New Jersey Institute of Technology Digital Commons @ NJIT

Theses

**Electronic Theses and Dissertations** 

6-30-1954

## Linear growth rates of single copper sulfate crystals

Arthur Oswald Hansen New Jersey Institute of Technology

Follow this and additional works at: https://digitalcommons.njit.edu/theses

Part of the Chemical Engineering Commons

### **Recommended Citation**

Hansen, Arthur Oswald, "Linear growth rates of single copper sulfate crystals" (1954). *Theses*. 2256. https://digitalcommons.njit.edu/theses/2256

This Thesis is brought to you for free and open access by the Electronic Theses and Dissertations at Digital Commons @ NJIT. It has been accepted for inclusion in Theses by an authorized administrator of Digital Commons @ NJIT. For more information, please contact digitalcommons@njit.edu.

# **Copyright Warning & Restrictions**

The copyright law of the United States (Title 17, United States Code) governs the making of photocopies or other reproductions of copyrighted material.

Under certain conditions specified in the law, libraries and archives are authorized to furnish a photocopy or other reproduction. One of these specified conditions is that the photocopy or reproduction is not to be "used for any purpose other than private study, scholarship, or research." If a, user makes a request for, or later uses, a photocopy or reproduction for purposes in excess of "fair use" that user may be liable for copyright infringement,

This institution reserves the right to refuse to accept a copying order if, in its judgment, fulfillment of the order would involve violation of copyright law.

Please Note: The author retains the copyright while the New Jersey Institute of Technology reserves the right to distribute this thesis or dissertation

Printing note: If you do not wish to print this page, then select "Pages from: first page # to: last page #" on the print dialog screen



The Van Houten library has removed some of the personal information and all signatures from the approval page and biographical sketches of theses and dissertations in order to protect the identity of NJIT graduates and faculty.

#### LINEAR GROWTH RATES OF SINGLE

#### COPPER SULPATE CRYSTALS

#### BY

#### ARTHUR O. HANSEN

POLYTECHNIC INSTITUTE OF BROOKLYN, 1950

SUBMITTED IN PARTIAL PULFILIMENT

OF THE REQUIRIMENTS

FOR THE DEGREE OF

MAST R OF SCIENCE

IN CHEMICAL ENGINEERING

IN THE

GRADUATE DIVISION

### AT THE

NEWARK COLLEGE OF ENGINEERING

1954

SIGNATURE OF AUTHOR

#### TABLE OF CONTENTS

Title Page Approval Sheet Acknowledgement Abstract

Introduction

- I Review of Literature
- II Description of Apparatus
- III General Procedure
  - IV Sequence of Study
  - V Detailed Procedure
    - A. Measurement of Solution Concentration
    - B. Solubility Data
    - C. Measurement of Crystal Growth
- VI Celculations
- VII Data
  - A. Pertinent Data
  - B. Primary Data
  - C. Calculated Data
  - D. Summary of Hixson-Knox Data
  - E. Summary of McCabe-Stevens Data
- VIII Disgrams and Graphs
  - IX Discussion
  - X Nomenclature
  - XI Bibliography

APPROVAL SHEET

APPROVED BY

Contraction of the Party

والمركبين بالملاق

0.07

ويستعاده ووجها

## ACKNOWLEDGEMENT

The writer gratefully acknowledges the counsel and advice of Executive Associate George Keeffe throughout the course of this thesis; and the permission of Mr. T.J. Sullivan for use of the crystel apparatus in this work.

#### ABSTRACT

The purpose of this work was to study and measure the factors influencing crystal growth.

Approximately 250 single crystals of CuSO4.5H20 were grown under controlled conditions of supersaturation, solution velocity, and temperature.

The data from this work indicates that:

- (a) Crystal growth rate is independent of crystal size for the size range covered (4 to 12 mesh).
- (b) Crystal growth rate is directly proportional to the degree of supersaturation, or driving force for each concentration of solution studied.
- (c) Crystal growth rate varies exponentially with the velocity of the solution passing the crystal

$$R_{b} = f(u^{m})$$

(d) The value of the exponent "m" increases as the temperature (and concentration) of the growth solution increases. This indicates that there must be more than one dimensionless group containing the velocity term.

> The following empirical equations were obtained for the four different solutions used:

Solution A	- Saturation temperature = 28° C.
	$L_{ag} \frac{R_{b}}{AC} = 0.240 \ Log 22 + 0.2900$
Solution B	- Saturation temperature = 37° C.
	$\log \frac{R_0}{AC} = 0.265 \log 11 + 0.5682$
Solution C	- Saturation temperature = $47^{\circ}$ C.
	$\log \frac{R_0}{\Delta c} = 0.288 \log 12 + 0.6128$
Solution D	- Saturation temperature = $58^{\circ}$ C.
	$Log \frac{R_0}{AC} = 0.407 \ Log 2 + 0.6721$

(e) The following empirical equation was derived which composites the above equations and which effectively summarizes all the data in this work:

$$R_{0} = 30,000 \text{ AC } u^{2} \text{ C} \frac{-400 \text{ m}}{T}$$

The velocity range in this work was from 2.2 to 20.6 centimeters per second.

