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# Image Haze Removal Algorithm Based on Nonsubsampled Contourlet Transform

## BOWEN ZHANG<sup>®1</sup>, MANLI WANG<sup>®2</sup>, AND XIAOBO SHEN<sup>®1</sup>

<sup>1</sup>School of Computer Science and Engineering, Nanjing University of Science and Technology, Nanjing 210094, China <sup>2</sup>School of Physics and Electronic Information Engineering, Henan Polytechnic University, Jiaozuo 454003, China Corresponding author: Manli Wang (wml920@163.com)

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**ABSTRACT** In order to avoid the noise diffusion and amplification caused by traditional dehazing algorithms, a single image haze removal algorithm based on nonsubsampled contourlet transform (HRNSCT) is proposed. The HRNSCT removes haze only from the low-frequency components and suppresses noise in the high-frequency components of hazy images, preventing noise amplification caused by traditional dehazing algorithms. First, the nonsubsampled contourlet transform (NSCT) is used to decompose each channel of a hazy and noisy color image into low-frequency sub-band and high-frequency direction subbands. Second, according to the low-frequency sub-bands of the three channels, the color attenuation prior and dark channel prior are combined to estimate the transmission map, and use the transmission map to dehaze the low frequency sub-bands. Then, to achieve the noise suppression and details enhancement of the dehazed image, the high-frequency direction sub-bands of the three channels are shrunk, and those shrunk sub-bands are enhanced according to the transmission map. Finally, the nonsubsampled contourlet inverse transform is performed on the dehazed low-frequency sub-bands and enhanced high-frequency sub-bands to reconstruct the dehazed and noise-suppressed image. The experimental results show that the HRNSCT provides excellent haze removal and noise suppression performance and prevents noise amplification during dehazing, making it well suited for removing haze from noisy images.

**INDEX TERMS** Image processing, image restoration, haze removal, nonsubsampled contourlet transform, noise suppression.

#### **I. INTRODUCTION**

With the rapid development of the Internet of Things, big data, and cloud computing technologies, video devices are increasingly used in outdoor video surveillance systems. However, hazy weather significantly affects the image quality of the video surveillance systems and the subsequent image processing results, such as image segmentation, target recognition [1], and other tasks. Numerous haze removal algorithms have been proposed to improve the quality of hazeaffected images.

Most existing dehazing algorithms are based on image enhancement [2], [3], physical models [4]–[6] or machine learning [7], [8]. These algorithms can be divided into two categories, namely those with and without noise suppression.

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Dehazing algorithms without noise suppression ability focus on estimating atmospheric light or a transmission map. For example, Ancuti *et al.* [9] used local atmospheric light to replace the global atmospheric light of traditional dehazing algorithms. Shin *et al.* [10] integrated radiation and reflection data to optimize the transmission map estimation.

A fast image dehazing algorithm based on a simple linear transformation was presented by Wang *et al.* [11], the dehazing algorithm that used the linear transformation was faster than classic methods. Lou *et al.* improved the maximum reflectance prior (MRP) and used it to remove haze from nighttime images [12].

The transmission map in these dehazing algorithms is estimated based on a prior obtained from the image statistics; this topic is a research hotspot. The well-known dark channel prior (DCP) [13] refers to prior knowledge based on the statistics of haze-free images. Since it is a statistical law,

it is inevitable that there is a deficiency in some specific scenes. The hazy image cannot include the sky area when the DCP is used to estimate a transmission map, and dehazed images by DCP are prone to produce halo effect. Therefore, numerous methods [14]-[18] that optimize or refine the transmission map estimated by the DCP were developed. Sahu and Seal [19] presented an image dehazing method that calculated a transmission map of the non-sky and sky regions of the hazy image using DCP and luminance stretching, respectively. The luminance stretching method could restore hazy images that included the sky, and the dehazed images were clearer than those obtained from the DCP method. In addition to DCP, some scholars have successively proposed transmission map estimation methods [20]-[26] with prior constraints, such as the color ellipsoid prior [20] and the color attenuation prior (CAP) [21].

With the development of deep machine learning methods, dehazing algorithms [27]–[31], and [32] based on deep machine learning methods have also been developed.

Dong *et al.* [33] proposed a multi-scale boosted dehazing network with dense feature fusion to preserve spatial information in the U-Net architecture. The results showed that the U-Net architecture was suitable for dehazing and provided good dehazing performance. Shao *et al.* [34] presented a dehazing net with a bidirectional translation network to achieve domain adaptation between the synthetic and real image domains. The dehazing net improved the performance of the dehazing model trained by synthetic hazy images. Shao *et al.* [34] proposed a binocular image dehazing network (BidNet) for removing haze from stereo images. The BidNet included a stereo transmission map estimation network and an atmospheric light estimation network and achieve dehazing for stereo images based on the physical scattering model.

Nonetheless, the methods of the above-mentioned documents except for [4], [30], and [31], do not consider noise interference in hazy images. The noise in hazy images is often amplified when these algorithms are used to remove haze, leading to the distortion of the dehazed images and the loss of details.

Gao and Hu *et al.* [4] introduced a noise term into the atmospheric scattering model and analyzed the reasons for the noise amplification caused by traditional dehazing algorithms. The authors proposed a depth-chromaticity regularization method based on the strong correlation between the depth and chromaticity of an image and the transmission map. The regularization method aimed to optimize the transmission map and the dehazed image and suppressed noise (noise in the original image and noise resulting from dehazing). In [30] and [31], dehazing algorithms with noise suppression were proposed.

Although the dehazing algorithms in [4], [30], and [31] have noise suppression functions, they focus on reducing the influence of noise on the estimated transmission map and suppressing the noise amplified by the haze removal process. However, these algorithms may still amplify the noise during the dehazing process.

Thus, in this study, a single-image haze removal algorithm based on nonsubsampled contourlet transform (HRNSCT) is proposed to prevent noise diffusion and amplification during haze removal by decoupling the haze removal and noise suppression processes in the contourlet transform domain.

The highlights of this paper are as follows.

1. The HRNSCT algorithm decouples the haze removal and noise suppression of hazy images, minimizing the risk of noise amplification during the haze removal process of traditional algorithms.

2. The transmission map and atmospheric light are estimated accurately by using the low-frequency sub-bands of the hazy image and combining the CAP and the DCP. This approach improves the estimated transmission map and avoids noise interference when estimating the transmission map and atmospheric light.

