

5-18-2022

Mechanical Testing Methods for Evaluating Thermoplastic Permanent Pavement Markings

Hyungyung Jo

Matthew Giroux

Kendra Erk

Chelsea Davis

Follow this and additional works at: <https://docs.lib.purdue.edu/msepubs>

This document has been made available through Purdue e-Pubs, a service of the Purdue University Libraries.
Please contact epubs@purdue.edu for additional information.

1 **Mechanical Testing Methods for Evaluating Thermoplastic Permanent Pavement Markings**

2

3 **Hyungyung Jo**

4 School of Materials Engineering

5 Purdue University, West Lafayette, IN, USA, 47907

6 Email: jo24@purdue.edu

7

8 **Matthew Giroux**

9 School of Materials Engineering

10 Purdue University, West Lafayette, IN, USA, 47907

11 Email: girouxm@purdue.edu

12

13 **Kendra A. Erk**

14 School of Materials Engineering

15 Purdue University, West Lafayette, IN, USA, 47907

16 Email: erk@purdue.edu

17

18 **Chelsea S. Davis**

19 School of Materials Engineering

20 Purdue University, West Lafayette, IN, USA, 47907

21 Email: chelsea@purdue.edu (Corresponding Author)

22

23 Word Count: 2984 words

24

25 *Submitted [11/10/2021]*

26

1 **ABSTRACT**

2 The durability of permanent pavement markings (PPMs) on roadways is important for drivers'
3 safety. There are mainly two failure modes: cohesive failure that occurs internally in PPMs through
4 small defects, such as internal pores, and adhesive failure that occurs along the interface between
5 PPMs and road surfaces. Thus, it is critical to characterize the intrinsic mechanical properties of
6 PPMs as well as the adhesion of PPMs on road surfaces to understand their mechanical
7 performance and ultimately, the durability of PPMs. In this study, flexural modulus and flexural
8 strength of PPMs was characterized via three-point bend testing, while fracture toughness was
9 determined with single edge notch bend testing. To analyze the adhesive performance of PPMs on
10 asphalt, a shear adhesion testing approach was developed to measure the apparent debonding
11 energy of PPM specimens on asphalt. The shear adhesion test was performed on asphalt road
12 surfaces and cut surfaces to investigate the chemical and mechanical interfacial effects on
13 adhesion. Two commercial thermoplastics PPM with different mechanical properties were
14 investigated to study how various factors directly affect the adhesion of PPMs on asphalt surfaces.
15 Through the mechanical tests, the relationships between the intrinsic materials properties of PPMs
16 and the mechanical performance of PPMs on asphalt were studied. A PPM material which had
17 lower modulus and higher deformation energy exhibited greater adhesion performance on asphalt,
18 especially when the PPM material was applied at higher asphalt surface temperatures on rough
19 asphalt surfaces.

20

21 **Keywords:** Permanent pavement marking, Thermoplastic, Adhesion test

22

1 **INTRODUCTION**

2 Permanent pavement markings (PPMs) are utilized on roadways to provide clear pathways and
3 traffic information to road users. In order to enhance driver safety, PPMs must be highly visible
4 and durable on roadways. Understanding the mechanical properties and adhesion of PPMs is
5 critical to predict the PPM's service lifecycle which can prevent dangerous confusion on roadways.
6 However, there have been widespread issues in which PPMs become abraded, cracked, and peeled
7 over time.(1)(2) Various external factors, including the condition of the roadway surface, traffic
8 volume, and environmental conditions, can result in adhesive and cohesive failures of PPMs.(3)(4)
9 PPM adhesion is affected by the type of pavement (material and grade) as well as the condition of
10 the pavement (age, dryness, temperature) that it is applied to.(5)(6) PPMs can also be significantly
11 damaged through snowplowing and salt/aggregate use in winter.(7) Internal factors also influence
12 the performance of PPMs on different roadways, including the intrinsic material properties of the
13 PPM (elastic modulus, tensile strength, hardness) and how these properties change in response to
14 environmental conditions, such as variation in temperature and humidity.(8)(9)(10) However,
15 many previous studies have focused on evaluating the retroreflectivity or the durability of PPMs
16 based on ASTM standards using image analysis before and after a wear test. (7)(11)(12)(13) There
17 is a lack of understanding of how the mechanical and intrinsic materials properties of PPMs affect
18 the mechanical performance of PPMs on road surfaces.

