# Frame-Based Multiple-Description Video Coding with Extended Orthogonal Filter Banks

#### R. Bernardini,<sup>1</sup> M. Durigon,<sup>1</sup> R. Rinaldo,<sup>1</sup> A. Vitali,<sup>2</sup> and P. Zontone<sup>1</sup>

 <sup>1</sup> Dipartimento di Ingegneria Elettrica, Gestionale e Meccanica, Università degli Studi di Udine, via delle Scienze 208, 33100 Udine, Italy
 <sup>2</sup> ST Microelectronics, via C. Olivetti 2, 20041 Agrate Brianza, Italy

Received 4 August 2004; Revised 20 December 2004; Accepted 21 February 2005

We propose a frame-based multiple-description video coder. The analysis filter bank is the extension of an orthogonal filter bank which computes the spatial polyphase components of the original video frames. The output of the filter bank is a set of video sequences which can be compressed with a standard coder. The filter bank design is carried out by taking into account two important requirements for video coding, namely, the fact that the dual synthesis filter bank is FIR, and that loss recovery does not enhance the quantization error. We give explicit results about the required properties of the redundant channel filter and the reconstruction error bounds in case of packet errors. We show that the proposed scheme has good error robustness to losses and good performance, both in terms of objective and visual quality, when compared to single description and other multiple description video coders based on spatial subsampling. PSNR gains of 5 dB or more are typical for packet loss probability as low as 5%.

Copyright © 2006 Hindawi Publishing Corporation. All rights reserved.

#### 1. INTRODUCTION

Robust transmission of multimedia streams over error-prone packet networks has become an important issue in many scenarios, including wireless communications and distributed networking. In such applications, the usual approach of error recognition and packet retransmission may not be appropriate, because of the excessive delay caused by this technique. Moreover, a return channel may not exist or be inconvenient to use in applications with low-power simplified receivers. The use of error-correcting codes at the packet level is not useful when packets are lost because of congestion or delay, or when one of the different paths used for the packets, as in layered coding, totally fails. Recently, forward error correction (FEC) coding across packets has been suggested for robust transmission in the presence of packet losses [1]. In its simpler implementation, this technique consists in grouping N consecutive packets produced by the coder and in adding M - N "parity-check" packets, calculated by means of a block coder (e.g., a Reed-Solomon coder) applied across the N packets on a symbol-by-symbol basis. It has been noticed that this technique has a quick performance drop as soon as the packet loss rate exceeds the error recovery capability of the code. This is due to the fact that when error correction is not possible, the received information is totally useless [2].

Multiple description (MD) coding is a recently proposed solution, where a set of correlated, equally important descriptions of the source are generated at the coder and sent over independent channels [2]. Ideally, each of the descriptions should allow for a reasonable reconstruction of the source, permitting an increased quality as the number of received descriptions increases. Therefore, unlike the case of error-correcting codes, each piece of received information can be useful to increase the reconstruction quality. The requirement that each description is "good by itself" can be achieved by adding correlation, at the expense of a decrease in the overall rate-distortion performance.

Many approaches have been proposed to design MD coders that use different strategies for coding different data sources. MD coding comprises a very wide range of techniques such as MD scalar quantization [3], pairwise correlating transforms [4], spatial and temporal downsampling [5], correlating filter banks or frames [6], and matching pursuit algorithms [7]. Such approaches differ in terms of overall rate-distortion performance and complexity. For a more complete overview of MD techniques see, for example, the introductory paper [2] and references within.

A technique for MD of video in the spatial domain is presented in [8]. Each video frame is downsampled in order to create several descriptions of the source ([5] presents a similar technique for still images). Each video subsequence is then independently coded with the H.263 coder. A mechanism for changing the amount of redundancy among the descriptions is reported in [5]. An adaptive procedure for spatial and temporal downsampling is in [9]. The technique proposed in [8] is attractive because it allows for the use of a standard video codec on individual descriptions. Moreover, it offers compatibility with non-MD receivers and good error resilience, because missing information can be interpolated from the received one. Even in the case when only one description is received, the reconstruction quality can be acceptable. Any loss in the received streams, however, has to be appropriately recovered by *approximate* concealment techniques.

In this paper, we propose an MD video coding scheme where two descriptions are obtained by spatial polyphase subsampling in the column direction, and a third description is obtained by lowpass filtering the columns of the original video frames, followed by subsampling. Each of the descriptions is coded with an H.264 coder [10], the international standard currently vying to replace MPEG-2 for widespread technologies such as digital television, Internet streaming video, and DVD-Video [11]. We therefore extend the approach of [5, 8] by adding a visually consistent "paritycheck" image. As a matter of fact, this MD generating procedure can be interpreted within the framework of overcomplete bases expansion (frames) [6]. Frame expansions [6] permit exact reconstruction of lost information even in the presence of data losses, at the expense of added redundancy. General theorems of frame theory claim that the original signal can be obtained by linearly combining a set of suitable signals (such a set is known as the *dual frame*), using as coefficients the outputs of the analysis filter bank. In case of coefficient losses, however, the dual functions depend on the loss pattern and have to be computed at the receiver [12, 13].

The proposed approach combines the advantages of the MD schemes of [5, 8] with the error recovery capability provided by frame expansions. Error recovery can in fact be done exactly, similarly to what happens with FEC coding, when losses are not too numerous, that is, when the analysis basis after losses is still a complete system. It differs from FEC in that redundancy is added at the signal level, and that the dual functions after losses may cause some amplification of the quantization error, even if the overall system was designed to achieve perfect reconstruction. Moreover, even if losses are so numerous that the system becomes incomplete, one can resort to using the source implicit redundancy, as in [5, 8], and reconstruct the signal with good fidelity. The price to pay is the cost of the additional parity-check video sequence. The experimental results show that the proposed scheme is indeed competitive for relatively high bit rates and loss probability.

Toward the design of the proposed scheme, we derive some general theoretical results. First, we show how to construct redundant FIR filter banks by adding a redundant channel to a generic orthogonal filter bank, while preserving FIR reconstruction. Since the spatial polyphase subsampling we consider in the proposed MD video coding scheme is just a very special case of an orthogonal filter bank, we can use this result for the design of the redundant channel filter. On the other hand, since orthogonal filter banks are ubiquitously used in subband and transform coding, the results we present in this paper can be used for the extension of other available schemes. We then consider the general problem of quantization error enhancement due to the use of nonorthogonal bases expansions. This problem cannot be avoided in overcomplete frame expansions in the presence of coefficient losses. We give explicit results on error bounds and derive criteria for filter bank design to mitigate the effect.

We compare the performance of the proposed solution with that of two MD coding schemes based on spatial subsampling. In particular, one of the schemes produces four descriptions based on the four spatial polyphase components of the original frame, while the second scheme is similar to the one we propose here and considers even and odd rows separation. Bilinear interpolation from correctly received frames is again used for error concealment. Note that, unlike the case of frame-based analysis, "exact" error recovery is never possible in the latter two systems in the presence of packet losses. In all schemes, individual descriptions are coded using independent H.264/AVC video coders. After error recovery or concealment, frames are copied onto the decoders' frame buffers at the receiver, in order to mitigate the effect of error propagation due to differential coding.

The organization of the paper is as follows. Section 2 recalls some basic tools and the notation used in this paper. In Section 3 we describe in some detail the proposed MD video codec. In Section 4 we present some experimental results evaluating the rate-distortion performance of the proposed scheme, comparing it with the other two MD schemes and with standard single-description (SD) coding. Section 5 draws the conclusions.

#### 2. FRAMES AND FILTER BANKS

In this section, we briefly recall some results of frame theory which will be used in this paper [14].

A family of signals  $\Phi = \{\phi_k \in \ell^2(\mathbb{Z})\}_{k \in \mathbb{Z}}$  constitutes a frame if for any signal  $x \in \ell^2(\mathbb{Z})$  there exist two constants 0 < A and  $B < \infty$  such that

$$A\|x\|^{2} \leq \sum_{k \in \mathbb{Z}} |\langle x, \phi_{k} \rangle|^{2} \leq B\|x\|^{2},$$
(1)

where  $\langle f, g \rangle = \sum_{n} f(n)g^{*}(n)$  is the scalar product between f and g. Linear function  $F : \ell^{2}(\mathbb{Z}) \to \ell^{2}(\mathbb{Z})$  defined as

$$y_k = (Fx)_k \triangleq \langle x, \phi_k \rangle \tag{2}$$

maps *x* into the corresponding sequence of scalar products and it is known as the *frame (or analysis) operator* associated with  $\Phi$ . The left-hand inequality in (1) guarantees that it is possible to reconstruct the original signal *x* from the scalar products  $y = \{y_k\}_{k \in \mathbb{Z}}$  and that it is possible to compute a set of *dual* signals  $\tilde{\phi}_k$  such that

$$x = F^{\dagger} y = \sum_{k \in \mathbb{Z}} y_k \widetilde{\phi}_k.$$
(3)



FIGURE 1: Block diagram of the proposed frame-based MD coder.

The operator  $F^{\dagger}$  is called the *dual* or *pseudoinverse* operator of *F*. Moreover, the left-hand inequality in (1) grants for a *robust* reconstruction, in the sense that if  $\hat{y} = y + \epsilon$  is a noisy version of *y* and  $\hat{x} = F^{\dagger}\hat{y} = \sum_{k \in \mathbb{Z}} \hat{y}_k \tilde{\phi}_k$  is the reconstructed signal, then

$$\|x - \hat{x}\|^2 \le \frac{\|\epsilon\|^2}{A},\tag{4}$$

that is, coefficient error is not amplified more than 1/*A*. In addition, reconstruction via  $F^{\dagger}$  is optimal, in the sense that  $\hat{x} = F^{\dagger} \hat{y}$  minimizes  $||F\hat{x} - \hat{y}||$  [15].

Suppose that during the transmission some coefficients  $y_k$  are lost and let I be the set of the indexes of the lost coefficients and let  $y_{I^c}$  be the sequence of received coefficients. If subset  $\Phi_I \triangleq \{\phi_k, k \notin I\}$  is still a frame, one can recover x by "pretending" that it was analyzed with subframe  $\Phi_I$ . If  $F_I$  is the frame operator corresponding to  $\Phi_I$ , one can obtain x as  $x = F_I^{\dagger} y_{I^c}$ . Operator  $F_I^{\dagger}$  can be efficiently implemented by means of the algorithm suggested in [12, 13] which expresses  $F_I^{\dagger}$  as  $F_I^{\dagger} = F^{\dagger}R$ , where R is a *restoring operator* which recovers the missing coefficients from the known ones.

In the framework of oversampled filter banks, one computes a vector of output coefficients in each channel j = 1, ..., N, via convolution, that is,

$$y_j(n) = \sum_{m \in \mathbb{Z}} x(m) h_j(Mn - m), \quad j = 0, \dots, N - 1 > M - 1.$$
(5)

The right-hand side of (5) can be interpreted as the scalar product between the input and the analysis vector  $\phi_{Nn+j}(m) \triangleq h_j(Mn - m)$ . By appropriate filter design, the  $\phi_{Nn+j}$  constitute a frame. Oversampling, that is, choosing N > M, implies that there is redundancy in the coefficients  $y_j(n)$  which can be exploited to reconstruct x even if some coefficients are lost. It is possible to show that the dual frame of (5) can be implemented by means of an oversampled synthesis filter bank which will be called the *dual filter bank of* (5) [16]. If both filter bank (5) and its dual are made of FIR filters, we will say that (5) is a *doubly FIR* (DFIR) filter bank. The use of DFIR filter banks is ubiquitous in image and video processing, due to ease of implementation and the problem of signal extension at the borders in the spatial direction when using IIR filters.

