Revisiting Néel 60 years on: The magnetic anisotropy of L1₀ FeNi (tetrataenite) **p**

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ABSTRACT

The magnetocrystalline anisotropy energy of atomically ordered $L1_0$ FeNi (the meteoritic mineral tetrataenite) is studied within a firstprinciples electronic structure framework. Two compositions are examined: equiatomic Fe_{0.5}Ni_{0.5} and an Fe-rich composition, Fe_{0.56}Ni_{0.44}. \bigotimes It is confirmed that, for the single crystals modeled in this work, the leading-order anisotropy coefficient K_1 dominates the higher-order of coefficients K_2 and K_3 . To enable comparison with experiment, the effects of both imperfect atomic long-range order and finite temperature are included. While our computational results initially appear to undershoot the measured experimental values for this system, careful scrutiny of the original analysis due to Néel *et al.* [J. Appl. Phys. **35**, 873 (1964)] suggests that our computed value of K_1 is, in fact, consistent with experimental values, and that the noted discrepancy has its origins in the nanoscale polycrystalline, multivariant nature of experimental samples, that yields much larger values of K_2 and K_3 than expected *a priori*. These results provide fresh insight into the existing discrepan- $\frac{12}{3}$ cies in the literature regarding the value of tetrataenite's uniaxial magnetocrystalline anisotropy in both natural and synthetic samples.

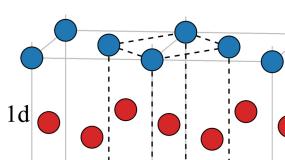
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I. INTRODUCTION

Permanent magnets are of critical importance in many technological applications, prime examples being in electrical power generation and electric motors that are essential in the transition to a low-carbon future. At present, the vast majority of permanent magnets used for advanced applications contain significant amounts of rare-earth elements such as samarium and neodymium,¹ with examples being SmCo₅² and Nd₂Fe₁₄B;^{3,4} the latter compound also requires incorporation of rare and expensive dysprosium and/or terbium for robust high-temperature performance. These rare-earth elements are a constrained resource accompanied by concerns around price volatility and the long-term stability of the global supply chain.^{5,6} There are also concerns over the environmental impact of their extraction⁷ and processing. Overall, these conditions motivate a globally concerted effort to develop rare-earth-free permanent magnets for use in advanced applications. One such candidate under consideration is atomically ordered Fe-Ni that crystallizes in the tetragonal $L1_0$ structure.⁸ (The $L1_0$ structure is visualized in Fig. 1.) This compound, which is naturally found in extremely slowly cooled metallic meteorites, is also referred to as tetrataenite.⁹

Although there are significant challenges associated with its formation that arise from a low atomic ordering temperature and sluggish kinetics,¹⁰ the L1₀ phase is thermodynamically stable relative to its atomically disordered, face-centered-cubic (fcc) counterpart, and a number of attempts have been made to synthesize it in the laboratory.^{10–23} Tetrataenite is known, both from experimental measurements^{10–24} and from theoretical calculations,^{25–31} to possess a sufficiently large uniaxial magnetocrystalline anisotropy energy (MAE) to be useful as a "gap magnet,"³² with anticipated performance below that of the rare-earth magnets but above that of oxide ferrite magnets.

To date, computational modeling of tetrataenite's magnetocrystalline anisotropy has focused on evaluating its uniaxial anisotropy energy, K_U , which is the difference in energy between the system magnetized in the $\hat{\mathbf{z}}$ direction compared to that along the $\hat{\mathbf{x}}$



1a

FIG. 1. Visualization of the L1₀ ordered structure imposed on a face-centered tetragonal lattice. The conventional simple tetragonal cell, with 1a sites at the corners and a 1d site at the center, is indicated by dashed black lines. The simple tetragonal unit cell has lattice parameters c' = c, $a' = b' = a/\sqrt{2}$, where *a* and *c* are the face-centered tetragonal lattice parameters. Perfectly ordered L1₀ Fe_{0.5}Ni_{0.5} has all 1a (blue) sites occupied by Fe atoms, and all 1d (red) sites occupied by Ni atoms. The disordered Fe_{0.5}Ni_{0.5} alloy in which every site is occupied with a 50% probability of either Fe or Ni has a face-centered cubic lattice with c = a.

direction, rather than resolving it into its separate coefficients, i.e., $K_U = K_1 + K_2 + K_3$. In addition, these calculations have primarily focused on the equiatomic binary composition, Fe_{0.5}Ni_{0.5}, at T = 0 K and with perfect atomic order.^{25–31} However, experimental measurements of this material's magnetocrystalline anisotropy are invariably performed at finite temperature (typically room temperature) on samples with *imperfect* atomic order.^{10–19,22,24,33} (A summary of the

experimental data can be found in Table I.) These factors are significant, because both decreasing atomic long-range order and increasing temperature reduce the magnetocrystalline anisotropy of $L1_0$ materials.^{34–36}

Computational predictions²⁵⁻³¹ give an MAE for L1₀ $Fe_{0.5}Ni_{0.5}$ in the range of 0.23–0.78 MJ m⁻³, while experimental observations^{10–16,18,19,22,24} fall in the range of 0.2–0.93 MJ m⁻³. Although at first glance there appears to be consistency between experiment and theory, we again emphasise that theoretical calculations are performed at T = 0 K on systems with perfect atomic order, while experimental measurements are performed at room temperature on samples with imperfect atomic order. Further analysis of the experimental data^{8,10,27} has suggested that the MAE of this material could reach the range of 1.0-1.3 MJ m⁻³. Typically, ab initio estimates of MAE values for L10 transition-metal/noblemetal systems have been in good agreement with the corresponding experimental data, for example for FePd,³⁷ FePt,^{34,35,37,38} and CoPt,³⁸ where the *ab initio* values for idealized systems tend to, if anything, slightly overestimate MAE values. The discrepancy between experimental and computational results for FeNi is therefore striking, and we suggest that it highlights a gap in understanding of the underlying physical origin of magnetocrystalline anisotropy in this material.

