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# **Factors Influencing Labor Share: Automation, Task Innovation, and Elasticity of Substitution**

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1 October 2023

Online at <https://mpra.ub.uni-muenchen.de/118730/>  
MPRA Paper No. 118730, posted 12 Oct 2023 08:29 UTC

# Factors Influencing Labor Share: Automation, Task Innovation, and Elasticity of Substitution \* †

Last updated: October 1, 2023

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## Abstract

This paper explores the underlying factors contributing to the recent decline in labor share, focusing specifically on the roles of automation and the development of new tasks that are exclusive to humans. First, our paper strengthens the argument that automation has a negative impact on labor share. Second, we are the first to empirically estimate the influence of new human-exclusive tasks on labor share. Our findings suggest that the positive impact of human-exclusive tasks dominates the negative impact brought about by automation. Third, we find that the elasticity of substitution between labor and capital is less than one, offering a coherent framework for predicting how various factors —capital price, robot price, and wages— impact labor share. We identify two distinct mechanisms through which robots negatively affect labor share: automation and a reduction in the price of robots. Our general equilibrium model predicts that the latter will gain increasing importance in the future as robots become more prevalent. Lastly, we estimate the elasticity of substitution between tasks to be one, empirically validating an assumption that many existing studies have made.

(JEL D24, D33, E24, E25, J23, O33, O57)

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\*We extend our heartfelt thanks to Giovanni Peri for his ongoing guidance and invaluable support. We are also deeply grateful to Òscar Jordà, Athanasios Geromichalos, Colin Cameron, Takuya Ura, Kathryn Russ, and Mark Siegler for their invaluable advice and insights throughout the course of this project.

†Replication data and code and the most recent version of paper:

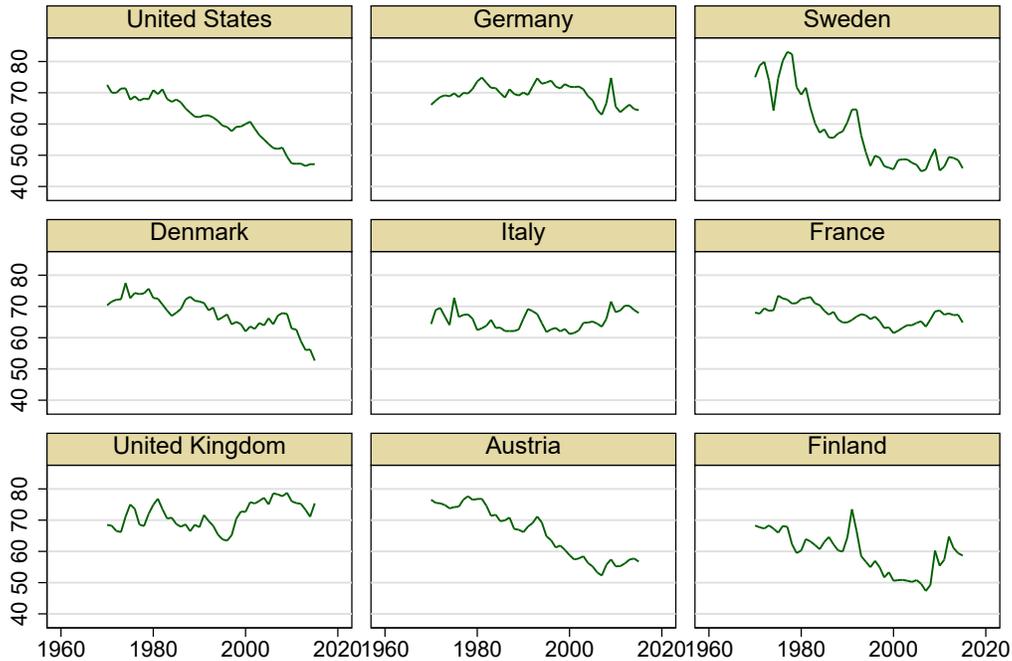
<https://github.com/jayjeo/public/tree/main/Laborshare>

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# 1 Introduction

Karabarbounis and Neiman (2014) and Autor et al. (2020) have noted that the global labor share has followed a declining trend since the early 1980s, with an average decrease of about five percentage points. Figure 1, based on data compiled by Gutiérrez and Piton (2020), compares the labor shares in the manufacturing sector between the USA and the eight EU nations that we studied. While the USA, Sweden, Denmark, and Austria have witnessed significant declines, other countries report comparatively slight decreases. This discrepancy indicates that global labor share trends exhibit considerable heterogeneity, further underscoring our aim to investigate variations across countries and sectors to better understand this decline.<sup>1</sup>

Figure 1: Labor shares



Although the precise cause of this decline is still a topic of debate, advancements in automation emerge as a possible key driver. The urgency of addressing the diminishing labor share intensifies with the accelerated growth in automation and artificial intelligence technologies. For instance, Boston Dynamics has unveiled Atlas, a humanoid robot with impressive speed and capabilities.<sup>2</sup> The recent debut of Chat-GPT 4, which

<sup>1</sup>In this context, our study aligns with Graetz and Michaels (2018), which assesses seventeen EU countries, although their focus is predominantly on productivity growth rather than the decrease in labor share.

<sup>2</sup><https://youtu.be/-e1.QhJ1EhQ>

astoundingly achieved a 10% ranking in the United States bar exam, further underscores the rapid evolution of AI systems.<sup>3</sup>

The influence of automation on labor share remains a prominent topic in active research. Several studies such as those by Acemoglu and Restrepo (2020), Acemoglu et al. (2020), Dauth et al. (2021), and Martinez (2018) suggest that automation reduces labor share. In contrast, findings from research like De Vries et al. (2020) and Gregory et al. (2016) propose that automation amplifies labor share. Moreover, studies by Humlum (2019) and Hubmer and Restrepo (2021) explore the diverse impacts of automation on various population groups and industry sectors.

Yet, another factor potentially promoting labor share is the ‘emergence of new tasks’ –innovative tasks beyond the capabilities of robots. Autor (2015) contends that the sustained relevance of human labor in the future will largely depend on the pace at which the ‘emergence of new tasks’ outstrips the advancement of automation. Despite its significance, the effect of the emergence of new tasks on labor share is still relatively underexplored. Our primary objective is to assess the impacts of the interaction between the rise of automation and the emergence of new tasks on the labor share.

Automation and the emergence of new tasks are not the only factors contributing to changes in labor share. In literature, many other reasons have been meticulously examined, especially using causality techniques. However, fewer studies attempt to measure multiple reasons within a unified framework (Bergholt et al., 2022).<sup>4</sup> Grossman and Oberfield (2022) highlighted the importance of utilizing general equilibrium analysis, stating: “Many authors present different sides of the same coin ... Even if the various mechanisms are all active, it becomes difficult to gauge what part of the effect estimated in one study has already been accounted for elsewhere”. To address this challenge, we adopt a general equilibrium model, an approach that represents a contribution to the existing literature. The study most akin to ours is that of Acemoglu and Restrepo (2022). They too utilize a general equilibrium model, though their main focus is on wage inequality rather than the decline in labor share.

Our analysis incorporates five potential determinants within our general equilibrium model: automation, the emergence of new tasks, capital price, robot price, and wages.<sup>5</sup> Our most significant contribution lies in the empirical examination of the im-

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<sup>3</sup><https://youtu.be/EunbKbPV2C0>

<sup>4</sup>Bergholt et al. (2022) points out that “while a large literature has discussed each of these four explanations in isolation, an empirical analysis including all of them in the context of the same model is lacking. Our aim is to fill this gap.”

<sup>5</sup>In this context, the research by Bergholt et al. (2022) closely aligns with our study. They examine rising markups, increased worker bargaining power, a declining investment price, and escalating automation as

pact of the emergence of new tasks on labor share. To the best of our knowledge, we are the first to empirically investigate this relationship. Our findings indicate that the emergence of new tasks serves as an effective counterbalance to the negative effects of automation on labor share. This is particularly the case in the USA, where the advent of new tasks holds substantial importance.

We find that the elasticity of substitution *between labor and non-robot capital* is below one. This allows us to make coherent predictions about the directional impact of three price-related factors on labor share —non-robot capital price, robot price, and wages— based solidly on our general equilibrium model. First, the correlation between the non-robot capital price and the labor share is negative (gross complement). Second, an increase in real wages positively affects labor share. Third, a decline in robot prices negatively impacts labor share. These directional trends are confirmed by our regression results.

This finding underscores the negative effect of robotics on labor share through two key mechanisms. First, advancements in robotic capabilities lead to the displacement of tasks traditionally carried out by humans, thereby reducing labor share. Second, a decrease in the cost of robots, even without improvements in functionality, also contributes to a lower labor share. Our general equilibrium model predicts that as robots become more prevalent, the impact of this second mechanism —referred to as the robot price channel— will intensify. This implies that as automation expands in the future, our regression coefficient for robot price is likely to increase in magnitude and become statistically significant.

Our results enrich the existing literature by emphasizing the importance of the elasticity of substitution *between labor and capital*, which has also been highlighted by recent studies like those of Martinez (2018), Oberfield and Raval (2021), and Zhang (2023). Our work resonates with studies like Glover and Short (2020), which also report the elasticity below one and stress the importance of bias correction when estimating this. To address omitted variable bias, we regress factors such as automation, the emergence of new tasks, wages, robot prices, and capital prices on labor share, indicating the significance of automation and the emergence new tasks. Our findings are consistent with Glover and Short (2020).

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factors contributing to the falling labor share. Although their methodology, which employs time series techniques (Structural VAR with sign restrictions) and focuses exclusively on the USA, differs from ours, their findings are in line with our results. They identify automation as a principal driver of the reduction in labor share. Interestingly, they conclude that a declining capital price does not contribute to the decrease in labor share.

In contrast, our findings do not support the hypothesis of Karabarbounis and Neiman (2014), who claim that falling capital prices account for half of the recent labor share decline. For their argument to hold, the elasticity would have to be greater than one (gross substitute). Likewise, Piketty and Zucman (2014) suggests potential for gross substitutability, a position we do not support.

Looking forward, as automation becomes increasingly prevalent, both our model and empirical data suggest that the elasticity of substitution *between labor and non-robot capital* will approach, but not surpass, one. This indicates that the influence of the labor price channel on increasing labor share is likely to diminish in the future.

We further contribute to the existing literature by empirically showing that the elasticity of substitution *between different tasks* is near one. Many studies, such as those by Autor (2013) and Acemoglu and Autor (2011), have relied on the Cobb-Douglas production function for tasks, implicitly assuming this elasticity approaches one. Additionally, the static version of Acemoglu and Restrepo (2018) builds on Acemoglu and Autor (2011) by allowing for a general elasticity of substitution between tasks. Meanwhile, Acemoglu and Restrepo (2019) adopts a CES form and uses an elasticity value of 0.8 in their empirical work, a figure derived from Oberfield and Raval (2021)'s estimation of the elasticity *between labor and capital*.

In the following section, we present our general equilibrium model, while Section 3 details the datasets we used. Section 4 conducts the regression analysis, and Section 5 performs various accountings to ascertain which mechanism predominantly explains labor share decline across different countries and industries. Finally, Section 6 provides our concluding remarks. Separately in our Online Appendix,<sup>6</sup> we discuss why the Superstar-firm hypothesis proposed by Autor et al. (2020) falls short of fully explaining the global decline in labor share, even though it adequately accounts for the situation in the USA.

## 2 Model

Acemoglu and Restrepo (2018) have offered a formal model that outlines how labor share is influenced by ‘automation’ and the ‘emergence of new tasks.’ We have refined our model based on their static version. Our key contribution is the distinction we make between robots and other capital equipment, a distinction their model does not delineate. Acemoglu and Restrepo (2020) found that advancements in robotics negatively impact wages and employment. Conversely, they discovered that other forms of capital

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<sup>6</sup>[https://github.com/jayjeo/public/blob/main/Laborshare/Online\\_Appendix.pdf](https://github.com/jayjeo/public/blob/main/Laborshare/Online_Appendix.pdf)

Figure 2: Examples of Robot

(a) Robot



(b) Not robot<sup>8</sup>



positively impact these variables. This distinction emphasizes that ‘robots’ and ‘capital’ can carry different implications for labor demand.

We adhere to the definition of a robot as specified by ISO standard 8373:2012, which describes it as an “automatically controlled, reprogrammable, multipurpose manipulator programmable in three or more axes.”<sup>7</sup> The International Federation of Robotics (IFR) also strictly adheres to this definition (Müller, 2022). We source our robot data from the IFR.

In Figure 2, Panel (a) depicts a robot. However, Panel (b) is not robot because this milling machine does not come with any type of hook-up to have it run automatically. Therefore, it is neither reprogrammable nor automatically controlled. Additionally, it cannot be considered multipurpose, as it is designed solely for milling. Also, it does not operate on three or more axes. This example underscores the narrow definition of a robot.

We define ‘automation’ as the enhancement of robots’ capabilities, which allows them to perform tasks that were previously unachievable. Meanwhile, we define the ‘emergence of new tasks’ as new tasks that human-workers are expected to perform because those are beyond the capabilities of robots. For instance, according to ONET, the job description for Urban and Regional Planners (SOC 19-3051) expanded from 19 responsibilities in 2019 to include tasks related to statistics and data management. Pre-

<sup>7</sup>Acemoglu and Restrepo (2020) also defines robots in a manner consistent with this description: “fully autonomous machines that do not need a human operator and can be programmed to perform several manual tasks ... This definition excludes other types of equipment.”

<sup>8</sup>Vertical milling machine by [harborfreight](#)

viously, their responsibilities included: (1) holding public meetings with officials and scientists, (2) advising planning officials on project feasibility and cost-effectiveness, and (3) mediating community disputes. One year later, their scope of tasks widened to incorporate: (1) preparing reports using statistics, (2) developing and maintaining maps and databases, and (3) researching, compiling, analyzing, and organizing information. This serves as a prototypical example of the emergence of new tasks, illustrating that individuals aspiring to become Urban and Regional Planners must now acquire skills in data handling and statistics.

Our model holds advantages over existing literature, such as Berg et al. (2018) and DeCanio (2016), which also introduced robots as a separate factor from traditional capital. Firstly, our model comprehensively incorporates factors affecting labor share, most importantly automation and the emergence of new tasks, in addition to factor prices. This allows us to quantitatively analyze the extent to which each factor affects labor share across different sectors and countries. Secondly, our model delivers in-depth interpretations regarding the substitutability between labor, capital, and robots. From the regression equations derived from the task-based model, we gain unique insights into the degree of substitutability among factors, as well as the tasks conducted by either labor or robots.

## 2.1 Environment

### 2.1.1 Firms

In the model, firms face monopolistic competition, which allows them to generate positive profits. For simplicity, we assume that the production function is the same for all firms<sup>9</sup>. Also, for brevity, we omit the time subscript.

Each firm utilizes a continuum of tasks, indexed between  $N - 1$  and  $N$ , in addition to capital, for production. As in Acemoglu and Restrepo (2018),  $N$  increases over time due to the emergence of new tasks, which can only be conducted by labor. Additionally, there is an index  $I$  that falls between  $N - 1$  and  $N$ .  $I$  is related to the possibility of automation and thus increases along with improvements in automation technology. Specifically, tasks below  $I$  in firm  $i$  can technically be conducted by either labor or robots, while tasks above  $I$  can only be performed by labor, as follows:

$$t_j(i) = m_j(i) + \gamma_j l_j(i) \quad \text{if } j \leq I \quad (1)$$

$$t_j(i) = \gamma_j l_j(i) \quad \text{if } j > I \quad (2)$$

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<sup>9</sup>Introducing heterogeneity in terms of Hicks-neutral productivity does not change our analysis.

