

QCD tests with Kaon decays

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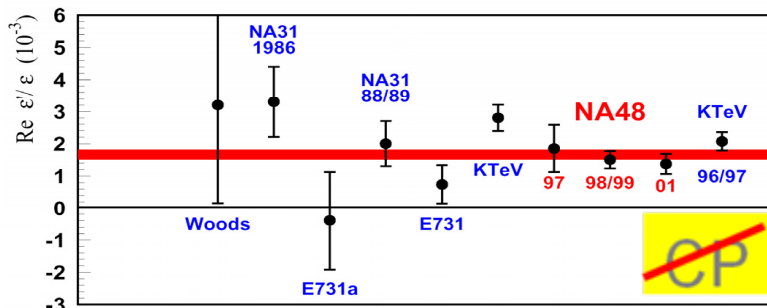
14th Lomonosov Conference on Elementary Particle Physics
Moscow, 19-25 August, 2009

1. Measurement of $\pi\pi$ scattering lengths from “cusp” effect in the decay $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$ and $Ke4$ decays $K^\pm \rightarrow \pi^+ \pi^- e^\pm \nu$
2. Precision measurements of $K^\pm \rightarrow \pi^\pm \pi^0 \gamma$
3. Branching fractions and form factors of the rare decays $K^\pm \rightarrow \pi^\pm e^+ e^-$ and $K^\pm \rightarrow \pi^\pm \mu^+ \mu^-$

*On behalf of NA48 Collaboration

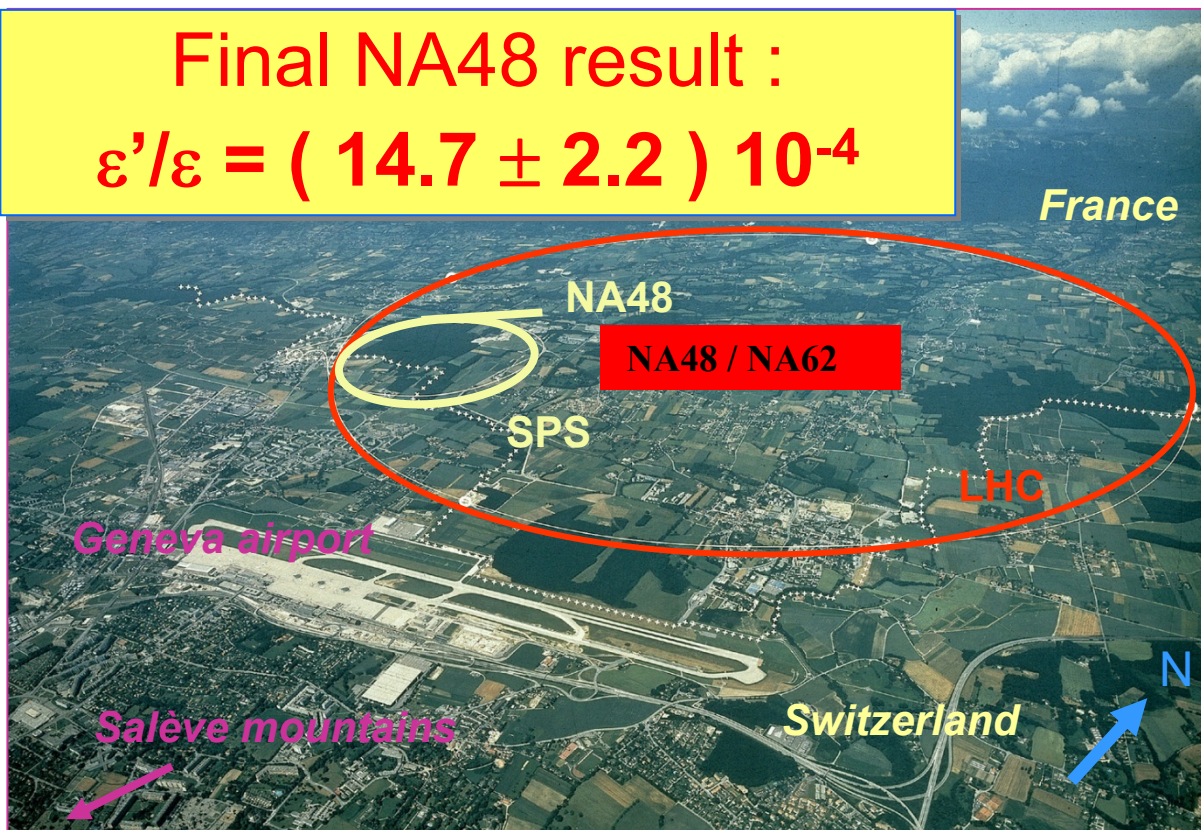
The NA48/NA62 experiment

A fixed target experiment at the CERN SPS dedicated the study of CP violation and rare decays in the kaon sector



Final NA48 result :

$$\epsilon'/\epsilon = (14.7 \pm 2.2) 10^{-4}$$



NA48

1997	ε'/ε run	K _L + K _S
1998	ε'/ε run	K _L + K _S
1999	ε'/ε run K _L + K _S	K _S High Int.
2000	K _L only	K _S High Intensity NO Spectrometer
2001	ε'/ε run K _L + K _S	K _S High Int.

NA48/1

2002	K _S High Intensity
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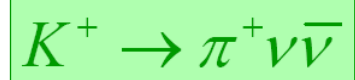
NA48/2

2003	K ⁺ High Intensity
2004	K ⁺ High Intensity

NA62

2007	K [±] _{e2} /K [±] _{μ2} run
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NA62 phase II measurement of the decay



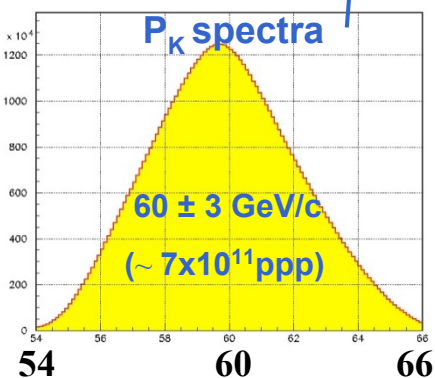
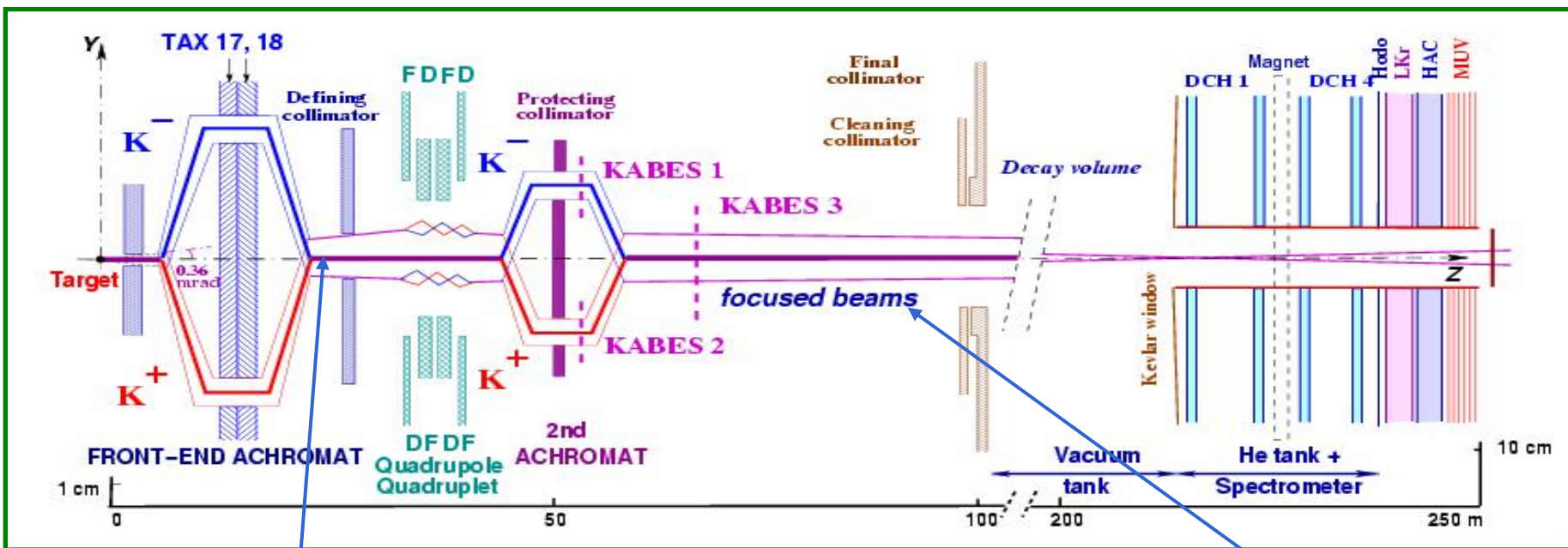
(2008-2010 R&D & construction
2011 start of data taking)

NA48/2 simultaneous K^\pm beam

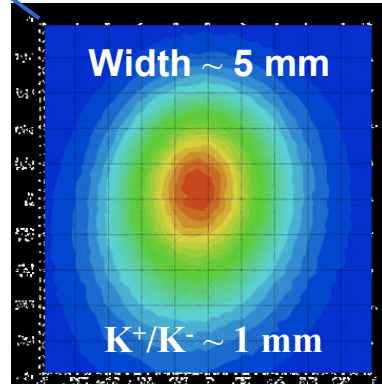


NA48-2 beams: simultaneous K^+/K^- , focused, high momentum, narrow band

designed to precisely measure $K^\pm \rightarrow \pi^+\pi^-\pi^\pm$ ($\pi^0 \pi^0 \pi^\pm$) Dalitz-plot density to search for direct CPV and **tuned for K_{e2} measurement.**



- Simultaneous, unseparated, focused beams
- Flux ratio: $K^+/K^- \sim 1.8$
- Similar acceptance for K^+ and K^- decays
- Large charge symmetrization of experimental conditions



NA48 detector



➤ Magnetic spectrometer (4 DCHs)

- 4 views : redundancy \Rightarrow high efficiency;

$$\sigma_p/p = (1.0 \oplus 0.044 p)\% \quad (p \text{ in } GeV/c)$$

➤ Hodoscope

- fast trigger;
- precise time measurement ($\sigma_t = 150 \text{ ps}$).

➤ Liquid Krypton EM calorimeter (LKr)

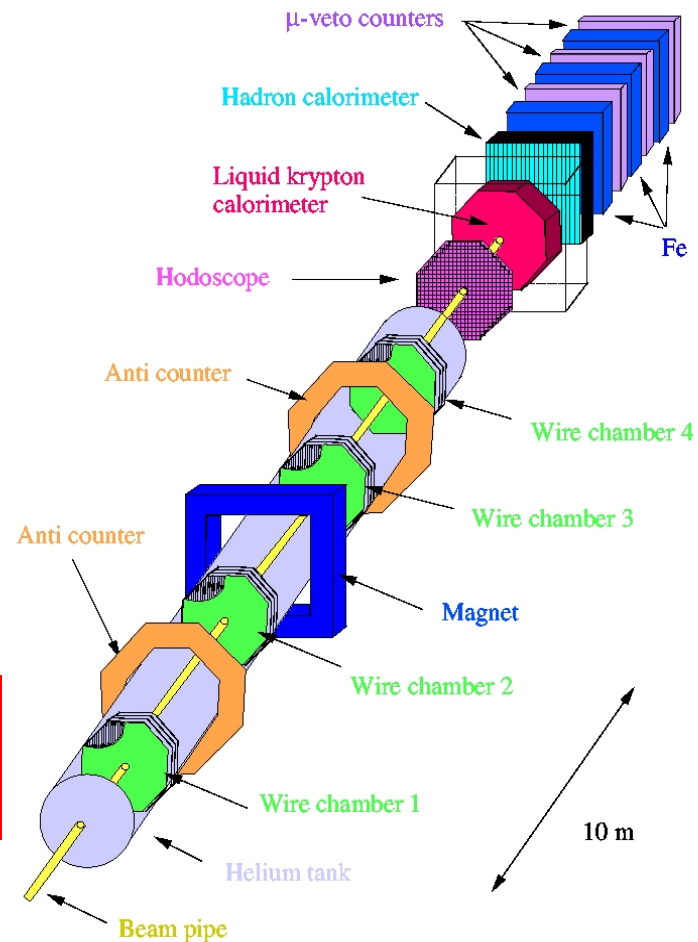
- Quasi-homogeneous ionization chamber
- 27 electromagnetic radiation lengths long active volume
- Segmented transversally 13248 cells, $2 \times 2 \text{ cm}^2$
- Energy resolution (E in GeV):

$$\sigma_E/E = (3.2/\sqrt{E} \oplus 9.0/E \oplus 0.42)\% \quad (E \text{ in } GeV)$$