In addition, we note that almost all computational studies, and most experiments, do not resolve the anisotropy energy into its separate coefficients, K_1 , K_2 , and K_3 . These coefficients have their origins in the symmetry of the underlying crystal structure. For a tetragonal crystal structure, K_1 is the leading (second-order) term go in an expansion of the magnetocrystalline anisotropy energy, while K_2 and K_3 are higher-order (fourth order) terms.³⁹ Significantly, the two seminal works on this material by Néel *et al.*¹⁰ and Paulevé *et al.*¹¹ do indeed provide values for these separate K_2 and K_3 coefficients but they are unusually large for a uniaxial material. These large values of K_2 and K_3 are noted to make a significant contribution to the total uniaxial anisotropy coefficient, K_U .

TABLE I. Experimental measurements of the magnetocrystalline anisotropy of FeNi, with sample description and atomic order parameter, *S*, where provided. Blank fields in the table indicate values not provided in the associated reference. Uncertainties are quoted where provided in the associated reference. *K*_U denotes the conventional measurement of the uniaxial anisotropy, the difference in energy between a system magnetized in the \hat{z} direction and one magnetized in the \hat{x} direction. We note that the order parameter provided by Néel *et al.* in Ref. 10 is an estimate, rather than a direct measurement.

e Composition lisk) $Fe_{0.5}Ni_{0.5}$ here) $Fe_{0.5}Ni_{0.5}$ $Fe_{0.5}Ni_{0.5}$	<i>S</i> 0.41–0.45 (Estimate) 0.6 ± 0.2	<u>Т (К)</u> 293	<i>K_U</i> 0.55 0.55	<i>K</i> ₁ 0.32	<i>K</i> ₂ 0.23	<i>K</i> ₃
here) $Fe_{0.5}Ni_{0.5}$		293		0.32	0.23	
	0.6 ± 0.2		0 55			
Fe _{0.5} Ni _{0.5}	0.6 ± 0.2		0.55	0.3	0.17	0.08
	0.0 ± 0.2	Room T.	0.63			
Fe _{0.5} Ni _{0.5}	0.33	Room T.	0.58			
Fe _{0.5} Ni _{0.5}	0.5 ± 0.1	Room T.	0.50 ± 0.01			
Fe _{0.5} Ni _{0.5}	0.48 ± 0.05	Room T.	0.70 ± 0.02			
Fe _{0.5} Ni _{0.5}	0.4	Room T.	0.7			
Fe _{0.6} Ni _{0.4}	0.2	Room T.	0.93			
Fe _{0.57} Ni _{0.43}			0.84			
Fe _{0.5} Ni _{0.5}		35	< 0.2			
Fe _{0.5} Ni _{0.5}		300	~0.35			
Fe _{0.5} Ni _{0.5}	0.60	Room T.	0.55			
	$\begin{array}{c} Fe_{0.5}Ni_{0.5}\\Fe_{0.5}Ni_{0.5}\\Fe_{0.5}Ni_{0.5}\\Fe_{0.6}Ni_{0.4}\\Fe_{0.57}Ni_{0.43}\\Fe_{0.57}Ni_{0.5}\\Fe_{0.5}Ni_{0.5}\\Fe_{0.5}Ni_{0.5}\\\end{array}$	$\begin{array}{cccc} Fe_{0.5}Ni_{0.5} & 0.5\pm0.1 \\ Fe_{0.5}Ni_{0.5} & 0.48\pm0.05 \\ Fe_{0.5}Ni_{0.5} & 0.4 \\ Fe_{0.6}Ni_{0.4} & 0.2 \\ Fe_{0.57}Ni_{0.43} \\ Fe_{0.5}Ni_{0.5} \\ Fe_{0.5}Ni_{0.5} \\ Fe_{0.5}Ni_{0.5} \end{array}$	$\begin{array}{c cccc} Fe_{0.5}Ni_{0.5} & 0.5 \pm 0.1 & Room \ T. \\ Fe_{0.5}Ni_{0.5} & 0.48 \pm 0.05 & Room \ T. \\ Fe_{0.5}Ni_{0.5} & 0.4 & Room \ T. \\ Fe_{0.6}Ni_{0.4} & 0.2 & Room \ T. \\ Fe_{0.57}Ni_{0.43} & & \\ Fe_{0.5}Ni_{0.5} & 35 \\ Fe_{0.5}Ni_{0.5} & 300 \end{array}$	$\begin{array}{c ccccc} Fe_{0.5}Ni_{0.5} & 0.5\pm0.1 & Room T. & 0.50\pm0.01 \\ Fe_{0.5}Ni_{0.5} & 0.48\pm0.05 & Room T. & 0.70\pm0.02 \\ Fe_{0.5}Ni_{0.5} & 0.4 & Room T. & 0.7 \\ Fe_{0.6}Ni_{0.4} & 0.2 & Room T. & 0.93 \\ Fe_{0.57}Ni_{0.43} & & 0.84 \\ Fe_{0.5}Ni_{0.5} & 35 & <0.2 \\ Fe_{0.5}Ni_{0.5} & 300 & \sim0.35 \end{array}$	$\begin{array}{c ccccc} Fe_{0.5}Ni_{0.5} & 0.5\pm0.1 & Room T. & 0.50\pm0.01 \\ Fe_{0.5}Ni_{0.5} & 0.48\pm0.05 & Room T. & 0.70\pm0.02 \\ Fe_{0.5}Ni_{0.5} & 0.4 & Room T. & 0.7 \\ Fe_{0.6}Ni_{0.4} & 0.2 & Room T. & 0.93 \\ Fe_{0.57}Ni_{0.43} & & 0.84 \\ Fe_{0.5N}i_{0.5} & 35 & <0.2 \\ Fe_{0.5}Ni_{0.5} & 300 & \sim0.35 \end{array}$	$\begin{array}{c ccccc} Fe_{0.5}Ni_{0.5} & 0.5\pm0.1 & Room T. & 0.50\pm0.01 \\ Fe_{0.5}Ni_{0.5} & 0.48\pm0.05 & Room T. & 0.70\pm0.02 \\ Fe_{0.5}Ni_{0.5} & 0.4 & Room T. & 0.7 \\ Fe_{0.6}Ni_{0.4} & 0.2 & Room T. & 0.93 \\ Fe_{0.57}Ni_{0.43} & & 0.84 \\ Fe_{0.5N}i_{0.5} & 35 & <0.2 \\ Fe_{0.5}Ni_{0.5} & 300 & \sim0.35 \end{array}$

