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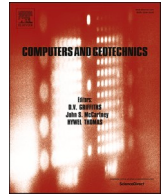
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Root size effects on transverse root-soil interactions

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ABSTRACT

For smaller lateral plant roots in coarse-grained soils, a potentially large relative size of soil particles compared to the roots may affect their transverse resistance. Even for the larger roots of trees, particle size effects may be important, e.g. when testing 1:N reduced scale models in a geotechnical centrifuge. The Discrete Element Method (DEM) was used to investigate this problem. A rigid lateral root segment under transverse loading in plane strain was simulated and compared with Finite Element Method (FEM) simulations, where the soil was modelled as a continuum (no particle size effects). Even at the lower root/particle diameter ratios (d_r/D_{50}) investigated (6 to 21), particle size effects on transverse capacity were negligible upon push-in, while during uplift, they were observed for $d_r/D_{50} < 8$, arising from the dimension of the uplifted soil volume above the root. The material properties of roots are also typically diameter dependent. Further simulations of long flexible roots subject to end rotation were performed employing a beam-on-non-linear-Winkler-foundation approach, using p - y curves obtained from the DEM or FEM simulations. Compared with particle-size related effects, diameter-dependent variation of material properties had a much larger controlling effect on root capacity and stiffness as relevant for plant/tree overturning.

1. Introduction

Plant roots are natural soil anchors which could play a prominent and sustainable role in risk mitigation strategies for geotechnical infrastructure (e.g. as a nature-based solution, NBS) through modifying the groundwater regime (Smethurst et al. 2012) and/or through direct mechanical soil strength improvement (Stokes et al. 2009; Karimzadeh et al. 2021, 2022). Given that landslides, debris flows and windstorms are common hazards that can cause ecosystem degradation and vegetation destruction (McCarthy et al. 2010; Cui et al. 2012; Zhang et al. 2023), understanding root-soil interaction behaviour under transverse loads has long been of interest in forestry. It is also of interest in Civil Engineering, e.g. trees could provide protection against earthquake-induced landslides (Liang et al. 2015) and windthrown trees in slopes may be a trigger for landslides (Jakob and Lambert 2009).

An increasing body of research has used scaled (1: N) root models to systematically investigate root-soil mechanical interactions in the

laboratory, either under 1 g conditions (Mickovski et al. 2010; Harnas et al. 2016; Zhang et al. 2018) or at elevated gravity within a geotechnical centrifuge (Liang et al. 2015; Zhang et al. 2023). Compared with field winching (pulling) tests of trees or field shearbox tests, key variables (e.g. model root properties, root architecture, soil properties, groundwater conditions and loading conditions) in these N -g tests can be closely controlled. However, scale effects related to particle size may exist (Liang and Knappett 2017) in case of over-scaling of the root model, where the surrounding soil can no longer be considered as a continuum, especially for coarse granular soils. Even for root-soil interactions at 1:1 (full) scale in the laboratory or in the field, roots with small diameter (compared with particle size) may similarly be subject to scale effects related to particle size in coarse-grained soils (e.g. gravels or granular tills). Based on centrifuge testing of foundations, existing studies have found that particle size effects depend on the shear band formation (Lehane and White 2005; Lehane et al. 2005; Athani et al. 2017), soil-structure interface roughness (Sinnreich 2011) and stress

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level (Bałachowski 2007). Garnier et al. (2007) suggested that the ratio of the diameter of shallow footing to particle size should be larger than 35 to avoid any particle size effects, whereas Ovesen (1981) reported no scale effects on uplift resistance of plates in loose and dense sand even with the ratio reduced to 25. Similarly, Palmer et al. (2003) found no significant particle size effects on the uplift resistance of buried pipelines at a threshold ratio of 80. However, compared with foundations and pipelines, plant roots could result in much lower structure-grain size ratios, which has been rarely investigated (e.g. Mickovski et al. 2010). Also, in contrast to conventional geotechnical structures, plant roots are normally located at very shallow depth, in which case the effect of low confining stress (and correspondingly high dilatancy) should also be considered.

Considering the tree overturning problem shown schematically in Fig. 1, under external lateral loading (e.g. from wind), individual lateral roots may be idealised to be either uplifted or pushed into the soil. The aim of this study is to first numerically simulate a rigid lateral root segment of such a root system under a plane strain condition, validating performance against physical model testing, and then using the model to investigate the influence, if any, of potential particle size effects that may arise at different d_r/D_{50} ratios, e.g. 1:N scale physical model tests of lateral roots of a particular prototype. For a higher N, chosen to avoid boundary effects in designing such tests, the model roots become smaller while the soil particle size remains the same; this changes the ratio of root diameter (d_r) to mean particle size (D_{50}) under the same effective stress conditions. This is analogous to a field scenario considering progressively smaller tree roots at similar depths within a coarse-grained soil. To this end, three dimensional (3D) Discrete Element Method (DEM) simulations, capable of modelling particle-scale interactions, were employed to replicate the behaviour of rigid lateral root segments of different diameters interacting with a granular bed. The results were then compared with equivalent Finite Element Method (FEM) simulations, where the soil was modelled as a continuum and hence did not incorporate particle size effects, to identify any deviations from the continuum behaviour. Subsequently, the force–displacement behaviour observed from these simulations was incorporated within a numerical model of a flexible lateral root subject to rotation at one end (consistent with the loading seen during tree overturning), as these roots provide a large proportion of the anchorage resistance of a tree according to existing field (Coutts 1986; Crook and Ennos 1996) and laboratory physical testing (Zhang et al. 2023). A beam-on-non-linear-Winkler-foundation (BNWF) approach using p - y curves from the FEM or DEM

simulations was employed, to investigate the relative magnitude of particle size effects to other root-size dependent characteristics such as root stiffness and strength.

2. Physical modelling of lateral root uplift for validation

2.1. Soil

A uniformly graded medium to fine sand (HST95 Congleton silica sand) was used for testing. This sand is a specific fraction of the sand extracted at Bent farm, Congleton, Cheshire, and has been widely used at the University of Dundee for physical model tests. The particle size distribution (PSD) of the sand is shown in Fig. 2, while some other index properties are summarised in Table 1. The coefficients of uniformity and curvature of the soil were 1.5 and 1, respectively, and its maximum and minimum density were 1.8 and 1.5 Mg/m³, respectively. The critical state friction angle of the sand was 32° based on direct shear tests across a range of relative densities (9–93 %) and effective confining stresses (5–200 kPa), as reported by Al-Defae et al. (2013).

2.2. Physical testing of lateral root-soil interaction

The lateral root analogue investigated in this study was simplified to be straight, based on two field trees: a 27-year-old *Pinus pinaster* tree grown in a deep sandy spodosol in the “Landes de Gascogne” forest in south-west France (Danjon and Reubens 2008) and a 19-year-old *P. pinaster* tree grown in a shallower sandy spodosol in Cestas, France (Danjon et al. 2013), where in each case a large proportion of lateral roots were ~ 60 mm in diameter and located at ~ 130 mm below the soil surface. Correspondingly, a 60 mm diameter steel T-bar buried at 130 mm depth (denoted as z_r , from ground surface to the root centreline) was fabricated to simulate an idealised lateral straight cylindrical root segment at 1:1 (full) scale for validation of subsequent numerical models.

A test container with internal dimensions of 800 mm (length) × 500 mm (width) × 550 mm (height) was used. The length of the T-bar (i.e., the root analogue) was 430 mm (Fig. 3). The HST95 sand was initially air pluviated to create a uniform soil bed with a depth of 120 mm to the underside of the root with a relative density of 60–65 % (corresponding to the dry density 1.67 ± 0.01 Mg/m³). The root analogue was then suspended above this soil and pluviated until the model root was buried to a depth of 130 mm (such that the cover depth $c = 100$ mm and $c/d_r = 1.67$). A water head 300 mm higher than the soil surface was applied at the bottom of the model soil for bottom-up saturation. To achieve drained behaviour, the model root was uplifted vertically at a rate of 0.0025 mm/s, which was one order of magnitude slower than the

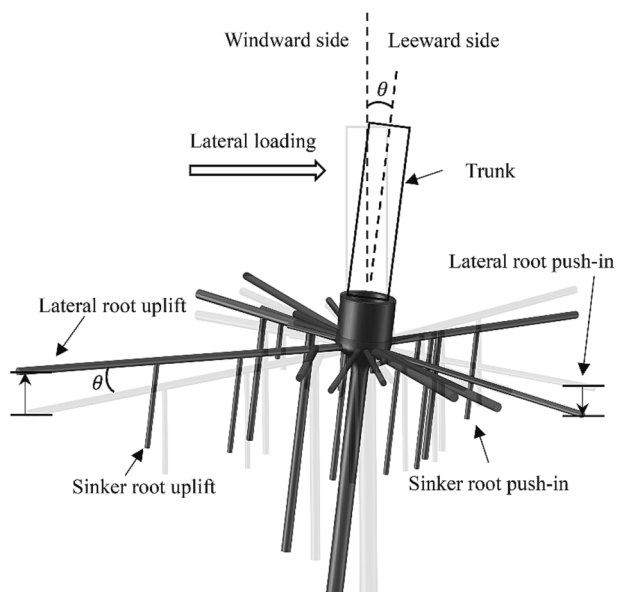


Fig. 1. A simplified root system under lateral loading.

