# Giant Pulsations Excited by a Steep Earthward Gradient of Proton Phase Space Density: Arase Observation 

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We present observational evidence of drift resonance between westward propagating odd mode standing ultralow-frequency waves and energetic protons.

Compressional $\sim 13 \mathrm{mHz}$ ( Pc 4 band) waves and proton flux oscillations at $>50 \mathrm{keV}$ were detected at $\sim 03 \mathrm{hr}$ magnetic local time by the Arase satellite on 15 April 2017. The azimuthal wave number ( $m$ number) is estimated to be $\sim-50$ from ground observations, while the theory of drift resonance gives $m \quad \sim \quad-49$ for odd mode waves and $\sim 110 \mathrm{keV}$ protons, providing that the drift resonance indeed took place in this event. We also found a steep
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earthward gradient of proton phase space density, which can quantitatively explain the wave excitation. The observed waves show typical features of giant pulsations (Pgs), regarding local time, $m$ number, and flux oscillations. This study, therefore, has great implications to the field line mode structure and excitation mechanism of Pgs.

## Keypoints:

- Pc4 ULF waves and proton flux oscillations were observed by Arase and ground magnetometers.
- The azimuthal wave number estimated from ground magnetometers is
consistent with the theory of drift resonance.
- The steep gradient of proton phase space density is responsible for the wave excitation.



## 1. Introduction

Drift resonance or drift-bounce resonance between charged particles and ultralowfrequency (ULF) waves have been drawing attentions for a long time. Since Southwood et al. [1969] first proposed the resonance mechanisms, many researchers have considered that westward propagating poloidal $\operatorname{Pc} 4-5$ (the frequency range of $1.7-22 \mathrm{mHz}$ ) waves with large azimuthal wave number ( $m$ number) observed in the inner magnetosphere are excited through drift resonance or drift bounce resonance with the ring current ions. The resonance condition is

$$
\begin{equation*}
\omega-m \omega_{d}=N \omega_{b} \tag{1}
\end{equation*}
$$

where $\omega$ is a wave angular frequency, $m$ denotes the azimuthal wave number (defined to be positive for eastward propagation), $N$ is an integer that corresponds to mode structure of ULF waves along the field line $(N=0, \pm 2, \ldots$ for odd mode and $N= \pm 1, \pm 3, \ldots$ for even mode), and $\omega_{d}$ and $\omega_{b}$ are drift and bounce angular frequencies, respectively. According to Southwood et al. [1969], whether the resonant particles contribute to wave growth or damping depends on the sign of

$$
\begin{equation*}
\frac{d f}{d W}=\left.\frac{\partial f}{\partial W}\right|_{M_{r e s}, L}+\left.\frac{d L}{d W} \frac{\partial f}{\partial L}\right|_{M_{r e s}, W_{r e s}} \tag{2}
\end{equation*}
$$

where $f$ is the phase space density, $M_{\text {res }}$ is the magnetic moment of resonant particles, $L$ is the McIlwain's L-shell parameter [McIlwain, 1961], and $W_{\text {res }}$ is the resonant energy. If $\frac{d f}{d W}$ is positive (negative), waves are excited (damped) and particles lose (gain) energy.

Equation (1) gives a constraint among resonant energy, mode structure of ULF waves along the field line, and $m$ number in drift resonance or drift-bounce resonance. Driftbounce resonance ( $N=-1$ ) between $80-170 \mathrm{keV}$ protons and second harmonic poloidal
waves with $m \sim-100$ was reported by Takahashi et al. [1990] and Min et al. [2017]. Takahashi et al. [2018] also discussed the drift-bounce resonance ( $N=1$ ) between 1 -10 keV protons and second harmonic poloidal waves with $m \sim-200$. Dai et al. [2013] showed fundamental poloidal waves with $m \sim-70$ are excited by drift resonance $(N=0)$ with $\sim 90 \mathrm{keV}$ protons. These large- $m$ waves are generally observed only by satellites because ionospheric screening effects prevent detection of these waves by ground magnetometers [Hughes $\mathcal{E}$ Southwood, 1976].