In this work, we address the issues outlined above. We use a fully relativistic, first-principles-based framework to study the magnetocrystalline anisotropy of this system, providing results for both the equiatomic composition Fe0.5Ni0.5 as well as for an Fe-rich composition that is more consistent with experimentally determined composition of tetrataenite in some meteorite samples,^{8,9,40} Fe0.56Ni0.44. We use our modeling framework to study the dependence of the magnetic torque on the direction of magnetization and confirm that the leading-order anisotropy coefficient K_1 dominates higher-order coefficients K_2 and K_3 for the univariant single crystals modeled in this work. We go on to examine the magnetocrystalline anisotropy energy of this compound at finite temperature, and find that its value remains high up to and well beyond room temperature. We also consider the effect of varying long-range atomic order and find that, for both compositions, decreasing atomic order consistently decreases the computationally predicted MAE. Finally, we perform calculations in which the effects of both finite temperature and imperfect atomic ordering are included. From a careful reading of the original analysis due to Néel et al.,¹⁰ we propose that our predicted MAE values for ideal single crystals are consistent with the experimental data, and that it is instead the nanocrystalline, multivariant nature of experimental samples⁴¹ that yield larger values of K_2 and K_3 than expected a priori.

These results have significant implications. First, they provide insight into the discrepancies between measured and predicted anisotropies of this compound in the existing literature, emphasizing that the higher-order anisotropy coefficients K_2 and K_3 appear to make a significant contribution to this material's experimentally observed total uniaxial anisotropy energy. Second, these results demonstrate the impact of varying Fe:Ni ratio on the predicted value of K_1 , and conclude that an equiatomic composition is expected to exhibit superior magnetic performance compared to those of off-stoichiometry compositions. Finally, it is shown that the finite-temperature magnetocrystalline anisotropy of this material is remarkably robust, lending support for its potential use in elevated temperature applications. This work therefore supports renewed contemplation of this compound as a suitable material for advanced magnets.

This paper is structured as follows. In Sec. II, we briefly outline the underlying theory and our methodology for obtaining the MAE from first principles using the torque method as well as provide relevant computational details. Then, in Sec. III, we provide results of our calculations and carefully set them in an experimental context. Finally, in Sec. IV, we summarize our results, venture an outlook on their implications, and suggest possible further work.

II. METHODOLOGY

Our technique for modeling the magnetocrystalline anisotropy energy of a material is based on evaluations of torque when a system is magnetized in a given direction. These torques are obtained by evaluating derivatives of an energy, where the energy is obtained ab initio via density functional theory (DFT) calculations in which relativistic effects, notably spin-orbit coupling, are included.⁴² The method is a numerically robust way of calculating MAE values which are on the scale of 1 meV/atom or smaller. Further, by considering torque as a function of angle, the method enables direct evaluation of the separate anisotropy coefficients K_1 , K_2 , and K_3 , as well as the usual uniaxial anisotropy constant K_U .

We use the Korringa-Kohn-Rostoker (KKR) formulation of DFT and the coherent potential approximation (CPA)⁴³ to describe the effects of partial atomic order.³⁷ In addition, the effects of magnetic fluctuations at finite temperature are included via the disordered local moment (DLM) picture.44

A. Magnetocrystalline anisotropy

The magnetocrystalline anisotropy energy describes the variation in energy of a ferromagnetic system due to a rotation of the magnetization direction. For a ferromagnet with the magnetization direction $\hat{\mathbf{n}}$, the MAE can be expressed as³

$$K = \sum_{\gamma} \kappa_{\gamma} g_{\gamma}(\hat{\mathbf{n}}), \qquad (1)$$

where κ_{γ} denote MAE coefficients and g_{γ} denote spherical harmonics fixing the orientation of $\hat{\mathbf{n}}$ with respect to the crystal axes. It is convenient to represent $\hat{\mathbf{n}}$ in spherical polar coordinates by $\hat{\mathbf{n}} = (\sin\theta\cos\phi, \sin\theta\sin\phi, \cos\theta)$, where θ and ϕ denote polar and azimuthal angles, respectively, in a coordinate frame specified by the crystal axes.

In a tetragonal uniaxial ferromagnet, the MAE is known to be well-described by³

$$K = K_1 \sin^2 \theta + K_2 \sin^4 \theta + K_3 \sin^4 \theta \cos 4\phi, \qquad (2)$$

30 October 2023 14:50:21 where K_1 , K_2 , and K_3 are the conventional anisotropy coefficients The total energy of the system is then written as

$$\mathscr{E}(\hat{\mathbf{n}}) = \mathscr{E}iso + K_1 \sin^2 \theta + K_2 \sin^4 \theta + K_3 \sin^4 \theta \cos 4\phi, \quad (3)$$

where *Eiso* represents the isotropic portion of the energy. The MAE coefficients K_1 , K_2 , and K_3 can be accessed from derivatives of this energy with respect to magnetization directions. Given an energy of the form in Eq. (3), we have that

$$\frac{\partial \mathscr{E}}{\partial \theta} = K_1 \sin 2\theta + 2K_2 \sin 2\theta \sin^2 \theta$$

$$+ 2K_3 \sin 2\theta \sin^2 \theta \cos 4\phi,$$
(4)

$$\frac{\partial \mathscr{E}}{\partial \phi} = -4K_3 \sin^4 \theta \sin 4\phi, \tag{5}$$

and evaluation of these quantities at particular values of θ and ϕ leads directly to the coefficients.