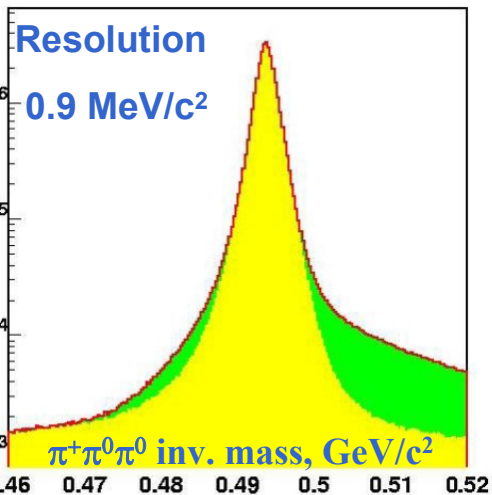
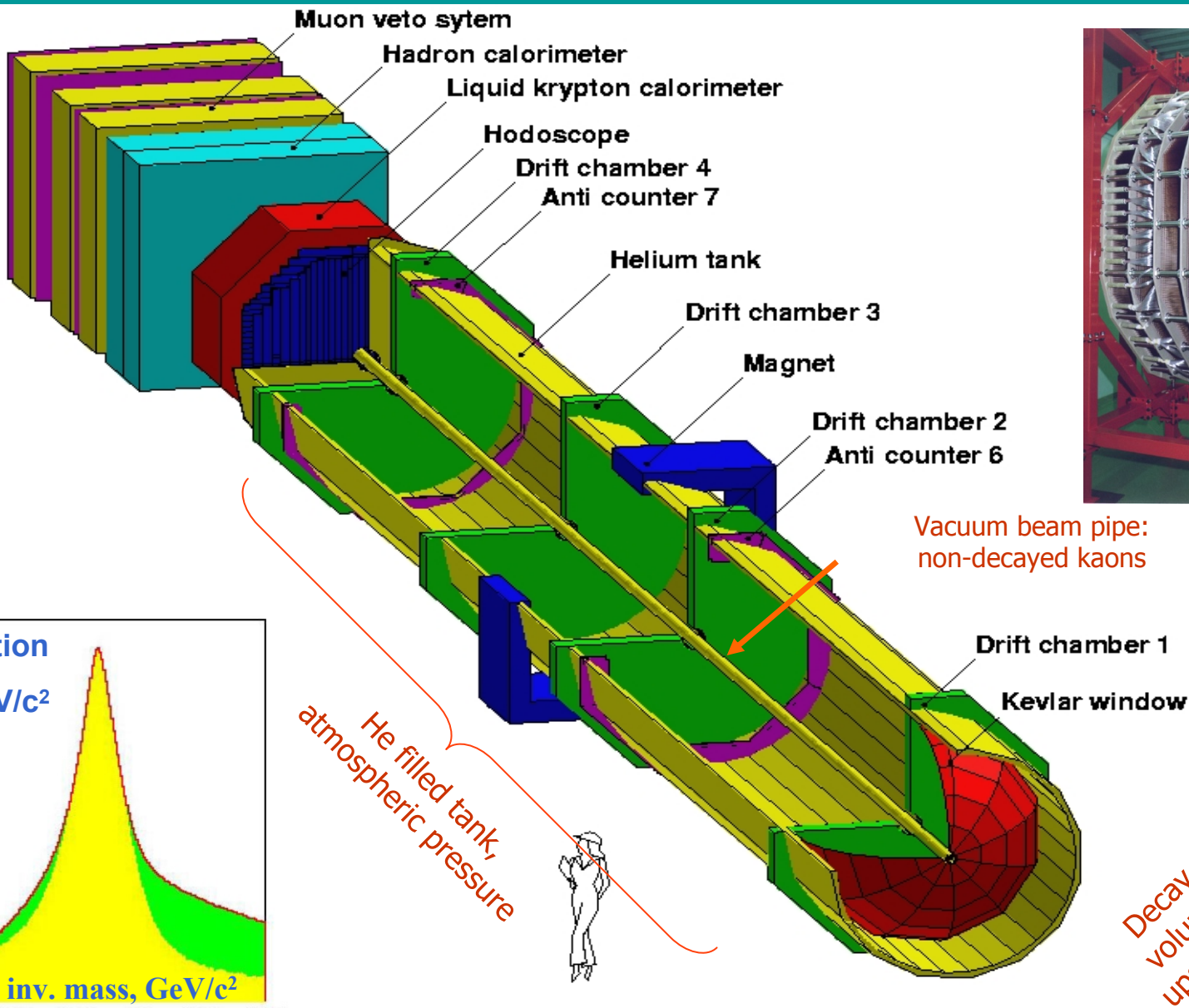
$$\sigma_x = \sigma_y = 0.42/E^{1/2} + 0.6 \text{ mm}$$

Cambridge, CERN, Chicago, Dubna, Edimburgh,
Ferrara, Firenze, Mainz, Northwestern, Perugia, Pisa,
Saclay, Siegen, Torino, Vienna

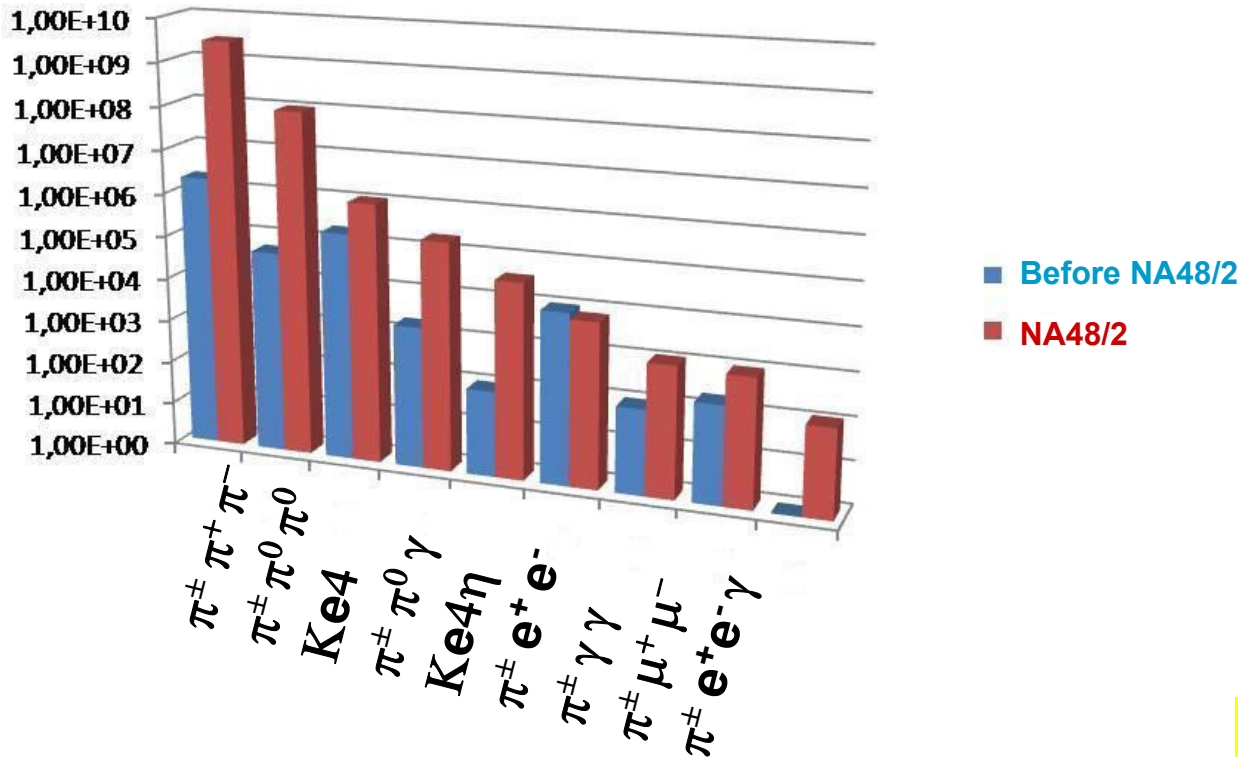
The NA48 Detector



The NA48/NA62 experiment

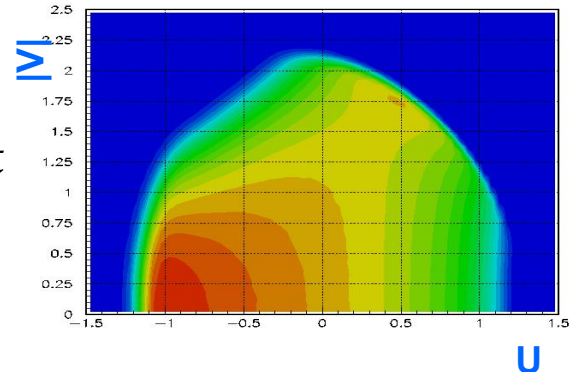


NA48/2 Data taking



NA48 Experimental hall

- Unprecedented statistics in many channels
- Two years of data taking (2003 and 2004)
- Main purpose was to measure direct CP violation in charged kaon decays, through asymmetry in Dalitz plot distribution
- New limits on CP violation in charged kaon decays



$$A_g^{\text{ch}} = (-1.5 \pm 2.1) \times 10^{-4}$$

$$A_g^0 = (1.8 \pm 1.8) \times 10^{-4}$$



$\pi\pi$ scattering lengths in K_{e4} and $K3\pi$ decays

QCD test with Kaons



The important free parameter of Chiral Perturbation Theory is the quark condensate $\langle qq \rangle$, it determines the relative size of mass and momentum terms in the power expansion.

a_0 and a_2 are the **S-wave** $\pi\pi$ scattering lengths in Isospin states **I=0** and **I=2**. They enter in all $\pi\pi$ scattering amplitudes.

The relation between $\langle qq \rangle$ and the scattering lengths a_0 and a_2 is known from this theory with high precision.

The experimental measurement of a_0 and a_2 provides important constraints for ChPT parameters



Kaon decays \rightarrow ideal laboratory to study the low energy (below 1 GeV) regime of hadronic physics

Two different approaches to measure a_0 and a_2

Hadronic decay mode $K3\pi$

- large BR's :
 $K^\pm \rightarrow \pi^0 \pi^0 \pi^\pm = 1.7\%$
- 60×10^6 events analyzed
- results on partial sample
 \rightarrow Phys. Lett. B633 (2006)
- full statistics paper submitted

Semileptonic decay mode $Ke4$

- small BR's :
 $K^\pm \rightarrow \pi^+ \pi^- e^\pm \nu = 4.1 \times 10^{-5}$
- 1.1×10^6 events analyzed
- results on partial sample
 \rightarrow EPJ C54 (2008)



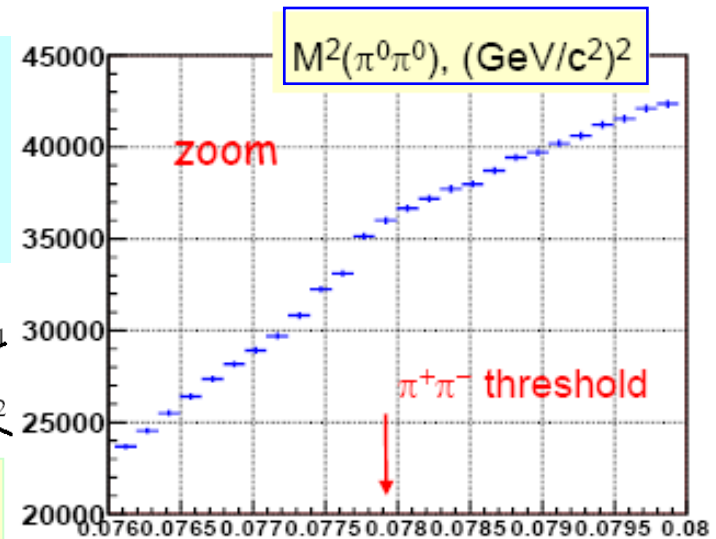
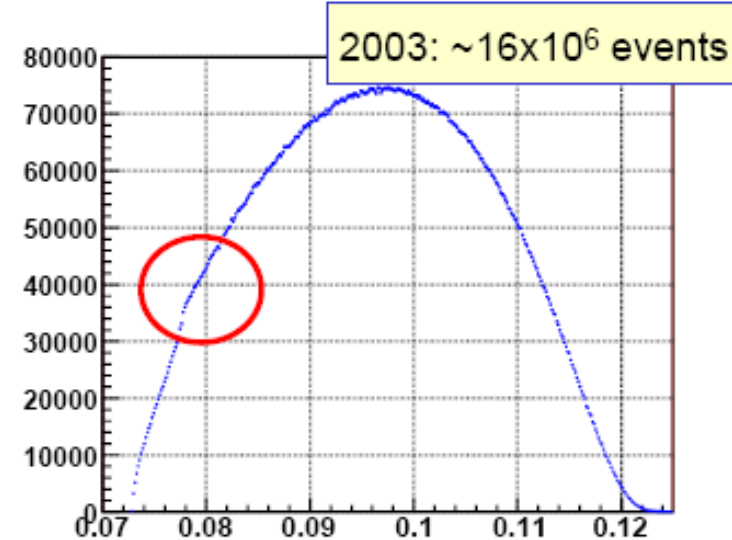
Cusp effect in $K^\pm \rightarrow \pi^0\pi^0\pi^\pm$

Thanks to:

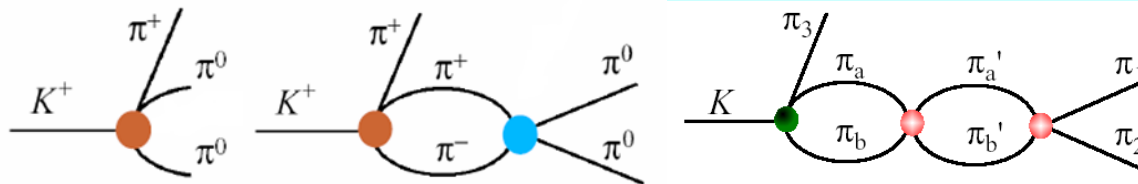
- ✓ Very high **statistics**,
- ✓ Very good calorimeter **resolution**
- ✓ Proper M_{00} **reconstruction strategy**

