

# Exploiting W. Ellison model for seawater communication at gigahertz frequencies based on world ocean atlas data

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Electromagnetic (EM) waves used to send signals under seawater are normally restricted to low frequencies ( $f$ ) because of sudden exponential increases of attenuation ( $\alpha$ ) at higher  $f$ . The mathematics of EM wave propagation in seawater demonstrate dependence on relative permeability ( $\mu_r$ ), relative permittivity ( $\epsilon_r$ ), conductivity ( $\sigma$ ), and  $f$  of transmission. Estimation of  $\epsilon_r$  and  $\sigma$  based on the W. Ellison interpolation model was performed for averaged real-time data of temperature ( $T$ ) and salinity ( $S$ ) from 1955 to 2012 for all oceans with 41 088 latitude/longitude points and 101 depth points up to 5500 m. Estimation of parameters such as real and imaginary parts of  $\epsilon_r$ ,  $\epsilon_r'$ ,  $\epsilon_r''$ ,  $\sigma$ , loss tangent ( $\tan \delta$ ), propagation velocity ( $V_p$ ), phase constant ( $\beta$ ), and  $\alpha$  contributes to absorption loss ( $L_a$ ) for seawater channels carried out by using normal distribution fit in the 3 GHz–40 GHz  $f$  range. We also estimated total path loss ( $L_{PL}$ ) in seawater for given transmission power  $P_t$  and antenna (dipole) gain. MATLAB is the simulation tool used for analysis.

## KEYWORDS

absorption loss ( $L_a$ ), normal distribution fit, seawater, total path loss ( $L_{PL}$ ), W. Ellison interpolation model

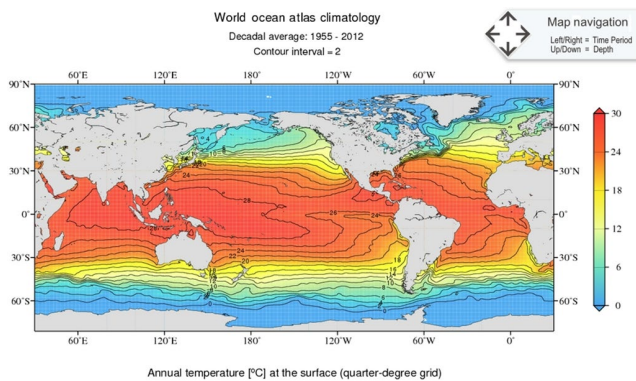
## 1 | INTRODUCTION

The oldest known application of electromagnetic (EM) waves in seawater is the magnetic compass used for navigation. EM sources such as dipoles, loop antennas, and so on, and sensors are useful tools found in many diverse areas of oceanographic study such as physical oceanography, seafloor geophysics, marine chemistry, and marine biology. Advanced development of EM wave applications within these scientific disciplines has also been applied to emerging seawater navigation engineering systems. Applications include oil and gas exploitation and recovery, commercial fishing, weather

prediction, tsunami warning, and underwater wireless communication technology [1]. EM communication also has important applications in geophysical surveys and investigation of the seafloor. Acoustic waves with low propagation velocities ( $\sim 1500$  m/s) can travel long distances in seawater with minimum attenuation. However, EM waves in seawater provide higher data rates at short ranges, with reliable communication across the sea/air boundary. Maxwell's equations regarding the electric and magnetic field properties in a conducting medium (seawater) have helped develop mathematical descriptions of EM fields using dipole sources within seawater [2].

The strong covalent bond between hydrogen ( $H$ ) and oxygen ( $O$ ) atoms in seawater molecules cause no free electrons in the conduction band until they jump to a higher energy level upon application of a high-amplitude electric field,  $E$ . Fresh water, which has a lower  $\sigma$  value than seawater ( $\sim 0.01$  S/m), undergoes dielectric breakdown upon application of an electric field of a few megavolts per centimeter (MV/cm). This dielectric breakdown creates an electric arc. However, the salt in seawater dissociates into positive and negative ions, making seawater a good electric conductor at all  $E$  field levels. Seawater with an applied  $E$  can be treated as a conductor with  $\sigma$  ranging from  $\sim 2.5$  S/m in cold deep waters to  $\sim 6$  S/m in very warm waters [3]. The value of  $\sigma$  typically used in the literature for open ocean is  $\approx 4$  S/m. Seawater is also considered non-magnetic due to its permeability,  $\mu$  (H/m), which is the same as that of free space ( $\mu_0 = 4\pi \times 10^{-7}$ ) H/m [4].

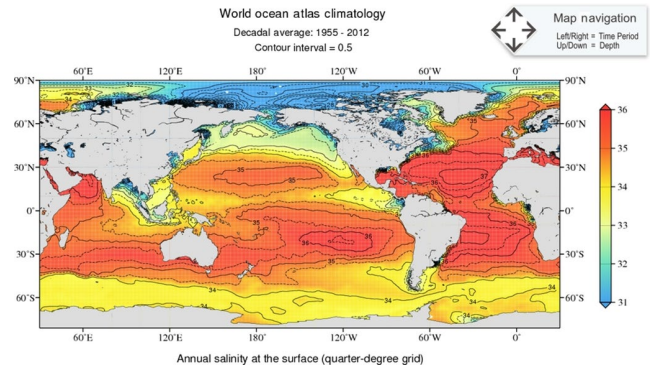
In the tropics, where there is an excess of primarily short waves from incoming solar radiation as compared to outgoing long-wave radiation, the surface waters are warmer (with a maxima of  $25^\circ\text{C}$  to  $30^\circ\text{C}$ ) than those at adjacent latitudes. In contrast, surface waters at higher latitudes are cooler, with the freezing point of seawater around  $-2^\circ\text{C}$ . The waters in these latitudes are cooler because energy lost to the atmosphere and outer space by outgoing long-wave radiation exceeds incoming solar radiation. Figure 1 shows global ocean surface temperatures, reflecting tropical warming and polar cooling. However, the distribution of  $T$  with latitude varies zonally due to variations of general oceanographic circulation patterns with the seasons. Historically, the ocean's  $S$  value was determined by chemical titration of a sample collected in a bottle lowered on a wire from ship. In the 1970s, considerable research was conducted on both the definition and measurement of  $\sigma$  to state seawater  $S$ . Technological advancements helped in measuring  $S$ , which