, where  $m_j(i)$  and  $l_j(i)$  represent the number of robots and labor used for task  $j$  in firm  $i$ .  $\gamma_j$  represents the productivity of labor for task  $j$ . The productivity,  $\gamma_j$ , increases with a higher task index,  $j$ .

Tasks,  $t_j(i)$ , are aggregated using Constant Elasticity of Substitution (CES) aggregator, and both the aggregated tasks and capital are further combined using another CES function. Therefore, the production function is:

$$Y(i) = \left( T(i)^{\frac{\sigma-1}{\sigma}} + K(i)^{\frac{\sigma-1}{\sigma}} \right)^{\frac{\sigma}{\sigma-1}} \quad (3)$$

$$T(i) = \left( \int_{N-1}^N t_j(i)^{\frac{\zeta-1}{\zeta}} dj \right)^{\frac{\zeta}{\zeta-1}} \quad (4)$$

, where  $T(i)$  and  $K(i)$  represent the number of aggregated tasks and capital used for the production of the final good  $i$ , denoted as  $Y(i)$ . Meanwhile,  $\sigma$  and  $\zeta$  represent the elasticity of substitution between aggregated tasks and capital, and the elasticity of substitution between tasks, respectively.

Factor markets are assumed to be perfectly competitive. Additionally, since we focus on long-run change in labor share, it is reasonable to assume that factors are supplied elastically. For further simplicity, we assume that factors are supplied perfectly elastically at a given factor price at each period.

### 2.1.2 Households

The representative consumer consumes an aggregated continuum of final goods, with the mass of final goods assumed to be 1 for simplicity. It's also assumed that there is no disutility from the supply of labor. The utility function of the representative consumer takes the following form:

$$U = \left( \int_0^1 Y(i)^{\frac{\eta-1}{\eta}} di \right)^{\frac{\eta}{\eta-1}} \quad (5)$$

, where  $\eta$  represents the elasticity of substitution between final goods.

The representative consumer's budget constraint is as follows:

$$\int_0^1 P(i)Y(i)di = \int_0^1 \left( \int_{N-1}^N W_j l_j(i) dj + \int_{N-1}^N \psi m_j(i) dj + RK_i + \Pi_i \right) di \quad (6)$$

, where  $W_j$ ,  $\psi$ , and  $R$  represent wage for labor conducting task  $j$ , robot price, and capital price, respectively.

## 2.2 Labor Share

A step-by-step process for this section is provided in Appendix A. We set an assumption related to robot and labor productivity for simple algebra in deriving the equilibrium in the model.

**Assumption 1.**  $\psi < \frac{W_I}{\gamma_I}$

The above assumption implies that it is efficient to use a robot for task  $j$  below  $I$ . This means that whenever firms can technologically replace labor with a robot, they would want to do so.<sup>10</sup>

Based on the Assumption 1 and by solving the firm's cost minimization problem, factor demands, the price for the aggregated task, and the marginal cost of firm  $i$  are derived as follows:

$$l_j(i) = 0, \text{ if } j \leq I \quad (7)$$

$$l_j(i) = \gamma_j^{\zeta-1} \left( \frac{W_j}{P_T} \right)^{-\zeta} T(i), \text{ if } j > I \quad (8)$$

$$m_j(i) = \left( \frac{\psi}{P_T} \right)^{-\zeta} T(i), \text{ if } j \leq I \quad (9)$$

$$m_j(i) = 0, \text{ if } j > I \quad (10)$$

$$T(i) = \left( \frac{P_T}{MC(i)} \right)^{-\sigma} Y(i) \quad (11)$$

$$K(i) = \left( \frac{R}{MC(i)} \right)^{-\sigma} Y(i) \quad (12)$$

$$P_T = \left[ (I - N + 1)\psi^{1-\zeta} + \int_I^N \left( \frac{W_j}{\gamma_j} \right)^{1-\zeta} dj \right]^{\frac{1}{1-\zeta}} \quad (13)$$

$$MC(i) = [P_T^{1-\sigma} + R^{1-\sigma}]^{\frac{1}{1-\sigma}} \quad (14)$$

$$W_j l_j(i) = \left( \frac{W_j}{\gamma_j} \right)^{1-\zeta} \cdot P_T^\zeta \cdot T_i \quad (15)$$

, where  $P_T$  and  $MC_i$  represent the price for the aggregated task and marginal cost of firm  $i$ , respectively.

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<sup>10</sup>This is reasonable considering that robot prices have significantly decreased while wages have steadily increased.

Based on Equations (7) to (14), labor share is derived:

$$S_L = \frac{\eta - 1}{\eta} \frac{\int_I^N \left( \frac{W_j}{\gamma_j} \right)^{1-\zeta} dj}{P_T^{1-\zeta}} \frac{P_T^{1-\sigma}}{P_T^{1-\sigma} + R^{1-\sigma}} \quad (16)$$

$$, \text{ where } P_T \equiv \left[ (I - N + 1)\psi^{1-\zeta} + \int_I^N \left( \frac{W_j}{\gamma_j} \right)^{1-\zeta} dj \right]^{\frac{1}{1-\zeta}}$$

It is worth mentioning that the term,  $\frac{\eta-1}{\eta}$ , is the inverse of the firm's mark-up. Since we focus on labor income as a fraction of total factor income, we denote it as  $S_L^f$  as follows:

$$S_L^f \equiv \frac{\eta}{\eta - 1} S_L = \frac{\int_I^N \left( \frac{W_j}{\gamma_j} \right)^{1-\zeta} dj}{P_T^{1-\zeta}} \frac{P_T^{1-\sigma}}{P_T^{1-\sigma} + R^{1-\sigma}} \quad (17)$$

### 2.3 Estimating Equations

By taking the natural log of Equation (17) and then computing the total derivative of the resulting equation with respect to the exogenous variables in the model ( $I$ ,  $N$ ,  $R$ ,  $W$ , and  $\psi$ ), we obtain the following estimating equation:

$$\begin{aligned}
d \ln S_L^f = & \\
& - \left[ (1 - \zeta) + \left( -(1 - \zeta) + S_K^f(1 - \sigma) \right) \times \frac{\int_I^N \left( \frac{W_j}{\gamma_j} \right)^{1-\zeta} dj}{P_T^{1-\zeta}} \right] d \ln \gamma \\
& + \left[ \underbrace{\frac{\left( \frac{W_I}{\gamma_I} \right)^{1-\zeta}}{\int_I^N \left( \frac{W_j}{\gamma_j} \right)^{1-\zeta} dj}}_{\text{Direct loss by } dI: (-)} + \left( -(1 - \zeta) + S_K^f(1 - \sigma) \right) \times \underbrace{\frac{1}{1 - \zeta} \frac{\psi^{1-\zeta} - \left( \frac{W_I}{\gamma_I} \right)^{1-\zeta}}{P_T^{1-\zeta}}}_{\text{Change in aggregated task price by } dI: (-)} \right] dI \\
& + \left[ \underbrace{\frac{\left( \frac{W_N}{\gamma_N} \right)^{1-\zeta}}{\int_I^N \left( \frac{W_j}{\gamma_j} \right)^{1-\zeta} dj}}_{\text{Direct gain by } dN: (+)} + \left( -(1 - \zeta) + S_K^f(1 - \sigma) \right) \times \underbrace{\frac{1}{1 - \zeta} \frac{-\psi^{1-\zeta} + \left( \frac{W_N}{\gamma_N} \right)^{1-\zeta}}{P_T^{1-\zeta}}}_{\text{Change in aggregated task price by } dN: (+)/(-)} \right] dN \\
& + \left[ \underbrace{(1 - \zeta)}_{\text{Direct gain by } d \ln W: (+)} + \left( -(1 - \zeta) + S_K^f(1 - \sigma) \right) \times \underbrace{\frac{\int_I^N \left( \frac{W_j}{\gamma_j} \right)^{1-\zeta} dj}{P_T^{1-\zeta}}}_{\text{Change in aggregated task price by } d \ln W: (+)} \right] d \ln W \\
& - \left[ S_K^f(1 - \sigma) \right] d \ln R \\
& + \left[ \left( -(1 - \zeta) + S_K^f(1 - \sigma) \right) \times \underbrace{\frac{(I - N + 1)\psi^{1-\zeta}}{P_T^{1-\zeta}}}_{\text{Change in aggregated task price by } d \ln \psi: (+)} \right] d \ln \psi
\end{aligned} \tag{18}$$

, where  $W \equiv \frac{\int_I^N \left( \frac{W_j}{\gamma_j} \right)^{1-\zeta} dj}{\int_I^N W_j^{-\zeta} \gamma_j^{\zeta-1} dj}$  is the average wage, and assume  $d \ln W = d \ln W_j$  for all  $j$ . Additionally,  $d \ln \gamma$  represents the change in labor productivity. It also is assumed that  $d \ln \gamma = d \ln \gamma_j$  for all  $j$ .

The coefficients of the five explanatory variables ( $dI$ ,  $dN$ ,  $d \ln W$ ,  $d \ln R$ , and  $d \ln \psi$ ) in Equation (18) reflects not only the direct effect caused by the change in the variable, but also the general equilibrium effects that influence the labor share through changes in the price of the aggregated tasks. Changes in automation technology,  $dI$ , changes in the emergence of new tasks,  $dN$ , and changes in wage,  $d \ln W$ , directly affect the labor share.  $dI$  directly causes labor to be replaced by robots in task  $I$ , which results in a

decrease in labor share by  $\frac{\left(\frac{W_I}{\gamma_I}\right)^{1-\zeta}}{\int_I^N \left(\frac{W_j}{\gamma_j}\right)^{1-\zeta} dj}$ .<sup>11</sup> In contrast,  $dN$  and  $d \ln W$  directly increase labor share by  $\frac{\left(\frac{W_N}{\gamma_N}\right)^{1-\zeta}}{\int_I^N \left(\frac{W_j}{\gamma_j}\right)^{1-\zeta} dj}$  and  $1 - \zeta$  respectively.

All five variables affect the price of the aggregated task, which in turn influences the labor share. The impact of this price change on the labor share is multiplied by the factor  $-(1 - \zeta) + S_K^f(1 - \sigma)$ . The sign of this indirect effect hinges on the values of  $\sigma$  and  $\zeta$ . In Equation (19), the term  $-(1 - \zeta) + S_K^f(1 - \sigma)$  recurs frequently, exerting a significant impact on many coefficients.

Given that we utilize data for robot penetration, as employed in Acemoglu and Restrepo (2020) –which corresponds to  $(I - N + 1)$ – and data for the emergence of new tasks –which corresponds to  $N$  in our model– we adjust Equation (18) as follows:

$$\begin{aligned}
d \ln S_L^f = & \\
& - \left[ (1 - \zeta) + \left( -(1 - \zeta) + S_K^f(1 - \sigma) \right) S_L^T \right] d \ln \gamma \\
& + \left[ -\frac{\left(\frac{W_I}{\gamma_I}\right)^{1-\zeta}}{\int_I^N \left(\frac{W_j}{\gamma_j}\right)^{1-\zeta} dj} + \left( -(1 - \zeta) + S_K^f(1 - \sigma) \right) \frac{1}{1 - \zeta} \frac{\psi^{1-\zeta} - \left(\frac{W_I}{\gamma_I}\right)^{1-\zeta}}{P_T^{1-\zeta}} \right] d(I - N + 1) \\
& + \left( S_N^L - S_I^L \right) \frac{1}{1 - \zeta} \left[ S_M^T(1 - \zeta) + S_L^T S_K^f(1 - \sigma) \right] dN \\
& + \left[ (1 - \zeta) + \left( -(1 - \zeta) + S_K^f(1 - \sigma) \right) S_L^T \right] d \ln W \\
& - \left[ S_K^f(1 - \sigma) \right] d \ln R \\
& + \left[ \left( -(1 - \zeta) + S_K^f(1 - \sigma) \right) S_M^T \right] d \ln \psi
\end{aligned} \tag{19}$$

, where  $S_L^T \equiv \frac{\int_I^N \left(\frac{W_j}{\gamma_j}\right)^{1-\zeta} dj}{P_T^{1-\zeta}}$  and  $S_M^T \equiv \frac{(I-N+1)\psi^{1-\zeta}}{P_T^{1-\zeta}}$  represent the labor share and robot share in the aggregated tasks, respectively.  $S_N^L \equiv \frac{\left(\frac{W_N}{\gamma_N}\right)^{1-\zeta}}{\int_I^N \left(\frac{W_j}{\gamma_j}\right)^{1-\zeta} dj}$  and  $S_I^L \equiv \frac{\left(\frac{W_I}{\gamma_I}\right)^{1-\zeta}}{\int_I^N \left(\frac{W_j}{\gamma_j}\right)^{1-\zeta} dj}$  represent the share of labor income conducting task  $N$  and  $I$  out of the total labor income, respectively. Next section, we discuss the datasets used in this paper and the construction of the variables.

<sup>11</sup>This term indicates labor losses of  $\gamma(I)^{(\zeta-1)(1-\alpha)}$  in task  $I$  out of the total  $\int_I^N \gamma(j)^{(\zeta-1)(1-\alpha)} dj$

## 3 Data

### 3.1 Automation and New Tasks by Acemoglu and Restrepo (2019)

Acemoglu and Restrepo (2019) (henceforth referred to as AR) presents a tool for inferring automation and the emergence of new tasks (henceforth, ENT). This tool utilizes a relatively small set of variables: labor compensation, employee count, value-added, wage, and investment price. The AR framework enables the inference of automation and ENT.

Fundamentally, the AR framework operates under the assumption that if there is an observed *increase* in labor share (an indicator of the total income in an economy that goes to labor), it must be attributed to ENT. Conversely, if there is a *decrease*, it is attributable to automation. This principle is clearly articulated in Figure 1 of their paper.

The online appendix of the AR paper elaborates on this framework. For ease of reference, we include it in our Appendix C. Equation (AR4) represents the percentage change in labor share, which can be broken down into Equations (AR6) and (AR7). The former represents the percentage change in substitution effects, while the latter shows the percentage change in ‘task contents.’ A positive (negative) result in Equation (AR7) is interpreted as indicative of emerging new tasks (automation). Given that the percentage change in substitution effects (Equation AR6) is usually minimal, the percentage change in ‘task contents’ (Equation AR7) virtually mirrors the percent change in labor share (Equation AR4).

To summarize, AR’s inference of automation and ENT is largely based on the percent change in labor share. However, using these inferred variables in our primary analysis presents a challenge due to the expected high correlation with labor share, which could lead to reverse causality. Furthermore, there is no certainty that the inferred variables accurately represent the real-world values of automation and ENT. Consequently, we require variables obtained through direct measurement.

For the purpose of assessing automation, we will use data provided by the International Federation of Robotics (IFR), which gives us the number of automated machines at the country-industry-year level. To analyze ENT, we will use data from ONET, which offers information on the number of new tasks in the USA, measured at the occupation-year level. This data is collected directly by ONET.

### 3.2 The International Federation of Robotics

The International Federation of Robotics (IFR) provides data on the number of automated machines (both flow and stock) at the country-industry-year level. Rather than using the raw data on the number of robots from the IFR, we utilize the Adjusted Penetration of Robots (APR), as proposed by Acemoglu and Restrepo (2020). APR is defined as in Equation (20):

$$\text{APR}_{i,(t5,t1)} \equiv \frac{M_{i,t5} - M_{i,t1}}{L_{i,2005}} - \frac{Y_{i,t5} - Y_{i,t1}}{Y_{i,t1}} \frac{M_{i,t1}}{L_{i,2005}} \quad (20)$$

$$= \left( \frac{M_{i,t5} - M_{i,t1}}{M_{i,t1}} - \frac{Y_{i,t5} - Y_{i,t1}}{Y_{i,t1}} \right) \frac{M_{i,t1}}{L_{i,2005}} \quad (21)$$

$$= (g_M - g_Y) \frac{M_{i,t1}}{L_{i,2005}} \quad (22)$$

, where  $i$  is the industry sector (country  $\times$  industry in our case), and t5 is 5-year after t1.  $M$  is the number of robots (stock),  $L$  is the number of employees,  $Y$  is value-added (in real terms).