Giant pulsations (Pgs) are another type of ULF waves that are considered to be excited through wave-particle interactions. Pgs generally have large amplitudes with highly monochromatic waveform and are observed by ground magnetometers. The east-west component of the magnetic field amplitude is dominant on the ground, and this indicates that Pgs are related to poloidal waves in the magnetosphere [Chisham $\mathcal{G}$ Orr, 1991; Glassmeier, 1980]. It has been reported that Pgs propagate westward $(m<0)$ and have smaller $m$ number $(|m|=10-40)$ [Takahashi et al., 1992; Chisham et al., 1997; Glassmeier et al., 1999; Motoba et al., 2015] than those of the large- $m$ waves $(|m|=70-200)$. Ground observations have revealed that Pgs tend to be detected in the morning sector (around 03 MLT) and at $L \sim 6$ during equinoxes or low solar activity [Sucksdorff, 1939; Brekke et al., 1987; Chisham EJ Orr, 1994; Motoba et al., 2015]. Although there are a few suggestions that substorm injection and drift velocity dispersion could create the MLT dependence of Pgs [Glassmeier et al., 1999; Wright et al., 2001], the reason of the locality and solar activity dependence has not been fully understood yet. In addition, the oscillation mode of Pgs remains to be determined. Both drift resonance with fundamental waves
and drift-bounce resonance with second harmonic waves are considered as possible mechanisms of excitation of Pgs [Takahashi et al., 1992, 2011; Chisham © Orr, 1991; Wright et al., 2001]. Assuming that $\sim 10 \mathrm{keV}$ protons resonate with second harmonic poloidal waves through drift-bounce resonance, some authors conducted numerical simulations and explained the MLT or solar activity dependence by the change of open/closed orbit of $\sim 10$ keV protons [Chisham, 1996; Ozeke \& Mann, 2001]. However, no satellite observations have provided evidence that $\sim 10 \mathrm{keV}$ protons excite Pgs. Geosynchronous satellites have observed proton flux oscillations at $>95 \mathrm{keV}$ related to Pgs [Thompson $\mathcal{E}$ Kivelson, 2001; Motoba et al., 2015], and this supports drift resonance with fundamental mode waves. In these observations, however, it was not discussed if Pgs are excited by resonant particles or vice versa, according to equation (2). Because geosynchronous satellites hardly move in the radial direction, it is difficult to evaluate the radial gradient of phase space density, or the second term of the right-hand side of equation (2). Several studies have pointed out that a bump-on-tail structure causes a positive $\frac{\partial f}{\partial W}$ and excites Pgs [Glassmeier et al., 1999; Wright et al., 2001]; however, the relative importance between the first term and the second term of equation (2) has not been discussed yet.

In this study, we report Pc4 ULF waves and proton flux oscillations observed by the Arase satellite [Miyoshi et al., 2018] and ground magnetometers on 15 April 2017. We estimate the radial gradient of the proton phase space density $\left(\frac{\partial f_{H^{+}}}{\partial L}\right.$, where $f_{H^{+}}$is the proton phase space density) from the radial motion of Arase to examine the instability condition. We also examine $\frac{\partial f_{H^{+}}}{\partial L}$ at the apogee using an ion sounding technique [e.g., Su et al., 1977] and find direct evidence of drift resonance driven by the unstable spatial
distribution of $f_{H^{+}}$. Finally, implications for the oscillation mode structure and excitation mechanism of Pgs are discussed.