19 In this study, various testing methods were utilized to quantitatively assess the mechanical
20 performance of PPMs on asphalt using PPM thermoplastic materials. The PPM thermoplastic is
21 known as one of the most durable pavement markings, and the second most widely used PPM in
22 the United States.(14) The PPM thermoplastic materials behave mechanically in many different
23 ways and often debond from road surfaces by cracking and then flaking off from the surface. Thus,
24 the ability to resist crack propagation can be a critical factor in evaluating the durability of PPM
25 thermoplastics. Single edge notch bend (SENB) testing was performed to determine the fracture
26 toughness and the cohesive fracture energy of PPMs. Three-point bend (3PB) testing was also
27 employed to measure the flexural modulus and the flexural strength of PPMs. To evaluate the
28 adhesive performance of PPMs on asphalt, an adhesion test was developed in this study based on
29 a Mode II in-plane shear failure. The shear adhesion test can measure the total mechanical energy,
30 including elastic and plastic deformation in the thermoplastic PPM, required to induce the adhesive
31 or cohesive failure of PPMs on asphalt. The performance of PPM thermoplastic is known to be
32 sensitive to environmental conditions, such as the asphalt surface temperature at which PPM
33 thermoplastic is applied.(5) Thus, measuring the fracture energy of PPMs on asphalt as a function
34 of asphalt surface application temperatures could validate the new methodology as well as improve
35 our understanding of the relationship between intrinsic properties of PPMs and the mechanical
36 performance of PPMs on asphalt.

37

38 **MATERIALS AND METHODS**

39 Two commercially available PPM thermoplastics, labeled PPM-1 and PPM-2, were provided
40 by Ennis-Flint, Inc. and used as-received in this study. Both PPM thermoplastic materials are
41 comprised of approximately 80 wt% ceramic materials (calcium carbonate titanium dioxide and
42 glass beads) in 20 wt% polymer resin. The 3-point bend (3PB) testing and the single edge notch
43 bend (SENB) testing were utilized to characterize intrinsic mechanical properties of both PPMs.
44 The new methodology proposed in this study to evaluate the performance of PPMs on asphalt was

1 the shear adhesion test on asphalt surfaces. The sample preparation procedure was based on the
 2 manufacturer recommended application instructions for each PPM. Five to six different specimens
 3 were used for each trial of all mechanical tests to obtain representative data and determine sample
 4 to sample variation.

5 **Three-Point Bend Test and Single Edge Notch Bend Test**

6 The 3PB test was performed to measure the flexural modulus and the flexural strength of PPMs
 7 using a universal testing machine (ADMET).

$$8 \quad \sigma_{bend} = \frac{3FL}{2wd^2} \quad \text{Equation 1}$$

$$9 \quad \varepsilon_{bend} = \frac{6Dd}{L^2} \quad \text{Equation 2}$$

10 The flexural stress, σ_{bend} , and the flexural strain, ε_{bend} , were determined by Equation 1 and
 11 2, respectively, where F is the load, L the span, w the width, d the thickness of the specimen, and
 12 D the deflection.(15) The flexural modulus was determined by linear fitting in the elastic region,
 13 and the flexural strength was defined as the yield stress or maximum stress value.

14 The SENB test was conducted to determine the fracture toughness (K_{IC}), and the cohesive
 15 fracture energy (G_f). Fracture toughness indicates a materials' resistance to crack propagation. The
 16 load was applied to a notched specimen, having a 3 mm pre-crack length of the total 6 mm thick
 17 sample, in the 3PB fixture. The K_{IC} was calculated by Equation 3 when the specimen fractured,

$$18 \quad K_{IC} = \frac{SF_c}{tw^{3/2}} f(\lambda) \quad \text{Equation 3}$$

19 where the crack shape factor is defined as

$$20 \quad f(\lambda) = \frac{3\lambda^{1/2}\{1.99-\lambda(1-\lambda)(2.15-3.93\lambda+2.7\lambda^2)\}}{2(1+2\lambda)(1-\lambda)^{3/2}} \quad \text{Equation 4}$$

21 with $\lambda = \frac{a}{w} \sim 0.5$, and F_c is the maximum load. S , t , w and a are the span length, the thickness,
 22 the width, and the pre-crack length of the sample, respectively.(16) The cohesive fracture energy,
 23 G_f , was also determined by Equation 4 based on the load-deflection graph, where U_0 is area
 24 underneath the load-displacement curve, mg is the weight of the specimen (mass multiplied by
 25 the acceleration due to gravity), d_0 is displacement at fracture, and A is the fracture surface
 26 area.(17)

