) \end{gathered}$ | $\begin{gathered} (-2.1311,-0.5037, \\ -0.3527) \end{gathered}$ |
| $\epsilon_{c c, 3 D}$ | 1.1017 | 1.5491 | 1.6543 | 1.6035 | 2.8593 |
| $\epsilon_{c c .2 D}$ | 0.7748 | 1.4978 | 1.3331 | 1.4842 | 2.8378 |
| $\epsilon_{\text {OC. } 3 \mathrm{D}}$ | 1.5909 | 1.8064 | 1.5752 | 1.7094 | 2.4474 |
| $\epsilon_{\text {OC.2D }}$ | 1.5888 | 1.5565 | 1.3180 | 1.7076 | 2.4218 |
| Time for CC (Sec) | 0.1320 | 0.1410 | 0.1944 | 0.1324 | 0.1387 |
| Time for OC (Sec) | 47.1253 | 48.7252 | 55.1040 | 48.7728 | 47.0343 |



Figure 7.15: Circular Geometry Source Locations Estimated by CC and OC at 8 kHz Outdoor using VocoPro system, (a) The $x, y$ coordinates of estimated source Locations, (b) The $z$ coordinate of the estimated source locations.

## Results for the 4 kHz Case

Table 7.10 shows the results we obtained for the case of 4 kHz . Using the results from Table 7.10 we plot the $x, y$ coordinates of the estimated source locations in Fig. 7.16a while Fig. 7.16b plots the bargraph for the $z$-coordinate of the estimated source locations along with the actual source locations.

Table 7.10: Circular Outdoor results using VocoPro at 4 kHz . Slow Machine was used.