Finally, let us introduce some terminology. A filter bank like the one in (5), with *N* channels and sampling factor *M*,

will be called an N/M filter bank. If the first M impulse responses are

$$h_j(n) = \delta(n+j), \quad j = 0, \dots, M-1,$$
 (6)

the first M channels operate a polyphase decomposition of the input signal and we will say that (5) is a *systematic filter bank*, the first M channels are the *systematic channels* and the remaining N - M ones are the *redundant channels*. This nomenclature stems from the fact that, if (6) is true, one can read the samples of signal x by directly looking at the first Mchannels.

#### 3. SYSTEM OVERVIEW

The MD scheme proposed in this paper uses standard H.264/AVC coders on the output of an oversampled filter bank operating in the spatial direction and originating three video subsequences  $y_i$ .

A detailed description of the system is shown in Figure 1. The descriptions are generated using a 3/2 one-dimensional filter bank applied to columns of every sequence frame. The filter outputs are subsampled by a factor 2. Thus, for an  $N_r \times N_c$  input frame, the scheme originates 3 descriptions with dimension  $N_r/2 \times N_c$  pixels.

The descriptions are coded using three independent H.264/AVC standard coders, as shown in Figure 1. Note that the compressed streams have a standard format and this allows non MD-enabled decoder to decode the MD stream by simply keeping one description and discarding the others. This back-compatibility issue can be quite important.

The system structure implies that one must use filters such that sequences  $y_j$  are compressible by the standard coder. For example, since an H.264/AVC coder is used, filters  $h_j$  must not be highpass since the generated sequences would be difficult to code.

For the sake of simplicity, we choose a systematic filter bank, that is,  $h_0(n) = \delta(n)$ ,  $h_1(n) = \delta(n + 1)$ . This actually corresponds to send the even rows to the first channel and the odd rows to the second one. The third filter  $h_2(n)$  is a lowpass filter, designed according to the criterion described in Section 3.1.

The H.264/AVC coder divides the input frame into slices made from macroblocks (MB) organized into rows. Each slice is then sent over the network in a single packet. The reason for subsampling along the columns is that the loss of



FIGURE 2: Block diagram of the proposed decoder.

one slice results in a limited number of contiguous lost coefficients in each column, hopefully permitting error recovery. It is easy to see that the slice organization of H.264/AVC implies that the loss of a single packet gives rise to the loss of a rectangular region in one video frame of a subsequence, whose dimensions is equal to the dimensions of a slice. Since we are applying the filter bank columnwise, a loss of a rectangle of coefficients will look like a loss of  $S_h$  consecutive coefficients, where  $S_h$  is the slice height. In other words, the synthesis filter bank will experience losses in bursts whose length is a multiple of  $S_h$ .

On the receiver side (Figure 2), the video streams are independently processed by H.264/AVC synchronized decoders. In [12, 13], a practical algorithm for dual frame computation with low delay and reduced complexity is presented. The scheme of [12, 13] puts in front of the synthesis block a restoration stage which recovers, whenever possible, the missing coefficients from the received ones, "hiding" the losses from the synthesis filter bank. The decoders are therefore connected to a restoring block R, which recovers channel errors by implementing the algorithm of [12, 13] when  $\Phi_I$  is still a subframe. In this case, the cascade of the restoring procedure with the original dual filter bank is indeed equivalent to the dual of the lossy frame operator  $\Phi_I$ . We remark that this solution needs only local information and does not introduce any relevant delay in the decoding process. Moreover, the computational complexity is reasonable, since it basically requires the inversion of a matrix with dimension corresponding to the number of lost coefficients in a column (see [12, 13] for a detailed discussion). When slices are lost in the same position in two out of three descriptions,  $\Phi_I$ becomes incomplete and missing regions have to be recovered using an approximate concealment technique. In particular, we interpolate one missing systematic channel from the correctly received stream using bilinear interpolation, then feed these two subimages to the usual restoring block.<sup>1</sup> This typically gives acceptable results, due to the high spatial correlation among descriptions in the proposed scheme. In Section 4 we will see a temporal interpolation technique that slightly improves reconstructed video quality in case of incomplete  $\Phi_I$ . Another important aspect in using the H.264

codec is to avoid error propagation due to direct-mode prediction [10]. If a reference frame (e.g., a P frame) is lost, B slices coded in direct mode cannot be decoded, even if the data relative to the B frame are received correctly. The solution we adopt is to mark B blocks as lost when they are coded in direct mode with respect to corrupted reference information, and to treat them as those lost because of channel failures.

The output of the restoring block, with concealment in case of unrecoverable errors followed by application of the algorithm of [12, 13], is a set of three recovered subframes with dimension  $N_r/2 \times N_c$ . These subframes are then fed into the synthesis filter bank, whose output is an approximation of the original full-size sequence. Recovered subframes for each description are copied into the corresponding decoder frame buffer, in order to limit error propagation from reference frames due to interframe coding.

#### 3.1. System design

In order to make the scheme of Figure 1 effective, it is necessary to design the third filter  $h_2$ . As anticipated,  $h_2$  must be a lowpass filter since its output must be a compressible sequence. Moreover,  $h_2$  must be such that the filter bank in Figure 1 is DFIR and such that the lower bound resulting after the loss of one packet is as large as possible.

In this section, we solve this problem by presenting a general analysis and providing results for the solution of the following problems which generalize the problem of designing  $h_2$ .

(1) Given an orthogonal filter bank with M channels, we want to add a redundant channel so that the resulting filter bank is doubly FIR.

(2) We want to design a systematic (M+1)/M DFIR filter bank so that the lower bound of subframe  $\Phi$  resulting after losses is as large as possible. When losses occur, we implicitly analyze the signal with a frame with a smaller lower bound, and this may cause quantization error enhancement according to (4).

In the following we will give a necessary and sufficient condition on the redundant channel filter to result in a doubly FIR filter bank. The second problem is more complex and we will derive lower and upper bounds on the frame bound  $A_I$ , which can be used to limit the overall reconstruction

<sup>&</sup>lt;sup>1</sup> When two channels out of three are received,  $\Phi_I$  is indeed a frame.

error according to (4). The bounds are written as a function of the polyphase components of the (M + 1)th redundant channel filter, so they can be used for the filter choice or design. We take into account the case of *L* consecutive coefficients lost in a channel. This hypothesis derives from the fact that we are considering a framework where coefficients from each channel are grouped into packets, and a packet loss corresponds to a set of consecutive coefficients missing at the receiver.

#### 3.1.1. Doubly FIR filter banks

In detail, we will analyze the following problem.

*Problem 1.* Let  $h_j$ , j = 0, ..., M - 1, be the impulse responses of an orthogonal *M*/*M* FIR filter bank. Find a filter *g* such that the resulting (M + 1)/M filter bank is a doubly FIR filter bank.

The solution to Problem 1 is contained in the following theorem.

**Theorem 1.** Let  $h_j$ , j = 0, ..., M-1, and g be as in Problem 1. The filter bank made of  $h_j$ , j = 0, ..., M-1, and g is doubly FIR if and only if

$$\sum_{n} g(n)g(n-Mk) = \|g\|^2 \delta(k), \quad \forall k \in \mathbb{Z},$$
(7)

that is, if and only if g is orthogonal to its own translations of multiples of M.

*Proof.* Let  $g_k(n) = g(k + nM)$  be the *k*th polyphase component of *g* and let  $G_k(z)$  be its *z*-transform. The polyphase matrix relative to the new filter bank is

$$\mathbf{K}(z) = \begin{bmatrix} \mathbf{H}(z) \\ G_0(z) & G_1(z) \cdots & G_{M-1}(z) \end{bmatrix} = \begin{bmatrix} \mathbf{H}(z) \\ \mathbf{G}^t(z) \end{bmatrix}, \quad (8)$$

where  $\mathbf{H}(z)$  is the polyphase matrix of the orthogonal filter bank  $h_0, \ldots, h_{M-1}$ , and  $\mathbf{G}^t(z) = \begin{bmatrix} G_0(z) & G_1(z) \cdots & G_{M-1}(z) \end{bmatrix}$ is the transpose of the vector of the *z*-transforms of the polyphase components of *g*. According to Cvetković and Vetterli [16] the extended filter bank is doubly FIR if and only if

$$r(z) \triangleq \det \left( \mathbf{K}^t(z^{-1})\mathbf{K}(z) \right) = \alpha z^{-k}, \quad \exists \alpha \in \mathbb{C}, \ k \in \mathbb{Z}.$$
(9)

By observing that

$$r(z^{-1}) = \det \left( \mathbf{K}^{t}(z)\mathbf{K}(z^{-1}) \right) = \det \left( \left[ \mathbf{K}^{t}(z^{-1})\mathbf{K}(z) \right]^{t} \right) = r(z),$$
(10)

it follows that (9) is true if and only if r(z) is a constant. With some algebra and by exploiting well-known results about determinants [17], one can write

$$r(z) = \det \left( \mathbf{H}^{t}(z^{-1})\mathbf{H}(z) + \mathbf{G}(z^{-1})\mathbf{G}^{t}(z) \right)$$
  
= det  $\left( \mathbf{I} + \mathbf{G}(z^{-1})\mathbf{G}^{t}(z) \right)$   
= 1 +  $\mathbf{G}^{t}(z)\mathbf{G}(z^{-1}) = 1 + \sum_{k=0}^{M-1} G_{k}(z^{-1})G_{k}(z).$  (11)

It is clear that (11) is a constant if and only if  $r(z) - 1 = \sum_{k=0}^{M-1} G_k(z^{-1})G_k(z)$  is. Observing that r(z) - 1 is the *z*-transform of the sampled version of the correlation of *g*, it follows that r(z) is a constant, and the filter bank is doubly FIR, if and only if (7) is true, that is, *g* is orthogonal to its own translations.

A consequence of Theorem 1 is that, if M = 2, the only possible filter with linear phase resulting in a doubly FIR filter bank is the 2-tap Haar filter [18]. If we consider a systematic filter bank, as we will do in the proposed video coding scheme, this implies to work blockwise. More precisely, the filter bank is equivalent to mapping each pair of consecutive samples into the triple made of the two samples and their average.

If linear phase is necessary, as in image and video coding applications, and one does not want to work blockwise, the dual filter bank will necessarily have IIR impulse responses. In this case, if the decay of the impulse responses of the resulting IIR filters is fast enough, the dual filters can be approximated with possibly short FIR filters, for example, by truncation of the filter kernels. The corresponding DFIR filter bank introduces a small error in the reconstruction process which can be negligible in coding applications. The situation is similar to what happens for nearly perfect reconstruction orthogonal filter banks, where linear-phase filters can be used at the expense of a small error in the reconstruction [14].

