Article

A CFD Modelling Approach for the Operation Analysis of an Exhaust Backpressure Valve Used in a Euro 6 Diesel Engine

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Abstract: Harvesting residual thermal energy from exhaust gases with thermoelectric generators is one of the paths that are currently being explored to achieve more sustainable and environmentally friendly means of transport. In some cases, thermoelectric generators are installed in a by-pass configuration to regulate the mass flow entering the thermoelectric generator. Some manufacturers are using throttle valves with electromechanical actuators and electronic control in the exhaust pipe to improve techniques for active control of pollutant emissions in reciprocating internal combustion engines, such as the exhaust gas recirculation. The above-mentioned circumstances have motivated the approach of this work: computational fluid dynamics (CFD) modelling of the operation of a throttle valve used for establishing adequate exhaust backpressure conditions to achieve the low pressure exhaust gas recirculation in Euro 6 engines. The aim of this model is to understand the flow control process with these types of valves in order to incorporate them in an exhaust system that will include two thermoelectric generators used to convert residual thermal energy into electrical energy. This work presents a computational model of the flow through the throttle valve under different temperatures and mass flow rates of the exhaust gas with different closing positions. For all cases, the values of the pressure drop were obtained. In all cases studied, the level of agreement between the modelled and experimental results exceeds 90%. The developed model has helped to propose a correlation to estimate the mass flow rate of exhaust gas from easily measurable quantities.

Keywords: compression ignition engines; simulation; back pressure valve; performance

1. Introduction

The use of valves in reciprocating internal combustion engines, both spark and compression ignition engines, was a very common solution for mass flow regulation. Most typical examples are the use of throttle valves in carburetors [1–3] or in exhaust gas recirculation (EGR), for modifying the exhaust gas vorticity at the entry to the inlet manifold [3] or, during the last years, for regulating the back pressure in the exhaust pipe for controlling the high- and low-pressure EGR [4]. In this case, the authors proposed to change between high- and low-pressure EGR configuration depending on the engine operation for increasing the potential of use of both systems. A similar work is presented in [5], but in this case, the authors concluded that the angle of electronic-variable valves has impact on the back pressure in exhaust systems.

Other types of valves such as spool valves [6] or angle-seat valves [7] have also been studied and characterized for gas flow control. X. Pan et al. [6] studied the discharge coefficients of a servo-spool valve under laminar and turbulent flows. The authors established a mathematical model for the orifice flow by means of computational fluid dynamics (CFD) for solving the discharge coefficient and Reynolds number. In [7], the authors proposed a method for characterizing discharge and resistance coefficients of air discharged from a

reservoir. In this work, the authors used as a test valve an angle-seat valve with different opening sections. Gülmez and Özmen [8] presented a sensitivity analysis of the effect of a backpressure valve installed in the exhaust pipe of a diesel engine. They determined the level of the negative effect of the backpressure valve on volumetric efficiency of the engine among other parameters.

Harvesting residual thermal energy from exhaust gases is one of the paths that are currently being explored to achieve more sustainable and environmentally friendly means of transport [8,9]. In a previous work [10], the authors of this paper experimentally studied the effect of the installation in the exhaust pipe of a thermoelectric generator on the pumping losses of a Euro 3 diesel engine.

These facts have motivated the approach of this work: the thermo-fluid dynamic modelling of the operation of a current throttle valve used for establishing adequate exhaust backpressure conditions to achieve low-pressure exhaust gas recirculation in Euro 6 engines. The aim of this model is to understand the flow control process with these types of valves to incorporate them in an exhaust system that will include two thermoelectric generators to convert residual thermal energy into electrical energy as energy-harvesting technology. This work presents a computational fluid dynamic model that calculates the exhaust gas flow around of the back pressure throttle valve under different temperatures and mass flow rates of the exhaust gas with different closing positions. For all cases, the values of the pressure drop were obtained. In all cases studied, the level of agreement between the modelled and experimental results exceeds 90%.

The methodology, experimental facilities and techniques used are presented in Section 2. Section 3 describes the proposed 3D model of the backpressure valve and the fluid-mechanical model used. The experimental results of the tests, the results of the proposed model and its validation are developed in Section 4, while conclusions are presented in Section 5.

2. Experimental Installation and Methodology

Figure 1 shows different views of the experimental installation used in this work. As a gas generator, an early Euro 6 Diesel automotive engine with R9M code, mounted in NISSAN Xtrail vehicles, was used.

| (a) | (b) |
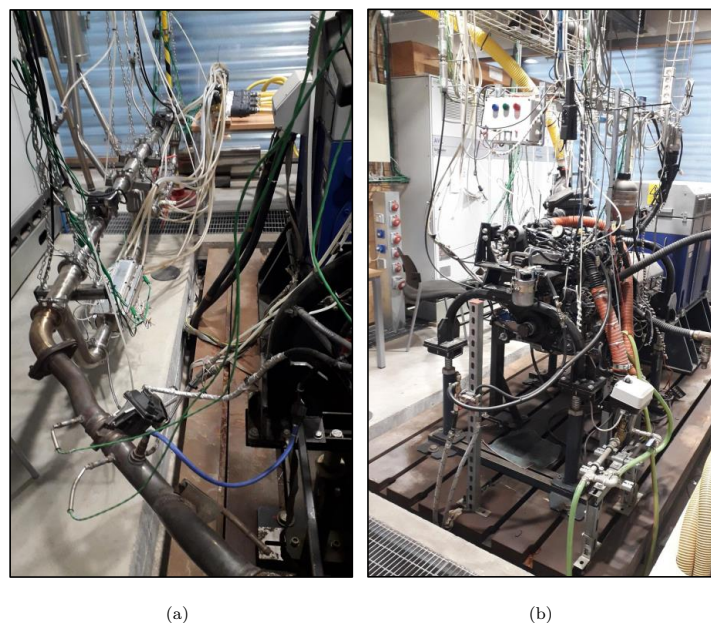
Figure 1. (**a**) View of the instrumented engine exhaust system. (**b**) Front view of the engine test bench.