3. The HRNSCT algorithm allows for dehazing only the low-frequency components of hazy images and provides a new approach for dehazing hazy images with noise.

4. The noise in the dehazed image is suppressed by shrinking the high-frequency sub-bands of the original hazy image, providing a new method for the noise suppression of dehazing algorithms.

The remainder of this paper is organized as follows.

The HRNSCT framework is described in Section II, including image decomposition, scene depth, and atmospheric light estimation, transmission map estimation based on two priors, noise suppression, haze-free low-frequency sub-band recovery, noise suppression, high-frequency detail enhancement, and haze removal. The HRNSCT algorithm is described in Section III. The dehazing results of the HRNSCT are provided and compared with those of other algorithms in Section IV. The parameters of the HRNSCT are analyzed in Section V, and the conclusions are presented in Section VI.

# II. DECOUPLED FRAMEWORK OF HAZE REMOVAL AND NOISE SUPPRESSION

As described in [36], haze mainly occurs in the low-frequency part of an image. A noise term n is added to the atmospheric scattering model, and the hazy image and the dehazed image are expressed as high-frequency components and lowfrequency components, respectively. The atmospheric scattering model is defined in Eq. (1):

$$\boldsymbol{I} = \boldsymbol{I}_l + \boldsymbol{I}_h = \boldsymbol{J}_l \cdot \boldsymbol{t} + A(1 - \boldsymbol{t}) + \boldsymbol{J}_h \cdot \boldsymbol{t} + \boldsymbol{n}, \qquad (1)$$

where  $I_l = J_l \cdot t + A(1 - t)$ ,  $I_h = J_h \cdot t + n$ . I,  $I_l$ , and  $I_h$ , respectively, are the hazy image, the low-frequency component, and the high-frequency component of the hazy image. J,  $J_l$ , and  $J_h$  denote the target (dehazed) image, the lowfrequency component, and the high-frequency component of the dehazed image, respectively. n refers to Gaussian noise with zero mean. A represents the global atmospheric light.  $t = e^{-\beta d(x,y)}$  is the transmission map, d(x, y) refers to the scene depth, and  $\beta$  denotes the scattering coefficient of the atmosphere.



FIGURE 1. Framework of the image haze removal algorithm based on the nonsubsampled contourlet transform (HRNSCT).

Equation (1) indicates that if A and t are known, and the interference of noise n can be eliminated, the dehazed image J can be obtained from the hazy image I. However, only the hazy image I is known in Eq. (1). If I can be decomposed into the low-frequency component  $I_l$  and the high-frequency component  $I_h$ ,  $I_l$  contains almost all the haze and the contour structures of the image, and  $I_h$  includes the texture details and noise of the image. Subsequently, the haze is removed from the  $I_l$ , and the noise is suppressed in the  $I_h$ , thereby decoupling the haze removal and noise suppression processes. After the image is decomposed, the haze removal process is converted into the estimation of the atmospheric light A and the transmission map. It is known from Refs. [11], [18] that A and t can be estimated using the CAP or the DCP. Nonetheless, both priors have advantages and disadvantages; thus, the two priors are both used to estimate A and t in this study.

The nonsubsampled contourlet transform (NSCT) is used to decompose the hazy image, and the CAP and DCP are combined to estimate the transmission map and atmospheric light. The framework of the HRNSCT is shown in Figure 1, where the red, green, and blue borders represent the r, g, bcolor channels of the color image.

#### A. IMAGE DECOMPOSITION USING NSCT

In [37] and [38], the nonsubsampled pyramid (NSP) transform and nonsubsampled directional filter bank (NSDFB) were used in the NSCT for multi-scale and multi-directional image decomposition. First, the image was decomposed into low-frequency and high-frequency components by the NSP. Then the high-frequency components were divided into different directional sub-bands in the frequency domain by the NSDFB. The multi-scale decomposition and frequencydomain segmentation are shown in Figure 2. After N iterations, a low-frequency sub-band and  $\sum_{j=1}^{n} 2^{j}$  high-frequency sub-bands were obtained. Since neither the NSP nor the NSDFB performs nonsubsampled operations, each sub-band matrix of the NSCT has the same size as the original input image.

For the convenience of description, the symbol  $T_{NSCT}()$  is used to indicate the NSCT operation. An image *I* is decomposed by the NSCT using the expression in Eq. (2), where  $C_l^c$ denotes the low-frequency sub-bands of the three channels of the color image, and  $C_l^c = I_l^c$ .  $C_{h,j,s}^c$  represent the highfrequency directional sub-bands of the three channels, which contain the texture details and almost all noise in the color image. *L* and  $S_j$  refer to the maximum decomposition scale of the NSCT and the number of directions on the given scale, respectively. *c* denotes the *r*, *g*, *b* channels of the color image.  $\{C_l^c, C_{h,j,s}^c, j = 1, 2, ..., L, s = 1, 2, ..., S_j\}$  denotes a set of all contourlet sub-bands of the image.

$$T_{NSCT}(I^{c}) = \left\{ C_{l}^{c}, C_{h,j,s}^{c}, j = 1, 2, \dots, L, s = 1, 2, \dots, S_{j} \right\},\ c \in \{r, g, b\}$$
(2)

### B. SCENE DEPTH AND ATMOSPHERIC LIGHT ESTIMATION

In [21], the CAP of hazy images was presented. The CAP indicates that the haze density of a hazy image is closely related to the brightness and saturation of the image. The scene depth d(x, y) and the haze density  $H_d(x, y)$  of the hazy



(b) Frequency domain segmentation

**FIGURE 2.** Nonsubsampled decomposition and frequency division of the NSCT. (a) Multiscale decomposition; (b) frequency-domain segmentation.

image are positively correlated with the difference between the brightness v(x, y) and saturation s(x, y) of the hazy image in the hue, saturation, value (HSV) color space. The deeper the scene depth in the hazy image, the greater the haze density is. In addition, the difference between brightness and saturation increases with increasing haze density. The proportional relationship between the scene depth of the hazy image and the haze density is defined in Eq. (3):

$$\boldsymbol{d}(x, y) \propto \boldsymbol{H}(x, y) \propto \boldsymbol{v}(x, y) - \boldsymbol{s}(x, y), \tag{3}$$

where d(x, y) and H(x, y) denote the scene depth and haze density, respectively. v(x, y) and s(x, y) denote the brightness and saturation, respectively, of the hazy image in the HSV color space, and (x, y) is the pixel coordinate of the hazy image.

