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# A Three-Phase Power-Flow Algorithm for Transmission Networks: a Hybrid Phase/Sequence Approach

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**ABSTRACT** In this paper, the three-phase generalization of a single-phase power flow (named PFPD) developed by the first author is presented. This three-phase formulation is chiefly conceived for HV/EHV transmission network applications, but it preserves a general validity for any power system. An iterative method for the solution achievement is throughout expounded. The algorithm quantitatively aims at investigating the impact of the asymmetrical transmission structures on power systems. This impact is evaluated in terms of voltage and current sequence components. Moreover, discussions on possible improvement actions to enhance the power quality are also developed. The algorithm is implemented in Matlab environment and tested by several fictitious networks. Eventually, extensive comparisons in terms of execution time, number of iterations and solution accuracy with the software DIgSILENT PowerFactory are presented.

**INDEX TERMS** Power flow, Three-phase power flow, Power system analysis, Power quality, Industrial power systems, Transmission network,

#### NOMENCLATURE

Symbol	Quantity		
A. Sets and	Indices	<u>Y</u> Geq, <u>Z</u> Geq	Admittance and impedance equivalent matrices
а	Slack-section		as seen at generator buses (three-phase)
$b \div g$	Generator sections	$\underline{T}_x$	Transformation matrix
$h \div m$	Load sections	<u>F</u>	Generalized Fortescue transformation matrix
$N_G$	Total number of the generator sections	ABC	Phase frame of reference
$N_M$	Total number of the network sections	0PN	Sequence component frame of reference
G	Set of the generator sections $a \div g$	0	Zero sequence component
L	Set of the load sections $h \div m$	Р	Positive sequence component
S	Shunt branches	N	Negative sequence component
0, 1, k	Initial, first,, k-th iteration	B. Variable	s and Parameters
t	Load typology	j	Imaginary unit
q	Quadrature component	<u>u</u>	Complex voltage
$\frac{1}{c}$	Corrected value	<u>u</u>	Complex voltage vector
R	Radial network	$ \underline{u} $	Voltage magnitude
$J_a^{ABC}$	Slack bus three-phase ideal current source	δ	Voltage angle
Y. YN. YSGL	Total bus admittance, network admittance.	<u>i</u>	Complex current
<u>1) 11, 1502</u>	shunt admittance matrices (three-phase)	<u>i</u>	Complex current vector
<u>Y</u> G, <u>Y</u> L	Generator and load admittance submatrices	<u>∆i</u>	Correcting current vector
$\overline{Y_{GG}}, \overline{Y_{GL}},$	Admittance submatrices of $\underline{Y}$ (three-phase)	<u>Y</u>	Complex admittance
$\underline{Y}_{LG}, \underline{Y}_{LL}$		r	Per unit length resistance

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x	Per unit length reactance
<u>S</u>	Complex power
р	Active power
q	Reactive power
α	Phasor rotation operator
C. Symbols	
Т	Matrix transposition
*	Complex conjugate
-1	Matrix inversion
÷	From to
$\otimes$	Hadamard element-wise multiplication
$\odot$	Positive sequence multiplication
1	Element-wise division
Im	Imaginary part of a complex quantity
D. Acronyms	
HV	High Voltage
EHV	Extra-High Voltage
MV	Medium Voltage
LV	Low Voltage
OHL	Over Head Line
GIL	Gas Insulated Line
OPGW	Optical fiber composite overhead Ground Wire
ITER	Number of iterations
MCA	Multiconductor Cell Analysis
DGS	DIgSILENT PowerFactory
PFPD	Power Flow of the University of Padova
PFPD_3P	Power Flow of the University of Padova (3
	Phase Power Flow) developed in this paper
PF[24]_3P	Power Flow implementation of [24] (3 Phase
	Power Flow)

#### I. INTRODUCTION

The three-phase power flow problem is a widely investigated topic in the technical literature, *e.g.* [1-19]. The hypothesis of perfectly balanced three-phase network, in fact, cannot be achieved in real power systems. Nonetheless, the great number of publications is chiefly focused on the distribution networks (some considerable examples are [1-7]). This fact is mainly due to the unbalanced distribution load configurations, the typical low voltage four-wire distribution system structures, and the growing presence of distributed generation [1-4]. Moreover, the high r/x ratios of the distribution lines make the problem particularly challenging and worthy of research [5,6].

For the transmission networks, instead, few contributions are presented in the last fifty years (after a careful review in the international technical literature, only the contributions [8-19] were found). In fact, it is often taken for granted that the transmission systems must be systematically operated in a balanced manner [1], [6], [8]. Therefore, power flows of transmission power systems can be computed by means of their equivalent single-circuit at the positive sequence.

Notwithstanding, an accurate knowledge of the voltage/current unbalance factors for the HV and EHV networks is fundamental to make power quality evaluations [9, 20]. This topic is becoming more and more important for

transmission networks and ought not to be underestimated. In fact, the network unbalance factors in the transmission power systems are going to increase [21], mainly for the following reasons:

- Increase of the existing transmission line loading due to the growing electricity demand (also due to the recent difficulty of erecting new OHLs),
- The possibility of incrementing the lengths of the transmission lines,
- The transpositions of transmission lines are very rarely adopted [20, 22].

In this paper, a three-phase power flow algorithm (named as PFPD\_3P) is presented. Beyond the evaluation of power quality, this algorithm can have a further practical/industrial fall out, by foreseeing the values of negative sequence currents in each section of the network. This is particularly important for synchronous generator/compensator [21, 23] negative sequence protections. Too high values of negative sequence currents, in fact, can bring to undesired generator and synchronous compensator protection trippings.

Twenty years ago, the first author had developed a matrix three-phase power flow algorithm (in the following named as PF[24] 3P) [24]. In the present paper, instead, the new threephase power flow algorithm PFPD\_3P is discussed and it takes its inspiration from a single-phase power flow algorithm (PFPD) recently developed [25]. In this way, a compact matrix approach can be exploited in order to achieve more rapidly the power flow solution. In fact, the interpretation of the (threephase) slack generator inside an "all-inclusive" (three-phase) admittance matrix allows reducing the CPU time, decreasing the number of iterations, and achieving greater precisions compared to those of the other methods. This englobing is made possible by treating the slack generator as quasi-ideal current source at positive sequence. In PFPD 3P, it is demonstrated that such way of modelling the slack generator is also possible if the three-phase extension of PFPD is considered. Thus, this paper further demonstrates the possibility of treating the slack generator as a quasi-ideal current source, at positive sequence, in power flow problems.

With regard to the existing resolution approaches, the threephase power flow algorithms are basically divided into two resolution categories [10]. The first ones *only* operate in the phase component frame of reference [5, 10-15], so both symmetrical and asymmetrical components are modelled by means of their phase matrices. With the phase sequence approach, however, it is not possible to exploit the main advantage of the symmetrical component approach by means of Fortescue Transformations. The second ones *only* operate in the symmetrical devices (like non-transposed lines), proper compensation techniques are adopted [9, 16-19]. These compensation techniques allow "symmetrizing" the

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asymmetrical components, so that the problem can be studied by using the three single-phase sequence circuits.

In the present algorithm, instead, each iterative cycle alternates the use of a sequence approach with that of phases by means of the Fortescue's transform and its inverse. As it is explained in the following, this is possible because some formulae involve the symmetry of some network devices (e.g., the formulae for computing the correcting currents into the synchronous generators). Whenever the Fortescue transform cannot be adopted (for instance, when non-transposed lines are involved), a phase approach is chosen. Therefore, differently from the existing three-phase power flow methods [8-19], PFPD 3P can be considered a hybrid one, by combining the merits of each frame of reference and without englobing the demerits deriving from the choice of a unique frame of reference. Thus, PFPD 3P is a novel three-phase matrix algorithm suitable for the study of transmission networks, characterized from a computational (hybrid) paradigm different from the existing ones.

As it is explained in the paper, the algorithm is easily selfimplementable, since only five matrix iterated formulae are employed. Eventually, such three-phase evaluations can be carried out efficiently (as it is described in the section dedicated to the computational performances) without the need of using the classical numerical techniques (*e.g.*, Newton-Raphson and derived).

# II. THE THREE-PHASE POWER FLOW ALGORITHM BASED ON PFPD

Recently, the first author published an AC single-phase power flow algorithm (named PFPD) based on an "all-inclusive" bus admittance matrix. This means that all the power flow data (*i.e.*, the network elements and the technical constraints) are embedded in a unique matrix, and an iterative procedure to achieve the solution is developed from it. Therefore, a concise, efficient, and rapid power flow has been presented [25].