Moreover, the magnetocrystalline anisotropy energy difference between the system magnetized in the \hat{z} and \hat{x} directions,

$$K_U := \mathscr{E}((1, 0, 0)) - \mathscr{E}((0, 0, 1)) = K_1 + K_2 + K_3, \tag{6}$$

is given by the evaluation of the derivative, $\frac{\partial \mathscr{E}}{\partial \theta}$ at $\theta = \frac{\pi}{4}$ and $\phi = 0$ directly, enabling us to obtain the MAE in a one-shot calculation. In practice, for a uniaxial ferromagnet, one expects K_1 to dominate K_2 and K_3 ,³⁹ and the anisotropy is typically written as

$$K = K_1 \sin^2 \theta. \tag{7}$$

B. Evaluating magnetic torques ab initio

To evaluate these derivatives and, therefore, the MAE coefficients, we use an expression from the KKR multiple scattering formalism for the magnetic torque, $^{34,37,45,46}_{4}$

$$\mathbf{T}^{(\hat{\mathbf{n}})} = -\frac{\partial \mathscr{E}^{(\hat{\mathbf{n}})}}{\partial \hat{\mathbf{n}}},\tag{8}$$

in which the effects of finite-temperature local moment fluctuations⁴⁴ can also be included. Using the stationary properties of the relativistic DFT energy $\mathscr{E}^{(\hat{\mathbf{n}})}$ with respect to the charge and magnetization densities, the derivation of the torque begins with the singleelectron energy-sum part of this energy. In terms of the integrated electronic density of states, $N^{(\hat{\mathbf{n}})}(E)$, for a system magnetized along a direction $\hat{\mathbf{n}}$, this energy is written as

$$\mathscr{E}^{(\hat{\mathbf{n}})} = -\int_{-}^{E_F^{(\hat{\mathbf{n}})}} N^{(\hat{\mathbf{n}})}(E) \,\mathrm{d}E.$$
(9)

In multiple scattering theory, the integrated density of states is expressed particularly succinctly using the Lloyd formula^{43,47}

$$N^{(\hat{\mathbf{n}})}(E) = N_0(E) - \frac{1}{\pi} \operatorname{Im} \ln \det\left(\underline{t}(\hat{\mathbf{n}}; E)^{-1} - \underline{\underline{G}}_0(E))\right), \qquad (10)$$

where $\underline{t}(\hat{\mathbf{n}}; E)$ describes an array of single-site-scattering t-matrices (combined into a super matrix in both site and angular momentum space) and $\underline{\underline{G}}_{0}(E)$ specifies the structure constants which contain all the information on the spatial location of the scatterers.⁴³

At a site *i*, the t-matrix describing the scattering of an electron from an effective scalar potential and local magnetic field, aligned with the spin-polarization of the electron density in that region and located in the unit cell surrounding the site, is obtained from the solution of the Dirac equation. This solution is found in a coordinate frame in which the *z* axis of the local coordinate frame is aligned with $\hat{\mathbf{n}}$.^{48,49} A simple transformation produces a t-matrix for the general coordinate frame,

$$\underline{t}_{i}(\hat{\mathbf{n}}; E) = \underline{R}(\hat{\mathbf{n}}) \, \underline{t}_{i}(\hat{\mathbf{z}}; E) \underline{R}(\hat{\mathbf{n}})^{+}, \tag{11}$$

where $\underline{R}(\hat{\mathbf{n}}) = \exp i\alpha_{\hat{\mathbf{m}}}(\hat{\mathbf{m}} \cdot \underline{\mathbf{J}})$, $\alpha_{\hat{\mathbf{m}}}$ is the angle of rotation about an axis $\hat{\mathbf{m}} = \frac{\hat{z} \wedge \hat{\mathbf{n}}}{|\hat{z} \wedge \hat{\mathbf{n}}|}$, and $\underline{\mathbf{J}}$ is the total angular momentum. The torque quantity $T_{\alpha_{\hat{u}}}^{(\hat{\mathbf{n}})} = -\frac{\partial \mathcal{E}^{(\hat{\mathbf{n}})}}{\partial \alpha_{\hat{\mathbf{n}}}}$, describing the variation of the total energy with respect to a rotation of the magnetization about a general axis $\hat{\mathbf{u}}$, is

$$T_{\alpha_{\hat{\mathbf{u}}}}^{(\hat{\mathbf{n}})} = -\frac{1}{\pi} \int_{-\infty}^{E_{F}^{(\hat{\mathbf{n}})}} \operatorname{Im} \frac{\partial}{\partial \alpha_{\hat{\mathbf{u}}}} \Big[\ln \det \Big(\underline{\underline{t}}(\hat{\mathbf{n}}; E)^{-1} - \underline{\underline{G}}_{0}(E) \Big) \Big] dE, \qquad (12)$$

which can be written as³⁷

$$T_{\alpha_{\hat{\mathbf{u}}}}^{(\hat{\mathbf{n}})} = -\frac{1}{\pi} \int_{F}^{F_{F}^{(\hat{\mathbf{n}})}} \operatorname{Im} \sum_{i} \operatorname{Tr} \left(\underline{\tau}_{li}^{(\hat{\mathbf{n}})}(E) \frac{\partial}{\partial \alpha_{\hat{\mathbf{u}}}} \left(\underline{R}(\hat{\mathbf{n}}) \underline{t}(\hat{\mathbf{n}}; E)^{-1} \underline{R}(\hat{\mathbf{n}})^{+} \right) \right) dE,$$
(13)

where the KKR scattering path operator^{43,50} is

$$\underline{\underline{f}}^{(\hat{\mathbf{n}})} = \left(\left(\underline{\underline{f}}^{(\hat{\mathbf{n}})} \right)^{-1} - \underline{\underline{G}}_{0} \right)^{-1}.$$
(14)