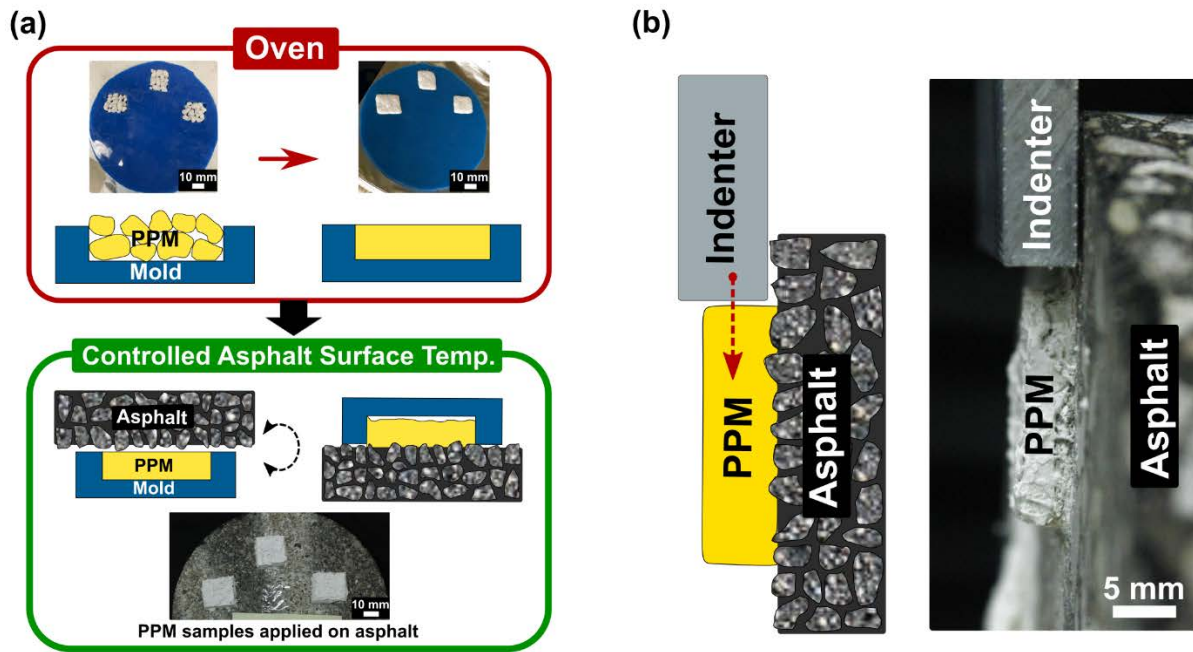
$$27 \quad G_f = (U_0 + mgd_0)/A \quad \text{Equation 5}$$

28 The mgd_0 term is assumed to be 0 since the weight of the specimen is negligible relative to
 29 the applied load. The area under the load-displacement curve represents the energy, U_0 , required
 30 to fracture the specimen. For 3PB and SENB test sample preparation, a silicone mold 12 mm wide
 31 by 120 mm long and a depth of 6 mm was used. Both tests were conducted at a crosshead speed
 32 of 0.02 mm/s using a span of 80 mm.

33 **Shear Adhesion Test**

34 In order to evaluate the performance of PPMs on asphalt, a shear adhesion test was developed
 35 as illustrated in **Figure 1**. When applying PPM specimens on asphalt, asphalt core surface

1 temperatures were variously controlled at 15, 25, 35, and 40 °C using a hot-plate or a freezer. Each
 2 thermoplastic sample was heated in the mold 20 mm wide by 20 mm long and a depth of 5 mm in
 3 an oven at the manufacturer recommended application temperatures for 10 min. For PPM-2, the
 4 sample was manually agitated on a hot-plate at the application temperature prior to being
 5 transferred into the mold and heated in the oven. When removing the molded thermoplastic from
 6 the oven, the surface temperature-controlled asphalt core was placed on the melted thermoplastic
 7 and inverted, as shown in **Figure 1(a)**. A soldering iron was additionally used to locally remelt
 8 each thermoplastic specimen to fill any visible pores and remove excess thermoplastic on the
 9 asphalt core. In order to evaluate the effect of surface roughness, thermoplastic PPM specimens
 10 applied to both smooth (cut) asphalt surfaces, and rough (road) asphalt surfaces were investigated.
 11 For the shear adhesion test, asphalt cores were vertically fixed on the universal testing machine
 12 (ADMET) and the shear force was applied at a crosshead speed of 0.1 mm/s by a flat indenter to
 13 the top of the thermoplastic specimens as shown in **Figure 1(b)** until fracture was observed. The
 14 apparent fracture energy was calculated by integrating the area under the load-displacement curve.
 15 In the case that a specimen failed cohesively, the area until the maximum load at which the
 16 specimen fractured was taken as the fracture energy.