The reasons that persuade the authors to investigate this topic is understanding if the three-phase extension of PFPD preserves its computational advantages. Obviously, the size of the three-phase power flow problem is greater than the corresponding single-phase one. Thus, any computational advantage is useful, even if the three-phase power flow is often intended as an off-line planning tool [12]. In light of this, a three-phase power flow formulation (PFPD\_3P) inspired by PFPD is described in the following. In general, power flow solutions are determined by solving a set of equations formulated from some technical constraints (typically power and voltages) known *a priori*. In the present approach, all the three-phase network sections are divided into three sets: the

slack, the generator, and the load sections. For these ones, the following technical constraints are set:

- 1. For the *SLACK section*: the three-phase positivesequence voltage  $\underline{u}_{a,P} = \underline{u}_{a,P} \boxed{1 \alpha^2 \alpha}^{T}$  is constrained, and the phasor  $\underline{u}_{a,P}$  is assigned as the system angle reference;
- 2. For the *Generator sections*: the positive-sequence injected active power  $p_{b,P}, \ldots, p_{g,P}$  and the positive-sequence voltage magnitudes  $|\underline{u}_{b,P}| \ldots |\underline{u}_{g,P}|$  are constrained;
- 3. For the *Load sections*: the constrained quantities are the complex power  $p_h + jq_h, \ldots, p_m + jq_m$  absorbed when they are subjected to their positive sequence nominal voltage (even null, when transit sections are considered).

It is worth noting that all these constraints are specified in the symmetrical component frame of reference. All these elements representing the constraints are included in the phase admittance matrix  $\underline{Y}_{SGL}^{ABC}$  represented in Fig. 1. For the generic generator/load (*i.e.*, shunt) element connected to the section *i*, in fact, the following relation can be written:

$$\underline{i}_{S,i}^{ABC} = \underline{Y}_{i}^{ABC} \, \underline{u}_{i}^{ABC}, \quad i = a \div m \tag{1}$$

where  $\underline{V}_{i}^{ABC}$  is the (3×3) admittance matrix linking the phase vector of the three entering currents in the shunt elements  $\underline{i}_{S,i}^{ABC}$  (*i.e.*, passive sign convention) with the phase vector of the three phase-to-ground voltages  $\underline{u}_{i}^{ABC}$ .



FIGURE 1. The diagonal block-matrix  $\underline{Y}_{SGL}^{ABC}$  storing the constraints of the three-phase power flow.

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FIGURE 2. Schematic representation of the three-phase power system (a: slack generator section, G: generator sections, L: load sections).

Obviously, for the active generators, (1) gives a set of negative currents (since they are injected from the generator terminals). By considering the total number *m* of the network sections, a  $(3m)\times(3m)$  square diagonal block matrix  $\underline{Y}_{SGL}^{ABC}$  can be defined. This matrix allows writing the following phase relation including all the *m* elements connected to the *m* sections:

$$\underline{i}_{S}^{ABC} = \underline{Y}_{SGL}^{ABC} \underline{u}^{ABC}$$
(2)

where

$$\underline{i}_{S}^{ABC} = \boxed{\left(\underline{i}_{S,a}^{ABC}\right) \left(\underline{i}_{S,b}^{ABC}\right)} \qquad \dots \qquad \left(\underline{i}_{S,g}^{ABC}\right) \left(\underline{i}_{S,h}^{ABC}\right) \qquad \dots \qquad \left(\underline{i}_{S,m}^{ABC}\right)^{T}$$

is the  $(3m) \times 1$  block vector of the entering currents in all the section phases of the elements and

$$\underline{\boldsymbol{u}}^{ABC} = \left[ \begin{array}{c} \underline{\boldsymbol{u}}_{a}^{ABC} \end{array} \right] \left( \underline{\boldsymbol{u}}_{b}^{ABC} \right) \qquad \cdots \qquad \left( \underline{\boldsymbol{u}}_{g}^{ABC} \right) \qquad \left( \underline{\boldsymbol{u}}_{h}^{ABC} \right) \qquad \cdots \qquad \left( \underline{\boldsymbol{u}}_{m}^{ABC} \right)^{T}$$

is the  $(3m)\times 1$  block vector of all the phase-to-ground voltages. In a section *i* where no elements are connected (*i.e.*, transit sections), the matrix  $\underline{Y}_i^{ABC}$  is null. These situations, for instance, occur in the busbar sections connecting power transformers with electrical lines. Moreover, it must be reminded that also the slack generator is modelled and included inside  $\underline{Y}_{SGL}^{ABC}$ . This inclusion is due to the formal possibility to consider the slack generator as a quasi-ideal current source, similarly to [25]. The three-phase admittance matrix  $\underline{Y}_N^{ABC}$ , instead, links the phase currents entering the network with its phase-to-ground voltages:

$$\underline{i}_{N}^{ABC} = \underline{Y}_{N}^{ABC} \underline{u}^{ABC}$$
(3)

where the network system is of course supposed linear and

$$\underline{i}_{N}^{ABC} = \boxed{\left(\underline{i}_{N,a}^{ABC}\right) \left(\underline{i}_{N,b}^{ABC}\right)} \dots \left(\underline{i}_{N,g}^{ABC}\right) \left(\underline{i}_{N,b}^{ABC}\right) \dots \left(\underline{i}_{N,m}^{ABC}\right)$$

is the  $(3m) \times 1$  block vector of the phase currents entering the network and  $\underline{u}^{ABC}$  is the same of (2). It is worth reminding that the construction of  $\underline{Y}_{N}^{ABC}$  is similar to the single-phase one, by using the *Linear transformation* techniques [12, 24].

By summing (2) and (3) member to member, the following relation is obtained:

$$\underline{i}^{ABC} = \underline{Y}^{ABC} \, \underline{u}^{ABC} \,, \tag{4}$$

where  $\underline{Y}^{ABC}$  is the three-phase "all-inclusive" admittance matrix containing all the network information,  $\underline{\mu}^{ABC}$  is the set of the phase-to-ground voltages, whereas

<i>i<sup>ABC</sup></i> =	$\left(\underline{J}_{a}^{ABC}\right)$	$\left(\boldsymbol{\theta}^{ABC}\right)$		$\left(\boldsymbol{\theta}^{ABC}\right)$	$\left( \boldsymbol{\theta}^{ABC} \right)$		$\left( \boldsymbol{\theta}^{ABC} \right)$	
--------------------------	--	--	--	--	--	--	--	--

is the vector of the three-phase currents injected at the sections  $a \div m$  of Fig. 2.



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FIGURE 3. Partitioned form of  $\underline{i}^{ABC} = \underline{Y}^{ABC} \underline{u}^{ABC}$ .

It is worth noting that all the current sub-vectors are null except the first one  $(\underline{J}_{a}^{ABC})$ : it represents the three-phase external current injection due to the current source modelling the slack generator at positive sequence. As in [25],  $\underline{Y}^{ABC}$  allows obtaining a series of matrix relations describing the steady-state regime of the entire three-phase power system of Fig. 2. By introducing the matrix partitioning shown in Fig. 3, the following two sets of linear equations are obtained:

$$\underline{i}_{G}^{ABC} = \underline{Y}_{GG}^{ABC} \underline{u}_{G}^{ABC} + \underline{Y}_{GL}^{ABC} \underline{u}_{L}^{ABC}$$
(5)

$$\boldsymbol{\theta}^{ABC} = \underline{Y}_{LG}^{ABC} \, \underline{\boldsymbol{u}}_{G}^{ABC} + \underline{Y}_{LL}^{ABC} \, \underline{\boldsymbol{u}}_{L}^{ABC} \tag{6}$$

and by applying the standard *Gauss-Rutishauser* matrix reduction techniques, (6) can be written as:

$$\underline{\boldsymbol{u}}_{L}^{ABC} = -\left[\underline{\boldsymbol{Y}}_{LL}^{ABC}\right]^{-1} \underline{\boldsymbol{Y}}_{LG}^{ABC} \underline{\boldsymbol{u}}_{G}^{ABC}$$
(7)

and substituted in (5), it follows:

$$\underline{\underline{i}}_{G}^{ABC} = \left[\underline{Y}_{GG}^{ABC} - \underline{Y}_{GL}^{ABC} \left(\underline{Y}_{LL}^{ABC}\right)^{-1} \underline{Y}_{LG}^{ABC}\right] \underline{u}_{G}^{ABC} =$$

$$= \underline{Y}_{Geq}^{ABC} \underline{u}_{G}^{ABC}.$$
(8)

The phase matrix  $\underline{Y}_{Geq}^{ABC}$  models the *Ward equivalent* network [33] as seen at the generator sections. By observing Fig. 4, the reversed structure of (8), *i.e.*,:

$$\underline{u}_{G}^{ABC} = \left[\underline{Y}_{Geq}^{ABC}\right]^{-1} i_{G}^{ABC} = \underline{Z}_{Geq}^{ABC} i_{G}^{ABC}, \qquad (9)$$

it can be seen that the vector of the injected currents by the slack current generator can be computed as follows:

$$\underline{J}_{a}^{ABC} = \underline{Y}_{Geq,aa}^{ABC} \underline{\mu}_{a}^{ABC} , \qquad (10)$$

where  $\underline{Y}_{Geq,aa}^{ABC}$  is the inverse of the diagonal first block matrix of the impedance matrix  $\underline{Z}_{Geq}^{ABC}$  (see Fig. 4): it represents the three-phase concept of admittance as seen at the slack bus section.