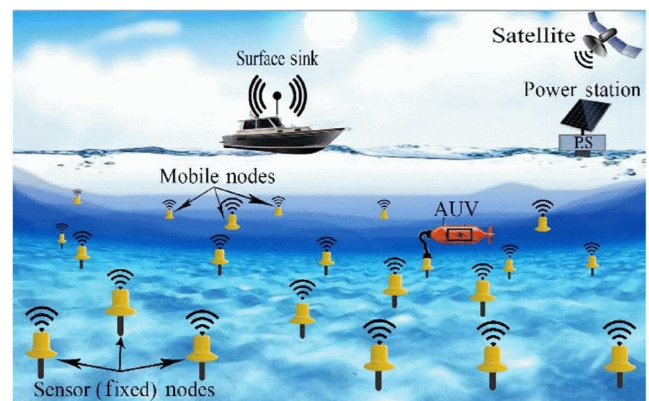
**FIGURE 1** Mean seawater surface temperature  $T$  ( $^\circ\text{C}$ ) averaged from 1955 to 2012. Mishonov, Alexey National Center for Atmospheric Research Staff (Eds). Last modified 13 October 2016. "The Climate Data Guide: World Ocean Atlas 2013 (WOA13)." Retrieved from <https://climatedataguide.ucar.edu/climate-data/world-ocean-atlas-2013-woa13>

was averaged from 1955 to 2012. The results are depicted in Figure 2 [5].

Acoustic waves are a major source for seawater communications and for tracking and telemetry applications. There are no alternatives to acoustic waves in long-range  $R$  (meters) applications, in spite of drawbacks such as multipath fading, narrow bandwidth, and susceptibility to propagation characteristics from background media such as animal noises and noise near the surface of the ocean from the movement of ships. Underwater electromagnetic wave (EMW) communication in the 100-m range was studied for half a century before 1970 using low-frequency underwater modems. High-frequency (GHz) EMWs can propagate through seawater with low damping to compensate for the shortcomings of acoustic waves considering the digital technology revolution in last few decades [6]. Figure 3 shows underwater wireless communication (UWC) architecture in a seawater environment. Sensor nodes can be both mobile and static and can deliver information data



**FIGURE 2** Mean seawater surface  $S$  (ppt) averaged from 1955 to 2012. Mishonov, Alexey National Center for Atmospheric Research Staff (Eds). Last modified 13 October 2016. "The Climate Data Guide: World Ocean Atlas 2013 (WOA13)." Retrieved from <https://climatedataguide.ucar.edu/climate-data/world-ocean-atlas-2013-woa13>



**FIGURE 3** UWC network architecture. © 2018 IEEE. Reprinted with permission from [M. Mostafa et al., *A comparative study on underwater communications for enabling C/U plane splitting based hybrid UWSN*, in Proc. IEEE Wireless Commun. Netw. Conf. (Barcelona, Spain), Apr. 2018]

to mobile autonomous underwater vehicles (AUVs) that establish an offshore link with the surface sink (the ship) [7].

## 2 | LITERATURE REVIEW AND MOTIVATION

Acoustic waves can travel at 1500 m/s, much slower than the propagation speed ( $V_p$ ) of EM waves in seawater, which is approximately  $3 \times 10^7$  m/s. This causes channel latency and Doppler effects for traveling acoustic signals. Oceans act as a waveguide for acoustic signals as they provide boundaries by the upper surface and the sea floor. Consequently, reflections from these surfaces must be considered and shadow zones need to be addressed. The main advantage of acoustic communication is its ability to propagate over large distances, which makes it a frequently used and successful communication technique [8]. Optical signals are also a mode of communication in seawater; however, they are generally used only for short-range data transfer. Their use is being explored in shallow waters (~100 m) where acoustic communication seems to be less effective due to manmade noise near the surface of the ocean. Optical signals can provide higher bandwidths and higher data rates as compared to acoustic signals. The main limitations for optical signals include rapid attenuation ( $\alpha$ ) and the scattering effect of particles suspended in seawater [9].

Underwater wireless sensor networks (UWSNs) are combinations of sensors used to monitor physical or environmental phenomena such as humidity, temperature, sound, vibration, pressure, or motion. Data are cooperatively passed through this network of sensors to a main sink. UWSNs are becoming smaller and cheaper to use for EM signaling. Because of the high attenuation of EM signals in seawater, UWSNs rely on sonic transducers for wireless communication. The use of more nodes to overcome high path loss ( $L_{PL}$ ) and attenuation in seawater contributes to the higher cost of EM signaling. EM waves reduce latency due to faster propagation and provide high data rates due to the high frequency of transmitted EM waves. Antennas for EM wave propagation in seawater must meet a number of requirements to overcome high path loss. For example, they must have high gain for both the transmitter and the receiver ( $G_T$  and  $G_R$ , respectively), that is, above 10 dB, and they must be small so that they can be fitted on a sensor surface. Most common antennas used for seawater communication using EM signals are bow-tie antennas, dipoles, loops, and so on [10].