#### 3.1.2. Reconstruction error in response to packet losses

The second problem we consider is the design of the redundant channel filter in a systematic filter bank to allow for a "good" reconstruction even in presence of packet losses. This means that the lower bound of  $\Phi_I$  must be as large as possible. As mentioned, we take into account the case of *L* consecutive coefficient losses in each channel. We will therefore analyze the lower bound of  $\Phi_I$  when a set of *L* consecutive coefficients is lost in a single channel.

*Property 1.* Let  $h_j$ , j = 0, ..., M, be the impulse responses of an (M + 1)/M systematic filter bank and let

$$y_j(n) = \sum_m x(m)h_j(Mn-m).$$
(12)

Let  $0 \le c \le M$  and suppose that a burst of *L* coefficients of the *c*th channel, that is, coefficients  $y_c(n)$ , n = 0, ..., L - 1, are lost. Let  $\Phi_I$  and  $A_I$  be the corresponding subframe and its lower bound, respectively.

Then, if c = M, we have  $A_I = 1$ ; otherwise

$$\frac{\min_{\omega} |H_{c,M}(e^{j\omega})|^{2}}{1+T+2\sqrt{T}} \leq A_{I} \leq \frac{2(N_{c}-1)||h_{c,M}||_{1}^{2}}{L} + \min_{\omega} |H_{c,M}(e^{j\omega})|^{2} \frac{L-N_{c}+1}{L}.$$
(13)

In (13),  $N_c$  is the length of  $h_{c,M}(n) = h_M(c + nM)$ , the *c*th polyphase component of  $h_M$ , while *T* is the 1-norm of the autocorrelation of filter  $h_M$  sampled with a factor *M*, namely,

$$T \triangleq \sum_{n \in \mathbb{Z}} |r(n)| = ||r||_1, \quad r(n) \triangleq \sum_m h_M(m)h_M(m - Mn).$$
(14)

The proof for the upper bound is reported in the appendix, Proof A.1, while the proof for the lower bound is in the appendix, Proof A.2.

Note that when  $L \gg N_c$ , the right-hand side of (13) is approximately equal to

$$\min_{\alpha} |H_{c,M}(e^{j\omega})|^2.$$
(15)

This suggests the following criterion to achieve a small reconstruction error in response to packet losses.

*Criterion 1.* Suppose bursts of coefficient losses are expected and let  $h_M$  be the (M + 1)th filter of an (M + 1)/M systematic filter bank. Choose  $h_M$  such that

$$\min_{\boldsymbol{c}\in\{0,\dots,M-1\}}\min_{\boldsymbol{\omega}}|H_{\boldsymbol{c},M}(\boldsymbol{e}^{j\boldsymbol{\omega}})|^2 \tag{16}$$

is as large as possible.

#### 3.2. MD 3 video codec: choice of the filter

From the results of Section 3.1, the filter for the redundant channel in the systematic filter bank under consideration should be chosen according to Criterion 1. We took into account the four- and eight-tap lowpass filters from the well known family of Daubechies filters [14] reported in Table 1. These two filters are orthogonal to their even translations, and therefore the resulting filter bank is exactly DFIR. We also considered a linear-phase redundant channel filter. In the following, we will refer to this filter as the symmetric 4-tap filter (Table 1). The use of a linear-phase filter can be useful for video coding purposes, also because it allows for symmetric rather than periodic signal extension in the analysis stage. Moreover, the symmetric filter was designed according to Criterion 1. As we will see, its performance is actually better than that of the 4-tap Daubechies filter and is comparable to that of the 8-tap Daubechies filter. Since the symmetric filter is not orthogonal to its translations, the hypotheses of Theorem 1 are not met exactly, and the resulting filter bank has IIR synthesis filters. These are very well approximated by the FIR filters of Table 2. The impulse responses of the dual filter bank are truncated to make the system DFIR so that the overall reconstruction error is negligible. In particular, it is easy to see that, when the input is modeled as a random process uniformly distributed in [0, 255], the cascade of the FIR analysis and synthesis filter banks, with no quantization, allows for a peak signal-tonoise ratio (PSNR) of about 60 dB. The PSNR is defined as

$$PSNR \triangleq 10 \log_{10} \frac{255^2}{MSE},$$
 (17)

where MSE is the mean squared reconstruction error with the input. The same reconstruction quality is obtained, with no quantization, with the video sequences we consider in Section 4.

Let us now consider the performance of the filters when losses and quantization are taken into account. Figure 3 compares the amplitude of the frequency responses of the two polyphase components of the 4-tap symmetric and Daubechies filters. As we can see, the 4-tap Daubechies filter has a smaller minimum in the first polyphase component. From (16), we conclude that the symmetric filter should perform better than the 4-tap Daubechies filter. This will be confirmed by the results in the experimental section.

#### 4. EXPERIMENTAL RESULTS

In this section, we evaluate the performance of the proposed video coding scheme (MD 3) presented in Section 3. Original sequences are in CIF format. This scheme is compared with other two MD systems based on spatial subsampling of original frames. The first one (MD 4) originates four descriptions from the spatial polyphase components of the original frame. Each description, whose dimension is 1/4 of that of the original frame, is compressed independently, packetized, and sent over an error-prone network. The second scheme (MD 2) has a similar structure, but only two descriptions are generated by separating the even and odd rows of the original frame. We compare the MD schemes with a standard single-description (SD) H.264/AVC coder which includes basic error concealment as described in [19]. The coders use the H.264/AVC test model software version JM6.0a. To increase robustness to channel errors and make a fair comparison, the SD coder uses the random intra-macroblock refresh coding option, that is, 100 macroblocks for every CIF frame are coded in intramode. No random intra-macroblock refresh coding option is activated in the MD schemes. Other coding options are the same for the SD and MD coders. In particular the GOP structure is I BBBB P BBBB P BBBB P BBBB I, and slices have a fixed 1000-byte dimension. Each slice is sent as a packet, and each packet is lost according to a certain probability model.

For the MD 2 scheme and the MD 4 scheme, in case of errors in one or more descriptions, appropriate error concealment via bilinear interpolation from correctly received descriptions is performed at the receiver. Similarly to our scheme, corrected subframes are copied into the corresponding receiver frame buffers to limit error propagation. B blocks that use direct mode prediction with respect to lost P slices are also marked as lost. In case all the descriptions are lost, basic error concealment is applied as in [19] in all the MD coders, including the frame-based one.

From a general viewpoint, the MD 2 and MD 4 schemes achieve robustness to packet losses by exploiting the inherent source redundancy. However, to recover the missing information at the receiver, a necessarily approximated procedure has to be used in any case. The proposed MD 3 scheme adds redundancy by processing the source with an oversampled filter bank. The price paid is the additional rate which has to

	Symmetric 4-tap			Daubechies 4-tap			Daubechies 8-tap		
п	$h_0(n)$	$h_1(n)$	$h_2(n)$	$h_0(n)$	$h_1(n)$	$h_2(n)$	$h_0(n)$	$h_1(n)$	$h_2(n)$
-2	0	0	$-1.04 \cdot 10^{-1}$	0	0	$+3.42 \cdot 10^{-1}$	0	0	$+1.63 \cdot 10^{-1}$
-1	0	1	$+5.77 \cdot 10^{-1}$	0	1	$+5.92 \cdot 10^{-1}$	0	1	$+5.05 \cdot 10^{-1}$
0	1	0	$+5.77 \cdot 10^{-1}$	1	0	$+1.58 \cdot 10^{-1}$	1	0	$+4.46 \cdot 10^{-1}$
1	0	0	$-1.04 \cdot 10^{-1}$	0	0	$-9.15 \cdot 10^{-2}$	0	0	$-1.98 \cdot 10^{-2}$
2	0	0	0	0	0	0	0	0	$-1.32 \cdot 10^{-1}$
3	0	0	0	0	0	0	0	0	$+2.18 \cdot 10^{-2}$
4	0	0	0	0	0	0	0	0	$+2.33 \cdot 10^{-2}$
5	0	0	0	0	0	0	0	0	$-7.49 \cdot 10^{-3}$

TABLE 1: Analysis filter banks for the symmetric 4-tap redundant channel filter, and the 4-tap and 8-tap Daubechies channel filters.

TABLE 2: Synthesis filter banks for the symmetric 4-tap redundant channel filter, and the 4-tap and 8-tap Daubechies channel filters.

	Symmetric 4-tap				Daubechies 4-tap				Daubechies 8-tap		
п	$\widetilde{h}_0(n)$	$\widetilde{h}_1(n)$	$\widetilde{h}_2(n)$	п	$\widetilde{h}_0(n)$	$\widetilde{h}_1(n)$	$\widetilde{h}_2(n)$	п	$\widetilde{h}_0(n)$	$\widetilde{h}_1(n)$	$\widetilde{h}_2(n)$
-6	$+1.09 \cdot 10^{-4}$	0	$+1.24 \cdot 10^{-4}$	-3	$+2.08 \cdot 10^{-2}$	0	0	-7	$+8.14 \cdot 10^{-4}$	0	0
-5	$-1.68 \cdot 10^{-4}$	$+1.09 \cdot 10^{-4}$	$-1.91 \cdot 10^{-4}$	-2	$-3.61 \cdot 10^{-2}$	0	0	-6	$-2.53 \cdot 10^{-3}$	0	0
$^{-4}$	$+1.52 \cdot 10^{-3}$	$-9.89\cdot10^{-4}$	$+1.74 \cdot 10^{-3}$	-1	$-1.25 \cdot 10^{-1}$	$+3.61 \cdot 10^{-2}$	$-6.10 \cdot 10^{-2}$	-5	$-1.40\cdot10^{-4}$	$+2.53 \cdot 10^{-3}$	$-5.00 \cdot 10^{-3}$
-3	$-2.35 \cdot 10^{-3}$	$+1.52 \cdot 10^{-3}$	$-2.68 \cdot 10^{-3}$	0	$+9.06 \cdot 10^{-1}$	$-6.25 \cdot 10^{-2}$	$+1.06 \cdot 10^{-1}$	-4	$+7.45 \cdot 10^{-3}$	$-7.84 \cdot 10^{-3}$	$+1.55 \cdot 10^{-2}$
$^{-2}$	$+2.14 \cdot 10^{-2}$	$-1.39 \cdot 10^{-2}$	$+2.43 \cdot 10^{-2}$	1	$-6.25 \cdot 10^{-2}$	$+7.61 \cdot 10^{-1}$	$+3.94 \cdot 10^{-1}$	-3	$-5.00 \cdot 10^{-3}$	$-7.45 \cdot 10^{-3}$	$+1.45 \cdot 10^{-2}$
-1	$+5.70 \cdot 10^{-2}$	$+2.14 \cdot 10^{-2}$	$-3.75 \cdot 10^{-2}$	2	$-3.61 \cdot 10^{-2}$	$-1.25 \cdot 10^{-1}$	$+2.28 \cdot 10^{-1}$	-2	$-7.06 \cdot 10^{-3}$	$+4.49 \cdot 10^{-2}$	$-8.82 \cdot 10^{-2}$
0	$+7.99 \cdot 10^{-1}$	$-1.94 \cdot 10^{-1}$	$+3.41 \cdot 10^{-1}$	3	0	$+3.61 \cdot 10^{-2}$	0	-1	$-4.70 \cdot 10^{-2}$	$+7.06 \cdot 10^{-3}$	$-1.32 \cdot 10^{-2}$
1	$-1.94 \cdot 10^{-1}$	$+7.99 \cdot 10^{-1}$	$+3.41 \cdot 10^{-1}$	4	0	$+2.08 \cdot 10^{-2}$	0	0	$+8.38 \cdot 10^{-1}$	$-1.52 \cdot 10^{-1}$	$+2.97 \cdot 10^{-1}$
2	$+2.14 \cdot 10^{-2}$	$+5.70 \cdot 10^{-2}$	$-3.75 \cdot 10^{-2}$	5	0	0	0	1	$-1.52 \cdot 10^{-1}$	$+8.29 \cdot 10^{-1}$	$+3.37 \cdot 10^{-1}$
3	$-1.391 \cdot 10^{-2}$	$+2.14 \cdot 10^{-2}$	$+2.43 \cdot 10^{-2}$	6	0	0	0	2	$-7.06 \cdot 10^{-3}$	$-4.70 \cdot 10^{-2}$	$+1.09 \cdot 10^{-1}$
4	$+1.52 \cdot 10^{-3}$	$-2.35 \cdot 10^{-3}$	$-2.68 \cdot 10^{-3}$	7	0	0	0	3	$+4.49 \cdot 10^{-2}$	$+7.06 \cdot 10^{-3}$	0
5	$-9.89 \cdot 10^{-4}$	$+1.52 \cdot 10^{-3}$	$+1.74 \cdot 10^{-3}$	8	0	0	0	4	$+7.45 \cdot 10^{-3}$	$-5.00 \cdot 10^{-3}$	0
6	$+1.09 \cdot 10^{-4}$	$-1.68 \cdot 10^{-4}$	$-1.92 \cdot 10^{-4}$	9	0	0	0	5	$-7.84 \cdot 10^{-3}$	$-7.45 \cdot 10^{-3}$	0
7	0	$+1.09 \cdot 10^{-4}$	$+1.24 \cdot 10^{-4}$	10	0	0	0	6	$-2.53 \cdot 10^{-3}$	$-1.40\cdot10^{-4}$	0
8	0	0	0	11	0	0	0	7	0	$+2.53 \cdot 10^{-3}$	0
9	0	0	0	12	0	0	0	8	0	$+8.14 \cdot 10^{-4}$	0