| Source Location | $\begin{gathered} \left(r \cos 30^{\circ}-r\right. \\ \left.r \sin 30^{\circ}, 0\right) \end{gathered}$ | $\left(r \cos 30^{\circ}-r, r \sin 30^{\circ}, 1\right)$ | $(-2 r, 0,0)$ | $(-2 r, 0,0.5)$ | (-3r, 0, 0) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Value | (-0.2 0.7500, 0) | $(-0.2,0.7500,1)$ | $(-3,0,0)$ | $(-3,0,0.5)$ | $(-4.5,0,0)$ |
| Description | In-between mic0 and $1\left(a_{0}, a_{1}\right)$ on the circumference at height of 0 m | In-between mic0 and 1 ( $a_{0}, a_{1}$ ) on the circumference at height of 1 m | At mic3 $\left(a_{3}\right)$ with zero height | At mic3 $\left(a_{3}\right)$ with 0.5 m height | Along the line (outside array) passing through mic3 $\left(a_{3}\right)$ and center of the array at height 0m |
| $\begin{gathered} \text { Exact TDs } \\ \left(\tau_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | $\begin{array}{cc} (0.0004, & 0.0040 \\ 0.0064, & 0.0062 \\ 0.0041) \end{array}$ | $\begin{array}{cc} (-0.0010, & 0.0032, \\ 0.0049, & 0.0053 \\ 0.0027) \end{array}$ | $\begin{array}{cc} (-0.0010, & -0.0044, \\ -0.0074, & -0.0044, \\ -0.0010) \end{array}$ | $\begin{array}{cc} (-0.0013, & -0.0043, \\ -0.0089, & -0.0043, \\ -0.0013) \end{array}$ | $\begin{gathered} (-0.0015, \\ -0.0086,-0.0056, \\ -0.0015) \end{gathered}$ |
| $\begin{aligned} & T D E_{C C} \\ & \left(\tau_{10}^{c c}, \tau_{20}^{c c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{array}{cc} \hline(0.0045, & 0.0070, \\ 0.0010, & 0.0075, \\ 0.0075) \end{array}$ | $\begin{array}{cc} \hline(0.0018, & 0.0040, \\ -0.0060, & 0.0053, \\ 0.0053) \end{array}$ | $\begin{array}{cc} \hline(0.0008, & 0.0025, \\ 0.0037, & 0.0027, \\ 0.0027) \end{array}$ | $\begin{array}{cl} (0.0040, & 0.0013, \\ 0.0043, & 0, \end{array}$ | $\begin{array}{cc} \hline(0.0013, & -0.0043, \\ -0.0075, & -0.0032, \\ -0.0032) \end{array}$ |
| $\begin{aligned} & T D E_{o c} \\ & \left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c}, \tau_{40}^{o c}\right) \end{aligned}$ | $\begin{array}{cc} \hline(0.0035, & 0.0015, \\ 0.0475, & 0.0022, \\ 0.0022) \\ \hline \end{array}$ | $\left.\begin{array}{cc} (-0.0020, & 0.0260, \\ 0, & -0.0022, \end{array}-0.0022\right)$ | $\begin{array}{cc} \hline(-0.0698, & 0.0013, \\ 0.0013, & 0.0018, \\ 0.0018) \\ \hline \end{array}$ | $\begin{array}{cc} \hline(0.0010, & 0.0040, \\ 0.0290, & 0.0020, \\ 0.0020) \end{array}$ | $\begin{array}{cc} \hline(-0.0005, & 0.0022, \\ -0.0032, & -0.0027, \\ -0.0027) \\ \hline \end{array}$ |
| $\begin{aligned} & X_{c c} \\ & \left(x_{s}^{c c}, y_{s}^{c c}, z_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (-1.5237,0.1922, \\ 0.9104) \end{gathered}$ | $\begin{gathered} (-0.9517,0.3933, \\ -0.6665) \end{gathered}$ | $\begin{gathered} (-1.4031,0.0528, \\ 0.1280) \end{gathered}$ | $\begin{gathered} (-1.5644,0.1223, \\ 0.4735) \end{gathered}$ | $\begin{gathered} (-1.6256,-0.2305, \\ -0.4376) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (-3.9176,0.2430, \\ 12.9866) \end{gathered}$ | $\begin{gathered} (-1.3257, \quad 0.8619, \\ -3.8709) \end{gathered}$ | $\begin{gathered} (0.6988,1.7034 \\ -1.6937) \end{gathered}$ | $\begin{gathered} (-3.7990,0.2737, \\ 2.1873) \end{gathered}$ | $\begin{gathered} (-1.3191,0.1965, \\ -0.1867) \end{gathered}$ |
| $\epsilon_{c c \_3 D}$ | 1.7006 | 1.8627 | 1.6029 | 1.4410 | 2.9166 |
| $\epsilon_{\text {cc_ } 2 \mathrm{D}}$ | 1.4364 | 0.8320 | 1.5977 | 1.4408 | 2.8836 |
| $\epsilon_{O C}$ [3D | 13.5177 | 5.0005 | 4.4104 | 1.8869 | 3.1924 |
| $\epsilon_{\text {OC_2D }}$ | 3.7520 | 1.1313 | 4.0722 | 0.8445 | 3.1870 |
| Time for CC (Sec) | 0.0533 | 0.0468 | 0.0454 | 0.0448 | 0.0464 |
| Time for OC (Sec) | 25.2732 | 24.8884 | 26.7861 | 24.1191 | 30.3864 |



Figure 7.16: Circular Geometry Source Locations Estimated by CC and OC at 4 kHz Outdoor using VocoPro system, (a) The $x, y$ coordinates of estimated source Locations, (b) The $z$ coordinate of the estimated source locations.

### 7.3.3 Rhombus Geometry Experiments and Results

In this section we discuss the results for the Rhombus geometry obtained using the VocoPro wireless microphone system. We are using the geometry with the source locations discussed in Section 5.2.1.Fig. 7.17 shows the experimental setup of the Rhombus geometry using the VocoPro system.


Figure 7.17: Rhombus geometry using VocoPro system outdoor

There are several experimental scenarios as was shown in Fig. 7.2. The results are organized with respect to the sampling rate and follow next.

## Results for the 8 kHz Case

Table 7.11 shows the results we obtained for the case of 8 kHz . Using the results from Table 7.11 we plot the $x, y$ coordinates of the estimated source locations in Fig. 7.18a while Fig. 7.18b plots the bargraph for the $z$-coordinate of the estimated source locations along with the actual source locations.