Significant advantages of EM propagation across seawater include an efficient antenna system that can be easily transported in compact units and immunity to acoustic noise and low-visibility areas. Over the past decade, digital technology has rapidly improved, leading to high data-rate

communication systems such as Bluetooth that make valuable use of high bandwidth and short-range technologies [11]. Major examples of these applications are communication between unmanned underwater vehicles (UUVs), submarines, or surface vessels, as well as diving communication and navigation. [12]

EM waves traveling in seawater in a positive  $z$ -direction are governed by Maxwell's equations. The electric ( $E$ ) and magnetic ( $H$ ) fields are described as follows in (1) and (2), respectively: [13]

$$E_x = E_0 e^{j\omega t - \gamma z} \quad (1)$$

and

$$H_y = H_0 e^{j\omega t - \gamma z}. \quad (2)$$

The propagation constant ( $\gamma$ ) of a medium, which depends on frequency ( $f$ ), conductivity ( $\sigma$ ), permittivity ( $\epsilon$ ), and permeability ( $\mu$ ) is presented in (3) [13].

$$\gamma = j\omega \sqrt{\mu_0 \mu_r (\epsilon_0 \epsilon_r - j\sigma/\omega)} = \alpha + j\beta. \quad (3)$$

Here,  $\alpha$  (Np/m) represents the attenuation factor and  $\beta$  (rad/m) represents the phase factor for traveling EM waves in seawater. For seawater,  $\mu_r$  is 1, which leaves us with only two variables in the analysis of  $\gamma$ . Returning to (3), there are two solutions, depending on the transition frequency,  $f_T = \omega_T/2\pi$ . The first is a solution for the conduction band, where the ratio of the conductivity and transmitted frequency is greater than the permittivity of seawater ( $\sigma/\omega > \epsilon$ ), and the second is for the dielectric band, where the ratio of the conductivity and transmitted frequency is less than the permittivity of seawater ( $\sigma/\omega < \epsilon$ ) [14]. Debye's theory describes the relationship between the relative permittivity,  $\epsilon_r$ , and the frequency,  $f$ , of EM waves in seawater. Debye makes the following assumptions [15]: (a) Water molecules are free and do not interact with each other; and (b) polarization contains induced and oriented components. The Debye model for  $\epsilon_r$  is described as follows: [15]

$$\epsilon_r = \epsilon_r' - \epsilon_r'' = \epsilon_\infty + (\epsilon_s - \epsilon_\infty / (1 + j\omega\tau)) + j\sigma/\omega\epsilon_0. \quad (4)$$

Here,  $\epsilon_\infty$  equals  $\epsilon$  at optical frequencies,  $\epsilon_0$  represents static  $\epsilon$ , and  $\tau$  is the relaxation time (s).  $\epsilon_r'$  represents the real part of  $\epsilon_r$  and  $\epsilon_r''$  represents the imaginary part of  $\epsilon_r$ ;  $\sigma$  is the ionic conductivity. The relaxation time,  $\tau$ , taken by the dielectric to reach a state of equilibrium is defined by (5) [13].

$$\tau = \epsilon/\sigma. \quad (5)$$

The conductivity,  $\sigma$ , of seawater is a function of  $T$  ( $^\circ\text{C}$ ) and  $S$  (ppt), denoted as  $\sigma(T \cdot S)$  for a given range  $-2 \text{ }^\circ\text{C} \leq T \leq 30 \text{ }^\circ\text{C}$

and  $20 \text{ ppt} \leq S \leq 40 \text{ ppt}$ , which leads to straightforward interpolation functions as represented in (6)–(10) [15].

$$\sigma(T, S) = c_1(T) + c_2(T)S. \quad (6)$$

The coefficients  $c_1$  and  $c_2$  are given in (7) and (8), respectively [15].

$$c_1(T) = 0.086 + 0.030T - 4.121 \times 10^{-4}T^2 \quad (7)$$

and

$$c_2(T) = 0.077 + 0.001T + 1.937 \times 10^{-5}T^2. \quad (8)$$

For  $f$  in the range of  $3 \text{ GHz} \leq f \leq 40 \text{ GHz}$ ,  $T$  in range  $-2 \text{ }^\circ\text{C} \leq T \leq 30 \text{ }^\circ\text{C}$ , and  $S$  (ppt) in the range  $20 \text{ ppt} \leq S \leq 40 \text{ ppt}$ . The  $\epsilon_r$  value of seawater, denoted as  $\epsilon_r(f \cdot T \cdot S)$ , is given with a precision of about 3% based on the W. Ellison model; it is described in terms of  $\epsilon'_r$  and  $\epsilon''_r$  in (9) and (10), respectively [15].

$$\epsilon'_r(f, T, S) = \epsilon_\infty(T, S) + (\epsilon_s(T, S) - \epsilon_\infty(T, S)) / (1 + 4\Pi^2 f^2 \tau^2(T, S)) \quad (9)$$

and

$$\epsilon''_r(f, T, S) = ((\epsilon_s(T, S) - \epsilon_\infty(T, S)) 2\Pi f \tau(T, S)) / (1 + 4\Pi^2 f^2 \tau^2(T, S)) + \sigma(T, S) / 2\Pi \epsilon_0 f. \quad (10)$$

Here,  $\epsilon_0 = 8.8419 \times 10^{-12} \text{ F/m}$ ,  $\epsilon_s$  and  $\tau$  for the given range are defined in (11) and (12), respectively [15].