#### INTRODUCTION

Although crystellisation continues to be one of the most important unit operations, little is known of the mechanism by which crystel growth takes place.

To obtain such knowledge, many growth studies of single crystals are necessary. It is generally understood that the two prime factors governing growth rates are the diffusional or physical process, and the chamical or ionic orientation reaction. Undoubtedly the relative importance of these factors vary with each crystalline substance.

It is believed that the growth process is an intermittent one, and not continuous. A definite activation energy is required to form a "unit" or "step" on a crystal surface, after which a layer of definite thickness rapidly "fills up" the remaining available crystal area. This concept explains many growth phenomena such as:

- (2) retention of geometric shape
- (b) strained growth under forced conditions
- (c) "twinning" this writer accounts for such a phenomena by visualising two crystals colliding face to face at the instant a layer is being formed.
- (d) growth of crystals in this work, wherein one side of a crystal is exposed to the full force of solution flow.

This study of the unit operation of crystallisation was made to confirm and supplement the past work of MeCabe and Knox. This writer has attempted to obtain data, correlate the effects of the prime variables, and develop expirical relationships in an original manner. Use of equipment and utilities was permitted by the Supervisor of the Research Department of the American Apricultural Chemical Co. at Carteret, N.J., for increased understanding of crystallization problems.

In conducting this study, and apparatus was used which composites many features used by perhaps a dozen different investigators. The following minor objectives were kept in mind in order to obtain the final correlations:

> 1. Simultaneous growth of several different size crystals under identical conditions of supersaturation, velocity, and concentration.

- 2. Obtain a greater degree of supersaturation than that obtained by previous investigators.
- 3. Ascertain the quantitative effect of supersaturetion under conditions of constant velocity.
- 4. Simultaneously grow single crystals under variable velocity but constant supersaturation conditions. This was not attempted by previous investigators.
- 5. Devise a simple, precise method for measuring solution concentration.
- 6. Obtain solubility data for the copper sulphatewater system of greater accursoy than data in the International Critical Tables and Scidell's "Solubility of Inorganic Compounds". Solubility data from these two references do not agree.

It is believed that this paper is the first to present the fact that solution velocity (agitation) exerts greater influence on a crystal growth process at high temperatures than at low temperatures. This is confirmed by a study of the data of Hixson-Knox.

This paper is the first to indicate that the growth rate of copper sulphate is directly proportional to the degree of supersaturation.

This is confirmed by a study of the data of Hizson-Knox.

#### References

- (9) <u>Curie 1885</u> "Each face of a crystal has a capillary constant which controls growth rate".
- (9) <u>Wulff 1901</u> This writer measured velocities of growth of ferrous alum and found that every face had its own rate of extension measured normally to surface. He assumed the capillary constants were proportional to the rates of growth of the various faces.
- (9) Noyes-Whitney dissolution theory

$$\frac{dW}{dt} = -R_0 = kA (AC)$$

(8) <u>Noves-Whitney</u> - rotated sticks of bensole acid and PbClp in fresh water at constant velocity and constant temperature. The following relation was obtained:

$$kt = ln \left[ \frac{c_s - c_o}{c_s - c} \right]$$

- (8) <u>Mars R. 1908</u> found certain salts whose rate of srystallization was independent of stirrer speed.
- (9) <u>Mars & 1912</u> "For many substances at low rates of growth and low supersaturation growth is a bimolecular or second-order reaction. As supersaturation increased the growth approached a first-order reaction".
- (9) <u>LeBlane-Sehmant</u> Studied several salts and found value of K in Noyes-Whitney equation to be different for growth and dissolution.
- (9) Nornat Modified Noyes-Whitney equation.

$$\frac{dy}{dt} = \frac{DA}{S} \times \Delta C$$

- (9) <u>Berthand</u> Stated that solution at surface of growing crystal was not saturated but was slightly supersaturated - growth occurs in pulses, is discontinuous.
  - (a) first order reaction:

$$\frac{dx}{dt} = k A [C_i - C_o]$$

(b) then stationary state - diffusion takes place

$$\frac{dx}{dt} = \frac{DA}{S} \left[ c_{B} - c_{i} \right]$$

#### References

(c) combining above equations:

$$\frac{1}{\overline{A}} \frac{\partial \chi}{\partial t} = \frac{D}{\delta + D/k} (c_B - c_o) = R(\Delta c)$$

(9) <u>Wenk, W.</u> (pupil of Marc) - Experiments with potassium sulfate.

$$\frac{dn}{dt} = k(c_{B}-c_{0})^{2}$$

(10) <u>Compbell, N.P. 1915</u> - The author suspended single potassium alum crystels in a slightly supersaturated, agitated solution. Obtained the relationship:

(2) <u>Wilhelm, Conklin & Sauer (1941)</u> - The rate of solution of sodium chloride crystals was studied - the following equation was obtained:

$$-\frac{\Delta w}{\Delta t} = \frac{D}{\delta} A \left( c_{s} - c_{B} \right) = k A \left( \Delta c \right)$$

- <u>du</u> = mass transfer rate
  - A = area of particles
  - D = specific diffusivity
  - 6 affective film thickness
  - k = diffusion rate constant
- (3) <u>Hirson, A.W. 19hk</u> Aut or described the effect of agitator speed on velocity of heterogenous resations.