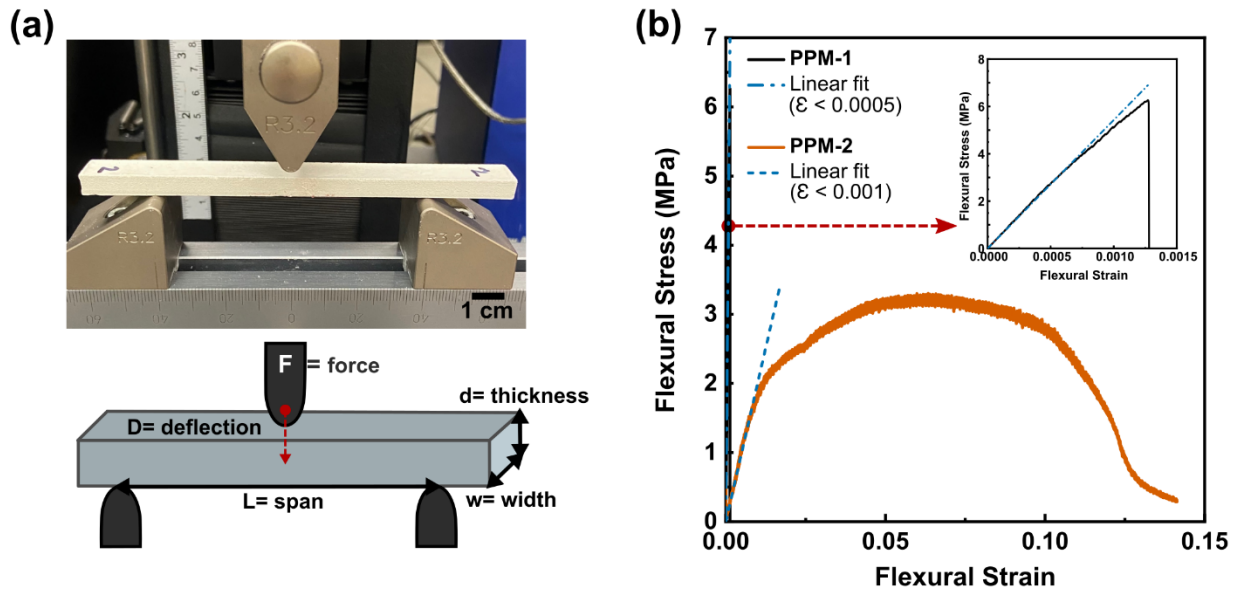
17
 18 **Figure 1. Schematic of permanent pavement marking (PPM) sample preparation procedure**
 19 **(a) and the shear adhesion test developed herein (b)**

20
 21 **RESULTS AND DISCUSSION**

22 **Figure 2** shows representative flexural stress versus flexural strain curves for PPM-1 and PPM-
 23 2 measured from the 3PB test. Flexural moduli were determined from linear slopes of the 3PB test
 24 curves in the low strain range from 0 to 0.0005 for PPM-1, and from 0 to 0.001 for PPM-2, due to
 25 the significantly different mechanical properties and subsequent elastic deformation regimes.
 26 Flexural modulus and flexural strength values are reported in **Table 1**. Notably, the flexural
 27 modulus of PPM-1 was approximately 24 times greater than that of PPM-2, while their flexural

1 strength values were similar in magnitude. PPM-1 exhibited brittle fracture behavior with a high
 2 resistance to bending deformation, since the PPM-1 specimen fractured at the maximum stress
 3 with little non-linear deformation as shown in the inset graph in **Figure 2(b)**. Alternatively, PPM-
 4 2 displayed a yield point followed by plastic deformation and ultimately failed at a lower stress
 5 but much higher strain value than PPM-1. It was mainly found that the mechanical properties were
 6 significantly different; PPM-1 was brittle whereas PPM-2 was compliant having a high capacity
 7 of stress absorption and energy dissipation before fracture.

8



9

10 **Figure 2. Photographic and schematic images (a) illustrating the 3PB test with key geometric**
 11 **parameters of the 3PB testing sample labelled. Flexural stress versus flexural strain curves**
 12 **(b) show the comparison of 3PB test results for the two PPMs. Inset in (b) shows the result**
 13 **of PPM-1 in greater detail.**

14

15 **Table 1. Flexural modulus and flexural strength of PPMs from 3PB test.**

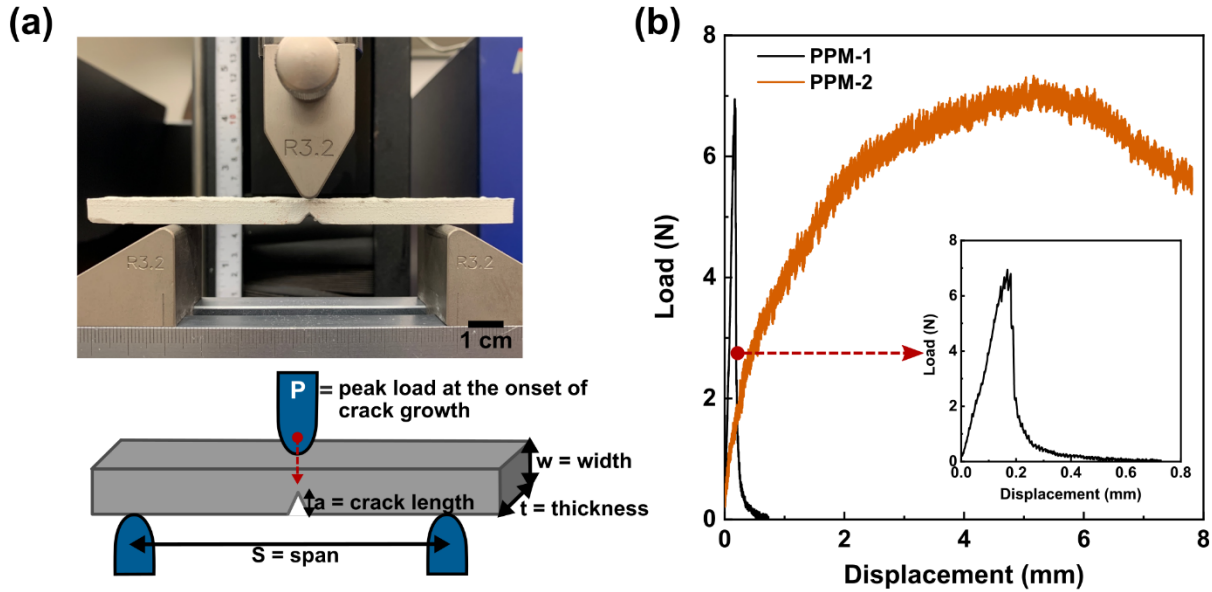
	Flexural Modulus (GPa)	Flexural Strength (MPa)
PPM-1	5.67 ± 0.69	6.66 ± 0.84
PPM-2	0.24 ± 0.05	4.00 ± 0.82