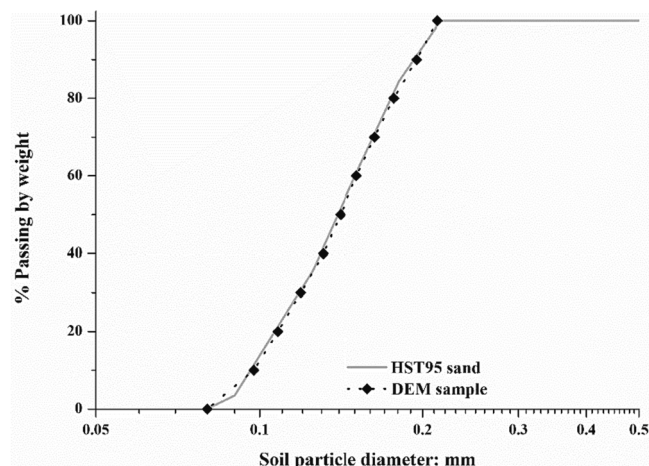


Fig. 2. Particle size distribution of experimental and numerical sands.

Table 1
HST95 sand key numerical parameters (after Al-Defae et al. 2013; Brown et al. 2019).

Soil index properties	Value
Mean particle size (D_{50}): mm	0.14
Maximum particle size (D_{100}): mm	0.21
Minimum void ratio	0.467
Maximum void ratio	0.769
DEM parameters	Value
Specific gravity (G_s)	2.65
Shear modulus: GPa	3
Poisson's ratio	0.3
Particle friction coefficient	0.264
Interface friction coefficient (root)	0.16
FEM parameters (corresponding to 60 % relative density)	Value
Peak friction angle (ϕ): °	41
Dilation angle (ψ): °	11
Reference oedometer stiffness (E_{oed}^{ref}): MPa	35.2
Reference secant stiffness (E_{50}^{ref}): MPa	44
Reference unloading/reloading stiffness (E_{ur}^{ref}): MPa	105.7
Reference low strain shear modulus (G_0^{ref}): MPa	118.8
Reference shear strain ($\epsilon_{s,0.7}$): %	0.0169

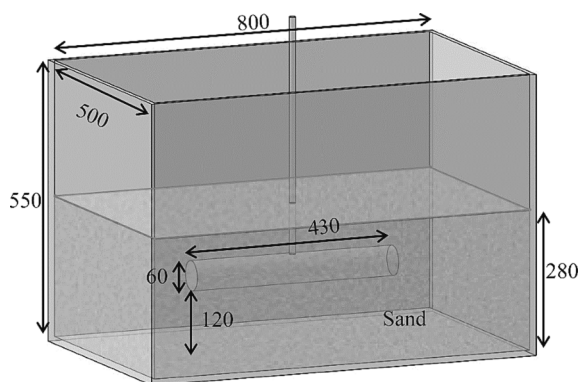


Fig. 3. Diagram of 1:1 physical test set-up for lateral root uplift test (all dimensions in mm).

drained loading rate adopted in previous direct shear tests of the same soil (i.e. 0.032 mm/s, [Lauder, 2010](#)), using a tension-compression loading frame (Instron 5985L7706, Instron Inc., US). The capacity of the load cell used to measure the uplift force was 30 kN with an accuracy of 1 mN. Force and displacement readings were logged at a sampling frequency of 1 Hz.

3. Numerical modelling and validation

3.1. Constitutive models and parameters

To model the root-soil interaction in DEM, Particle Flow Code (PFC) 3D 5.0.35 (Itasca Consulting Group, 2016) was employed. The mechanical interface interactions among particles and between the particle and root were modelled by a simplified Hertz-Mindlin contact model ([Mindlin and Deresiewicz 1953](#)). The contact model was calibrated to replicate the macroscopic mechanical behaviour of the HST95 sand. The particle size distribution (PSD) adopted was representative to the HST95 sand tested in the laboratory (see [Fig. 2](#)). The contact parameters ([Table 1](#)) for particle-particle interaction were calibrated against existing drained triaxial test data under a confining pressure of 60 kPa at two different relative densities (see [Fig. 4](#); after [Brown et al., 2019](#)). Following [Ciantia et al. \(2016\)](#), the DEM implementation of the triaxial tests used representative element volumes (REV), which, for the PSD of

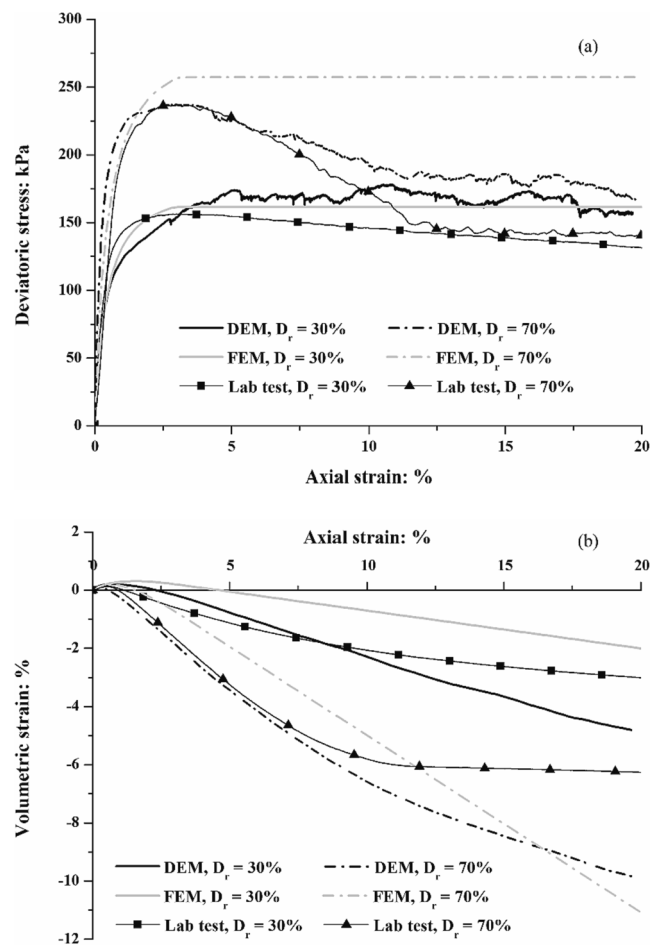


Fig. 4. Validation of triaxial tests of HST95 sand under a confining stress of 60 kPa: (a) Deviatoric stress - axial strain; (b) Volumetric strain - axial strain (DEM and laboratory data from [Brown et al. 2019](#); FEM from this study).

the HST95 sand, consist of around 5000 particles ([Brown et al. 2019](#)). Sample generation used the radius expansion technique ([Cundall and Strack 1979](#)) followed by a consolidation phase to the required relative densities. Stress-controlled servo rigid frictionless walls were used to reach an effective confining pressure of 60 kPa. During shearing of the REV, the stress-controlled servo was maintained on the lateral boundaries at the desired confining (cell) pressure. The bottom boundary was fixed, while the top boundary was displaced in a strain-control manner. To attain a quasistatic response, wall strain rates were capped such the inertial number was always maintained less than.

10^{-3} ([Ciantia et al. 2018](#)). Particle rotation was inhibited to simulate the interlocking effects of the sand, which was computationally efficient ([Arroyo et al. 2011](#)) and may be considered as a limit case for classical rolling-resistance contact models ([Rorato et al. 2021](#)). The coefficient of particle-structure interface friction was set to be 0.16 based on steel-soil direct shear interface tests.