It is worth noting that the above-mentioned mathematical steps can be thought as the three-phase generalization of the steady-state formulation of PFPD [25].

Notwithstanding, differently from PFPD, the current vector  $\underline{J}_{a}^{ABC}$  of the slack bus is not immediately known by means of (10). In fact, only the positive sequence slack voltage  $\underline{u}_{a,P}$  is scheduled, whereas  $\underline{u}_{a}^{ABC}$  is not completely known *a priori*, as it depends on the negative and zero sequence voltages of the slack section after (11), *i.e.*:

$$\underline{\boldsymbol{u}}_{\boldsymbol{a}}^{ABC} = \underline{\boldsymbol{u}}_{\boldsymbol{a},\boldsymbol{P}} + \underline{\boldsymbol{u}}_{\boldsymbol{a},\boldsymbol{N}} + \underline{\boldsymbol{u}}_{\boldsymbol{a},\boldsymbol{\theta}} \,. \tag{11}$$

In turn, the negative and zero sequence slack generator voltages depend on the negative and zero current circulations in its sequence networks, as shown in Fig. 5.



**FIGURE 4.**  $\underline{Z}_{Geq,aa}^{ABC}$  represents the network as seen from the slack section: its inverse allows computing the vector  $\underline{J}_{a}^{ABC}$  from  $\underline{u}_{a}^{ABC}$ 

However, the slack section sequence voltages are not analytically determinable. In fact, if the network as seen at the slack section is assumed to be unbalanced, the extent of this network unbalance varies from case to case. Thus, an iterative scheme to determine such sequence voltages allows finding  $\underline{u}_{a}^{ABC}$ . This iterative scheme is described thoroughly in Sect. IV. Once the convergence is achieved, the knowledge of  $\underline{u}_{a,P}$ ,  $\underline{u}_{a,N}$ ,  $\underline{u}_{a,\theta}$  allows computing  $\underline{u}_{a}^{ABC}$  by means of (11). As a result,  $\underline{J}_{a}^{ABC}$  can be computed by means of (10), so the vector  $\underline{i}^{ABC}$  is immediately known. The subsequent application of (9) and (7) allows computing  $\underline{u}_{G}^{ABC}$  and  $\underline{u}_{L}^{ABC}$  respectively. Therefore, the three-phase steady state regime of the network is completely defined.



**FIGURE 5.** Dependency of the slack generator voltage  $\underline{\mu}_{a}^{ABC}$  on its sequence networks.

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### III. THE PHASE COMPONENT MODELLING OF THE NETWORK COMPONENTS

In this section, it is explained how both the power flow constraints and the network elements are modelled and included inside the three-phase matrices  $\underline{Y}_{SGL}^{ABC}$  and  $\underline{Y}_{N}^{ABC}$ .

### A.THE ELEMENTS BELONGING TO THE MATRIX $\underline{Y}_{SGL}^{ABC}$

The  $\underline{Y}_{SGL}^{ABC}$  matrix holds all the generator and load models of the network.

#### 1) SLACK GENERATOR

One of the main novelties of this paper deals with the slack generator treated as a quasi-ideal current generator. This choice comes from the possibility to make a source transformation by considering the impedance of the equivalent positive sequence network exciting the system as infinitesimal [25] (*e.g.*,  $j10^{-5}$  p.u.). Hence, the slack generator positive sequence network can be considered as an ideal current source in parallel with an infinite shunt admittance (see Fig. 5). However, it was demonstrated in [25] that from an engineering point of view, an infinite admittance is an admittance with a very arbitrarily large value (*e.g.*,  $-j10^5$  p.u., as it will be detailed in Sect. IV).

Thus, the sequence component admittance matrix  $\underline{Y}_{a}^{\theta PN}$  modelling the three-phase slack generator can be built (see Fig. 5), and its phase matrix  $\underline{Y}_{a}^{ABC}$  can be derived by means of the Fortescue transformations:

$$\underline{Y}_{a}^{ABC} = \underline{F}^{-1} \underline{Y}_{a}^{\theta PN} \underline{F}$$
(12)

Therefore, the three-phase slack generator modelled as an admittance matrix can be embedded inside the "all-inclusive"  $\underline{Y}_{SGL}^{ABC}$  matrix.



FIGURE 6. Calculation of the phase admittance matrix  $\underline{Y}_{g}^{ABC}$  of the generator connected to the section g and its inclusion inside  $\underline{Y}_{SGL}^{ABC}$ .

#### 2) GENERATORS

Synchronous machines are the most employed devices for power generation in the transmission networks. From a structural point of view, a synchronous machine can be considered a symmetrical device, so its steady-state regime can be studied by means of the sequence networks represented in Fig. 6: only the positive sequence network is the active one, since the electromechanical power conversion takes place in this sequence. The presence of the negative and zero sequence passive networks, however, is fundamental to consider possible voltage distortions, due to negative and zero-sequence current flows. For steady-state transmission networks, these current flows are caused by the structure asymmetries (i.e., mainly non-transposed lines), and by the unbalanced loads. By considering a generator connected to the section g, its equivalent positive sequence admittance can be computed as in the following relations:

$$\frac{S}{\underline{s}_{g,P}} = -\underline{u}_{g,P} \underline{i}_{g,P}^{*}; \quad \underline{i}_{g,P} = -\frac{S}{\underline{u}_{g,P}} = \underline{y}_{g,P} \underline{u}_{g,P}; \\ \rightarrow \underline{y}_{g,P} = -\frac{p_{g,P}}{|\underline{u}_{g,P}|^{2}} + j \frac{q_{g,P}}{|\underline{u}_{g,P}|^{2}}.$$
(13)

Eq. (13) is the three-phase generalization of the PV constraints modelled in PFPD [25] as negative (sign, not sequence!) passive admittances: this generator modelling allows their inclusion into the unique  $\underline{Y}^{ABC}$ . Therefore, the building of the diagonal sequence admittance matrix  $\underline{Y}_{g}^{\theta PN}$ , shown in Fig. 6, is immediate. The phase matrix  $\underline{Y}_{g}^{ABC}$  can be immediately found by means of the Fortescue transformations applied to  $\underline{Y}_{g}^{\theta PN}$ :

$$\underline{Y}_{g}^{ABC} = \underline{F}^{-1} \underline{Y}_{g}^{\theta PN} \underline{F}$$



For each load typology, the analysis is conducted in sequence frame of reference, and the resulting sequence admittances are stored in a diagonal matrix (*azure:* zero sequence admittance, *yellow:* positive sequence admittance, and *green:* negative sequence admittance). The positive sequence admittance for each typology *t* (*yellow*) is computed as in (14).

FIGURE 7. Treatment of the three-phase balanced load (at the section *m*) as the composition of two types of load and shunt capacitive compensator.



Eventually, the phase admittance matrix  $\underline{Y}_{g}^{ABC}$  can be stored in the *g*-th position of  $\underline{Y}_{SGL}^{ABC}$  (Fig. 6).

#### 3) LOADS

A three-phase balanced load in section m can be easily treated by means of the sequence approach [24].

For such loads, the complex power absorbed by each terminal section are equal to:

$$\underline{S}_{m,A} = \underline{S}_{m,B} = \underline{S}_{m,C} \,.$$

As shown in Fig. 7, these loads can be thought as composed of three different types: (1) the asynchronous load, (2) the static, and (3) the reactive power compensation (to achieve a specific power factor target) devices. Such kinds of loads can be considered in parallel with each other and no mutual coupling is considered.

By denoting with  $\underline{S}_t$  the complex power absorbed by each of the three types of load under the nominal positive voltage (1 *p.u.*), its positive sequence star admittance can be computed as:

$$\underline{y}_{P,t} = \frac{\underline{S}_{P,t}^{*}}{\left|\underline{u}_{P,t}\right|^{2}} = \frac{p_{P,t} - jq_{P,t}}{1^{2}}, \ t=1,3$$
(14)

Obviously, the positive complex power  $\underline{S}_{P,t}$  absorbed by each load typology must be known *a priori*.

Eq. (14) is the generalization of PQ constraints modelled in PFPD [25] as passive admittances: this load modelling allows computing its corresponding phase frame of reference matrix to be included into the unique  $\underline{Y}^{ABC}$  total bus admittance matrix (see (15)).