16

17 The load versus displacement curve obtained from a SENB test is shown in **Figure 3**. The
 18 fracture toughness and the cohesive fracture energy values are indicated in **Table 2**. The fracture
 19 toughness value is a function of the maximum load and the geometry of the specimen. K_{IC} values
 20 of PPM-1 and PPM-2 were within the experimental error since there was no significant difference
 21 between their maximum load values as shown in **Figure 3**. For the cohesive fracture energy, it can
 22 be calculated by dividing the integrated area under the load-displacement graph by the fracture
 23 area of the specimen, assuming that there is no plastic deformation.(17)(18) The G_f value of

1 PPM-1 was measured to be 0.03 ± 0.01 kN/m. However, since there was significant plastic
 2 deformation observed in PPM-2 specimens, straightforward calculation of G_f is impossible.
 3 Comparing SENB data in **Figure 3**, PPM-1 exhibited a brittle fracture behavior, since the crack
 4 propagation occurred immediately after the crack opening initiated.(19) On the other hand, the
 5 PPM-2 specimen exhibited stable crack propagation until fracture since the plastic deformation
 6 took place at the crack tip.(20) This result indicates that PPM-2 requires more energy than PPM-1
 7 during the fracture process under the bending stress due to its higher resistance to crack
 8 propagation, as shown in **Figure 3**.

9



10

11 **Figure 3.** Photographic and schematic images (a) illustrating the SENB test with key
 12 geometric parameters of the SENB testing sample labelled. Displacement - load graph
 13 comparison for PPMs from the SENB test(b). Inset graph shows the result of PPM-1.

14

15 **Table 2.** Fracture toughness and cohesive fracture energy of PPMs from SENB test.

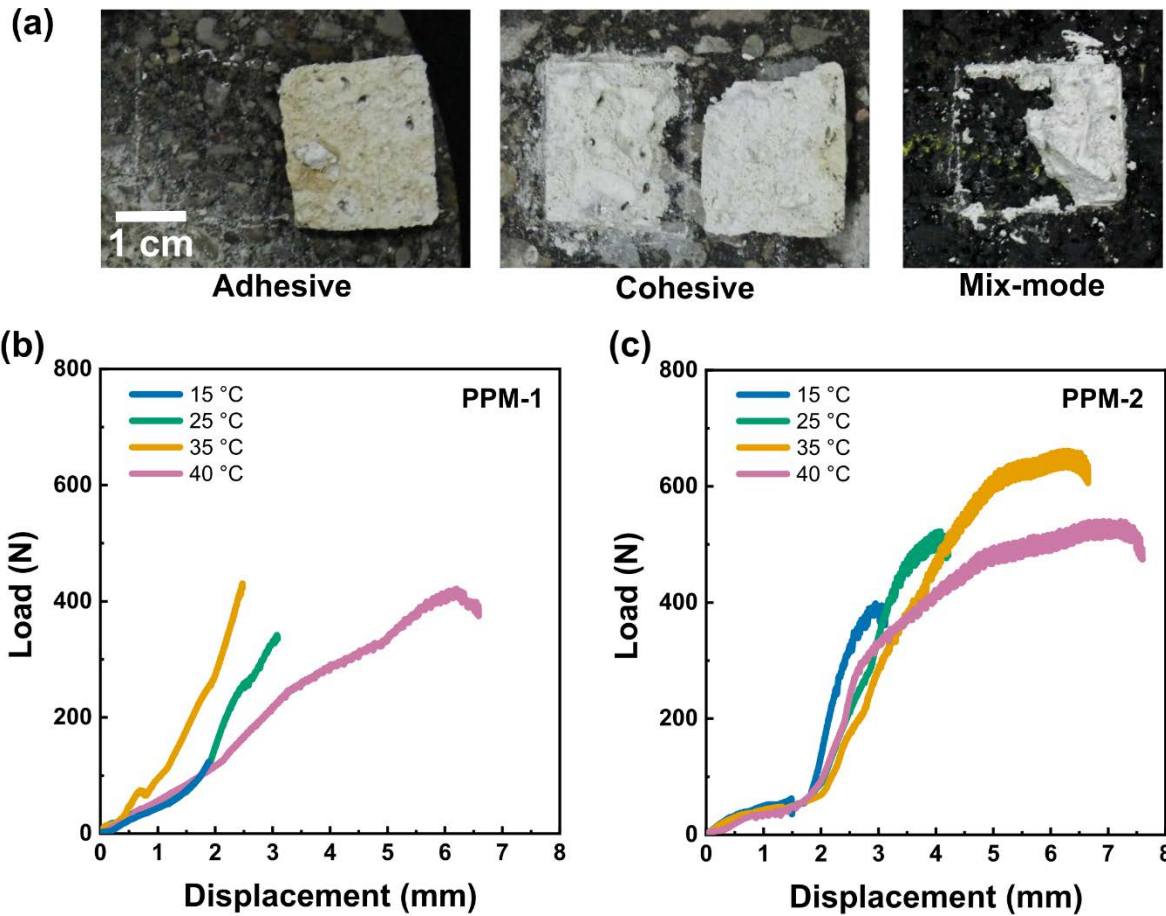
	Fracture Toughness (MPa \sqrt{m})	Cohesive Fracture Energy (kJ/m)
PPM-1	0.23 ± 0.04	0.03 ± 0.01
PPM-2	0.21 ± 0.03	