We employ APR as a proxy for  $d(I - N + 1)$ , primarily because the observable growth rate of the number of robots is not a suitable proxy for  $dI$ . The term  $dI$  encapsulates the theoretical concept of a ‘pure direction of automation,’ which is abstract and not directly observable in empirical settings. In contrast, the growth rate of the number of robots reflects an equilibrium outcome in real-world scenarios. Given this, we seek an alternative representation for  $dI$ . APR, as proposed by Acemoglu and Restrepo (2020), serves as an effective proxy for  $d(I - N + 1)$ .

The APR represents the 5-year growth rate of robots adjusted by labor input and the value-added within a given sector. Multiplication by  $\frac{M_{i,t1}}{L_{i,2005}}$  is necessary as the raw number of robots does not adequately represent our definition of automation. Consider, for instance, that the IFR began collecting data in many countries starting in 2004. A change from 1 robot to 100 robots between 2004 and 2005 would represent a growth rate of 9900%, whereas an increase from 100 to 200 robots between 2005 and 2006 would only reflect a 100% growth rate. These rates are not useful because the number of machines increased by the same amount (100) in both cases. The term  $\frac{M_{i,t1}}{L_{i,2005}}$  is introduced to adjust for this discrepancy. Suppose  $L_{i,2005} = 100$ . In 2005,  $g_M \times \frac{M_{i,t1}}{L_{i,2005}}$  equals 99%, and in 2006, it amounts to 100%, which makes them comparable. The underlying idea is that the 5-year difference in the number of machines across countries and industries is not directly comparable; we need to normalize it by dividing by the number of employees.<sup>12</sup>

<sup>12</sup>Instead of dividing by  $L_{i,2005}$ , dividing by ‘quantity’ would be more accurate, but it will not change the results significantly.

The second term in Equation (22),  $-g_Y$ , serves to measure the ‘penetration’ of robots. In other words, if the growth rate of robots exceeds that of value-added, we interpret this as a positive penetration. Within the AR framework, this penetration equates to  $I - N + 1$  in their terminology, which represents the length between  $N-1$  and  $I$ .

### 3.3 The Occupational Information Network

The Occupational Information Network (ONET), managed and maintained by the United States Department of Labor, serves as a comprehensive database of occupational information (National Center for O\*NET Development, 2023). For each Standard Occupational Classification (SOC),<sup>13</sup> ONET consistently updates the spectrum of tasks that workers are expected to perform. For example, in 2023, Automotive Engineers were assigned 25 responsibilities, which included the calibration of vehicle systems, control algorithms, and other software systems. When new tasks, previously nonexistent, come to light, ONET increases the number of tasks associated with the Automotive Engineering occupation. Furthermore, ONET periodically reports ‘Emerging new tasks’ about once or twice annually. These tasks have recently emerged but have not been extensively studied by the ONET department; hence, these specific tasks are not included in the occupational list. We incorporate these ‘Emerging new tasks’ in addition to our base number of tasks provided by ONET. This process completes our generation of ‘task scores’ by each occupation.

The ‘Task scores’ vary by Standard Occupational Classification (SOC) and year. AR translated this information into variations by industry and year using the US Census from IPUMS (Ruggles et al., 2020), a dataset comprising individual worker data with specific occupation codes.<sup>14</sup> After associating the ‘Task score’ with each individual, an average is calculated at the industry and year level. We denote this variable as the emergence of new tasks (ENT). ENT can also be formulated for EU countries using the EU Labor Force Survey (EU-LFS) instead of the US Census. It’s crucial to recognize that the ‘task scores’ from ONET are used to generate ENT for EU countries.

The European Commission has recently initiated a project akin to ONET, named ‘European Skills, Competences, Qualifications, and Occupations’ (ESCO). ESCO has dis-

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<sup>13</sup>SOC is an acronym for Standard Occupational Classification employed by US agencies. The ONET classification system (ONET-code) is a subclassification of the SOC system, hence, every ONET-code has a corresponding SOC. However, the ONET-code does not align perfectly with the Occupational Classification Code (OCC).

<sup>14</sup>Contrary to our approach, AR exclusively utilizes the ‘Emerging new tasks’ as reported by ONET. They do not combine these with the base number of tasks provided by ONET. We did not favor this method because the ‘Emerging new tasks’ reported by ONET are sparse and not thorough.

closed the tasks required for workers for a single year and has yet to release a Task score.

In the absence of a European equivalent of the ‘Task scores’, we depend on data from ONET. A foundational assumption in the creation of the EU’s ENT is that the task requirements in the USA mirror similar trends in the EU. For example, if the number of tasks required for Automotive Engineers surged in the USA in 2015, it is assumed that a similar trend occurred in the EU around the same period. Therefore, the variation for the EU originates from the differing composition of workers in each country, occupation, and year; regrettably, the EU-LFS does not offer more detailed industry variation beyond the manufacturing sector.

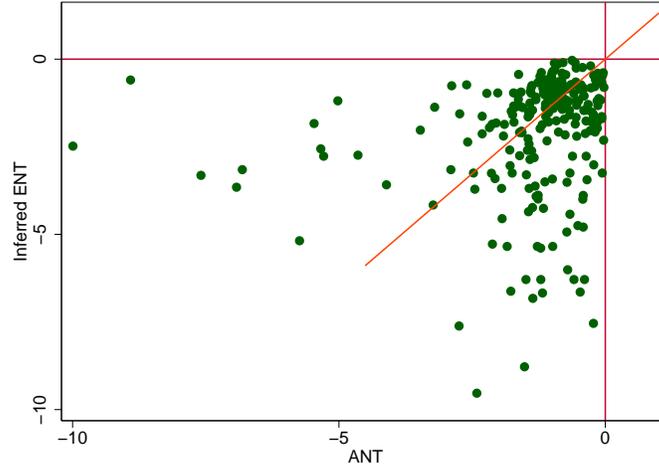
While we adopt AR’s concept when generating ENT, our method offers more refinement. Detailed explanations of this can be found in Appendix D. ENT can be compared with the inferred value of ENT proposed by AR. As mentioned earlier, the inferred variable may not be a true representation of the actual value obtained directly from data collection. Consequently, any discrepancies between ENT and the ‘inferred value of ENT’ do not necessarily indicate that ENT is misleading. Instead, it could suggest that the ‘inferred value’ is not an effective proxy for the real value.

We compared ENT and the ‘inferred value of ENT’ in the USA. First, both have fixed differences at the industry level. Therefore, to make meaningful comparisons across industries, the industry-fixed effect must be removed. We regress each variable solely on industry dummies and take the residual. Secondly, as we are interested in long-term growth rates, we convert the variables into 5-year growth rates. Figure 3 presents a scatter plot of the two variables’ growth rates. They are highly correlated.

Before concluding this section, it’s worth noting that ‘task contents’ constitute the sum of ‘inferred ENT’ and ‘inferred Automation’, which nearly matches the labor share (refer to Panel B of Figure 5 in AR). In Figure 3, we compared ENT and inferred ENT at the country and year level. *Acemoglu and Restrepo (2020)* performed a similar comparison at the industry level in the USA, focusing solely on the year 2018 (the growth rate from 1990 to 2018). Interestingly, they compared their version of ENT with ‘task contents’, while we believe that a comparison between ENT and ‘inferred ENT’ would be more appropriate. Using their replication code, we compared their version of ENT with the ‘inferred ENT’ they computed. The similarity was found to be insignificant. Our explanation for their insignificant comparison is provided in Appendix E. In essence, the reason lies in their comparison of ENT with the inferred ENT across industries at a single point in time (2018). As will be elaborated on in the appendix, the magnitude of inferred ENT across

Figure 3

(a) ENT and inferred ENT (5-year growth rate)



industries at a specific point in a year is meaningless. Consequently, the insignificant result is expected.

### 3.4 Capital Price

In our paper, we utilize the replicated values for capital price from Karabarbounis and Neiman (2014) (specifically, the their KLEMS version). To calculate this, we initially require the investment price, which the KLEMS data provides, including industry variations.

It's important to note that we don't directly observe the capital price, which represents the *usage* cost of one unit of capital. We do, however, observe the investment price, which signifies the *purchase* cost of one unit of capital. In accordance with the theory of investment by Jorgenson (1963), we can calculate the capital price as follows:

$$R_t = \xi_{t-1}(1 + i_t) - \xi_t(1 - \delta_t) \quad (23)$$

In this equation,  $R$  represents the capital price,  $\xi$  is the investment price,  $i$  is the nominal interest rate, and  $\delta$  is the depreciation rate. Equation (23) signifies that investors are indifferent between paying a *usage* cost for capital ( $R_t$ ) and *purchasing* capital, paying interest, and then selling the depreciated capital at a later date.

### 3.5 Robot Price

Unfortunately, the International Federation of Robotics (IFR) provided robot prices in the form of an average unit price until 2009, and as a price index until 2005. Klump et al. (2021) and Jurkat et al. (2022) provide in-depth information on this topic. They noted, “Due to the considerable effort involved and owing to compliance issues, the IFR no longer continues to construct the price indices.” An alternative method to obtain robot prices is by following the approach of Fernandez-Macias et al. (2021), which involves the use of UN Comtrade data.<sup>15</sup> We adopted this method, though, unfortunately, as they did not provide a replication code and data, there may be slight differences in our results.

UN Comtrade provides annual import and export values for HS847950.<sup>16</sup> They also provide the number of HS847950 for both imports and exports. Hence, we infer the robot prices by dividing the values by their numbers. Fernandez-Macias et al. (2021) illustrate in their Figures 3 and A1 that the robot price trends based on IFR and UN Comtrade data are similar. Furthermore, they demonstrate that the robot price has been steadily declining.

### 3.6 KLEMS

Aside from the IFR dataset, the ONET dataset, and Robot Price, we will use data from KLEMS.<sup>17</sup> KLEMS comes in two different versions: one follows national accounts, and the other follows growth accounts. The main difference between these versions is that the national accounts allow room for a markup greater than one, while the growth accounts do not. The latter assumes that the sum of labor cost and capital cost equals the value-added, implying that the markup is exactly one. As allowing for a markup is critical for our analysis, we use the national accounts when using KLEMS.

KLEMS shares similar characteristics with OECD STAN in terms of many national account variables at a country-industry-year level. Table 1 presents descriptive statistics. Predominantly, the values for OECD STAN and KLEMS are comparable, albeit not identical. In some instances, the values are in fact identical. This alignment is a result of collaborative projects aimed at fostering more consistent values between the two.

All nominal values are converted to real values through division by the chain-linked price index provided by KLEMS (VA.PI), following the methodology implemented by Karabarbounis and Neiman (2014).

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<sup>15</sup><https://comtradeplus.un.org/>

<sup>16</sup>Machinery and mechanical appliances; industrial robot, n.e.c. or included.

<sup>17</sup>KLEMS: EU level analysis of capital (K), labour (L), energy (E), materials (M) and service (S) inputs.

Table 1: Descriptive Statistics

Country	WL (labor comp)		RK (capital comp)		Value added		Labor Share	
	STAN	KLEMS	STAN	KLEMS	STAN	KLEMS	STAN	KLEMS
USA	867,789	851,834	292,456	308,662	1,647,140	1,593,719	52.85	53.60
DEU	366,787	366,806	104,117	104,034	569,189	570,196	64.67	64.57
SWE	256,507	256,540	115,040	124,370	502,728	502,728	51.17	51.18
DNK	219,076	226,496	199,337	220,713	410,478	426,533	55.33	54.87
ITA	140,568	140,568	57,107	54,924	253,368	253,353	55.60	55.60
FRA	135,093	135,098	52,379	41,244	226,181	226,181	59.74	59.74
GBR	110,603	109,347	26,230	25,535	171,778	170,498	64.45	64.19
AUT	28,106	29,959	9,427	12,090	51,011	54,254	55.22	55.31
FIN	17,100	17,979	7,512	7,204	33,112	34,848	51.91	51.85
PRT	11,537	12,897	3,166	3,166	20,575	23,030	56.06	55.99
Total	215,317	214,753	86,677	90,194	388,556	385,534	56.75	56.69

## 4 Regressions

Based on the specification in Equation (19), we provide consistent regression equations. Equation (25) is for the corresponding regression. It should be noted that the coefficient of  $d \ln \mu$  is required to be  $-1$ , as directed by Equation (24). Given that our emphasis is not on measuring the coefficient of  $d \ln \mu$ , we have transposed this term to the left-hand side, as depicted in Equation (25). This adjustment is consistent with the specification outlined in Equation (19).

$$\begin{aligned}
gr\_laborshare &= - gr\_markup \\
&+ \alpha_1 APR + \alpha_2 gr\_ENT \\
&+ \alpha_3 gr\_labor\ price + \alpha_4 gr\_robot\ price \\
&+ \alpha_5 gr\_capital\ price + \gamma_i + \gamma_j + \gamma_t + \gamma_{ij} + \varepsilon_{ijt} \quad (24)
\end{aligned}$$

$$\begin{aligned}
\Leftrightarrow gr\_laborshare \times markup &= \alpha_1 APR + \alpha_2 gr\_ENT \\
&+ \alpha_3 gr\_labor\ price + \alpha_4 gr\_robot\ price \\
&+ \alpha_5 gr\_capital\ price + \gamma_i + \gamma_j + \gamma_t + \gamma_{ij} + \varepsilon_{ijt} \quad (25)
\end{aligned}$$

, where  $gr$  indicates the variables are in a 5-year growth rate. APR and ENT stand for Adjusted Penetration of Robots and Emergence of New Tasks, respectively. We exclude the notation of  $gr$  from APR, as by definition, they already represent a 5-year growth rate (refer to Equation (22)). Within this context,  $i$ ,  $j$ , and  $t$  correspond to country, industry, and year, respectively.

For convenience, we have rewritten Equation (19) as Equation (26) below.  $\textcircled{A}$  repre-

sents ‘the share of the effective wage for task  $I$ ’ times  $-1$ . ⑥ represents the task price channel (the partial derivative). Lastly, ⑦ represents the price drop in the aggregate task ( $T$ ) when robots replace human labor.

$$\begin{aligned}
d \ln S_L^f = & \\
& - \left[ (1 - \zeta) + \left( -(1 - \zeta) + S_K^f(1 - \sigma) \right) S_L^T \right] d \ln \gamma \\
& + \underbrace{\left[ \underbrace{-\frac{\left(\frac{W_I}{\gamma_I}\right)^{1-\zeta}}{\int_I^N \left(\frac{W_j}{\gamma_j}\right)^{1-\zeta} dj}}_{\text{①}} + \underbrace{\left( -(1 - \zeta) + S_K^f(1 - \sigma) \right)}_{\text{②}} \underbrace{\frac{1}{1 - \zeta} \frac{\psi^{1-\zeta} - \left(\frac{W_I}{\gamma_I}\right)^{1-\zeta}}{P_T^{1-\zeta}}}_{\text{③}} \right]}_{\text{④}} d(I - N + 1) \\
& + \underbrace{\left( S_N^L - S_I^L \right) \frac{1}{1 - \zeta} \left[ S_M^T(1 - \zeta) + S_L^T S_K^f(1 - \sigma) \right]}_{\text{⑤}} dN \\
& + \underbrace{\left[ (1 - \zeta) + \left( -(1 - \zeta) + S_K^f(1 - \sigma) \right) S_L^T \right]}_{\text{⑥}} d \ln W \\
& + \underbrace{\left[ \left( -(1 - \zeta) + \underbrace{S_K^f(1 - \sigma)}_{\text{⑦}} \right) S_M^T \right]}_{\text{⑧}} d \ln \psi \\
& - \underbrace{\left[ S_K^f(1 - \sigma) \right]}_{\text{⑨}} d \ln R. \tag{26}
\end{aligned}$$

In Equation (26),  $S_L^f$  represents labor share times markup,  $I - N + 1$  is automation,  $N$  is emergence of new tasks,  $W$  is wage,  $\psi$  is robot price, and  $R$  is non-robot capital price. Meanwhile, the sum of the coefficients of  $d \ln W$  and  $d \ln \psi$  is equal to the negative coefficient of  $d \ln R$  (i.e.  $\text{⑨} = -\text{⑥} - \text{⑧}$ ). Therefore, we prefer to put this restriction to our regression accordingly.