K= ~NB

- where: K = reaction velocity constant
  - N = rpm of stirrer
  - $\propto, \beta$  = constants
- (a) When a reaction is diffusion controlled  $\beta \approx 1$ .
- (b) When reaction is controlled by the rate of interfacial reaction,  $\beta \rightarrow 0$
- (4) <u>Van Hook 1944</u> This writer added measured quantity of 40-60 mesh sucrose seeds to an agitated vessel containing supersaturated sugar syrup. He repeated this experiment with syrups of different saturations and obtained the following correlations:

$$-\frac{\partial c}{\partial t} = k \left( c - c \infty \right)$$
where  $k = \frac{1}{t} \log \frac{m_0 - m_\infty}{m - m_\infty}$ 

- C = weigh fraction sucrose in syrup  $C_{\infty} =$  fraction in saturated syrup No = refractive index of initial syrup m . final refractive index of syrup mon = index of saturated syrup t a time
- Van Hook 19hh Found that increasing viscosity of (5) sugar syrups did not effect orystallization rate. Viscosity was increased by addition of gum acacia and starch.
- <u>Hixon and Knox 1951</u> These authors collected voluminous data on the growth of single crystals of (6)copper sulfate and magnesium sulfate. The authors were able to correlate their data in the following mannert
  - (a) Diffusion mass transfer <u>[FoDE]</u> = c <u>DeVP</u> d <u>L</u> <u>Dm</u> e
  - (b) Surface reaction

$$W_{a} = F_{R} (M_{F} - M_{i})^{\alpha}; lm F_{R} = \frac{E}{RT} + b$$

(c) Diffusion - heat transfer

The authors considered this to be of negligible effect in the systems studied.

W.L. McCabe - R.P. Stevens - 1951 - Seed crystals of copper sulphate were introduced into a supersaturated solution which was agitated in a conventional vessel. Rate of growth was correlated with crystal size and degree of supersaturation:

It was thought that the crystal size was not a prime variable, but rather an apparent one since the relative velocity between solution and crystals increases as the crystal size increases under normal mixing conditions.

(7)

## References

Seed crystals were then enclosed in a perforated cage which was suspended in a flowing stream of solution. Experiments were also carried out in a reciprocating cage.

General correlation:

$$\frac{1}{F_g} = \frac{1}{F_o + \beta 2L} + \frac{1}{F_i}$$

$$F_g = \text{growth rate - }^{M/min}$$

$$F_o = \text{growth rate at zero velocity}$$

$$B = \text{constant}$$

$$\mathcal{L} = \text{velocity - }^{CM/sec.}$$

$$F_i = \text{interfacial growth rate}$$

V. Description of Apparatus

The apparatus used for the bulk of this work consists of the following:

- (1) <u>Orystalliser Tube</u> A pyrex glass tube 1-7/8 inches in diameter and about three feet high. The tube is provided with a tapered bottom and three outlets.
- (2) <u>Crystal Basket A basket constructed of 15</u> mesh copper screen was used to support 3 or h single crystals. The basket is supported in the crystalliser tube by means of a copper wire attached to a rubber stopper.
- (3) <u>Thermometer</u> (accurate) Temperature of the solution flowing past the growing crystal measured by a 0-110°C. thermometer (divisions 0.1°C.).
- (h) Dissolver A four liter Pyrez beaker.
- (5) <u>Heater</u> An electric heater designed for submersion in corrosive liquids. This heater is constructed of stainless steel and provided with 3 settings (low, medium, high) for variable heat output. This writer fitted the heat output adjustment knob with a numerical scale (reading 0-10) for better control of heat output. The heater is manufactured by the Stillman Co., N.Y.C. under the trade name "Chill Chaser".
- (6) <u>Recycle Pump</u> A steinless steel centrifugal pump used for circulating the copper sulphate solution.
- (7) <u>Thermometer</u> (ordinary) An ordinary 0-110°C. mercury thermometer.
- (8) <u>Cooler</u> an ordinary laboratory condenser provided with inlet and outlet for cooling water.
- (8A) <u>Cooler</u> a copper coil five feet long and 1/4 inch dismeter used in place of the glass cooler (8) to obtain greater cooling capacity.
- (9) <u>Small cool water tank</u> a two liter beaker provided with a bottom outlet.
- (10) <u>Cool water pump</u> same type pump as (6) used for circulating cooling water.

- (11) Large cool water tank An eight gallon iron bucket used for storing cooling water.
- (12) <u>Press crystallising tubes</u> three brass pipes (1", 3/4", 1/2" IPS) connected in series with or without the glass crystallizer tube to obtain 3 or h solution velocities.