16

17 The shear adhesion test developed in this study determined the apparent work of debonding as
 18 the total energy required to fully remove PPM specimens from the asphalt surface. Three different
 19 failure modes resulted from the shear adhesion test: adhesive, cohesive, and mix-mode failure
 20 (shown in **Figure 4(a)**). In **Figure 4(b)**, PPM-1 specimens applied at 15 °C and 35 °C failed
 21 adhesively, while PPM-1 specimens applied at 25 °C and 40 °C failed cohesively. The slopes of
 22 graphs for PPM-1 specimens applied at 15 °C and 35°C increased until they were adhesively
 23 failed, indicating that PPM-1 exhibited the dynamic adhesive fracture behavior on asphalt. On the

1 other hand, all PPM-2 specimens displayed in **Figure 4(c)** were adhesively failed. The slopes of
 2 the load versus displacement data for PPM-2 significantly increased once a displacement of 2 mm
 3 was reached as the indenter came fully into contact with the top surface of the sample. As PPM-2
 4 specimens initiated to yield, the slopes decreased until they were adhesively failed. This indicates
 5 that the PPM-2 specimen needs more energy to fracture including the elastic and plastic
 6 deformation energy, and the interfacial fracture energy.

7



8

9 **Figure 4. Photographic images (a) represent examples of fracture modes, adhesive, cohesive,**
 10 **and mix-mode, respectively. Shear adhesion test raw data of (b) PPM 1 and (c) PPM 2**
 11 **performed on rough (road) asphalt surface at substrate application temperatures of 15, 25,**
 12 **35, and 40 °C, as an example. (a) PPM-1 specimens applied at 15 °C and 35 °C failed**
 13 **adhesively while PPM-1 specimens applied at 25 °C and 40 °C failed cohesively. (b) All PPM-**
 14 **2 specimens failed adhesively.**