Table 7.11: Rhombus Outdoor results using VocoPro at 8 kHz . Fast Machine was used.

| Source Location | ( $2 \mathrm{r}, \mathbf{0}, \mathrm{h}$ ) | ( $\mathbf{r}, \mathbf{0}, 2 \mathrm{~h}$ ) | $\begin{aligned} & \left(2 r \cos 45^{\circ}\right. \\ & \left.2 r \sin 45^{\circ}, 2 h\right) \end{aligned}$ | $\begin{aligned} & \left(2 r \cos 75^{\circ},\right. \\ & \left.2 r \sin 75^{\circ}, h\right) \end{aligned}$ | $\begin{aligned} & \left(2 r \cos 88^{\circ},\right. \\ & \left.2 r \sin 88^{\circ}, h\right) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Value | (3, 0, 0.5) | $(3,0,1)$ | (2.12, 2.12, 1.00) | (0.77, 2.89, 0.5) | (0.10, 2.99, 0.5) |
| Description | On the line passing through mic1 $\left(a_{1}\right)$ and center of the array at height of 0.5 m | On the line passing through micl $\left(a_{1}\right)$ and center of the array at height of 1 m | In-between mic1 ( $a_{1}$ ) and $2\left(a_{2}\right)$ outside the circumference on which mics lye. | At angle of $75^{\circ}$ between $\operatorname{mic} 1\left(a_{1}\right)$ and $2\left(a_{2}\right)$ | At angle of $88^{\circ}$ between mic1 $\left(a_{1}\right)$ and $2\left(a_{2}\right)$ |
| $\begin{gathered} \text { Exact TDs } \\ \left(\boldsymbol{\tau}_{10}, \boldsymbol{\tau}_{20}, \boldsymbol{\tau}_{30}, \boldsymbol{\tau}_{40}\right) \end{gathered}$ | $\begin{array}{lll} (-0.0045, & 0.0009, \\ 0.0043, & 0, & 0) \end{array}$ | $\begin{array}{cc} (-0.0047, & 0.0007, \\ 0.0040, & -0.0002, \\ -0.0005) \end{array}$ | $\begin{array}{cc} (-0.0026, & -0.0026, \\ 0.0031, & 0.0007, \\ -0.0005) \end{array}$ | $\begin{array}{cc} (-0.0002, & -0.0042, \\ 0.0019, & 0.0013 \\ 0) \end{array}$ | $\begin{array}{cc} (0.0008, & -0.0045 \\ 0.0011, & 0.0013, \\ 0) \end{array}$ |
| $\begin{aligned} & T D E_{c c} \\ & \left(\tau_{10}^{c}, \tau_{20}^{c c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{array}{cc} (-0.0027, & 0.0014, \\ 0.0045, & 0.0021, \\ 0.0015) \end{array}$ | $\begin{array}{cc} \hline(-0.0035, & 0.0016, \\ -0.0063, & 0.0016, \\ 0.0019) \end{array}$ | $\begin{array}{cc} (-0.0011, & -0.0009, \\ -0.0029, & 0.0021, \\ 0) \end{array}$ | $\begin{array}{cc} \hline(-0.0001, & -0.0044, \\ 0.0018, & 0.0034, \\ -0.0001) \end{array}$ | $\begin{array}{cc} (0.0008, & -0.0045, \\ 0.0011, & 0.0043 \\ 0) \end{array}$ |
| $\operatorname{TVE}_{\left(\boldsymbol{\tau}_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c}, \tau_{40}^{o c}\right)}$ | $\begin{array}{cc} \hline(0.0027, & -0.0025, \\ -0.0011, & -0.0026, \\ -0.0035) \end{array}$ | $\begin{array}{cc} \hline(-0.0018, & 0.0006, \\ 0.0021, & 0.0016, \\ 0.0020) \end{array}$ | $\begin{array}{cc} \hline(0.0061, & -0.0039, \\ -0.0024, & 0.0030, \\ 0.0070) \end{array}$ | $\begin{array}{cc} \hline(0.0025, & -0.0030, \\ -0.0032, & 0.0045, \\ 0.0055) \end{array}$ | $\begin{array}{cc} (0.0011, & 0.0008, \\ 0.0041, & 0.0021, \\ 0) \end{array}$ |
| $\begin{aligned} & X_{c c} \\ & \left(x_{s}^{c c}, y_{s}^{c c}, \boldsymbol{Z}_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (0.3173, \quad 0.5778, \\ 0.4839) \end{gathered}$ | $\begin{gathered} (0.4477, \quad 0.5407, \\ 0.2471) \end{gathered}$ | $\begin{gathered} (0.2694, \quad 0.3486, \\ 0.7903) \end{gathered}$ | $\begin{gathered} (0.0164,-0.2205, \\ 0.8254) \end{gathered}$ | $\begin{gathered} (-0.0197,-0.9391, \\ 1.0127) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (-0.5406,0.6279, \\ 1.3058) \end{gathered}$ | $\begin{gathered} (-0.9036,0.3346, \\ 2.0920) \end{gathered}$ | $\begin{gathered} (0.9698,-1.6825, \\ 1.6196) \end{gathered}$ | $\begin{gathered} (0.9241,-0.8295, \\ 1.2376) \end{gathered}$ | $\begin{gathered} (0.4525, \quad 0.6390, \\ 0.4500) \end{gathered}$ |
| $\epsilon_{c c, 3 D}$ | 2.7443 | 2.7154 | 2.5704 | 3.2170 | 3.9642 |
| $\epsilon_{c c, 2 D}$ | 2.7443 | 2.6089 | 2.5618 | 3.2005 | 3.9309 |
| $\epsilon_{O C .3}{ }_{\text {c }}$ | 3.6850 | 4.0673 | 4.0206 | 3.7950 | 2.3778 |
| $\epsilon_{O C .2 D}$ | 3.5958 | 3.9179 | 3.9726 | 3.7226 | 2.3773 |
| Time for CC (Sec) | 0.0373 | 0.0377 | 0.0375 | 0.0377 | 0.0375 |
| Time for OC (Sec) | 44.7077 | 49.3199 | 48.9376 | 46.3949 | 50.2759 |