be spent to code the parity-check video sequence. However, exact recovery within frame theory is possible when losses are not too numerous. One has to resort to approximate interpolation solutions only when the received information corresponds to an incomplete system. We will see in the following that, in the presence of packet losses, MD 3 has the best overall performance. Moreover, the visual quality obtained with the proposed scheme is superior, because of the exact recovery capability for most error patterns.

#### 4.1. Comparison of the filters

We start by considering the redundant channel filter choice in the proposed MD 3 scheme. The simulations we present here are relative to 100 frames of the CIF sequence *Foreman*. Results are averages of 50 independent transmission trials, where packets are lost independently with probability  $P_{\ell}$ .

Figure 4 compares the PSNR of the reconstructed video with the two filters and with  $P_{\ell} = 0.1$ . The symmetric filter outperforms the Daubechies 4-tap filter by about 0.5 dB at high bit rates. The performance of the 8-tap Daubechies filter is indeed similar to that of the symmetric 4-tap filter.

It is well known that PSNR can give only an approximate indication of the video sequence quality. As a matter of fact, the visual quality corresponding to the use of the symmetric linear-phase filter is preferable to that obtained with the Daubechies 4-tap filter at all bit rates. Figure 5 shows details of the reconstructed frame of the sequence *Foreman* coded at about 2 Mbps. In both cases, the loss pattern corresponds to the complete loss of data from channel 1, that is, the video



FIGURE 3: Amplitude of the frequency response of the polyphase components of the Daubechies 4-tap filter and of the symmetric 4-tap filter. (a) First polyphase component. (b) Second polyphase component.

frame even rows are missing at the receiver. As it can be seen from Figure 5(a), using the 4-tap Daubechies filter leads to a granularity effect due to relevant quantization error enhancement. This annoying effect is particularly visible near edges and around the eyes, where the coding error is greater. The effect disappears in Figure 5(b) corresponding to the use of the symmetric 4-tap filter.

#### 4.2. Comparison of the MD coders

We compare here the performance of the proposed MD 3 scheme, adopting the symmetric 4-tap filter, with that of the SD, MD 2, and MD 4 schemes. The original video sequences are in CIF format, and the results are relative to 100 frames, averaged over 50 independent transmission trials. Packets are lost independently with probability  $P_{\ell}$ . Figures 6, 7, and 8 show the performance of the coders for the video sequences *News, Foreman*, and *Teeny*, respectively. The *News* sequence is characterized by low motion and a dark uniform background, whereas the *Teeny* sequence is characterized by large motion. Coding is performed for the same H.264/AVC QP values (QP = 19, 20, ..., 41), therefore different compression rates are obtained as a result of sequence motion content.

Despite the fact that the SD coder can exploit spatial redundancy more efficiently, it does not have the best performance even for  $P_{\ell} = 0$ , due to the intra-refresh coding option. Nonetheless, the performance of the SD coder drops



FIGURE 4: Rate-distortion comparison between the Daubechies 4tap filter and the symmetric 4-tap filter adopted in this work.  $P_{\ell} = 0.1$ .

very rapidly for increasing  $P_{\ell}$ . We expect that the MD coder with four descriptions presents good robustness to errors from a subjective quality point of view, at the expense of some coding inefficiency. The proposed frame-based coder adds 1.5 redundancy to the video stream, and has therefore a low coding efficiency but possibly good robustness to errors from both a subjective and objective quality point of view. Note that, with no coding, perfect reconstruction is still possible in this case even in the presence of errors. Finally, the MD coder with two descriptions has better coding efficiency but possibly worse performance in terms of subjective quality, since packet losses have to be corrected with the interpolation of entire rows.

It can be seen from Figures 6 and 7 that for loss probability  $P_{\ell} = 0.05$ , the proposed frame-based MD scheme performs better than the SD scheme and the MD scheme with four descriptions. Moreover, at relatively high bit rates, the proposed scheme has the best performance of all schemes. For  $P_{\ell} = 0.1$ , the advantage of the proposed solution is even more evident. For the *Teeny* sequence (Figure 6), the framebased MD 3 system and the MD 4 system show comparable performance which are significantly better than that of MD 2.

The intrinsic error recovery capability of the proposed MD 3 scheme plays an important role for visual quality in all coding conditions. Figure 9(b) shows a detail of the reconstructed video stream *Foreman* coded at about 1 Mbps when one description is lost. In Figure 9(a), we show the reconstructed frame for the MD scheme with two descriptions. It can be seen from the figure that the MD scheme with two descriptions can originate annoying artifacts, especially along diagonal edges.

These results are confirmed with a more realistic twostate Gilbert channel model for packet errors in each channel (instead of i.i.d. errors) [20]. In the experiments we supposed that different descriptions are sent on different channels and that each channel can be in a "good" or in a "bad" state. If a



FIGURE 5: Details of reconstructed frames for the MD 3 frame system, using (a) the Daubechies 4-tap filter and (b) the symmetric 4-tap filter adopted in this work.

channel is in the "good" state, then no packet is lost, while if it is in the "bad" state, then every packet is lost. The transition probabilities have been determined by fixing the packet error probability  $P_{\ell}$  and the mean error burst length. In the experiments we choose  $P_{\ell}$  equal to the loss probability used in the i.i.d. case to make comparisons easier. Figures 10, 11, and 12 show the rate-distortion comparison of the MD schemes for different values of  $P_{\ell}$ , with a mean error burst length of 4 packets (since a packet contains a row of macroblocks, a burst of length 4 causes the loss of approximately 22% of the image).

With all sequences, the proposed MD 3 frame-based scheme has the best performance at relatively high bit rates and packet error probability, making it an interesting technique for many application scenarios. Moreover, we remark that, due to the recovery possible within the framework of frame theory, the visual quality of the proposed solution does not present the typical artifacts originated by interpolation.

#### 4.3. Concealment using temporal information

We consider here an alternative approximate error concealment technique based on temporal information. It is used in the MD 3 system only when recovery with the dual frame is not possible, that is, when a slice is lost in the same position in two out of three descriptions.

Consider for the moment the case when two out of three descriptions are lost in the MD 3 system. If the correctly received description is not intracoded, its blocks are predicted from the content of the corresponding frame buffer. If this prediction is accurate (i.e., the prediction error is negligible), we can use motion information to predict blocks of lost descriptions using the motion vectors of the received subsequence. In other words, when the prediction error is negligible in the received subsequence, we trust the received motion vectors to predict the missing sequences from the corresponding frame buffers.

In case two out of three slices in the same position are lost, the proposed solution evaluates the MSE of the prediction error on the correctly received description, block by block. If this error is below a predefined threshold, the outlined temporal prediction procedure is used to recover one of the missing systematic channels, otherwise spatial interpolation is used. Then the received and reconstructed subimages are fed to the restoring block as before. The MSE threshold computation is based on the quantization error introduced by the H.264 coder. The mean square error  $MSE_{QP}$  corresponding to the H.264 quantization parameter QP can be written as [10]

$$MSE_{QP} \simeq 0.15 \cdot 2^{QP/3}$$
. (18)

The MSE threshold is assumed equal to  $\alpha \cdot \text{MSE}_{\text{QP}}$ , with  $\alpha = 3.^2$  Note that the H.264 adaptive prediction process is very accurate, and blocks as small as  $4 \times 4$  pixels are predicted.

The described temporal error concealment procedure can of course be used also for the MD 2 and MD 4 schemes. Figure 13 shows the PSNR for the sequence *Foreman* and i.i.d. packet errors with  $P_{\ell} = 0.1$ . The MD 2 scheme receives the greatest benefit from temporal interpolation, due to the fact that spatial interpolation alone performs poorly along the strong edges in the background of *Foreman*. Remember that the MD 3 scheme actually uses this interpolation procedure only when  $\Phi_I$  is incomplete, that is, only when a slice is lost in the same position in two out of three descriptions.

#### 5. CONCLUSIONS

In this paper, we present a multiple-description video coding scheme based on the extension, using frame-based analysis, of a filter bank that computes the spatial polyphase components of the input video frames. Each resulting video subsequence is then coded with a standard H.264 coder. A simple modification of the decoder allows to increase robustness to packet losses by exploiting the added redundancy by means of reconstruction via the dual frame. In the event of excessive errors, when the resulting frame operator becomes incomplete and no direct reconstruction is possible, bilinear spatial interpolation is used to recover necessary information. We also considered the case of an interpolation procedure which operates in the temporal domain. A detailed analysis toward system design and evaluation of reconstruction error bounds was carried out.

The proposed scheme shows a remarkably good performance when errors come into play and it shows several advantages. It permits good robustness to channel errors. Up

<sup>&</sup>lt;sup>2</sup> The value of  $\alpha$  has been obtained by means of experiments. The overall performance is not very sensitive to the value of  $\alpha$ .





FIGURE 6: Rate-distortion comparison of SD and MD schemes for the *News* CIF sequence and different values of  $P_{\ell}$  (i.i.d. channel). (a)  $P_{\ell} = 0.01$ . (b)  $P_{\ell} = 0.05$ . (c)  $P_{\ell} = 0.1$ .