A linear estimation model of the scene depth of a hazy image based on the CAP was developed in [18]:

$$\boldsymbol{d}(x, y) = \theta_0 + \theta_1 \boldsymbol{v}(x, y) + \theta_2 \boldsymbol{s}(x, y) + \boldsymbol{\varepsilon}(x, y), \qquad (4)$$

where  $\theta_0$ ,  $\theta_1$ , and  $\theta_2$  represent the unknown linear coefficients of the model.  $\varepsilon(x, y)$  refers to a random error term of the model with a Gaussian distribution with mean 0 and variance  $\sigma^2$ . In [18], the model (Eq. (4)) is trained using the hazy image set; the parameters of the trained model are  $\theta_0 = 0.121779$ ,  $\theta_1 = 0.959710$ ,  $\theta_2 = -0.780245$ , and  $\sigma = 0.041337$ . These parameters are used to estimate the scene depth of hazy images in this study.

Equation (1) indicates that the global atmospheric light A and transmission map t(x, y) have to be known to remove

haze from the low-frequency components of the hazy image. According to Eqs. (3) and (4), the greater the v(x, y) - s(x, y), the farther the scene depth distance is, and the brighter the area corresponding to the depth map is. Therefore, all grey values of the depth map are sorted; the pixel positions of the first 0.1% of the gray values of the depth map are marked, and the maximum of these pixel values in the low-frequency component  $I_{l}$  is regarded as the atmospheric light A. When the atmospheric light is computed, and the depth map is estimated using Eq. (4), white objects in the image can be mistaken for the atmospheric light. The basic scene depth  $d_{\rm b}(x, y)$  is replaced by the regional scene depth  $d_{\rm r}(x, y)$  when computing A to improve the robustness of the atmospheric light estimation.  $d_r(x, y)$  is obtained by filtering  $d_b(x, y)$  using a local minimum filter. The local minimum filter operator is defined in Eq. (5):

$$\boldsymbol{d}_{\mathrm{r}}(\boldsymbol{x},\boldsymbol{y}) = \underset{(\boldsymbol{x},\boldsymbol{y})\in w_{r}}{F_{\mathrm{min}}} \boldsymbol{d}_{\mathrm{b}}(\boldsymbol{x},\boldsymbol{y}), \tag{5}$$

where  $w_r$  denotes a  $r \times r$  neighborhood window centered on (x, y), and  $F_{\min}$  denotes the minimum filter operator.

We mark the pixel position of the first 0.1% of the grey values of  $d_r(x, y)$  and determine the maximum value at the corresponding position of  $I_l$  as the atmospheric light A.

#### C. TRANSMISSION MAP ESTIMATION BASED ON TWO PRIORS

The most common priors used for estimating the transmission map include the CAP and the DCP. Since both have advantages and disadvantages, both priors are used to estimate the transmittance transmission map.

According to the CAP,  $I_l$  is converted from the RGB color space to the HSV color space. Equation (4) is used to obtain the scene depth estimate  $d_b(x, y)$  of  $I_l$ . Because the edges and details of the original hazy image I retained by  $d_b(x, y)$  are not fine enough, halos may occur in the edge contour area of the dehazed image. Therefore,  $d_b(x, y)$  is filtered with a guided filter to refine the transmission map.

In [39] and [40], it is assumed during the use of the guided filter that the output image Q and the guide image G are locally linear, i.e., in the square window  $w_k$  centered on k, Q is the linear transformation of G, as defined in Eq. (6):

$$\boldsymbol{Q}_i = \boldsymbol{a}_k \boldsymbol{G}_i + \boldsymbol{b}_k, \quad \forall i \in w_k, \tag{6}$$

where  $a_k$  and  $b_k$  are the linear coefficients in the local window  $w_k$ , whose value can be estimated by the cost function (Eq. (7)):

In Eq. (7),  $\lambda$  refers to the balance factor to prevent  $a_k$  from becoming too large.  $I_l$  represents the filtered image. According to the linear ridge regression model,  $a_k$  and  $b_k$  can be calculated by Eq. (7):

$$\begin{cases} \boldsymbol{a}_{k} = \frac{\frac{1}{|w|} \sum_{i \in w_{k}} \boldsymbol{G}_{i} \boldsymbol{I}_{li} - \mu_{k} \boldsymbol{\bar{I}}_{lk}}{\sigma_{k}^{2} + \lambda} \\ \boldsymbol{b}_{k} = \boldsymbol{\bar{I}}_{lk} - \boldsymbol{a}_{k} \mu_{k}, \end{cases}$$
(7)



**FIGURE 3.** Transmission map and temporary values obtained from the color attenuation prior.

where  $\mu_k$  and  $\sigma_k^2$  are the mean and variance of the guide image **G** in the local window  $w_k$ . |w| denotes the number of pixels in the local window  $w_k$ , and  $\bar{I}_{lk} = \frac{1}{|w_k|} \sum_{i \in w_k} I_{li}$  is the mean value of the filtered image in the local window  $w_k$ .

When the scene depth is filtered, the sum image of the low-frequency sub-bands and the high-frequency directional sub-bands corresponding to the first decomposition scale of the hazy image is regarded as the guide image to avoid the influence of noise in the hazy image and include the sufficient details in the guide image. In other words, the calculation result of Eq. (8) is used as the guide image. In Eq. (8),  $C_l^c$  denotes the low-frequency sub-bands,  $C_{h,1,s}^c$  denotes the high-frequency directional sub-bands corresponding to the first decomposition scale, and  $S_1$  represents the number of decomposition directions corresponding to the first decomposition scale of the hazy image.

$$G = C_l^c + \sum_{s=1}^{S_1} C_{h,1,s}^c, \quad c \in \{r, g, b\},$$
(8)

The final refined scene depth estimate  $d_g(x, y)$  is obtained by filtering  $d_b(x, y)$ ; *G* is used as the guide image of the guided filter. For ease of description, the symbol  $F_g()$  is used to represent the guided filter operator,  $d_b(x, y)$  and *G* denote the image to be filtered and the guide image, respectively. This filtering process is expressed as Eq. (9):

$$\boldsymbol{d}_{\mathrm{g}}(x, y) = F_{\mathrm{g}}(\boldsymbol{G}, \boldsymbol{d}_{\mathrm{b}}(x, y)), \tag{9}$$

After  $d_g(x, y)$  is obtained, the transmission map  $t_1(x, y)$  is computed using Eq. (10):

$$\boldsymbol{t}_1(\boldsymbol{x}, \boldsymbol{y}) = \exp(-\beta \boldsymbol{d}_{\mathrm{g}}(\boldsymbol{x}, \boldsymbol{y})), \quad (10)$$

where  $\beta$  denotes the attenuation coefficient. The recommended range of  $\beta$  is [0.8,2.5]; the greater the value of  $\beta$ , the smaller the value of the transmission map is.