Table 2 is the regression result. Column (1) shows the Ordinary Least Squares (OLS) results without the coefficient restriction; Column (2) displays the OLS results with the coefficient restriction; Column (3) features the Non-linear Least Squares (NLS) results with the restriction; Column (4) contains the two-step Generalized Method of Moments

(GMM) results with the restriction; Finally, Columns (5-7) present the quantile regressions with the restriction. The coefficients across different quantiles retain the same sign as in the OLS regressions. This suggests that the implications hold steady across different quantiles of labor share. In Appendix F, we additionally present the quantile regressions without the restriction. The results do not differ from the quantile regressions with the restriction.

In Column (1), using OLS without the restriction, we test the null hypothesis that the restriction is non-binding. With an F-value of 1.54, we cannot reject the null hypothesis even at the 0.2 significance level. Given that the restriction is non-binding, the quantile regressions presented in Appendix F are meaningful.

For the remainder of our paper, we will use the results from Column (2) as our point of reference. It's worth noting that since the OLS in Column (2) and the NLS in Column (3) operate under different assumptions regarding the error term, their confidence intervals are expected to differ slightly, although this difference is not visible in Table 2. The GMM approach in Column (4) is more efficient than OLS, *even within a constrained environment*, under the assumptions that (a) the model is correctly specified, (b) the sample size is large, and (c) errors are independent (Newey and West, 1987). However, these assumptions may not hold in practice. Moreover, the results from Column (2), which serves as our reference, and the GMM results do not show substantial differences; the main divergence lies in the coefficient and standard error associated with APR, but even this difference is minimal.

Using Equation (26), we can determine the signs of  $\zeta$  and  $\sigma$ . Specifically,  $S_K^f > 0$  and the coefficient for  $d \ln R$  is negative, implying that  $\sigma < 1$ . Additionally, by plugging in  $S_K^f = 0.494$  that we acquired from dataset, we infer  $\sigma = 0.594$  as shown in Equation (27).

$$- \left[ \underbrace{S_K^f}_{0.494} (1 - \sigma) \right] = \underbrace{\alpha_5}_{-0.200} \quad (27)$$

The derivation of the value of  $\zeta$  is as follows. From Equation (26), using  $\alpha_3$ ,  $\alpha_4$ , and  $\alpha_5$ , we derive Equation (Zeta), which we illustrate in Figure 4. To keep things concise, denote  $\alpha_2 = 0.015$ ;  $\alpha_3 = 0.195$ ; and  $\alpha_4 = 0.005$ , then

$$\zeta = 1 - \alpha_3 + \alpha_4 \frac{S_L^T}{1 - S_L^T} \quad (\text{Zeta})$$

As we will demonstrate at the end of this section, we estimate  $S_L^T$ , which represents the share of labor cost out of the aggregated task cost (i.e. labor cost + robot cost),

Table 2: Regressions

Restriction Quantile	OLS	OLS	NLS	GMM	Quantile		
	(1) No	(2) Yes	(3) Yes	(4) Yes	(5) Yes	(6) Yes	(7) Yes
$\alpha_1$ : APR	-0.261* (0.113)	-0.235* (0.110)	-0.235* (0.110)	-0.178 (0.102)	-0.251** (0.094)	-0.121 (0.067)	-0.050 (0.042)
$\alpha_2$ : gr_ENT	1.468*** (0.372)	1.483*** (0.372)	1.483*** (0.372)	1.535*** (0.348)	0.522*** (0.076)	0.507*** (0.074)	0.444*** (0.059)
$\alpha_3$ : gr_labor price	20.200*** (2.387)	19.520*** (2.522)	19.520*** (2.522)	20.411*** (2.604)	13.326*** (0.589)	16.262*** (0.436)	17.311*** (0.371)
$\alpha_4$ : gr_robot price	1.016 (2.650)	0.529 (2.950)	0.529 (2.950)	4.424 (2.495)	3.917*** (0.828)	5.307*** (0.590)	3.796*** (0.391)
$\alpha_5$ : gr_capital price	-23.536*** (3.133)	-20.048*** (3.831)	-20.048*** (3.831)	-24.834*** (3.442)	-17.243*** (1.011)	-21.569*** (0.656)	-21.106*** (0.495)
$N$	1027	1027	1027	1027	1027	1027	1027
$R^2$	0.565	0.563	0.563				
pseudo $R^2$				0.386	0.540	0.444	0.578

Standard errors in parenthesis are heteroskedasticity-robust

\*  $p < 0.05$ , \*\*  $p < 0.01$ , \*\*\*  $p < 0.001$

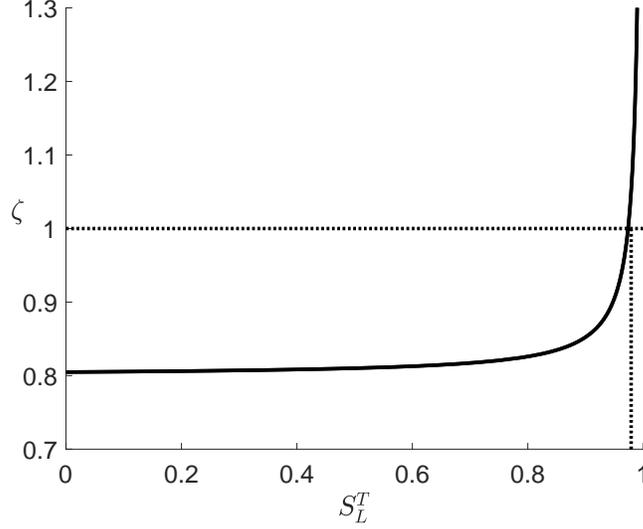
The coefficients and the standard errors have been multiplied by 100 for better readability.

to be 0.979. By substituting  $S_L^T = 0.979$  into Equation (Zeta), we derive an estimate of  $\zeta = 1.051$ , which is a value close to one. It's important to note that  $\zeta$  signifies the elasticity of substitution *between different tasks* and does not pertain to the elasticity between labor and robots *within a task*; our model considers robots and labor as perfect substitutes *within a task*.

To validate the reliability of  $\zeta$ , we have conducted sensitivity tests. Rather than relying on point estimates, we've used intervals encompassing one standard deviation around these estimates. For the coefficient of gr\_labor price, denoted as  $\alpha_3$ , the interval is (0.183, 0.208), resulting in  $\zeta$  falling within the interval of (1.038, 1.063). If we instead consider the interval for the coefficient of gr\_robot price, represented by  $\alpha_4$ , as (-0.009, 0.007), then  $\zeta$  falls within the interval of (0.364, 1.137). By considering intervals for both  $\alpha_3$  and  $\alpha_4$ , we find that  $\zeta$  falls within the interval of (0.352, 1.149). From this analysis, we can conclude that the uncertainty associated with  $\zeta$  predominantly arises due to the low significance of  $\alpha_4$ , gr\_robot price.

More generally, we present statistics for a linear combination of Equation (Zeta). The null hypothesis of  $1 - \zeta = 0$  is not rejected at the 0.05 significance level, with a confidence interval of (-2.747, 2.646). Therefore we argue that  $\zeta$  is close to 1.

Figure 4: Equation (Zeta)



Essentially, the elasticity of substitution between aggregate tasks and non-robot capital ( $\sigma$ ) fundamentally influences the relationships of wage, robot price, and capital price with labor share. Assuming that  $1 - \zeta$  is close to zero, Equation (26) demonstrates that the value of  $\sigma$  is pivotal in determining  $\textcircled{\alpha}_3$ ,  $\textcircled{\alpha}_4$ , and  $\textcircled{\alpha}_5$ , provided that  $S_K^f$ ,  $S_L^T$ , and  $S_M^T$  are empirically established values. First, the expression  $\left[ (1 - \zeta) + \left( -(1 - \zeta) + S_K^f(1 - \sigma) \right) S_L^T \right]$  simplifies to  $\left( S_K^f(1 - \sigma) \right) S_L^T$ , indicating that an increase in wages positively affects labor share. Second, the expression  $\left[ \left( -(1 - \zeta) + S_K^f(1 - \sigma) \right) S_M^T \right]$  simplifies to  $\left( S_K^f(1 - \sigma) \right) S_M^T$ , demonstrating that a decline in robot price leads to a decrease in labor share. Third, the expression  $-\left[ S_K^f(1 - \sigma) \right]$  shows the negative correlation between non-robot capital price and labor share. The regression results presented in Table 2 yield the consistent results. Coefficients  $\textcircled{\alpha}_3$ ,  $\textcircled{\alpha}_4$ , and  $\textcircled{\alpha}_5$  are 0.195, 0.005, and  $-0.200$ , respectively.<sup>18</sup>

The negative coefficient for robot price in our regression model reveals two key mechanisms through which advancements in robotics affect labor share. First, improved capabilities allow robots to execute tasks once reserved for humans, leading to a reduction in labor share. Second, a decline in robot costs, without an increase in functionality, similarly lowers the labor share. Overall, both mechanisms contribute to a decrease in

<sup>18</sup>Meanwhile, the sign of the coefficient for  $d(I - N + 1)$  is negative. To elaborate,  $\textcircled{\mathbb{A}} < 0$  by the definition of productivity-adjusted wage; We have demonstrated that  $\textcircled{\mathbb{B}}$  is indeed greater than zero.<sup>19</sup> ; and, as per Assumption 1,  $\textcircled{\mathbb{C}} < 0$ . Therefore,  $\textcircled{\mathbb{B}} \times \textcircled{\mathbb{C}} < 0$ . This means that both the direct effect ( $\textcircled{\mathbb{A}}$ ) and indirect effect ( $\textcircled{\mathbb{B}} \times \textcircled{\mathbb{C}}$ ) are negative. Here, we define the ‘direct effect’ as the effect that does not operate through the ‘task price’ channel. Conversely, we define the ‘indirect effect’ as the effect that necessarily passes through this channel.

labor share.

In the future, we anticipate that the second mechanism –the robot price channel– will become more prominent as the share of robots in society increases. This expectation is due to the term  $S_M^T$ . Note that among the three price factors in Equation (26),  $S_M^T$  appears solely in relation to robot price. Also noteworthy is that  $S_M^T \equiv \frac{(I-N+1)\psi^{1-\zeta}}{P_T^{1-\zeta}}$  includes the term  $I - N + 1$ , which corresponds to the share of robot tasks relative to the combined tasks of labor and robots. As  $I - N + 1$  increases in the future, the coefficient for robot price in Table 2 is likely to grow larger and become significant.

The condition  $\sigma < 1$  indirectly confirms that capital and labor are gross complementary, a result that aligns with the findings reported by Glover and Short (2020). Conversely, this result contradicts the hypothesis of gross substitutability ( $\sigma > 1$ ) posited by Karabarbounis and Neiman (2014) (henceforth referred to as KN). We clarify that the term  $\sigma$  in our general equilibrium model does not align exactly with the definition of  $\sigma$  in the work of KN as well as Glover and Short (2020). The divergence stems from our model’s distinction between robots and capital. Specifically, in our model,  $\sigma$  represents the elasticity of substitution between ‘non-robot capital’ and ‘aggregated tasks’, where the latter encompass both robot and labor inputs. Assuming a Cobb-Douglas production function between robot and labor input brings our definition of  $\sigma$  closer to that of KN.

Let  $\mu$  denote the elasticity of substitution between labor and non-robot capital. Given that our model incorporates two layers of production functions –Equation (3) and (4)– it is not possible to derive a closed-form solution for  $\mu$ . Assuming that  $\zeta$  converges to one, we can temporarily treat Equation (4) as a Cobb-Douglas function. It then follows that (the derivation process is provided in Appendix B):

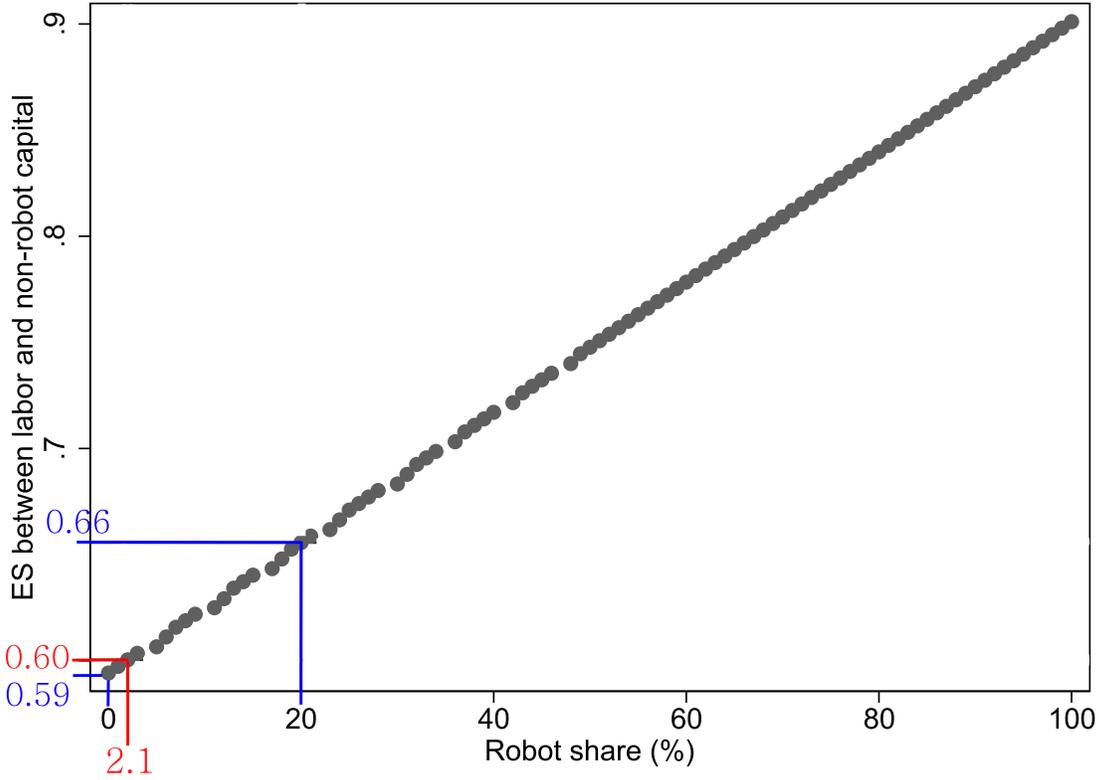
$$\begin{aligned} \mu &\equiv \frac{d\left(\frac{L}{K}\right) \frac{R}{\bar{W}}}{d\left(\frac{R}{\bar{W}}\right) \frac{L}{K}} \\ &= \frac{d\left(\frac{R^\sigma}{\bar{W}^{1-(N-I)(1-\sigma)}}\right) \frac{R}{\bar{W}}}{d\left(\frac{R}{\bar{W}}\right) \frac{R^\sigma}{\bar{W}^{1-(N-I)(1-\sigma)}}} \end{aligned} \quad (28)$$

$$\Rightarrow \sigma \text{ if } N - I = 1.$$

When  $I > N - 1$ , differentiating Equation (28) becomes infeasible. However, we can employ numerical approximation to estimate  $\mu$ . We use actual  $\bar{W}$  and  $R$  values from the dataset (all possible combinations of these), along with  $\sigma = 0.594$  as established in Equation (27). We introduce small random variations to each  $\bar{W}$  and  $R$  and consider sce-

narios where  $|\Delta \frac{R}{W}|$  is approximately 0.01. These values are then plugged into Equation (28) to obtain an approximated  $\mu$ .