For the static load and the reactive power compensation devices, the positive and negative sequence admittances are equal. In the case of the asynchronous loads, instead, the negative sequence admittance can be considered equal to

 $\xi_{\underline{y}_{P,I}}e^{j\Psi}$ , where  $\xi=5\div7$  and  $\psi=-60^{\circ}\div-75^{\circ}$  [24].

Moreover, since each type of load is considered as being symmetrical, its corresponding sequence admittance matrix is diagonal (Fig. 7).

Eventually, by exploiting the linearity of the system, these sequence matrices can be summed, and the phase admittance matrix  $\underline{Y}_{m}^{ABC}$  of the balanced load in the section *m* can be computed by means of the Fortescue transformations:

$$\underline{Y}_{m}^{ABC} = \underline{F}^{-I} \left( \underline{Y}_{1,m}^{0PN} + \underline{Y}_{2,m}^{0PN} + \underline{Y}_{3,m}^{0PN} \right) \underline{F}.$$
(15)

Similarly to the generator shown in Fig. 6,  $\underline{Y}_{m}^{ABC}$  can be stored in the *m*-th position of  $\underline{Y}_{SGL}^{ABC}$ .

The conciseness of this matrix approach allows modelling all the radial subtransmission/distribution networks supplied by the EHV/HV transmission sections as single equivalent loads (see Fig. 8).



FIGURE 8. Transformation of a radial sub-transmission/distribution system into an equivalent load.

		1	2		10	
$\underline{u}_{I}^{ABC}$	1	$\underline{Z}_{R(1,1)}^{ABC}$	$\underline{Z}_{R(1,2)}^{ABC}$		$\underline{Z}^{ABC}_{R(1,10)}$	$\underline{i}_{1}^{ABC}$
$\underline{u}_{2}^{ABC}$	2	$\underline{Z}_{R(2,1)}^{ABC}$	$\underline{Z}_{R(2,2)}^{ABC}$			<b>0</b> <sup>ABC</sup>
	-					
$\underline{u}_{10}^{ABC}$	10	$\underline{Z}_{R(10,1)}^{ABC}$			$\underline{Z}_{R(10,10)}^{ABC}$	<b>0</b> <sup>ABC</sup>
$\underline{u}^{ABC}$	-		$\underline{Z}_{R}^{ABC}$	$= \left[\underline{Y}_{R}^{ABC}\right]$	1	<i>i</i> <sup>ABC</sup>
$(3 \cdot 10 \times 10)$	1)		(3.10	)× 3·10)		$(3 \cdot 10 \times 1)$
FIGURE 9. Repre	sentat	ion of (1	6).			

For instance, the equivalent load formation of the radial network of Fig. 8 is described. This network consists of ten sections, so the associated three-phase network admittance matrix is  $(3\cdot10)\times(3\cdot10)$ , and it must be summed to the shunt admittance matrix (in which the loads are stored in the 8-th, 9-th and 10-th positions).

Consequently the  $(3.10)\times(3.10)$  "all-inclusive" matrix  $\underline{\underline{Y}}_{R}^{ABC}$  can be computed. Therefore, the impedance matrix  $\underline{\underline{Z}}_{R}^{ABC}$  is derived by inversion, *i.e.*,

$$\underline{\underline{u}}^{ABC} = \left[\underline{\underline{Y}}_{R}^{ABC}\right]^{-1} \underline{i}^{ABC} = \underline{\underline{Z}}_{R}^{ABC} \underline{i}^{ABC}.$$
 (16)

It can be immediately noted (see Fig. 9) that the subvector of the absorbed currents at the section 1 can be computed as follows:

$$\underline{i}_{l}^{ABC} = \underline{Y}_{R(l,l)}^{ABC} \underline{u}_{l}^{ABC}, \qquad (17)$$

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where  $\underline{\underline{Y}}_{R(I,I)}^{ABC}$  is the inverse of the first diagonal block element of  $\underline{\underline{Z}}_{R}^{ABC}$  ( $\underline{\underline{Z}}_{R(I,I)}^{ABC}$ ). Thus,  $\underline{\underline{Y}}_{R(I,I)}^{ABC}$  is the (3×3) admittance matrix modelling the entire network as an "equivalent load" as seen at the section 1.

$$\underline{Y}_{eq,1}^{ABC} = \underline{Y}_{R(1,1)}^{ABC}$$

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# B. THE ELEMENTS BELONGING TO THE NETWORK MATRIX $\underline{\mathbf{Y}}_{N}$

The network matrix  $\underline{Y}_{N}^{ABC}$  holds all the other elements of the network but the generators, and the loads. The steady-state three-phase modelling of the network devices and their insertion inside  $\underline{Y}_{N}^{ABC}$  is a well-investigated topic [12, 24], and different modelling approaches can be adopted.

The modelling used in this paper is briefly presented in the following.

1) ELECTRICAL LINES (OHLs, insulated cables, GILs)

Transmission OHLs, insulated cables, and GILs are firstly modelled by considering the presence of all their active and conductors (e.g., ground wires, metallic passive screens/armours, and enclosures). For this purpose, a multiconductor approach with n conductors in parallel with each other and with the ground is exploited [27-29]. Thus, single and double-circuit lines, and other complex configurations can be indifferently considered, without neglecting the real asymmetries of each line. The method is known as Multiconductor Cell Analysis (MCA) developed in 2009 by R. Benato. In order to provide some brief reminders, in Fig. 10, an elementary cell  $\Delta$  of a generic line is shown: it is modelled by means of three blocks: the longitudinal one (L), and the two transversal ones (Ts and  $T_R$ ). These blocks form a generalised multiconductor  $\pi$ circuit, and are modelled through the admittance matrices  $\underline{Y}_L$ , <u> $Y_{TS}$ </u>, and <u> $Y_{TR}$ </u>. For electrical lines, it is almost always  $\underline{Y}_{TR} = \underline{Y}_{TS} = \underline{Y}_{T}$ . It is worth reminding that  $\underline{Y}_{L}, \underline{Y}_{T}$  are computed by means of the Carson/Schelkunoff-Pollaczek/Carson-Clem formulations [30-32], and the classical formulations for the capacitive and conductive couplings between all the line conductors respectively.

By combining  $\underline{Y}_L$ ,  $\underline{Y}_T$ , the matrix formulation linking the entering currents at the sending and receiving ends of the cell  $\Delta$  with their voltages is represented in (18).

Then, the matrix cascade of each cell for computing the matrix of the entire line is applied. Fig. 12 shows the analytic formulation of the equivalent matrix of two cells: this operation must be repeated depending on the number of cells (if *c* is the number of cells, *c*-1 computations must be done). Thus, a unique  $(n \times n)$  admittance matrix of the entire line as seen at its terminals can be computed.

It is important to highlight that this MCA allows representing each element inside each cell. All these elements must be modelled by means of suitable circuits: their admittance matrix representations are performed by considering electrotechnical evaluations [27, 28, 33, 34].



FIGURE 10. Multiconductor cell represented as a generalized  $\Pi$ -circuit [30].



FIGURE 11. Matrix equivalent to the cascade of two multiconductor cells [31].

Once the  $(n \times n)$  admittance matrix of the electrical line is computed, the Kron's matrix reduction [35] is applied in order to consider the behaviour of the system as seen only at the phase conductors (see Fig. 13).

This reduction is fundamental and unavoidable since this power flow involves only the three phase active conductors.

This reduction can be achieved under the assumption that either the voltages (or alternatively the currents) of the passive conductors at the ends of the electric line are null. Hence, the dimensions of the line admittance matrices decrease (e.g.,  $(6 \times 6)$ -matrices for single-circuit lines). Thus, the effects of the passive conductors on the phase conductors is not neglected, even if this assumption of null voltages of the passive conductors is not completely true. For instance, Fig. 12 shows this matrix reduction for a five-conductor OHL line (three phases and two ground wires) for two different ground wire arrangements: 1) the two ground wires are earthed at their ends, 2) the two ground wires are unearthed or insulated at their ends. In both cases, the null voltage/current components allow erasing the columns of the  $\underline{Z}_{line}$ / $\underline{Y}_{line}$  matrices associated to the passive conductors. Similarly, also the rows of the  $\underline{Z}_{line}/\underline{Y}_{line}$  matrices associated to the passive conductors can be erased, since both the voltage and current quantities of the passive conductors must

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not be considered. Therefore, the  $(6 \times 6)$  admittance matrices  $\underline{\mathbf{Y}}_{line,eq}$  can be computed for both the cases. In Sect. VI, the influence on power losses of the two different ground wire practices are thoroughly evaluated. In this paper, this procedure is named as row/column elimination technique. It is worth noting that for the formation of  $\underline{\mathbf{Y}}_{line,eq}$  in the first case (earthed ground wires), no matrix inversion is needed. This fact is relevant, since the great majority of the OHL ground wires in real power systems are earthed (at the substation earthing grids and also at each tower). It can be proved that the computation of  $\underline{Y}_{line,eq}$  can be obtained also by means of the standard Gauss-Rutishauser matrix reduction techniques. However, this procedure is more computational expensive than the row/column elimination one. This matrix reduction is also applicable to insulated cables, and to GILs. However, the following considerations must be kept in mind when the power flow solutions are assessed:

- The Kron's reduction on OHL is generally based on a "light" assumption. In fact, the passive conductors of such lines are earthed at each tower and at the substation earthing grids, so the assumption of null voltage is quite accurate.
- The Kron's reduction on insulated cables is generally based on a "heavy" assumption. In general, in fact, the induced voltages in the passive conductors could not be negligible. In particular, they depend on the different screen bonding/earthing techniques (*e.g.*, cross bonding arrangement for HV/EHV cables [36], single-point bonding for very short HV/EHV cables, and solid bonding arrangements for MV/LV cables). Differently for GILs, the solid-bonding arrangement (or even the multiple point-bonding [37, 38]) allows considering the enclosure voltages practically null.