The $\pi^0\pi^0$ invariant mass distribution shows a **cusp-like anomaly** in the

$$M_{00}^2 = 4m_{\pi^\pm}^2 \quad \text{region}$$



interpreted as due to the **final state charge exchange scattering process**
 $\pi^+\pi^- \rightarrow \pi^0\pi^0$ in $K^\pm \rightarrow \pi^\pm\pi^+\pi^-$ decays



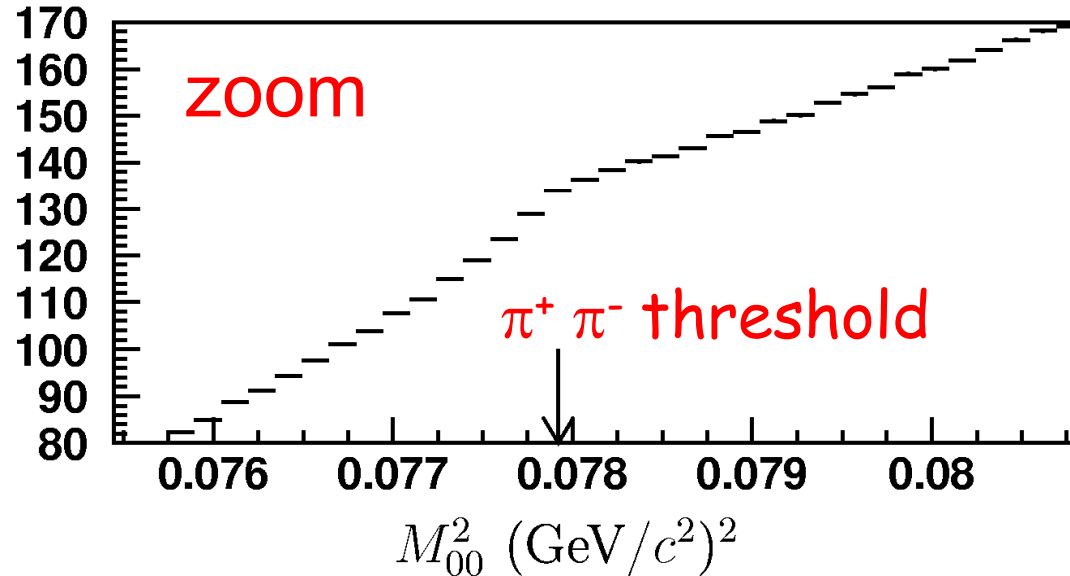
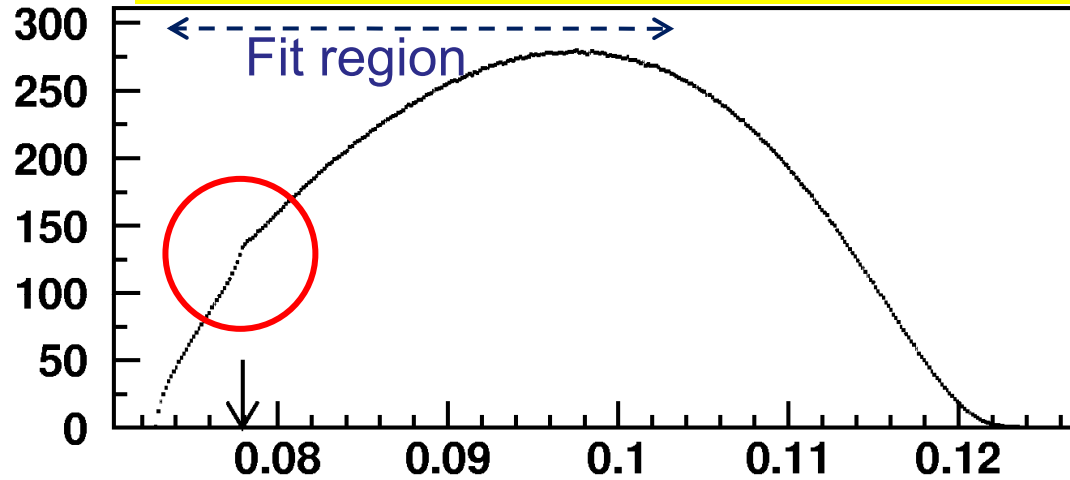
Statistic increased from 16M (2003)
(Batley et al., Phys. Lett. B 633 (2006) 173)
to 60 M (adding 2004) (paper submitted to EPJ)



Cusp effect in $K^\pm \rightarrow \pi^0\pi^0\pi^\pm$

$\times 10^3$

2003 & 2004 : ~ 60.31 millions events



Fit region is chosen to reach a minimum total error (systematic contribution grows with upper M^2_{00}).

Use 226 bins (instead of 176 as was in our first cusp paper (2006)).

Cusp effect - results

Two approaches to the fitting procedure:

Cabibbo-Isidori → rescattering model
JHEP 0503(2005)

Bern-Bonn → effective field theory
CGKR PLB 638(2006)
BFGKR NPB 806(2009)

a_2 free:

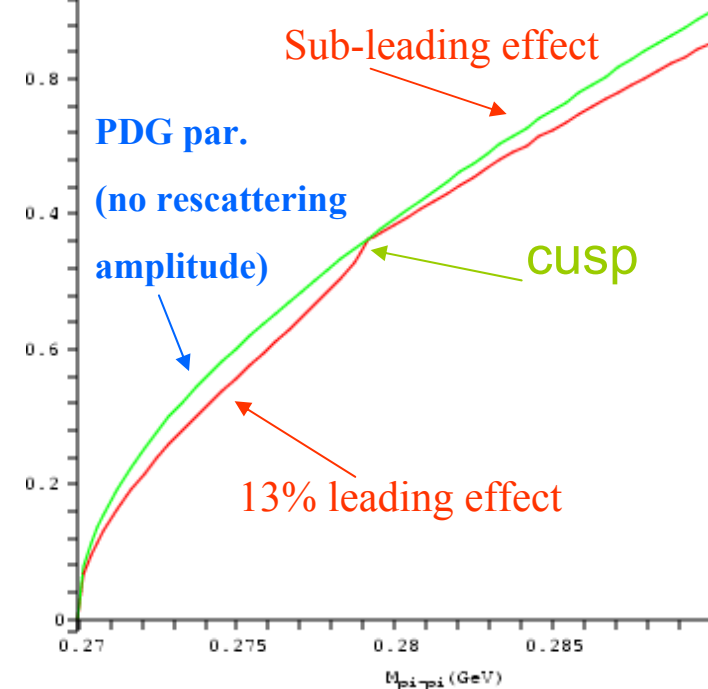
CI $a_0 - a_2 = 0.248 \pm 0.005_{\text{stat}} \pm 0.002_{\text{syst}} \pm 0.001_{\text{ext}} \pm 0.009_{\text{theor}}$
 $a_2 = -0.009 \pm 0.009_{\text{stat}} \pm 0.007_{\text{syst}} \pm 0.001_{\text{ext}} \pm 0.015_{\text{theor}}$

BB $a_0 - a_2 = 0.257 \pm 0.005_{\text{stat}} \pm 0.002_{\text{syst}} \pm 0.001_{\text{ext}} \pm 0.009_{\text{theor}}$
 $a_2 = -0.024 \pm 0.013_{\text{stat}} \pm 0.009_{\text{syst}} \pm 0.002_{\text{ext}} \pm 0.015_{\text{theor}}$

Using Chiral Perturbation Theory Constraint:

CI $a_0 - a_2 = 0.265 \pm 0.002_{\text{stat}} \pm 0.001_{\text{syst}} \pm 0.002_{\text{ext}} \pm 0.005_{\text{theor}}$
 $(a_0 = 0.2203, a_2 = -0.0443)$

BB $a_0 - a_2 = 0.263 \pm 0.002_{\text{stat}} \pm 0.001_{\text{syst}} \pm 0.002_{\text{ext}} \pm 0.005_{\text{theor}}$
 $(a_0 = 0.2186, a_2 = -0.0447)$

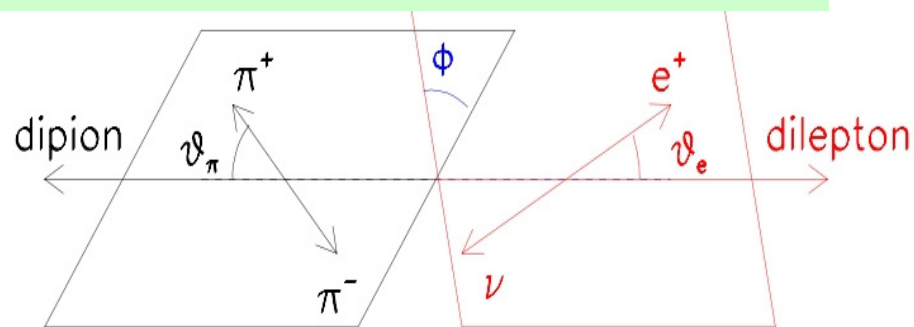


Ke4 - analysis



$K^+ \rightarrow \pi^+ \pi^- e^+ \nu$ decay used to measure

- Form Factors of the hadronic current (F, G, H)
- s and p-wave $\pi\pi$ scattering phase difference $\delta = \delta_s - \delta_p$
- $\pi\pi$ s-wave scattering lengths a_0 and a_2



The measurement exploits

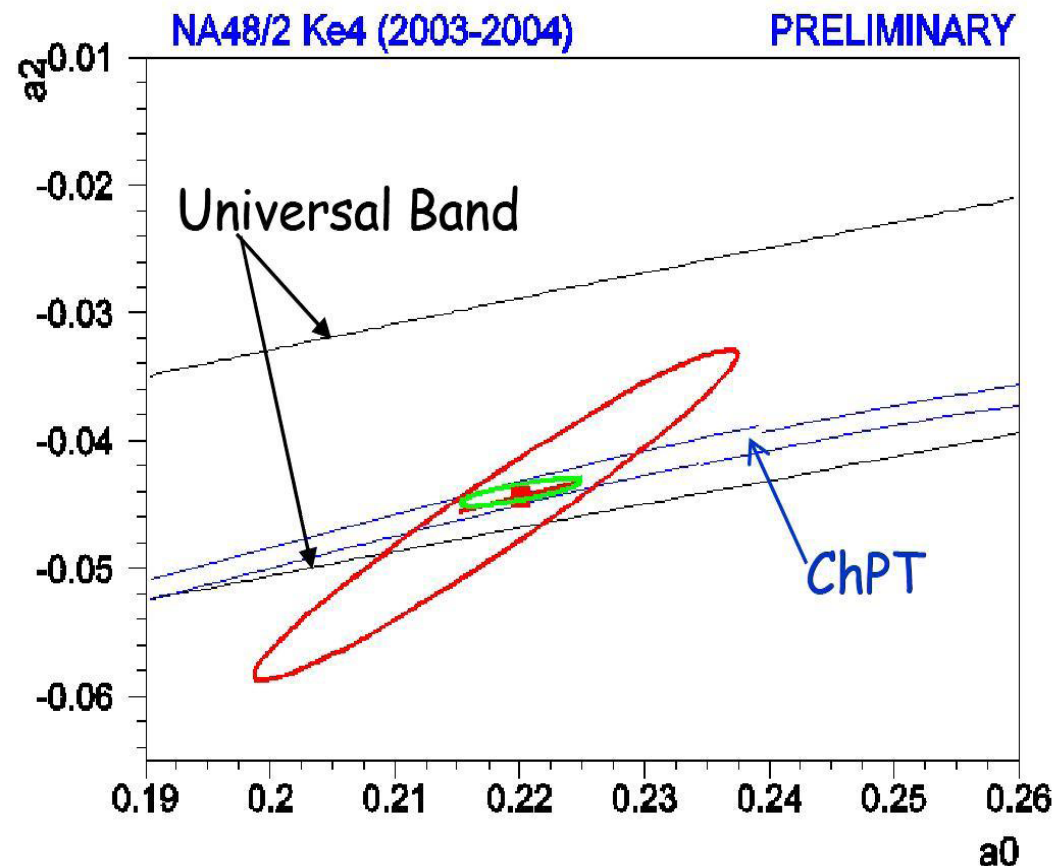
- the asymmetry of the dilepton system wrt the dipion system
- dispersion relation based on general properties like analyticity, unitarity and crossing symmetry (Roy equations)
- analytical properties of $\pi\pi$ scattering amplitudes and Roy equations allow to establish a **relation between the phase shift δ and the scattering lengths a_0 and a_2**