## 2. Instrumentation

The Arase satellite, whose main objective is exploration of the outer radiation belt, was launched on 20 December 2016 into an elliptical orbit with the apogee of $\sim 6 R_{E}$ and the perigee altitude of $\gtrsim 300 \mathrm{~km}$ [Miyoshi et al., 2018]. The satellite is spin stabilized $\left(\tau_{\text {spin }} \sim 8\right.$ sec, where $\tau_{\text {spin }}$ is the spin period) and equipped with comprehensive sensors for fields and particles. The magnetic field and energetic ion data from Magnetic Field Experiment (MGF) instrument [Matsuoka et al., 2018] and Medium-Energy Particle Experiments - Ion Mass Analyzer (MEP-i) [Yokota et al., 2017] on board the Arase satellite were analyzed in this study. The MEP-i instrument provides three dimensional flux data for $\mathrm{H}^{+}, \mathrm{He}^{++}$, $\mathrm{He}^{+}, \mathrm{O}^{++}, \mathrm{O}^{+}$, and $\mathrm{O}_{2}^{+}$with a time resolution of $\sim 8$ or $\sim 16 \mathrm{~s}$. The energy range of MEP-i was 5.1-109.6 keV/q before 21 April 2017 and is $9.6-184.2 \mathrm{keV} / \mathrm{q}$ afterward. The aperture of MEP-i has $2 \pi$-radian field of view (FOV) and ions entering through the aperture are detected by 16 anodes circularly arrayed at $22.5^{\circ}$ intervals. Since a normal vector of the $2 \pi$-radian FOV plane is almost perpendicular to the spin axis, MEP-i can scan $4 \pi$ sr due to the Arase's spin motion. The MEP-i measurements are divided into 16 spin phases and ions are detected in 16 energy channels for each spin phase.

## 3. Observations

Arase was located in the morning sector (2.9-3.4 hr of magnetic local time (MLT)) and passing the magnetic equator ( $-2.9^{\circ}$ to $2.9^{\circ}$ of magnetic latitude (MLAT)) during 0040-

0140 UT on 15 April 2017. Arase stayed around the apogee with the radial distance $(r)$ of (C)2018 American Geophysical Union. All Rights Reserved.
6.0-6.1 $R_{E}$. From the decrease of the AL index shown in Figure 1a, we infer that a small substorm started at 0140 UT. Figure 1b shows the magnetic field from Arase processed with a $30-200$ s band-pass filter $(\boldsymbol{\Delta B})$ in a mean field-aligned (MFA) coordinate system. In this system, the magnetic field averaged over a 5 -min moving window is defined as the background field and gives the direction of the $\mu$ (parallel) component ( $\mathbf{e}_{\mu}$ ), the direction of $\phi$ (azimuthal) component is defined as $\mathbf{e}_{\phi}=\mathbf{e}_{\mu} \times \mathbf{r}$, where $\mathbf{r}$ is the satellite position vector from the center of the Earth, and the direction of $\nu$ (radial) component is given by $\mathbf{e}_{\nu}=\mathbf{e}_{\phi} \times \mathbf{e}_{\mu}$. Four or more wave packets of Pc4 waves with a frequency of $\sim 13 \mathrm{mHz}$ are recognized in the $\Delta B_{\mu}$ component between 0040 UT and 0140 UT. Figures 1c-1f show the pitch angle $(\alpha)$ distribution of proton differential flux at energies from 56.3 keV to 109.6 keV . The flux oscillations are most clearly visible at 109.6 keV and are less significant in lower energies. Oscillations should have occurred at $>109.6 \mathrm{keV}$, but this energy range was not covered by MEP-i. The energy dependence of the amplitude of flux oscillations is also found in the power spectral densities (PSDs) of log proton flux at $\alpha=90^{\circ}$ in four energy channels covering $W=56.3-109.6 \mathrm{keV}$ (Figure 1g). Figure 1h shows PSDs of log proton flux at 109.6 keV in seven $\alpha$ bins covering $45^{\circ}-135^{\circ}$. We find that the PSD for $\log$ proton flux around $\alpha=90^{\circ}$ is 10 times larger than that for $\alpha<60^{\circ}$ and $\alpha>120^{\circ}$. The symmetric pitch angle dependence of proton flux oscillations observed in this event indicates that the ULF waves are odd mode waves according to Southwood $\S$ Kivelson [1981].