In any case, these simplifying hypotheses are considered licit for a good three-phase power flow study of a transmission network, as shown in Sect.V. A very precise steady-state regime evaluations on the passive conductors can be achieved by means of MCA [27, 28, 33, 39] which is a powerful circuital tool but not a power flow one. Further researches are ongoing to combine MCA with this power flow so to obtain a general multiconductor power flow. It is worth reiterating that the steady state regimes of passive conductors cannot be intrinsically known with the present power flow.

#### 2) POWER TRANSFORMERS

As the synchronous machines, the two/three-winding transformers can be considered symmetrical devices from a structural point of view. Thus, their steady-state regime can be licitly studied by means of their sequence networks. For a two-winding transformer, its positive-sequence two-port network is immediately inferable from its nameplate data. Its negative-sequence two-port network is the same of the positive one, except for the phase shift angle which is always the opposite of the positive one. The zero-sequence two-port network, instead, depends on its particular winding earthing and configuration.



GROUND WIRES <u>UNEARTHED</u> FROM THE SUBSTATION EARTHING GRIDS



FIGURE 12. Kron's reduction applied to two different five-conductor OHLs (with the OHL ground wires earthed and unearthed).

For these networks, their (2×2) admittance matrices can be computed, and opportunely put together in a unique (6×6) admittance sequence matrix  $\underline{Y}_{2n-tr}^{\theta PN}$  (see App. I).

Then, the phase admittance matrix  $\underline{Y}_{2w-tr}^{ABC}$  can be computed by means of the Fortescue generalised transformation [24]:

$$\underline{Y}_{2w-tr}^{ABC} = \underline{F}^{-1} \underline{Y}_{2w-tr}^{0PN} \underline{F}$$
(19)

where  $\underline{F}$  is the generalized (6×6) Fortescue matrix. The aforementioned procedure is also applicable to the threewinding transformers. The three-port sequence networks are described by means of (3×3) admittance matrices. These matrices are put together in a unique (9×9) admittance sequence matrix  $\underline{Y}_{3w-tr}^{ABC}$ , and then the phase matrix  $\underline{Y}_{3w-tr}^{ABC}$  is computed.

#### 3) SHUNT ELEMENTS

The following power system shunt elements are considered:

- capacitive/inductive shunt compensation in electrical substations;
- shunt compensation of long EHV/HV cable systems.

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Their admittance matrices can be easily computed by means of the inspection method or by inversion of their impedance matrices [28] and must be overlapped in the suitable positions of the three-phase admittance matrix  $\underline{Y}_{N}^{ABC}$  [36].

#### **IV. THE HYBRID ITERATIVE PROCEDURE**

The complete knowledge of  $\underline{Y}_{N}^{ABC}$  and  $\underline{Y}_{SGL}^{ABC}$  (and thus of the

"all-inclusive" matrix  $\underline{Y}^{ABC}$ ) allows computing the threephase power flow solution by means of the procedure described in Sect. II. However, the elements of  $\underline{Y}_{SGL}^{ABC}$  are not completely known since they depend on the power-flow solution.

Thus, an iterative method to compute the three-phase power flow problem is proposed. The iterative method does not need any numerical analysis technique, as in [25].

It is well known that a good initial guess is necessary for any iterative algorithm. In particular, the initial guess of  $\underline{V}_{SGL}^{ABC}$  is built by considering the following values:

### For the SLACK section: $\underline{y}_{a,P} = -j \cdot 10^5$ p.u.

As in [25], the slack generator is conceived as a quasi-ideal current source: hence, the slack section constraint can be stored inside  $\underline{Y}_{SGL}^{ABC}$ . Since the scheduled slack voltage is the positive one, the quasi-ideal current generator is set in the positive sequence network, as shown in Fig. 5.

The discussion about the choice of the initial value of  $\underline{y}_{a,P}$  is the same of the one described in [25].

For the negative and zero sequence networks, instead, the typical synchronous machine admittance values are considered, according to the machine typology chosen for the slack one.

#### For the load sections:

The load matrices  $\underline{Y}_{m}^{ABC}$  of all the load typologies described in sect. IV are initially computed by considering their positive sequence nominal voltage, *i.e.*, 1 p.u.

The three-phase voltages in the load sections, in fact, are actually the unknowns of the problem. However, if the network interconnections do not introduce high voltage drops, the choice to keep the load voltages to their nominal positive sequence value (1 p.u.) can be considered as a valid initial guess.

#### For the generator sections:

Eq. (13) allows computing the first guess for the positive sequence admittance which models the generator in section g:

$$\underline{y}_{g,P} = -\frac{p_{g,P}}{\left|\underline{u}_{g,P}\right|^2} + j \frac{q_{g,P}}{\left|\underline{u}_{g,P}\right|^2}, \text{ for } k=0.$$
(20)



FIGURE 13. Initial guess (k=0) of the generator reactive power  $q_b \div q_g$ .

Eq. (20) is the application of (13) for the initial guess of the iterative procedure.

For the positive sequence, it is worth noting that the only unknown value is the reactive power injected  $q_{g,P}$  in section g, since it depends on the power flow solution. Thus, all the generator reactive power initial guesses  $q_b \div q_g$  (for k=0) must be estimated in detail.

The discussion on the choice of the initial reactive power of the generators is the same of [25]: the network is firstly considered as ideal (the matrix  $\underline{Y}_{N}^{ABC}$  is imaginary), and (8) is applied. Then, after the Fortescue transformation, the vector of the reactive power injected by the positive sequence network can be computed. Fig. 13 summarizes the reactive power estimation procedure.

Also, in this paper, the three-phase power flow region of attraction of the solution can be assessed [40]. In fact, also in this algorithm, the only initial values are the reactive power  $q_{b} + q_{g}$ , of the generator sections. Therefore, evaluations on how ITER. changes with the initial generator reactive power guess can be made (see Sect. V).

#### A. The load/generator correcting current method

After the initial guess, the correcting-vector iterative procedure [25] is achieved by means of the formulae (21)+(25), and depicted in the flow-chart of Fig. 14.

This iterative scheme is basically the generalization of the procedures in [25].

The formulae (21)÷(25) are represented for the *k*-th iteration:

$$\underline{\boldsymbol{\mu}}_{G}^{ABC} = \underline{\boldsymbol{Z}}_{Geq}^{ABC} \left[ \underline{\boldsymbol{\varDelta}}_{G,c_{-q}}^{ABC} - \underline{\boldsymbol{Y}}_{GL}^{ABC} (\underline{\boldsymbol{Y}}_{LL}^{ABC})^{-I} \underline{\boldsymbol{\varDelta}}_{L,c}^{ABC} \right] \quad (21)$$

$$\underline{\underline{u}}_{L,c}^{ABC} = -\left[\underline{\underline{Y}}_{LL}^{ABC}\right]^{*} \underline{\underline{Y}}_{LG}^{ABC} \underline{\underline{u}}_{G}^{ABC} + \left[\underline{\underline{Y}}_{LL}^{ABC}\right]^{*} \underline{\underline{A}}\underline{\underline{i}}_{L,c}^{ABC} (22)$$

$$\underline{\underline{A}}_{L,c}^{i\theta PN} = \underline{\underline{Y}}_{LL} \bigcirc \left(\underline{\underline{I}}_{L,c}^{i\theta PN}\right)^{*} (22)$$

$$\underline{\mathcal{A}I}_{L,c} = -\underline{Y}_{L,P} \odot \left( I - \left| \underline{\mathcal{U}}_{L,c,P} \right| \right) / \left( \underline{\mathcal{U}}_{L,c,P} \right)$$
(23)  
$$\mathbf{\mathcal{A}};^{ABC} = \mathbf{Y}^{ABC} \mathbf{\mathcal{H}}^{ABC} + \mathbf{Y}^{ABC} \left[ \mathbf{Y}^{ABC} \right]^{-1} \mathbf{\mathcal{A}};^{ABC}$$
(24)

$$\underline{A}\underline{i}_{G,c}^{n,L,c} = \underline{Y}_{Geq}^{n,L,c} \underline{u}_{G,c}^{n,L,c} + \underline{Y}_{GL}^{n,L,c} \left[ \underline{Y}_{LL}^{n,L,c} \right] \underline{A}\underline{i}_{L,c}^{n,L,c}$$
(24)

$$\underline{\mathcal{A}i}_{G,c\_q,P} = -j \left[ Im \left( \underline{u}_{G,c,P} \otimes \underline{\mathcal{A}i}^{*}_{G,c,P} \right) \right] / \underline{\underline{u}}^{*}_{G,c,P}$$
(25)