Figure 7.18: Rhombus Geometry Source Locations Estimated by CC and OC at 8 kHz Outdoor using VocoPro system, (a) The $x, y$ coordinates of estimated source Locations, (b) The $z$ coordinate of the estimated source locations.

## Results for the 4 kHz Case

Table 7.12 shows the results we obtained for the case of 4 kHz . Using the results from Table 7.12 we plot the $x, y$ coordinates of the estimated source locations in Fig. 7.19a while Fig. 7.19b plots the bargraph for the $z$-coordinate of the estimated source locations along with the actual source locations.

Table 7.12: Rhombus Outdoor results using the VocoPro at 4kHz. Slow Machine was used.

| Source Location | ( $2 \mathrm{r}, \mathbf{0}, \mathrm{h}$ ) | ( $2 \mathrm{r}, \mathbf{0}, 2 \mathrm{~h}$ ) | $\begin{aligned} & \left(2 r \cos 45^{\circ},\right. \\ & \left.2 r \sin 45^{\circ}, 2 h\right) \end{aligned}$ | $\begin{aligned} & \left(2 r \cos 75^{\circ},\right. \\ & \left.2 r \sin 75^{\circ}, h\right) \end{aligned}$ | $\begin{aligned} & \left(2 r \cos 88^{\circ},\right. \\ & \left.2 r \sin 88^{\circ}, h\right) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Value | $(3,0,0.5)$ | $(3,0,1)$ | (2.12, 2.12, 1.00) | (0.77, 2.89, 0.5) | (0.10, 2.99, 0.5) |
| Description | On the line passing through micl $\left(a_{1}\right)$ and center of the array at height of 0.5 m | On the line passing through micl $\left(a_{1}\right)$ and center of the array at height of 1 m | In-between mic1 $\left(a_{1}\right)$ and $2\left(a_{2}\right)$ outside the circumference on which mics lye. | At angle of $75^{\circ}$ between $\operatorname{mic} 1\left(a_{1}\right)$ and $2\left(a_{2}\right)$ | At angle of $88^{\circ}$ between mic1 $\left(a_{1}\right)$ and $2\left(a_{2}\right)$ |
| $\begin{gathered} \text { Exact TDs } \\ \left(\boldsymbol{\tau}_{10}, \tau_{20}, \tau_{30}, \tau_{40}\right) \end{gathered}$ | $\left.\begin{array}{ll} (-0.0045, & 0.0009, \\ 0.0043, & 0, \end{array} 0\right)$ | $\begin{array}{cc} (-0.0047, & 0.0007, \\ 0.0040, & -0.0002, \\ -0.0005) \end{array}$ | $\begin{array}{cc} (-0.0026, & -0.0026, \\ 0.0031, & 0.0007, \\ -0.0005) \end{array}$ | $\begin{array}{cc} (-0.0002, & -0.0042 \\ 0.0019, & 0.0013 \\ 0) \end{array}$ | $\begin{array}{cc} (0.0008, & -0.0045, \\ 0.0011, & 0.0013 \\ 0) \end{array}$ |