$$\epsilon_s(T, S) = a_1(T) + S a_2(T) \quad (11)$$

and

$$\tau(T, S) = b_1(T) + S b_2(T). \quad (12)$$

The estimated coefficients  $a_i(t)$  and  $b_i(t)$  for  $i = 1, 2$  by least square regression analysis are described in (13)–(16) [15].

$$a_1(T) = 81.820 - 0.060T - 0.031T^2 + 0.003T^3 - 1.179 \times 10^{-4}T^4 + 1.483 \times 10^{-6}T^5, \quad (13)$$

$$a_2(T) = 0.125 + 0.009T - 9.55 \times 10^{-4}T^2 + 9.88 \times 10^{-5}T^3 - 3.061 \times 10^{-6}T^4 + 4.713 \times 10^{-8}T^5, \quad (14)$$

$$b_1(T) = 17.303 - 0.666T + 0.005T^2 + 0.001T^3 - 5.032 \times 10^{-5}T^4 + 5.827 \times 10^{-7}T^5, \quad (15)$$

$$b_2(T) = -0.006 + 2.357 \times 10^{-4}T + 5.076 \times 10^{-4}T^2 - 6.398 \times 10^{-5}T^3 + 2.463 \times 10^{-4}T^4 - 3.067 \times 10^{-8}T^5. \quad (16)$$

The interpolation function for  $\epsilon_\infty(T, S)$  is given in (17) [15].

$$\epsilon_\infty(T, S) = 6.458 - 0.042T - 0.006T^2 + 6.492 \times 10^{-4}T^3 - 1.232 \times 10^{-5}T^4 + 5.043 \times 10^{-8}T^5. \quad (17)$$

The terms  $\alpha$  and  $\beta$  depend on the dielectric properties of seawater given by Helmholtz model, formulated in (18) and (19), respectively, as [16]

$$\alpha = 2\pi / \lambda_0 \sqrt{1/2\epsilon' \left( \sqrt{1 + (\epsilon''/\epsilon')^2} - 1 \right)} \quad (18)$$

and

$$\beta = 2\pi / \lambda_0 \sqrt{1/2\epsilon' \left( \sqrt{1 + (\epsilon''/\epsilon')^2} + 1 \right)}. \quad (19)$$

Here,  $\lambda_0$  represents the free-space wavelength ( $c/f$ ).

The term  $\tan(\delta)$  is an important factor that describes the characteristics of a material (lossy or dielectric) and  $v_p$  is the propagation velocity in seawater. [13]

$$\tan(\delta) = \sigma / \omega \epsilon \quad (20)$$

and

$$v_p = \omega / \beta. \quad (21)$$

The penetration depth  $d_p$  for lossy material (seawater) can be estimated as [13]

$$d_p = 1/\alpha. \quad (22)$$

Finally, the overall path loss in seawater,  $L_{\text{PL}}$ , can be estimated as a combination of absorption loss  $L_a$  and free-space loss  $L_0$ , as depicted in (22) and (23), respectively. Here,  $P_T$  and  $P_R$  represent the transmitter and receiver power, respectively,  $G_T$  and  $G_R$  represent the transmitter and receiver antenna gains, respectively. The first part of equation represents the free-space loss,  $L_0$ , and the other part represents the absorption loss,  $L_a$ . The overall path loss,  $L_{\text{PL}}$ , can be depicted as the difference between the transmitter and receiver power  $P_R - P_T$ . Similarly,  $d$  represents the separation between the transmitter and receiver and the  $\lambda$  propagation wavelength of the signal transmitted [13].

$$P_R = P_T G_T G_R (\lambda / 4\pi d)^2 \times e^{-2\alpha d} = P_{TG_T G_R \times L_0 \times L_a} \quad (23)$$

and

$$L_{\text{PL}} (\text{dB}) = P_T (\text{dBm}) + G_{T,R} (\text{dB}) - 20 \log(4\pi d / \lambda) - 20 \log(e^{\alpha d}). \quad (24)$$

The absorption of EM waves in the gigahertz range occurs due to the dielectric properties of seawater. This can help us examine a method for frequency control in applications such as submarine to satellite and radar communication. It also confirms possibilities of the absorption band and how a low  $\sigma$  value can absorb EM waves across a wide frequency band [17]. The terms  $\epsilon_r$  and  $\sigma$  rapidly change in gigahertz frequency ranges, which motivated us to estimate accurate values for the given parameters across all latitude/longitude points for multiple depths of seawater. There are application areas that require perfect absorption of EM waves, such as military appliances, warships, and communication facilities, which should not be detected by radar in the gigahertz range. Radars generally determine the location of a target by absorbing EM waves and measuring their reflection from the surroundings. A new type of absorber suggested in research is seawater at a gigahertz frequency. These types of applications led us to estimate  $\epsilon_r$  and  $\sigma$ , which contributes to the  $\alpha$  value of the EM signal in seawater. The term  $\tan \delta$  determines the characteristics of seawater (Conductor, insulator, or dielectric) at multiple frequencies.

### 3 | SIMULATION RESULTS AND DISCUSSION

We analyzed the performance of the W. Ellison model based on real-time data averaged across multiple decades from 1955 to 2012 by using a normal distribution fit. We evaluated the performance of  $\sigma$  and  $\epsilon_r$  in seawater depths from 5 m to 5500 m, along with  $L_{PL}$  versus an achievable distance in seawater. The simulation parameters are depicted in Table 1.