FIGURE 7: Rate-distortion comparison of SD and MD schemes for the *Foreman* CIF sequence and different values of  $P_{\ell}$  (i.i.d. channel). (a)  $P_{\ell} = 0.01$ . (b)  $P_{\ell} = 0.05$ . (c)  $P_{\ell} = 0.1$ .



FIGURE 8: Rate-distortion comparison of SD and MD schemes for the *Teeny* CIF sequence and different values of  $P_{\ell}$  (i.i.d. channel). (a)  $P_{\ell} = 0.01$ . (b)  $P_{\ell} = 0.05$ . (c)  $P_{\ell} = 0.1$ .

to relatively high packet loss probabilities ( $P_{\ell} \simeq 0.1$  in our experiments), the intrinsic recovery capability of the frame based system can be exploited for most error patterns. As a



(a)



FIGURE 9: Details of reconstructed frames for (a) the MD 2 system and (b) the frame-based MD 3 system when one description is lost.

matter of fact, as long as the probability of losing data in the same position in two out of three descriptions is low, the reconstruction depends only on the quality of the individual descriptions. No artifacts are present in the reconstructed sequences because losses can be completely recovered by means of the redundancy provided by frame analysis. For larger values of  $P_{\ell}$ , when only one description is received for a given image region, one has to resort to approximate interpolation techniques. Also, when no description is received, concealment can be done by using successive or past frames according to the basic SD error recovery procedures of H.264. In the latter two cases, the visual quality and the PSNR can drop significantly. This is particularly evident when the subsequences are coded with good quality and spatial interpolation does not provide an acceptable approximation, for example, when the image sequence has diagonal edges.

The price to pay is the cost of coding the additional parity-check subsequence, together with the efficiency loss caused by coding two subsampled subsequences. On the other hand, frame analysis and synthesis, including the restoring block, can be implemented with reasonable complexity. The experimental results show, however, that the scheme can be competitive even for relatively small loss probability.





FIGURE 10: Rate-distortion comparison of MD schemes for the *News* CIF sequence and different values of  $P_{\ell}$  (Gilbert channel). (a)  $P_{\ell} = 0.01$ . (b)  $P_{\ell} = 0.05$ . (c)  $P_{\ell} = 0.1$ .

FIGURE 11: Rate-distortion comparison of MD schemes for the *Foreman* CIF sequence and different values of  $P_{\ell}$  (Gilbert channel). (a)  $P_{\ell} = 0.01$ . (b)  $P_{\ell} = 0.05$ . (c)  $P_{\ell} = 0.1$ .





FIGURE 12: Rate-distortion comparison of MD schemes for the *Teeny* CIF sequence and different values of  $P_{\ell}$  (Gilbert channel). (a)  $P_{\ell} = 0.01$ . (b)  $P_{\ell} = 0.05$ . (c)  $P_{\ell} = 0.1$ .

FIGURE 13: Improvements in rate-distortion performances of MD schemes for the *Foreman* sequence using temporal concealment (all schemes), followed by optimal frame inversion (MD 3 scheme only). (a) MD 2. (b) MD 4. (c) MD 3.

#### **APPENDIX**

#### PROOFS

For notation simplicity, we set  $g(n) \triangleq h_M(n)$ , the redundant channel filter of a systematic (M + 1)/M filter bank.

*Proof A.1.* We prove here the upper bound in (13). Consider first the case c = M, that is, only redundant coefficients are lost. In this case all the samples of x are received through the systematic channels and, obviously,  $||F_Ix|| \ge ||x||$  which implies  $A_I \ge 1$ . We can obtain  $A_I = 1$  by choosing x orthogonal to g and its translations of multiples of M. This proves the claim for c = M.

In order to prove the claim for c = 0, ..., M - 1, we will search for a specific *x* such that  $||F_Ix||^2/||x||^2$  is not larger than the right-hand side of (13). This will prove the claim. Since we are searching for *x* such that  $||F_Ix||$  is small, we choose *x* such that  $x(n) \neq 0$  only when n = c, c + M, ..., c + (L - 1)M. With no loss, the output of channel *c* is identically zero, except for *L* consecutive coefficients. Indeed, we suppose that these coefficients are actually lost. With this choice, any nonnull received coefficient arrives through the redundant channel only. It is easy to see that

$$y_{M+1}(n) = x_c \star g_c(n),$$
 (A.1)

where  $x_c(n) = x(c + nM)$  and  $g_c(n) = g(nM - c)$  are the *c*th polyphase component of *x* and *g*, respectively. Let  $\omega_0$  be such that  $\min_{\omega} |G_c(e^{j\omega})| = |G_c(e^{j\omega_0})|$  and choose

$$x_{c}(n) = \begin{cases} \exp(j\omega_{0}n) & \text{if } 0 \le n < L, \\ 0 & \text{otherwise.} \end{cases}$$
(A.2)

Let  $N_c$  be the length of  $g_c$ . Equation (A.1) implies that  $y_{M+1}(n) \neq 0$  only for  $n = 0, ..., N_c + L - 2$  and it is easy to recognize that if  $N_c - 1 \leq n \leq L - 1$ , then

$$y_c(n) = G_c(e^{j\omega_0}) \exp(j\omega_0 n).$$
(A.3)

By exploiting (A.3) one can write

$$||Fx||^{2} = \sum_{n=0}^{N_{c}+L-2} |x_{c} \star g_{c}(n)|^{2}$$

$$= \sum_{n=0}^{N_{c}-2} |x_{c} \star g_{c}(n)|^{2} + \sum_{n=N_{c}-1}^{L-1} |G_{c}(e^{j\omega_{0}}) \exp(j\omega_{0}n)|^{2}$$

$$+ \sum_{n=L}^{N_{c}+L-2} |x_{c} \star g_{c}(n)|^{2}$$

$$= \sum_{n=0}^{N_{c}-2} |x_{c} \star g_{c}(n)|^{2}$$

$$+ \sum_{n=L}^{N_{c}+L-2} |x_{c} \star g_{c}(n)|^{2} + (L - N_{c} + 1) |G_{c}(e^{j\omega_{0}})|^{2}.$$
(A.4)

By exploiting the well-known fact that  $|x_c \star g_c(n)| \le ||g_c||_1 ||x_c||_{\infty} = ||g_c||_1$ , one finds the following upper bound

$$\|Fx\|^{2} \leq 2(N_{c}-1) \|g_{c}\|_{1}^{2} + (L-N_{c}+1) |G_{c}(e^{j\omega_{0}})|^{2}.$$
(A.5)

By dividing (A.5) by  $||x||^2 = L$  (see (A.2)) one obtains (13).

*Proof A.2.* To prove the lower bound in (13), we need the following two lemmas, relating the frame bounds to the singular values of the analysis filter bank polyphase matrix.

**Lemma A.1.** Let **H** be the polyphase matrix of an N/M analysis filter bank and let  $\sigma_H(\omega)$  be the smallest singular value of  $\mathbf{H}(e^{j\omega})$ . Let  $A_H$  be the lower bound of the corresponding frame operator F. The following equality holds:

$$A_{H} = \inf_{\|x\|=1} \|Fx\|^{2} = \min_{\omega \in [0,2\pi]} \sigma_{H}^{2}(\omega).$$
(A.6)

*Proof of Lemma A.1.* Let  $\mathbf{H}(e^{j\omega}) = U(\omega)S(\omega)V^t(\omega)$  be the singular value decomposition of  $\mathbf{H}(e^{j\omega})$ . The problem of searching for the lower bound of *F* corresponds to searching for an input signal *x* with ||x|| = 1 such that

$$||Fx||^{2} = \sum_{j=0}^{N-1} ||y_{j}||^{2}$$
(A.7)

is as small as possible, where  $y_j$  is the output of the *j*th channel. By exploiting Parseval's identity one can rewrite (A.7) as

$$||F\mathbf{x}||^{2} = \sum_{j=0}^{N-1} \int_{0}^{2\pi} |Y_{j}(\omega)|^{2} d\omega = \int_{0}^{2\pi} \sum_{j=0}^{N-1} |Y_{j}(\omega)|^{2} d\omega$$
$$= \int_{0}^{2\pi} ||\mathbf{Y}(\omega)||^{2} d\omega = \int_{0}^{2\pi} ||\mathbf{H}(e^{j\omega})\mathbf{X}(\omega)||^{2} d\omega,$$
(A.8)

where  $\mathbf{Y}(\omega)$  is the vector  $[Y_0(\omega), \dots, Y_{N-1}(\omega)]^t$  and  $\mathbf{X}(\omega)$  is the vector  $[X_0(\omega), \dots, X_{M-1}(\omega)]^t$  of input polyphase component frequency transforms. It is well known that

$$\left\|\left|\mathbf{H}(e^{j\omega})\mathbf{X}(\omega)\right\|\right|^{2} \ge \left\|\mathbf{X}(\omega)\right\|^{2} \sigma_{H}(\omega)^{2}.$$
 (A.9)

By exploiting (A.9) in (A.8) one obtains

$$\|F\mathbf{x}\|^{2} \ge \int_{0}^{2\pi} \left\| \mathbf{X}(\omega) \right\|^{2} \sigma_{H}(\omega)^{2} d\omega.$$
(A.10)

Formula (A.10) can be verified with the equality sign by choosing  $\mathbf{X}(\omega)$  proportional to the *M*th column of  $V(\omega)$ , that is,

$$\mathbf{X}(\omega) = f(\omega)V_M(\omega) \tag{A.11}$$

for some function  $f : [0, 2\pi] \to \mathbb{C}$ . It is easy to see that ||x|| = 1 is equivalent to  $\int_0^{2\pi} |f(\omega)|^2 d\omega = 1$ . With choice (A.11), (A.10) becomes

$$\|F\mathbf{x}\|^{2} = \int_{0}^{2\pi} |f(\omega)|^{2} \sigma_{H}(\omega)^{2} d\omega.$$
 (A.12)

Let  $\omega_0 = \operatorname{argmin}_{\omega \in [0,2\pi]} \sigma_H(\omega)$ . By exploiting (A.12) one can write

$$\|Fx\|^{2} = \int_{0}^{2\pi} |f(\omega)|^{2} \sigma_{H}(\omega)^{2} d\omega$$
  

$$\geq \int_{0}^{2\pi} |f(\omega)|^{2} \sigma_{H}(\omega_{0})^{2} d\omega \qquad (A.13)$$
  

$$= \sigma_{H}(\omega_{0})^{2} \int_{0}^{2\pi} |f(\omega)|^{2} d\omega = \sigma_{H}(\omega_{0})^{2}.$$

Formula (A.13) shows that  $A_H$  in (A.6) cannot be smaller than  $\min_{\omega \in [0,2\pi]} \sigma_H^2(\omega)$ . It remains to show that for any  $\epsilon > 0$ we can find  $f_{\epsilon} \in L^2([0,2\pi]), ||f_{\epsilon}|| = 1$ , such that

$$\int_{0}^{2\pi} f_{\epsilon}^{2}(\omega) \sigma_{H}^{2}(\omega) d\omega \leq \sigma_{H}^{2}(\omega) + \epsilon.$$
 (A.14)

By exploiting the continuity of  $\sigma_H^2(\omega)$ , find  $\delta$  such that

$$\begin{aligned} |\omega - \omega_0| < \delta \implies |\sigma_H^2(\omega) - \sigma_H^2(\omega_0)| \\ &= \sigma_H^2(\omega) - \sigma_H^2(\omega_0) \le \epsilon. \end{aligned}$$
(A.15)

Let  $f_{\epsilon}$  be such that  $f_{\epsilon}(\omega) = 0$  if  $|\omega - \omega_0| \ge \delta$  and  $f_{\epsilon}(\omega) = 1/\sqrt{2\delta}$  if  $|\omega - \omega_0| < \delta$ . It follows that

$$\int_{0}^{2\pi} f_{\epsilon}^{2}(\omega)\sigma_{H}^{2}(\omega)d\omega = \int_{\omega_{0}-\delta}^{\omega_{0}+\delta} \frac{1}{2\delta}\sigma_{H}^{2}(\omega)d\omega$$
$$\leq \int_{\omega_{0}-\delta}^{\omega_{0}+\delta} \frac{1}{2\delta}(\sigma_{H}^{2}(\omega_{0})+\epsilon)d\omega \quad (A.16)$$
$$= \sigma_{H}^{2}(\omega_{0})+\epsilon.$$

The following lemma allows to set a lower bound on the smallest singular value of a systematic filter bank polyphase matrix **H**.