| $\begin{aligned} & T D E_{c c} \\ & \left(\tau_{10}^{c c}, \tau_{20}^{c c}, \tau_{30}^{c c}, \tau_{40}^{c c}\right) \end{aligned}$ | $\begin{array}{ll} (-0.0032, & 0.0020 \\ 0.0040, & 0.0013,0) \end{array}$ | $\begin{array}{cc} (-0.0022, & 0.0005, \\ 0.0035, & 0.0003, \\ -0.0005) \end{array}$ | $\begin{array}{cc} \hline(-0.0018, & -0.0010, \\ -0.0083, & 0.0015, \\ 0) \end{array}$ | $\begin{array}{cc} (-0.0003, & -0.0045, \\ 0.0018, & 0.0040, \\ -0.0008) \end{array}$ | $\begin{array}{cc} \hline(0.0008, & -0.0260, \\ -0.0103, & 0.0043, \\ 0) \end{array}$ |
| TDE ${ }_{\text {oc }}$ $\left(\tau_{10}^{o c}, \tau_{20}^{o c}, \tau_{30}^{o c}, \tau_{40}^{o c}\right)$ | $\begin{gathered} \hline(0.0270, \\ 0.0010, \quad 0.0283, \\ -0.0003) \end{gathered}$ | $\begin{array}{cc} \hline(0.0260, & 0.0255, \\ 0.0008, & 0.0262, \\ 0.0010) \end{array}$ | $\begin{array}{cc} (-0.0098, & -0.0082, \\ 0.0018, & 0.0005 \\ -0.0035) \end{array}$ | $\begin{array}{cc} \hline(-0.0053, & -0.0020, \\ -0.0018, & -0.0013, \\ -0.0047) \end{array}$ | $\begin{array}{cc} (-0.0015, & -0.0015, \\ -0.0010, & 0.0008 \\ 0.0020) \end{array}$ |
| $\begin{aligned} & X_{C c} \\ & \left(x_{s}^{c c}, y_{s}^{c c}, z_{s}^{c c}\right) \end{aligned}$ | $\begin{gathered} (0.3033,0.3796, \\ 0.6088) \end{gathered}$ | $\begin{gathered} (1.2047,0.4033, \\ 0.7482) \end{gathered}$ | $\begin{gathered} (0.8028,0.7836, \\ 0.4722) \end{gathered}$ | $\begin{gathered} (-0.0561,-0.5727, \\ 0.7866) \end{gathered}$ | $\begin{gathered} (-1.6690,-5.8132, \\ -1.0062) \end{gathered}$ |
| $\begin{aligned} & X_{o c} \\ & \left(x_{s}^{o c}, y_{s}^{o c}, Z_{s}^{o c}\right) \end{aligned}$ | $\begin{gathered} (-0.5057, \quad 0.9780, \\ 0.6664) \end{gathered}$ | $\begin{gathered} (-0.2734,0.8594, \\ 2.3395) \end{gathered}$ | $\begin{gathered} (0.5888,1.1176, \\ 1.6950) \end{gathered}$ | $\begin{gathered} (-0.5587,0.5970, \\ -0.4409) \end{gathered}$ | $\begin{gathered} (-0.0996,-0.0778, \\ 1.1513) \end{gathered}$ |
| $\epsilon_{\text {cc_ } 3 D}$ | 2.7255 | 1.8572 | 1.9492 | 3.5714 | 9.1046 |
| $\epsilon_{c c \_ \text {2D }}$ | 2.7233 | 1.8401 | 1.8764 | 3.5599 | 8.9792 |
| $\epsilon_{O C}$ [3D | 3.6434 | 3.6397 | 1.9576 | 2.8123 | 3.1425 |
| $\epsilon_{O C-2 D}$ | 3.6396 | 3.3843 | 1.8301 | 2.6502 | 3.0743 |
| Time for CC (Sec) | 0.0446 | 0.0466 | 0.0450 | 0.0448 | 0.0440 |
| Time for OC (Sec) | 24.2646 | 29.0311 | 27.3696 | 25.5099 | 32.8518 |