Figure 4 clearly indicates that we cannot assume constant  $T = 20^\circ\text{C}$  for oceans. The figure shows  $T$  on the y-axis and the number of occurrences with normal distribution fit (NDF) along the x-axis. We can see that  $T$  remains approximately constant between  $-2^\circ\text{C}$  and  $2^\circ\text{C}$  up to a depth of 400 m. As we go deeper than 400 m, we can see that  $T$  starts to increase linearly to  $30^\circ\text{C}$ . From a depth of 2500 m,  $T$  starts

to decrease linearly up to approximately 3500 m. From there to a depth of 5500 m, it remains constant again in the range from  $-2^\circ\text{C}$  to  $2^\circ\text{C}$ , with the greatest number of occurrences between  $10^\circ\text{C}$  and  $30^\circ\text{C}$ .

Figure 5 shows the  $S$  averaged data between 1955 and 2012 at different depth points (101) up to 5500 m. From the

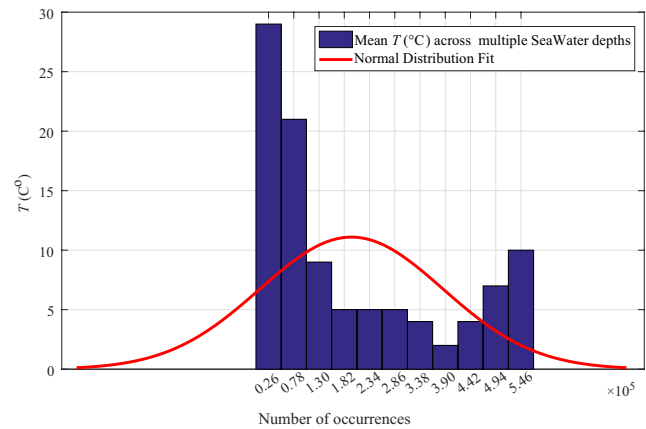


FIGURE 4  $T$  ( $^\circ\text{C}$ ) for various seawater depths with NDF

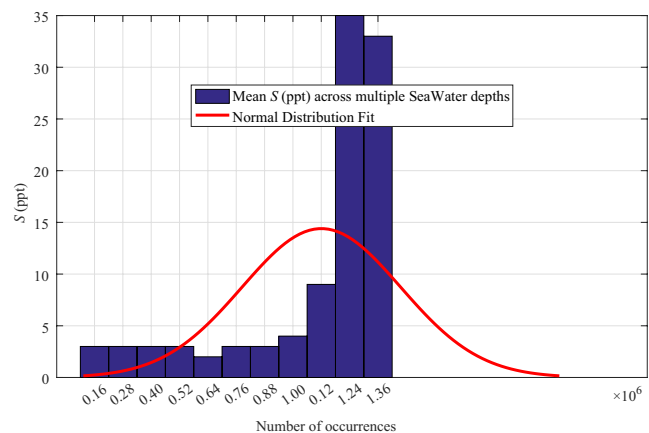


FIGURE 5  $S$  values (ppt) for various seawater depths with NDF

TABLE 1 Simulation parameters

Oceans	Indian, Southern, Pacific, Atlantic, Arctic
Seawater depth (m)	5 to 5500
Seawater depth points	101 (distributed non-uniformly)
Latitude/Longitude	(0 to $\pm 90$ )/ (0 to $\pm 180$ )
Latitude/Longitude Points	41 088
Frequency range for analysis	$3\text{ GHz} \leq f \leq 49\text{ GHz}$
$P_T$ for analysis	30 dBm
$G_{T,R}$ for analysis	10

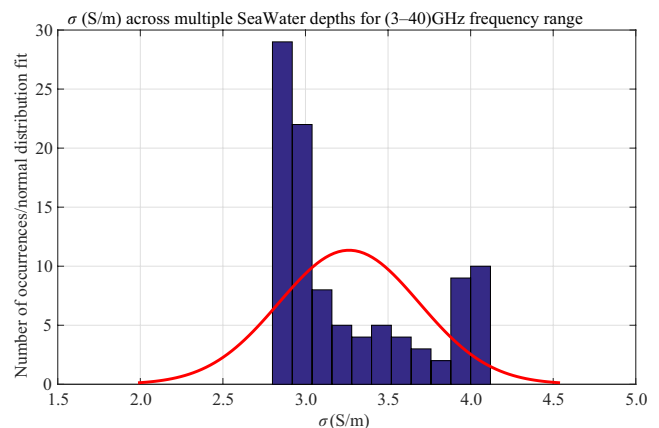
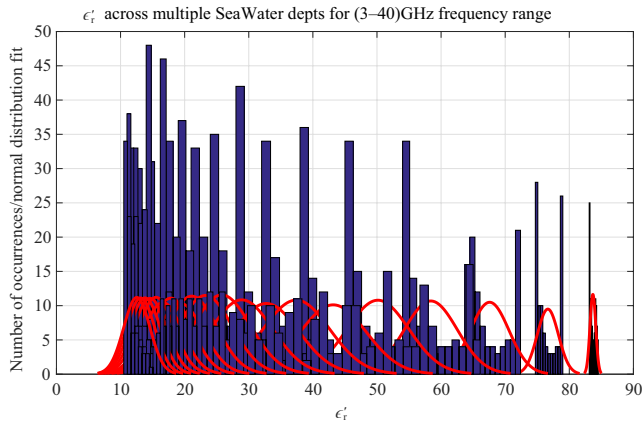