Eq. (25) represents the positive sequence quadrature component current vector that springs out the same injection of positive sequence reactive power of (24). These generator current injections computed in (25) are more suitable to correct the positive sequence reactive power which are the real unknowns of the three-phase power flow (positive sequence active power are constrained, as explained in Sect. II). This is the three-phase generalization of the concept already presented in PFPD [25].

Eq. (25) must not be applied for the slack section since both the active and reactive power are unknown quantities:

$$\underline{\varDelta i}_{G,c_q,P}(1,1) = \underline{\varDelta i}_{G,c}(1,1)$$

For each iteration, (21) and (22) allow computing the phase voltages of the generator and load sections, and can be obtained considering the generalization of (5) and (6).

Eq. (23), (24), and (25) allow computing the positive sequence correcting currents to be applied iteratively in each load and generation section. These correcting currents are computed starting from the technical constraints given to the sequence component frame of reference. Afterwards, these currents must be converted in the phase frame of reference to be embedded into (21) and (22) of the subsequent (k+1)-th iteration.

Differently from the other methods, these formulations are defined in both the sequence component and phase frame of reference. Therefore, the impact of the system unbalance due to the presence of negative and zero sequence currents/voltages can be assessed. For this reason, this three-phase approach is referenced as a *hybrid* one.

Fig. 14 schematically represents the three-phase power flow algorithm flow-chart. It is worth noting the alternations of the phase formulations with the sequence component ones through the  $\underline{F}$  and  $\underline{F}^{I}$  transformations for each cycle (once again the *hybrid* approach).

In Fig. 14, it can be seen that the correcting currents for k=0 are all set to zero except for the slack bus sub-vector. After using (21), the application of  $\underline{F}$  allows computing the generator voltages in sequence component frame of reference. In this way, the  $\underline{T}_x$  transformation allows correcting the positive sequence voltage of all the generators: a new corrected vector  $\underline{u}_{GI,c}$  can be built by changing the calculated positive sequence voltage magnitudes with the constrained ones, but by keeping  $\delta_b \dots \delta_g$  angles unchanged.

Afterwards, the application of  $\underline{F}^{I}$  allows passing to the phase frame of reference and applying (22) to compute the

phase voltage vector of loads  $\underline{\boldsymbol{\mu}}_{L,c}^{ABC}$ . Thus, all the phase components of the voltage vectors are computed. These block vectors are necessary to compute the correcting current vectors by means of  $\underline{\boldsymbol{F}}$  and  $\underline{\boldsymbol{F}}^{I}$  transformations, and (23), (24), (25). The procedure is iterated until convergence, *i.e.*, until any mismatch of positive sequence generator voltage is within the tolerance.

### B. The generator correcting current method

So far, the algorithm is based on the calculation of two correcting current sets (one for the generator sections  $\Delta \underline{i}_{G}^{ABC}$ , and one for the load sections  $\Delta \underline{i}_{L}^{ABC}$ ). In order to reduce the computational cost of each iterative cycle, this section investigates the possibility of using an alternative iterative scheme, by exploiting only the generator correcting current set.

Thus, by posing  $\Delta \underline{i}_{L}^{ABC} = 0$  the above-mentioned formulation becomes:

$$\underline{\mu}_{G}^{ABC} = \underline{Z}_{Geq}^{ABC} \underline{\Delta i}_{G,c_q}^{ABC}$$
(26)

$$\underline{\mathbf{\Delta i}}_{G,c}^{ABC} = \underline{Y}_{Geq}^{ABC} \underline{\mathbf{u}}_{G,c}^{ABC}$$
(27)

$$\underline{\Delta i}_{G,c\_q,P} = -j \left[ \operatorname{Im} \left( \underline{u}_{G,c,P} \otimes \underline{\Delta i}_{G,c,P}^* \right) \right] / \underline{u}_{G,c,P}^*$$
(28)



FIGURE 14. Flow chart of the PFPD\_3P load/generator correcting current iterative scheme for the first iteration.

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FIGURE 15. Flow chart of the PFPD\_3P load/generator correcting current iterative scheme for the first iteration (i.e.,  $\Delta \underline{i}_{L}^{ABC} = \theta$ ).

Eq. (28) (which is the same of (25)) must not be applied to the slack section since the active and reactive power are unknown quantities:

$$\underline{\Delta i}_{G,c,q,P}(1,1) = \underline{\Delta i}_{G,c,P}(1,1).$$

As it will described in the following section, the series of (26), (27), and (28) allows computing the power flow, bringing to a CPU-Time and ITER reduction.

The authors think that this result is remarkable since a three-phase power flow solution is achieved by applying only three iterated formulae.

Fig. 15 shows the flow-chart of the algorithm without correcting the load sections.

No matrix inversion is necessary for each iteration, differently from [24], and this advantage is fundamental when considering three-phase power flows.

#### V. PFPD\_3P PERFORMANCE ASSESSMENTS

### A. Preliminary comparison between the new PFPD\_3P and the old PF[24]\_3P

In order to check the improvements and the enrichments of PFPD\_3P versus the old algorithm [24] (which is called as PF[24]\_3P in the following), a performance comparison between their two implementations is shown. These two algorithms are implemented in Matlab environment and their performance are assessed under the same conditions. Several fictitious transmission networks are tested, which differ in topologies and load/generation scenarios. Table I shows ITER. and CPU-time comparisons between PFPD\_3P and PF[24]\_3P for a voltage tolerance equal to 2 mV, by testing the 18-section network (see Fig. 16 for the representation and App. II for the description) and other test networks. The convergence tolerance used is very small to produce a very accurate power flow solution. In these networks, all the loads

are considered as "equivalent loads" (see Sect. III A3), hence only the generator correcting current method (see Sect. IV B) is employed. Furthermore, it is worth underlining that the old PF[24] 3P allowed only the generator correcting current method and not also the generator/load correcting current one. The tests are performed in a PC using an Intel (R) Core (TM) i7-7700K CPU @ 4.2 GHz processor, with a 32 GB RAM. By observing Table I, it is possible to note a CPUtime improvement for PFPD 3P, and this fact is especially observed for the 300 section case: a considerable CPU time reduction is achieved. In fact, the novel iterative cycle is composed of only three formulae, i.e., (26)÷(28), and this synthetic formulation is due to the three-phase slack generator inclusion inside the "all-inclusive" admittance matrix. Hence, the single-phase improvements of the algorithm presented in [25] are still valid in the three-phase generalisation presented in this paper. Moreover, in order to check the PFPD 3P solution consistency, extensive comparisons with the solutions of PF[24] 3P show negligible maximum solution differences (*i.e.*, 10<sup>-7</sup> p.u. for the phase magnitudes, and  $10^{-6}$  deg. for the phase angles).

#### B. Comparison between the new PFPD 3P and DGS

In order to validate PFPD\_3P with a reliable software benchmark, all the analysed networks are also tested in the commercial software DGS. The DGS software implements the Newton-Raphson method to compute the three-phase power flow solution. As in [25] and in [41], a self-made interface procedure to automatically pass all the network data from Matlab environment to DGS software is exploited. Firstly, all the power flow solution differences between PFPD\_3P and DGS are assessed, and maximum differences of the orders of magnitude equal to  $10^{-3}$  p.u. for the phase magnitudes, and  $10^{-2}$  deg. for the phase angles are found. The minimum differences are instead of the orders of magnitude of  $10^{-6}$  p.u. for the phase magnitudes, and  $10^{-4}$  deg. for the phase angles. Such differences confirm the very good agreement between PFPD\_3P and DGS solutions.

Table II compares ITER and CPU-time of PFPD\_3P and DGS by considering both the generator and generator/load correcting current methods (see Sect. IV A, and Sect. IV B, respectively), thus the 18-section network loads are considered both as lumped and equivalent. When the network loads are considered as equivalent ones, it is not possible to run the simulations with the generator/load correcting current method (grey area in Table II).