Figure 7.19: Rhombus Geometry Source Locations Estimated by CC and OC at 4 kHz Outdoor using VocoPro system, (a) The $x, y$ coordinates of estimated source Locations, (b) The $z$ coordinate of the estimated source locations.

### 7.3.4 Observations for the VocoPro Outdoor Experiments

Looking at the results in subsections 7.3 .1 to 7.3 .3 we can find the numerical facts about the results of VocoPro system outdoor. We present these numerical facts in subsection 7.3.4 and then based on these numerical facts we deduce the observations and present them in subsection 7.3.4

## Numerical Facts

1. In outdoor experiments using VocoPro system the CC produces more accurate results than OC for all the geometries.
2. $80 \%$ of the time the CC produces more accurate results for the Pyramid geometry by a factor of at least 1.21 than CC i.e. CC 3D-MSE $\left(\epsilon_{C C \_3 D}\right)$ is
at least 1.21 times less than OC 3D-MSE $\left(\epsilon_{O C \_3 D}\right)$ at 8 kHz . For 4 kHz case $80 \%$ of the times CC produce more accurate results than OC by a minimum factor of 1.19. The runtime for CC is at least 460 times less than the runtime for OC.
3. For Circular geometry 8 kHz case, the CC produces more accurate results than OC $60 \%$ of the times by a minimum factor of 1.066 while for the 4 kHz case CC produces better results than OC by a minimum factor of $1.3100 \%$ of the times. The minimum runtime for OC is at least 340 times more than CC runtime.
4. For Rhombus geometry 8 kHz case, the CC produces more accurate results than CC $80 \%$ of the times by a minimum factor of 1.18 while for the 4 kHz case CC produces better results than OC by a minimum factor of $1.00560 \%$ of the times. The minimum runtime for OC is at least 540 times more than CC runtime.
5. In specific cases, the OC produces better results than CC. However, on average CC is better than OC accuracy-wise in outdoor using VocoPro system. Especially the runtime for CC is much less than the OC runtime.

## Outdoor VocoPro Experiments Observations

Looking at the numerical facts in subsection 7.3 .4 we can make the following observations for the experiments carried out outdoor using VocoPro system.

1. The CC is producing the best results for all the geometries in outdoor using

VocoPro system with a minimum 3D-MSE $\epsilon_{C C_{3} D}$ of 1.85 m for Rhombus, 1.10 m for Circular and 0.44 m for Pyramid Geometry. The reason of which is that there is less distortion in the signal shape because of the absence of reverberations and nearby reflections which is favorable for the CC algorithm.
2. The Pyramid geometry is still the best accuracy-wise and the Rhombus the worst geometry among all the three geometries.
3. Overall, about $75 \%$ of the times CC produces more accurate results than OC in outdoor environment using VocoPro system.
4. Overall, the minimum runtime of the OC in any case of the outdoor experiments using VocoPro system is 340 times more than the CC runtime.
5. Overall, the CC algorithm is better both accuracy-wise and runtime than OC in outdoor using VocoPro system.

### 7.4 An Abstract Observation of All Experimental Results

In this section we provide an abstract observation of all the experiments that we conducted both indoor and outdoor in a tabular form. Table 7.13 summarizes the observations for the indoor experiments while Table 7.14 summarizes those of the outdoor experiments. An entry of OC (or CC) in both Table 7.13 and Table 7.14
means that OC (or CC ) is better accuracy-wise than the CC (or OC) algorithm. The runtime for CC is always less than half a second while that for OC is at least ten seconds.