The main characteristics of the engine tested are: 1.6 L, 4-cylinder, 4-stroke, with both hot flow & high-pressure and cooled flow and low-pressure exhaust gas recirculation

(EGR). The engine is also equipped with a variable geometry turbocharger with an inter-cooler and a common-rail injection system with fuel multi-injection. The exhaust system includes a diesel oxidation catalyst and a diesel particle filter as aftertreatment devices. The main values of the engine output are maximum-rated power 96 kW (at 4.000 min^{-1}) and maximum-rated torque 320 Nm (at 1750 min^{-1}). The engine was coupled to an AVL asynchronous electric machine working as a dynamometer. All the tests were carried out by means of the α/n control mode, through the AVL Emcon 400 control system. Fuel consumption was conditioned and measured by means of an AVL FuelExact 740. Thermodynamic diagnosis was carried out using an AVL IndiMicro 602 (which includes an in-cylinder pressure sensor GH14P and its glow plug adaptor AG03) and an AVL IndiCOM2013(2.5) system for combustion analysis. For registering both the engine speed and the piston position, both trigger and crankshaft angle pulses were provided by an AVL model 365C optical angle encoder coupled to the engine crankshaft.

Figure 2 shows a view of the exhaust back pressure valve (Pierburg, model PBT GF-30) under study in this work. This valve was originally used for the operation of the low-pressure and cooled EGR of the engine.


Figure 2. View of the exhaust back pressure valve.

Although the valve is normally electronically controlled by the electronic control unit (ECU) of the engine, for this work, the valve was independently controlled. Valve position was controlled by means of an electronic module designed for that purpose. It consists of a L298N DC motor driver, a MCP3208 high-precision analog-to-digital converter and an Atmega328p microcontroller. A block diagram of the designed electronic module is presented in Figure 3.
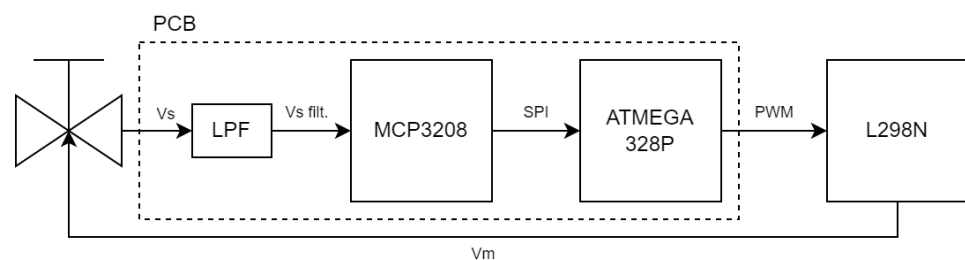
Figure 3. Scheme of the connection of the control module.

The regulator designed for the valve control is presented in Figure 4. This regulator was digitally implemented in the microcontroller as the sum of two different control algorithms: a sliding control to compensate for the force generated by the spring that has the valve on the shaft and a PID (proportional integral derivative) modified to the needs of the plant.
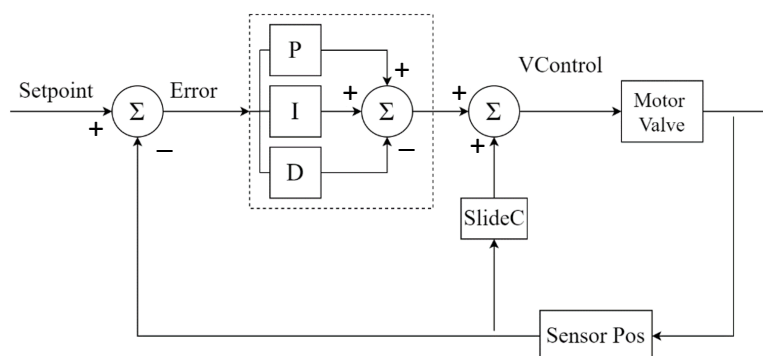
**Figure 4.** Block diagram of the regulator used for the valve control.

By complementing these algorithms with analog and digital filters, it is possible to position the butterfly with an error of only 0.7 degrees. The control is capable of effectively compensating for the disturbances generated by the thrust of the gas as well as eliminating electromagnetic interference from the environment.

Experimental tests have helped to understand the dependence between the backpressure valve closing angle, engine behaviour and exhaust gas flow. However, the main objective of the experimental data was to validate the proposed model. From the results of all simulations, a correlation was proposed with which the exhaust gas mass flow can be determined as a function of easily measurable engine variables. Being able to control the mass flow rate through the valve is essential in order to optimise the operating conditions of a thermoelectric generator installed in the exhaust pipe of an engine.

3. Model Description

3.1. Back Pressure Valve

In Figure 5a,b, it is shown how the backpressure valve is not symmetrical. It is convex on the upstream flow side and concave on the downstream flow side. Additionally, it is not completely circular. The diameter of the valve at its central part is greater than the inner diameter of the pipe, so that when the valve is completely closed, touching the inside of the pipe, the angle between the plane of the valve and the axial axis of the pipe is approximately 70 degrees. The 3D model of the valve is shown in Figure 5c,d for the upstream flow side and downstream flow side, respectively.

(a)　　　　(b)　　　　(c)　　　　(d)
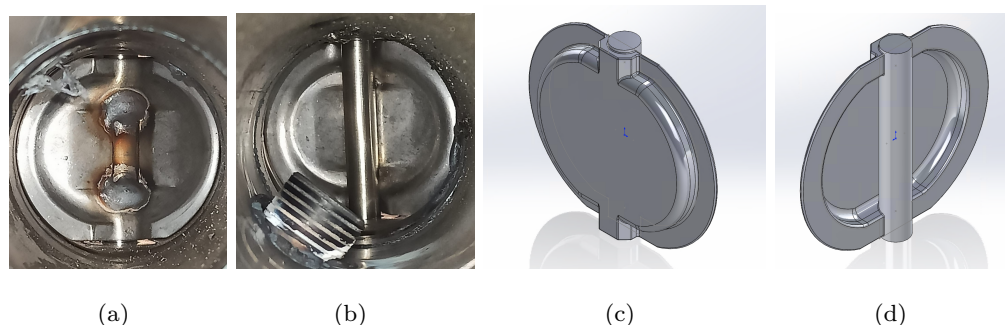
Figure 5. Physical model of the valve: (**a**) upstream side of the valve, (**b**) downstream side of the valve, (**c**) upstream side 3D model, and (**d**) downstream side 3D model.