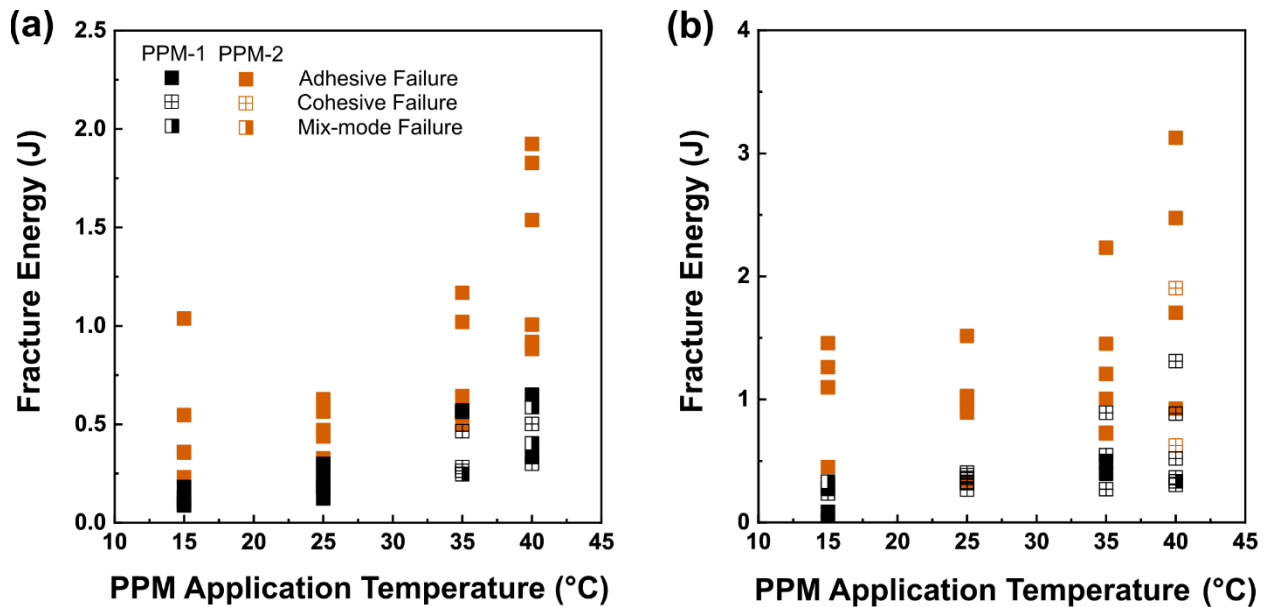
15

16 For PPM-1 specimens tested on the smooth asphalt surface (shown in **Figure 5(a)**), most
 17 specimens applied at 15 °C and 25 °C failed adhesively, while various failure modes including the
 18 cohesive and mix-mode failure were observed for PPM-1 specimens applied at 35 °C and 40 °C.
 19 PPM-1 specimens on the rough asphalt surface (**Figure 5(b)**) also showed various failure modes
 20 and higher apparent fracture energy values than PPM-1 tested on smooth surfaces (**Figure 5(a)**).

1 For PPM-2, all specimens failed adhesively on the smooth asphalt surfaces, and most specimens
 2 (except two samples applied at 40 °C) also failed adhesively on the rough asphalt surface. On both
 3 smooth and rough asphalt surfaces, the fracture energies of PPM-1 and PPM-2 increased as the
 4 asphalt surface application temperature increased.

5 Comparing the rough and smooth asphalt surfaces, fracture energy results and thus the
 6 adhesion strength from the smooth asphalt surfaces were considered to be dominated by chemical
 7 interactions between the asphalt and PPMs. Therefore, the results indicate that as the asphalt
 8 surface application temperature increased, the degree of mechanical interlocking between the
 9 asphalt and PPMs was more likely to occur, resulting in an increase in the apparent fracture
 10 energy.(3)(6) For the shear adhesion tests on rough asphalt surfaces, since PPM specimens could
 11 more strongly mechanically interlock with the rough asphalt surfaces compared to the smooth
 12 surfaces, overall fracture energies on the rough asphalt surfaces were approximately 50% higher
 13 than analogous adhesion values on the smooth asphalt surfaces. Additionally, the results from the
 14 rough asphalt surfaces essentially reflect mechanical interactions between PPMs and asphalt.
 15 Referring back to the bending measurements presented in Figure 4, PPM-2 is compliant enough to
 16 attain more plastic deformation, resulting in the higher fracture energy, compared to PPM-1.(21)
 17 Through the shear adhesion test, it would be expected that the brittle PPM-1 will be cracked and
 18 mainly cohesively fractured whereas the more compliant PPM-2 will be plastically deformed and
 19 adhesively failed on asphalt surfaces.

20



21

22 **Figure 5. Comparison of shear adhesion test (a) on smooth (cut) asphalt surfaces and (b)**
 23 **rough (road) asphalt surfaces.**

24

25 CONCLUSIONS

26 A shear adhesion test was developed to quantify the debonding energy of thermoplastic PPMs
 27 on asphalt surfaces. It was shown that the shear adhesion test was sensitive to differences in the
 28 adhesive performance of PPMs applied at different asphalt surface temperatures. Through the

1 classical mechanical characterization, PPM-1 was found to exhibit a brittle fracture behavior in
2 which rapid crack propagation took place. Notably, the dynamic, unstable fracture in PPM-1 was
3 observed to initiate and propagate from small defects, such as internal pores, or along the interface
4 between glass beads and the polymer matrix. Similarly, from the shear adhesion test, PPM-1
5 exhibited an unstable fracture behavior on asphalt. In contrast, PPM-2, which has a relatively low
6 flexural modulus compared to PPM-1, primarily displayed adhesive failure over the various
7 asphalt surface application temperatures. Overall, when PPMs are able interlock mechanically with
8 the rough asphalt surfaces, cohesive fracture mechanisms dominated the shear adhesion failure,
9 resulting in higher fracture energies. Additionally, it was found that the environmental temperature
10 was a critical factor affecting the adhesion between the asphalt and PPMs since the apparent
11 fracture energy increased as the asphalt surface application temperature increased.

12

13 **ACKNOWLEDGMENTS**

14 This work was supported by the Joint Transportation Research Program administered by the
15 Indiana Department of Transportation and Purdue University under Project Number SPR-4423.
16 The contents of this paper reflect the views of the authors, who are responsible for the facts and
17 the accuracy of the data presented herein and do not necessarily reflect the official views or policies
18 of the sponsoring organizations. These contents do not constitute a standard, specification, or
19 regulation.

20

21 **AUTHOR CONTRIBUTIONS**

22 The authors confirm contribution to the paper as follows: study conception and design: H. Jo,
23 K. Erk, C. Davis; data collection: M. Giroux; analysis and interpretation of results: H. Jo, M.
24 Giroux, C. Davis, K. Erk; draft manuscript preparation: H. Jo, C. Davis; All authors reviewed the
25 results and approved the final version of the manuscript. The authors do not have any conflicts of
26 interest to declare.