To provide a continuum comparison, root-soil interaction was also simulated by two-dimensional (2D) plane-strain FEM simulations using PLAXIS 2019. A non-linear elasto-plastic constitutive model, called 'hardening soil with small strain stiffness' ('HS small'), was employed. The key soil parameters summarised in [Table 1](#) were previously calibrated for the HST95 sand by [Al-Defae et al. \(2013\)](#) based on an extensive series of drained direct shear and oedometer compression tests.

[Fig. 4](#) demonstrates the performance of both the DEM and FEM parameters under drained triaxial compression against element test data. When the axial strain was less than or equal to that resulting in peak

strength the shearing behaviour was generally well captured by both models. Beyond this point, however, the soil softening behaviour observed in the element tests can be reproduced by the DEM but not by the FEM when using the hardening soil model, as expected. The uplift/push-in resistance of individual lateral roots associated with peak strength (based on studies of uplift/push-in resistance of buried pipelines: (White et al. 2008; Wu et al. 2021) is of principal interest in this paper.

3.2. Modelling procedure

To reduce runtime, the dimension of the lateral root analogue and its burial depth were both scaled down by 20 times, the same scale factor as adopted in previous physical modelling studies of the same two root systems (Zhang et al. 2020). A 3D DEM model with periodic boundaries (Ciantia et al. 2018) in the out of plane dimension (root axis direction) was developed, at model scale, to recreate the approximate plane strain condition considered in the laboratory (Fig. 5(a)). To replicate the same effective stress conditions, an elevated acceleration field at 20 g should be imposed to a water-saturated model. However, to avoid having to explicitly simulate water in DEM, a lower g-level at 12 g was applied to the dry model so that the effective stress regime was identical to that of saturated soil tested in the laboratory, following Eq. (1):

$$N_d = \left(1 - \frac{1}{G_s}\right) N_s \quad (1)$$

where N_d and N_s are g-levels for dry and saturated case. The domain size in the DEM model (Table 2) was chosen to be large enough (i.e. $B_h/D_r = 6$, where B_h is the width of the domain) to avoid unwanted boundary effects on the modelling of root-soil interaction. To efficiently generate a homogeneous and equilibrated DEM soil sample, the periodic cell replication method (PCRM) proposed by Ciantia et al. (2018) was employed. In PCRM, pre-equilibrated homogeneous $2.5D_{100}$ -thick (0.53

Table 2
Domains and root sizes of horizontal root simulations.

d_r/D_{50}	$N = N_s$	N_d	Uplift		Push-in		Notes
			D_h/d_r	B_h/d_r	D_h/d_r	B_h/d_r	
28	15	9	4	6	–	–	$d_r = 3$ mm, validation test
21	20	12	4	6	11	16	
17	25	15	5	8	13	20	
14	30	18	6	10	16	24	
11	38	23	7	12	20	29	
9	50	30	9	16	27	39	
6	75	45	14	24	40	59	
3	150	90	28	48	–	–	

mm) periodic cells at desired porosity, consistent with the laboratory test, were replicated to fill the entire domain. Further increasing the thickness of the chamber was observed to show negligible boundary effects on the root behaviour. The contact forces and interparticle reference gaps were then adjusted to achieve the desired initial gravitational stress state (Ciantia et al. 2018). The root analogue was represented by a rigid, wished-in-place cylinder which was displaced vertically upward, at a constant rate of 4 mm/s to limit the inertial number to be lower than 10^{-3} (Ciantia et al. 2019).

To have a direct comparison with the DEM simulation, the 1:20 scaled model test was also simulated with a 2D plane strain FEM model (Fig. 5(b)), where a wished-in-place circular root was modelled with a rigid circular plate element. The FEM domain was discretised into 21,268 15-noded plane strain elements. Zero thickness interface elements were used to model root-soil interaction, thereby allowing for the opening of any gap at the root-soil interface in case of zero effective normal stress occurring during loading (no tension condition). The coefficient of lateral earth pressure K_0 was determined by Jaky's (Jaky 1944) formula (i.e. $K_0 = 1 - \sin\phi'$, where ϕ' is the soil peak friction angle). To model the process of uplift, a uniform vertical displacement was imposed to all of the nodes of the plate elements that formed the root analogue.

3.3. Validation of lateral root-soil interaction

Following the scaling laws shown in Table 3 (Nakahara et al. 2005), the force–displacement (p - y) curve obtained from the DEM simulation was scaled to the prototype scale for comparing with the physical model tests (Fig. 6). Note that the data directly obtained from the DEM was smoothed by applying the Adjacent-Averaging method to every 2500 data points. The overall shape of the curves from the laboratory test and the DEM (smoothed), especially post-peak softening behaviour at large displacement, were consistent with each other, although the DEM simulation slightly overestimated the peak uplift force by less than 10 % and displayed a higher pre-peak stiffness. The peak uplift force predicted by the FEM was also close, approximately 5 % lower than the model test. However, due to severe mesh distortion at large displacement, the FEM simulation could not proceed further than this, in contrast to the DEM that was able to simulate the complete uplift.

Table 3
Scale laws used in this study (after Nakahara et al. 2005).

Parameter	Scaling law: Model/Prototype
Length/Depth	1/ N
Mass density	1
Acceleration	N
Stiffness	1
Stress	1
Force	1/ N^2
Displacement	1/ N

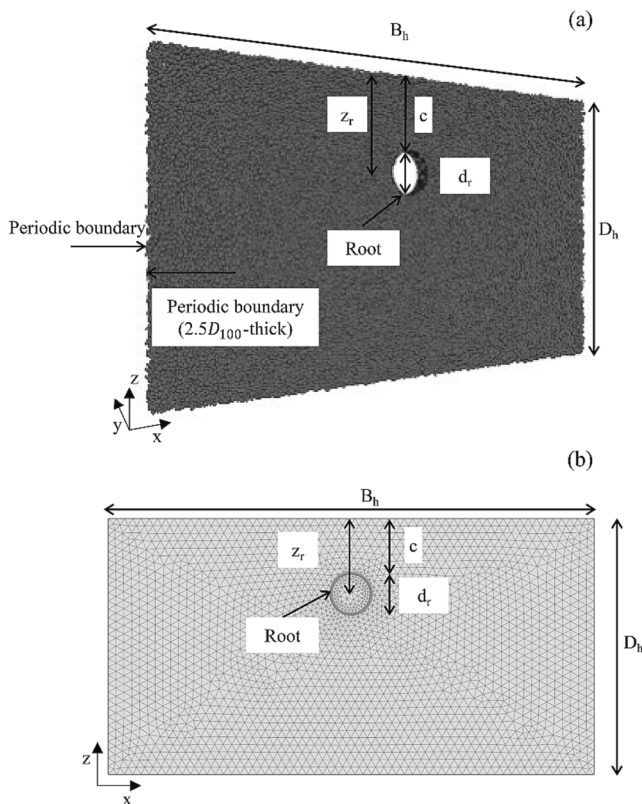


Fig. 5. Diagram of test set-up for numerical modelling of horizontal root in: (a) DEM; (b) FEM.

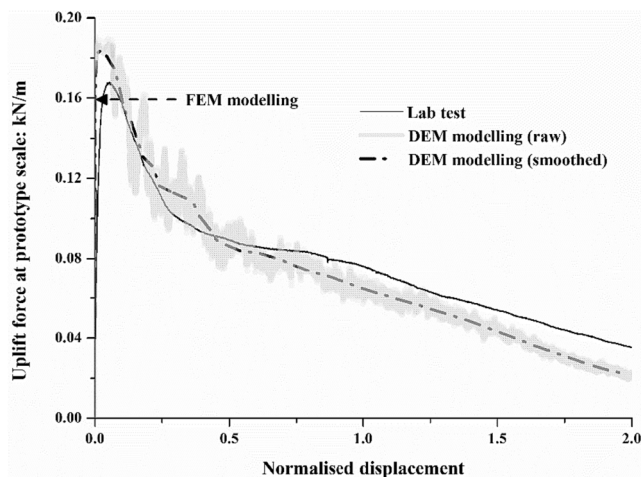


Fig. 6. Validation of lateral root uplift.