Measurement performed using minimization and fitting procedures

Ke4 - a_0 and a_2 results

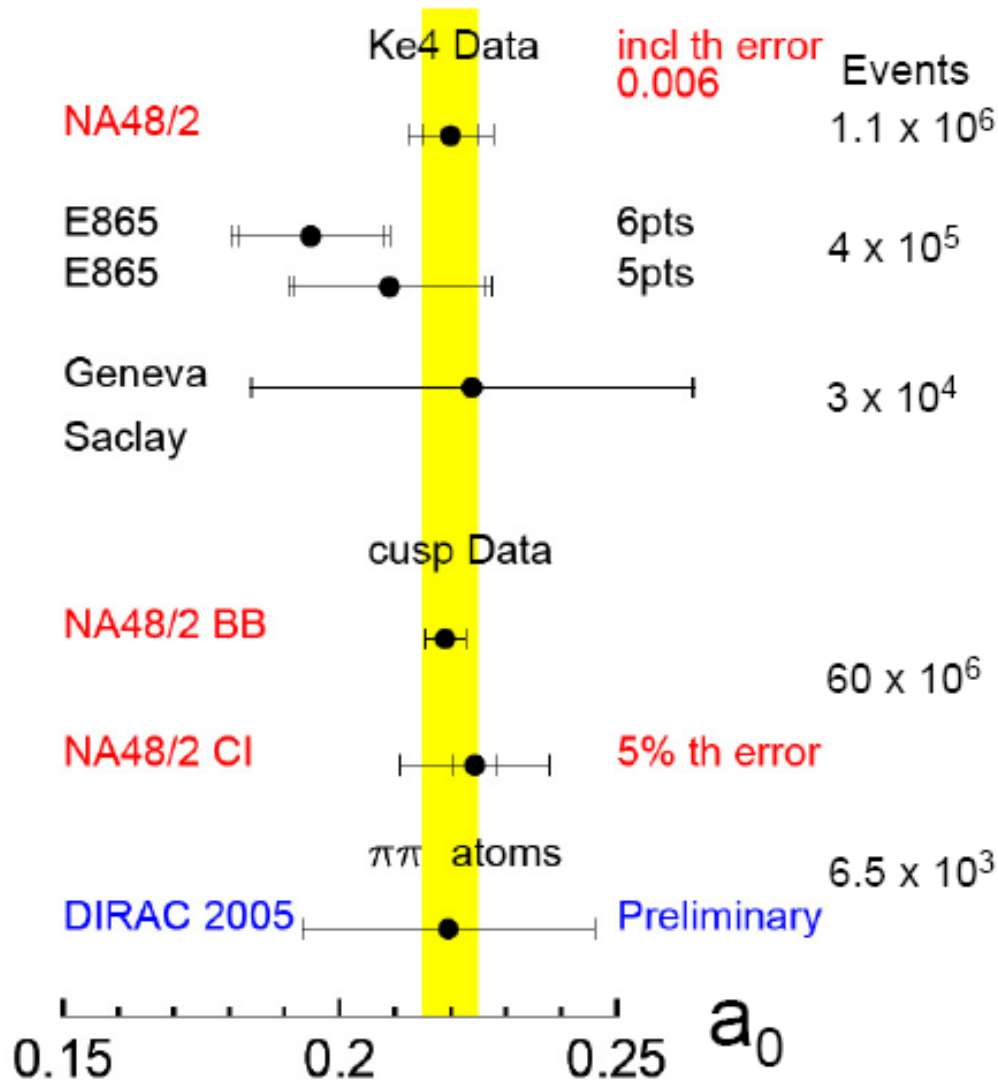


1p fit (ChPT)	
a_0	$0.2206 \pm 0.0049_{\text{stat}}$ $\pm 0.0018_{\text{syst}}$ $\pm 0.0064_{\text{theor}}$
2p fit	
a_0	$0.2220 \pm 0.0128_{\text{stat}}$ $\pm 0.0050_{\text{syst}}$ $\pm 0.0037_{\text{theor}}$
a_2	$-0.0432 \pm 0.0086_{\text{stat}}$ $\pm 0.0034_{\text{syst}}$ $\pm 0.0028_{\text{theor}}$



Precise ChPT prediction, CGL NPB 603(2001), PRL86(2001)
 $a_0 = 0.220 \pm 0.005$ and $a_2 = -0.0444 \pm 0.0008$
or $(a_0 - a_2) = 0.265 \pm 0.005$

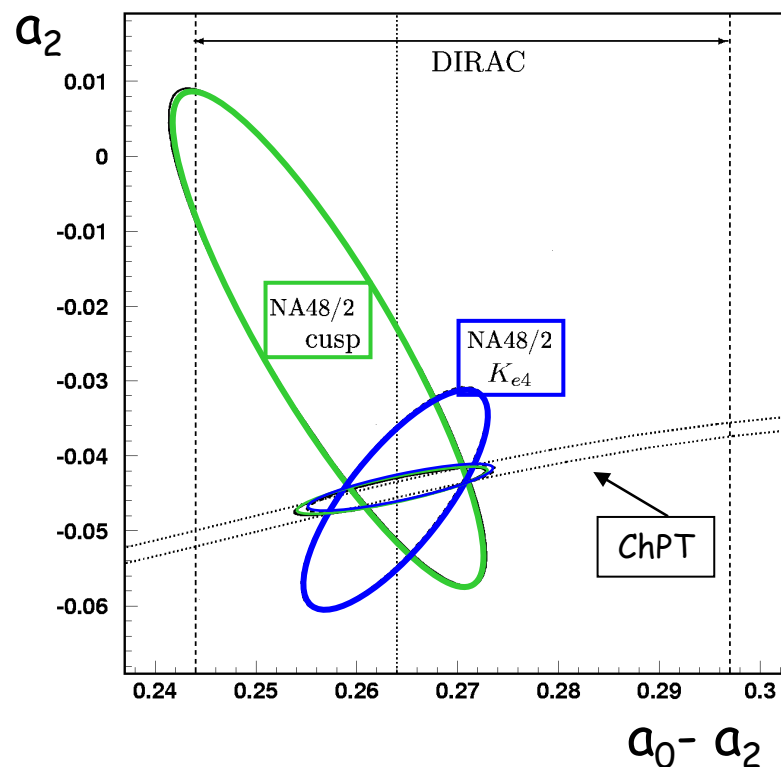
Ke4 and Cusp a_0 results



Cusp and Ke4 - scattering lengths results



- ✓ Two statistically independent measurements by NA48/2:
60 M $K3\pi$; 1.13 M Ke4
- ✓ Different systematics:
Cusp: calorimeter and trigger
Ke4: electron misID and background
- ✓ Different theoretical inputs:
Cusp: rescattering in final state and ChPT expansion
Ke4: Roy equation and isospin breaking connection

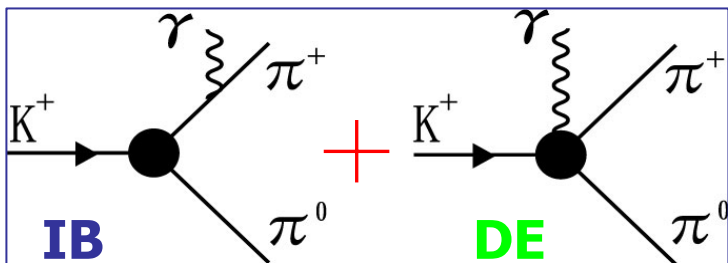


- ✓ Large overlap in the $(a_0 - a_2, a_2)$ plane
- ✓ Impressive agreement with ChPT predictions
- ✓ Also shown DIRAC results: $|a_0 - a_2|$ extracted from pionium lifetime PLB619(2005)
- ✓ Cusp effect in $K_L \rightarrow \pi^0 \pi^0 \pi^0$ KTeV ($68 \cdot 10^6$) [PRD 78, 032009 (2008)]
NA48 ($100 \cdot 10^6$) work in progress



$K^{\pm} \rightarrow \pi^{\pm} \pi^0 \gamma$ rare decay

Theoretical framework and motivation



Differential rate

$$\frac{\partial \Gamma^\pm}{\partial W} = \underbrace{\frac{\partial \Gamma_{IB}^\pm}{\partial W}}_{\text{IB}} \left[1 + \underbrace{2 \cos(\pm\phi + \delta_1^1 - \delta_0^2) m_\pi^2 m_K^2}_{\text{INT}} |X_E|^2 W^2 + \underbrace{m_\pi^4 m_K^4 (|X_E|^2 + |X_M|^2)}_{\text{DE}} W^4 \right]$$

Lorentz invariant $W^2 = \frac{(P_K^* \cdot P_\gamma^*)(P_\pi^* \cdot P_\gamma^*)}{(m_K m_\pi)^2}$

DE can occur via electric and magnetic dipole transitions X_E and X_M

Inner Bremsstrahlung (IB)

: BR = $(2.75 \pm 0.15) \cdot 10^{-4}$ PDG ($55 < T_\pi^* < 90$ MeV)

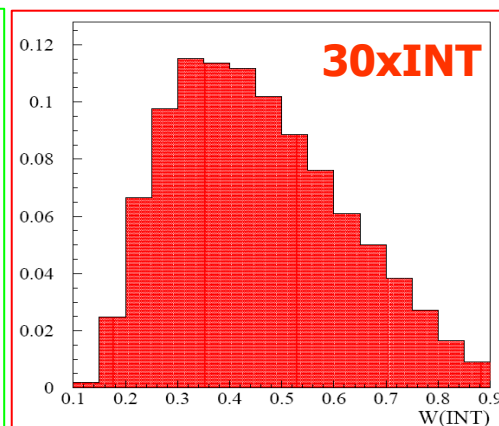
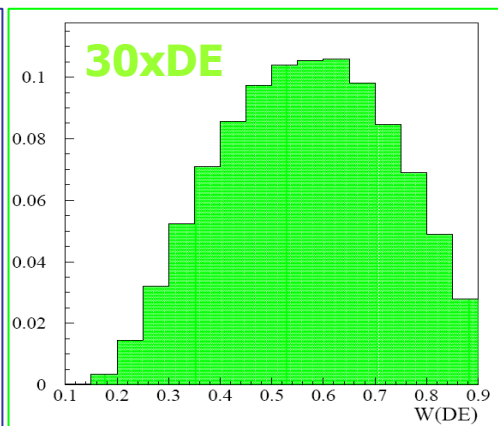
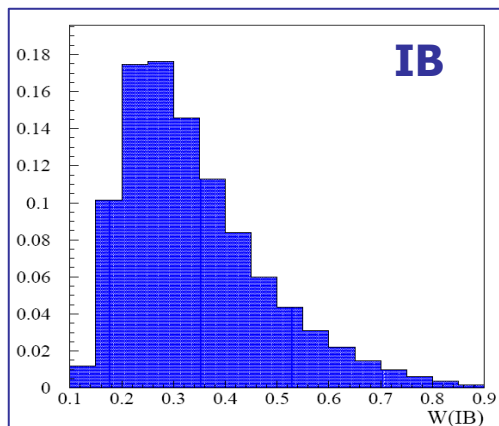
Direct Emission (DE)

: BR = $(4.3 \pm 0.7) \cdot 10^{-6}$ PDG ($55 < T_\pi^* < 90$ MeV)

Interference (INT)

: not yet measured

Very different distributions!



Event reconstruction and signal region

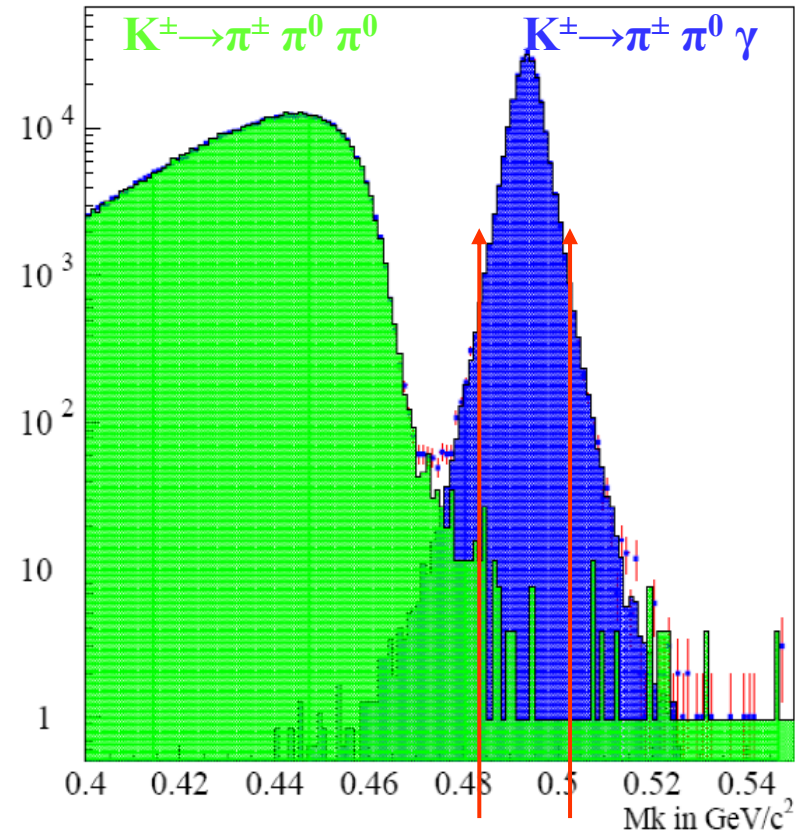


● NA48/2 measurement of $K^\pm \rightarrow \pi^\pm \pi^0 \gamma$ decay

- both K^+ and K^- present in the beam:
possibility to study CP violating effects
- Enlarged T_π^* region in the low energy part
($0 < T_\pi^* < 80$ MeV) wrt previous experiments
- Background contribution $< 1\%$ wrt DE,
mainly $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$
- W resolution better than 1×10^{-2}
- Order % γ mistagging prob. for IB, DE and INT
- Fit performed with both polynomial and likelihood techniques

● High statistics:

- More than 1 M reconstructed events
(the full number is used for the CPV measurements)
- After a cut on W [0.2, 0.9] and on E_γ (> 5 GeV), still 600 k events left in the region $M_K \pm 10$ MeV for the measurement of DE and INT fraction



Fitting techniques and fit results



- Extended Maximum Likelihood Fit (*main method*)

- An algorithm assigns weights to MC W distributions of the 3 components to reproduce data

$$Data(i) = (1 - \alpha - \beta) \cdot IB(i) + \alpha \cdot DE(i) + \beta \cdot INT(i)$$