 TABLE I

 CPU-times and Iter for New PFPD\_3P and Old PF[24]\_3P

 with a Maximum Positive Sequence Voltage Tolerance of 2 mV

	Gen correction								
	PFPD_3P		PF[24]_3P						
System	CPU Time (ms)	ITER	CPU Time (ms)	ITER					
18 sections	0.481	5	5.003	8					
41 sections	0.886	7	Convergence not ac	hieved					
60 sections	1.136	18	132.34	11					
300 sections	24.1	17	6720.0	18					
600 sections	78.0	17	31317.0	20					

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TABLE II CPU-TIMES AND ITER FOR PFPD\_3P AND DGS WITH A MAXIMUM ACCEPTABLE POWER FLOW MISMATCH OF 1 kVA FOR BOTH PFPF\_3P AND DGS

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		Gen correction				Gen/load correction			
	PF	PD_3P	D	GS	PFP	D_3P	DO	GS	
~ .	CPU	ITER	CPU	ITER	CPU	ITER	CPU	ITER	
System	Time		Time		Time		Time		
	(ms)		(ms)		(ms)		(ms)		
18 sections									
(equivalent	1.031	6	51.02	8					
loads)									
18 sections	0.773	5	29.14	5	4.624	8	25.98	5	

TABLE III CPU-times and Iter for PFPD\_3P and DGS with a Maximum Acceptable Power Flow Mismatch of 1 kVA for both PFPF 3P and DGS

	Gen correction			Gen/load correction				
	PFPD_3P		DGS		PFPD_3P		DGS	
System	CPU Time (ms)	ITER	CPU Time (ms)	ITER	CPU Time (ms)	ITER	CPU Time (ms)	ITER
18 sections	0.773	5	29.14	5	4.624	8	25.98	5
41 sections	0.907	7	43.71	7	6.417	9	41.78	4
60 sections	2.81	17	78.3	8	18.705	17	49.7	6
300 sections	95.12	14	158.7	4	150.7	17	152.8	4
600 sections	476.0	17	333.0	5	381.0	16	301.0	5

Table III compares ITER and CPU-time of PFPD\_3P and DGS by considering both the iterative approaches for four tested networks (18, 41, 60, 300 section networks). The 300-section network is a three-phase version of the classical single-phase IEEE-300 bus network, and it is chosen to demonstrate the efficiency of PFPD 3P when dealing with

large three-phase networks. Eventually, a 600 section network is considered for further testing the algorithm. Eventually, to use the same convergence criterion adopted by DGS, all the iterative cycles of Table II and III are stopped for a maximum acceptable power flow mismatch equal to 1 kVA. Table II and III allow inferring the following considerations:

- The CPU times of PFPD\_3P are always lower than the ones of DGS for the first four networks. However, the last case study shows a slightly trend reversal: this is due to the fact that DGS is an optimized software compared with a self-implemented Matlab-based algorithm. This means that each PFPD\_3P iterative cycle (*i.e.*, (21)÷(25) or (26)÷(28)) is faster than each DGS one.
- The generator correcting current method allows reducing the CPU-Time and ITER compared to the load/generator correcting current method. In fact, in the generator correcting current method, only three-iterated formulae are used (*i.e.*, (26)÷(28)).

About the two different above-mentioned iterative approaches, also their regions of attraction are different. This concept is graphically represented, for the 18-section network, in Fig 17. It is worth noting that the region of attraction for the generator correcting current method is almost always beneath the region of attraction of the other iterative method. But most importantly, the region of attraction of the generator correcting current method is more variable/sensitive. This is because, in this approach, the iterative scheme is based on the computation of the correcting currents in the generator section only. Thus, the initial generator reactive power estimation has a greater



impact in the correcting current calculation, and consequently in the convergence achievement. VI. POWER QUALITY EVALUATIONS BY MEANS OF PDPD\_3P

### In this section, some power quality evaluations on the 18section fictitious network are presented. These evaluations are increasingly important for the challenging future networks. Moreover, the remarks/comments for the 18section network are still valid/confirmed by the other tested networks. Therefore, PFPD\_3P makes possible the following technical evaluations:

#### A. Power quality variation with the length of the lines

The great majority of HV/EHV electrical lines are not transposed [20, 22]. This fact contributes to the power system unbalance increase, and this effect is stronger the longer the transmission lines are.

Fig. 18 shows, for instance, the section voltage unbalance factors for different line lengths: all the considered line lengths are the 50%, or 100%, or 150% of the 18-section network ones. Fig. 18 allows confirming how much the voltage unbalance factors grow in all the sections (both generation and load sections) as the line lengths increase.

**B.** Power quality variation with the power system loading In order to have a safe power system operation, the load sections should not be characterised by excessively high power absorptions. One of the reasons is due to the power system power quality. In fact, the more power the system absorbs, the higher the unbalance factors are (that is due to the higher current circulation in the power lines).











FIGURE 19. Voltage unbalance factors of each section of the 18-section network as the overall power system loading changes.

Fig. 19 shows the section voltage unbalance factors for different values of the apparent power absorbed by each section (the apparent power values are the 50%, 75%, 100%, 125% of the 18-section network ones: the scheduled active power of all the generators are also changed proportionally to guarantee the balance between generation and loading). It can be noted that the voltage unbalance factors tend to grow in the network sections as the network loading increases.

# C. Power quality variation with the percentage of asynchronous share

The load composition affects the unbalance factors of the system. In fact, the presence of a remarkable percentage of electrical machines into a load section have positive effects on the network power quality.

It is known, in fact, that the rotating electrical machinery can play a key role in the lowering of the negative sequence voltage levels, due to their high negative sequence admittance values.

For instance, Fig. 20 shows a voltage unbalance factor comparison (considering the 18-section network) by considering all the loads with the asynchronous shares equal to 0% (static load) and 60% respectively, at the same conditions (same power flow technical constraints and same network data). It is worth noting that in the case of an asynchronous share percentage of 0%, the voltage unbalance factors are higher. Physically, this is due to the higher negative sequence admittances of the asynchronous loads, which drain the negative sequence currents. Fig. 21 shows this concept: in the load sections the absorbed current unbalance factors grow (red line) when the percentage of the asynchronous share is turned up to 60%. The voltage symmetrisation, in fact, is due to the higher negative sequence current drain in the load sections (the transit sections are excluded from the representation of Fig. 21, since no current drain can occur in these network sections).

# D. Power quality improvement by means of synchronous compensators;

Synchronous compensators could play an important role in the future transmission networks, although the massive penetration of static devices which regulate the reactive power. In fact, the synchronous machines, in addition to regulating the reactive power flows, can lower the network

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voltage unbalance factors. Fig. 22 shows, for instance, how the voltage unbalance factor decreases in all the network sections when a unique synchronous compensator is applied at section 9 (see Fig. 17).

The presence of negative sequence currents in the network may have detrimental impacts on rotating equipment, *i.e.*, synchronous machines or induction motors. In fact, negative sequence currents cause rotating field moving in opposite direction to the rotor rotation. These fields produce pulsating torques/vibrations, induced currents, and machinery temperature rise which reduce both the machine life and efficiency. Table IV shows the negative sequence current flows in rotating equipment, by considering asynchronous shares equal to 0% and 60%. The case where a synchronous compensator is inserted at section 9 of the 18section network is also shown. In addition to the considerations on power quality, an important industrial fall out can be derived from the application of PFPD 3P, e.g., on the operation of the protections. In fact, suitable protections are installed to preserve the generators from continuous negative sequence current, which are typically set in a range 8÷15% of the machine rated current [20]. Therefore, the ability to compute the negative sequence current values is a basic knowledge to predict protection behaviours. TABLE IV

LOAD CONFIGURATIONS USING PFPD_3P (TOLERANCE = $10^{-7}$ P.U.)							
	0% ASYNCHRONOUS SHARES	60% ASYNCHRONOUS SHARES					
	$\underline{\boldsymbol{i}}_{\boldsymbol{S},N}\left(p.u. ight)$	$\underline{\boldsymbol{i}}_{\boldsymbol{S},N}\left(p.u.\right)$					
Generator SECTION 1	0.0166	0.011					
Generator SECTION 2	0.0288	0.0289					
Generator SECTION 3	0.0166	0.013					
Synchronous compensator SECTION 9	0.0291	0.0133					

NEGATIVE SEQUENCE CURRENT FLOWS (IN P.U.) IN ROTATING EQUIPMENT OF THE 18-SECTION NETWORK FOR TWO DIFFERENT ASYNCHRONOUS

*E.* Power losses comparisons by considering different ground wire earthing methods

The passive conductors of the AC electrical lines are subjected to induced voltages. Therefore, induced currents can circulate in such conductors, and their entities depend on the passive conductor earthing methods. These currents globally affect the power losses of the power system and their evaluations can be assessed by the present PFPF\_3P. The 18-section network is considered, and all the electrical lines are treated as OHLs (see Fig. 23). For this network, two different ground wire earthing arrangements are considered: the former with all the ground wires unearthed and insulated from the towers and from the substation earthing grids, and the latter with all the ground wires earthed.