After 0140 UT, toroidal or compressional waves with higher frequency were observed, but the proton flux did not oscillate. Since these waves are related to the small substorm
(Figure 1a), they are considered to be transient toroidal waves (TTWs) [Saka et al., 1996; Takahashi et al., 1996; Nosé et al., 1998] or Pi2 waves.

To evaluate the instability condition, equation (2), we calculated each term in that equation. The radial distribution of $f_{H^{+}}$was estimated using proton measurements made during 0000-0300 UT as Arase moved radially. The coverage of $L$ was from 5.6 to 6.1 during this interval. Figure 2a shows the radial profile of $f_{H^{+}}$evaluated at $W=109.6 \mathrm{keV}$ and $M=1.1-1.3 \mathrm{keV} / \mathrm{nT}$, which correspond to the protons showing strong oscillations at $W=109.6 \mathrm{keV}$ and $\alpha=90^{\circ}$ at the apogee. At $L>6$, where the Pc 4 waves were observed, we find an earthward gradient of $f_{H^{+}}$. The gradient of the negative slope obtained at $L=6,0-6.1$ is $-575 \mathrm{~s}^{3} \mathrm{~km}^{-6} / R_{E}$. According to equation (2), the negative energy gradient stabilizes the plasma. Therefore, another driver of destabilization is required for wave excitation. The energy dependence of $f_{H^{+}}$at the apogee was also examined (Figure 2b). The $f_{H^{+}}$averaged over the period between 0055 UT and 0115 UT is used. It seems that $\frac{\partial f_{H^{+}}}{\partial W}$ is negative around energy of 109.6 keV and $\frac{\partial f_{H^{+}}}{\partial W}$ obtained from $f_{H^{+}}$at 87.6 and 109.6 keV is $-9.70 \mathrm{~s}^{3} \mathrm{~km}^{-6} / \mathrm{keV}$.

We also used an ion sounding technique to evaluate the radial gradient of $f_{H^{+}}$at the apogee. Figure 2c shows $f_{H^{+}}$at $W=109.6 \mathrm{keV}$ and $\alpha=90^{\circ}$ as a function of time and the direction of proton guiding center relative to the spacecraft. The direction is specified using the $\mu-\phi$ coordinates defined for the magnetic field. A clear depletion of $f_{H^{+}}$with guiding center located anti-earthward from Arase $(+\nu)$ is found. Figure 2 d shows the difference between the proton phase space density with anti-earthward guiding center $\left(f_{H^{+}}(+\nu)\right)$ and earthward guiding center $\left(f_{H^{+}}(-\nu)\right)$. The averaged value of the
difference between $f_{H^{+}}(+\nu)$ and $f_{H^{+}}(-\nu)$ during 0055-0115 UT is $-130 \mathrm{~s}^{3} \mathrm{~km}^{-6}$. The Larmor radius of 109.6 keV proton at the apogee is $0.087 R_{E}$ and the radial gradient of $f_{H^{+}}$is estimated to be $-748 \mathrm{~s}^{3} \mathrm{~km}^{-6} / R_{E}$. This is comparable to the result obtained from the radial motion of Arase. When the earthward gradient of $f_{H^{+}}$appeared during 0030-0140 UT, the Pc4 pulsations increase their amplitudes as shown in Figure 2e. This strongly suggests that the earthward gradient of $f_{H^{+}}$is related to the wave excitation.