#### **Lemma A.2.** Let **H** be any $M \times M$ matrix

$$\mathbf{H} = \begin{bmatrix} \mathbf{U} & \mathbf{0} \\ \mathbf{a}^t & b \end{bmatrix},\tag{A.17}$$

where  $\mathbf{U}^{\mathsf{t}}\mathbf{U} = \mathbf{I}$  and  $\mathbf{a} \in \mathbb{C}^{M-1}$ ,  $b \in \mathbb{C}$ ; and let  $\sigma_H$  be the smallest singular value of **H**. The following inequality holds:

$$\sigma_{H}^{2} \geq \frac{|b|^{2}}{|b|^{2} + \|\mathbf{a}\|^{2} + 1 + 2\|\mathbf{a}\|}.$$
 (A.18)

*Proof of Lemma A.2.* First observe that one can always suppose  $\mathbf{U} = \mathbf{I}$  since one can multiply (A.17) by diag( $\mathbf{U}^t$ , 1) and this does not change the singular values of  $\mathbf{H}$ . In order to find a lower bound to the smallest singular value of  $\mathbf{H}$ , we will first search for an upper bound to the largest singular value of matrix of form (A.17). By applying such an upper bound to

$$\mathbf{H}^{-1} = \begin{bmatrix} \mathbf{I} & 0\\ -\frac{\mathbf{a}^t}{b} & \frac{1}{b} \end{bmatrix}$$
(A.19)

and remembering that  $\sigma_H$  is the inverse of the largest singular value of  $\mathbf{H}^{-1}$  we will be able to obtain the desired lower bound.

As it is well known, the largest singular value of a matrix **H** is the matrix 2-norm  $||\mathbf{H}|| = \sup_{||x||=1} ||\mathbf{H}x||$ . Let  $x = [\mathbf{u}^t, \nu]^t \in \mathbb{C}^N$  be such that ||x|| = 1. The squared norm of **H**x is

$$\|\mathbf{H}x\|^{2} = \|[\mathbf{u}^{t}, \mathbf{u}^{t}\mathbf{a} + bv]^{t}\|^{2} = \|\mathbf{u}\|^{2} + |\mathbf{u}^{t}\mathbf{a} + bv|^{2}$$
  
=  $\|\mathbf{u}\|^{2} + \|\mathbf{u}\|^{2}\|\mathbf{a}\|^{2}\cos^{2}\phi + |b|^{2}|v|^{2} + 2\Re(bv\mathbf{u}^{t}\mathbf{a}),$   
(A.20)

where  $\phi$  is the angle between **a** and **u**. By observing that  $\|\mathbf{u}\| \le 1, |\nu| \le 1$ , and

$$\Re(b\mathbf{v}\mathbf{u}^{t}\mathbf{a}) \leq |b\mathbf{v}\mathbf{u}^{t}\mathbf{a}| \leq |b||\mathbf{v}|\|\mathbf{u}\|\|\mathbf{a}\| \leq |b|\|\mathbf{a}\| \quad (A.21)$$

one can find an upper bound to (A.20):

$$\|\mathbf{H}x\|^2 \le 1 + \|\mathbf{a}\|^2 + |b|^2 + 2|b| \|\mathbf{a}\|.$$
 (A.22)

By applying (A.22) to (A.19) one obtains that the square of the largest singular value of  $\mathbf{H}^{-1}$  is not larger than

$$\mu = 1 + \frac{\|\mathbf{a}\|^2}{|b|^2} + \frac{1}{|b|^2} + \frac{2\|\mathbf{a}\|}{|b|^2} = \frac{|b|^2 + \|\mathbf{a}\|^2 + 1 + 2\|\mathbf{a}\|}{|b|^2}.$$
(A.23)

Therefore, the square of the smallest singular value of H is not smaller than

$$\frac{1}{\mu} = \frac{|b|^2}{|b|^2 + \|\mathbf{a}\|^2 + 1 + 2\|\mathbf{a}\|}.$$
 (A.24)

In order to prove the left-hand inequality in (13), we will show that the lower bound corresponding to losing all the coefficients of channel *c* cannot be larger than  $\min_{\omega \in [0,2\pi]} |G_c(e^{j\omega})|^2/(1 + T + 2\sqrt{T})$ . If all the coefficients of channel *c* are lost, subframe  $\Phi$  corresponds to a frame obtained by means of an *M/M* filter bank whose polyphase matrix **H** is obtained from the original filter bank polyphase matrix **K** by deleting the *c*th row. According to Lemma A.1, the lower bound of the frame operator corresponding to  $\Phi$  is equal to minimum of  $\sigma_H^2(\omega)$  where  $\sigma_H(\omega)$  is the smallest singular value of  $\mathbf{H}(e^{j\omega})$ . By suitably permuting the column of  $\mathbf{H}$  (such an operation does not change the singular values) one can always bring **H** in the form

$$\mathbf{H}(\omega) = \begin{bmatrix} \mathbf{I} & \mathbf{0} \\ \mathbf{a}(\omega)^t & G_c(e^{j\omega}) \end{bmatrix}.$$
 (A.25)

By applying Lemma A.2 to (A.25) one obtains that for each  $\omega$ ,

$$\sigma_{H}^{2}(\omega) \geq \frac{|G_{c}(e^{j\omega})|^{2}}{|G_{c}(e^{j\omega})|^{2} + ||\mathbf{a}(\omega)^{t}||^{2} + 1 + 2||\mathbf{a}(\omega)^{t}||}.$$
 (A.26)

Finally, in order to prove the claim, we need to find an upper bound for the denominator in (A.26). We have

$$|G_{c}(e^{j\omega})|^{2} + ||\mathbf{a}(\omega)^{t}||^{2} = \sum_{k=0}^{M-1} |G_{k}(e^{j\omega})|^{2} = R(\omega),$$
(A.27)

where  $R(\omega)$  denotes the Fourier transform of the autocorrelation r(n) defined in Property 1. By observing that

$$|R(\omega)| = \left|\sum_{n \in \mathbb{Z}} r(n) \exp(j\omega n)\right| \le \sum_{n \in \mathbb{Z}} |r(n)| = T,$$
(A.28)

one obtains that  $\|\mathbf{a}(\omega)^t\| \leq \sqrt{T}$  and

$$|G_{c}(e^{j\omega})|^{2} + ||\mathbf{a}(\omega)^{t}||^{2} + 1 + 2||\mathbf{a}(\omega)^{t}|| \leq T + 1 + 2\sqrt{T}.$$
(A.29)

By exploiting (A.29) in (A.26) one obtains

$$\sigma_{H}^{2}(\omega) \geq \frac{|G_{c}(e^{j\omega})|^{2}}{|G_{c}(e^{j\omega})|^{2} + ||\mathbf{a}(\omega)^{t}||^{2} + 1 + 2||\mathbf{a}(\omega)^{t}||}$$

$$\geq \frac{|G_{c}(e^{j\omega})|^{2}}{T + 1 + 2\sqrt{T}}.$$
(A.30)

#### REFERENCES

- A. E. Mohr, E. A. Riskin, and R. E. Ladner, "Unequal loss protection: graceful degradation of image quality over packet erasure channels through forward error correction," *IEEE Journal* on Selected Areas in Communications, vol. 18, no. 6, pp. 819– 828, 2000.
- [2] V. K. Goyal, "Multiple description coding: compression meets the network," *IEEE Signal Processing Magazine*, vol. 18, no. 5, pp. 74–93, 2001.
- [3] V. A. Vaishampayan, "Design of multiple description scalar quantizers," *IEEE Transactions on Information Theory*, vol. 39, no. 3, pp. 821–834, 1993.
- [4] Y. Wang, M. T. Orchard, V. A. Vaishampayan, and A. R. Reibman, "Multiple description coding using pairwise correlating transforms," *IEEE Transactions on Image Processing*, vol. 10, no. 3, pp. 351–366, 2001.
- [5] S. Shirani, M. Gallant, and F. Kossentini, "Multiple description image coding using pre- and post-processing," in *Proceedings* of International Conference on Information Technology: Coding and Computing (ITCC '01), pp. 35–39, Las Vegas, Nev, USA, April 2001.
- [6] P. L. Dragotti, S. D. Servetto, and M. Vetterli, "Optimal filter banks for multiple description coding: analysis and synthesis," *IEEE Transactions on Information Theory*, vol. 48, no. 7, pp. 2036–2052, 2002.
- [7] X. Tang and A. Zakhor, "Matching pursuits multiple description coding for wireless video," *IEEE Transactions on Circuits* and Systems for Video Technology, vol. 12, no. 6, pp. 566–575, 2002.
- [8] M. Gallant, S. Shirani, and F. Kossentini, "Standard-compliant multiple description video coding," in *Proceedings of International Conference on Image Processing (ICIP '01)*, vol. 1, pp. 946–949, Thessaloniki, Greece, October 2001.
- [9] O. A. Lotfallah and S. Panchanathan, "Adaptive multiple description coding for internet video," in *Proceedings of IEEE International Conference on Acoustics, Speech, and Signal Processing (ICASSP '03)*, vol. 5, pp. 732–735, Hong Kong, China, April 2003.
- [10] Joint Video Team of ITU-T ISO/IEC JTC 1, "Draft ITU-T Recommendation and Final Draft International Standard of Joint

Video Specification (ITU-T Rec. H.264—ISO/IEC 14496-10 AVC)," Joint Video Team (JVT) of ISO/IEC MPEG and ITU-T VCEG, JVT-G050, March 2003.