FIGURE 20. Voltage unbalance factor comparison for the 18-section network with the asynchronous shares (a.s.) equal to 0% (static load) and 60% respectively.



FIGURE 21. Current unbalance factor comparison for the 18-section network with the asynchronous shares (a.s) equal to 0% (static load) and 60% respectively.





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FIGURE 23. The single and the double circuit line towers used to perform the power loss evaluation of Sect. VI E.

 
 TABLE V

 18-section Network Power Losses for Two Different (Earthed and Unearthed) Ground Wire Configurations Computed by

MEANS OF PFPD_3P (TOLERANCE = $10^{-7}$ P.U.)							
	EARTHED GROUND WIRES	UNEARTHED GROUND WIRES					
Total Power Losses [MW]	20.769	20.131					

These two configurations are modelled by considering the two different procedures expounded in Sect. III B,1 (Fig. 12), and by considering suitable resistance values to model the earth wire links along the lines by means of MCA.

In particular, the single-circuit line (see Fig. 23a) has two different ground wires (i.e., a steel and an OPGW ground wires:  $r=2.66 \ \Omega/\text{km}$  and  $r=0.28 \ \Omega/\text{km}$ , respectively), whereas the double-circuit line (see Fig. 23b) has only one steel ground wire ( $r=2.66 \Omega/km$ ). Moreover, the tower footing resistance ( $r_{tower}=15 \Omega$ ), and the soil resistivity  $(r_{soil}=100 \ \Omega m)$  are supposed to be equal for the two cases. The main difference between the two configurations is the ground wire/tower contact resistance which is  $r_{lcr}=1$  G $\Omega$  for the insulated ground-wire towers, whereas  $r_{so}=1 \text{ m}\Omega$  for the earthed ground wires. In Table V the power loss comparison between these two ground wire configurations is carried out: the network power losses, by considering all the ground wires earthed, are 3.17% greater than the case with the insulated ground wires. This percentage increase is the 0.03% of the global active power generated in the 18-section network (2.3722 GW). These simulations are performed by using the load/generation correcting current method with a convergence tolerance of 10<sup>-7</sup> p.u. However, a thorough power loss evaluation can be directly carried out by knowing exactly the steady state-regime of the passive conductors (that can be assessed with a passive conductor power flow tool, which it has never been developed). Therefore, the global losses can be estimated thoroughly. Moreover, the network losses due only to the ground wire presence can be estimated. A further research could combine PFPD 3P with the MCA method in order to achieve this goal.

#### **VII. OPEN QUESTIONS**

From the knowledge of the phase voltages in all the sections of the analysed network, all the section phase currents are determinable by means of the nodal (three-phase) admittance matrix. This is valid only for the active conductors (the phases), but obviously not for the passive ones (for instance the ground wires of OHLs or metallic screens of insulated cables). Nevertheless, in this paper, the effects due to those passive conductors can be included in the admittance matrix modelling such lines, by the Kron's reduction matrix techniques [35]. However, further researches are developing a multiconductor power flow, by combining the present technique with the MCA [27-29, 42, 43].

Thus, that future multiconductor power flow would allow directly considering both the currents and voltages in each section of all the active and passive conductors (metallic screens, ground wires, or enclosures of GILs [37, 38]) of the transmission lines. That future result could be conceived as the final generalization of this research.

#### VIII. CONCLUSIONS

A novel hybrid (with the simultaneous use of phase and sequence component frames of reference) three-phase power flow algorithm based on the slack generator treatment as a quasi-ideal current source, at positive sequence, is presented. This open algorithm combines the merits of each frame of reference without englobing the demerits deriving from the application of a unique frame of reference. Two different iterative procedures are developed (i.e., the generator and the load/generator correcting current methods), and their validation is carried out by means of extensive solution comparisons with the old power flow algorithm PF[24]\_3P, developed in 2000, and the commercial software DIgSILENT PowerFactory. Moreover, the paper shows a strong CPU-time improvement compared with the other methods. This is due to the low number of formulae for each iteration of PFPD 3P. By using the generator correcting current method only, it is possible to include in the model also large radial subtrasmission/distribution systems by considering them as equivalent lumped load sections, so to reduce the dimensions of the system. By this new three-phase power flow, a detailed power quality assessment of the HV/EHV network can be performed in terms of unbalance factors, and power losses also considering the passive conductors (e.g., ground wires of OHLs). A possible improvement of power quality is also presented by means of a synchronous compensator insertion into the EHV grid: the forecast of negative sequence currents into the synchronous generator and compensator sections plays a key role in investigating possible tripping of negative sequence protections. PFPD 3P, namely the three-phase generalization of single-phase PFPD, keeps all the merits of his "parent":

- It is an open and fast algorithm, a tool for researchers and a powerful ally to Transmission System Operators;
- The convergence procedure is based on the circuit theory and not on numerical analysis techniques;
- All the load, generator and slack bus sections are englobed into a unique bus admittance matrix: this is possible also for slack generator since it is considered as a quasi-ideal current source at positive sequence;

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- Convergence is guaranteed by the suitable injections of two correcting current vectors into all the generators (including slack one) and all the loads: alternatively, only correcting current vectors into all the generators (including slack one) can be used in order to further speed up the algorithm;
- This open algorithm allows obtaining strong performances in terms of greater precision of the solution (tolerance up to 10<sup>-15</sup> p.u.), shorter execution times.

Further researches are on-going towards the combination of MCA with this power flow algorithm in order to evaluate the steady-state regime of both active and passive conductors without any simplifying hypothesis. This future result could be conceived as the final generalization of this research.

#### **APPENDIX I**

In the load/generator current iterative procedure, a clarification about (23) *i.e.*,

$$\underline{\varDelta i}_{L,c}^{\theta PN} = -\underline{Y}_{L,P} \odot \left( 1 - \left| \underline{u}_{L,c,P} \right|^2 \right) / \left( \underline{u}_{L,c,P} \right)^*.$$

is necessary. In (23), the symbol " $\odot$ " takes on the meaning of "positive sequence multiplication". This notation is introduced to summarize the procedure giving the sequence correcting currents due to the positive sequence voltages  $\underline{u}_{L,c,P}$  only. Therefore,  $\underline{u}_{L,c,P}$  and the elements connected to the positive sequence voltages of the load admittance submatrix  $\underline{Y}_L$  must be considered in (23). All the elements connected to the positive sequence voltages of  $\underline{Y}_L$  are stored in the matrix indicated as  $\underline{Y}_{L,P}$ .

In order to explain how to compute  $\underline{Y}_{L,P}$ , an example involving only the (3×3) block load admittance  $\underline{Y}_m$  modelling the *m*-th load is considered. By making a simple consideration on the matrix/vector multiplication, it is clear that the impact of the positive sequence voltage  $\underline{u}_{m,P}$  on the sequence correcting currents  $\underline{Ai}_{m,c}^{0PN}$  is due to the second column of the matrix  $\underline{Y}_m$  only (see Fig. A1). Therefore, each element of  $\underline{Ai}_{m,c}^{0PN}$  is simply the product of the second column of  $\underline{Y}_m$  for the scalar  $\underline{u}_{m,P}$ . However, (23) indicates that the above-mentioned procedure must be applied for each load section: thus, the complete vector  $\underline{Ai}_{L,c}^{0PN}$  representative of all the load sections can be computed, by means of (23) uniquely.





Eventually, it worth clarifying that the squaring present in (23) is a point-wise squaring (each element of the vector  $|\underline{u}_{L,c,p}|$  must be squared).

#### **APPENDIX II**

The 18-section network (see Fig. 16) consists of three generator sections, fifteen load sections (eight of which are transit sections) connected each other by means of fifteen non-transposed electrical lines. The coexistence of both single and double (the line between sections 7 and 8) circuits is considered. All the loads are three-phase symmetrical ones. In section 9, it is possible to insert a synchronous compensator. Moreover, three-phase power flow studies with load sections or equivalent load sections can be assessed and the simulations can be carried out for both cases. In particular, when the equivalent loads are considered, the subtransmission/distribution network underlying their sections are characterized by the presence of seven feeders and seven transformers supplying seven loads. About that, Fig. 16 allows noting how the equivalent load in section 18 allows reducing all the fifteen underlying sections (from 19 to 33) in unique lumped one. Therefore, by considering all the loads (transit ones excluded) of the 18-section network, 105 sections are globally reduced into seven equivalent sections.

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