FIGURE 6  $\sigma$  values (S/m) for various depths of seawater with NDF

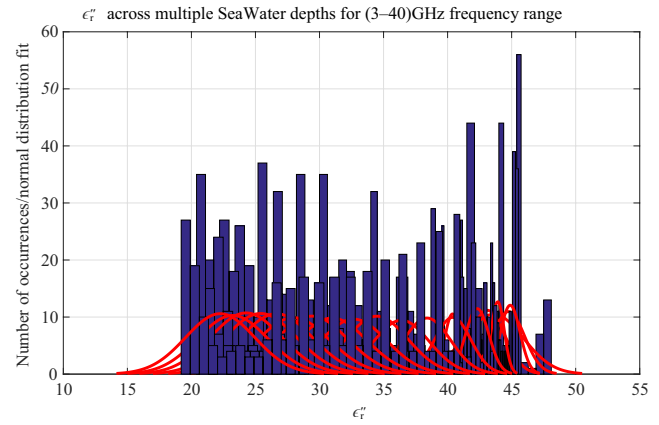


**FIGURE 7**  $\epsilon'_r$  values for various depths of seawater with NDF

seawater surface to a depth of 2000 m, the  $S$  value remained steady at around 35 ppt. From 2000 m up to 5500 m,  $S$  spreads in a non-uniform pattern between 5 ppt and 35 ppt. This is a clear deviation from standard assumption of  $S$ . It also defines characteristics at random seawater depths in nature.

Figure 6 shows  $\sigma$  values with NDF along multiple seawater depths estimated based on (6). It also shows variation of  $\sigma$  (S/m) with frequency with mean value of  $\sigma$  (S/m) between (2.8 to 4.2).  $\epsilon'_r$  defines the energy dissipation of  $E$  (V/m) due to seawater molecule polarization which is normally assumed ( $\approx 81$ ) at all frequencies and ocean depths. Figure 7 clearly indicates that  $\epsilon'_r$  cannot be assumed constant across all seawater depths and frequency ranges (3 GHz to 40 GHz) estimated using the model given in (9). At 3 GHz,  $\epsilon'_r$  is approximately 85, and as the seawater depth increases, it goes to 10. Similarly, we see at 40 GHz that the seawater surface  $\epsilon'_r$  is approximately 18. As the depth of seawater increases, it reaches a minimum value of 10.

$\epsilon''_r$  represents the loss in energy due to the conductivity of seawater and the vibration of seawater molecules when subjected to an electric field. In Figure 8, we can see that  $\epsilon''_r$  changes both with depth and frequency based on (10). At 3 GHz,  $\epsilon''_r$  is approximately 48 at the seawater surface. As we go deeper, it starts decreasing and reaches a minimum value of 3 at 5500 m. At 40 GHz, the value of  $\epsilon''_r$  varies from 25 to 2 in extreme depths. Figure 8 also depicts the



**FIGURE 8**  $\epsilon''_r$  values for various seawater depths with NDF

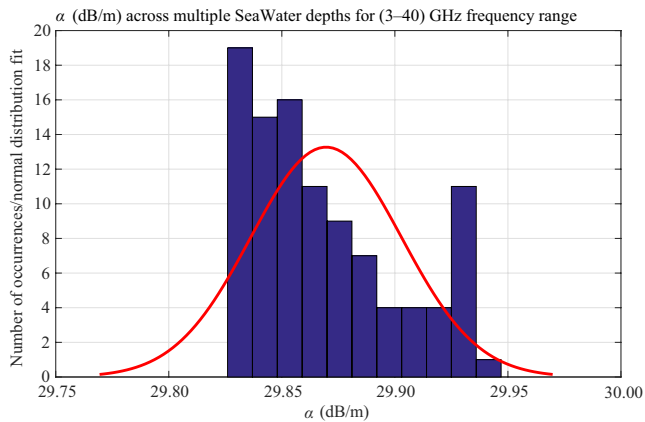
low-frequency behavior of seawater, which is close to that of a conductor. As the frequency increases, seawater behaves like an insulator.

Table 2 shows values for the estimated parameters  $\alpha$ ,  $\sigma$ ,  $V_p$ ,  $d_p \approx 1/\alpha$ ,  $\tan \delta$ ,  $\epsilon''_r$ , and  $\epsilon'_r$  for a 5-m depth at multiple frequencies. It also includes the 3.1 GHz frequency for Wi-Fi communication in seawater. Figure 9 shows  $\alpha$  values estimated based on the Helmholtz model mentioned for (18) using real-time data of all oceans (Indian, Pacific, Southern, Atlantic, and Arctic) averaged between 1955 and 2012. The value of  $\alpha$  remains approximately constant up to 4000 m; beyond this up to 5500 m, it starts to decrease. For 3 GHz at the seawater surface,  $\alpha$  is 20 dB/m, and as we go deeper, it is nearly 14. Similarly, for 40 GHz at the surface,  $\alpha$  is 34 dB/m; at the extreme depth point, it is 27 dB/m. At low frequencies, the gap between  $\alpha$  values is large as compared to higher frequencies.

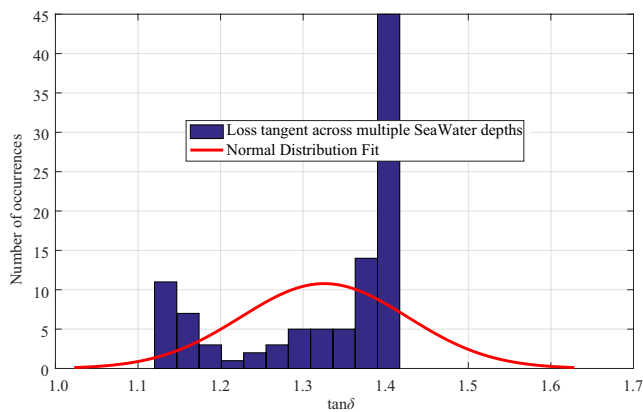
The loss tangent ( $\tan \delta$ ) parameter of a dielectric material quantifies its inherent dissipation of EM energy. It is an important factor for recognizing the type of material, whether it is a lossy dielectric, a lossless dielectric, or good conductor. In Figure 10, we estimated  $\tan \delta$  based on (20) at multiple frequencies. Across seawater depths up to 500 m,  $\tan \delta$  increases linearly. As we go deeper,  $\tan \delta$  remains approximately constant. The seawater surface range of  $\tan \delta$  is 0.46–1.85, and at extreme seawater depths it is 0.45 to 1.82. At 3 GHz, the initial value