Figure 3 shows the estimated basic scene depth  $d_b(x, y)$ , regional scene depth  $d_r(x, y)$ , final scene depth  $d_g(x, y)$ , and the transmission map  $t_1(x, y)$  of the hazy image from left to right.

Subsequently, the transmission map  $t_2(x, y)$  is estimated using the DCP to compensate for the defects of the estimate obtained from the CAP. The DCP is an empirical result obtained from the statistics of many haze-free outdoor images. The grey values of one of the three channels of the haze-free images in the RGB space are always close to zero. In other words, the minimum grey values of the three channels r, g, b tend to zero. Hence, the real scene image without sky

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areas satisfies the dark primary color defined in Eq. (11):

$$J^{\text{dark}} = \min_{(x,y)\in\Omega(x,y)} (\min_{c\in\{r,g,b\}} (J^c(x,y))),$$
(11)

where  $\Omega(x, y)$  represents the local window centered on (x, y), and  $J^c$  is one of the color channels of the haze-free image J. In the non-sky and haze-free image, the dark primary color  $J^{\text{dark}}$  tends to zero according to the DCP.

According to the DCP and the atmospheric scattering model, the transmission map  $\tilde{t}(x, y)$  can be estimated by Eq. (12) when the atmospheric light is known.

$$\tilde{\boldsymbol{t}}(\boldsymbol{x},\boldsymbol{y}) = 1 - \alpha \cdot \min_{(\boldsymbol{x},\boldsymbol{y})\in\Omega(\boldsymbol{x},\boldsymbol{y})} (\min_{\boldsymbol{c}\in\{r,g,b\}} (\boldsymbol{I}_l^c(\boldsymbol{x},\boldsymbol{y}))), \quad (12)$$

where  $\alpha$  denotes a weight factor that controls the residual haze. The range of  $\alpha$  is  $0 < \alpha < 1$ , and the recommended value is 0.95.

Similar to the basic scene depth estimation  $d_b(x, y)$ ,  $\tilde{t}(x, y)$ also has the disadvantage of insufficient details. Therefore,  $\tilde{t}(x, y)$  is also filtered by a guided filter, and G is used as the guide image to obtain an improved estimate of the transmission map  $t_2(x, y)$ , i.e.,  $t_2(x, y) = F_g(G, \tilde{t}(x, y))$ . Furthermore, the same guide image G is used for filtering  $t_2(x, y)$  and  $d_g(x, y)$  to minimize inconsistencies in the details of the two transmission maps estimated by the two priors.

The two transmission maps  $t_1(x, y)$  and  $t_2(x, y)$  are fused using Eq. (13) to obtain the final transmission map t(x, y). In Eq. (13),  $\mu$  represents the balance factor that determines the contribution of each transmission map to the final transmission map t(x, y). The value range of  $\mu$  is the interval [0,1].

$$t(x, y) = \mu \cdot t_1(x, y) + (1 - \mu) \cdot t_2(x, y),$$
(13)

#### D. HAZE-FREE LOW-FREQUENCY SUB-BAND RECOVERY

If *A* and t(x, y) are known, the value range of t(x, y) is limited to [0.05, 1.0] to eliminate the very low and very high grey values in the low-frequency sub-bands of the haze-free image. Thus, the low-frequency sub-bands of the haze-free image are obtained by Eq. (14). Let  $\hat{C}_l = I_{ld}$ , i.e., the dehazed low-frequency sub-bands are regarded as the low-frequency sub-bands of  $J_l$ .

$$I_{ld}(x, y) = \frac{I_l(x, y) - A}{\min(\max(t(x, y), 0.05), 1.0)} + A, \quad (14)$$

#### E. NOISE SUPPRESSION AND HIGH-FREQUENCY DETAIL ENHANCEMENT

According to Eq. (1), the remaining task after removing haze from  $I_l$  is to remove noise from  $I_h$  and obtain the high-frequency component of  $J_h$ . First, the high-frequency sub-bands  $\{C_{h,j,s}^c, j = 1, 2, ..., L, s = 1, 2, ..., S_j\}$  need be shrunk to remove or suppress noise in the hazy image. Then, the high-frequency sub-bands after threshold shrinkage are compensated for the difference relative to  $C_l^c$  according to the transmission map.

Threshold shrinkage is a classic noise suppression method. When a hard threshold function is used to remove noise, the denoised image has a relatively high peak signal-to-noise ratio, and the edges are emphasized.

A hard threshold function is used for noise suppression in the high-frequency sub-bands to reduce the loss of details in the dehazed image. The hard threshold function is defined in Eq. (15):

$$\tilde{\boldsymbol{C}}_{h,j,s}^{c} = \begin{cases} \boldsymbol{C}_{h,j,s}^{c}, & \left| \boldsymbol{C}_{h,j,s}^{c} \right| > k_{j}T_{j,s}\sigma^{c}, \\ 0, & otherwise, \end{cases}$$

$$j \in 1, 2, \dots, L, \quad s \in S_{j}, \ c \in \{r, g, b\}$$
(15)

where  $k_j$  denotes threshold scale coefficient of the *j*th decomposition scale.  $T_{j,s}$  represents the frequency-domain root mean square of the high-frequency sub-bands, which calculated using Eq. (16).  $\sigma^c$  denotes the noise variance of the channels of the hazy image, and the other symbols have the same meaning as in Eq. (2).