Six models were created, one for each valve opening angle. As shown in Figure 6, the simulated valve openings range from 0 to 50 degrees in increments of 10 degrees. Figure 6 shows the isometric view of the six developed models.
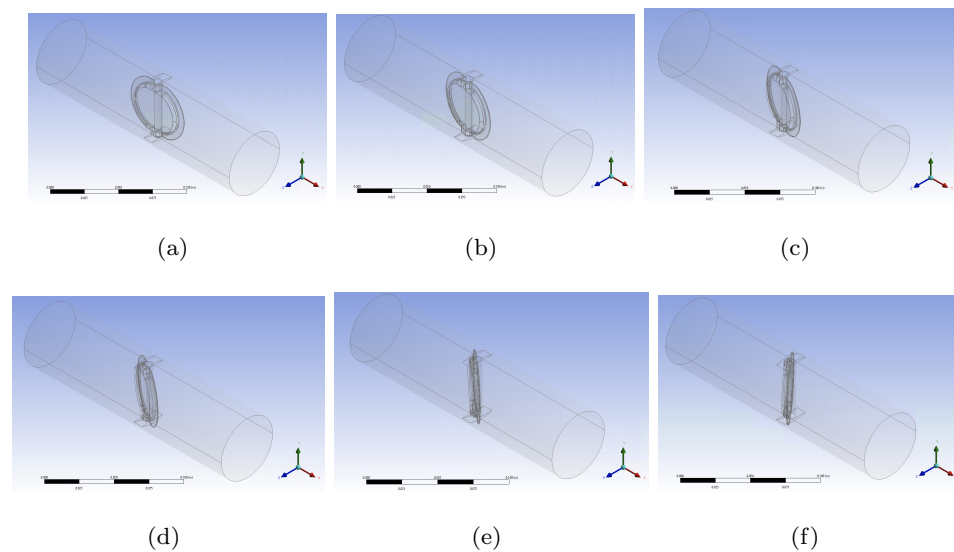
Figure 6. Three-dimensional model for each angle: (**a**) 0, (**b**) 10, (**c**) 20, (**d**) 30, (**e**) 40, and (**f**) 50 degrees.

The meshing of any of the models in Figure 6 was carried out taking into account the interaction of the fluid with the walls of the pipe and the valve using both hydrodynamic and thermal boundary layers. The inflation technique was used so that the maximum y^+ throughout the domain is less than 5, as shown in Figure 7. In this way, the shear stresses due to viscosity within the boundary layer are as close to reality as possible [11]. Four-node linear tetrahedrons and six-node linear wedges were used in the meshing. A mesh convergence study determined that the number of three-dimensional elements in the resulting mesh was between 3,400,000 and 4,000,000, depending on the valve opening. The quality of the mesh measured by the orthogonal quality parameter was around 0.15 in all cases, as a minimum value. As an example, Figure 7 shows the meshing of the model shown in Figure 6d.
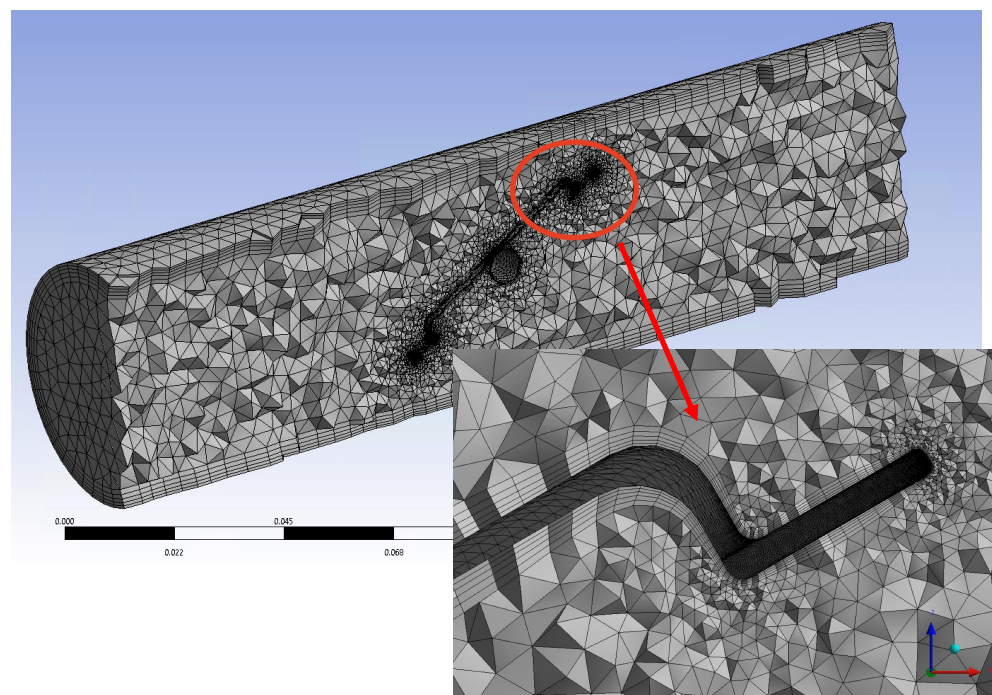
Figure 7. Axial–vertical cross-section of a 3D meshed model of a valve rotated 30 degrees from fully open.

It was considered that the radial temperature difference in the tube is negligible, and since the modelled valve is installed in a stationary engine test bench, heat dissipation outside the tube by natural convection, using the Churchill–Chu correlation, and radiation were considered. The inlet and outlet boundary conditions are of known mass flow rate and pressure, respectively. The turbulence boundary conditions are turbulent intensity equal to 5% and turbulent viscosity ratio equal to 10. The pressure–velocity coupling with the SIMPLE scheme was used as the solution method. Second-order spatial discretisation was used for pressure, density, momentum and energy, while first-order discretization was used for turbulent kinetic energy and turbulent dissipation rate. A convergence criterion of 10^{-3} was used for all variables, except for energy, which was set to 10^{-6}.