Since $\frac{\partial \underline{R}(\hat{\mathbf{n}})}{\partial \alpha_{\hat{\mathbf{u}}}} = i(\underline{\mathbf{J}} \cdot \hat{\mathbf{u}})\underline{R}(\hat{\mathbf{n}})$ and $\frac{\partial \underline{R}(\hat{\mathbf{n}})^{+}}{\partial \alpha_{\hat{\mathbf{u}}}} = -i(\underline{\mathbf{J}} \cdot \hat{\mathbf{u}})\underline{R}(\hat{\mathbf{n}})$, we obtain $T_{\alpha_{\hat{\mathbf{n}}}}^{(\hat{\mathbf{n}})} = \frac{1}{2} \int_{F_{F}}^{E_{F}^{(\hat{\mathbf{n}})}} \operatorname{Im} i \sum_{i} \operatorname{Tr} \left(\underline{\tau}_{ii}^{(\hat{\mathbf{n}})}(E) \left[(\mathbf{J} \cdot \hat{\mathbf{u}}) \underline{t}(\hat{\mathbf{n}}; E)^{-1} - \underline{t}(\hat{\mathbf{n}}; E)^{-1} (\mathbf{J} \cdot \hat{\mathbf{u}}) \right] \right) dH$

$$\Gamma_{\alpha_{\hat{\mathbf{u}}}}^{(\mathbf{n})} = \frac{1}{\pi} \int \operatorname{Im} i \sum_{i} \operatorname{Tr} \left(\underline{\tau}_{ii}^{(\mathbf{n})}(E) \left[(\underline{\mathbf{J}} \cdot \hat{\mathbf{u}}) \underline{t}(\hat{\mathbf{n}}; E)^{-1} - \underline{t}(\hat{\mathbf{n}}; E)^{-1} (\underline{\mathbf{J}} \cdot \hat{\mathbf{u}}) \right] \right) dE.$$
(15)

This closed-form expression enables us to evaluate the torque for a given magnetization direction $\hat{\mathbf{n}}$. By sampling a range of values of θ and ϕ , it is therefore possible to extract values of the coefficients K_1, K_2 , and K_3 separately along with the conventional uniaxial anisotropy, K_U . We note that this technique for evaluating the MAE has previously exhibited exceptional fidelity when applied to other alloys crystallising in the L1₀ structure, giving values in excellent agreement with experimental literature for the FePd³⁷ and FePt³⁴ systems, along with explaining the dependence of the MAE on the long-range atomic order parameter.³⁵ In addition, the method has also been used with success to study a number of rare-earth-based systems^{51,52} and other magnetic grameter.³⁵

C. Computational details

We use the all-electron HUTSEPOT code⁵⁴ to generate selfconsistent, one-electron potentials within the KKR formulation of density functional theory (DFT).43,55 We perform spin-polarized, scalar-relativistic calculations within the atomic sphere approximation $(ASA)^{56}$ with an angular momentum cutoff of lmax = 3 for basis set expansions, a $20 \times 20 \times 20$ k-point mesh for integrals over the Brillouin zone, and employ a 24-point semi-circular Gauss-Legendre grid in the complex plane to integrate over valence energies. We use the local density approximation (LDA) and the exchange-correlation functional of Perdew-Wang.⁵⁷ For all calculations, we use lattice parameters of a = b = 3.560 Å, and c = 3.577 Å, obtained in an earlier first-principles study.²⁹ The c/aratio is 1.0048, consistent with a very low tetragonality. These lattice parameters are broadly consistent with both earlier experimental^{17,33,58,59} and computational^{8,25,26,28} studies. The conventional simple tetragonal (A6) representation of the L1₀ unit cell with a two atom basis is used, as visualized in Fig. 1.

A comment should be made about the suitability of the ASA as used in this work to study the MAE via calculations of the magnetic torque of the FeNi system. The ASA description of the self-consistent potentials of the KKR-CPA formulation of DFT is known to be most suitable for description of close-packed systems.^{49,60} L1₀ FeNi, with its underlying face-centered tetragonal

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lattice and a c/a ratio close to unity, can be classified as closepacked and we therefore believe the ASA to be appropriate. In addition, the relativistic DLM picture required to study finitetemperature effects has only been implemented within a spherical potential approximation, such as the ASA employed in this work. So-called "full potential" schemes, such as those used in Ref. 28, are expected to be necessary to accurately describe more complex crystal structures, especially if the MAE is calculated from direct energy differences rather than the magnetic torque.

Utilization of the inhomogeneous CPA^{61,62} allows observation of the effects of partial atomic order on the predicted MAE. An order parameter S is defined to describe partial Fe-Ni atomic order in our configurations, where S = 1 describes a maximally ordered state, and S = 0 corresponds to a state which is completely disordered and both lattice sites shown in Fig. 1 are equivalent. For the equiatomic composition, Fe_{0.5}Ni_{0.5}, the concentration of Fe on the 1a (1d) site is given by 0.5 + 0.5S (0.5 - 0.5S). For the Fe-rich composition, Fe_{0.56}Ni_{0.44}, the concentration of Fe on the 1a (1d) site is given by 0.56 + 0.44S (0.56 - 0.44S). The Ni concentrations can be inferred as the concentrations of Fe and Ni must sum to unity on all lattice sites.

To compute the MAE of our considered structures, we use the MARMOT code,⁴⁵ which solves the single-site scattering problem on a fully relativistic footing, naturally including spin-orbit effects. The crystal structure for the MARMOT calculations is the same as that used for the HUTSEPOT calculations, and the angular momentum expansion was again truncated at lmax = 3, while the remaining input parameters were left at the MARMOT default values. This includes a 240×40 mesh for angular sampling of the CPA integral and an adaptive scheme for Brilluoin zone integrations. MARMOT is used for both the zero and finite temperature calculations.

III. RESULTS

A. Functional form of the anisotropy: K₁, K₂, and K₃

To explore the functional form of the magnetocrystalline anisotropy, we evaluate the magnetic torque over a range of values of θ and ϕ and fit the *ab initio* data to the form given in Eqs. (4) and (5). Displayed in Table II are our obtained values of K_1 , K_2 , and K_3 for Fe_{0.5}Ni_{0.5} and Fe_{0.56}Ni_{0.44} at T = 0 K with the perfect atomic order parameter S = 1.0. Notably K_1 is almost four orders of magnitude larger than K₂ and K₃. We find similar results for calculations performed on systems with imperfect atomic order and at finite temperature; K_1 is always at least two orders of magnitude greater than K_2 and K_3 . We note that Ref. 28 found a similar

TABLE II. Computed values of K1, K2, K3, and KU for Fe0.5Ni0.5 and Fe0.56Ni0.44 with atomic order parameter S = 1 and temperature T = 0 K. It can be seen that K_1 is orders of magnitude larger than K_2 or K_3 for both compositions.