$$T_{j,s} = \sqrt{\frac{\sum\limits_{m=1}^{M} \sum\limits_{n=1}^{N} |\mathcal{F}(\boldsymbol{C}_{j,s}^{M_z})|^2}{M \times N}},$$
(16)

where  $M_Z$  is an M × N matrix with the same number of rows and columns as  $I^c(x, y)$ ; the values are defined in Eq. (17).  $C_{j,s}^{M_Z}$  denotes the decomposition sub-bands of  $M_Z$ , which are decomposed by the NSCT. The same parameters (scale and direction filter number) as in the decomposed  $I^c(x, y)$  are used.  $\mathcal{F}()$  and  $|\cdot|$  denote the two-dimensional Fourier transform (FT) and the absolute value operator, respectively.

$$M_Z(m,n) = \begin{cases} 1, & m = M/2, n = N/2 \\ 0, & otherwise \end{cases}$$
, (17)

 $\sigma^{c}$  is calculated by the empirical formula of the wavelet noise estimation (Eq. (18)), where *med*() refers to the median operator,  $|\cdot|$  denotes the absolute value operator, and  $W_{d1}^{c}$  denotes the diagonal high-frequency coefficient that is obtained using single-scale "sym8" wavelet decomposition of  $I^{c}(x, y)$ .

$$\sigma^{c} = \frac{med(|\mathbf{W}_{d1}^{c}|)}{0.6745}, \quad c \in \{r, g, b\},$$
(18)

After the shrunk high-frequency sub-bands  $\tilde{C}_{h,j,s}^c$  have been obtained, details enhancement is performed using Eq. (19) according to the transmission map t(x, y) to compensate for the attenuation of  $\tilde{C}_{h,j,s}^c$  relative to  $C_l^c$ .

$$\hat{\boldsymbol{C}}_{h,j,s}^{c} = \frac{\tilde{\boldsymbol{C}}_{h,j,s}^{c}}{\min(\max(\boldsymbol{t}(x, y), 0.1), 0.9)}, \quad c \in \{r, g, b\}, \quad (19)$$

where  $\hat{C}_{h,i,s}^{c}$  denotes the enhanced high-frequency sub-bands.

#### F. RECONSTRUCTION OF THE DEHAZED IMAGE

After performing low-frequency haze removal, high-frequency noise suppression, and high-frequency details enhancement, the noise- and haze-suppressed image  $I_d$  is obtained by applying the nonsubsampled contourlet inverse

transformation. For convenience of expression, the symbol  $T_{NSCT}^{-1}$  denotes the nonsubsampled contourlet inverse transformation; this process is defined in Eq. (20).

$$\mathbf{I}_{d} = T_{NSCT}^{-1} \left( \left\{ \hat{\boldsymbol{C}}_{l}^{c}, \hat{\boldsymbol{C}}_{h,j,s}^{c}, j = 1, 2, \dots, L, s = 1, 2, \dots, S_{j} \right\} \right), \\
c \in \{r, g, b\}$$
(20)

After the dehazed image  $I_d$  has been reconstructed, a Gamma correction is performed to increase the grey values of low-brightness pixels. The gamma correction transform is defined as:

$$\boldsymbol{I}_{\mathrm{d},\mathrm{g}} = (\boldsymbol{I}_{\mathrm{d}})^{\gamma},\tag{21}$$

where the range of  $\gamma$  is  $0 < \gamma \le 1$ ; a value of 0.8 is used in this study.

#### **III. IMPLEMENTATION OF THE HRNSCT ALGORITHM**

The HRNSCT algorithm includes four steps. First, the nonsubsampled contourlet decomposes the hazy image. Second, in the contourlet domain, the CAP and DCP are used to estimate the transmission map and atmospheric light and obtain the haze-free low-frequency sub-bands. The high-frequency sub-bands of the hazy image are shrunk in the contourlet domain for noise suppression, followed by the enhancement of these sub-bands according to the transmission map. Finally, the nonsubsampled contourlet inverse transform is performed to reconstruct the haze-free image in the RGB space, and the Gamma correction is applied to brighten the dark areas.

The details of the HRNSCT are defined in Algorithm 1.

Algorithm 1 Image Haze Removal Algorithm Based on Non
subsampled Contourlet Transform
Input: Hazy color image <i>I</i>
Initialization: Assign values to all parameters
<b>Step 1</b> While $c \in \{r, g, b\}$ , do
1. Decompose $I^c$ using NSCT
<b>Step 2</b> 1. Compute $t_1(x, y)$ and $t_2(x, y)$
2. Obtain the dehazed low-frequency image $I_{ld}(x, y)$
<b>Step 3</b> 1. Compute $\sigma^c$ and $\hat{\sigma}_{i,s}$
2. Reduce $C_{h is}^c$
3. Obtain the enhanced high-frequency sub-band
$\hat{C}^c_{h,j,s}$
<b>Step 4</b> 1. Reconstruct the dehazed image $I_d$ using $\hat{C}_l^c$ , $\hat{C}_{h_i}^c$
2. Correct $I_d$ using gamma correction
End

**Output:** Dehazed image  $I_{d,g}$ 

#### **IV. NUMERICAL EXPERIMENTS**

An edge quality metric is often used in image fusion [41]. In this study, the ratio of the increased number of visible edges in the dehazed image to visible edges of the original image  $R_{ve}$ , the mean visibility level  $M_{vl}$  [42], and the noise variance  $N_v$  are used to evaluate the dehazed images of hazy images without or with low-density noise. In contrast, the noise variance, i.e., the natural image quality evaluator (NIQE) [43],

and the structural similarity index measure (SSIM) are used to evaluate the dehazed images of hazy images with highdensity noise.