×

× ,

(13) <u>Control Panel</u> - Consists of two dial-rheostats (SERIE FERDING 0-100) for controlling flow rates of copper sulphate solution and cooling water.

#### VII. <u>Oeneral Procedure</u>

A solution of predetermined concentration of copper sulphate is introduced into the crystallisation apparatus. By preheating the solution 10-15°C. above the saturation temperature, crystallisation, or freeze up in the apparatus is avoided.

The solution pump is then started to circulate the solution around the apparatus. The cooling system is then placed in operation to bring the solution down to the saturation temperature. As the saturation temperature is approached, the electric submerged heater is turned on. To maintain a stable system, the solution temperature in the dissolver is kept above saturation. By controlling the degree of heat input plus heat removal from the system, any desired supersaturation can be maintained in the crystallizer tube.

The solution is then sampled for a check on the concentration by taking a hot Baume measurement (see Detailed Procedure).

Three or four different size crystals (6 to 12 mesh) are then individually weighed and placed in a copper wire basket, which in turn is suspended in the top of the crystallizer tube. The time is then noted.

A record of the crystallizer temperature is kept throughout the run.

After the growth period (from 20 to 120 minutes depending upon growth rate) the crystals are removed and weighed.

The cooling and heating adjustments are then changed in preparation for the next run.

Care is taken to insure that the temperature in the dissolver is above the saturation temperature. Otherwise, the solution will "break" and freeze up the entire apparatus. When this occurs, the tedicus operation of dissembling, cleaning and reassembly of the entire apparatus is often necessary.

With most of the growth experiments, the solution was raised 5-10°C. above the saturation temperature for 15-30 minutes between each run. This dissolved any small arystals (rarely present) in the cooler or the line leading to the crystallizer. From 3 to 8 experiments (runs) were made in a series. Fresh solutions were made up for each series. Dust particles and insoluble matter were removed by filtering through Super-Cel.

#### IV. Sequence of Study

Potassium alum was the material first selected for study since large crystals of this substance may be grown with comparative case. Considerable experimental time was devoted to the simultaneous growth of single crystals and a fluidized crystal bed. The single crystals were permitted to grow suspended in a wire basket at the top of a crystallizer tube. A moving bed of crystals at the lower tapered end of the crystallizer tube was permitted to grow at the same time under identical conditions of concentration and temperature.

After four such experiments the system for study was changed to GuSO<sub>H</sub>.5H2O because of the greater availability of physical data such as viscosity, density, etc. Furthermore, it was desired to check the data with that of McCabe (1) and Hixson (2).

Experiments number 5, 7, and 8 were conducted to simultaneously measure growth rates of single crystals and a fluidised bed as was proviously done with alon.

The rest of the experiments were concerned with the growth of single crystels only for reasons later taken up in the discussion.

Runs 5, 6, 7, 8, were designated as Series I, and the results were found to be of a magnitude similar to that reported by Macabe (1), for solutions at 28°C.

For the second series a solution concentration of 63 grams CuSOL. ShoO per 100 grams of free water ( $C_{\rm p}$  = 63) was prepared (saturation temperature about 1.7° C). For this series, velocity was kept constant and  $\wedge C$  was varied.

A copper cooling tube was substituted for the glass cooling condenser prior to Series III.

Series III was also carried out at about  $h7^{\circ}$  C., at constant velocity, and under conditions of variable supersaturation ( $\Lambda$ C).

For Series IV and V, the glass crystalliser tube was replaced by three brass tubes (1" IPS, 3/4" IPS, 1/2" IPS) connected in series. Crystals were grown in each of these tubes in order to ascertain the effect of velocity on growth rate. A velocity range of 2.8, 7.0, 11.5, and 20.6 on per second was thus obtained. With the glass orystalliser tube, the velocity range was limited by the output of the pump. Series VI was conducted to check Series III. Series III, IV, V, and VI, were done using about the same concentration of solution (Cg = 63,  $T_{\rm S}$  =  $47^{\circ}$  C).

Series VII was done at one velocity using a weaker solution ( $C_B = 53$ ,  $T_S = 37^\circ C_*$ )

The eighth series was conducted using the three brass tubes and a solution having same concentration as Series VII.

To cover further the study of the concentration and velocity variable, series IX and X were carried out using solutions ( $C_B = h\mu_s$ ,  $T_S = 27^\circ$  0.) and ( $C_B = 78$ ,  $T_S = 58^\circ$ 0.). The effect of four different solution velocities was obtained by connecting the glass crystallizer tube and the three brass tubes in series.

#### DETAILED PROCEDORE

#### MEASUREMENT OF SOLUTION CONCENTRATION

The copper sulphate used in this work was of a technical grade:

Brand Name :	Nichols Triangle Brand
Producert	Phelps Dodge
Coppert	25.2% Cu Minimum
Blue Vitriol:	99% Minimum
Insolubles:	1% Nazimum

#### Method

1. A weighed amount (40-150 gm) of crystals in a 400 cc beaker is dissolved by heating with approximately 300 cc of water. The temperature of the solution is then brought to 63°C.