Composition	Anisotropy constants (MJ m ⁻³)				
	K_1	K_2	K_3	K_U	
Fe _{0.5} Ni _{0.5}	0.9582	-0.0008	0.0001	0.96	
Fe _{0.56} Ni _{0.44}	0.6122	-0.0003	0.0006	0.61	

outcome in their computational study for perfectly ordered (S = 1)L1₀ Fe_{0.5}Ni_{0.5} at T = 0 K; the leading-order anisotropy constant K_1 dominated higher-order constants K_2 and K_3 . We are able to extend this result and find that the dominance of K_1 over K_2 and K_3 holds for systems modeled with imperfect atomic order and at finite temperature. This outcome confirms that the MAE values of ideal single crystals modeled in our calculations are well-described by the standard formula for a uniaxial ferromagnet and, for the remainder of this paper, the torque will always be evaluated at the positions $\theta = \pi/4$, $\phi = 0$ to directly obtain the uniaxial anisotropy constant $K_1 = K_U$.

We calculate K_1 for maximally ordered (S=1) L1₀ Fe_{0.5}Ni_{0.5} at T = 0 K to be 0.96 MJ m⁻³, while for Fe_{0.56}Ni_{0.44} we calculate it to be 0.61 MJ m $^{-3}.$ Our calculated MAE for the equiatomic $\mathrm{Fe_{0.5}Ni_{0.5}}$ composition is broadly consistent with values of 0.23-0.78 MJ m⁻ that were previously obtained using a variety of other computational ⁻³¹ However, we note that these values appear to be low techniques.²⁵)-19,22,24,33 in comparison with experimentally determined ones¹ of 0.2-0.93 MJ m⁻³, especially given that these measurements were performed on samples with imperfect atomic order and at room temperature. As noted in the introduction, analysis of the experimental data^{8,10,27} has suggested that the magnetocrystalline anisotropy energy of $L1_0$ -type FeNi could reach the range of 1.0-1.3 MJ m⁻³. Since ab initio computational estimates of the MAE for L10 transition metal systems are usually in good agreement with experimental data and, if anything, tend to overestimate the anisotropy constants, this computational underestimate stands out.

B. Effects of finite temperature and imperfect atomic order

To make the comparison between theory and experiment more direct, we incorporate the effects of temperature and impersimulate the MAE of a single-variant FeNi crystal at room temperature with the atomic order parameter as furnished in the experimental reports (Table I).

For these finite-temperature calculations, we use the disordered local moment (DLM) description of the magnetocrystalline anisotropy at finite temperature, as outlined in Sec. II. This method has been used with fidelity in the past to study other ferromagnetic L1₀-structured materials^{34,37} as well as rare-earth-based permanent magnets.⁵¹

Shown in the left panel of Fig. 2 is a plot of K_1 for maximally ordered $L1_0$ Fe_{0.5}Ni_{0.5} as a function of temperature, along with a plot of the total magnetization, M, of the two-atom unit cell. It can be seen that, as expected, the anisotropy decreases as temperature increases, but that the decrease is very gradual, with the anisotropy energy at T = 300 K computed as 0.889 MJ m⁻³, around 90% of the T = 0 value. This robust finite-temperature performance is intriguing; it is clear that the anisotropy energy does not obey a simple power law ($K_1 \propto M^{\alpha}$) as it does in other L1₀ materials such as FePt.³⁴ This aspect was studied by Yamashita and Sakuma,⁶³ who used an atomistic spin model to find similar unusual finitetemperature behavior in L10 FeNi.

Proceeding, in the right panel of Fig. 2 is a plot of the same quantities for the Fe-rich composition in its maximally ordered

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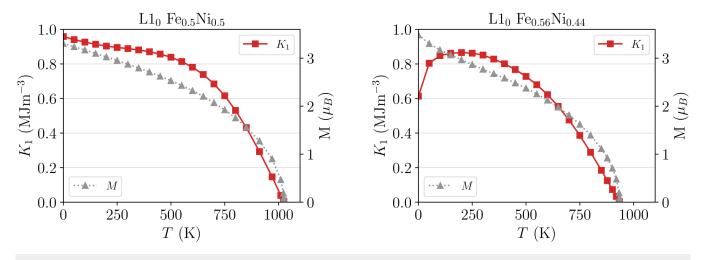


FIG. 2. Anisotropy constant K_1 and magnetization *M* calculated as a function of temperature for a perfectly ordered crystal of L1₀ Fe_{0.56}Ni_{0.5} (left) for a maximally ordered crystal of L1₀ Fe_{0.56}Ni_{0.44} (right). It can be seen that, in both cases, the predicted finite-temperature anisotropy remains high up to and beyond room temperature. Neither case obeys a simple power law of $K_1 \propto M^{\alpha}$. Notably, for the Fe-rich composition, the excess Fe on the Ni sublattice magnetically disorders very rapidly, indicating that the magnetocrystalline anisotropy of this composition at T = 300 K is actually *higher* than its zero-temperature value.

state, with the 1a site having an occupancy of pure Fe, while the 1d site has occupancy Ni_{0.88}Fe_{0.12}. As we increase the temperature away from zero, there is a sharp jump in K_U and an associated decrease in M, resulting in a predicted K_U value at finite temperature which is only marginally lower than for the equiatomic composition. This sharp increase in K_U for the Fe-rich composition is associated with a rapid magnetic disordering of the excess Fe on the 1d lattice site in our calculations. This excess Fe, which makes a significant negative contribution to the total magnetic torque in the zero-temperature calculations, makes a much smaller contribution to the torque once it has magnetically disordered, resulting in an increase in the predicted K_U value for this composition. The rapid magnetic disordering is understood by considering the underlying face-centered tetragonal lattice. Pure Fe on an fcc lattice with this lattice spacing exhibits competition between ferromagnetic and antiferromagnetic ordering,⁶⁵ and in this system this competition is manifest by a rapid disordering of the excess Fe on the Ni sites.