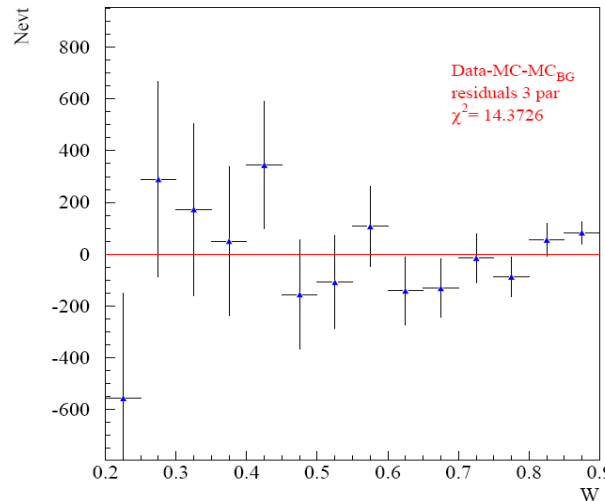
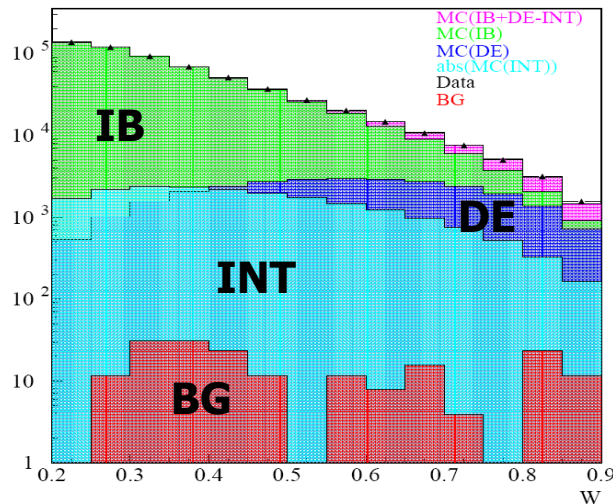
- This algorithm relies on the very different W distributions

- Polynomial Fit (*used as cross-check*)

- The ratio $W(Data)/W(IBMC)$ is fitted with polynomial function: $F = c \cdot (1 + aW^2 + bW^4)$

Systematics	DE x 10 ⁻²	INT x 10 ⁻²
Acceptance	<0.10	<0.15
L1 trigger	0.01	0.03
L2 trigger	--	0.30
Energy scale	0.09	0.21
Total	0.14	0.39

INT has never been observed before!



Final result (2003+2004):

$$\text{Frac}(DE)_{T^*\pi(0-80)\text{MeV}} = \%DE / \%IB = (3.32 \pm 0.15_{\text{stat}} \pm 0.14_{\text{sys}}) \cdot 10^{-2}$$

$$\text{Frac}(INT)_{T^*\pi(0-80)\text{MeV}} = \%INT / \%IB = (-2.35 \pm 0.35_{\text{stat}} \pm 0.39_{\text{sys}}) \cdot 10^{-2}$$

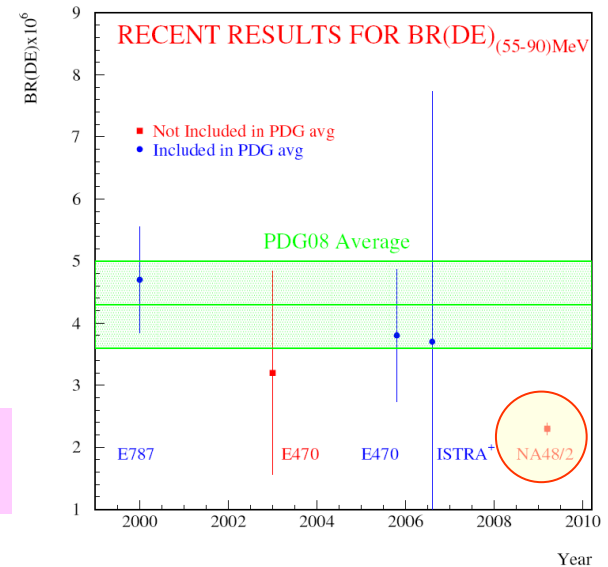
Comparison with previous experiments



The BR(DE) assuming INT=0 ($T_\pi^* = 55-90$) MeV polynomial fit technique

- BR(DE) $_{T^*\pi(55-90)\text{MeV}} = (2.32 \pm 0.05_{\text{stat}} \pm 0.077_{\text{sys}}) \cdot 10^{-6}$
- PDG08_{avg} = $(4.3 \pm 0.7) \cdot 10^{-6}$
- **Bad χ^2 probability of the polynomial fit: indicates that INT=0 is a wrong assumption**

$K^\pm \rightarrow \pi^\pm \pi^0 \gamma$ – first extraction of X_E X_M



Under the following approximations:

$\phi = 0$ and $\cos(\delta_1 - \delta_0) = \cos(6.5^\circ) \sim 1$

X_E and X_M can be extracted using the formulae:

Magnetic and electric components

$$X_E = (-24 \pm 4_{\text{stat}} \pm 4_{\text{sys}}) \text{ GeV}^{-4}$$

$$X_M = (254 \pm 11_{\text{stat}} \pm 11_{\text{sys}}) \text{ GeV}^{-4}$$

$$X_E = \frac{\text{Frac}(INT)}{2 \cdot (0.105 \cdot m_K^2 m_\pi^2)}$$

$$X_M = \sqrt{\frac{\text{Frac}(DE) - m_K^4 m_\pi^4 |X_E|^2 \cdot 2.27 \cdot 10^{-2}}{2.27 \cdot 10^{-2} \cdot m_K^4 m_\pi^4}}$$

WZW reducible anomaly prediction for $X_M \sim 260 \text{ GeV}^{-4}$

$K^\pm \rightarrow \pi^\pm \pi^0 \gamma$ – CPV parameters measurements:
asymmetry and ϕ angle: compatible with 0



$$K^{\pm} \longrightarrow \pi^{\pm} \gamma^{*} \longrightarrow \pi^{\pm} l^{+} l^{-}$$

rare decays

Theoretical framework and motivation

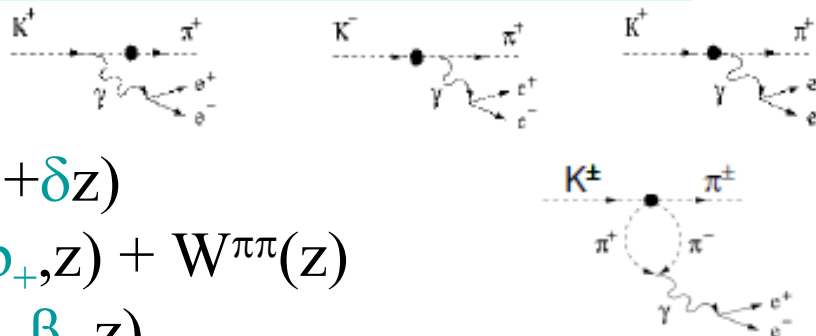


- **NA48/2 measurement of $K^\pm \rightarrow \pi^\pm \gamma^* \rightarrow \pi^\pm l^+l^-$ decay**

$$d\Gamma_{\pi ee}/dz \sim \rho(z) \cdot |W(z)|^2$$

$z=(M_{ee}/M_K)^2$, $\rho(z)$ phase space factor

- suppressed FCNC processes
- one-photon exchange
- useful test for ChPT



- (1) polynomial: $W(z) = G_F M_K^2 \cdot f_0 \cdot (1 + \delta z)$
- (2) ChPT $O(p^6)$: $W(z) = G_F M_K^2 \cdot (a_+, b_+, z) + W^{\pi\pi}(z)$
- (3) ChPT, large- N_c QCD: $W(z) = W(w, \beta, z)$
- (4) Mesonic ChPT: $W(z) = W(M_a, M_\rho, z)$

- (2) D'Ambrosio et al. JHEP 8 (1998) 4
- (3) S. Friot et al. PLB 595 (2004) 301
- (4) Dubnickova et al. hep-ph/0611175

(f_0, δ) or (a_+, b_+) or (w, β) or (M_a, M_ρ) determine a model-dependent **BR**

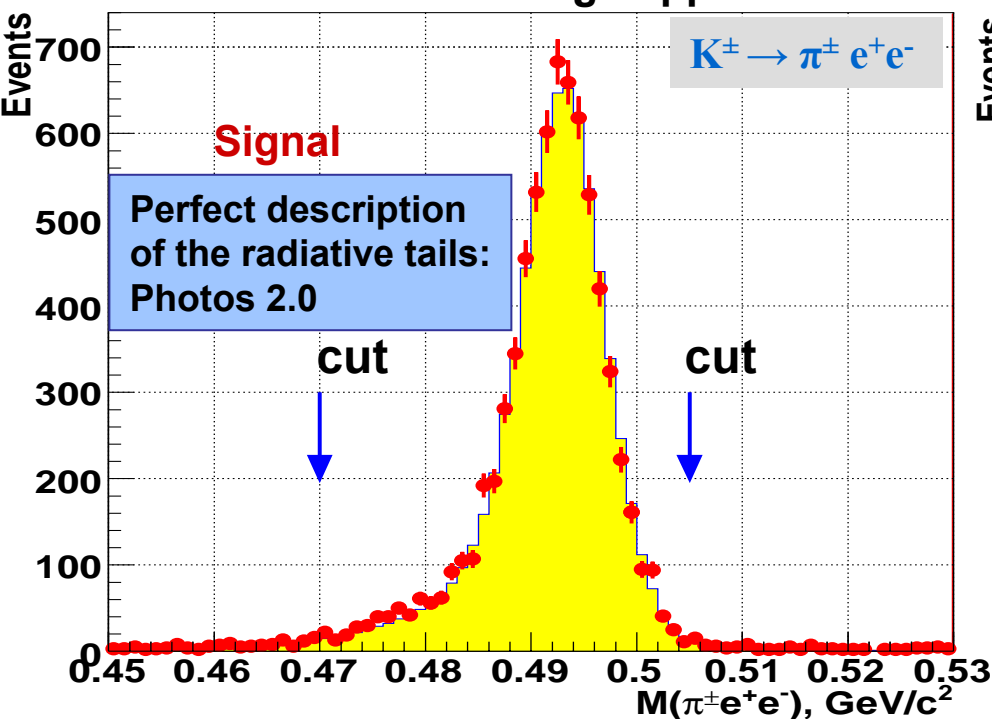
- Parameters of models and BR in full kinematical range
- Model-independent **BR ($z > 0.08$)** in visible kinematical range

$K^\pm \rightarrow \pi^\pm e^+ e^-$ - Signal and normalisation sample



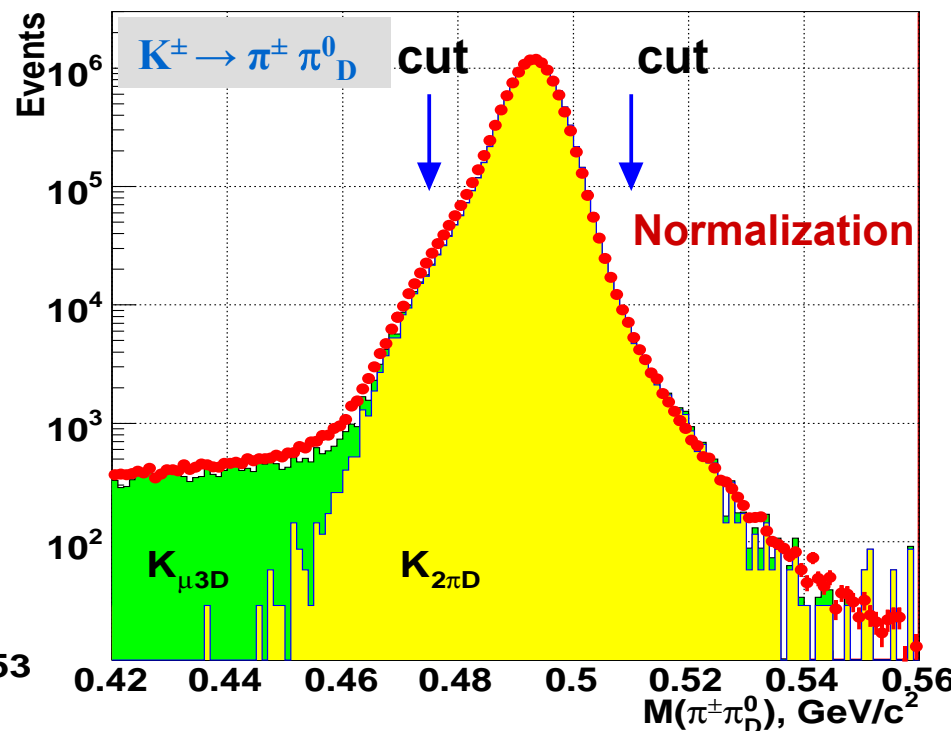
Selections of both channels based on very similar conditions:
systematics (trigger, PID) in the BR ratio cancel partially