**TABLE 2** Estimated parameters for 5-m depth at multiple frequencies

Parameters	3 GHz	3.1 GHz	10 GHz	20 GHz	30 GHz	40 GHz
$\alpha$ (Np/m)	1.056e+02	1.64e+02	5.572e+02	1.258e+03	1.839e+03	2.2959e+03
$\sigma$ (S/m)	4.050	4.050	4.050	4.050	4.050	4.050
$V_p$ (m/s)	3.155e+07	3.250e+07	3.707e+07	4.557e+07	5.373e+07	6.094e+07
$d_p \approx 1/\alpha$ (m)	0.0095	0.0083	0.0018	7.949e-04	5.437e-04	4.355e-04
$\tan \delta$	0.571	0.582	0.737	1.153	1.447	1.615
$\epsilon''_r$	47.967	47.032	43.057	39.549	32.692	26.983
$\epsilon'_r$	83.965	81.035	58.349	34.273	22.582	22.582



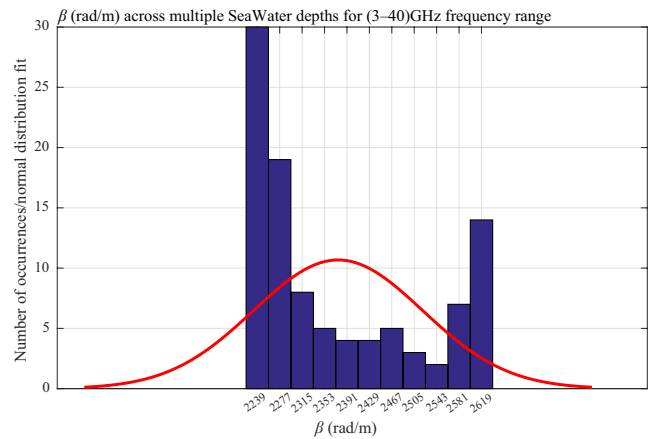
**FIGURE 9**  $\alpha$  values (dB/m) for various seawater depths with NDF



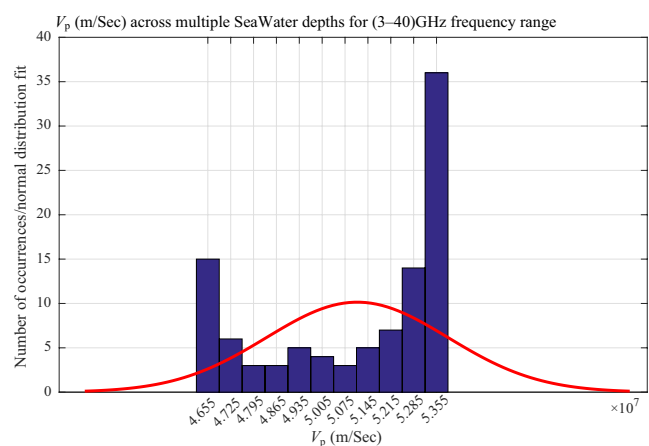
**FIGURE 10**  $\tan \delta$  values for various seawater depths with NDF

is 1.6, more like a conductor, but at 500 m, it goes to 1.82 and behaves more like an insulator. Similarly, for 40 GHz, the value starts from 0.46 and goes up to 0.45 at all seawater depths.

Table 3 shows the estimated values for the parameters  $\alpha$ ,  $\sigma$ ,  $V_p$ ,  $d_p \approx 1/\alpha$ ,  $\tan \delta$ ,  $\epsilon_r''$ , and  $\epsilon_r'$  for the 100-m depth at multiple frequencies. It also includes the 3.1 GHz frequency for Wi-Fi communication in seawater.  $\beta$ , the imaginary part of  $\gamma$ , contributes in estimating seawater and  $v_p$ .  $\beta$  also plays an important role in determining the phase change when EM waves cross the sea/air interface, estimated using the model depicted in (19). Figure 11



**FIGURE 11**  $\beta$  values (rad/m) for various seawater depths with NDF



**FIGURE 12**  $V_p$  values (m/s) for various depths of seawater with NDF

shows  $\beta$  values across the frequency range. At 3 GHz,  $\beta$  reaches a maximum value of 4000 rad/m at the seawater surface and starts decreasing, similar to  $\alpha$ , reaching a minimum value of 1000 rad/m at extreme depths. At 40 GHz near the surface,  $\beta$  is approximately 500 rad/m, but at 5500 m, it is 100 rad/m.