4. Parametric study of particle size effects

4.1. General description of modelling methodology

Particle size effects on lateral roots during both uplift and push-in movements were investigated using the validated DEM models. The principle of these simulations was to scale down the diameter (d_r) and buried depth (z_r) of a straight lateral root analogue by a variable factor N and then to scale up the gravitational acceleration by N times so that the prototype virtual model and stress regime were the same for all the simulations. However, the particle size was not scaled through this approach, so the number of soil particles in contact with the root would be proportionally reduced as N increased. Thus, this modelling method is equivalent to selecting different scale factors to model the lateral root during the design of a centrifuge experiment. It is also a convenient way of changing only the ratio of d_r/D_{50} while using identical DEM particle assemblies. Following the conventional scaling laws (e.g. Nakahara et al. 2005), force at prototype scale could be obtained by multiplying the simulated force in each case by N^2 . The response obtained at prototype scale should be the same in all cases of different N , if particle size effects are absent. The prototype diameter and buried depth were selected to be 60 mm and 130 mm, respectively ($z_r/d_r = 2.2$), the same as that adopted in the validation experiment. The diameters of the scaled roots were informed by the sizes of individual roots considered in the 1:20 scale model tree root system ($d_r = 3, 2.4, 2$ and 1.6 mm) tested by Zhang et al. (2020). Additional smaller diameters (1.2 mm and 0.8 mm) were also considered to cover a wider range of d_r/D_{50} (i.e. < 10 ; Table 2). For uplift cases only, $d_r = 4$ and 0.4 mm cases were added to further extend the range, based on the results from the initial simulations.

The rates of applied vertical uplift and push-in were set to be 4 mm/s for all cases to ensure that the loading process of the roots of different sizes remained quasi-static. The methods used to generate the DEM particle assembly in each case were the same as those used in the preceding validation section. The dimension of the domain in 4 mm case has the same B_h/D_r and D_h/D_r ratios with the 3 mm root case, and for other cases the B_h and D_h were determined to be the same as those adopted in the validation section. Corresponding FEM simulations were also conducted using the same dimensions as the DEM models for making direct comparison following the procedures used for model validation.

4.2. Uplift of lateral roots

Fig. 7(a) compares the uplift resistances at prototype scale obtained from DEM simulation of scaled lateral roots, which have the same prototype dimension. It is evident that as d_r/D_{50} was reduced from 28 to 8,

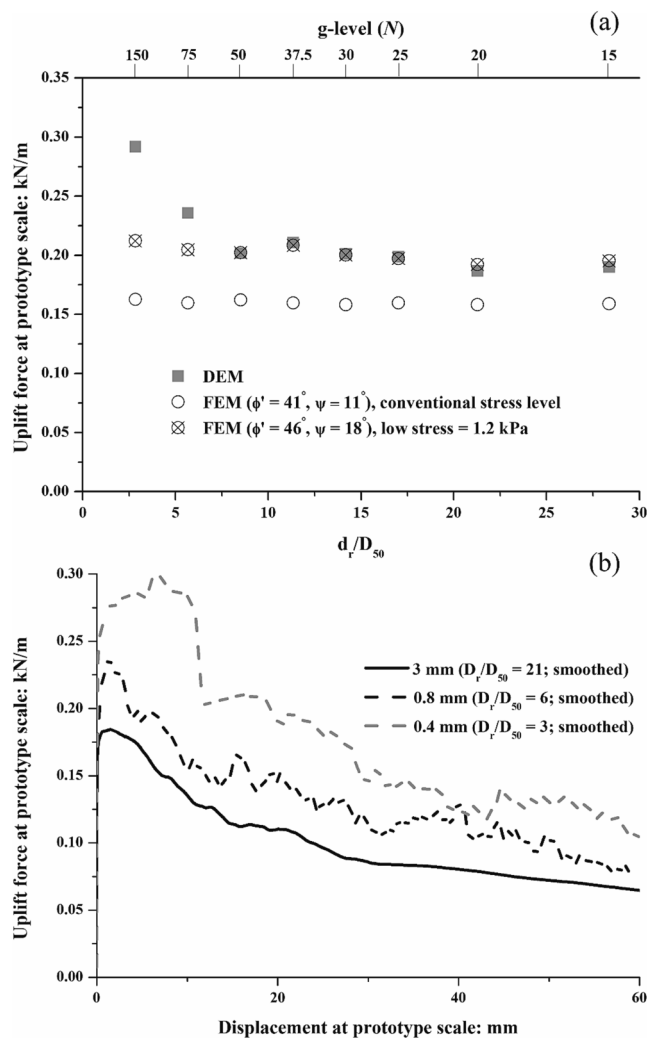


Fig. 7. (a) Uplift resistance of horizontal roots with different scale factors; (b) Load-displacement curves of 3, 0.8 and 0.4 mm roots from DEM uplift simulations.

the values of uplift resistance were similar; however, a substantial increase in the resistance was observed when d_r/D_{50} was reduced below 8. The load–displacement curves of the 3, 0.8 and 0.4 mm roots (corresponding to d_r/D_{50} of 21, 6 and 3, respectively) are depicted in Fig. 7(b), showing a noticeable increase in the uplift resistance when d_r reduced to 0.8 mm. This suggests that $N = 50$ (which corresponds to d_r/D_{50} of 8) is the maximum scale factor that would be free from particle size effects when testing a scaled 60 mm diameter tree root in HST95 sand on the centrifuge, or that the same root would begin to see particle size effects in the field in a gravelly soil with $D_{50} \geq 7.5$ mm. The threshold ratio of d_r/D_{50} derived (i.e. 8) for this specific root-soil system was much smaller than those reported by Ovesen (1981) and Palmer et al. (2003), who found no obvious particle size effects on the uplift resistance of circular plates and pipelines down to threshold ratios of 44 and 80, respectively. This was because no further tests using increased scale factors were conducted in previous research due to the large prototype dimension of conventional geotechnical structures. However, the root analogue considered in the present study has a much smaller prototype dimension than other engineering structures such as plates and pipelines tested previously, such that lower structure-grain size ratios needed investigating.

For the FEM simulations, as expected, over the entire range of d_r/D_{50} , the prototype uplift resistance remained effectively constant because the soil in these simulations was considered to be a continuum where par-

particle size effects were implicitly absent. Ignoring the particle size effect could lead to a substantial underprediction of the uplift resistance at large scale factors (e.g. $\sim 40\%$ at $N = 150$). Even above the threshold d_r/D_{50} value (i.e. 8), the resistance obtained from the FEM was approximately 15% lower than that from the DEM. This discrepancy arises because the input peak strength and dilation angle used in FEM in Table 1 were those appropriate for conventional stress levels considered in routine laboratory testing for conventional geotechnical systems (friction and dilation angles of 41° and 11° , respectively) rather than the extremely low confining stress, 1.2 kPa, considered in the model tests. Bolton (1986) quantified the effects of dilation in terms of an increase in the soil peak friction angle as

$$\phi' - \phi'_{crit} = AI_R \quad (2)$$

where A is a dimensionless factor to account for strain type ($A = 5$ for plane strain); ϕ'_{crit} is the soil friction angle at critical state (32° for the HST95 sand in this study); and I_R is given by

$$I_R = I_D(Q - \ln p') - R \quad (3)$$

where I_D is the relative density of the sand, p' is the mean effective confining stress of the soil; Q and R are fitting parameters according to the intrinsic sand characteristics, taken to be 10 and 1 respectively when $0 < I_R < 4$ (Bolton 1986). At low confining stress level, however, Chakraborty and Salgado (2010) suggested using $Q = 7.1 + 0.75 \ln p'$ (for plane strain) and $R = 1$, respectively. After obtaining a revised ϕ' using these expressions, following (Bolton 1986) the corresponding dilation angle ψ can be calculated as

$$\phi' - \phi'_{crit} = 0.8\psi \quad (4)$$

Based on these calculations, the peak friction angle and the dilation angle at low confining stress were modified to be 46° and 18° , respectively. Using these values in the FEM simulations, the prediction of uplift resistance was much improved (Fig. 7), showing a consistent result with the DEM simulation for d_r/D_{50} above the threshold value of 8.