Table 7.13: Abstract Observations (accuracy-wise) of Indoor Results

|  | RevoLabs System |  | VocoPro System |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Less-Reverberant | More-Reverberant | Less-Reverberant | More-Reverberant |
| Pyramid | OC | OC |  |  |
| Circular | OC | OC | CC | CC |
| Rhombus | OC | OC | OC |  |

Table 7.14: Abstract Observations (accuracy-wise) of Outdoor Results

|  | RevoLabs System | VocoPro System |
| :---: | :---: | :---: |
| Pyramid | CC | CC |
| Circular | oc | CC |
| Rhombus | CC | cc |

### 7.5 Conclusions

This chapter provided in detail the results and analysis of the experiments carried out in an outdoor environment using RevoLabs and VocoPro wireless microphone
systems. The RevoLabs system provides better accuracy than the VocoPro system. It was oberved that outdoor experiments produce better results than the indoor. Especially, the CC method provides better accuracy than the OC algorithm. The OC algorithm produces good results in moderately reverberant environment such as the center of the hall than CC. But in dense reverberant environments its accuracy deteriorates, though its accuracy is still better than the CC.

The results of the VocoPro system are better in an outdoor environment than indoor. The limited sensitivity of the VocoPro system limits its applicability for less loud events such as a clap or unloaded gunshot while RevoLabs system provides better results in such situations.

## CHAPTER 8

## CONCLUSIONS AND FUTURE

## WORK

### 8.1 Conclusions

This thesis focused on the implementation of an impulsive acoustic source localization (IASL) system. The system was implemented using the classical CrossCorrelation (CC) method and a new time delay estimation algorithm called Orthogonal Clustering (OC). To properly analyze, assess and compare the results of these two methods the system implementation was carried out for several practical scenarios.

The system was implemented both for an indoor and outdoor environment in three-dimensions (3D) using two different wireless microphone systems. An attempt was also made to implement the system on a Wireless Sensor Network (WSN) but due to hardware limitations and issues (discussed in chapter 4) we
could not proceed with the implementation. Two different sampling rates of 4 kHz and 8 kHz were considered for system implementation to check the performance of both of the algorithms at reduced rates. Considering the situation that may arise in practical applications in an indoor environment, experiments were performed both in a less and a more reverberant environment to analyze the effects of the environmental factors on the performance of the system.

Through several experimentations it was found that the Pyramid geometry was producing the best results, accuracy-wise, among all the presented geometries in all the indoor and outdoor scenarios except few special cases. The Rhombus geometry was producing the most erroneous results among the presented geometries. The RevoLabs microphone system was producing relatively accurate results than the VocoPro both in the indoor and outdoor environments.

The OC algorithm was producing relatively accurate results than CC in a reverberant environment. However, it was observed that the OC accuracy deteriorates as the reverberation increases. The CC algorithm outperforms, on the average, the OC algorithm in an outdoor environment. Furthermore, the runtime for OC algorithm is much higher than the CC algorithm. In all the scenarios the CC runtime was always less than a second while the minimum runtime observed for the OC algorithm was more than 10 seconds.

### 8.2 Future Work and Recommendation

Possible future directions are as follows.

1. The OC algorithm was compared only with the CC algorithm. A comparison is desired between OC and the algorithms developed for indoor environments like Adaptive Eigenvalue Decomposition.
2. Simple Least Squares (LS) method was used to estimate the source locations from over-determined system which does not take into account the uncertainty of the design matrix. Advanced mathematical tools such as Total Least Squares (TLS) can be applied to reduce the effect of uncertainty of both of the design and observation matrix on the estimation process.
3. Furthermore, the OC algorithm uses Minimum Mean Square Estimation(MMSE) or Maximum A Priori (MAP) estimation methods for the channel impulse response (CIR) estimation. TLS can be applied at this stage of the algorithm to reduce the effect of uncertainty of the design matrix on the results.
4. No post processing was carried out on the signals captured through microphones. A noise reducing process may be desired to apply to the acquired signals to improve the results.

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