The noise variance is calculated using the empirical formula of wavelet noise (Eq. (18)).  $R_{ve}$  and  $M_{vl}$  are defined in Eq. (22) and Eq. (23), and the SSIM is defined in Eq. (24).

$$R_{\rm ve} = \frac{n_r - n_0}{n_0}, \qquad (22)$$
$$M_{\rm vl} = \exp\left(\frac{1}{n_r} \sum_{i \in \wp_r} \log r_i\right), \qquad (23)$$

where  $n_r$  and  $n_0$  denote the number of visible edges in the dehazed image and the original hazy image.  $r_i$  is the gradient ratio of the dehazed image and the original hazy image.  $\wp_r$  represents the number of visible edges in the dehazed image.

$$SSIM(x, y) = \frac{(2\mu_x\mu_y + C_1)(2\sigma_{xy} + C_2)}{(\mu_x^2 + \mu_y^2 + C_1)(\sigma_x^2 + \sigma_y^2 + C_2)},$$
 (24)

where *x* and *y* are the reference image and comparison image,  $\mu_x$  and  $\mu_y$  denote the mean values of *x* and *y*, respectively,  $\sigma_x$  and  $\sigma_y$  refer to the variances of *x* and *y*, respectively,  $\sigma_{xy}$ represents the covariances of *x* and *y*, respectively,  $C_1$  and  $C_2$  are constants to avoid a zero denominator, where  $C_1 = (K_1L)^2$  and  $C_2 = (K_2L)^2$ ; *L* is the range of grey values. In this study, L = 255,  $K_1 = 0.01$ , and  $K_2 = 0.03$ .

All the codes are implemented in Matlab R2014b, and the experiments are conducted on a PC running Windows 10 with 16 G of RAM and a 2.7 GHz i7 CPU.

In the experiment, hazy images were selected from the image sets in [4], [21], FRIDA [44], O-HAZE [45], I-HAZE [45], [46], and [47], and the other hazy imagesare selected from real hazy images.

Three types of experiments were conducted to verify the performance of low-frequency dehazing, high-frequency noise reduction, and comprehensive performance for dehazing and noise reduction of HRNSCT.

#### A. LOW-FREQUENCY DEHAZING

In the experiment, the low-frequency dehazing performance is evaluated visually and using objective indicators. The parameters of the HRNSCT are as follows: the scale of the NSCT decomposition image is 3; the number of directional filter banks corresponding to each scale is 2, 4, and 8;  $\lambda =$ 0.015, r = 15,  $\beta = 2.2$ ,  $\mu = 0.5$ ,  $k_j = [0 \ 3 \ 3 \ 4]$ , and  $\gamma = 0.6$ .

A comparison of the original and dehazed images T1-T3 is shown in Figure 4. The results of the evaluation indicators are shown in Figure 5.

Figure 4 shows that the HRNSCT significantly reduces the amount of haze in the images. In the dehazed images, the amount of residual haze is greater in the distant areas than nearby. However, most areas are haze-free and show no halos. The results indicate that it is feasible to achieve haze removal in the image by removing haze only in the low-frequency domain.



(b) Dehazed images

**FIGURE 4.** Results of haze removal by the HRNSCT in the low-frequency domain. (a) Original hazy images; (b) dehazed images.



**FIGURE 5.** Results of the evaluation indicators of the dehazed images. (a) Comparisons of  $N_V$  in the original and dehazed images; (b)  $R_{Ve}$  and  $M_{VI}$ .

As shown in Fig. 5 (a), the noise variance of the dehazed images T1 and T3 is lower than that of the original images, however, that of dehazed image T2 is slightly higher than that of T2, but that of dehazed image T2 is less 0.9. The result shows that the HRNSCT does not result in significant noise diffusion or amplification during haze removal.

Figure 5 (b) shows that the  $R_{ve}$  of the dehazed images is greater than 1, indicating that the number of visible edges in



FIGURE 6. Noise variance of original and dehazed images.



(b) Dehazed images

**FIGURE 7.** Dehazing results for hazy images with different noise level. (a) Original hazy images with different noise levels; (b) dehazed images.

the dehazed images is more than twice that of the original hazy images. The visibility indicator  $M_{vl}$  is greater than 1, showing a significant increase in the contrast of the dehazed image.

The results in Figures 4 and 5 demonstrate that the HRN-SCT algorithm achieves excellent haze removal performance only by removing the haze from the low-frequency sub-bands.

#### **B. HIGH-FREQUENCY NOISE SUPPRESSION**

The objective of this experiment was to verify that the HRNSCT can decouple the haze removal and noise suppression in the contourlet transform domain. The HRNSCT was applied to remove haze of 60 hazy images with different Gaussian noise.

The noise variance of the original and dehazed images is shown in Figure 6.

The noise variances of the dehazed images and the original hazy images are considerably different. Those of the dehazed images are close to 1. The results indicate that the shrink of the high-frequency directional sub-bands of the original hazy images successfully suppresses the noise in the dehazed images.

The original images T61 and T62 with different noise levels and the dehazed images are shown in Figure 7. The

#### TABLE 1. Results of the evaluation indicators for the T70 image.

Algorithm	Image	Original $N_v$	$N_{v}$ ( $\downarrow$ )	$R_{ m ve}$ ( $\uparrow$ )	$M_{ m vl}$ ( $\uparrow$ )
HRCAP	T70	0.51	0.69	2.01	1.07
DehazeNet			0.54	1.02	1.18
AMEF			1.16	1.83	1.92
DHGC			1.08	2.24	1.81
DHMP			1.12	1.66	1.33
MSW			0.64	2.01	1.67
HRNSCT			<u>0.48</u>	2.03	1.83

TABLE 2. Results of the evaluation indicators for the T71 image.

Algorithm	Image	Original $N_v$	$N_{v}$ $(\downarrow)$	$R_{ m ve}$ ( $\uparrow$ )	$M_{ m vl}$ ( $\uparrow$ )
HRCAP	T71	0.12	<u>0.19</u>	4.62	1.58
DehazeNet			<u>0.19</u>	4.32	1.62
AMEF			0.31	4.76	2.22
DHGC			0.30	6.59	2.42
DHMP			0.49	4.77	1.99
MSW			0.24	5.87	2.35
HRNSCT			<u>0.19</u>	5.18	2.50

enlargements of the dehazed images show that more detail is lost, and the edges become less clear as the noise variance increases. The reason is that the noise conceals the details in the original hazy images, making it impossible to restore these details at a high noise variance.

Figures 4 to 7 indicate that the HRNSCT algorithm achieves the decoupling of the haze removal and noise suppression by removing haze from the low-frequency sub-bands and suppressing noise in the high-frequency sub-bands.

#### C. COMPREHENSIVE PERFORMANCE VERIFICATION OF THE HRNSCT

The HRNSCT, HRCAP [21], DehazeNet (deep learning method) [27], AMEF [48], DHGC [49], DHMP [50], and MSW [51] are used to dehaze the test images, and the performances of the seven algorithms are compared using visual evaluations and the objective indicators.