4.3. Mechanisms controlling particle size effects during uplift

The DEM-computed velocity profile, at an uplift displacement of $0.02 d_r$, where the uplift force peaked, is shown in Fig. 8 for two contrasting root diameters. It should be noted that particles with a velocity lower than $1/10$ th of the root velocity (i.e. 0.4 mm/s at model scale) are not presented as this is considered a threshold level between stationary and moving particles. White et al. (2008) and Giampa et al. (2017) used the assumption of a wedge of soil uplifted with shear planes inclined to the vertical at the dilation angle to develop analytical solutions based on limit equilibrium for the assessment of uplift capacity of pipelines and circular plate anchors, respectively. Under this assumption, the weight of the affected soil wedge (W) in plane strain can be calculated as

$$W = \gamma' z_r d_r + \gamma' z_r^2 \tan \psi - \frac{\pi \gamma' d_r^2}{8} \quad (5)$$

where γ' is the effective (buoyant) unit weight of the soil. White et al. (2008) assumed that the normal effective stress acting on the sliding planes was equal to the in-situ value inferred from K_0 conditions, in

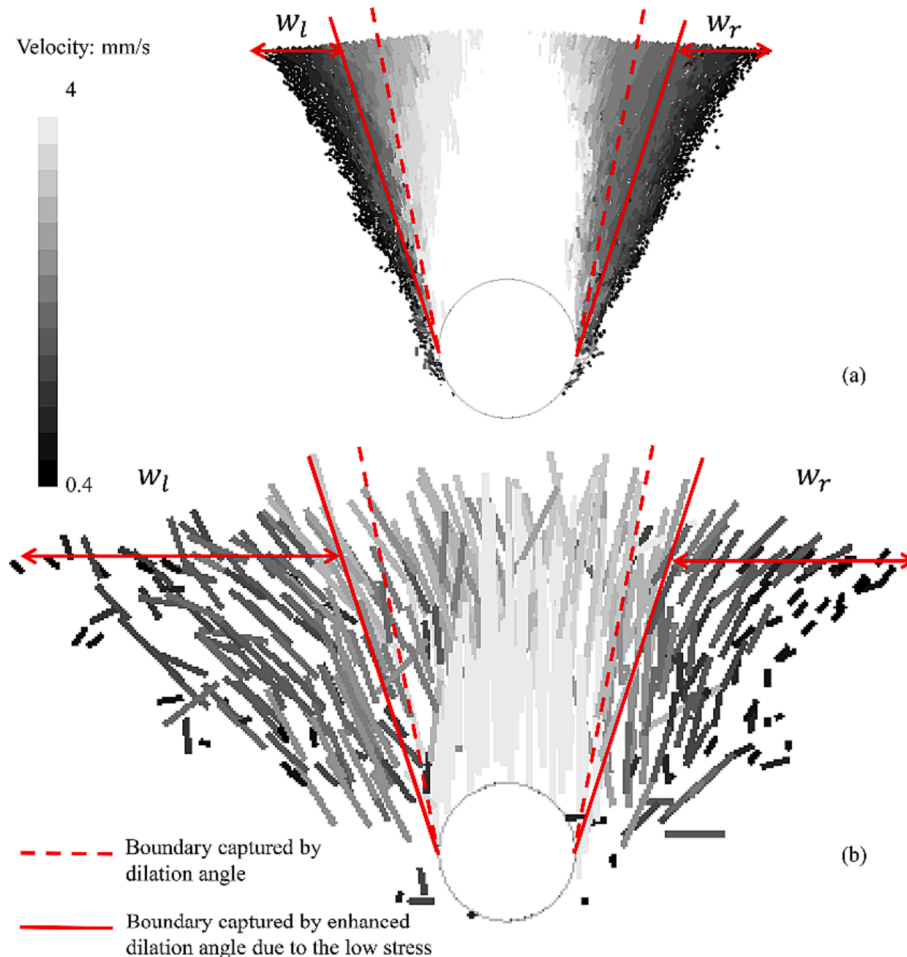


Fig. 8. Velocity field and particle tracks from DEM at $0.02 d_r$ uplift displacement for: (a) 3 mm root; (b) 0.8 mm root.

which case the vertical force acting on the sliding block (S) can be calculated using:

$$S = \gamma' z_r^2 (\tan\phi' - \tan\psi) \left(\frac{1 + K_0}{2} - \frac{(1 - K_0)\cos 2\psi}{2} \right) \quad (6)$$

Giampa et al. (2017) reviewed previous studies and proposed a modified expression for S :

$$S = \gamma' z_r^2 (\tan\phi' - \tan\psi) \cos(\phi' - \psi) \quad (7)$$

In this study, using Eq. (7) returns a higher value of S than that by Eq. (6), such that a higher uplift resistance per unit length P results, where:

$$P = W + S \quad (8)$$

As shown in Fig. 9, the results of the analytical solutions using White et al. (2008) and Giampa et al. (2017) were superimposed with the DEM simulation results given in Fig. 7. Note that both analytical solutions used the friction and dilation angles based on Eqs. (2) and (4) to capture the low confining stress effect. For $d_r/D_{50} > 8$, when particle size effects were negligible, the DEM simulations fell within the range suggested by the two analytical solutions. By plotting the dilation angles under conventional and low confining stress in the particle velocity profile (dashed and solid lines respectively in Fig. 8), it is apparent that considering enhanced dilation due to the low confining stress condition captured a larger volume of the affected soil block, however there were a significant number of particles outside the analytical soil block which appeared to also be mobilised in DEM, which could contribute some additional weight to the soil block. This was not accounted for by the analytical model and was expected to lead to an additional contribution to the horizontal root uplift capacity.

The width of this additional affected zone to the left and right of the analytical block (w_l and w_r in Fig. 8) were measured from DEM and the average values (w) normalised by mean particle size (w/D_{50}) in each case are presented in Fig. 10. A strong positive linear correlation can be obtained between w/D_{50} and d_r/D_{50} with $R^2 = 0.94$:

$$\frac{w}{D_{50}} = 0.56 \frac{d_r}{D_{50}} + 3.2 \quad (9)$$

Considering the weight contribution from the additional affected zone (in terms of increasing the volume of the uplifted block) and incorporating this within the analytical model proposed by White et al. (2008), the uplift resistance per unit length P can be modified as:

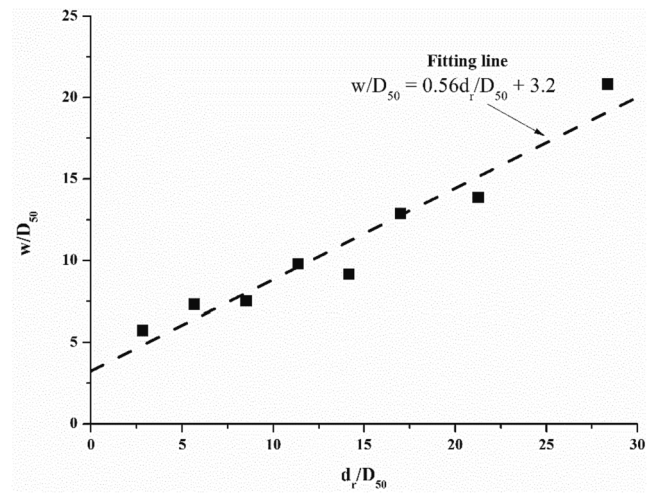


Fig. 10. Relationship between the width of additional affected zone and root diameter.

$$P = \gamma' z_r d_r + \gamma' z_r^2 \tan\psi + \gamma' (0.56 d_r + 3.2 D_{50}) z_r + \gamma' z_r^2 (\tan\phi'_{max} - \tan\psi) \left(\frac{1 + K_0}{2} - \frac{(1 - K_0)\cos 2\psi}{2} \right) - \frac{\pi \gamma' d_r^2}{8} \quad (10)$$

This modified expression resulted in a much better match with the DEM simulations (Fig. 9), capturing the particle size effect as d_r/D_{50} reduces and the widened zone of shearing becomes proportionally larger compared to the diameter of the root. Indeed, as shown in Fig. 8, the dimension of the additional affected zone relative to the 0.8 mm root (i. e. w/d_r ; Fig. 8b) was larger than that compared to the 3 mm root (Fig. 8a) due to the intercept of 3.2 in Eq. (9). This term is not associated with root diameter and results in particle size effects (through $3.2D_{50}$ in Eq. (10)) for fine lateral roots (or large roots at highly reduced scale) but becomes negligible for coarse roots (or lower scale factors). However, the magnitude of this term may be dependent on soil particle shape, relative density, particle size distribution, and friction angle. How this term might be correlated with such soil properties requires further systematic simulations in the future.