• $M_{ee} > 140$ MeV – cut for bg suppression



7253 candidates
BG: 71 events estimated
with data **BG/SIG. ~ 1.0%**

• Additional γ in the normalisation channel



12.12 M candidates
BG/Signal ~ 0.15%
BG subtracted with MC

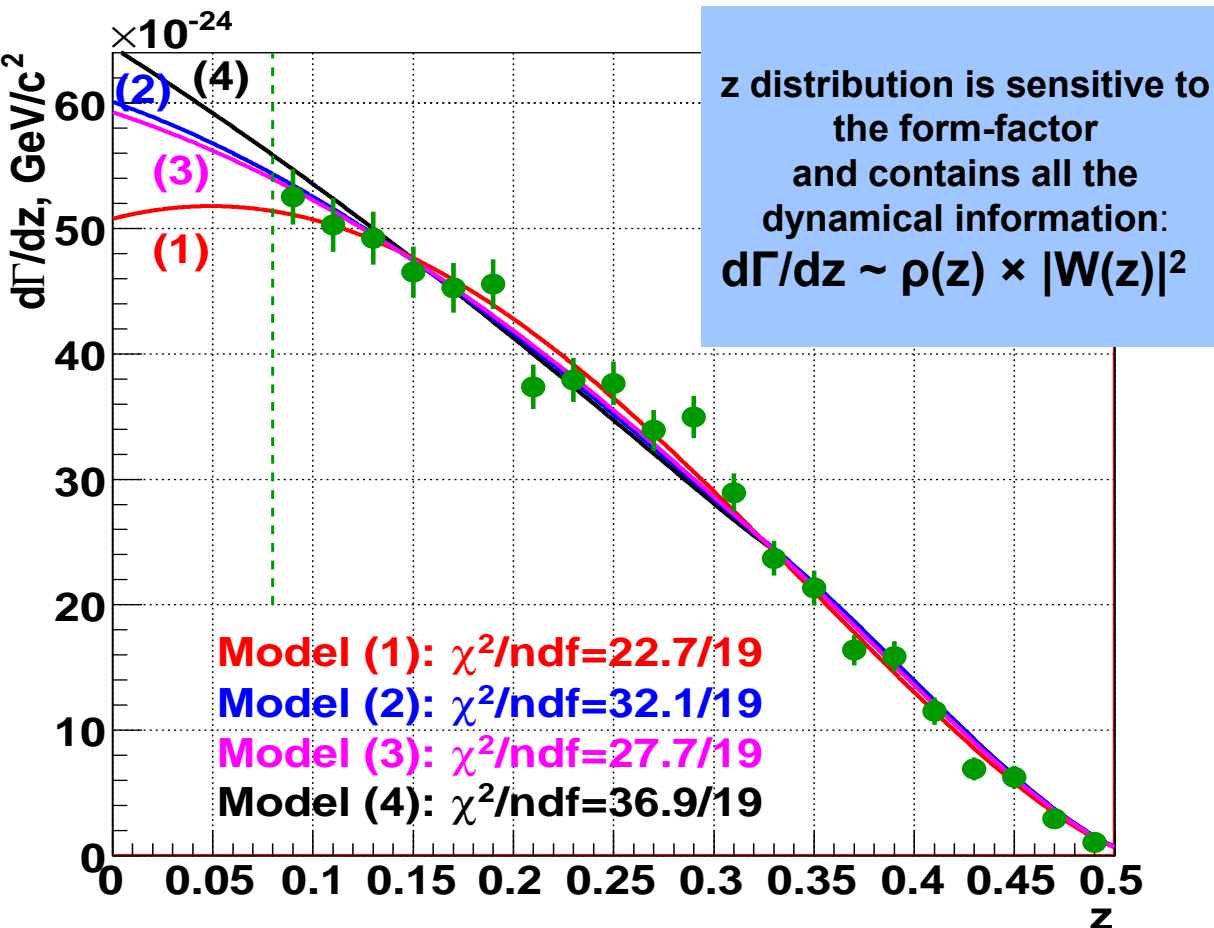
Kaon decay flux (2003+2004): $\Phi_K = 1.70 \times 10^{11}$ with **Flavianet'08 $K^\pm \rightarrow \pi^\pm \pi^0$ BR**

$K^\pm \rightarrow \pi^\pm e^+ e^-$ - form factor measurement



GOALS

- Model-independent BR integrating $d\Gamma/dz$ in the observable z region
- Model dependent BRs using fit parameters.
- All models agree reasonably well with data



Fit results

$$\delta = 2.32 \pm 0.18_{\text{stat+syst}}$$

$$|f_0| = 0.531 \pm 0.016_{\text{stat+syst}}$$

$$a_+ = -0.578 \pm 0.016_{\text{stat+syst}}$$

$$b_+ = -0.779 \pm 0.066_{\text{stat+syst}}$$

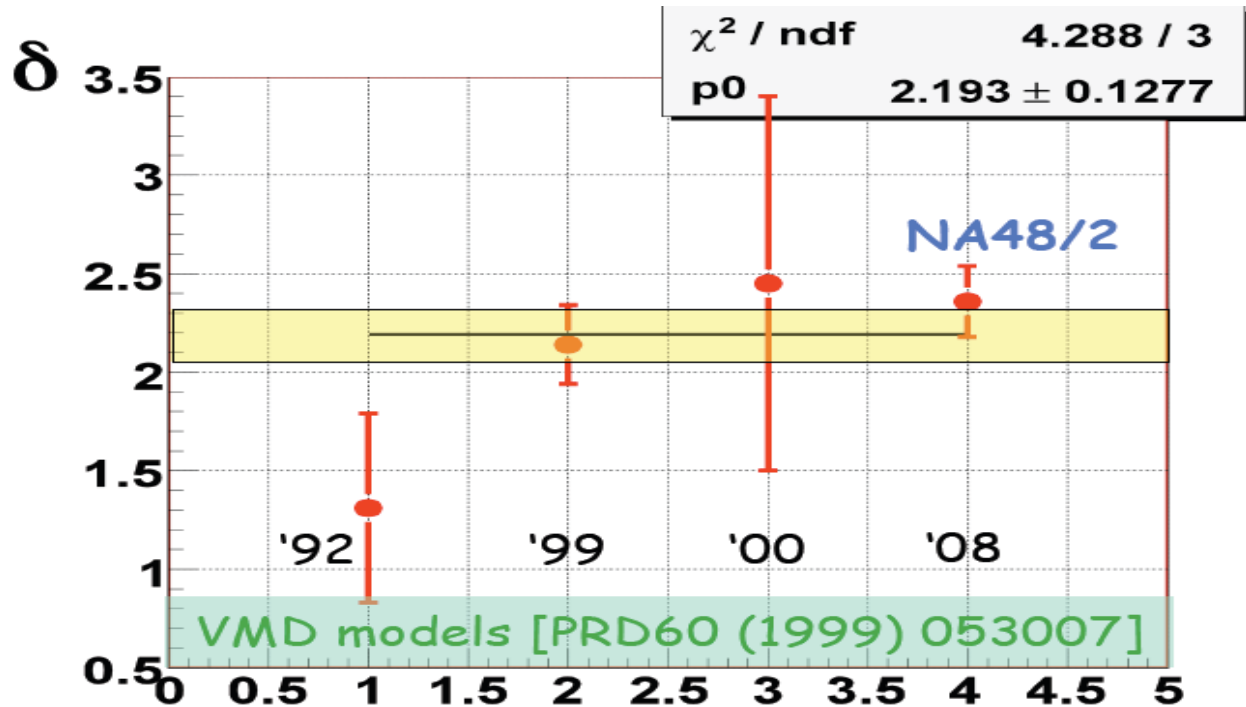
$$w = 0.057 \pm 0.007_{\text{stat+syst}}$$

$$\beta = 3.45 \pm 0.30_{\text{stat+syst}}$$

$$M_a = 0.974 \pm 0.035_{\text{stat+syst}} \text{ GeV}$$

$$M_\rho = 0.716 \pm 0.014_{\text{stat+syst}} \text{ GeV}$$

$K^\pm \rightarrow \pi^\pm e^+ e^-$ - Results



Form Factor δ	Process δ	value
Alliegro et al	$K^+ \rightarrow \pi^+ e^+ e^-$	1.31 ± 0.48
Appel et al.[E865]	$K^+ \rightarrow \pi^+ e^+ e^-$	2.14 ± 0.20
Ma et al.[E865]	$K^+ \rightarrow \pi^+ \mu^+ \mu^-$	$2.45^{+1.30}_{-0.95}$
NA48/2	$K^\pm \rightarrow \pi^\pm e^+ e^-$	2.32 ± 0.18

$K^\pm \rightarrow \pi^\pm e^+ e^-$ - Results



$$BR_{mi} \times 10^7 (M_{ee} > 140 \text{ MeV}/c^2) = 2.28 \pm 0.03_{\text{stat}} \pm 0.04_{\text{syst}} \pm 0.06_{\text{ext}} = 2.28 \pm 0.08$$

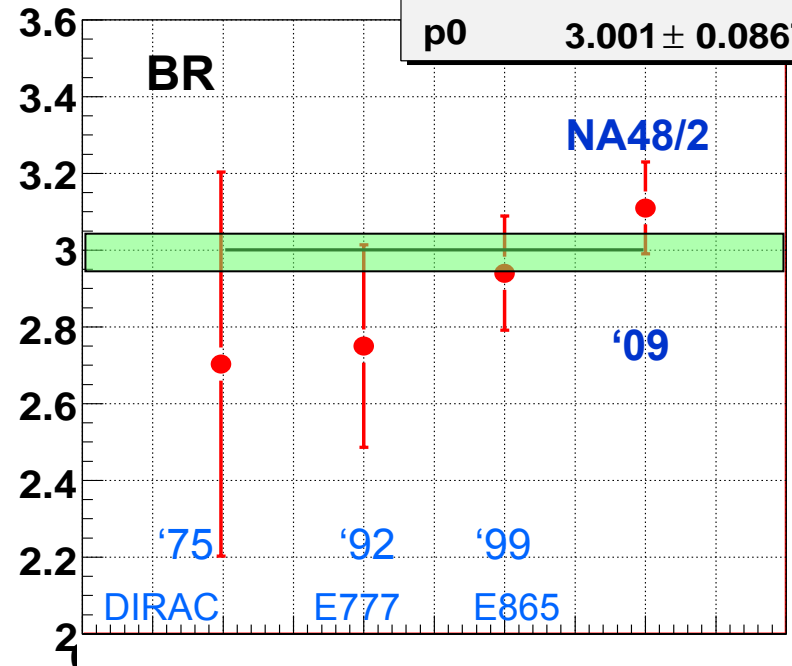
Combined result of the 4 models

$$BR = (3.11 \pm 0.04_{\text{stat}} \pm 0.05_{\text{syst}} \pm 0.08_{\text{ext}} \pm 0.07_{\text{model}}) \times 10^{-7} = (3.11 \pm 0.12) \times 10^{-7}$$

CP violating asymmetry (first measurement! correlated K^+/K^- uncertainties excluded):

$$\Delta(K^\pm_{\pi ee}) = (BR^+ - BR^-) / (BR^+ + BR^-) = (-2.2 \pm 1.5_{\text{stat}} \pm 0.6_{\text{syst}})\%$$

χ^2 / ndf 2.259 / 3
 p0 3.001 ± 0.08676



Measurement	events	BR × 10 ⁷
Bloch et al., PL 56 (1975) B201	(41)	2.70 ± 0.50
Alliegro et al. [E777], PRL 68 (1992) 278	(500)	2.75 ± 0.26
Appel et al. [E865], PRL 83 (1999) 4482	(10000)	2.94 ± 0.15
NA48/2 final (2009)	(7253)	3.11 ± 0.12

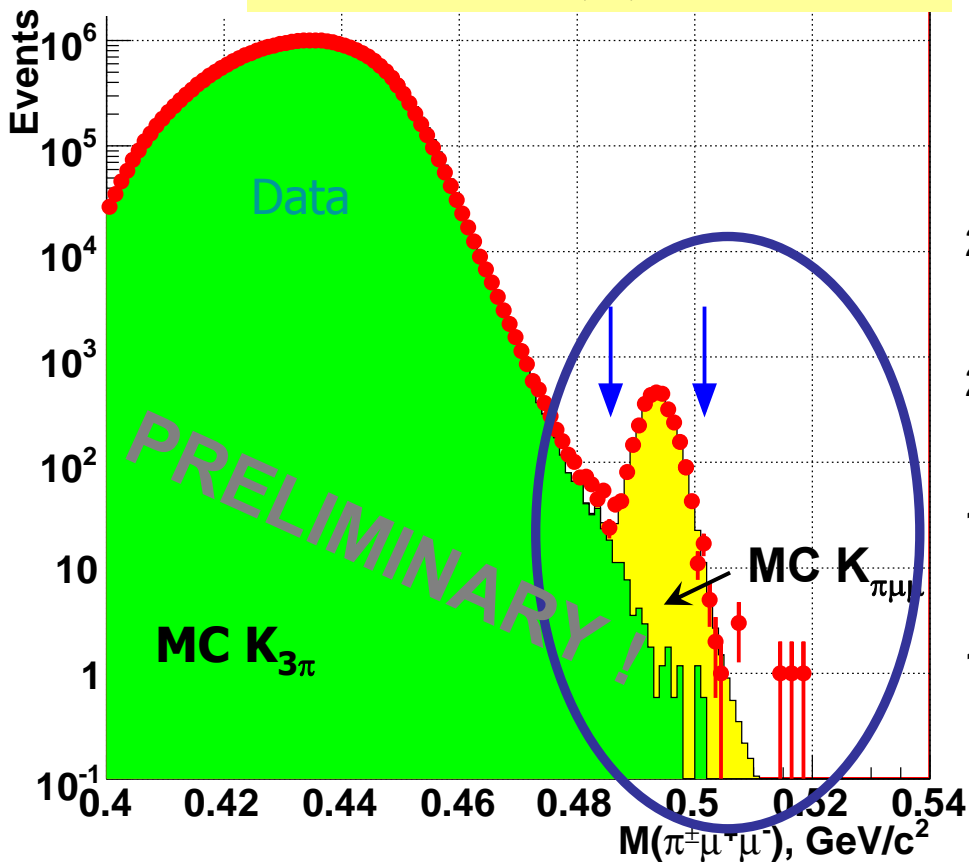
- Form factor measurements for Model 1, 2 and 3* in agreement with previous measurements
- Model 4 – never tested before
- J. Prades, e-Print: arXiv:0707.1789 [hep-ph], predicts (up to its sign) $a_+ = -(0.6^{+0.6}_{-0.23})$, in agreement with our result