Figure 5: Elasticity of Substitution between Labor and Non-robot Capital



Assuming a Cobb-Douglas production function for Equation (4), the length between  $N - 1$  and  $I$  is equivalent to the percentage of tasks that are automated. Figure 5 presents the results. When the length between  $N - 1$  and  $I$  is zero, we find that  $\mu = \sigma = 0.594$ . This stage indicates the absence of automation tasks and all tasks being executed by labor. Even when we assume 20% of tasks are automated, the divergence from  $\sigma$  is minimal, at most  $\mu = 0.656$ . Consequently, we argue that in the context of the KN model, the elasticity of substitution between labor and non-robot capital closely approximates  $\sigma$ . Our analysis suggests that  $\mu$  ranges between 0.594 and 0.656, supporting the idea of a gross complementary relationship between the two. In the future, as automated robots come to constitute a large portion of tasks, the elasticity of substitution between labor and non-robot capital may move closer to one. However, making this prediction with accuracy would require more thorough research.

Recent research underscores the importance of quantifying this elasticity of substitution between labor and capital, as highlighted by Martinez (2018), Oberfield and Raval

(2021), and Zhang (2023). Many studies report an elasticity less than one, endorsing the concept of gross complementarity. However, Piketty and Zucman (2014) suggest the potential for gross substitutability. They observed an escalating capital-output ratio and argued that this trend could consistently account for the declining labor share if the elasticity of substitution between labor and capital exceeds one—a position we do not support.

Our finding also contradicts the hypothesis proposed by KN, who argue that the falling price of capital accounts for half of the recent decline in labor share. For their argument to hold, the elasticity of substitution between labor and capital must be greater than one (gross substitutes). They directly measured the correlation between the trend of capital price and labor share without using instrumental variables. In contrast, Glover and Short (2020) reached a different conclusion, that of gross complements, by using cross-country variation with instrumental variables. They argue that correcting for bias is critical when estimating the correlation between the capital price and labor share. Our paper addresses omitted variable bias using a control function approach. We regress automation, the emergence of new tasks, wages, and robot price, along with capital price, on labor share, believing that this approach corrects for omitted variable bias. Our study supports Glover and Short (2020).

Table 3: Regressions using gr\_ENT\_USdetail

	OLS	OLS	NLS	GMM	Quantile		
	(1)	(2)	(3)	(4)	(5)	(6)	(7)
Restriction	No	Yes	Yes	Yes	Yes	Yes	Yes
Quantile					0.2	0.5	0.8
$\alpha_1$ : APR	-0.245* (0.110)	-0.217* (0.107)	-0.217* (0.107)	-0.161 (0.098)	-0.324*** (0.088)	-0.133* (0.055)	-0.108* (0.048)
$\alpha_2$ : gr_ENT_USdetail	0.555** (0.177)	0.552** (0.176)	0.552** (0.176)	0.544*** (0.165)	0.272*** (0.064)	0.180*** (0.031)	0.227* (0.113)
$\alpha_3$ : gr_labor price	20.390*** (2.379)	19.659*** (2.502)	19.659*** (2.502)	20.366*** (2.577)	13.463*** (0.442)	16.066*** (0.449)	16.499*** (0.549)
$\alpha_4$ : gr_robot price	2.109 (2.710)	1.611 (3.023)	1.611 (3.023)	5.873* (2.554)	3.985*** (0.777)	5.991*** (0.553)	4.315*** (0.424)
$\alpha_5$ : gr_capital price	-24.983*** (3.319)	-21.269*** (3.965)	-21.269*** (3.965)	-26.238*** (3.603)	-17.447*** (0.953)	-22.057*** (0.637)	-20.814*** (0.640)
$N$	1027	1027	1027	1027	1027	1027	1027
$R^2$	0.555	0.552	0.552				
pseudo $R^2$				0.386	0.537	0.441	0.574

Standard errors in parenthesis are heteroskedasticity-robust

\*  $p < 0.05$ , \*\*  $p < 0.01$ , \*\*\*  $p < 0.001$

The coefficients and the standard errors have been multiplied by 100 for better readability.

Meanwhile, Table 3 represents the regressions, which are analogous to those in Table 2, with the exception that it utilizes ENT\_USdetail instead of ENT. ENT remains constant across sectors in both the EU and the USA. In contrast, ENT\_USdetail is sector-specific in the USA but uniform in EU countries. This distinction stems from the EU-LFS’s limitation in offering variations beyond the primary manufacturing sector. Conversely, the US Census provides differentiation at the two-digit sector level. When formulating ENT, we aligned with the broader manufacturing sector representation of the EU-LFS for both the EU and the USA to maintain consistency. However, in creating ENT\_USdetail, we incorporated the detailed sector classifications from the US Census for the USA, while preserving the more generalized manufacturing sector for the EU countries. For consistency between the USA and EU, we prefer using ENT.

The coefficients for both ENT and ENT\_USdetail consistently outweigh those for APR. Notably, the coefficients for ENT\_USdetail are significantly smaller than those for ENT. This suggests that if we had access to an EU-LFS dataset offering more granular sector variations, the dominance might diminish. Investigating this remains a task for future work.

**Estimation of  $S_L^T$ :** Before concluding this section, let us explain how we estimated  $S_L^T$ , which denotes the share of labor cost out of the combined task cost (i.e., labor cost + robot cost). There isn’t official data available that directly provides this value, but it is necessary to infer  $\zeta$ . As a result, we must rely on various sources to accurately estimate this value. Let’s assume labor cost to be 100 without loss of generality. According to KLEMS data, the rental cost for OMach is recorded as 13.595. But it’s important to note that OMach encompasses not just robots but also a range of other items, including equipment, machinery, engines, and turbines (Stehrer et al., 2019; Gouma and Timmer, 2013). Therefore, the challenge is to determine the share of robots within the broader category of OMach. The most reliable approach we can consider involves utilizing UN Comtrade data, which offers information about import and export values by detailed commodity categories. By calculating the total export values of commodities corresponding to OMach,<sup>20</sup> and separately calculating the total export values of HS Code 8479 (which pertains to robots),<sup>21</sup> we find that the ratio between these values is 13.595 : 0.71. In brief, the ratio between labor cost, OMach cost, and robot cost is 100 : 13.595 : 0.71.

It is essential to acknowledge that the equipment cost for robots is estimated to be

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<sup>20</sup>HS Classification 84 excluding 8401, 8402, 8403, 8404, 8405, 8429, 8440, 8443, 8470, 8471, and 8472.

<sup>21</sup>Machinery and mechanical appliances; having individual functions, n.e.c. in this chapter.

around 33.04%<sup>22</sup> of the total robot costs, covering aspects such as operation, training, software, maintenance, and disposal (Zhao et al., 2021). The UN Comtrade estimate of 0.71 corresponds to the equipment cost. Therefore, the total cost of the robot amounts to  $0.71/0.33 = 2.149$ . Finally, we compute  $S_L^T = 97.90$  by performing the calculation  $100/(100 + 2.149)$ .

To explore the implications of the regression results further, we will now shift to the accounting exercise.

## 5 Accounting Exercise

Based on the regression results from Column (1) of Table 2, we have assembled a series of accounting tables. These comprehensive contents can be accessed in the Excel file, which is provided in the associated footnote.<sup>23</sup> This file contains information on ‘Average variables’ and their contribution to change in labor shares.

$$\text{chg\_APR} = \text{Coefficient of APR} \times \text{Average APR}. \quad (29)$$

For instance, the term ‘Average APR’ refers to the APR value averaged over the period from 2005 to 2019. We use this average to mitigate short-term fluctuations in the variable. The ‘Coefficient of APR’ is the regression result in Column (1) of Table 2. Finally,  $\text{chg\_APR}$  quantifies how the five-year growth rate of labor share ( $S_L^f$ ) has changed due to automation (APR).<sup>24</sup>

In the Excel file, odd-numbered sheets correspond to ‘Average variables,’ and even-numbered sheets correspond to ‘chg\_variables.’ Sheets 1 and 2 present data by country  $\times$  sector, with samples provided in Tables 4 and 5, respectively. Sheets 5 and 6 are aggregated by country (Tables 6 and 7, respectively). Sheets 9 and 10 are aggregated by sector (Tables 8 and 9, respectively). Aggregation is based on ‘Average variables’ from the country  $\times$  sector data in Excel Sheet 1. These values are then aggregated using the corresponding value-added as weights.

The remaining sheets in the Excel file —Sheets 3, 4, 7, 8, 11, and 12— are structured similarly, but they use `gr_ENT_USdetail` instead of `gr_ENT`.<sup>25</sup> For readability, our focus remains on the sheets using `gr_ENT`. For more information, please refer to the ‘Readme’ sheet in the Excel file.

<sup>22</sup> $33.04\% = 35.73\% \times (1 - 0.075)$ , where 0.075 represents taxes, transactions, and after-sales fees.

<sup>23</sup><https://github.com/jayjeo/public/blob/main/Laborshare/accounting.xlsx>

<sup>24</sup> $S_L^f$  is defined in Equation (19) in the Model section.

<sup>25</sup>The meaning of `gr_ENT_USdetail` is explained in detail in the paragraph following Table 3.

Table 4: Average Variables

location	sector	$gr_{S_L^f}$	APR	$gr_{ENT}$	$gr_{capital}$ price	$gr_{labor}$ price	$gr_{robot}$ price
AUT	10-12	-0.117	0.179	0.844	1.050	6.297	-6.329
AUT	13-15	-1.138	0.010	0.844	4.247	-6.828	-0.269
AUT	16-18	1.133	0.093	0.844	8.614	7.769	4.088
AUT	20-21	-0.092	0.005	0.844	7.983	29.063	2.271
AUT	22-23	-0.785	1.588	0.844	2.904	6.136	-3.634
AUT	24-25	-0.492	1.622	0.844	-2.119	3.285	-8.967
AUT	26-27	-4.332	0.605	0.844	6.693	13.105	1.870
AUT	28	-1.731	0.532	0.844	1.102	15.561	-4.435
AUT	29-30	-1.850	3.111	0.844	6.732	18.560	1.394
AUT	31-33	0.054	0.449	0.844	-0.615	10.690	-6.559
DEU	10-12	0.887	0.240	0.866	0.327	4.385	-8.220
DEU	13-15	1.455	0.016	0.866	-1.175	6.638	-8.417
DEU	16-18	1.363	-0.285	0.866	4.886	8.845	-1.630
DEU	19	-0.431	0.263	0.866	-27.546	-28.091	-39.132
DEU	20-21	2.617	0.006	0.866	1.309	5.617	-9.444
DEU	22-23	1.544	1.222	0.866	1.623	5.949	-6.842
DEU	24-25	0.715	0.794	0.866	4.053	8.588	-4.858
DEU	26-27	2.096	-0.091	0.866	9.482	14.893	0.193
DEU	28	0.731	0.783	0.866	-4.410	-0.925	-14.783
DEU	29-30	-1.136	-2.512	0.866	1.370	7.288	-8.982
DEU	31-33	-0.101	-0.176	0.866	-4.635	-2.412	-14.182
ITA	10-12	0.958	1.261	0.740	3.239	6.690	-9.521
ITA	13-15	-0.799	-0.010	0.740	7.401	8.281	-9.742
ITA	16-18	-1.230	0.145	0.740	4.422	7.198	-7.637
ITA	19	-12.079	0.386	0.740	-21.279	-32.843	-32.373
ITA	20-21	-0.577	0.021	0.740	0.778	3.375	-11.734
ITA	22-23	-2.164	0.857	0.740	2.693	6.952	-9.869
ITA	24-25	0.165	0.820	0.740	4.655	10.120	-7.668
ITA	26-27	-1.610	0.119	0.740	-7.317	-1.766	-18.731
ITA	28	0.212	0.709	0.740	-1.078	4.907	-12.576
ITA	29-30	-4.697	-2.286	0.740	-0.022	5.243	-11.992
ITA	31-33	0.975	0.034	0.740	-2.031	1.273	-14.446
USA	10-12	0.242	0.060	2.555	-7.774	-5.949	-16.491
USA	13-15	-0.177	0.001	2.555	-3.711	2.706	-9.983
USA	16-18	-0.530	0.004	2.555	-2.363	1.841	-8.808
USA	19	-3.414	0.032	2.555	2.938	9.504	-6.019
USA	22-23	-0.100	0.066	2.555	-3.510	-0.021	-11.694
USA	24-25	-0.366	0.078	2.555	2.311	6.349	-5.663
USA	26-27	0.167	0.184	2.555	21.149	37.001	15.158
USA	28	-0.418	0.025	2.555	-4.846	0.530	-12.613
USA	29-30	-1.493	0.475	2.555	-0.417	0.900	-8.770
USA	31-33	0.049	0.079	2.555	-2.198	8.760	-7.501

Table 5: Chg\_Variables

location	sector	$gr_S_L^f$	chg_sum	chg _fixed effects	chg_APR	chg_ gr_ENT	chg_gr _capital price	chg_gr _labor price	chg_gr _robot price
AUT	10-12	-0.117	0.939	-1.255	-0.042	1.251	-0.210	1.229	-0.033
AUT	13-15	-1.138	-0.081	0.856	-0.002	1.251	-0.852	-1.333	-0.001
AUT	16-18	1.133	2.189	1.149	-0.022	1.251	-1.727	1.516	0.022
AUT	20-21	-0.092	0.964	-4.370	-0.001	1.251	-1.600	5.673	0.012
AUT	22-23	-0.785	0.272	-1.203	-0.373	1.251	-0.582	1.198	-0.019
AUT	24-25	-0.492	0.565	-1.324	-0.381	1.251	0.425	0.641	-0.047
AUT	26-27	-4.332	-3.275	-5.610	-0.142	1.251	-1.342	2.558	0.010
AUT	28	-1.731	-0.675	-4.594	-0.125	1.251	-0.221	3.037	-0.023
AUT	29-30	-1.850	-0.793	-3.594	-0.731	1.251	-1.350	3.623	0.007
AUT	31-33	0.054	1.110	-2.211	-0.106	1.251	0.123	2.087	-0.035
DEU	10-12	0.887	1.943	-0.032	-0.056	1.284	-0.065	0.856	-0.043
DEU	13-15	1.455	2.511	-0.256	-0.004	1.284	0.236	1.296	-0.044
DEU	16-18	1.363	2.419	0.330	0.067	1.284	-0.980	1.726	-0.009
DEU	19	-0.431	0.626	-0.429	-0.062	1.284	5.523	-5.483	-0.207
DEU	20-21	2.617	3.674	1.607	-0.002	1.284	-0.262	1.096	-0.050
DEU	22-23	1.544	2.600	0.804	-0.287	1.284	-0.325	1.161	-0.036
DEU	24-25	0.715	1.772	-0.164	-0.186	1.284	-0.813	1.676	-0.026
DEU	26-27	2.096	3.152	0.840	0.021	1.284	-1.901	2.907	0.001
DEU	28	0.731	1.787	0.062	-0.184	1.284	0.884	-0.181	-0.078
DEU	29-30	-1.136	-0.079	-3.054	0.590	1.284	-0.275	1.423	-0.047
DEU	31-33	-0.101	0.955	-0.753	0.041	1.284	0.929	-0.471	-0.075
ITA	10-12	0.958	2.015	0.608	-0.296	1.097	-0.649	1.306	-0.050
ITA	13-15	-0.799	0.258	-0.922	0.002	1.097	-1.484	1.616	-0.051
ITA	16-18	-1.230	-0.173	-1.714	-0.034	1.097	-0.887	1.405	-0.040
ITA	19	-12.079	-11.023	-9.713	-0.091	1.097	4.266	-6.411	-0.171
ITA	20-21	-0.577	0.480	-1.053	-0.005	1.097	-0.156	0.659	-0.062
ITA	22-23	-2.164	-1.108	-2.768	-0.201	1.097	-0.540	1.357	-0.052
ITA	24-25	0.165	1.221	-0.684	-0.193	1.097	-0.933	1.975	-0.041
ITA	26-27	-1.610	-0.553	-2.645	-0.028	1.097	1.467	-0.345	-0.099
ITA	28	0.212	1.268	-0.769	-0.167	1.097	0.216	0.958	-0.066
ITA	29-30	-4.697	-3.641	-6.239	0.537	1.097	0.004	1.023	-0.063
ITA	31-33	0.975	2.032	0.364	-0.008	1.097	0.407	0.248	-0.076
USA	10-12	0.242	1.298	-2.786	-0.014	3.788	1.559	-1.161	-0.087
USA	13-15	-0.177	0.879	-4.128	-0.000	3.788	0.744	0.528	-0.053
USA	16-18	-0.530	0.527	-4.047	-0.001	3.788	0.474	0.359	-0.047
USA	19	-3.414	-2.358	-7.373	-0.007	3.788	-0.589	1.855	-0.032
USA	22-23	-0.100	0.956	-3.454	-0.015	3.788	0.704	-0.004	-0.062
USA	24-25	-0.366	0.690	-3.826	-0.018	3.788	-0.463	1.239	-0.030
USA	26-27	0.167	1.223	-5.584	-0.043	3.788	-4.240	7.222	0.080
USA	28	-0.418	0.639	-4.152	-0.006	3.788	0.972	0.103	-0.067
USA	29-30	-1.493	-0.437	-4.326	-0.112	3.788	0.084	0.176	-0.046
USA	31-33	0.049	1.106	-4.775	-0.019	3.788	0.441	1.710	-0.040