Our computed Curie temperature of $L1_0$ Fe_{0.5}Ni_{0.5} is 1025 K, in reasonable agreement with experimental measurements on the material that measured a Curie temperature of at least 830 K.⁸ We note that our Curie temperature determination is obtained within a mean-field theory and is, therefore, expected to be an overestimate of its true value. The Curie temperature of 1220 K obtained by Yamashita and Sakuma,^{63,64} using a perturbative approach to treat spin–orbit coupling, is higher than the value we obtain. For the Fe-rich composition, a marginally reduced Curie temperature of 935 K is predicted within our model. For both compositions, these Curie temperatures are theoretical estimates, as the material is expected to atomically disorder below this temperature.^{10,66}

A comment should also be made about magnetic moments predicted in our modeling. For reference, we provide the magnetic moments at T = 0 K for an atomic order parameter of S = 1 for both of the studied compositions in Table III. The total

magnetization of the system compares well with experimental data, for example with the magnetization of just over $1.6 \mu_B$ /atom for an equiatomic composition measured in Ref. 19.

We now move on to considering the effects of imperfect g atomic ordering on the predicted MAE. In Fig. 3, we show the zero temperature MAE of both compositions as a function of atomic long-range order parameter, S. Decreasing atomic long-range order consistently decreases the calculated MAE for both compositions. This behavior is expected based on results obtained for other L1₀ compounds, such as FePt and FePd, from both experimental³⁶ and computational³⁵ studies. We note that recent work by Izardar and Ederer,²⁹ which used supercell calculations to represent partially ordered L1₀ FeNi structures, concluded that the MAE for S = 0.75was comparable to that obtained from perfect S = 1.0, with a value around 0.54 MJ m⁻³. This outcome is contrary to our results which show a sizeable MAE decrease with decreased atomic order. However, Izardar *et al.* utilized only 32 atoms in each supercell—a relatively small number—and obtained a large spread in calculated MAE values for the specific supercell configurations used to represent a particular order parameter.

TABLE III. Magnetic moments associated with Fe and Ni L1₀ systems considered in this work, at T = 0 K and with an atomic order parameter of S = 1. We also give the total magnetization of the two-atom unit cell. The Fe-rich composition has excess Fe sitting on the 1*d* site.

Composition	Magnetic moment (μ_B)				
	Total	Fe (1 <i>a</i>)	Ni (1 <i>d</i>)	Fe(1 <i>d</i>)	
Fe _{0.5} Ni _{0.5}	3.24	2.62	0.62		
Fe _{0.56} Ni _{0.44}	3.43	2.60	0.63	2.26	

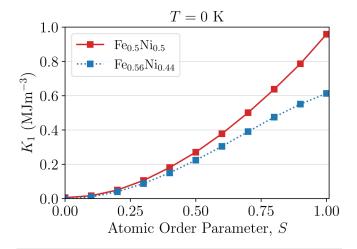


FIG. 3. MAE as a function of atomic long-range order parameter, *S*, for L1₀ Fe–Ni for both the equatomic and Fe-rich compositions, evaluated at T = 0 K. For both cases, decreasing long-range order decreases the predicted MAE, although the drop is sharper for the equiatomic composition than for the Fe-rich case.

C. Comparison with experimental data

To make as close as possible a comparison with the existing experimental data, we now provide results for calculations including the effects of *both* imperfect atomic long-range order and finite temperature. Visualized in Fig. 4 is a plot of K_1 against S at a

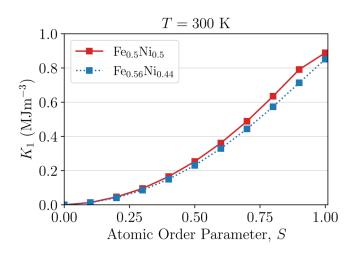


FIG. 4. MAE as a function of atomic long-range order parameter, S, for L1₀ Fe–Ni for both both the equatomic and Fe-rich compositions, evaluated at T = 300 K. As for the calculations at T = 0 K, decreasing atomic order impacts the predicted anisotropy of the system. The predicted values of K_1 for Fe_{0.5}Ni_{0.5} are only slightly decreased compared to their value at T = 0 K, while for the Fe-rich composition the anisotropy at T = 300 K is *increased* compared to its zero temperature value, due to the rapid magnetic disordering of the excess Fe on the Ni sublattice.

simulated temperature of T = 300 K. When the results of the equiatomic composition, Fe_{0.5}Ni_{0.5}, are considered, it can be seen that K_1 is only fractionally decreased at 300 K compared to its value at 0 K, lending support for this material's potential use in applications with high operating temperatures. For the Fe-rich composition, there is a marked increase in K_1 across the range of *S* values compared to the data obtained at T = 0 K, particularly at larger values of *S*, where the system is close to being fully atomically ordered. This increase is associated with the unusual finite-temperature behavior visualized in the right-hand panel of Fig. 2, associated with the excess Fe on the 1d lattice site rapidly disordering with increasing temperature.

We now use the calculated temperature and atomic long-range order dependence of the MAE to make a direct comparison with the experimental values for FeNi summarized in Table I. Considering first the total uniaxial anisotropy, K_U , it appears that the calculated values are significantly lower than the experimental ones. For example, the experimental determination of Ito *et al.*²² of $K_U = 0.55$ MJ m⁻³ for a single-variant thin film of L1₀ Fe_{0.5}Ni_{0.5} with S = 0.6 at T = 293 K may be contrasted with our calculated anisotropy coefficients, for the same conditions, of $K_1 = 0.3616$, $K_2 = 0.0005$, $K_3 = -0.0001$ MJ m⁻³ that provide a uniaxial anisotropy constant of $K_U = 0.36$ MJ m⁻³, a markedly smaller value.

Table I's summary of experimental data is obtained from a variety of sources. We note that not all references disclose the atomic order parameter *S* for the sample, making a direct comparison with our results challenging. In addition, only two references by Neél and co-workers^{10,11} resolve the measured anisotropy, K_U g into its separate components, K_1 , K_2 , K_3 , and of these two references only one¹⁰ provides an atomic long-range order parameter in addition to the measured anisotropy coefficients.