*fit done by the authors of Model 3 using BNL E865 data

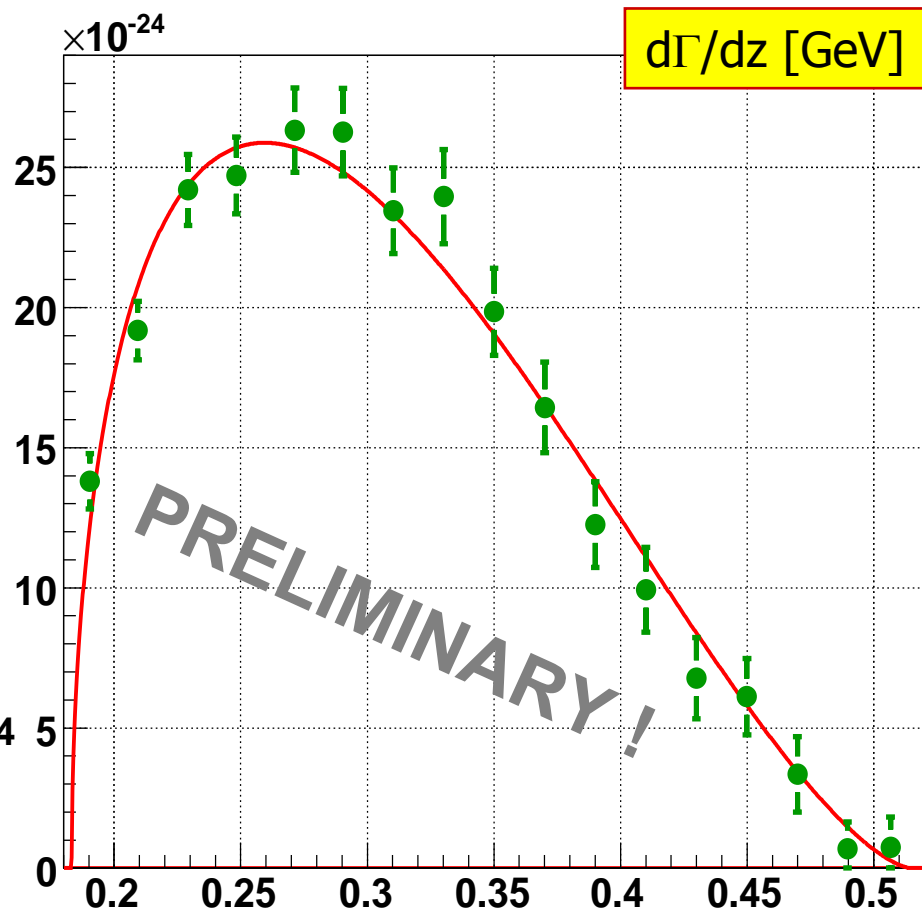
$K^\pm \rightarrow \pi^\pm \mu^+ \mu^-$ - Signal region and fit



Data: Normal $\mu^+ \mu^-$ candidates



Fit to the linear form-factor



~3100 reconstructed events
in the signal region:
**4 times larger sample than
the existing world statistics!**

Conclusions on QCD tests in NA48/2



$\pi\pi$ scattering lengths in Ke4 and $\text{K}3\pi$

- ⊙ NA48/2 has recorded and analyzed $1.15 \cdot 10^6$ Ke4 and $60 \cdot 10^6$ $\text{K}3\pi$ events
- ⊙ $\pi\pi$ scattering lengths results from Ke4 and $\text{K}3\pi$ are fully consistent
- ⊙ the experimental results are in very good agreement with ChPT
- ⊙ the achieved experimental precision on a_0 is now competitive with the theoretical precision (± 0.005) in both decay modes

$\text{K}^\pm \rightarrow \pi^\pm \pi^0 \gamma$

- ⊙ Precise measurement of DE contribution and first measurement of INT term
- ⊙ Extraction of XM and XE values
- ⊙ The BR(DE), assuming INT=0 (55-90) MeV, gives bad χ^2 fit
- ⊙ Measurements of CPV parameters
- ⊙ Final result, paper in preparation

$\text{K}^\pm \rightarrow \pi^\pm e^+ e^-$

- ⊙ Precision comparable with world's best
- ⊙ BR and form factor measurements in agreement with ChPT and other measurements
- ⊙ First limit on CPV asymmetry
- ⊙ Paper published in PLB

$\text{K}^\pm \rightarrow \pi^\pm \mu^+ \mu^-$

- ⊙ Four times larger sample than the existing world statistics has been collected
- ⊙ Analysis is well advanced. Aim to bless

preliminary results this year.

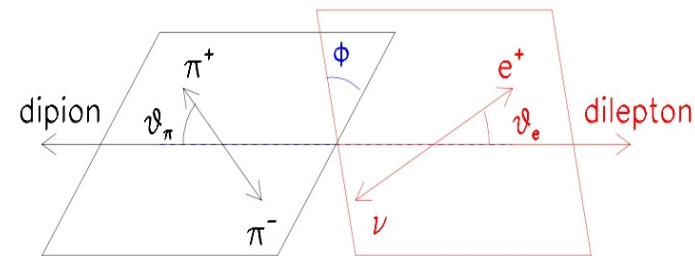


Spares

Ke4 analysis



- Use 5 kinematic variables (Cabibbo-Maksymowicz 1965) $S_\pi (M^2_{\pi\pi})$, $S_e (M^2_{e\nu})$, $\cos\theta_\pi$, $\cos\theta_e$, ϕ
- partial wave expansion of the amplitudes (s and p)
- \rightarrow 2 axial form factors (F and G) + 1 vector (H)
- map the 5D space of variables with 4 form factors + 1 phase
- fitting parameters: $F_s, F_p, G_p, H_p, \delta = \delta_s - \delta_p$
- Define iso-populated boxes in the 5-dimension space:
 $10(M_{\pi\pi}) \times 5(M_{e\nu}) \times 5(\cos\theta_p) \times 5(\cos\theta_e) \times 5(\phi) = 15000$ boxes
- The form factors and phase shift are extracted by minimizing a log-likelihood estimator in 10 independent $M_{\pi\pi}$ bins
- Only relative form factors ($F_p/F_s, G_p/F_s, H_p/F_s$) are measured (no overall normalization from BR)
- The variation of the form factors with $M_{\pi\pi}$ is then fitted to extract the form factors parameters
- analytical properties of $\pi\pi$ scattering amplitudes and dispersion relations (Roy equations) allow to establish a relation between the phase shift δ and the scattering lengths a_0 and a_2





preliminary 2003+ 2004

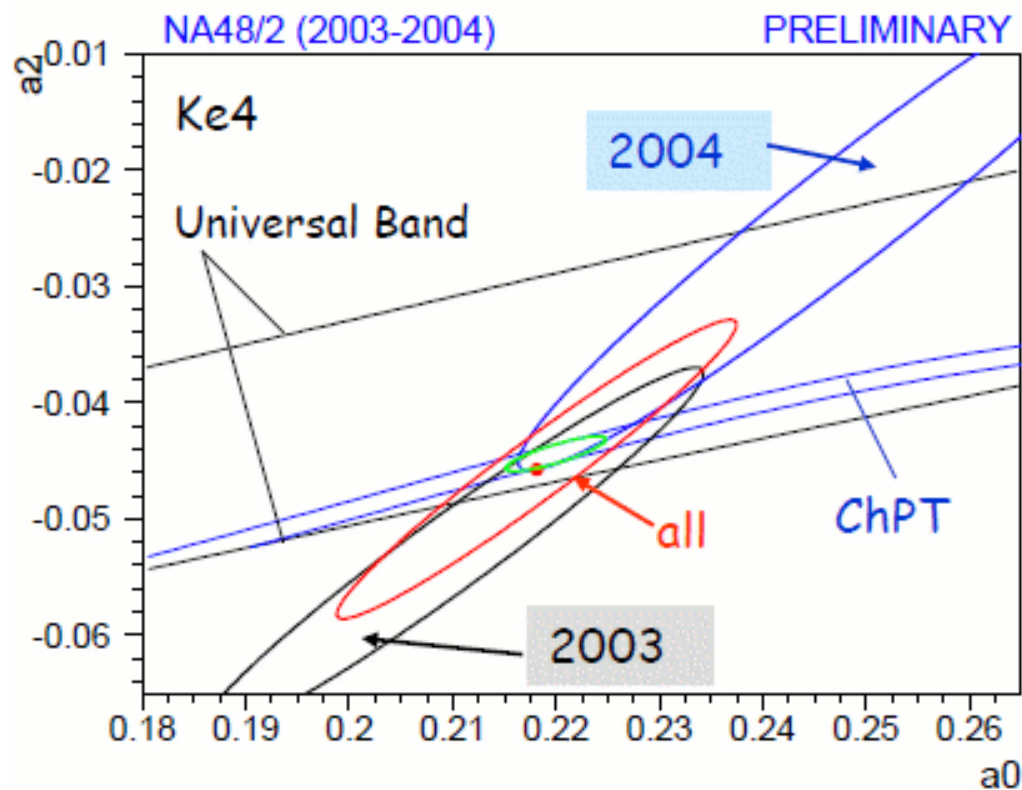
	stat	syst
$f'_s/f_s = 0.158 \pm 0.007 \pm 0.006$		
$f''_s/f_s = -0.078 \pm 0.007 \pm 0.007$		
$f'_e/f_s = 0.067 \pm 0.006 \pm 0.009$		
$f_p/f_s = -0.049 \pm 0.003 \pm 0.004$		
$g_p/f_s = 0.869 \pm 0.010 \pm 0.012$		
$g'_p/f_s = 0.087 \pm 0.017 \pm 0.015$		
$h_p/f_s = -0.402 \pm 0.014 \pm 0.008$		

Results in agreement with published
2003 data analysis

Ke4 - a_0 and a_2 results



1p fit (ChPT)	
a_0	$0.2206 \pm 0.0049_{\text{stat}}$ $\pm 0.0018_{\text{syst}}$ $\pm 0.0064_{\text{theor}}$
2p fit	
a_0	$0.2220 \pm 0.0128_{\text{stat}}$ $\pm 0.0050_{\text{syst}}$ $\pm 0.0037_{\text{theor}}$
a_2	$-0.0432 \pm 0.0086_{\text{stat}}$ $\pm 0.0034_{\text{syst}}$ $\pm 0.0028_{\text{theor}}$



Precise ChPT prediction, CGL NPB 603(2001), PRL86(2001)

$a_0 = 0.220 \pm 0.005$ and $a_2 = -0.0444 \pm 0.0008$

or $(a_0 - a_2) = 0.265 \pm 0.005$

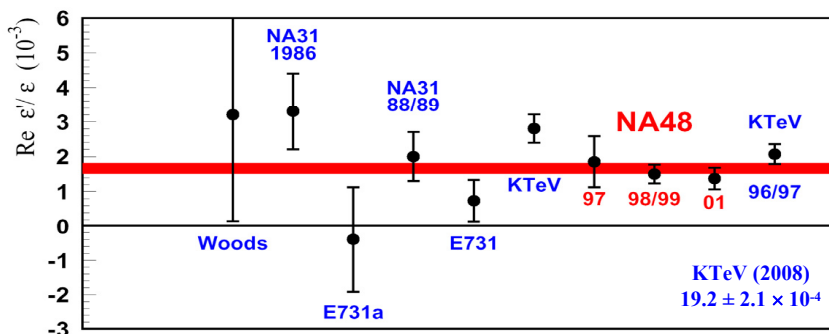
The NA48/NA62 experiment



- **NA48 (1997-2001):**

Direct CP-Violation in neutral K

$$\text{Re}(\epsilon'/\epsilon) = (14.7 \pm 2.2) \cdot 10^{-4}$$



- **NA48/1 (2002):**

Rare K_S decays and hyperons

- **NA48/2 (2003-2004):**

Direct CP-Violation in charged K

- **NA62 (2007-2008) and P326 (2008...):**

$R(K_{e2}/K_{\mu2})$, and new experiment $K^+ \rightarrow \pi^+ \nu \bar{\nu}$

NA48

1997	ϵ'/ϵ run	$K_L + K_S$
1998	ϵ'/ϵ run	$K_L + K_S$
1999	ϵ'/ϵ run $K_L + K_S$	K_S Hi. Int.
2000	K_L only	K_S High Intensity NO Spectrometer
2001	ϵ'/ϵ run $K_L + K_S$	K_S High Int.