4.4. Behaviour during push-in

The peak push-in force with first 10 mm penetration is compared at prototype scale in Fig. 11(a), with the force–displacement curve of the roots of maximum and minimum simulated diameter shown in Fig. 11 (b). Although some differences were observed in terms of the stiffness of the push-in curve, possibly due to the lower B_h/d_r ratio for bigger roots, the prototype values of push-in resistance of the model roots of different diameters at model scale in the DEM simulation were largely similar, within the range of d_r/D_{50} examined. This means that particle size effects were not prominent under this loading condition. Other studies have investigated particle size effects for other shallow penetration problems, such as Toyosawa et al. (2013). They explored the case of shallow foundations (of diameter d_r) at the ground surface and those at an embedment depth z_r of $0.5 d_r$, finding a reduction in the minimum d_r/D_{50} ratio to avoid particle size effects as z_r/d_r increased (from $d_r/D_{50} = 50$ at $z_r/d_r = 0$ to $d_r/D_{50} = 33$ at $z_r/d_r = 0.5$). This suggests that particle size effects may vanish as structures are more deeply buried, i.e. z_r/d_r gets larger (Fig. 12). In this paper, the root analogues were buried at $z_r/d_r = 2.2$ and no particle size effects were identified during vertical penetration (at least down to $d_r/D_{50} = 6$), consistent with the findings reported by Toyosawa et al. (2013). As in the uplift case, when ignoring the effects of the low confining stress regime on the continuum strength parameters, the results obtained from the FEM simulations were consistently lower than those from the DEM (~45 % for the push-in

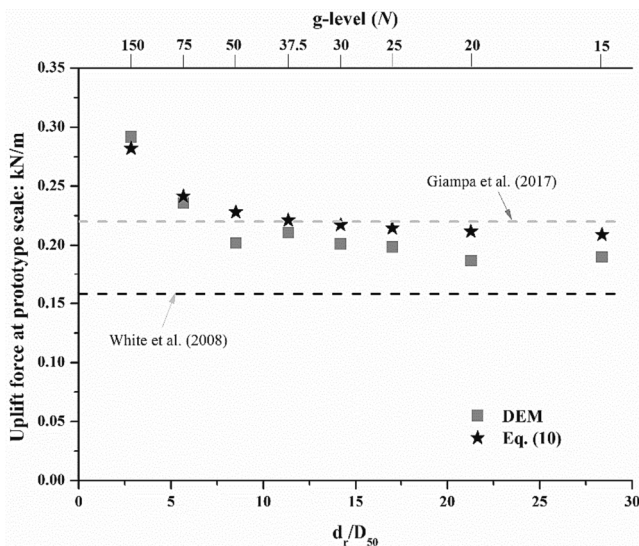


Fig. 9. Comparison of uplift force between DEM simulations and analytical studies.

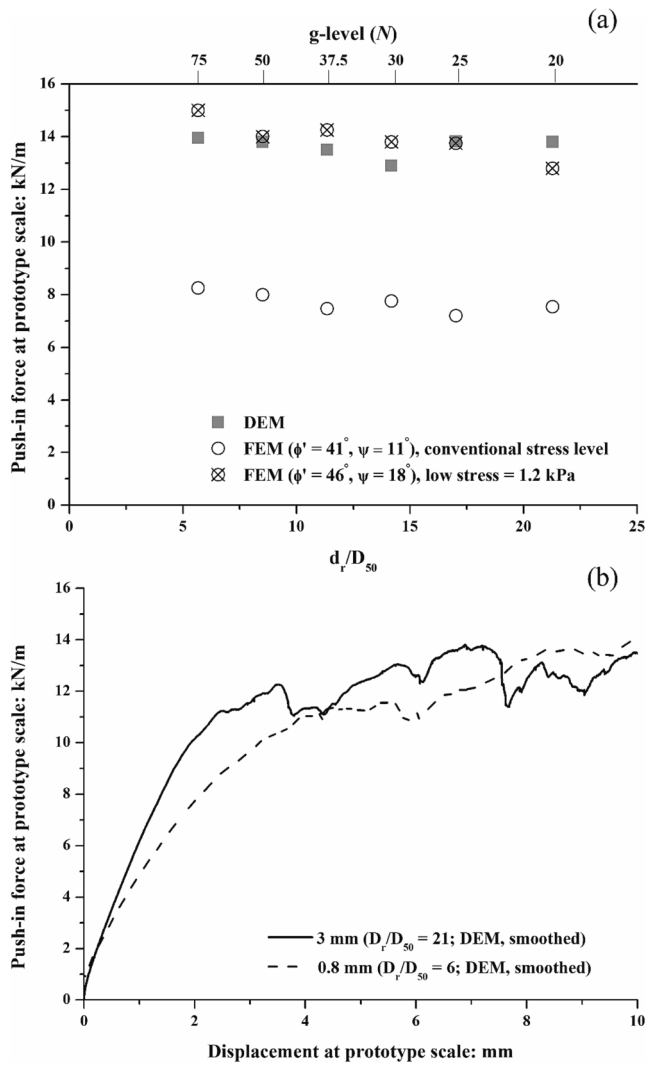


Fig. 11. (a) Push-in resistance of horizontal roots with different scale factors; (b) Load-displacement curves of 3 and 0.8 mm roots from DEM push-in simulations.

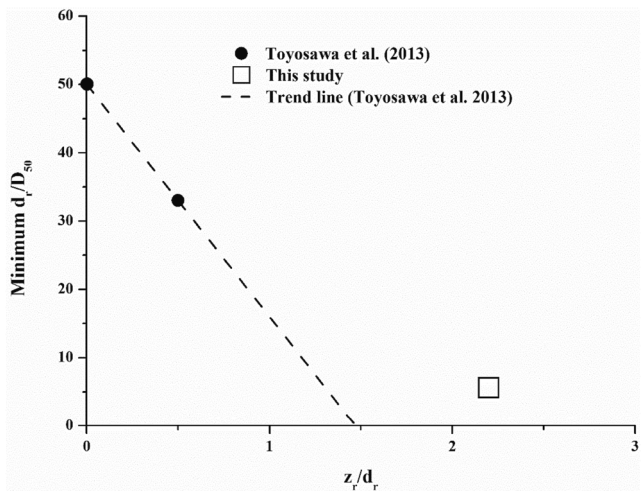


Fig. 12. Minimum diameter of rigid objects to avoid particle size effects at different burial depths.

condition). As before, adjusting the strength parameters to account for the low-stress effects (i.e. using Eqs. (2) and (4)) substantially improved the prediction accuracy of the FEM (Fig. 11(a)).

5. Modelling of whole lateral root behaviour under tree overturning

5.1. Numerical simulation set-up and procedures

In addition to the root size effects on soil-structure interaction properties explored in the previous sections, roots themselves typically exhibit material properties which are dependent on diameter (Schwarz et al. 2010; Mao et al. 2012):

$$T_r = \alpha_T d_r^{\beta_T} \tag{11}$$

$$E_r = \alpha_E d_r^{\beta_E} \tag{12}$$

where T_r is the tensile strength, E_r is the root Young's modulus and $\alpha_T, \beta_T, \alpha_E,$ and β_E are empirical fitting parameters. To explore the relative magnitude of these root size dependencies, numerical simulations were conducted, adopting a BNWF approach to model a long flexible lateral root subject to rotation at one end to simulate the action applied by the trunk during tree overturning, with the force-displacement behaviour obtained from previous DEM/FEM simulations incorporated.

The BNWF approach, which has significant advantages in computational efficiency compared to continuum FE models of root-soil interaction (e.g. Mickovski et al., 2011; Dupuy et al., 2007), was conducted using the non-linear FE programme ABAQUS to solve the beam-on-spring problem. As shown in Fig. 1, the windward lateral roots rotate about the centreline of the root system upon an external loading. A schematic diagram of this problem, as discretised within the BNWF framework, is depicted in Fig. 13. The root was modelled using deformable 2D beam elements, which are flexible in both shear and bending. A linear elastic-perfectly plastic model was used to model the stress-strain behaviour of the root. A series of fixed rigid vertical beams, which sat at a close and uniform vertical offset (i.e. 0.0004 mm) from the discrete nodes along the root, were established to prescribe a fixed boundary condition. Non-linear p - y springs were then connected between the root and the fixed beams to capture the root-soil interaction, with this behaviour being parametrised from the DEM/FEM simulations reported earlier. Compared with the traditional p - y method for small deformations (e.g. lateral loading of piles), where the springs are considered to remain perpendicular to the original position of the root before loading, in the present study the force always acted perpendicular to the displaced root section, such that the analyses would be representative at large applied rotations (see Meijer et al. 2019). This was achieved by using a connector element with the Cartesian type and a rotating local reference frame in ABAQUS.