Figure 3 shows the ground magnetometer observations of the ULF waves at European quasi-Meridional Magnetometer Array (EMMA) [Lichtenberger et al., 2013]. The solid line in Figure 3a represents the magnetic field footprint of Arase traced by the T04s model [Tsyganenko $\varepsilon$ Sitnov, 2005] in altitude adjusted corrected geomagnetic (AACGM) coordinates. Figure 3b shows the filtered east-west component of the magnetic field ( $\Delta B_{y}$ ) observed at Kevo (KEV, $L=6.5$ ), Ivalo (IVA, $L=5.9$ ), Muonio (MUO, $L=5.7$ ), Sodankylä (SOD, $L=5.4$ ), and Ranua (RAN, $L=4.9$ ). The bottom panel is the $\Delta B_{\mu}$ component observed by Arase. Pc4 waves with a frequency of $\sim 12-14 \mathrm{mHz}$ were observed at the ground. The Pc 4 waves observed at SOD and RAN, which were near the footprint of Arase, have a wave packet structure similar to that observed by Arase. The amplitudes of the Pc 4 waves observed on the ground have a peak at IVA, implying that wave source was located at $L \sim 6$. Even though the wave amplitudes ( $\sim 5 \mathrm{nT}$ peak-to-peak) are slightly small compared to typical Pgs, the localization of the waves in the morning sector and around $L=6$ is a typical feature of Pgs [e.g., Takahashi et al., 2011; Motoba et al., 2015].

From the delay between oscillations at the satellite and ground stations, the direction of wave propagation can be estimated. After 0055 UT, the footprint of Arase was located
to the west of the ground stations. During this period, the wave packets were observed earlier at SOD and RAN than at Arase (for example, see the wave packets observed at SOD and RAN during 0100-0110 UT and that observed by Arase during 0104-0114 UT). This suggests that the wave packets and wave phase were propagating westward. We confirmed this finding by estimating the $m$ number from the phase difference of the Pc 4 waves observed at MUO and SOD. These stations are chosen because they are separated longitudinally by $2.2^{\circ}$ at the almost same geomagnetic latitude ( $64.5^{\circ}$ and $65.3^{\circ}$, respectively). The $m$ number was derived from the following equation:

$$
\begin{equation*}
m=\frac{\theta_{M U O}-\theta_{S O D}}{\left|l o n_{M U O}-l_{S O D}\right|} \tag{3}
\end{equation*}
$$

where $\theta_{M U O(S O D)}$ and $\operatorname{lon}_{M U O(S O D)}$ are phase of the magnetic field oscillations and longitude of MUO (SOD) in AACGM coordinates, respectively. The $\Delta B_{y}$ components for MUO and SOD for the time period when Arase detected a steep earthward gradient are shown in Figure 3c. During this data period, the $\Delta \mathrm{B}_{y}$ components observed at MUO and SOD have a same peak frequency at $12-14 \mathrm{mHz}$ (Figure 3d), where the coherence is greater than 0.8 (Figure 3e), and the cross phase is in the small range from $-108^{\circ}$ to $-113^{\circ}$. From the cross phase, we obtained $m \sim-49$ to -52 . Westward propagation with a moderate $m$ number is also a typical feature of Pgs [e.g., Allan et al., 1983].

## 4. Discussion

To discuss the excitation mechanism of the Pg-like waves observed by Arase and the ground stations, we first examine the resonance signature of the drift resonance or driftbounce resonance. The polarization of the waves observed around the magnetic equator has been discussed in previous studies. Poloidal mode waves are usually considered to be (C)2018 American Geophysical Union. All Rights Reserved.
related to the drift resonance or drift-bounce resonance; however, the radial perturbation of the magnetic field of fundamental (or odd mode) poloidal waves will be small and the compressional perturbation will become prominent near the magnetic equator as explained in Takahashi et al. [1992]. Since the location of Arase was near the magnetic equator and the Pc 4 waves had finite amplitudes in the $\Delta B_{\mu}$ component but not in the $\Delta B_{\nu}$ and $\Delta B_{\phi}$ components (Figure 1b), we conclude that the waves had an odd mode standing structure along the background magnetic field line. The pitch angle dependence of proton flux oscillations (Figures 1c and 1h) supports this interpretation of the mode structure. Both compressional and poloidal waves have an azimuthal electric field which can accelerate ions, thus the wave polarization is not crucial for drift or drift-bounce resonance.