The dehazing results of the seven algorithms for the lownoise hazy images T69 and T70 and the composite noisefree hazy image T71 are shown in Figure 8. T69 has dense haze; thus, the denominator in the indicator  $R_{ve}$  (the number of visible edges  $n_0$  in the original hazy image) approaches zero. Therefore, the dehazing results of the 7 algorithms for T69 are only evaluated visually.

The results of the evaluation indicators of the dehazed image T71 are listed in Table 1, and those of T72 are listed in Table 2.

The results in Fig. 8 show that all seven algorithms provide good dehazing performance for removing light haze or medium haze. However, there are great significant performance differences for removing dense haze.

As shown in Fig. 8 (a), HRCAP, DehazeNet, and AMEF provide low performance for removing dense haze. The DHMP results in color distortion, the DHGC causes spots,



(c)T71.

FIGURE 8. Haze removal results for hazy images with low noise. (a) T69; (b) T70; (c) T71.

and the dehazing result of MSW shows striping. The HRN-SCT provides the best dehazing performance.

In Figure 8(b), the overall brightness of the dehazed images obtained from the HRCAP, DHGC, and MSW is low, and there are several dark areas. The performances of the DehazeNet, AMEF, DHMP, and HRNSCT are similar. However, the enlargement shows that the images obtained from the AMEF and HRNSCT have more detail than those of the other algorithms. Therefore, the AMEF and HRNSCT provide the best dehazing performances for T70.

A shown in Figure 8(c), the DHGC provides the best dehazing performance for T71; however, the results obtained from the HRNSCT and the other five algorithms are almost indistinguishable visually.

In Tables 1 and 2, 'Original  $N_v$ ' denotes the noise variance of the original hazy images.  $N_v$ ,  $R_{ve}$ , and  $M_{vl}$  denote the evaluation indicators of the dehazed images. The bold underlined numbers represent the optimal values. The  $\downarrow$  symbol indicates that the smaller the value, the better the result is, and vice versa for the  $\uparrow$  symbol.

Table 1 shows that the  $N_v$  value of the HRNSCT algorithm is optimal, indicating that the noise level of the dehazed image obtained from the HRNSCT was the lowest. HRN-SCT achieved the optimal results for all indicators for a comparison with HRCAP, DehazeNet, DHMP, and MSW. Comparing with AMEF and DHGC, the  $N_v$  and  $R_{ve}$  values of the HRNSCT were better than those of the AMEF, and the  $N_v$ and  $M_{vl}$  values of the HRNSCT were better than those of the DHGC. Therefore, the dehazing performance of HRNSCT is better than that of the other six algorithms for T70.

As shown in Table 2, the  $N_v$  values of the HRCAP, DehazeNet, and HRNSCT algorithms were optimal and identical. The  $R_{ve}$  and  $M_{vl}$  values of the HRNSCT algorithm were better than those of the HRCAP, DehazeNet, AMEF, and DHMP. The  $N_v$  and  $M_{vl}$  values of the HRNSCT algorithm were better than those of the DHGC and MSW. Therefore, comparing the other six algorithms, the dehazing performance of HRNSCT is better than that of the other six algorithms for T71.

The results in Figure 8 and Tables 1 and 2 demonstrate that the proposed HRNSCT algorithm has similar dehazing performance to the DHGC and MSW algorithms for haze removal from images with low or no noise.

Subsequently, to further verify the performances of HRN-SCT and the other algorithms for removing haze from noisy images, the seven algorithms were used to remove haze from hazy images T72, T73, and T90 with Gaussian noise. The dehazing results of the seven algorithms are shown in Figure 9.

In Figure 9, comparing with the original hazy images, dehazing effects of all dehazing images of T72, T73 and T90 are obvious. However, the enlargements show that the HRCAP, DehazeNet, AMEF, DHGC, and DHMP result in noise amplification during haze removal from noisy images.

The MSW and HRNSCT algorithms provide the best noise suppression performance. However, the MSW algorithm produces spots in the dehazed images. Hence, the visual comparison of the dehazed images of the 7 algorithms indicates that the HRNSCT algorithm provides the best performance for removing haze from noisy images.

Because the  $R_{ve}$  and  $M_{vl}$  indicators are sensitive to noise, the noise variance  $N_v$ , the SSIM and NIQE are used to evaluate the dehazing image. The evaluation indicators of the dehazing images T72, T73, and T90 are shown in Figure 10.

In Figure 10(a), the smaller the  $N_v$  value, the lower the noise level of the dehazed image is. The  $N_v$  values of the dehazed images obtained from the HRCAP, DehazeNet, AMEF, DHGC, and DHMP algorithms were larger than those of the original images, indicating that these five algorithms increase the noise variance. In contrast, the  $N_v$  values of the dehazed images obtained from the MSW and HRNSCT algorithms were reduced. The  $N_v$  value was lowest for the



variance Voise ' HRCAP DehazeNet HRNSCT DHMP DHGC MSW AME Origir (a)  $N_v$  values Comparisons of SSIM of different haze removal images 0.8 0.′ 0.6 0 SSIM(† 0.40 3 0.2 0. HRCAP HRNSCT AMER DHGC DHMP MSW Origine (b) SSIM values Comparisons of NIQE of different haze removal images 12 T73 10 NIQE(L) HRCAP DehazeNet DHMP Original HRNSCT AMER DHGC MSW

Comparisons of noise variance of different haze removal images

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FIGURE 9. Haze removal results for hazy images with noise. (a) T72; (b) T73; (c) T90.

HRNSCT. These results indicate that the HRNSCT algorithm provides the best noise suppression performance, followed by the MSW.

In Figure 10(b), the larger the SSIM value, the higher the similarity is between the original image and the dehazed image. The SSIM values are lower for the dehazed images than the original images for the six algorithms, whereas those of the HRNSCT are higher in the dehazed images. This finding indicates that the HRNSCT algorithm causes the least image distortion among the seven dehazing algorithms.

In Figure 10(c), the smaller the NIQE value, the better the image quality is. The NIQE values are higher for the dehazed images than the original images for the five algorithms, whereas those of the MSW and HRNSCT are lower. This result shows that the MSW and HRNSCT algorithms increase the image quality after dehazing, whereas the other five algorithms decrease the image quality during the haze removal from noisy images. The HRNSCT provides the low-

(c) NIQE values.