An example of spring properties for a 3 mm root is shown in Fig. 14 (a). Since no scale effects related to particle size were observed when the root was pushed into the soil, the curve up to the peak force obtained from FEM was used, with the plateau added post-peak. The uplift properties of the spring is detailed in Fig. 14(b). In the case of DEM being used to define p - y curves, DEM simulation data was used directly as the

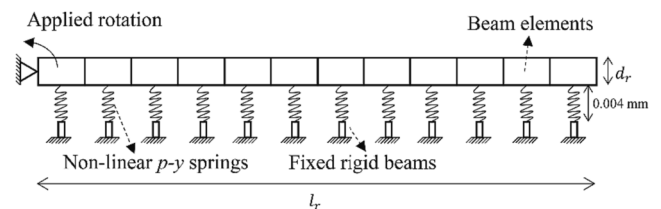


Fig. 13. Schematic diagram (not to scale) of root-soil system undergoing rotation loading (BNWF model).

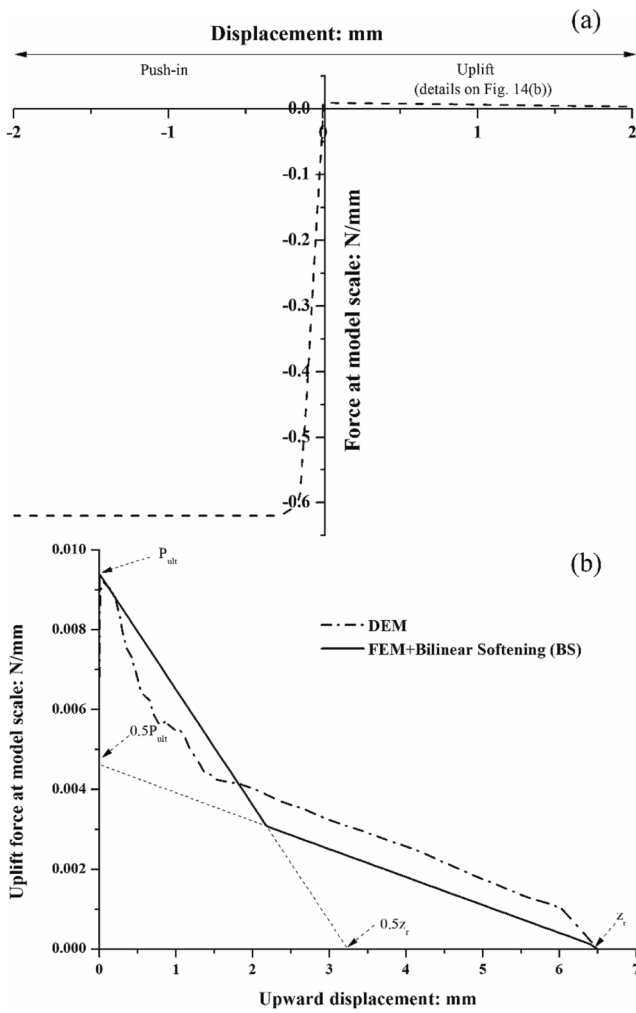


Fig. 14. (a) An example of the p - y curve for 3 mm lateral root; (b) Specification of uplift properties.

complete uplift process was simulated. Due to difficulties in simulating large (post-peak) deformation in FEM, for FEM defined uplift p - y curves, bilinear softening (BS; Fig. 14(b)) was assumed beyond the displacement δ_{ult} corresponding to the peak force (P_{ult}) from FEM, to complete the response over the complete extraction of a segment from the ground. The inflection point was determined as the intersection of the line connecting $(0, \frac{P_{ult}}{z_r})$ and $(z_r, 0)$ and the line connecting (δ_{ult}, P_{ult}) and $(\frac{z_r}{2}, 0)$. The end point was $(z_r, 0)$ to represent the uplift force becoming zero when the root leaves the soil. A hinged connection with fixed conditions in the horizontal and vertical directions was incorporated at the loading point to prevent any unwanted movement during rotation (applied through displacement control). Other than at this point, movement of the root was unrestrained, other than by the spring reactions.

Table 4
Simulations of whole lateral root uplift.

Simulation ID	N	Diameter (d_r): mm	d_r/D_{50}	Length (l_r): mm	Young's modulus (E_r): GPa	Tensile strength (T_r): MPa	p - y property
LR04	20	3.0	21	150	3.04	93.0	FEM + BS
LR05	20	3.0	21	150	3.04	93.0	DEM
LR08	75	0.8	6	40	3.04	93.0	FEM + BS
LR09	75	0.8	6	40	3.04	93.0	DEM
LR10	75	0.8	6	40	8.68	185.0	FEM + BS
LR11	75	0.8	6	40	8.68	185.0	DEM

The simulations of lateral root uplift (anticlockwise rotation in Fig. 13) conducted and the corresponding input parameters are summarised in Table 4. Initially, a 3 mm diameter root was simulated. The root was 150 mm long (simulations LR04 and LR05) according to the 1:20 scale model of a 60 mm diameter root from centrifuge model testing reported by Zhang et al. (2020). The scaled roots, made of 3D printed (layered) Acrylonitrile Butadiene Styrene (ABS) plastic in this study, were found to display diameter dependency in both tensile strength and Young's modulus similar to plant roots i.e. following negative power laws. According to a series of bending tests on root analogues of varying diameter conducted by Liang et al. (2015), the fitting parameters for Eqs. (11) and (12), $\alpha_T, \beta_T, \alpha_E, \beta_E$, were 164.7, -0.52 , 7.27 and -0.79 , respectively, where T_r, E_r, d_r are in MPa, GPa, and mm, respectively and the Poisson ratio of ABS plastic was taken as 0.35.

The number of springs, controlling the size of the discretised elements along the root, was determined based on a sensitivity analysis. It was reduced from 1 spring/mm until a noticeable difference appeared on the computed moment-rotation curves. An example of results for 3 mm diameter root (length of 150 mm; LR04) is shown in Fig. 15. It can be seen that when the spring density was reduced to 0.5/mm (i.e. 75 springs over 150 mm root length), the root behaviour was almost identical to the initial condition (1/mm). However, when the spring density was 0.033/mm, the moment capacity was overestimated by approximately 20 %. Note that 0.2/mm (corresponding to 30 springs) can be considered as the threshold value since the efficiency could be improved by 2.5 times with limited discrepancies observed, compared with the finest case of 1/mm.

A subsequent set of simulations were conducted considering the same prototype but simulated at different scale factors, with only the p - y parameters changed (i.e. only d_r/D_{50} changed with constant root properties; LR08 and LR09) and with both the p - y and material properties being a function of d_r (LR10 and LR11) to investigate the relative magnitude of root-size effects associated with d_r/D_{50} and with E_r and T_r .

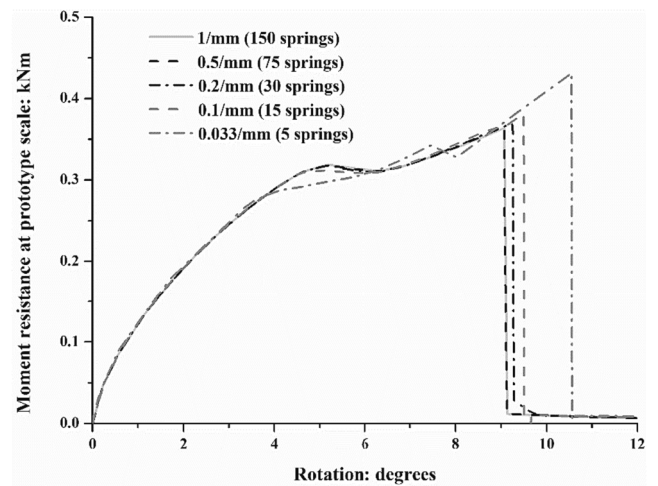


Fig. 15. Results of sensitivity analysis to determine an optimised number of springs to model the behaviour of a lateral root with 3 mm diameter.

when scaling field cases in physical model tests. LR08 and LR10 were also separately rotated clockwise (Fig. 13) to study scale effects related to material properties when the whole root was pushed into the soil.