For each valve opening angle, seven gas inlet temperatures to the valve were simulated, ranging from 200 to 500 °C in steps of 50 °C, and nine mass flow rates, ranging from 20 to 100 g/s in steps of 10 g/s. Therefore, a total of 6 × 7 × 9 = 378 simulations were carried out. The geometries were created in SolidWorks®, the meshings were conducted in Ansys® Meshing® 2021 R2, and the simulations in Ansys® Fluent® 2021 R2.

The computer used to tune the models and perform sensitivity studies for each mesh was a Workstation Dell Precision 5820 with 28-core Intel Xeon W-2175, 2.5 GHz. The supercomputer used to perform the 378 simulations was Picasso, belonging to the University of Malaga, with 30,616 cores and 156 TB of RAM.

3.2. Turbulence Model

Mass flow rate was between 20 and 100 g/s. The average gas temperature was between 200 and 500 °C; thus, the dynamic viscosity was between 2.60×10^{-5} and 3.62×10^{-5} Pa·s.

Therefore, the average Reynolds number was between 13,500 and 94,200, indicating that the flow was predominantly turbulent. Turbulent flows can be simulated through computational fluid dynamic modelling using three different approaches: DNS (direct numerical simulation) [12], LES (large eddy simulation) [13,14], and RANS (Reynolds-averaged Navier–Stokes) [15]. The citation order corresponds to the decreasing calculation precision and increasing computational time cost.

As the bibliography review showed, most used methods for modelling the internal flow inside the exhaust pipe were Reynolds-averaged Navier–Stokes. Among the works which used the RANS method, most of the consulted works modelled the turbulence by means of $k - \varepsilon$ equations [16–19]. This is justified by the reasonable balance between the computational time cost and the precision of the calculation method.

The present work is based on renormalisation group (RNG) $k - \varepsilon$ turbulence modelling. This mathematical technique is used for solving the Navier–Stokes equations (Equations (1) and (2)) applied to each fluid. An exhaustive description of the RNG theory and its application to turbulent flows can be found in [20].

$$\frac{\partial}{\partial t}(\rho k) + \frac{\partial}{\partial x_i}(\rho k u_i) = \frac{\partial}{\partial x_j}\left(\alpha_k \mu_{eff} \frac{\partial k}{\partial x_j}\right) + G_k + G_{bu} - \rho\varepsilon - Y_M \tag{1}$$

$$\frac{\partial}{\partial t}(\rho\varepsilon) + \frac{\partial}{\partial x_i}(\rho\varepsilon u_i) = \frac{\partial}{\partial x_j}\left(\alpha_\varepsilon \mu_{eff} \frac{\partial\varepsilon}{\partial x_j}\right) +$$
$$C_{1\varepsilon}\frac{\varepsilon}{k}(G_k + C_{3\varepsilon}G_{bu}) - C_{2\varepsilon}\rho\frac{\varepsilon^2}{k} - R_\varepsilon \tag{2}$$

In Equations (1) and (2), G_k is the turbulence kinetic energy generation caused by the mean velocity gradients, G_{bu} is the generation of turbulence kinetic energy due to the floatability, while Y_M is the contribution of the dilatation variability in compressible turbulence to the overall dissipation rate. The terms α_k and α_ε are the inverse of the Prandtl numbers for k and ε, respectively.

For modelling thermal and hydrodynamic boundary layers, an enhanced wall treatment was used in Equation (2). Both pressure gradients and thermal effects were taken into account inside the boundary layers.

Enhanced wall treatment for the ε-equation is a near-wall modelling method that combines a two-layer model with so-called enhanced wall functions. If the near-wall mesh is fine enough to be able to resolve the viscous sublayer (typically with the first near-wall node placed at $y^+ \approx 1$), then the enhanced wall treatment will be identical to the traditional two-layer zonal model. However, the restriction that the near-wall mesh must be sufficiently fine everywhere might impose too large a computational requirement. Ideally, one would like to have a near-wall formulation that can be used with coarse meshes (usually referred to as wall-function meshes) as well as fine meshes (low-Reynolds number meshes). In addition, excessive error should not be incurred for the intermediate meshes where the first near-wall node is placed neither in the fully turbulent region, where the wall functions are suitable, nor in the direct vicinity of the wall, where the low-Reynolds number approach is adequate.

According to reference [21], the thermophysical properties of the exhaust gas are similar to those of air as a real gas at the same temperature and pressure. The majority of the composition of both gases is nitrogen. Both the density and viscosity of air vary with local pressure and temperature. The density of air was modelled using the Redlich–Kwong equation of state and dynamic viscosity using the Sutherland equation.

4. Results and Discussion

4.1. Test Results

4.1.1. Engine Operating Conditions

In Table 1, the measured average values for the four engine operating modes with the backpressure valve fully open are shown. $\dot{m}$ is the mass flow rate of exhaust gases. T_{up} and p_{up} are the temperature and pressure of the exhaust gases before the backpressure valve. As shown in Figures 8 and 9, for each of the four engine operating modes, the backpressure valve was progressively closed in steps of 10% up to 50%, and from that point onwards, in steps of 5%. For operating mode A, the backpressure valve was closed up to 80%, for mode B up to 75%, for mode C up to 60%, and for mode D up to 50%. This sequence was chosen to avoid affecting the normal behaviour of the engine, so that the extra pressure drop caused by the valve closure was always less than 160 mbar.

**Table 1.** Engine operating conditions.

Operating Mode:	A	B	C	D
Symbol in Figures	○	△	□	◇
Engine speed (min^{-1})	1500	1500	2000	2500
Torque (Nm)	50	100	150	200
BMEP (bar)	3.98	8.07	11.77	16.50
$\dot{m}$ (g/s)	19.47	26.88	47.75	73.78
T_{up} (°C)	241.12	309.83	353.46	432.42
p_{up} (mbar)	3.38	6.15	22.50	52.81

4.1.2. Valve Closing

As shown in Figure 8, the mean instantaneous pressure inside the combustion chamber was experimentally measured for each engine operating mode and backpressure valve closure. A total of 1440 points per thermodynamic cycle of in-cylinder pressure were recorded (each pressure value was recorded every 0.5 degree of crank angle). For all operating modes, 20 thermodynamic cycles were recorded and used to calculate the mean in-cylinder pressure.