Table 6: Average Variables (Country)

location	$gr_{S_L^f}$	APR	gr_ENT	gr_capital price	gr_labor price	gr_robot price
AUT	-1.070	0.888	0.844	3.225	11.194	-2.607
DEU	0.755	-0.248	0.866	1.195	5.722	-8.392
DNK	-1.613	0.515	0.905	0.543	3.226	-10.233
FIN	0.084	0.114	1.296	3.701	-3.846	-2.480
FRA	-0.203	0.055	0.847	3.084	11.117	-1.664
GBR	0.192	0.160	1.349	2.991	4.502	-11.483
ITA	-0.808	0.286	0.740	1.177	5.125	-11.464
PRT	-0.114	0.254	-0.213	-4.991	-1.902	-3.538
SWE	2.083	0.474	0.641	-2.740	0.055	-5.962
USA	-0.675	0.140	2.555	2.690	9.188	-4.854

Table 7: Chg\_Variables (Country)

location	$gr_{S_L^f}$	chg_APR	chg_ gr_ENT	chg_gr _capital price	chg_gr _labor price	chg_gr _robot price
AUT	-1.070	-0.209	1.251	-0.647	2.185	-0.014
DEU	0.755	0.058	1.284	-0.240	1.117	-0.044
DNK	-1.613	-0.121	1.342	-0.109	0.630	-0.054
FIN	0.084	-0.027	1.921	-0.742	-0.751	-0.013
FRA	-0.203	-0.013	1.255	-0.618	2.170	-0.009
GBR	0.192	-0.038	2.000	-0.600	0.879	-0.061
ITA	-0.808	-0.067	1.097	-0.236	1.000	-0.061
PRT	-0.114	-0.060	-0.316	1.001	-0.371	-0.019
SWE	2.083	-0.111	0.951	0.549	0.011	-0.032
USA	-0.675	-0.033	3.788	-0.539	1.794	-0.026

Table 8: Average Variables (Sector)

sector	$gr_{S_L^f}$	APR	gr_ENT	gr_capital price	gr_labor price	gr_robot price
10-12 Food products	0.268	0.408	1.634	-3.941	-1.696	-11.569
13-15 Textiles, wearing apparel	0.092	0.002	1.288	1.904	5.285	-7.046
16-18 Wood and paper products	-0.432	0.065	1.522	1.359	1.255	-4.661
19 Coke and refined petroleum	-2.828	0.068	2.246	-0.083	7.053	-7.974
20-21 Chemicals	-0.259	0.020	0.905	2.112	13.004	-8.738
22-23 Rubber and plastics	0.072	0.612	1.532	-0.681	2.424	-8.652
24-25 Basic metals	-0.141	0.439	1.534	2.103	6.294	-5.866
26-27 Electrical and optical	3.206	0.053	1.851	16.359	26.709	9.709
28 Machinery and equipment	-0.779	0.762	1.370	-4.151	-0.978	-12.671
29-30 Car and Transport equipment	-1.668	-0.612	1.563	-1.300	2.589	-9.756
31-33 Other manufacturing	0.031	0.158	1.482	-2.691	2.863	-9.860

Table 9: Chg\_Variables (Sector)

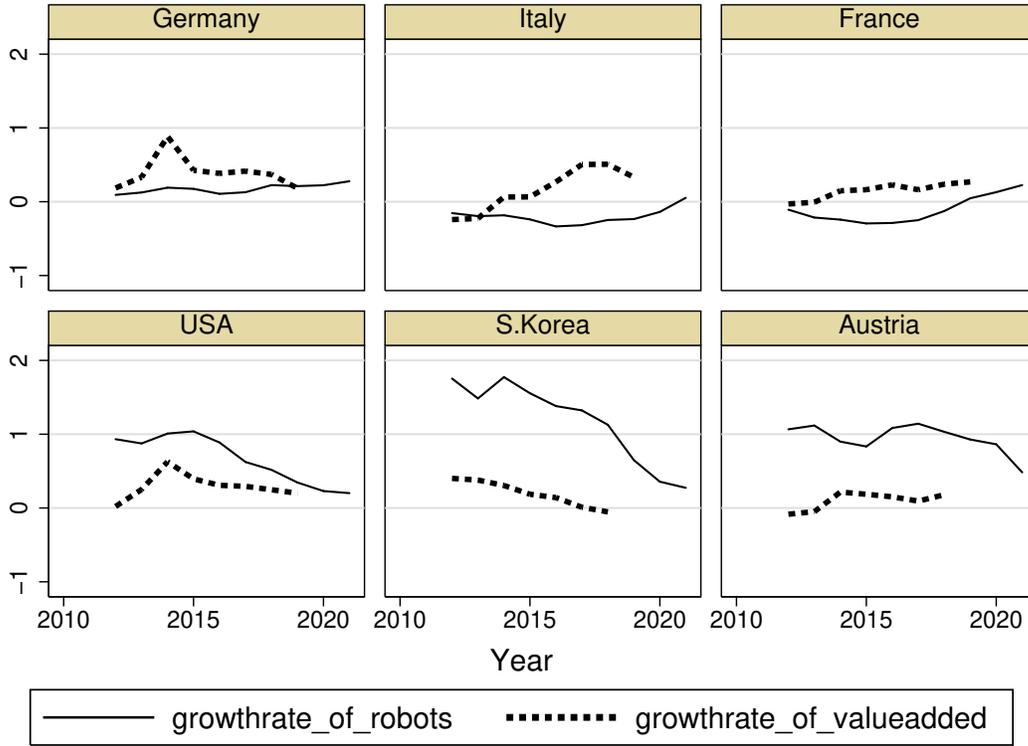
sector	gr_ $S_L^f$	chg_APR	chg_gr gr_ENT	chg_gr _capital price	chg_gr _labor price	chg_gr _robot price
10-12 Food products	0.268	-0.096	2.423	0.790	-0.331	-0.061
13-15 Textiles, wearing apparel	0.092	-0.001	1.910	-0.382	1.032	-0.037
16-18 Wood and paper products	-0.432	-0.015	2.257	-0.272	0.245	-0.025
19 Coke and refined petroleum	-2.828	-0.016	3.330	0.017	1.377	-0.042
20-21 Chemicals	-0.259	-0.005	1.342	-0.423	2.538	-0.046
22-23 Rubber and plastics	0.072	-0.144	2.272	0.137	0.473	-0.046
24-25 Basic metals	-0.141	-0.103	2.275	-0.422	1.228	-0.031
26-27 Electrical and optical	3.206	-0.012	2.744	-3.280	5.213	0.051
28 Machinery and equipment	-0.779	-0.179	2.032	0.832	-0.191	-0.067
29-30 Car and Transport equipment	-1.668	0.144	2.317	0.261	0.505	-0.052
31-33 Other manufacturing	0.031	-0.037	2.198	0.540	0.559	-0.052

The tables reveal patterns not readily discernible through regression results alone. Starting from Table 4 (Excel Sheet 1), we observe that APR is mostly positive. This implies that automation is outpacing value-added growth in most countries and sectors. Meanwhile, gr\_ENT is generally positive, indicating that task indices are increasing over time. Robot prices are predominantly declining, suggesting that robots become more affordable. Contrary to robot trend, capital prices and wages vary across countries and sectors.

Shifting our attention to Table 5 (Excel Sheet 2), in the analysis of chg\_APR, patterns vary by country and industry. For instance, results for the ‘Car and Transport Equipment’ sector show variation between countries. Austria and the USA display negative signs, indicating deeper penetration of robots (APR) –that is, a faster growth of robots compared to value-added in this particular industry. In contrast, countries like Germany, France, and Italy show positive signs, indicating lighter penetration of robots— a slower pace of robots growth relative to value-added in the same industry. Figure 6 further elucidates this trend, revealing that the USA, South Korea, and Austria are experiencing more accelerated robot growth relative to their value-added.

In Table 5, both chg\_APR and chg\_robot price are mostly negative. The results for chg\_gr\_capital prices are mixed, displaying both positive and negative signs across various countries and industries. This suggests a more complex influence of ordinary capital –such as buildings, equipment, and non-robot machinery– on labor share. This distinction underscores the need to consider different types of capital separately when examining their effects on labor share.

Figure 6: Robot and GDP in manufacturing (5-year growth rate)



Graphs by location\_order

As we examine  $chg\_gr\_ENT$ , a distinct pattern becomes apparent:  $chg\_gr\_ENT$  outperforms  $chg\_APR$  in the majority of cases. This indicates that the emergence of new tasks has a more pronounced impact on labor share than automation does. Particularly in the USA, the magnitude of  $chg\_gr\_ENT$  significantly exceeds that of  $chg\_APR$ , signaling a robust innovation landscape in terms of new task development.

Despite the USA's notable innovation in new tasks, it has seen a particularly sharp decline in labor share. We attribute this to the rising market concentration within the country, as detailed by Autor et al. (2020). Additional insights on this can be found in our [online appendix](#), where we provide an analysis showing that this increase in concentration, leading to the decline in labor share, is largely specific to the USA and does not extend to European Union countries. For future research, we recommend an examination of firm-level data in EU countries, possibly utilizing resources like the Amadeus database. This should be complemented by an in-depth study into the influence of automation on market concentration, as initiated by Firooz et al. (2022).

Our accounting analysis reveals that the emergence of new tasks (ENT) has had a

positive impact on labor share, despite the negative effects of increasing automation. This suggests a balancing act between robots and the emergence of new tasks, with the latter currently holding more sway. Tables 6 and 7 illuminate this dominance (Excel Sheets 5 and 6). We obtain these tables by aggregating data to the country level. During this aggregation, we base our calculations on the ‘Average variables’ from Table 4 and use value-added by country  $\times$  sector as weights. We then apply relevant coefficients derived from the regression in Column (2) of Table 2 to generate ‘chg\_variables’.

Lastly, we examine Tables 8 and 9 (Excel Sheets 9 and 10), which are aggregated at the sector level using value-added as weights. Similar to the previous tables, APR generally exhibits positive values, indicating a faster rate of automation relative to the growth of value-added. This trend is most pronounced in the ‘Machinery and Equipment’ sector, which showcases a significantly high APR. In contrast, the ‘Car and Transport Equipment’ sector is the sole sector to record a negative APR. Given the analysis period, which spans from 2005 to 2019, this implies that automation in the ‘Car and Transport’ sector has largely stagnated since 2005. While the rate of automation has increased in many other sectors, this sector appears to have seen a relatively slower pace of technological integration compared to its value-added growth.

It is important to exercise caution in interpreting these results. Specifically, this analysis does not provide information about the absolute level of automation within each sector. Instead, it sheds light on the relative penetration of automation in comparison to value-added growth. That is, a negative APR indicates a slower growth rate of automation relative to value-added growth, not necessarily a low level of automation in absolute terms.

## 6 Concluding Remarks

The objective of this paper is to investigate the underlying causes of the recent decline in labor share, with a particular focus on automation and the emergence of new tasks. While existing studies offer conflicting perspectives (Acemoglu and Restrepo, 2020; Graetz and Michaels, 2018; Dauth et al., 2021; De Vries et al., 2020; Humlum, 2019), our analysis affirms that automation has a negative effect on labor share.

We are the first to investigate the influence of the emergence of new tasks on labor share. Our results indicate that this factor serves as an effective counterbalance to the negative effects of automation on labor share. This observation is especially pertinent in the United States, where the development of new tasks is particularly robust.

We also provide a direct answer to our research question concerning the effects of three price factors —capital price, robot price, and wage— on labor share. We find that capital price is negatively correlated with labor share, while the other factors positively correlate. Specifically, an increase in real wages enhances labor share, whereas a decline in robot prices reduces it. These conclusions are derived from our key finding that the elasticity of substitution between labor and non-robot capital is less than one. Incorporating this into our model allows us to coherently predict the directional influence of these three price factors on labor share, a finding that is consistently corroborated by our regression analysis.

Meanwhile, we would like to clarify that the focus of this paper is not to investigate whether this decline in labor share exacerbates income inequality or necessitates policy interventions. Although some studies have posited a correlation between a declining labor share and increasing income inequality, a more comprehensive examination of causality is necessary. (ILO and OECD, 2015; Torres et al., 2011). As such, we set these topics aside and concentrate on identifying the reasons for the decline within a unified framework.

However, as a policy recommendation, we suggest that governments implement ONET programs aimed at keeping people updated on task requirements for specific occupations. Providing such information will enable individuals to identify emerging labor demands and prepare accordingly, thus improving the alignment between labor supply and demand. This, in turn, could bolster labor share. While the USA is the only country currently offering ONET, the EU has recently initiated a similar project.<sup>26</sup> However, many countries, such as South Korea with its Korea Employment Information Service (KELS), offer job information and matching services but lack ONET-style service.

In the current landscape, our paper shows that while automation contributes to a declining labor share, the introduction of new tasks exerts a significantly more positive impact on labor share. Drawing on our general equilibrium model, we anticipate that in the future, the robot price channel will gain greater importance as the prevalence of robot usage increases.

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<sup>26</sup>The European Commission has recently initiated a project akin to ONET, named 'European Skills, Competences, Qualifications, and Occupations' (ESCO). ESCO has disclosed the tasks required for workers for a single year and has yet to release a Task score.