Using observational parameters, we examine the resonance condition shown in equation (1). The bounce and drift angular frequencies are obtained from the following equations (4) and (5) for the dipole field [Hamlin et al., 1961]:

$$
\begin{equation*}
\omega_{b}=\frac{\pi \sqrt{2 W / m_{p}}}{2 L R_{E} T\left(\alpha_{e q}\right)} \tag{4}
\end{equation*}
$$

where $m_{p}$ is mass of proton and $T\left(\alpha_{e q}\right)=1.351-0.925 \sin \alpha_{e q}+0.558 \sin ^{2} \alpha_{e q}-0.248 \sin ^{3} \alpha_{e q}$ (Oimatsu et al., 2018), and

$$
\begin{equation*}
\omega_{d}=-\frac{6 W L P\left(\alpha_{e q}\right)}{q B_{E} R_{E}^{2}}+\frac{2 \Psi_{0}(\mathrm{Kp}) L^{3} \sin \phi}{B_{E} R_{E}^{2}}+\Omega_{E} \tag{5}
\end{equation*}
$$

where $q$ is the electric charge, $B_{E}$ is the magnitude of the magnetic field on the earth's surface at the magnetic equator, $P\left(\alpha_{e q}\right)=0.340+0.226 \sin \alpha_{e q}-0.154 \sin ^{2} \alpha_{e q}+0.88 \sin ^{3} \alpha_{e q}$ (Oimatsu et al., 2018), $\Psi_{0}(\mathrm{Kp})$ is the Volland-Stern electric potential model as a function of Kp index [Volland, 1973; Stern, 1975], $\phi$ is the azimuthal angle eastward positive from the midnight, and $\Omega_{E}$ is the corotational electric field potential. As the AL index was less (C)2018 American Geophysical Union. All Rights Reserved.
than 300 nT in the event period, the dipole field well describes the inner magnetosphere. The value of $B_{E}$ is obtained from the IGRF-12 model [Thébault et al., 2015]. The energy of protons that resonate with the Pc 4 waves is shown in Figure 4 for different values of $N$. Protons at $\alpha=90^{\circ}$ and Pc 4 waves with a frequency of 12.7 mHz are considered in this calculation. Because the ULF waves observed in this event are considered to be odd mode waves, the drift resonance $(N=0)$ or drift-bounce resonance ( $N= \pm 2$ ) are possible. Since the flux oscillations due to the drift-bounce resonance with odd mode waves should have a peak of amplitudes at $\alpha<90^{\circ}$ and $\alpha>90^{\circ}$ (Yang et al., 2011a; Yang et al., 2011b), which is not the case in the present study, only the drift resonance can explain the wave excitation. Figure 4 shows that if $N=0$ and the resonance energy is 109.6 keV , where the proton flux was strongly oscillating, the $m$ number is theoretically estimated to be -49 . This is consistent with the $m$ number estimated from ULF observations at the ground stations ( $m \sim-50$ ). Therefore, the drift resonance is plausible in this event. Since 109.6 keV is the highest energy measured by MEP-i, the possibility of the drift resonance at slightly higher energies can not be excluded.

From equation (2), we determine whether wave are excited or damped through the drift resonance. According to Southwood et al. [1969], $\frac{d L}{d W}$ is given by $\frac{m L^{2}}{q R_{E}^{2} \omega B_{E}} \cdot \frac{\partial f}{\partial L}$ was obtained from the ion sounding technique (Figures 2c and 2d), and $\frac{\partial f}{\partial W}$ was determined from the energy spectrum during 0055-0115 UT (Figure 2b). We substitute the value of $m$ number estimated from the ground observation during 0055-0115 UT ( $m \sim-50$ ) in equation (2). Finally, we obtain the following $\frac{d f}{d W}$ at $M=1.1-1.3 \mathrm{keV} / \mathrm{nT}$ and $W=109.6 \mathrm{keV}$ :

$$
\begin{equation*}
\frac{d f}{d W}=-9.70+\left(-1.73 \times 10^{-2}\right) \times\left(-7.48 \times 10^{2}\right)=3.22\left(\mathrm{~s}^{3} \mathrm{~km}^{-6} / \mathrm{keV}\right)>0 \tag{6}
\end{equation*}
$$