For all engine operating modes, except for the high-load mode (mode D), a slightly decreasing trend is observed between the measured instantaneous pressure inside the combustion chamber and the degree of closure of the backpressure valve, as shown in

Figure 8a–c. This trend is consistent with that reported in [22]. This behaviour is consistent with the BMEP obtained for each mode (A, B, and C), as shown in Figure 9a. It can be concluded that, since the engine is turbocharged, a lower mass flow rate of exhaust gases through the turbine, as shown in Figure 9b, implies lower power production in the turbine and therefore lower power in the cylinder-boosting compressor, which slightly decreases the mean instantaneous pressure inside the combustion chamber.
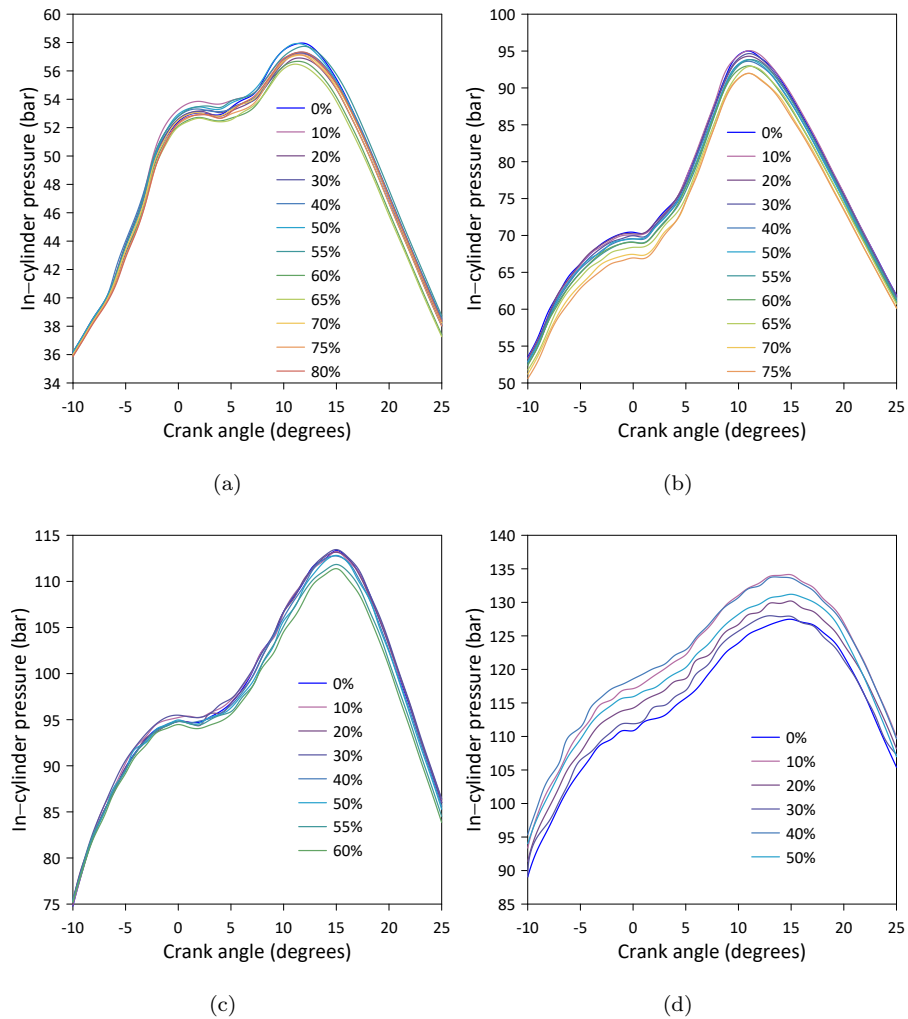

Figure 8. In−cylinder pressure vs. crank angle. (**a**) Mode A, (**b**) Mode B, (**c**) Mode C and (**d**) Mode D.

From Figure 8d, no clear trend can be observed between the instantaneous mean pressure inside the cylinder and the closure of the back pressure valve for the high-load operating mode (Mode D). This may be because, regardless of the decrease in the mass flow rate of exhaust gases circulating through the turbine, as shown in Figure 9b, the energy of the exhaust gases is more than enough to power the turbine and, consequently, the compressor that supercharges the engine.

From Figure 9d, it can be observed that with the increase in the degree of closure of the backpressure valve and therefore the decrease in the mass flow rate, ash shown in Figure 9b, the average temperatures upstream of the backpressure valve increase. This may be due to the decrease in the circulation velocity of the exhaust gas, which leads to a lower convective heat transfer coefficient within the exhaust pipe and consequently to a lower rate of dissipation of heat power.

(a)

(b)

(c)