The well-mixed solution is then quickly weighed and transferred to a hydrometer sylinder. A standardized hydrometer is then inserted and a reading rapidly taken. The temperature is then noted (invariably  $60^{\circ}$  C  $\pm$  0.3°)

Data	Gma TAY	<u>Gas Soln</u>	<u>\$ AV</u>	Be 60
	90+0	305.5	29.4	24.2
	105.0	298.1	35.2	29.0
	120,1	301.8	39.8	32+7
	135.0	304+4	44.3	36.7
	150+0	440.4	34.08	29.1
	90.1	369.6	24.4	20.05
	45.2	364.2	12.4	9.4

2. The data was then plotted on a large sheet of graph paper (rectangular coordinates). The seven points were found to lie on a straight line which when extended gave a negative baume value (~2.2° Be) at zero percent CuSOL.5HpO. This was expected since the plot was based on a temperature of 60° C.

- 3. About 25 points were then picked from the plot and recalculated. Weight percent was converted to Grams CuSOL.5H20 per 100 gms. of free water.
- 4. The 25 values were then replotted as gms Cu304.5H20 per 100 gm. of free water vs. Be 60°C. (Figure I)

Concentration data for this work (C<sub>p</sub>) was obtained from Baume data by the use of this plot. Some skill and reasonable speed is required for taking the baume data, otherwise surface evaporation will change the concentration. DETAILED PROCEDURE - SOLUEILITY DATA

- 1. Set up apparatus as shown on Figure C.
- 2. Add copper sulfate solution and a large excess of 20 mesh crystals to the inner beaker so that the liquid level is even with that of the outer water bath.
- 3. Turn on both agitators and bring the temperature of the water bath to about 1/2°C. above desired temperature in inner vessel. Maintain constant temperature of outer bath.
- 4. When the temperature in the inner beaker reaches a constant value, note the time and temperature.
- 5. Maintain temperature of inner and outer fluids to the nearest 0.1°C. for 1/2 hour.
- 5. Stop inner agitator, allow 15 seconds for any crystal fines to settle, and quickly draw a solution sample. Obtain baume value by method previously described.
- 7. Start inner agitator, and obtain a check baume value on a second sample after 15 minutes.
- 8. Obtain baume data in this manner at four other saturation temperatures. Plot a smooth curve of baume versus  $T_S$  to verify data.
- 9. Convert baume data and plot concentration versus saturation temperature on figure I.

#### DETAILED PROCEDURE

#### MEASUREMENT OF CRYSTAL ORONTH

- 1. Select and weigh a clear, well formed crystal to 0.0001 gram.
- 2. Transfer with rubber forceps to previously cleaned and dried copper basket.
- 3. Suspend basket in orystallizer tube when temperature is constant. Note time.
- 4. After growth period, remove basket and place on a blotter paper.
- 5. Immediately dip basket and crystal two or three times in 90% methanol.
- 6. Place basket on another blotter paper.
- 7. Dump srystal onto a sheet of dry filter paper and allow to dry for ten minutes.
- 8. Weigh crystel discard, or use for following run.

#### CALCULATION + orystal geometry

During the source of this work, it was noted that the erystels were not all of the same shape. Some of the crystals were elongated and others were stubby. In general, the crystals grown for this work had the same shape and were visually selected from a previously prepared quantity of crystals.

For simplicity of presentation and evaluation of data, this writer has defined the growth rate,  $R_{D,s}$  as follows:

$$R_{\rm D} = 1,120 \left[ \frac{\omega_2^{\sqrt{3}} - \omega_1^{\sqrt{3}}}{\Theta} \right]$$

where: R<sub>D</sub> = linear growth rate - microns per minute
Wg = final weight of crystal - mgm
Wl = initial weight of crystal - mgm
@ = growth time - minutes

The constant (1,120) was obtained by calculation on the basis of an observed crystal shape and the value of the crystal density from Lange's Handbook ( $\rho = 2.286$  gm/cc)

- Observed average erystal dimensions - relative
- assume two of the axis perpendicular

a:b:e:d:e: = 1:1.5:4.0:1.7:1.1

(1) Area S =  $\frac{\alpha^2}{2} + 2\alpha^2 + \frac{\alpha^2}{2} = 3\alpha^2$ 

(2) Crystal volume = 
$$5 \times b = 3a^2b = 4.5a^2$$

(3) Crystal area = 
$$2[2ab+2bc]+2(3a^2)$$
  
=  $4[1.5a^2+(1.5a)(1.1a)]+6a^2$   
=  $18.6a^2$ 

Crystal weight (mgm) =  $p \frac{mgm}{mm^3} \times V mm^3$   $W = gV = 2.286 \times 4.5 a^3$  $a = 0.460 w^{V_3}$  (1) Sphericity - The size of an irregular particle may be expressed as the dismeter of a sphere having the same surface area as the particle. (used by Hixson)

$$A = 18.6 a^{2} = \pi D^{2}$$

$$D = 2.43 a = 2.43 \quad (.460 w^{3}) = 1.120 w^{3}$$

$$H_{D} = \frac{\Delta D}{\Theta} = \left[\frac{\Delta w^{3}}{\Theta} \times 1.120\right] \frac{mm}{min}$$

$$R_{D} \frac{m}{min} = 1.120 \quad \frac{\Delta w^{3}}{\Theta}$$

(2) McCabe Method - The size of the crystal is expressed as the square root of the product of the longest and shortest dimension.