The  $V_p$  values of EM waves in air (free space) are assumed to be approximately constant,  $3 \times 10^8$  m/s. For seawater, the value mostly assumed in the literature is  $3 \times 10^7$  m/s for each

**TABLE 3** Estimated parameters for 100-m depth at multiple frequencies

Parameters	3 GHz	3.1 GHz	10 GHz	20 GHz	30 GHz	40 GHz
$\alpha$ (Np/m)	1.017e+02	1.627e+02	5.633e+02	1.258e+03	1.816e+03	2.247e+03
$\sigma$ (S/m)	3.831	3.831	3.831	3.831	3.831	3.831
$V_p$ (m/s)	3.206e+07	3.283e+07	3.798e+07	4.727e+07	5.606e+07	6.373e+07
$d_p \approx 1/\alpha$ (m)	0.0098	0.0076	0.0018	7.949e−04	5.506e−004	4.450e−04
$\tan \delta$	0.556	0.573	0.770	1.220	1.526	1.690
$\epsilon_r''$	45.433	45.001	42.489	38.118	30.934	25.263
$\epsilon_r'$	81.578	80.037	55.117	31.223	20.260	14.945

**TABLE 4** Estimated parameters for 500-m depth at multiple frequencies

Parameters	3 GHz	3.1 GHz	10 GHz	20 GHz	30 GHz	40 GHz
$\alpha$ (Np/m)	92.004	92.863	5.823e + 02	1.247e + 03	1.731e + 03	2.089e + 03
$\sigma$ (S/m)	3.052	3.052	3.052	3.052	3.052	3.052
$V_p$ (m/s)	3.329e + 07	3.699e + 07	4.044e + 07	5.222e + 07	6.278e + 07	7.155e + 07
$d_p \approx 1/\alpha$ (m)	0.0109	0.0100	0.0017	8.019e - 04	5.777e - 04	4.787e - 04
$\tan\delta$	0.518	0.563	0.872	1.420	1.730	1.843
$\epsilon_r''$	39.588	39.953	41.253	34.225	26.342	20.918
$\epsilon_r'$	76.336	75.001	47.256	24.0988	15.221	11.346

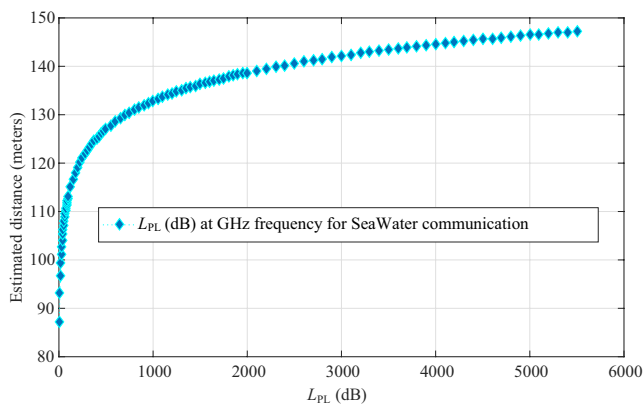
depth and frequency based on (21). We estimated  $v_p$  based on averaged real-time data for multiple decades at multiple depths in the world's oceans. In Figure 12, we can clearly see that at the seawater surface,  $v_p$  remains approximately constant up to 4000 m ( $0.25\text{--}0.65 \times 10^7$  m/s). Beyond this depth, it starts increasing again exponentially up to 5500 m, achieving a maximum limit of  $2.5 \times 10^7$ . The range for  $V_p$  for extreme depths lies between  $1.25$  to  $2.25 \times 10^7$  which is clearly different from the value that is normally assumed in the literature. Table 4 shows the values for the estimated parameters  $\alpha$ ,  $\sigma$ ,  $V_p$ ,  $d_p \approx 1/\alpha$ ,  $\tan\delta$ ,  $\epsilon_r''$ , and  $\epsilon_r'$  500-m depth at multiple frequencies, including 3.1 GHz for Wi-Fi communication in seawater.

Figure 13 depicts the achievable distance in seawater considering the overall loss,  $L_a, L_0$  for a given range of frequencies from 3 GHz to 40 GHz. The value of  $L_{PL}$  increases suddenly initially, but after a certain minimum distance, the overall loss remains approximately constant. For the analysis, we used a frequency range of 3 GHz to 40 GHz at  $P_T = 30$  dBm and a transmitter and receiver antenna gain of  $G_{T,R} = 10$ . The Rayleigh distance for the dipole antenna was approximately 5 m. The maximum achievable distance was 150 m, with maximum decay in transmission power. But for short-range communication within a few meters, gigahertz frequencies are a

suitable choice in seawater. This can provide higher transmission data rates with minimum propagation delay.

## 4 | CONCLUSION AND FUTURE WORK

This paper presents detailed analysis of the W. Ellison model parameters for seawater,  $\epsilon_r$  and  $\sigma$ , based on real-time data for all oceans. We used specifically averaged annual data from 1955 to 2012 from the National Centre For Environmental Information (NCEI). An interpolation model for  $\sigma$  was analyzed for 3 GHz to 40 GHz at multiple depths. The analysis showed that the  $\sigma$  value varied from 4 to 0.01 on average for multiple frequencies. The  $\epsilon_r'$  values at the seawater surface for multiple frequencies varied from 15 to 85, and at a seawater bottom depth of 5500 m, it ranged from 0.5 to 9.5 rather than remaining at a fixed value of 81. Similarly, the  $\epsilon_r''$  values for the seawater surface were between 25 and 45, and at maximum seawater depth, it was approximately 2–4. We also analyzed the channel performance for seawater based on the estimated total path loss  $L_{PL}$  versus achievable distance. From the results, it was clear that we can use gigahertz frequencies for seawater communication within a few meters; beyond that, the achievable distance is higher but with much higher  $L_{PL}$ . In the future we want to look at this problem in the context of e-navigation, bringing existing and new technologies together to improve safety of navigation, commercial efficiency, and security. Challenge for industries working through the International Maritime Organization (IMO) will be to produce a unified strategy for integration and to develop systems to meet the requirements through Smode. The concept of Smode is the default setting to bring all inputs such as radar, charts, and positioning for e-navigation to one platform. This all needs to be achieved through acceptable cost and benefits. E-navigation will be used for monitoring all kinds of activities in the world's oceans.

**FIGURE 13**  $L_{PL}$  values for seawater communication at gigahertz frequencies

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