(d)
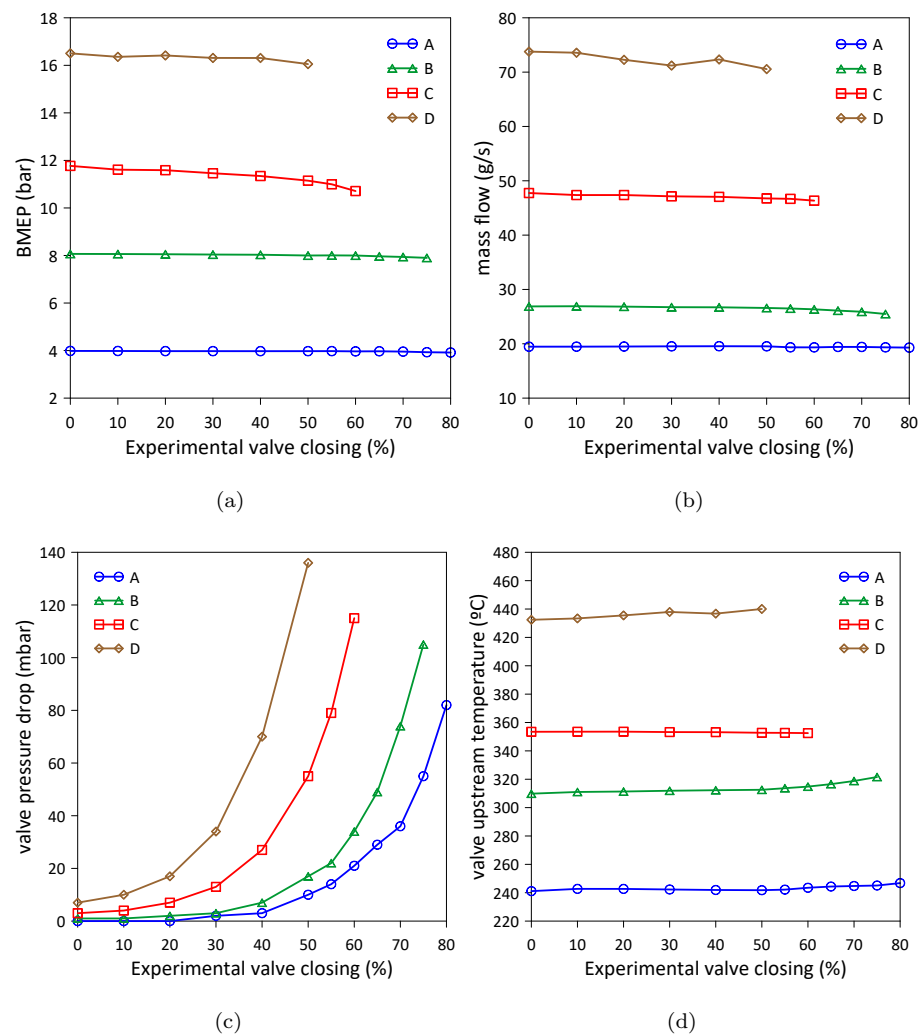
Figure 9. Average experimental data (**a**) BMEP, (**b**) mass flow, (**c**) valve pressure drop and (**d**) valve upstream temperature vs. valve closing.

Figure 9c shows how the increase in the degree of closure of the back pressure valve leads to a potential increase in the pressure drop of the exhaust gas as it passes through the back pressure valve [7].

4.2. Model Results

As an example, Figure 10 shows the velocity, temperature, and pressure results in the axial plane, and Figure 11 shows the streamlines of a simulation with the valve rotated 30 degrees from fully open, a mass flow rate of 60 g/s, and an upstream exhaust gas temperature of 400 °C. The results obtained are consistent with [22]. It can be observed that the acceleration of the gas as it passes through the valve implies a significant decrease in temperature, as a result of the transfer of thermal energy to kinetic energy, and therefore an increase in pressure drop.

As discussed in Section 3.1, a total of 378 simulations were carried out, with the following combinations: mass flow rate equal to {20, 30, 40, 50, 60, 70, 80, 90, 100} (g/s), valve rotation angle with respect to the fully open position equal to {0, 10, 20, 30, 40, 50} degrees, and gas temperature upstream of the valve equal to {200, 250, 300, 350, 400, 450, 500} (°C). The results of all these simulations are represented in Figure 12, classified by the valve rotation angle.

(a)

(b)

(c)
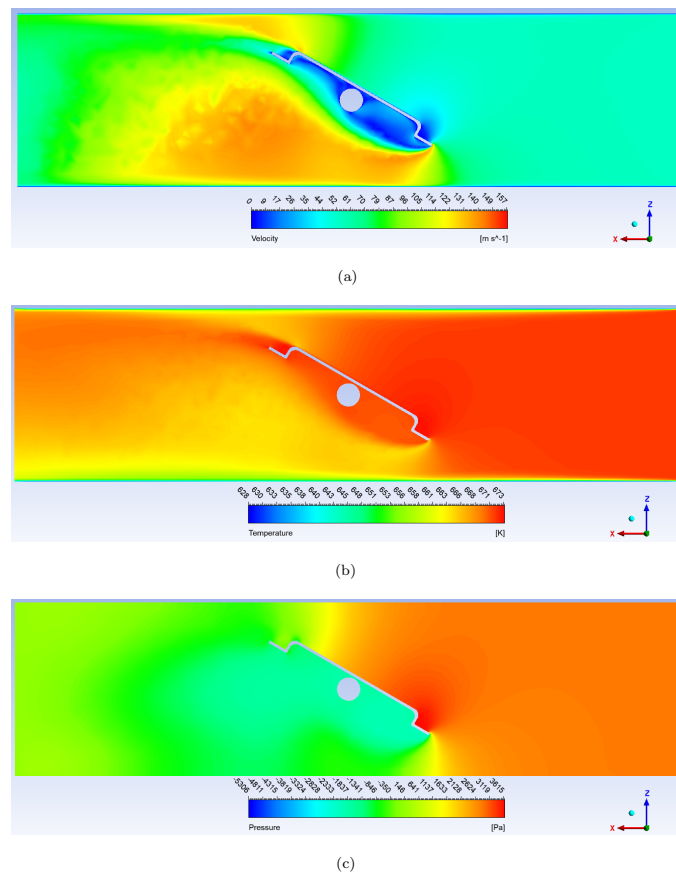
Figure 10. Valve closing 30 degrees. Velocity (**a**), temperature (**b**) and pressure (**c**) field in axial plane.
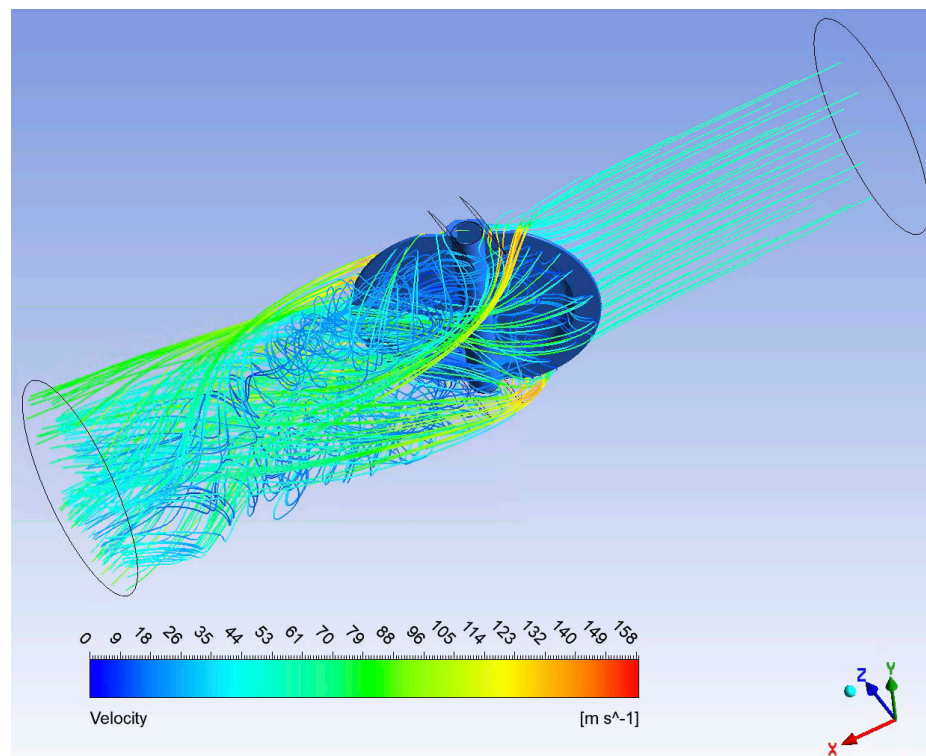