- [11] I. E. G. Richardson, H.264 and MPEG-4 Video Compression, John Wiley & Sons, New York, NY, USA, 2003.
- [12] R. Bernardini, M. Durigon, and R. Rinaldo, "Low-delay reconstruction of punctured frame-coded streams," in *Proceedings* of 37th Asilomar Conference on Signals, Systems and Computers, vol. 2, pp. 1519–1523, Pacific Grove, Calif, USA, November 2003.
- [13] R. Bernardini and R. Rinaldo, "Efficient reconstruction from frame-based multiple descriptions," *IEEE Transactions on Signal Processing*, vol. 53, no. 8, part 2, pp. 3282–3296, 2005.
- [14] I. Daubechies, *Ten Lectures on Wavelets*, SIAM, Philadelphia, Pa, USA, 1992.
- [15] R. Rao and S. K. Mitra, *Generalized Inverse of Matrices and Its Applications*, John Wiley & Sons, New York, NY, USA, 1971.
- [16] Z. Cvetković and M. Vetterli, "Oversampled filter banks," *IEEE Transactions on Signal Processing*, vol. 46, no. 5, pp. 1245–1255, 1998.
- [17] F. A. Graybill, Matrices with Applications in Statistics, Wadsworth & Brooks/Cole, Belmont, Calif, USA, 1983.
- [18] M. Vetterli and J. Kovačević, Wavelets and Subband Coding, Signal Processing, Prentice-Hall, Englewood Cliffs, NJ, USA, 1995.
- [19] T. Stockhammer, M. M. Hannuksela, and T. Wiegand, "H.264/ AVC in wireless environments," *IEEE Transactions on Circuits* and Systems for Video Technology, vol. 13, no. 7, pp. 657–673, 2003.
- [20] J. Apostolopoulos, T. Wong, W.-T. Tan, and S. Wee, "On multiple description streaming with content delivery networks," in *Proceedings of 21st Annual Joint Conference of the IEEE Computer and Communications Societies (INFOCOM '02)*, vol. 3, pp. 1736–1745, New York, NY, USA, June 2002.

**R. Bernardini** was born in Genova (Italy) in 1964. He received the "Laurea in Ingegneria Elettronica" degree from the University of Padova in 1990. Since then he has been with the Dipartimento di Elettronica e Informatica, Università di Padova, with a scholarship of the Consorzio Padova Ricerche, and, from November 1992 to November 1995, as a Ph.D. student. He spent the last year of his Ph.D. at formerly AT&T Bell Labs (Murray



Hill). From April 1996 to April 1997 he was in EPFL (Lausanne) as a Postdoctoral Fellow. Now he is working as a researcher in the Dipartimento di Ingegneria Elettrica, Gestionale e Meccanica, Università di Udine. His main interests are in the area of multidimensional signal processing, wavelets, filter banks, and robust transmission.

**M. Durigon** was born in 1976. He graduated in telecomunication engineering from the University of Padova, Italy, in 2002. He is currently a Ph.D. student at the University of Udine, Italy. His research interests include image and video lossless compression, video streaming in lossy environments, and multiple description coding.



**R. Rinaldo** obtained the "Laurea in Ingegneria Elettronica" degree in 1987 from the University of Padova, Padova, Italy. From 1990 to 1992, he was with the University of California at Berkeley, where he received the M.S. degree in 1992. He received the Doctorate degree in "Ingegneria Elettronica e dell'Informazione" from the University of Padova in 1992. In 1992 he joined the Dipartimento di Elettronica e Informat-



ica, Università di Padova, as a "ricercatore." Starting from November 1st 1998, he became an Associate Professor in communications and signal processing in the same department. In November 2001, he became an Associate Professor in the Dipartimento di Ingegneria Elettrica, Gestionale e Meccanica, Università di Udine. Since December 2003, he has been a professor in the same department. His interests are in the field of multidimensional signal processing, video signal coding, fractal theory, and image coding.

**A. Vitali** was born in Bergamo, Italy, in 1971. He received a degree in electronic engineering in 1998 from Politecnico di Milano, Italy. In 1998, he joined ST-Microelectronics' research group on advanced system technologies. He worked on digital receivers and on digital multistandard decoders for analog TV. In 2001 he switched to advanced video algorithms for digital TV, mainly aimed at nonstandard video



compression methods. In the meanwhile he gave several lectures on digital electronics (Politecnico di Pavia, Italy). Since 2002 he has been working on joint source-channel coding, mainly aimed at internet/wireless video streaming. He authored or coauthored several patents and publications. Since 2004, he has been teaching Microelectronics (University of Bergamo). His interests are in pure and applied mathematics.

**P. Zontone** received the Laurea in Electrical Engineering, from the University of Udine, Italy, in 2004. At present, she is working toward the Ph.D. degree in Information and Industrial Engineering at the University of Udine. Her research interests include multidimensional signal processing, joint sourcechannel coding, and video communication in error-prone networks.



## **Special Issue on**

# Transforming Signal Processing Applications into Parallel Implementations

#### **Call for Papers**

There is an increasing need to develop efficient "systemlevel" models, methods, and tools to support designers to quickly transform signal processing application specification to heterogeneous hardware and software architectures such as arrays of DSPs, heterogeneous platforms involving microprocessors, DSPs and FPGAs, and other evolving multiprocessor SoC architectures. Typically, the design process involves aspects of application and architecture modeling as well as transformations to translate the application models to architecture models for subsequent performance analysis and design space exploration. Accurate predictions are indispensable because next generation signal processing applications, for example, audio, video, and array signal processing impose high throughput, real-time and energy constraints that can no longer be served by a single DSP.

There are a number of key issues in transforming application models into parallel implementations that are not addressed in current approaches. These are engineering the application specification, transforming application specification, or representation of the architecture specification as well as communication models such as data transfer and synchronization primitives in both models.

The purpose of this call for papers is to address approaches that include application transformations in the performance, analysis, and design space exploration efforts when taking signal processing applications to concurrent and parallel implementations. The Guest Editors are soliciting contributions in joint application and architecture space exploration that outperform the current architecture-only design space exploration methods and tools.

Topics of interest for this special issue include but are not limited to:

- modeling applications in terms of (abstract) control-dataflow graph, dataflow graph, and process network models of computation (MoC)
- transforming application models or algorithmic engineering
- transforming application MoCs to architecture MoCs
- joint application and architecture space exploration

- joint application and architecture performance analysis
- extending the concept of algorithmic engineering to architecture engineering
- design cases and applications mapped on multiprocessor, homogeneous, or heterogeneous SOCs, showing joint optimization of application and architecture

Authors should follow the EURASIP JASP manuscript format described at http://www.hindawi.com/journals/asp/. Prospective authors should submit an electronic copy of their complete manuscript through the EURASIP JASP manuscript tracking system at http://www.hindawi.com/mts/, according to the following timetable:

Manuscript Due	September 1, 2006		
Acceptance Notification	January 1, 2007		
Final Manuscript Due	April 1, 2007		
Publication Date	3rd Quarter 2007		

#### **GUEST EDITORS:**

**F. Deprettre**, Leiden Embedded Research Center, Leiden University, Niels Bohrweg 1, 2333 CA Leiden, The Netherlands; edd@liacs.nl

**Roger Woods**, School of Electrical and Electronic Engineering, Queens University of Belfast, Ashby Building, Stranmillis Road, Belfast, BT9 5AH, UK; r.woods@qub.ac.uk

**Ingrid Verbauwhede**, Katholieke Universiteit Leuven, ESAT-COSIC, Kasteelpark Arenberg 10, 3001 Leuven, Belgium; Ingrid.verbauwhede@esat.kuleuven.be

**Erwin de Kock**, Philips Research, High Tech Campus 31, 5656 AE Eindhoven, The Netherlands; erwin.de.kock@philips.com

Hindawi Publishing Corporation http://www.hindawi.com

# Special Issue on Video Adaptation for Heterogeneous Environments

#### **Call for Papers**

The explosive growth of compressed video streams and repositories accessible worldwide, the recent addition of new video-related standards such as H.264/AVC, MPEG-7, and MPEG-21, and the ever-increasing prevalence of heterogeneous, video-enabled terminals such as computer, TV, mobile phones, and personal digital assistants have escalated the need for efficient and effective techniques for adapting compressed videos to better suit the different capabilities, constraints, and requirements of various transmission networks, applications, and end users. For instance, Universal Multimedia Access (UMA) advocates the provision and adaptation of the same multimedia content for different networks, terminals, and user preferences.

Video adaptation is an emerging field that offers a rich body of knowledge and techniques for handling the huge variation of resource constraints (e.g., bandwidth, display capability, processing speed, and power consumption) and the large diversity of user tasks in pervasive media applications. Considerable amounts of research and development activities in industry and academia have been devoted to answering the many challenges in making better use of video content across systems and applications of various kinds.

Video adaptation may apply to individual or multiple video streams and may call for different means depending on the objectives and requirements of adaptation. Transcoding, transmoding (cross-modality transcoding), scalable content representation, content abstraction and summarization are popular means for video adaptation. In addition, video content analysis and understanding, including low-level feature analysis and high-level semantics understanding, play an important role in video adaptation as essential video content can be better preserved.

The aim of this special issue is to present state-of-theart developments in this flourishing and important research field. Contributions in theoretical study, architecture design, performance analysis, complexity reduction, and real-world applications are all welcome.

Topics of interest include (but are not limited to):

- Heterogeneous video transcoding
- Scalable video coding
- Dynamic bitstream switching for video adaptation

- Signal, structural, and semantic-level video adaptation
- Content analysis and understanding for video adaptation
- Video summarization and abstraction
- Copyright protection for video adaptation
- Crossmedia techniques for video adaptation
- Testing, field trials, and applications of video adaptation services
- International standard activities for video adaptation

Authors should follow the EURASIP JASP manuscript format described at http://www.hindawi.com/journals/asp/. Prospective authors should submit an electronic copy of their complete manuscript through the EURASIP JASP manuscript tracking system at http://www.hindawi.com/mts/, according to the following timetable:

Manuscript Due	September 1, 2006		
Acceptance Notification	January 1, 2007		
Final Manuscript Due	April 1, 2007		
Publication Date	3rd Quarter 2007		

#### **GUEST EDITORS:**

**Chia-Wen Lin**, Department of Computer Science and Information Engineering, National Chung Cheng University, Chiayi 621, Taiwan; cwlin@cs.ccu.edu.tw

**Yap-Peng Tan**, School of Electrical and Electronic Engineering, Nanyang Technological University, Nanyang Avenue, Singapore 639798, Singapore; eyptan@ntu.edu.sg

**Ming-Ting Sun**, Department of Electrical Engineering, University of Washington, Seattle, WA 98195, USA ; sun@ee.washington.edu

**Alex Kot**, School of Electrical and Electronic Engineering, Nanyang Technological University, Nanyang Avenue, Singapore 639798, Singapore; eackot@ntu.edu.sg **Anthony Vetro**, Mitsubishi Electric Research Laboratories, 201 Broadway, 8th Floor, Cambridge, MA 02138, USA; avetro@merl.com

Hindawi Publishing Corporation http://www.hindawi.com

### **Special Issue on**

# Knowledge-Assisted Media Analysis for Interactive Multimedia Applications

#### **Call for Papers**

It is broadly acknowledged that the development of enabling technologies for new forms of interactive multimedia services requires a targeted confluence of knowledge, semantics, and low-level media processing. The convergence of these areas is key to many applications including interactive TV, networked medical imaging, vision-based surveillance and multimedia visualization, navigation, search, and retrieval. The latter is a crucial application since the exponential growth of audiovisual data, along with the critical lack of tools to record the data in a well-structured form, is rendering useless vast portions of available content. To overcome this problem, there is need for technology that is able to produce accurate levels of abstraction in order to annotate and retrieve content using queries that are natural to humans. Such technology will help narrow the gap between low-level features or content descriptors that can be computed automatically, and the richness and subjectivity of semantics in user queries and high-level human interpretations of audiovisual media.