In the previous studies, only the bump-on-tail structure was considered as the energy source of Pgs [Glassmeier et al., 1999; Wright et al., 2001]. This result, however, suggests that the Pc4 waves were excited by the earthward gradient of $f_{H^{+}}$even if the negative slope of $f_{H^{+}}$in the energy spectrum suppress the instability. The good correspondence between the steep earthward gradient of $f_{H^{+}}$and wave excitation in Figures 2c and 2d supports this interpretation. When the spatial gradient and the energy gradient have opposite effects on the wave generation, Pgs with relatively small amplitudes may be excited as in the case of the present study.

## 5. Conclusions

On 15 April 2017, the Arase satellite detected a compressional magnetic field oscillation in the Pc 4 band that was related to a giant pulsation observed on the ground. We examined in far more detail the oscillations of the flux of energetic ( $56.3-109.6 \mathrm{keV}$ ) protons than reported previously [Glassmeier et al., 1999; Thompson 8 Kivelson, 2001; Motoba et al., 2015]. We found evidence that the waves had an odd mode standing structure along the background magnetic field and that the waves were in drift resonance with $\sim 110 \mathrm{keV}$ protons. The Arase satellite also detected an earthward gradient of $f_{H^{+}}$. Several previous studies considered the bump-on-tail structure in energy spectrum of $f_{H^{+}}$ as an energy source of Pgs. However, the Pc4 waves examined in this study are excited by the steep earthward gradient of $f_{H^{+}}$. We suggest that the spatial distribution of the phase space density also plays an important role in the exicitation of Pgs.

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Figure 1. (a) The AL index. (b) The magnetic field observed by Arase in MFA coordinates. The blue line represents radial component, the green line represents azimuthal component, and the red line represents parallel component. (c-f) The pitch angle distribution of proton differential flux at energies of $109.6,87.8,70.3$, and 56.3 keV . (g) PSDs for $\Delta B_{\mu}$ component and log proton flux at $\alpha=90^{\circ}$ and $W$ $=56.3-109.6 \mathrm{keV}$. (h) PSDs for $\Delta B_{\mu}$ component and proton flux at $W=109.6 \mathrm{keV}$ and $\alpha=45^{\circ}-145^{\circ}$.


Figure 2. (a) The radial profile of $f_{H^{+}}$at $W=109.8 \mathrm{keV}$ and $M=1.1-1.3 \mathrm{keV} / \mathrm{nT}$. The standard deviation is shown for each point. (b) The energy dependence of $f_{H^{+}}$near the apogee. (c) $f_{H^{+}}$obtained from an ion sounding technique as a function of time and the direction of proton guiding center relative to the spacecraft. (d) 3 -min running average of $f_{H^{+}}(+\nu)$ (red line) and $f_{H^{+}}(-\nu)$ (blue line), and the difference between $f_{H^{+}}(+\nu)$ and $f_{H^{+}}(-\nu)$ (black line). (e) $\Delta B_{\mu}$ component observed by Arase. The TTWs or Pi2 wave oscillations are colored in gray.


Figure 3. (a) Locations of the Arase's magnetic field footprint and EMMA magnetometer stations in AACGM coordinates. The large solid circles indicate locations of Arase every one hour. The small solid circles are marked every 10 minutes. (b) $\Delta B_{y}$ component observed at the magnetometer stations. The background field is removed by a Savitzky-Golay filter with a window width of 200 s . (c) $\Delta B_{y}$ components observed at MUO (black line) and SOD (red line) during 0055-0115 UT. (d-f) Power spectra, coherence, and cross phase estimated from the data shown in (c). The spectral peaks are highlighted by shading in gray. Only the data points with coherence greater than 0.8 are shown in the cross phase.



Figure 4. Energy of protons that are in resonance with ULF waves at $L=6.1$ as a function of the $m$ number of the waves, shown for a wave frequency of 12.7 mHz and the equatorial pitch angle of $90^{\circ}$.