NA48/1

2002	K_S High Intensity
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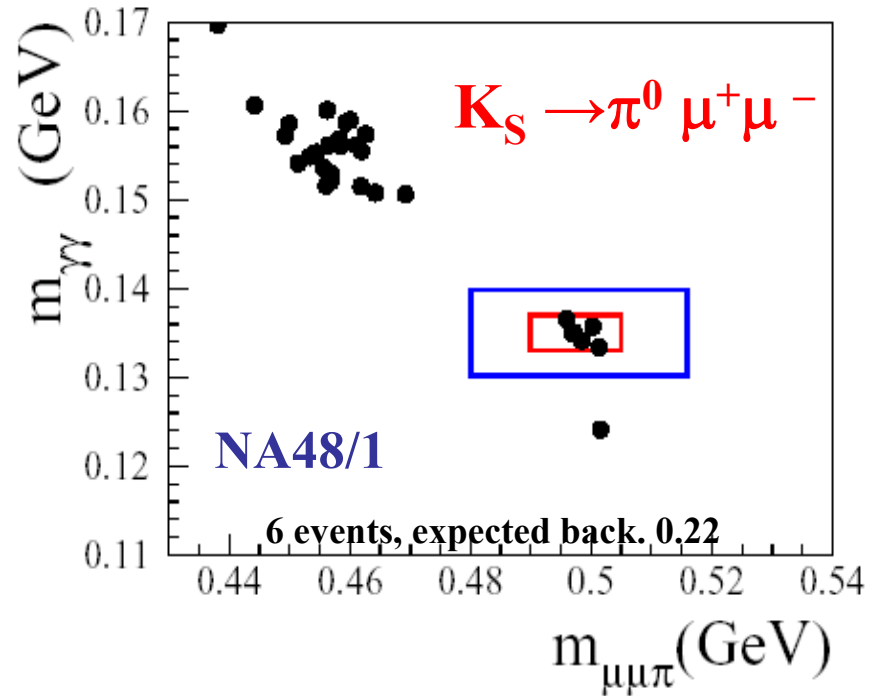
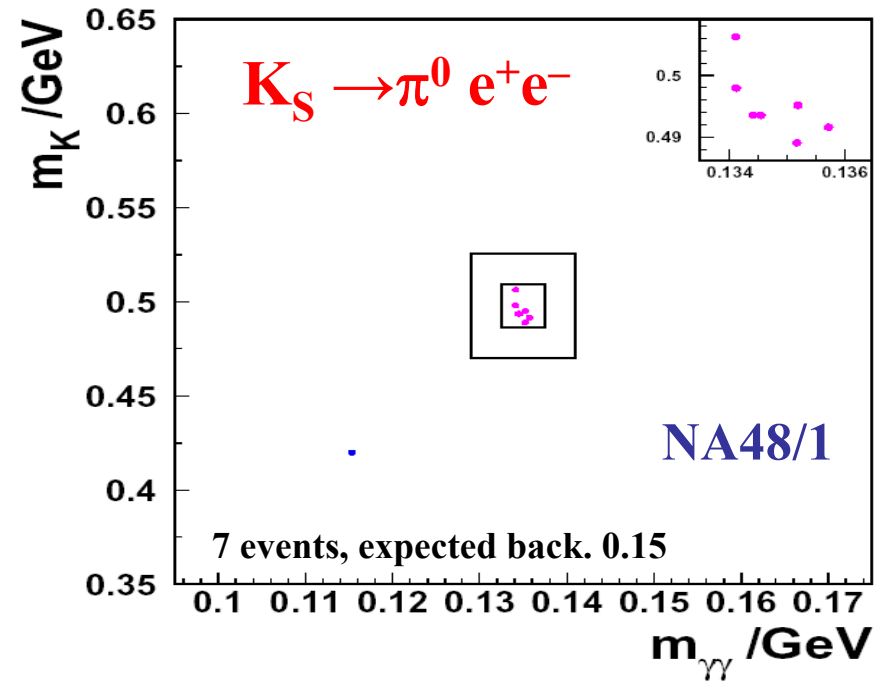
NA48/2

2003	K^\pm High Intensity
2004	K^\pm High Intensity

NA62

2007	$K_{e2}^+ / K_{\mu2}^+$ run
------	-----------------------------

$K_{S,L}^0 \rightarrow \pi^0 e^+e^-$ and $K_{S,L}^0 \rightarrow \pi^0 \mu^+\mu^-$



$$\text{BR}(K_L \rightarrow \pi^0 ee) = (5.8_{-2.3}^{+2.8} \text{ stat} \pm 0.8 \text{ syst}) \times 10^{-9} \quad \text{NA48/1 PLB 576 (2003)}$$

$$\text{BR}(K_L \rightarrow \pi^0 \mu\mu) = (2.9_{-1.2}^{+1.4} \text{ stat} \pm 0.2 \text{ syst}) \times 10^{-9} \quad \text{NA48/1 PLB 599 (2004)}$$

$$\text{BR}(K_L \rightarrow \pi^0 ee) < 2.8 \times 10^{-10} @90\%CL \quad \text{KTeV PRL93, 021805 (2004)}$$

$$\text{BR}(K_L \rightarrow \pi^0 \mu\mu) < 3.8 \times 10^{-10} @90\%CL \quad \text{KTeV PRL86, 5425 (2001)}$$

$K_L^0 \rightarrow \pi^0 e^+ e^- (\mu^+ \mu^-)$ in SM



- Using the K_S measurements, the K_L BR can be predicted (extracting the short-distance physics contribution)
- Interference between short and long distance physics

Constructive

$$B_{K_L^0 \rightarrow \pi^0 e^+ e^-} = 3.7_{-0.9}^{+1.1} \times 10^{-11}$$

$$B_{K_L^0 \rightarrow \pi^0 \mu^+ \mu^-} = 1.5_{-0.3}^{+0.3} \times 10^{-11}$$

now favored by two independent analyses*

Destructive

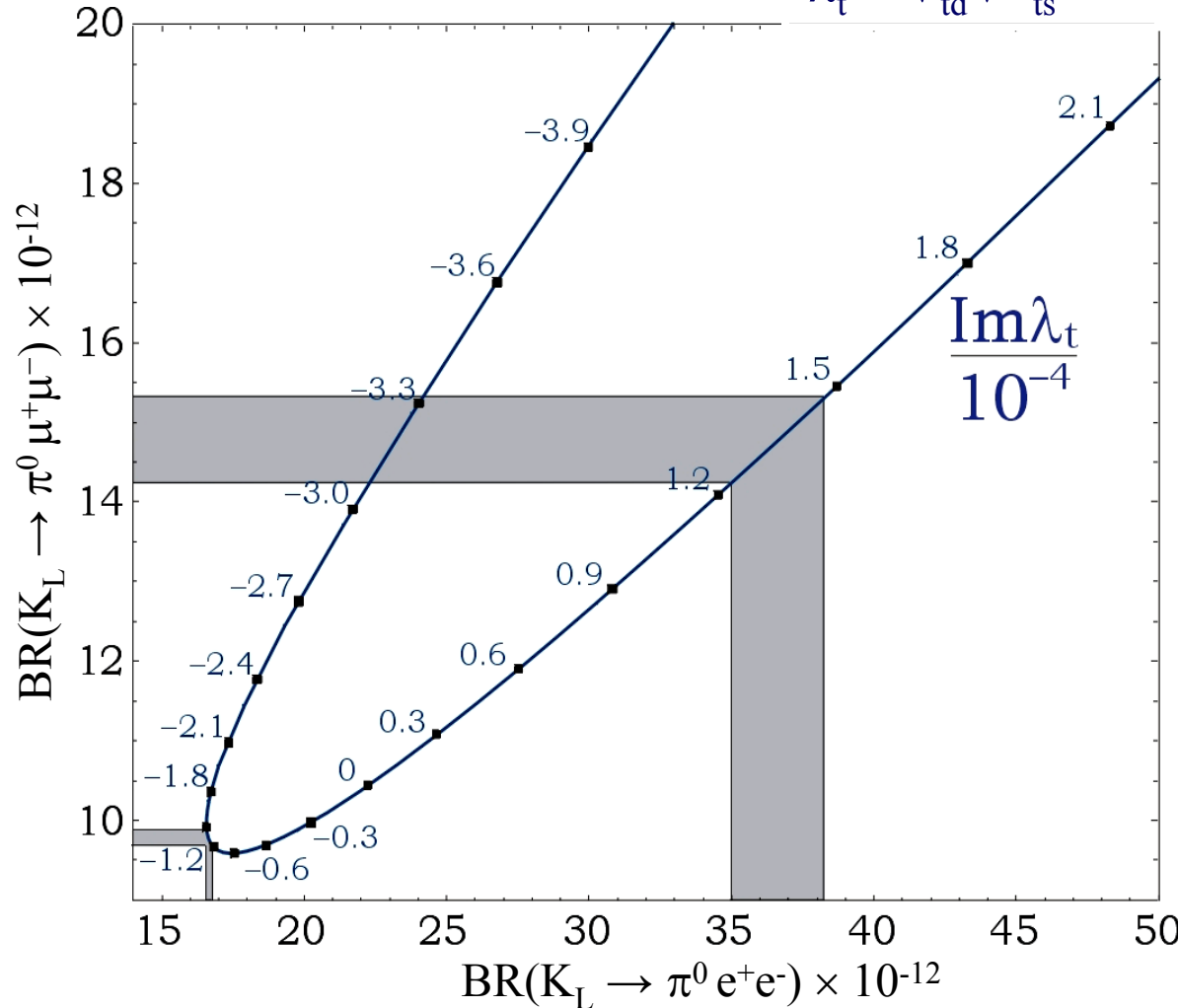
$$B_{K_L^0 \rightarrow \pi^0 e^+ e^-} = 1.7_{-0.6}^{+0.7} \times 10^{-11}$$

$$B_{K_L^0 \rightarrow \pi^0 \mu^+ \mu^-} = 1.0_{-0.2}^{+0.2} \times 10^{-11}$$

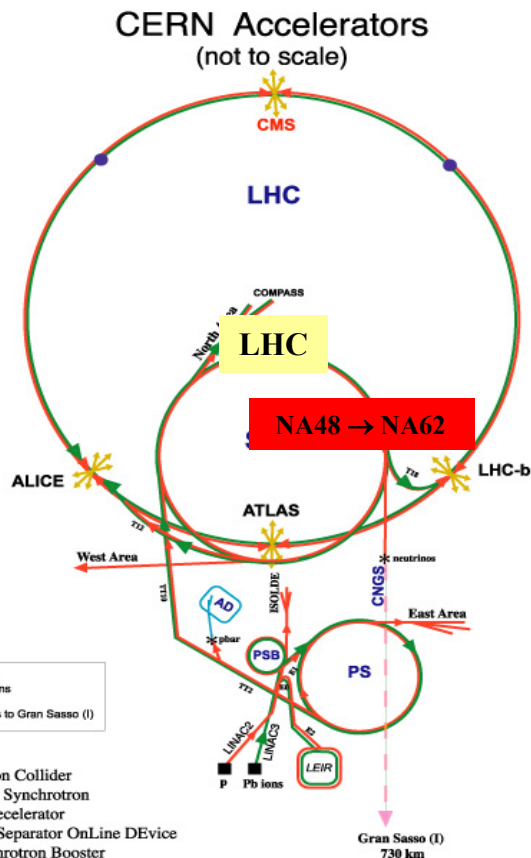
* G. Buchalla, G. D'Ambrosio, G. Isidori, Nucl.Phys.B 672, 387 (2003)

* S. Friot, D. Greynat, E. de Rafael, hep-ph/0404136, PL B 595

$$\lambda_t = V_{td} V_{ts}^*$$



The NA62 experiment

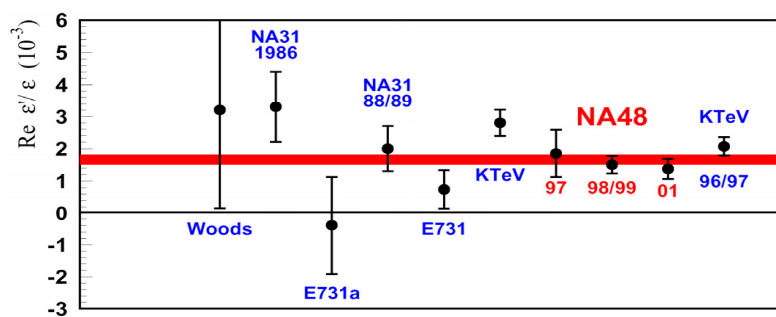


LHC: Large Hadron Collider
 SPS: Super Proton Synchrotron
 AD: Antiproton Decelerator
 ISOLDE: Isotope Separator OnLine DEvice
 PSB: Proton Synchrotron Booster
 PS: Proton Synchrotron
 LINAC: LINear ACcelerator
 LEIR: Low Energy Ion Ring
 CNGS: Cern Neutrinos to Gran Sasso

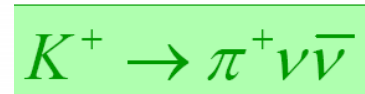
NA48	1997	ϵ'/ϵ run	$K_L + K_S$	
	1998	ϵ'/ϵ run	$K_L + K_S$	
	1999	ϵ'/ϵ run	$K_L + K_S$	K_S Hi. Int.
	2000	K_L only	K_S High Intensity	NO Spectrometer
NA48/1	2001	ϵ'/ϵ run	$K_L + K_S$	K_S High Int.
	2002	K_S High Intensity		
NA48/2	2003	K^* High Intensity		
	2004	K^* High Intensity		

NA62 phase I
 Dedicated 2007 run to measure:

$$R_K = \frac{\Gamma(K^\pm \rightarrow e^\pm \nu_e)}{\Gamma(K^\pm \rightarrow \mu^\pm \nu_\mu)}$$



NA62 phase II
 measurement of the decay



(2008-2010 R&D & construction
 2011 start of data taking)