27

28 **REFERENCES**

- 29 1. Dwyer, C., and R. Becker. *Evaluation of Hardened Paint Pavement Markings*. Publication
30 FHWA-AZ-020747. FHWA, Arizona Department of Transportation, 2020.
- 31 2. Xu, L., Z. Chen, X. Li, and F. Xiao. Performance, Environmental Impact and Cost Analysis
32 of Marking Materials in Pavement Engineering, the-State-of-Art. *Journal of Cleaner*
33 *Production*, 2021. 294: 126302.
- 34 3. Texas Department of Transportation. *Pavement Marking Handbook*. 2004.
- 35 4. Songchitruksa, P., G. L. Ullman, and A. M. Pike. Guidance for Cost-Effective Selection of
36 Pavement Marking Materials for Work Zones. *Journal of Infrastructure Systems*, 2011. 17:
37 55–65.
- 38 5. New York State Department of Transportation. *Pavement Marking Material Guidelines*
39 *New York State*. 2002.
- 40 6. Gates, T. J., H. G. Hawkins, and E. R. Rose. *Effective Pavement Marking Practices for*

- 1 *Sealcoat and Hot-Mix Asphalt Pavements*. Publication FHWA/TX-03/4150-22003, Texas
2 Department of Transportation, 2014.
- 3 7. Lee, J. T., T. L. Maleck, and W. C. Taylor. Pavement Marking Material Evaluation Study
4 in Michigan. *Institute of Transportation Engineers (ITE)*, 1999. 69: 44–51.
- 5 8. Mirabedini, S. M., F. Zareanshahraki, and V. Mannari. Enhancing Thermoplastic Road-
6 Marking Paints Performance Using Sustainable Rosin Ester. *Progress in Organic Coatings*,
7 2020. 139: 105454.
- 8 9. Mirabedini, S. M., S. S. Jamali, M. Haghayegh, M. Sharifi, A. S. Mirabedini, and R.
9 Hashemi-Nasab. Application of Mixture Experimental Design to Optimize Formulation and
10 Performance of Thermoplastic Road Markings. *Progress in Organic Coatings*, 2012. 75:
11 549–559.
- 12 10. Jiang, Y. *Durability and Retro-Reflectivity of Pavement Markings (Synthesis Study)*.
13 Publication FHWA/IN/JTRP-2007/11, Indiana Department of Transportation, 2008.
- 14 11. Mohamed, M., A. Abdel-Rahim, E. Kassem, K. Chang, and A. G. McDonald. Laboratory-
15 Based Evaluation of Pavement Marking Characteristics. *Journal of Transportation*
16 *Engineering, Part B: Pavements*, 2020. 146: 04020016.
- 17 12. ASTM D713-12. *Standard Practice for Conducting Road Service Tests on Fluid Traffic*
18 *Marking*. 1998.
- 19 13. Ozelim, L., and R. E. Turochy. Modeling Retroreflectivity Performance of Thermoplastic
20 Pavement Markings in Alabama. *Journal of Transportation Engineering*, 2014. 140: 1–6.
- 21 14. Rasdorf, W., J. Hummer, G. Zhang, and W. Sitzabee. *Pavement Marking Performance*
22 *Analysis*. North Carolina Department of Transportation, 2009.
- 23 15. Coldea, A., M. V. Swain, and N. Thiel. Mechanical Properties of Polymer-Infiltrated-
24 Ceramic-Network Materials. *Dental Materials*, 2013. 29: 419–426.
- 25 16. Adachi, T., M. Osaki, W. Araki, and S. C. Kwon. Fracture Toughness of Nano- and Micro-
26 Spherical Silica-Particle-Filled Epoxy Composites. *Acta Materialia*, 2008. 56: 2101–2109.
- 27 17. Malvar, L. J., and G. E. Warren. *Fracture Energy for Three-Point Bend Tests on Single-
28 Edge Notched Beams*. 1988.
- 29 18. Gao, W., X. Liu, S. Chen, T. Q. Bui, and S. Yoshimura. A Cohesive Zone Based DE/FE
30 Coupling Approach for Interfacial Debonding Analysis of Laminated Glass. *Theoretical*
31 *and Applied Fracture Mechanics*, 2020. 108: 102668.
- 32 19. Ishikawa, M., H. Ogawa, and I. Narisawa. Brittle Fracture in Glassy Polymers. *Journal of*
33 *Macromolecular Science, Part B*, 1981. 19: 421–443.
- 34 20. Duckworth, J., T. Arahira, and M. Todo. Fracture Characterization of Novel Bioceramic
35 Microbeads Filled Polymer Composite. *Journal of Materials Science*, 2020. 55: 8954–8967.
- 36 21. Wang, H. Use of End-Loaded-Split (ELS) Test to Study Stable Fracture Behaviour of
37 Composites under Mode II Loading. *Composite Structure*, 1996. 36: 71–79.
- 38