$$L = \sqrt{ac} = 2a$$

$$L = 2 (.460 \text{ w}^{1/3}) = .920 \text{ w}^{1/3} \frac{\text{mm}}{\text{min}}$$

$$R_{L} = 920 \frac{\Delta w^{1/3}}{\Theta} = \frac{\mu}{\text{min}}$$

### CALCULATION - Velocity

FLOW AREA CORRECTION - Copper Basket



Å3	01 01 (pi	r square	• inch)	flow	<b>2</b>	30 (2.54 m	~	X	•0286-15 <sup>-</sup> (0786) <sup></sup>
		Ŋ			*	2.00			
S,	arca	of vire	= 2.00/6.4	5	<b>\$</b>	31%			
	Area	Pactor	= 10031		<b>3</b> 8	•69			

#### PERTINENT AREAS

		Inside Dismeter Inches	Inside Dismeter cm	In <b>sid</b> e Arga one
1/2"	Brass	0.622	1.58	1,96
3/4*	Brass	0.824	2.09	3.43
1"	Brass	1.049	2.66	5.55
	Glass	1.875	4.77	17.90

PLOW AREA CONRECTION

,

- interference of flow by verious size orystals.

Since correction is small, assume crystal has a simple shape:



Weight Crystel	Volume cm3	X	Area (3x)(2x)
20.0 mgm	.00875	<b>.1135</b>	•08 em2
30.0	.0131	.130	.10
40.0	.0175	•143	-12
10,0	-00437	•090	•05
50.0	.0218	<b>,19</b>	• 14

For simplicity, an area crystal correction for the glass tube for h crystals = 0.33 cm<sup>2</sup> and correction for the brass tubes is assumed to be 0.07 cm<sup>2</sup>.

#### CORRECTED TUBE AREAS

Glass tube IA =  $17.90 \times .69 = 0.33 = 12.0 \text{ cm}^2$   $1/2^{\text{H}}$  Brass IA =  $1.96 \times .69 = 0.07 = 1.28$   $3/4^{\text{H}}$  Brass IA =  $3.43 \times .69 = 0.07 = 2.29$  $1^{\text{H}}$  Brass IA =  $5.55 \times .69 = 0.07 = 3.76$ 

#### VELOCITIES

 Sample calculation: At a rheostat setting of 65 the flow rate is 2000 ce per minute through the glass tube. Calculate velocity.

 $\mathcal{U} = \frac{2000}{60} \frac{\text{cm}^3}{\text{sec}} \times \frac{1}{12.0 \text{ cm}^2} = 2.78 \frac{\text{cm}}{\text{sec}}$ 

(2) Sample calculation: At a rheostat setting of 65 the flow rate is 1580 on per minute through the brass tubes. Calculate velocity in 1/2" tube.

CALCULATION - conversion of Hizson Data

OROWEL HATE - For comparative purposes

convert:

$$W_{a5} = \frac{\#mol}{hr ft^2} \longrightarrow G \frac{mqm}{min - mm^2} \longrightarrow R_b \frac{microns}{min}$$
**cale:**  

$$W_{a5} = \frac{\#mol}{hr ft^2} \times 249.7 = \frac{\#}{\#mol} \times 454000 = \frac{mgm}{\#} \times \frac{1}{60} = \frac{hr}{min} \times \frac{1}{305^2} = \frac{ft^2}{mm^2}$$

$$\frac{Maf}{Maf} \times 20.4 = G$$

From the growth rate conversion plot (Figure IA)

 $R_{\rm D} = 1470 \ {\rm G}$  , and

RD = 1470 (20-4 Was)

Rp = 30,000 Waf

Thus, to convert Hizzon's growth values to the units used in this work, multiply by a factor of 30,000.

DEGREE OF SUPERSATURATION . For comparative purposes

caler

(2) 
$$C_v = \frac{M_v}{1-M_v} \times \frac{250}{18} \times 100$$
;  $C_L = \frac{M_L}{1-M_L} \times \frac{250}{18} \times 100$ 

(3) 
$$\Delta C = 1390 \left[ \frac{y_{v}}{1-y_{v}} - \frac{y_{i}}{1-y_{i}} \right] = \frac{1390 \Delta y_{i}}{1-y_{i}+y_{i}+y_{i}}$$