# A Appendix: Model Derivations

## A.1 Environment

There is a representative household with utility function in Equation (30):

$$U = \left( \int_0^1 Y(k)^{\frac{\eta-1}{\eta}} dk \right)^{\frac{\eta}{\eta-1}}. \quad (30)$$

There are infinite number of identical firms  $i$  with production functions in Equation (33) and (34):

$$t_j(i) = m_j(i) + \gamma_j l_j(i) \text{ if } j \leq I \quad (31)$$

$$t_j(i) = \gamma_j l_j(i) \text{ if } j > I \quad (32)$$

$$T(i) = \left( \int_{N-1}^N t_j(i)^{\frac{\zeta-1}{\zeta}} dj \right)^{\frac{\zeta}{\zeta-1}} \quad (33)$$

$$Y(i) = \left( T(i)^{\frac{\sigma-1}{\sigma}} + K(i)^{\frac{\sigma-1}{\sigma}} \right)^{\frac{\sigma}{\sigma-1}}. \quad (34)$$

By Assumption 1, Equation (31) simplifies to Equation (35). Without this assumption, the algebra becomes too complex to yield a closed-form solution. The implication of this assumption is that whenever robot operation is technically feasible, firms opt for robots over labor. This is because, according to Assumption 1, the cost of using a robot is lower than the cost of labor for unit of production.

$$t_j(i) = m_j(i) \text{ if } j \leq I \quad (35)$$

## A.2 Step 1: derive $P_T$ , and optimal inputs for robot\* and labor\*

We derive  $P_T$ , the price for an aggregated task,  $T(i)$ , by solving the cost minimization problem. We assume perfectly competitive market.

min cost(i) for  $T(i)$  s.t. Equation(35), (32), and (33)

$$\Rightarrow \min \int_{N-1}^I \psi m_j dj + \int_I^N w_j l_j dj \text{ s.t. } \left( \int_{N-1}^I m_j^{\frac{\zeta-1}{\zeta}} dj + \int_I^N (\gamma_j l_j)^{\frac{\zeta-1}{\zeta}} dj \right)^{\frac{\zeta}{\zeta-1}} = T(i)$$

$\Rightarrow$  This finds optimal inputs for robot\* and labor\* to produce T(i)

$\Rightarrow$  Specifically, letting  $T(i)=1$  means the minimization solution is the price for T(i),  $P_T$  :

$$\Rightarrow P_T = \left[ (I - N + 1)\psi^{1-\zeta} + \int_I^N \left( \frac{w_j}{\gamma_j} \right)^{1-\zeta} dj \right]^{\frac{1}{1-\zeta}} \quad (36)$$

### A.3 Step 2: find optimal inputs for $T(i)$ and $K(i)$

Next, we find optimal inputs for  $T(i)$  and  $K(i)$  to produce  $Y(i)$ .

min cost(i) for  $Y(i)$  s.t. Equation(34)

$\Leftrightarrow \min P_T \cdot T(i) + R \cdot K(i)$  s.t. Equation(34)

$\Rightarrow$  This finds optimal inputs for  $T(i)^*$  and  $K(i)^*$  to produce  $Y(i)$

$\Rightarrow$  Specifically, the minimization solution is the minimum cost for producing  $Y(i)$

$$\Rightarrow \begin{cases} T(i)^* = Y(i)P_T^{-\sigma} \\ K(i)^* = Y(i)R^{-\sigma} \\ \text{Cost for } Y(i) = Y(i) [P_T^{1-\sigma} + R^{1-\sigma}]^{\frac{1}{1-\sigma}} \\ \quad = Y(i) \times AC \\ \quad = Y(i) \end{cases}$$

We let  $[P_T^{1-\sigma} + R^{1-\sigma}]^{\frac{1}{1-\sigma}} = 1$  as a numeraire. This numeraire significantly simplifies the algebraic complexity. Since we let  $AC = 1$ ,  $MC$  is also one.

### A.4 Step 3: find a demand function for $Y(i)$

Next, we find a demand function for  $Y(i)$  by minimizing consumption cost.

min cost for consumption s.t. Equation(30)

$\Leftrightarrow \min \int_0^1 P(i)Y(i)di$  s.t. Equation(30)

$\Rightarrow$  Specifically, this yields a demand function for  $Y(i)$

$$\Leftrightarrow Y(i) = \left( \frac{P(i)}{\mathbb{P}} \right)^{-\eta}, \text{ where } \mathbb{P} \equiv \left[ \int_0^1 P(i)^{1-\eta} di \right]^{\frac{1}{1-\eta}}$$

### A.5 Step 4: find firm(i)'s profit

The final goods market is the monopolistic competition that allows firms' positive profit. Until now, we know two things: (1) a demand function for  $Y(i)$ , and (2) the minimum cost for producing  $Y(i)$ . Firm's profit maximization problem yields:

$$P(i)^* = \frac{\eta}{\eta - 1}$$

$$\Rightarrow \Pi(i) = \frac{1}{\eta - 1} Y(i)^*$$

Meanwhile, we naturally get optimal  $Y(i)$  as below, but this is redundant for this paper.

$$Y(i)^* = \left( \frac{\eta}{(\eta-1)\mathbb{P}} \right)^{-\eta}, \text{ where } \mathbb{P} \equiv \left[ \int_0^1 P(i)^{1-\eta} di \right]^{\frac{1}{1-\eta}}$$

### A.6 Step 5: derive the labor cost for producing optimal $Y(i)$

In Step 1, we already found optimal inputs of  $l_j(i)$  to produce  $T(i)$ . Therefore we can also know the optimal labor cost at task  $j$  for firm  $i$  to produce  $T(i)$ .

$$\begin{aligned} l_j(i)^* &= \left( \frac{W_j(i)}{\gamma_j P_T} \right)^{-\zeta} \gamma_j^{-1} T(i) \\ \Rightarrow W_j(i) l_j(i)^* &= \left( \frac{W_j(i)}{\gamma_j} \right)^{1-\zeta} P_T^\zeta T(i) \end{aligned}$$

And we also derived optimal  $T(i)$  while in Step 2:  $T(i)^* = Y(i) P_T^{-\sigma}$ . Plugging in this to the equation above,

$$W_j(i) l_j(i)^* = \left( \frac{W_j(i)}{\gamma_j} \right)^{1-\zeta} P_T^{\zeta-\sigma} Y(i)$$

Therefore, the optimal labor cost for firm  $i$  to produce  $Y(i)$  by using every task from  $I$  to  $N$  is:

$$\begin{aligned} \int_I^N W_j(i) l_j(i)^* dj &= \int_I^N \left( \frac{W_j(i)}{\gamma_j} \right)^{1-\zeta} P_T^{\zeta-\sigma} Y(i) dj \\ &= \int_I^N \left( \frac{W_j(i)}{\gamma_j} \right)^{1-\zeta} dj \cdot P_T^{\zeta-\sigma} Y(i) \end{aligned}$$

### A.7 Step 6: derive an expression for labor share

Until now, we have figured out (1) labor cost, (2) total cost, and (3) profit. Putting all together, we find labor share. Since we prefer not to focus on  $\frac{\eta-1}{\eta}$ , we move this term to the left-hand side.

$$\begin{aligned} S_L(i) &= \frac{\text{Labor cost}(i)}{\text{Total cost}(i) + \text{Profit}(i)} = \frac{\text{Labor cost}(i)}{Y(i) + \frac{1}{\eta-1} Y(i)} \\ &= \frac{\eta-1}{\eta} \frac{\text{Labor cost}(i)}{\text{Total cost}(i)} \\ \Leftrightarrow \frac{\eta}{\eta-1} S_L(i) &= \frac{\text{Labor cost}(i)}{\text{Total cost}(i)} \\ &\equiv S_L^f(i) \end{aligned}$$

After substituting the expressions for Labor cost(i) and Total cost(i) that we derived earlier, we finally construct a detailed expression for  $S_L^f(i)$ .

$$\begin{aligned}
S_L^f(i) &= \frac{\text{Labor cost}(i)}{\text{Total cost}(i)} \\
&= \frac{\int_I^N W_j(i)l_j(i)dj}{Y(i)} \\
&= \frac{\int_I^N W_j(i)l_j(i)dj}{P_T T(i) + RK(i)} \\
&= \frac{\int_I^N \left(\frac{W_j(i)}{\gamma_j}\right)^{1-\zeta} dj \cdot P_T^{\zeta-\sigma} Y(i)}{P_T^{1-\sigma} Y(i) + R^{1-\sigma} Y(i)} \\
&= \frac{\int_I^N \left(\frac{W_j(i)}{\gamma_j}\right)^{1-\zeta} dj}{P_T^{1-\zeta}} \frac{P_T^{1-\sigma}}{P_T^{1-\sigma} + R^{1-\sigma}} \\
&\quad , \text{ where } P_T \equiv \left[ (I - N + 1)\psi^{1-\zeta} + \int_I^N \left(\frac{W_j}{\gamma_j}\right)^{1-\zeta} dj \right]^{\frac{1}{1-\zeta}}
\end{aligned}$$

## B Appendix: Derivation of $\mu$

Let  $\mu$  denote the elasticity of substitution between labor and non-robot capital. We have two layers of production fuctions:

$$Y(i) = \left( T(i)^{\frac{\sigma-1}{\sigma}} + K(i)^{\frac{\sigma-1}{\sigma}} \right)^{\frac{\sigma}{\sigma-1}} \quad (37)$$

$$T(i) = \left( \int_{N-1}^N t_j(i)^{\frac{\zeta-1}{\zeta}} dj \right)^{\frac{\zeta}{\zeta-1}} \quad (38)$$

, where  $T(i)$  and  $K(i)$  represent ‘the number of aggregated tasks’ and ‘capital’ used for the production of the final good  $i$ , denoted as  $Y(i)$ . Tasks,  $t_j(i)$  are as follows:

$$t_j(i) = m_j(i) + \gamma_j l_j(i) \quad \text{if } j \leq I \quad (39)$$

$$t_j(i) = \gamma_j l_j(i) \quad \text{if } j > I \quad (40)$$

With Assumption 1 in Model section, Equation (39) becomes Equation (41):

$$t_j(i) = m_j(i) \quad \text{if } j \leq I \quad (41)$$

Combining Equations (38), (40), and (41), we get Equation (42):

$$T(i) = \left( \int_{N-1}^I m_j(i)^{\frac{\zeta-1}{\zeta}} dj + \int_I^N (\gamma_j l_j(i))^{\frac{\zeta-1}{\zeta}} dj \right)^{\frac{\zeta}{\zeta-1}} \quad (42)$$

Next, we assume  $\lim_{\zeta \rightarrow 1}$  and convert Equation (42) to Equation (43) below:

$$\exp \left\{ \int_{N-1}^I \ln m_j dj + \int_I^N \ln(\gamma_j l_j) dj \right\}. \quad (43)$$

Under the Cobb-Douglas production function, it is necessary to derive  $P_T$ , which will differ from the  $P_T$  derived in the CES case. Essentially, we will do the same procedure of Step 1 in Appendix A except that we now use Cobb-Douglas production function (Equation 43).

$$\min \int_{N-1}^I \psi m_j dj + \int_I^N w_j l_j dj \quad \text{s.t. Equation(43)} = 1 \quad (44)$$

We derive optimal  $l_j^*$  and  $m_j^*$  as follows:

$$\forall j, \quad m_j^* = m = \frac{1}{\psi^{N-1}} \prod_I^N \frac{w_j}{\gamma_j} \quad (45)$$

$$\forall j, \quad l_j^* = \frac{\psi^{I-N+1}}{w_j} \prod_I^N \frac{w_j}{\gamma_j} \quad (46)$$

Plugging in  $m_j^*$  and  $l_j^*$  into  $\int_{N-1}^I \psi m_j dj + \int_I^N w_j l_j dj$ , we derive  $P_T$ :

$$P_T = \psi^{I-N+1} \prod_I^N \frac{w_j}{\gamma_j} \quad (47)$$

We introduce a parameter  $\beta_j$  to act as a weight for the wage distribution corresponding to each worker indexed by  $j$ . Employing  $\beta_j$  allows us to define a representative wage measure,  $W$ , whose properties we will elucidate in subsequent discussions.

$$w_j \equiv \beta_j W \quad (48)$$

A representative wage,  $W$ , is total labor cost for producing  $Y(i)$  divided by total number of workers to produce  $Y(i)$ :

$$W \equiv \frac{\left( \int_I^N w_j l_j^* dj \right) T(i)}{\left( \int_I^N l_j^* dj \right) T(i)} \quad (49)$$

$$= \frac{N - I}{\int_I^N \frac{1}{w_j} dj} \quad (50)$$

$$= W \frac{N - I}{\int_I^N \frac{1}{\beta_j} dj} \quad (51)$$

$$\therefore \frac{N - I}{\int_I^N \frac{1}{\beta_j} dj} = 1 \quad (52)$$

Hence, it is evident that  $\beta_j$  functions as the weight of the wage pertaining to the individual indexed by  $j$ . It holds that  $\beta_j$  varies with the index  $j$ , oscillating around a value of one:

We make an assumption that an infinitesimal change in the representative wage,  $W$ , does not alter the distribution of the wage weight,  $\beta_j$ . In other words,

**Assumption 2.**  $\forall j, \frac{\partial \beta_j}{\partial W} = 0$

We resume the discussion of  $P_T$  in Equation (47). Inserting  $w_j \equiv \beta_j W$  into the equation yields:

$$P_T = \psi^{I-N+1} \cdot \prod_I^N \left( \frac{\beta_j}{\gamma_j} \right) \cdot W^{N-I} \quad (53)$$

We define  $L(i)$  as total number of workers to produce  $Y(i)$ . Therefore it satisfy the following equation:

$$WL(i) = \int_I^N w_j l_j^* dj \times T(i) \quad (54)$$

Specifically, the term  $WL(i)/P_T T(i)$  represents the share of labor cost in the aggregate task cost for producing  $Y(i)$ :

$$\frac{WL(i)}{P_T T(i)} = \frac{\int_I^N w_j l_j^* dj \times T(i)}{P_T T(i)} \quad (55)$$

$$= N - I \quad (56)$$

This result confirms the well-known property of Cobb-Douglas function that the share of costs that goes to labor is always equal to the power of the Cobb-Douglas function,  $N - I$ .

From the equation discussed above, we derive the expression for  $L(i)$ :

$$L(i) = (N - I) \frac{P_T T(i)}{W} \quad (57)$$

, where  $T(i)$  is as follows. We detailed this derivation in Step 2 of Appendix A.

$$T(i) = \left( \frac{P_T}{MC} \right)^{-\sigma} Y(i) \quad (58)$$

Combining Equations (57) and (58) yields:

$$L(i) = \frac{(N - I) P_T}{W} \left( \frac{P_T}{MC} \right)^{-\sigma} Y(i). \quad (59)$$

In Step 2 in Appendix A, we derived:

$$K(i) = \left( \frac{R}{MC} \right)^{-\sigma} Y(i). \quad (60)$$

Hence, combining Equations (53), (59), and (60) yields:

$$\frac{L(i)}{K(i)} = (N - I) \psi^{(I-N+1)(1-\sigma)} \left( \prod_I^N \frac{\beta_j}{\gamma_j} \right)^{1-\sigma} \left( \frac{R^\sigma}{\mathbb{W}^{1-(N-I)(1-\sigma)}} \right) \quad (61)$$

$$= \alpha \left( \frac{R^\sigma}{\mathbb{W}^{1-(N-I)(1-\sigma)}} \right) \quad (62)$$

, where we denote  $\alpha \equiv (N - I) \psi^{(I-N+1)(1-\sigma)} \left( \prod_I^N \frac{\beta_j}{\gamma_j} \right)^{1-\sigma}$  for notational convenience. This is without loss of generality because  $\alpha$  is not a function of  $R$  or  $\mathbb{W}$ .