FIGURE 10. Results of the evaluation indicators for different algorithms

and different images. (a) N<sub>V</sub>; (b) SSIM. (c) NIQE.

est NIQE values, demonstrating that it provides the best haze removal performance for the T71, T73, and T90 hazy images with noise.

The results presented in Figures 9 and 10 show the superiority of the HRNSCT over the other algorithms for removing haze from noisy images.

The computational complexity of the HRNSCT depends primarily on the NSP and NSDFB of the NSCT. The NSDFB comprises a larger proportion of the NSCT operation than the NSP. Therefore, the HRNSCT has the same computational complexity as the NSDFB and a computational complexity of  $O(n^2)$  for the NSDFB for an image of size  $n \times n$ . Hence, the computational complexity of the HRNSCT is  $O(n^2)$  for each channel of the color image.

The average runtimes of the seven algorithms for dehazing 60 hazy images with an average size of  $512 \times 480$  are shown in Figure 11.



FIGURE 11. Comparison of the runtimes of the seven haze removal algorithms.



**FIGURE 12.** Dehazing results for different  $\mu$  values.

The order of the average runtime of the 7 algorithms is MSW < HRCAP < DHGC < AMEF < DHMP <DehazeNet < HRNSCT. The HRNSCT has the longest average runtime because it is implemented in the Matlab environment. The HRNSCT algorithm can be improved by increasing its processing speed using program optimization or GPU hardware acceleration in practical applications.

#### V. PARAMETER ANALYSIS AND DISCUSSION

The proposed HRNSCT algorithm provides the best dehazing and noise reduction performances in comparison with comparable algorithms. We analyze the role of the main parameters of the HRNSCT algorithm in the following section. The parameter  $\alpha$  plays a role in preserving the haze in the DCP estimation of the transmission map. The balance factor  $\mu$  controls the contribution of the CAP and DCP to the final transmission map. The parameter  $\gamma$  makes the role of improvement low grey value pixels and compression high grey value pixels. Threshold proportional coefficient  $k_i$  plays a role in setting the threshold. The larger the  $k_i$ , the stronger the noise suppression effect. Nonetheless, if  $k_i$  is large, which will lead to the loss of weak details. The recommended range of  $k_i$  is [4,6] when the noise variance of the hazy image is less than 2, other recommended ranges are [2,4]. The details of these parameters are not repeated here. The following focuses on analyzing the roles of the balance factor  $\mu$  and the atmospheric attenuation coefficient  $\beta$ .

Figure 12 shows the results of using different  $\mu$  values for haze removal from image T91 (from the O-HAZE dataset).

The dehazed image becomes brighter as the  $\mu$  value increases, but the residual haze increases, indicating that the



FIGURE 13. Evaluation indicators of images dehazed with different  $\mu$  values.



**FIGURE 14.** Haze removal results of T4 for different  $\beta$  values.

smaller the value of  $\mu$ , the stronger the impact of the DCP and the weaker the impact of the CAP in the transmission map.

The evaluation indicators of images dehazed with different  $\mu$  values are provided in Figure 13.

As the  $\mu$  value increases,  $N_v$  decreases, and the rate of increase decreases, with few changes after reaching a  $\mu$  value of 0.5. The NIQE shows a similar trend, exhibiting few changes after reaching a  $\mu$  value of 0.8. The SSIM value increases with an increase in the  $\mu$  value and stabilizes after reaching a  $\mu$  value of 0.5.

The visual evaluation and the evaluation indicators suggest that the optimal  $\mu$  value range is [05,0.8].

Figure 14 shows the haze removal results of image T74 for  $\mu = 0.5$  and different  $\beta$  values.

As the  $\beta$  value increases, the dehazing performance of the HRNSCT and the clarify of the images increases. However, a very large  $\beta$  value will darken the images. Therefore, the visual quality of the dehazed image should be considered comprehensively when the parameter values are changed. The experiment results show that the suitable range of the  $\beta$  value is [0.8,2.2].

#### **VI. CONCLUSION**

The HRNSCT algorithm was proposed for haze removal from noisy images. Based on theoretical analyses and numerical experiments, the following conclusions can be drawn.

The HRNSCT algorithm has excellent noise- and hazesuppression performance, only by dehazing the lowfrequency sub-bands and shrinking the high-frequency subbands of the original image. The HRNSCT algorithm decouples the haze removal and noise suppression processes in the contourlet transform domain. This approach prevents the noise amplification caused by traditional dehazing algorithms during the haze removal process. Since most hazy images include noise, the HRNSCT algorithm is well suited for dehazing noisy images. Although the HRNSCT algorithm provided excellent results for simultaneous haze removal and noise suppression, it currently has a relatively long runtime. Thus, it is necessary to optimize and accelerate the HRNSCT algorithm in the future. Alternatively, similar algorithms based on deep learning should be developed and designed along with the idea of decoupling haze removal and noise suppression of the HRNSCT algorithm.

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**BOWEN ZHANG** was born in Jiaozuo, China. He is currently pursuing the bachelor's degree with the School of Computer Science and Engineering, Nanjing University of Science and Technology. He has published a number of articles in image processing journals. His research interests include image dehazing and image enhancement.



**MANLI WANG** was born in Jiaozuo, China, in 1981. He received the B.S. degree in electrical engineering and automation, the M.S. degree in control theory and control engineering from Henan Polytechnic University, and the Ph.D. degree from the School of Mechanical Electronic and Information Engineering, China University of Mining and Technology, Beijing, China, in 2020. He has published a number of articles in image processing journals. His research interests include image

denoising and image enhancement.



**XIAOBO SHEN** received the B.Sc. and Ph.D. degrees from the School of Computer Science and Engineering, Nanjing University of Science and Technology, in 2011 and 2017, respectively. He is currently a Full Professor with the School of Computer Science and Engineering, Nanjing University of Science and Technology, China. He has authored over 30 technical papers in prominent journals and conferences, such as IEEE TRANSACTIONS ON NEURAL NETWORKS AND LEARNING

SYSTEMS, IEEE TRANSACTIONS ON IMAGE PROCESSING, IEEE TRANSACTIONS ON CYBERNETICS, NIPS, ACM MM, AAAI, and IJCAI. His primary research interests include multi-view learning, multi-label learning, network embedding, and hashing.