5.2. Scale effects on whole lateral root rotational behaviour

Fig. 16 compares the moment-rotation curves, expressed at prototype scale, obtained from the simulations LR04, LR05, LR08 and LR09, where lateral roots had the same prototype and could be considered as a geometrically scaled model choosing different scale factors N . The E_r and T_r of the root used in all these simulations were identical, and they were determined based on the 3 mm ABS plastic rod. In this case, the moment resistances should be the same if particle size effects in the root-soil interaction are absent. The curves are in excellent agreement during the first 2.5° rotation, and the initial rotational stiffness were practically the same. Beyond this, some discrepancies appeared. For the cases using p - y properties derived from FEM + BS (i.e. LR04 and LR08) their moment capacities (at approximately 9° rotation) are similar, around 0.37 kNm. The 5 % difference was due to differences in meshing between FEM simulations for the different diameter cases. The moment resistance of the 0.8 mm root, using the p - y property derived from the DEM simulation, was approximately 20 % higher, compared with that of the 3 mm root due to the difference in d_r/D_{50} (i.e. LR09 and LR05), implying particle size effects, similar to those illustrated in Fig. 7. Sharp drops of moment were observed at the end of simulations because roots were pulled out of the soil, where the force from most springs became to 0 under the large relative displacement. Moreover, it can be seen that the uplift resistances of the 3 mm root, in which the particle size effect could be neglected, using the properties derived from either DEM or FEM + BS (LR05 and LR04) are rather close, suggesting the suitability of the BS assumption for approximation of post-peak behaviour (in the absence of particle size effects) such that simple plane strain FEM simulations may be used to parameterise p - y curves in cases of sufficiently high d_r/D_{50} , rather than computationally expensive DEM simulations.

The simulations LR10 and LR11 had the same condition as LR08 and LR09, respectively, except that T_r and E_r were varied according to Eqs. (11) and (12) to consider the effects of diameter-dependency, which existed in physical model tests. Comparisons of the moment-rotation curves of these four simulations are depicted in Fig. 17(a). The results show that increasing the E_r (from 3 to 8.7 GPa) increased both the initial stiffness and the moment resistance by approximately 2.5 and 1.5 times. However, this in turn made the root response more brittle, having a much lower rotation angle corresponding to the peak resistance (θ_p), by approximately 50 %. Note that no plastic failure appeared within the root in any of the simulations, indicating that the soil had been

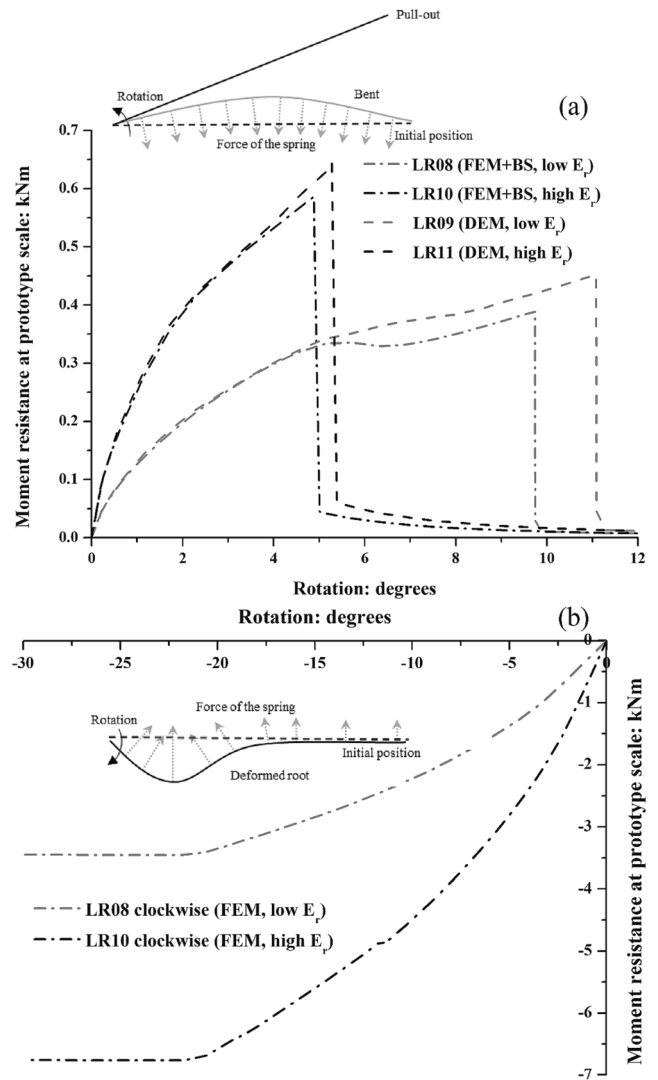


Fig. 17. Scale effects related to Young's modulus on root moment-rotation curve: (a) anticlockwise rotation; (b) clockwise rotation.

mobilised to its peak resistance before the roots broke and that the differences in root behaviour shown in Fig. 17(a) were due to the variation of the root Young's modulus rather than the tensile strength. Fig. 17(b) compares the cases of LR08 and LR10 but with the loading in the clockwise direction to simulate the whole lateral root pushed into the soil. In contrast to uplift cases, roots started yielding at 10° rotation and fully yielded at 21° rotation. In this case, the tensile strength of the root controlled the moment capacity, which was defined by the roots yielding and increased by approximately a factor of two resulting from the increase of T_r from 93 to 185 MPa. The stiffness of the root contribution to overturning resistance is also increased with increasing E_r , as with the uplift cases in Fig. 17(a). While it is common to measure tensile strength of plant roots, Young's modulus is rarely reported in the literature. The results here demonstrate the importance of the parameter on the contributions of individual lateral roots to tree overturning stability.

6. Conclusions

This study has presented an investigation into potential root size effects that may arise in the transverse uplift or push-in of horizontally-orientated plant roots, such as the lateral roots of trees during overturning. 3D DEM numerical simulations were validated against laboratory uplift tests and were then employed to work as a 'virtual centrifuge'

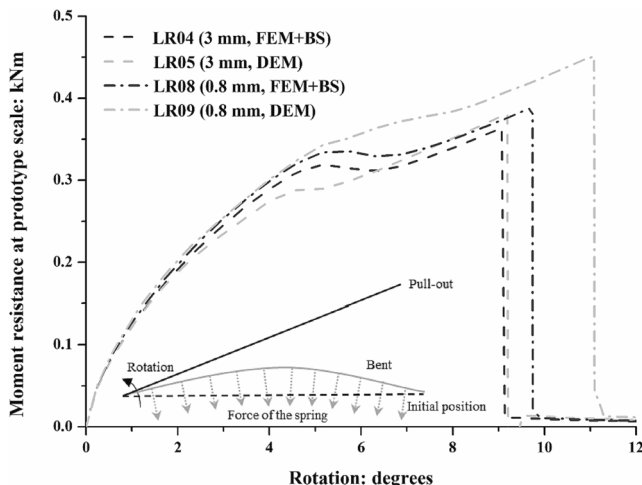


Fig. 16. Scale effects related to particle on root moment-rotation curve.

to replicate the behaviour of lateral root segments of different diameters interacting with a granular bed and allow the ratio of root to particle diameter to be changed with the same prototype geometry and confining stress conditions. Results were compared with validated FEM simulations, where the soil was considered as a continuum and strength parameters representative for low confining stresses were used.

It was found that a change in d_r/D_{50} did not significantly affect the push-in resistance. This implies that estimates of this element of resistance could be based on conventional continuum analytical approaches (e.g. bearing capacity of buried pipelines). In terms of the uplift resistance, particle size effects were observed when d_r/D_{50} was lower than 8, arising from the dimension of the additional uplifted soil block above the root with a width of $3.2D_{50}$, which is significant for a fine root but negligible for a coarse root. This was incorporated into an analytical expression for uplift resistance which validated well against the DEM data.

A series of simulations of whole lateral root rotation (consistent with tree overturning) were then performed in which a BNWF approach using p - y curves were obtained based on the previous DEM or FEM results. Due to difficulties in simulating large deformation in FEM, a simplified Bilinear Softening (BS) approximation was assumed to complete the uplift curve of the root post-peak. The scale effects related to particle size affected the peak moment resistance in uplift at prototype scale by approximately 20 % when d_r/D_{50} was reduced from 21 to 6 (corresponding to simulation of a 60 mm diameter root at either $N = 20$ or 75, respectively) and when root material properties were held constant. Comparatively, the variation in material properties with diameter typical of plant roots (i.e. following a negative power law) had a much larger controlling effect on the root moment capacity and stiffness when the whole root was uplifted and when pushed into the soil. In addition, E_r was important in the uplift case, where stiffer and stronger roots resulted in a reduction of θ_p (rotation at failure) and made the root response more brittle, while the moment capacity was principally controlled by T_r in the push-in case.

The results can be used to inform the design of physical model (e.g. centrifuge) tests of root-soil systems in terms of the selection of appropriate scale factors, and also provide guidance on input parameters for root-soil interaction models at field (1:1) scale. Further research using different particle size distributions, and thus varying d_r/D_{50} through different values of D_{50} , along with corresponding physical tests, are required to generalise these findings.

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Data availability

Data will be made available on request.

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