When we consider the resolution of the total uniaxial anisotropy into its separate coefficients, K_1 , K_2 , and K_3 , the origin of the discrepancy becomes clear. For example, the experimental value of $K_1 = 0.32$ MJ m⁻³ reported by Néel and co-workers in Ref. 10 for a specimen of estimated order parameter S = 0.41-0.45 at T = 293 K is in close alignment with our results, as shown in Fig. 4. However, Ref. 10 also reports experimental determinations of large values of K_2 and K_3 , which we do not find. These large values are unexpected for a uniaxial ferromagnetic material, an assessment noted by the authors of the original study. Indeed one of the authors, Néel, developed a theory to account for the unexpectedly large K_2 and K_3 values in these nanocrystalline samples.^{10,11}

The picture described by Néel is of a polycrystalline sample consisting of individual nanocrystals with $L1_0$ atomic layering directions (determining the magnetic easy axis) that are not all aligned along a common direction. (Note that there are three possible directional variants of the $L1_0$ structure, with layering perpendicular to $\hat{\mathbf{x}}$, $\hat{\mathbf{y}}$, or $\hat{\mathbf{z}}$ directions.) Néel proposes that these nanocrystals are smaller than the size of magnetic domains within the sample, with a suggested nanocrystal size of approximately 150 Å. It is concluded that exchange coupling between nanocrystals can lead to finite macroscopic values of K_2 and K_3 , even though individual nanocrystals themselves are assumed to have a negligible value of these coefficients. It is known that meteoritic tetrataenite samples have nanoscale structures.⁴¹ In addition, laboratory-grown

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films often contain step edges, dislocations, and other structural imperfections, which may lead to similar exchange-coupling mechanisms that could impact the measured anisotropy. We emphasise that these large K_2 and K_3 values, which are not captured within first-principles calculations, appear to make a significant contribution to the total uniaxial anisotropy, K_U , of this system.

Néel's argument is predicated on his assumption that the application of a magnetic field along the $\hat{\mathbf{x}}$ direction during the annealing process will favor L10 layering along that same direction. To quantify this effect, we use our computational formalism for modeling atomic arrangements in alloys⁶⁷⁻⁶⁹ in which relativistic effects and, therefore spin-orbit coupling, can be included.³⁴ We find that, for a sample magnetized along the $\hat{\mathbf{x}}$ direction, the predicted ordering is indeed an L10-type layering along the x direction, with an ordering temperature of 508 K. However, the difference in energy between layering along the $\hat{\mathbf{x}}$ direction and layering along \hat{y} or \hat{z} directions is only 0.7 MJ m⁻³, comparable to our calculated magnetocrystalline anisotropy energy constant K_1 . This small but detectable difference supports Néel's hypothesis that samples annealed with an applied field parallel to the $\hat{\mathbf{x}}$ direction will produce crystallites with L10 layering along all three crystal axes, but layering along the $\hat{\mathbf{x}}$ direction will be favored over that along the other two directions. The hypothesis that an inhomogeneous, nanostructured sample can yield unexpectedly large higherorder anisotropy coefficients is also supported by other authors, for example, by recent computational work on inhomogeneous FePt using atomistic spin modeling.7

We suggest, therefore, that more data from both experimental measurements and computational modeling are required to resolve this intriguing apparent discrepancy between theory and experiment. It may be that a mechanism, similar to that outlined by Néel, is unrecognized but at play in a number of the experimental data sets. Further experimental work that resolves the magnetocrystalline anisotropy into its separate K_1 , K_2 , and K_3 components will enable definitive conclusions to be drawn about this disparity. In addition, atomistic and micromagnetic modeling are anticipated to provide further insight into the proposed exchange coupling mechanism and attendant magnetic properties of the multivariant geometry described by Néel.

IV. CONCLUSIONS

In summary, we have carried out an *ab initio* computational study of the magnetocrystalline anisotropy energy of two L1₀-type FeNi compositions, equiatomic Fe_{0.5}Ni_{0.5} and Fe-rich Fe_{0.56}Ni_{0.44}. This rare-earth-free compound is of interest as a sustainable advanced permanent magnet material. We confirm that the modeled magnetic torque of ideal single crystals is well-described by the standard formula for a uniaxial ferromagnet, with the leading-order magnetocrystalline anisotropy energy coefficient K_1 dominating the higher-order coefficients K_2 and K_3 . This dominance persists to finite temperature and is also predicted in samples with imperfect atomic order. Moreover, we find that a significant MAE persists to high temperatures, affirming this material's potential as a useful "gap" magnet.

To compare computational outcomes as faithfully as possible with experimental ones, we have included the effects of both finite temperature and imperfect atomic order on the predicted magnetocrystalline anisotropy. It is confirmed that both increasing temperature and decreasing atomic order decrease the MAE of this compound. We have made a detailed comparison of our computed anisotropy coefficients with those of the experimental literature and find that our calculated values of K_1 appear to be consistent with the experimental data. However, the experimental reports from Néel *et al.*¹⁰ and Paulevé *et al.*¹¹ detail significant K_2 and K_3 values, which we do not find.

We suggest that the noted discrepancy between computational and experimental literature values of the uniaxial magnetocrystalline anistropy constant K_U has its origins in these large K_2 and K_3 values observed in the early experiments. These values significantly contribute to the experimentally observed uniaxial magnetocrystalline anisotropy constant, K_U . It is proposed that these large K_2 and K_3 values have their origins in the polycrystalline, multivariant nature of experimental samples.

Further experimental work should seek to resolve separate values for K_1 , K_2 , and K_3 at both very low and at finite temperatures to better understand the magnetocrystalline anisotropy of this material. Further computational/theoretical work could focus on micromagnetic or atomistic spin modeling to better understand the model proposed by Néel¹⁰ and its consequences.

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AUTHOR DECLARATIONS

Conflict of Interest

The authors have no conflicts to disclose.

Author Contributions

Christopher D. Woodgate: Conceptualization (equal); Data curation (equal); Formal analysis (equal); Investigation (equal); Methodology (equal); Validation (equal); Visualization (equal); Writing – original draft (equal); Writing – review & editing (equal). **Christopher E. Patrick:** Software (supporting); Writing – review & editing (supporting). **Laura H. Lewis:** Conceptualization (equal); Funding acquisition (equal); Project administration (equal); Supervision (equal); Writing – review & editing (supporting). **Julie B. Staunton:** Conceptualization (equal); Funding acquisition (equal); Methodology (equal); Project administration (equal); Resources (equal); Supervision (equal); Writing – review & editing (equal).

ARTICLE

DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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