This special issue focuses on truly integrative research targeting of what can be disparate disciplines including image processing, knowledge engineering, information retrieval, semantic, analysis, and artificial intelligence. High-quality and novel contributions addressing theoretical and practical aspects are solicited. Specifically, the following topics are of interest:

- Semantics-based multimedia analysis
- Context-based multimedia mining
- Intelligent exploitation of user relevance feedback
- Knowledge acquisition from multimedia contents
- Semantics based interaction with multimedia
- Integration of multimedia processing and Semantic Web technologies to enable automatic content sharing, processing, and interpretation
- Content, user, and network aware media engineering
- Multimodal techniques, high-dimensionality reduction, and low level feature fusion

Authors should follow the EURASIP JASP manuscript format described at http://www.hindawi.com/journals/asp/. Prospective authors should submit an electronic copy of their complete manuscript through the EURASIP JASP manuscript tracking system at http://www.hindawi.com/mts/ according to the following timetable:

Manuscript Due	September 1, 2006		
Acceptance Notification	January 15, 2007		
Final Manuscript Due	April 1, 2007		
Publication Date	3rd Quarter, 2007		

#### **GUEST EDITORS:**

**Ebroul Izquierdo**, Department of Electronic Engineering, Queen Mary, University of London, Mile End Road, London E1 4NS, United Kingdom; ebroul.izquierdo@elec.qmul.ac.uk

**Hyoung Joong Kim**, Department of Control and Instrumentation Engineering, Kangwon National University, 192 1 Hyoja2 Dong, Kangwon Do 200 701, Korea; khj@kangwon.ac.kr

**Thomas Sikora**, Communication Systems Group, Technical University Berlin, Einstein Ufer 17, 10587 Berlin, Germany; sikora@nue.tu-berlin.de

Hindawi Publishing Corporation http://www.hindawi.com

# Special Issue on Super-resolution Enhancement of Digital Video

#### **Call for Papers**

When designing a system for image acquisition, there is generally a desire for high spatial resolution and a wide fieldof-view. To achieve this, a camera system must typically employ small f-number optics. This produces an image with very high spatial-frequency bandwidth at the focal plane. To avoid aliasing caused by undersampling, the corresponding focal plane array (FPA) must be sufficiently dense. However, cost and fabrication complexities may make this impractical. More fundamentally, smaller detectors capture fewer photons, which can lead to potentially severe noise levels in the acquired imagery. Considering these factors, one may choose to accept a certain level of undersampling or to sacrifice some optical resolution and/or field-of-view.

In image super-resolution (SR), postprocessing is used to obtain images with resolutions that go beyond the conventional limits of the uncompensated imaging system. In some systems, the primary limiting factor is the optical resolution of the image in the focal plane as defined by the cut-off frequency of the optics. We use the term "optical SR" to refer to SR methods that aim to create an image with valid spatial-frequency content that goes beyond the cut-off frequency of the optics. Such techniques typically must rely on extensive a priori information. In other image acquisition systems, the limiting factor may be the density of the FPA, subsequent postprocessing requirements, or transmission bitrate constraints that require data compression. We refer to the process of overcoming the limitations of the FPA in order to obtain the full resolution afforded by the selected optics as "detector SR." Note that some methods may seek to perform both optical and detector SR.

Detector SR algorithms generally process a set of lowresolution aliased frames from a video sequence to produce a high-resolution frame. When subpixel relative motion is present between the objects in the scene and the detector array, a unique set of scene samples are acquired for each frame. This provides the mechanism for effectively increasing the spatial sampling rate of the imaging system without reducing the physical size of the detectors.

With increasing interest in surveillance and the proliferation of digital imaging and video, SR has become a rapidly growing field. Recent advances in SR include innovative algorithms, generalized methods, real-time implementations, and novel applications. The purpose of this special issue is to present leading research and development in the area of super-resolution for digital video. Topics of interest for this special issue include but are not limited to:

- Detector and optical SR algorithms for video
- Real-time or near-real-time SR implementations
- Innovative color SR processing
- Novel SR applications such as improved object detection, recognition, and tracking
- Super-resolution from compressed video
- Subpixel image registration and optical flow

Authors should follow the EURASIP JASP manuscript format described at http://www.hindawi.com/journals/asp/. Prospective authors should submit an electronic copy of their complete manuscript through the EURASIP JASP manuscript tracking system at http://www.hindawi.com/mts/, according to the following timetable:

Manuscript Due	September 1, 2006		
Acceptance Notification	February 1, 2007		
Final Manuscript Due	April 15, 2007		
Publication Date	3rd Quarter, 2007		

#### **GUEST EDITORS:**

**Russell C. Hardie**, Department of Electrical and Computer Engineering, University of Dayton, 300 College Park, Dayton, OH 45469-0026, USA; rhardie@udayton.edu

**Richard R. Schultz**, Department of Electrical Engineering, University of North Dakota, Upson II Room 160, P.O. Box 7165, Grand Forks, ND 58202-7165, USA; RichardSchultz@mail.und.nodak.edu

**Kenneth E. Barner**, Department of Electrical and Computer Engineering, University of Delaware, 140 Evans Hall, Newark, DE 19716-3130, USA; barner@ee.udel.edu

### **Special Issue on**

# Advanced Signal Processing and Computational Intelligence Techniques for Power Line Communications

#### **Call for Papers**

In recent years, increased demand for fast Internet access and new multimedia services, the development of new and feasible signal processing techniques associated with faster and low-cost digital signal processors, as well as the deregulation of the telecommunications market have placed major emphasis on the value of investigating hostile media, such as powerline (PL) channels for high-rate data transmissions.

Nowadays, some companies are offering powerline communications (PLC) modems with mean and peak bit-rates around 100 Mbps and 200 Mbps, respectively. However, advanced broadband powerline communications (BPLC) modems will surpass this performance. For accomplishing it, some special schemes or solutions for coping with the following issues should be addressed: (i) considerable differences between powerline network topologies; (ii) hostile properties of PL channels, such as attenuation proportional to high frequencies and long distances, high-power impulse noise occurrences, time-varying behavior, and strong inter-symbol interference (ISI) effects; (iv) electromagnetic compatibility with other well-established communication systems working in the same spectrum, (v) climatic conditions in different parts of the world; (vii) reliability and QoS guarantee for video and voice transmissions; and (vi) different demands and needs from developed, developing, and poor countries.

These issues can lead to exciting research frontiers with very promising results if signal processing, digital communication, and computational intelligence techniques are effectively and efficiently combined.

The goal of this special issue is to introduce signal processing, digital communication, and computational intelligence tools either individually or in combined form for advancing reliable and powerful future generations of powerline communication solutions that can be suited with for applications in developed, developing, and poor countries.

Topics of interest include (but are not limited to)

- Multicarrier, spread spectrum, and single carrier techniques
- Channel modeling

- Channel coding and equalization techniques
- Multiuser detection and multiple access techniques
- Synchronization techniques
- Impulse noise cancellation techniques
- FPGA, ASIC, and DSP implementation issues of PLC modems
- Error resilience, error concealment, and Joint sourcechannel design methods for video transmission through PL channels

Authors should follow the EURASIP JASP manuscript format described at the journal site http://asp.hindawi.com/. Prospective authors should submit an electronic copy of their complete manuscripts through the EURASIP JASP manuscript tracking system at http://www.hindawi.com/mts/, according to the following timetable:

Manuscript Due	October 1, 2006		
Acceptance Notification	January 1, 2007		
Final Manuscript Due	April 1, 2007		
Publication Date	3rd Quarter, 2007		

#### **GUEST EDITORS:**

**Moisés Vidal Ribeiro**, Federal University of Juiz de Fora, Brazil; mribeiro@ieee.org

Lutz Lampe, University of British Columbia, Canada; lampe@ece.ubc.ca

Sanjit K. Mitra, University of California, Santa Barbara, USA; mitra@ece.ucsb.edu

**Klaus Dostert**, University of Karlsruhe, Germany; klaus.dostert@etec.uni-karlsruhe.de

Halid Hrasnica, Dresden University of Technology, Germany hrasnica@ifn.et.tu-dresden.de

Hindawi Publishing Corporation http://asp.hindawi.com

## **Special Issue on**

# Numerical Linear Algebra in Signal Processing Applications

#### **Call for Papers**

The cross-fertilization between numerical linear algebra and digital signal processing has been very fruitful in the last decades. The interaction between them has been growing, leading to many new algorithms.

Numerical linear algebra tools, such as eigenvalue and singular value decomposition and their higher-extension, least squares, total least squares, recursive least squares, regularization, orthogonality, and projections, are the kernels of powerful and numerically robust algorithms.

The goal of this special issue is to present new efficient and reliable numerical linear algebra tools for signal processing applications. Areas and topics of interest for this special issue include (but are not limited to):

- Singular value and eigenvalue decompositions, including applications.
- Fourier, Toeplitz, Cauchy, Vandermonde and semiseparable matrices, including special algorithms and architectures.
- Recursive least squares in digital signal processing.
- Updating and downdating techniques in linear algebra and signal processing.
- Stability and sensitivity analysis of special recursive least-squares problems.
- Numerical linear algebra in:
  - Biomedical signal processing applications.
  - Adaptive filters.
  - Remote sensing.
  - Acoustic echo cancellation.
  - Blind signal separation and multiuser detection.
  - Multidimensional harmonic retrieval and direction-of-arrival estimation.
  - Applications in wireless communications.
  - Applications in pattern analysis and statistical modeling.
  - Sensor array processing.

Authors should follow the EURASIP JASP manuscript format described at http://www.hindawi.com/journals/asp/. Prospective authors should submit an electronic copy of their complete manuscript through the EURASIP JASP manuscript tracking system at http://www.hindawi.com/mts/, according to the following timetable:

Manuscript Due	October 1, 2006		
Acceptance Notification	February 1, 2007		
Final Manuscript Due	May 1, 2007		
Publication Date	3rd Quarter, 2007		

#### **GUEST EDITORS:**

**Shivkumar Chandrasekaran**, Department of Electrical and Computer Engineering, University of California, Santa Barbara, USA; shiv@ece.ucsb.edu

**Gene H. Golub**, Department of Computer Science, Stanford University, USA; golub@sccm.stanford.edu

Nicola Mastronardi, Istituto per le Applicazioni del Calcolo "Mauro Picone," Consiglio Nazionale delle Ricerche, Bari, Italy; n.mastronardi@ba.iac.cnr.it

**Marc Moonen**, Department of Electrical Engineering, Katholieke Universiteit Leuven, Belgium; marc.moonen@esat.kuleuven.be

**Paul Van Dooren**, Department of Mathematical Engineering, Catholic University of Louvain, Belgium; vdooren@csam.ucl.ac.be

**Sabine Van Huffel**, Department of Electrical Engineering, Katholieke Universiteit Leuven, Belgium; sabine.vanhuffel@esat.kuleuven.be

Hindawi Publishing Corporation http://www.hindawi.com