(h) Assume you'n denominator to be negligible,

simplify: 
$$\Delta C = 1390 \left[ \frac{\Delta Y}{1-2 \text{ yv}} \right]$$

## PERTINENT DATA

Exp't.	Solution Concentration	Growth Temp.ºC.	Degree Supersatin	Growth Rate	Velocity	Reynolds Number	
					and a second state of the		•
FIRST S	ERIFS						
5678	45•7 45•45 45•4 44•7	27+4 27+35 27+8 27+8	1.9 1.7 1.3 0.5	3.67 2.56 3.16 1.41	3*04 ***	815 820 825 840	
SECOND	SERIES						
10 11 12 13	63.24 63.57 63.57 63.57	47 <b>•3</b> 45•2 44•1	-0.51 2.57 3.82 3.72	-9.9 7.75 16.7 22.6	3,04 ,,	930 905 905	Dissolution Reject run
14 15	63.90 63.90	42.0 45.8	6.60 2.10	46.0 12.4	11 11 11 11 11 11 11 11 11 11 11 11 11	975 940	
THIPD S	RIES			,			
16 17 18 19 20	62.25 62.58 62.91 64.23	42.9 44.0 45.3 46.5	4.50 4.23 3.31 2.75 1.53	22.8 22.8 17.8 13.8 5.4	2*8 ** **	825 825 875 850 875	Reject run
FOURTH	SERIES						
224 222 232 244 242	60.60 60.60 60.60 60.60 60.60	42.2 42.2 40.3 39.9 39.9	3.10 3.10 5.00 5.40 5.40	23.7 20.6 32.1 47.0 38.8	11.5 7.0 4.3 7.0 4.3	1500 1160 690 865 680	
FIFTH S	ERIES						
25x 26x 26x 26z 26z 27x 27x 27x 28x 28x 28x 28x 28x 28x 28x 28x 28x 28	63.90 63.90 63.90 63.90 63.90 63.90 63.90 63.90 63.90 63.90 63.55 64.56 64.56 64.56 64.55 64.55	404 4004 4004 4004 4004 4004 40	7 <sub>1</sub> 65 8 <sub>1</sub> 20 5 <sub>1</sub> 10 1 <sub>1</sub> 91 4 <sub>1</sub> 75	63.5 58.5 61.7 55.6 40.1 27.6 21.5 18.1 22.5 18.1 27.5 15.5 15.5 15.5 15.5 15.5 15.5 15.5 1	20.6 11.5 20.6 11.5 7.0 20.6 11.5 7.0 20.6 11.5 7.0 20.6 11.5 7.0	1910 1410 1900 1400 1090 2000 1480 1140 2110 1560 1210 2070 1530	

### PERTINENT DATA

Exp't. No.	Solution Concentration CB	Growth Temp*°C. T2	Degree Supersatin AC	Growth Rate Ro	Velocity	Roynolds Number	
SIXTI	SERIES			,			
30 31	63.4 63.9	46.4 45.2	0.9 2.9	4.77	2.8 2.8	870 850	Meenintinn
133 34 36	64+2 64-3 64+6	45.8 38.4 42.8	2.4 10.6 6.4	8.66 39.8 31.0	3.0 2.8 2.8	920 <sup>*</sup> 750 800	/a oo o an on on
SEVENT	<u>I SERIES</u>						
38 39 40	52.8 53.1 52.5	35+5 36+4 34+6	1.9 1.3 2.4	8.84 4.64 10.4	2.8 2.8 2.8	810 820 800	n Tenn
たた	52+5 52+8 52+5	32.2 33.5 30.1	4.6 3.8 6.4	15.1 17.0 26.9	2.8 2.8 2.8	765 775 730	an a sea an
EIGHTH	SERIES			`			
45x 45y 46x 46x 467 467 467 47x	51.8 51.8 51.8 51.8 51.8 51.8 51.8 52.37 52.37	35.5 35.5 35.5 35.5 35.5 35.5 35.5 35.5	0*9 0*9 0*9 0*9 0*9 2*72 2*72 2*72	8.30 2.8 7.07 5.06 6.87 6.35 21.3 21.0	20.6 7.0 20.6 11.5 7.0 20.6 11.5	2010 Rejected 1150 2010 1480 1150 1930 1420	î Run
472 48X 48Y 48Z 49X 49X 49Z	52.37 52.95 52.95 52.95 52.95 52.95 52.95 52.95	34.1 32.2 32.2 30.85 30.85 30.85 30.85	2.72 5.05 5.05 5.20 6.20 6.20	19.2 37.6 35.4 31.3 42.0 47.6 38.3	7.0 20.6 11.5 7.0 20.6 11.5 7.0	1100 1840 1360 1050 1800 1330 1030	