Figure 11. Streamlines in the valve closing 30 degrees.

In Figure 12, the colour map represents the drop in exhaust gas pressure in the valve under different conditions. Contour lines of constant exhaust gas pressure drop are shown.

It can be observed that the valve angle and the exhaust gas mass flow rate are the two factors that most affect pressure drop, while the temperature of the exhaust gas has a less significant effect. An increase in the valve closure angle results in an increase in pressure drop [5], due to the increased flow velocity. An increase in the exhaust gas mass flow rate results in an increase in pressure drop, as the flow velocity increases and the pressure drop increases with higher flow rates. A slight increase in exhaust gas temperature results in a minor increase in pressure drop due to a decrease in density, resulting in a minor increase in gas velocity, while the mass flow rate remains constant.

In Figure 12, the experimental measurements of the four modes tested experimentally are shown. The percentage of valve closure in which the experimental pressure drop in the valve is of the same order as the pressure drop resulting from the modelling is shown in parentheses.
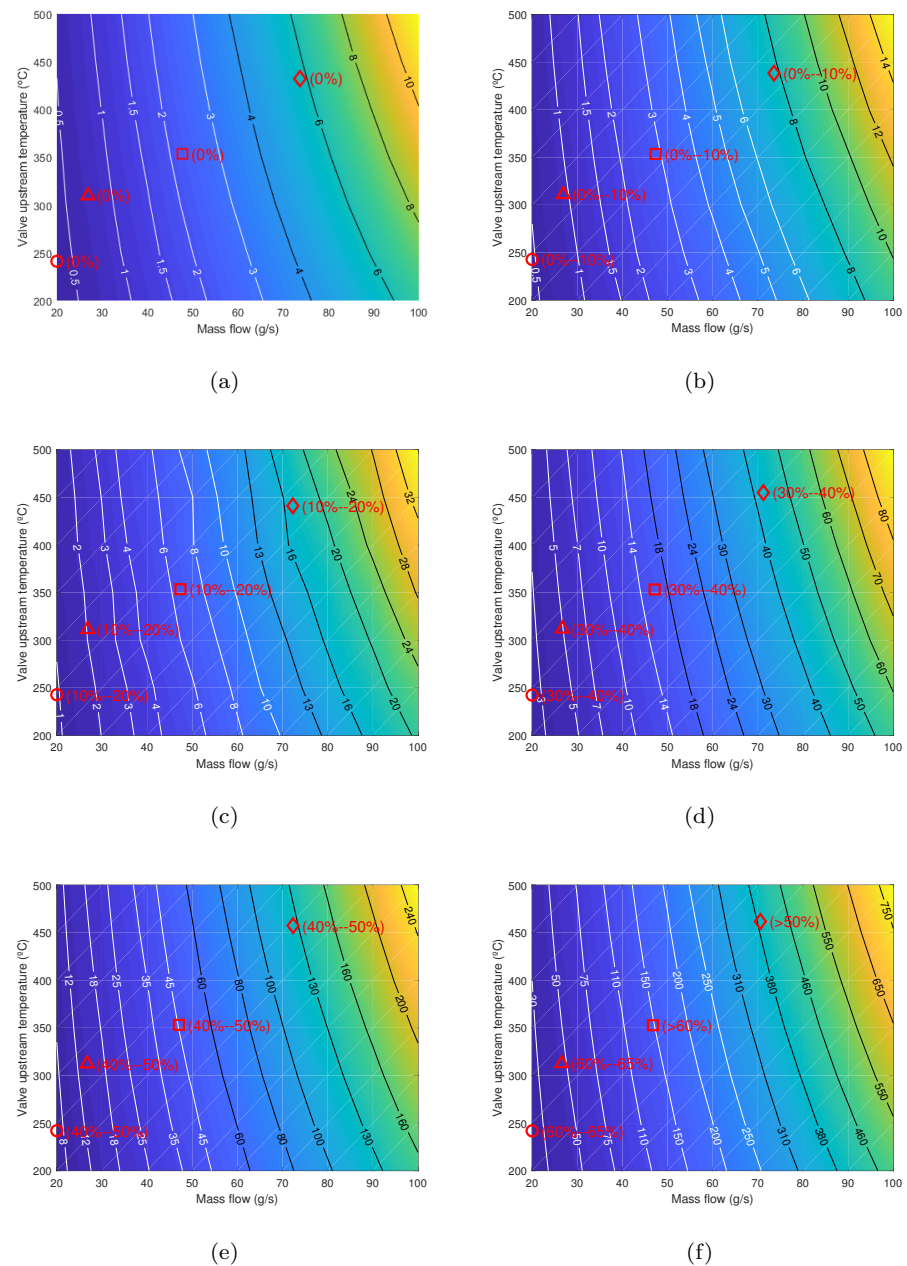
Figure 12. Pressure drop (mbar) vs. valve upstream temperature and mass flow. Closing angle: (**a**) 0, (**b**) 10, (**c**) 20, (**d**) 30, (**e**) 40 and (**f**) 50 degrees.