Finally, we denote  $\mu$  as the elasticity of substitution between non-robot capital and labor:

$$\mu \equiv \frac{d\alpha \left( \frac{R^\sigma}{\mathbb{W}^{1-(N-I)(1-\sigma)}} \right) \frac{\frac{R}{\mathbb{W}}}{\alpha \left( \frac{R^\sigma}{\mathbb{W}^{1-(N-I)(1-\sigma)}} \right)}}{d \left( \frac{R}{\mathbb{W}} \right)} \quad (63)$$

$$= \frac{d \left( \frac{R^\sigma}{\mathbb{W}^{1-(N-I)(1-\sigma)}} \right) \frac{\frac{R}{\mathbb{W}}}{\left( \frac{R^\sigma}{\mathbb{W}^{1-(N-I)(1-\sigma)}} \right)}}{d \left( \frac{R}{\mathbb{W}} \right)} \quad (64)$$

$$\Rightarrow \sigma \text{ if } N - I = 1.$$

## C Appendix: Acemoglu and Restrepo (2019)

Let me first introduce their notations in Table 10.

The decomposition starts from the percent change in the wage bill normalized by population (Equation (AR1)). Since  $\ln \left( \frac{W_t L_t}{N_t} \right)$  can be expressed as  $\ln \left( Y_t \sum_i \chi_{it} s_{it}^L \right)$ , Equation (AR1) can be decomposed as Equation (AR2);

Table 10

Notation	Meaning
$i$	Industry sector
$P_i$	The price of the goods produced by sector $i$
$Y_i$	Output (value added) of sector $i$
$Y = \sum_i P_i Y_i$	Total value added (GDP) in the economy
$\chi_i = \frac{P_i Y_i}{Y} = \frac{P_i Y_i}{\sum_i P_i Y_i} = \frac{GDP_i}{GDP}$	The share of sector $i$ 's GDP
$W_i$	Wage per worker in sector $i$
$L_i$	Number of workers in sector $i$
$W_i L_i$	Total wage bill in sector $i$
$WL = \sum_i W_i L_i$	Total wage bill in the economy
$\ell_i = \frac{W_i L_i}{WL}$	The share of the wage bill in sector $i$
$s_i^L = \frac{W_i L_i}{P_i Y_i} = \frac{\text{Total wage bill}_i}{GDP_i}$	The labor share in sector $i$
$S^L = \frac{WL}{Y} = \frac{\text{Total wage bill}}{GDP}$	The labor share in the economy
$\Gamma_i = \Gamma(N_i, I_i)$	The task content of production with regards to labor in sector $i$
$\gamma_i^L$	The comparative advantage schedules for labor in sector $i$
$\gamma_i^K$	The comparative advantage schedules for capital in sector $i$

$$\ln \left( \frac{W_t L_t}{N_t} \right) - \ln \left( \frac{W_{t0} L_{t0}}{N_{t0}} \right) \quad (\text{AR1})$$

$$= \ln \left( \frac{Y_t}{N_t} \right) - \ln \left( \frac{Y_{t0}}{N_{t0}} \right) \quad (\text{AR2})$$

$$+ \ln \left( \sum_i \chi_{it} s_{it}^L \right) - \ln \left( \sum_i \chi_{it0} s_{it0}^L \right)$$

$$= \ln \left( \frac{Y_t}{N_t} \right) - \ln \left( \frac{Y_{t0}}{N_{t0}} \right)$$

$$+ \ln \left( \sum_i \chi_{it} s_{it}^L \right) - \ln \left( \sum_i \chi_{it0} s_{it}^L \right)$$

$$+ \ln \left( \sum_i \chi_{it0} s_{it}^L \right) - \ln \left( \sum_i \chi_{it0} s_{it0}^L \right)$$

$$\approx \ln \left( \frac{Y_t}{N_t} \right) - \ln \left( \frac{Y_{t0}}{N_{t0}} \right)$$

$$+ \sum_i \frac{s_{it}^L}{\sum_j \chi_{jt0} s_{jt}^L} (\chi_{it} - \chi_{it0})$$

$$+ \ln \left( \sum_i \chi_{it0} s_{it}^L \right) - \ln \left( \sum_i \chi_{it0} s_{it0}^L \right)$$

$$\approx \ln \left( \frac{Y_t}{N_t} \right) - \ln \left( \frac{Y_{t0}}{N_{t0}} \right) \quad (\text{AR3})$$

$$+ \sum_i \frac{s_{it}^L}{\sum_j \chi_{jt0} s_{jt}^L} (\chi_{it} - \chi_{it0})$$

$$+ \sum_i \ell_{it0} (\ln s_{it}^L - \ln s_{it0}^L) \quad (\text{AR4})$$

The first-order Taylor expansion of the last term of Equation (AR3) yields Equation (AR5); Denote  $(1 - \sigma)(1 - s_{it0}^L) \left( \ln \frac{W_{it}}{W_{it0}} - \ln \frac{R_{it}}{R_{it0}} - g_{i,t0,t}^A \right)$  as **Substitution<sub>*i,t0,t*</sub>**, we can rewrite Equation (AR5) as AR8; Denote  $(\ln s_{it}^L - \ln s_{it0}^L) - \text{Substitution}_{i,t0,t}$  as **ChangeTaskContent<sub>*i,t0,t*</sub>**, we can rewrite Equation (AR8) as (AR9).

$$\approx \ln \left( \frac{Y_t}{N_t} \right) - \ln \left( \frac{Y_{t0}}{N_{t0}} \right) \quad (\text{AR5})$$

$$+ \sum_i \frac{s_{it}^L}{\sum_j \chi_{jt0} s_{jt}^L} (\chi_{it} - \chi_{it0})$$

$$+ \sum_i \ell_{it0} \left[ (1 - \sigma)(1 - s_{it0}^L) \left( \ln \frac{W_{it}}{W_{it0}} - \ln \frac{R_{it}}{R_{it0}} - g_{i,t0,t}^A \right) \right] \quad (\text{AR6})$$

$$\left. + \frac{1 - s_{it0}^L}{1 - \Gamma_{it0}} (\ln \Gamma_{it} - \ln \Gamma_{it0}) \right] \quad (\text{AR7})$$

$$\approx \ln \left( \frac{Y_t}{N_t} \right) - \ln \left( \frac{Y_{t0}}{N_{t0}} \right)$$

$$+ \sum_i \frac{s_{it}^L}{\sum_j \chi_{jt0} s_{jt}^L} (\chi_{it} - \chi_{it0})$$

$$+ \sum_i \ell_{it0} \left[ \text{Substitution}_{i,t0,t} \right.$$

$$\left. + \frac{1 - s_{it0}^L}{1 - \Gamma_{it0}} (\ln \Gamma_{it} - \ln \Gamma_{it0}) \right]$$

$$\approx \ln \left( \frac{Y_t}{N_t} \right) - \ln \left( \frac{Y_{t0}}{N_{t0}} \right) \quad (\text{AR8})$$

$$+ \sum_i \frac{s_{it}^L}{\sum_j \chi_{jt0} s_{jt}^L} (\chi_{it} - \chi_{it0})$$

$$+ \sum_i \ell_{it0} \left[ \text{Substitution}_{i,t0,t} \right.$$

$$\left. + (\ln s_{it}^L - \ln s_{it0}^L) - \text{Substitution}_{i,t0,t} \right]$$

$$\begin{aligned}
&\approx \ln\left(\frac{Y_t}{N_t}\right) - \ln\left(\frac{Y_{t0}}{N_{t0}}\right) && \text{(AR9)} \\
&+ \sum_i \frac{s_{it}^L}{\sum_j \chi_{jt0} s_{jt}^L} (\chi_{it} - \chi_{it0}) \\
&+ \sum_i \ell_{it0} \left[ \text{Substitution}_{i,t0,t} \right. \\
&\quad \left. + \text{ChangeTaskContent}_{i,t0,t} \right] \\
&\approx \ln\left(\frac{Y_t}{N_t}\right) - \ln\left(\frac{Y_{t0}}{N_{t0}}\right) \\
&+ \sum_i \frac{s_{it}^L}{\sum_j \chi_{jt0} s_{jt}^L} (\chi_{it} - \chi_{it0}) \\
&+ \text{Substitution}_{t0,t} \\
&+ \sum_i \ell_{it0} \left[ \text{ChangeTaskContent}_{i,t0,t} \right]
\end{aligned}$$

$\sum_i \ell_{it0} [\text{ChangeTaskContent}_{i,t0,t}]$  can be decomposed again into Equation (AR10), assuming that over five-year windows, an industry engages in either automation or the creation of new tasks but not in both activities.

$$\begin{aligned}
\text{Displacement}_{t-1,t} &= \sum_{i \in \mathcal{I}} \ell_{i,t0} \min \left\{ 0, \frac{1}{5} \sum_{\gamma=t-2}^{t+2} \text{ChangeTaskContent}_{i,\gamma-1,\gamma} \right\} && \text{(AR10)} \\
\text{Reinstatement}_{t-1,t} &= \sum_{i \in \mathcal{I}} \ell_{i,t0} \max \left\{ 0, \frac{1}{5} \sum_{\gamma=t-2}^{t+2} \text{ChangeTaskContent}_{i,\gamma-1,\gamma} \right\}
\end{aligned}$$

To sum up, starting from Equation (AR1), it can be decomposed into 1) productivity, 2) composition, 3) substitution, 4) displacement, and 5) reinstatement effects.

$$\begin{aligned}
&\ln\left(\frac{W_t L_t}{N_t}\right) - \ln\left(\frac{W_{t0} L_{t0}}{N_{t0}}\right) && \text{[Wage bill per capita]} && \text{(AR11)} \\
&\approx \ln\left(\frac{Y_t}{N_t}\right) - \ln\left(\frac{Y_{t0}}{N_{t0}}\right) && \text{[Productivity effect]} \\
&+ \sum_i \frac{s_{it}^L}{\sum_j \chi_{jt0} s_{jt}^L} (\chi_{it} - \chi_{it0}) && \text{[Composition effect]} \\
&+ \text{Substitution}_{t0,t} && \text{[Substitution effect]} \\
&+ \text{Displacement}_{t0,t} && \text{[Displacement effect (Automation)]} \\
&+ \text{Reinstatement}_{t0,t} && \text{[Reinstatement effect (New tasks)]}
\end{aligned}$$

## D Appendix: Generation of ENT

Our detailed work differs from that of Acemoglu and Restrepo (2019) in several ways. They generated a ‘Task score’ only for 2018, whereas we generated it on a yearly basis. Additionally, they provided their version of the ENT variable only for the year 2018 in the USA, while our ENT varies by country×year (and industry×year in the USA).

Our matching procedure from ‘Task score’ to the US Census also differs. They convert the ‘Task score’ from SOC to OCC. In contrast, we use SOC as it is. The US Census provides both SOC and OCC for occupational taxonomy, allowing us to simply use SOC to match the US Census with the ‘Task score’.

Moreover, when matching ‘Task score’ to EU-LFS, using SOC is more advantageous than using OCC. EU-LFS uses ISCO for occupational taxonomy, and ISCO (4-digits) matches with SOC (6-digits).<sup>27</sup> This granular level of crosswalk matching is made possible by the recent work of Frugoli and ESCO (2022). They used machine learning and natural language processing for the initial matching, followed by human experts cross-checking to generate the final crosswalks.

## E Appendix: Why AR’s comparison was insignificant

We argue that the reason for their insignificant result is that they used just one time point (2018) and compared the ‘inferred emergence of new tasks’ across industries. In contrast, our comparison utilized yearly variation.

As we will explain carefully now, the size of ‘inferred emergence of new tasks’ across industries at a given point in a year has no meaningful interpretation. Equation (AR10) in Appendix C clearly demonstrates this. For simplicity, let’s assume that  $l_{i,t0}$  are equal across industries. Suppose there are five subsectors within, say, the automotive industry, and we focus on just one year. Suppose the ‘change in task contents’ in the automotive industry is given as Table 11. Then the ‘inferred emergence of new tasks’ for the automotive industry is 6, and ‘inferred Automation’ is 8. It is important to note that each sector’s ‘change in task contents’ is the result of combining (summing) ‘inferred emergence of new tasks’ and ‘inferred Automation’ in its sub-subcategory. For example, the ‘change in task contents’ for Sector A in this instance was -7, which would be a combination of 2 and -9. What if, in Sector A, the ‘change in task contents’

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<sup>27</sup>The excel file for the crosswalk between ISCO and SOC is in this [link](#). This is publicly released by ONET and ESCO.

is -2, which was a combination of 30 and -32? Even though -7 is larger than -2, the ‘inferred emergence of new tasks’ and ‘inferred Automation’ in the subcategory of Sector A were much larger in the case of -2. This case is shown in the second row of Table 11, which yields ‘inferred emergence of new tasks’ as 1.6 and ‘inferred Automation’ as -1.8. Comparing the two examples (in the first and second rows), ‘inferred emergence of new tasks’ in the first row is larger than in the second row. However, it does not mean that the automotive industry has lower ‘inferred emergence of new tasks’ in the second row. Therefore, the inference method by AR is meaningful only as the relative size between ‘inferred emergence of new tasks’ and ‘inferred Automation’ (the first row is  $\frac{6}{6+8} = 0.43$  and the second row is  $\frac{1.6}{1.6+1.8} = 0.47$ ). Additionally, it is meaningful in the relative size across years. For example, for the automotive industry, when did it experience a rapid increase, and when was it flat? However, it is crucial to understand that it is not meaningful across industries at a given year. This is why our version of the comparison removed the fixed effects and used only error terms.

Table 11: Example for Equation (AR10)

Decomposition result		⇒	Inferred conclusion	
Sectors	Change in task contents in labor		Inferred Emerging new tasks	Inferred Automation
A	-7		0	-7
B	20		20	0
C	-3		0	-3
D	10		10	0
E	-30		0	-30
			6	-8

Decomposition result		⇒	Inferred conclusion	
Sectors	Change in task contents in labor		Inferred Emerging new tasks	Inferred Automation
A	-2		0	-2
B	5		5	0
C	-1		0	-1
D	3		3	0
E	-6		0	-6
			1.6	-1.8

## F Appendix: Quantile without restriction

Only quantile regressions are different from Table 2.

Table 12: Regressions

	OLS	OLS	NLS	GMM	Quantile		
	(1)	(2)	(3)	(4)	(5)	(6)	(7)
Restriction	No	Yes	Yes	Yes	No	No	No
Quantile					0.2	0.5	0.8
$\alpha_1$ : APR	-0.261* (0.113)	-0.235* (0.110)	-0.235* (0.110)	-0.178 (0.102)	-0.260*** (0.072)	-0.129 (0.080)	-0.061 (0.054)
$\alpha_2$ : gr_ENT	1.468*** (0.372)	1.483*** (0.372)	1.483*** (0.372)	1.535*** (0.348)	0.511*** (0.076)	0.524*** (0.083)	0.414*** (0.069)
$\alpha_3$ : gr_labor price	20.200*** (2.387)	19.520*** (2.522)	19.520*** (2.522)	20.411*** (2.604)	13.182*** (0.543)	16.124*** (0.530)	16.962*** (0.362)
$\alpha_4$ : gr_robot price	1.016 (2.650)	0.529 (2.950)	0.529 (2.950)	4.424 (2.495)	4.065*** (1.011)	5.117*** (0.694)	3.899*** (0.432)
$\alpha_5$ : gr_capital price	-23.536*** (3.133)	-20.048*** (3.831)	-20.048*** (3.831)	-24.834*** (3.442)	-18.715*** (1.108)	-21.623*** (0.885)	-22.054*** (0.636)
$N$	1027	1027	1027	1027	1027	1027	1027
$R^2$	0.565	0.563	0.563				
pseudo $R^2$				0.386	0.541	0.445	0.579

Standard errors in parenthesis are heteroskedasticity-robust

\*  $p < 0.05$ , \*\*  $p < 0.01$ , \*\*\*  $p < 0.001$

The coefficients and the standard errors have been multiplied by 100 for better readability.

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