In experimental tests of flow in a back pressure valve, it is more cost-effective to measure the pressure drop using a differential pressure gauge than to measure the mass flow rate. Therefore, a correlation is proposed based on the results of the simulations that relate the four variables, Equation (3). The result of this correlation is the mass flow rate $\dot{m}$ in (g/s). A correlation coefficient of $R^2 = 0.984$ and a mean squared error of 0.32 were obtained.

$$\dot{m} = 181.8(1 - \sin(\theta))^{1.51} T^{-0.28} \Delta p^{0.50} \qquad (3)$$

In Equation (3), θ is the angle of rotation of the valve with respect to the fully open position, T is the temperature of the gas upstream of the valve in °C, and Δp is the pressure drop of the gas through the valve in mbar.

The experimental valve closing angle is difficult to measure, and even if it is measured, the actual value may differ from the assumed one. To quantify this deviation, the angle that the valve should have (*y*-axis of Figure 13) was compared with the experimental valve closing angle measured (*x*-axis of Figure 13).
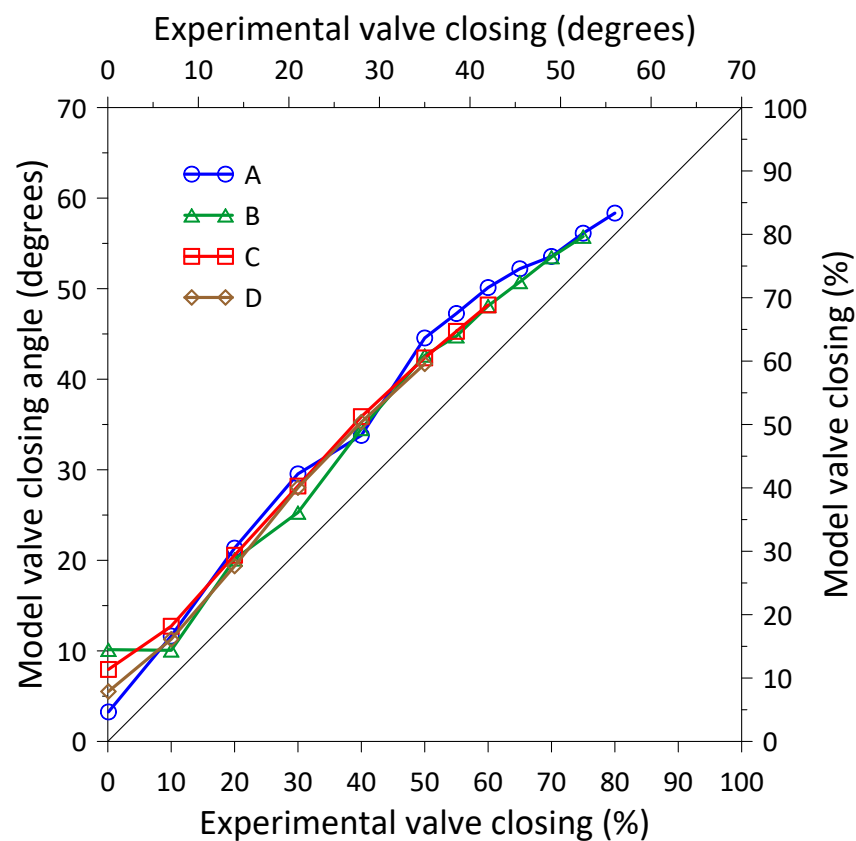

Figure 13. Model valve closing angle vs. experimental valve closing angle.

In Figure 13, it is shown that there is a linear correlation between the experimentally measured valve closing angle and the valve angle obtained with the correlation of Equation (3). For all test modes with closing angles less than 50 degrees, there is a deviation of about 5 degrees between the two angles, with the experimentally measured angle being lower than the one obtained by the correlation.

5. Conclusions

The fluid-dynamic behaviour of an electronically controlled exhaust backpressure valve was analysed, operating at different opening degrees under different speed regimes and load degrees of a Euro 6 internal combustion engine. The following conclusions can be drawn from this research:

- The negative effect that the closure of the backpressure valve has on the instantaneous in-cylinder pressure was observed. Assuming no effect on the average pressure inside the cylinder with full opening, a reduction in the in-cylinder pressure was measured between 1.3% and 3.9% for valve closures between 50% and 80%, respectively, for medium–high load levels.
- It was observed that with an increase in the closure of the pressure relief valve, the effective average pressure of the engine decreases between 0.07 and 1.06 bar for valve closures between 50% and 80%, respectively, for medium–high load levels. However, for that range of valve closures, increases in the temperature of the exhaust gases upstream of the valve are observed between 5.7 and 11.7 °C.
- The development of this work has made possible to propose a CFD model. With this model, the flow around the valve was simulated under different temperatures and the mass flows of exhaust gas and different closing positions of the backpressure valve. For all cases, pressure drop values were obtained. The level of agreement between the results obtained by the model compared to experimental measurements is around 91%.
- The developed model helped to propose a correlation to estimate the mass flow rate of exhaust gas from easily measurable quantities on a test bench, such as gas temperature, valve closing angle, and pressure drop.
- A positive deviation of around 5 degrees of backpressure valve closing was obtained between the modelled angle and the experimental angle for all engine operating conditions and all valve closing angles.

Abbreviations

C	constant
G	generation
k	turbulence kinetic energy
$\dot{m}$	mass flow rate
p	pressure
t	time
T	temperature
u	velocity
x	direction
Y_M	fluctuating dilatation
α	inverse Prandtl number
ε	rate of dissipation
μ	dynamic viscosity
ρ	density

Subscripts

bu	buoyancy
ε	rate of dissipation
i	index
j	index
k	turbulence kinetic energy
up	upstream

Acronyms

BMEP	Brake Mean Effective Pressure
CFD	Computational Fluid Dynamic
DNS	Direct Numerical Simulation
ECU	Electronic Control Unit
EGR	Exhaust Gas Recirculation
LES	Large Eddy Simulation
PID	Proportional Integral Derivative
RANS	Reynolds Averaged Navier–Stokes
RNG	Re-Normalization Group

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