## PERTINENT DATA

Exp't. No.	Solution Concentration $C_B$	Growth Tersp.*C. T2	Degree Supersatin	Growth Rate Ro	Velocity	Reynolds Number
NINTH :	SERIES					
50A 50X 50Z 51A 51X 51X 51X 51Z 52A 52X 52Y 527	43.7 43.7 43.7 43.7 43.7 43.7 43.7 43.7	24.8 25.0 25.0 25.0 24.8 24.8 24.8 24.8 24.8 24.8 24.8 24.8	2.3 2.1 2.1 2.2 2.2 2.2 2.2 2.2 1.35 1.35 1.35	5.43 8.24 6.32 6.47 6.47 6.83 7.47 6.83 7.47 6.81 2.87 3.50	2.2 20.6 11.5 7.0 2.2 20.6 11.5 7.0 2.2 20.6 11.5 2.2 20.6 11.5	590 1820 1340 1040 590 1850 1360 1050 590 1840 1360
TENTH S	4:3•95 <u>BERTES</u>	20+V	1022	2010	7+0	7020
53A 554 555 56 57 58 59 60A 60X	80.1 80.3 77.87 78.24 78.24 78.24 78.4 78.6 78.6	57.8 58.3 58.5 55.1 55.1 53.6 55.1	1.5 1.0 -1.7 1.1 3.54 HROWTH - SAT 5.8 3.9 3.9 3.9	8.92 5.47 -13.5 9.66 22.3 URATION 39.8 24.8 60.7	2.2 2.2 2.8 2.8 2.8 2.8 2.8 2.8 2.8 2.8	712 715 Dissolution 912 880 854 690 2140
60Z	78.6 78.6	55+1 55+1	3*9 3*9	50.7 144.0	11•5 7•0	1590 1230 Rejected Run
212 35 37	60 <b>*60</b> 64*5 65*2	45.6 48.2 49.4	0.62 -14 -1.1	-6.66 -21.6	Dissolu 2.8 I 2.8 I	ition, Reject Dissolution Dissolution

NG	)†t.	Initial Weight Crystal <u>mam</u> Wi	Final Weight Crystal <u>mam</u> Wz	Cube Root Difference $\Delta(\omega^{\gamma_3})$	Growth Time <u>Minutes</u> $\Theta$	Average Growth Temp. T2	Baume of Solution Bes <sup>60</sup>	Notes
5	a b c d f	2.6 9.7 14.9 19.1 23.5 34.2	Lost 16.4 22.6 28.4 33.2 50.2	0.408 0.367 0.376 0.349 0.445	118	27.4°	25.8*	Mossy Growth on crystals
6	vg. b c d e f	6.7 13.6 19.8 30.0 14.7 21.1	8.4 15.9 23.1 34.4 17.1 24.4	0.389 avg. 0.147 0.128 0.142 0.143 0.143 0.127 0.136	60	27+35°	25.7*	
7	A b b d c f	8.4 15.9 23.1 34.4 17.1 24.4	10.9 20.4 28.6 41.4 21.3 30.0	0.137 avg. 0.186 0.217 0.209 0.210 0.196 0.208	73	27 <b>.8</b> °	25 <b>.</b> 67°	
8 8	a b c d	10.8 20.3 28.0 41.0	13.8 23.5 31.8 46.4	0.204 avg. 0.139 0.136 0.130 0.146 0.150 avg.	120	27.8-	25.4*	
9	a b c d	7.7 19.1 27.2 36.7	12.9 28.9 39.2 49.0	0.374 0.394 0.390 0.336 0.374 sys.	54	45.1°	32 <b>•3</b> °	Much mossy growth on crystals Reject run
0	2 b 0 d	9.4 18.1 22.3 25.1	3.8 8.5 11.7 12.2	-0.551 -0.586 -0.544 -0.625 -0.577	65	47 <b>•3</b> °	31.8	Dissolution

2

pit.	Initial Weight Crystal Mgm	Pinel Weight Crystel MRM	Cube Root Difference	Growth Time Minutes	Average Growth Temp.	Baume of Solution	Notes
(maining and a start of the sta	W,	W2	$\Delta(\omega^{\prime})$	θ	Τ2	Be260	
	6.0	14.5	0-1111				
้ษิ	14.4	23.5	0.130		2		
e	15.7	24.2	0,388	60	45.20	31.9°	
đ	26.3	38.5	0.405			•••	
Avg.			0.416 avg.				
2 8	7-1	2.7	0.866	• -			Slight moss
9	11.6	36+5	1.054	60	44.10	31.9°	growth on
¢	16.1	37-6	0.823				crystals
đ	33•7	66.5	0.823				
Ave.			0.892 avg.				
3 a	14.5	27.7	0.587				
ъ	23.5	42.4	0.595				
•	24.2	43-3	0.620	30	44.20	31.9°	
đ	38.5	64+0	0,620			*	
AVS+			0.606 avg.				
1 A	6.1	25.2	1.104				Slight mossy
b	10.8	27.8	0.818	***	*		Growth on
¢	15.3	32.9	0.719	20	42.00	32.00	orystals
đ	16.8	32.7	0.637			·	
AVE.			0.820				
f 🐥 🗌	7.2	11.8	0+347				
D	14.0%	21.0	0.337	20	1.2 00		
8	20.0	20 eu	0, 309	50	45.0*	36+11	
Avs.			0.331 avg.				
: 8	15.8	29.4	0.577				
ъ	19.5	35.Ó	0.578				
G	23.8	42.4	0.611	29	42.40	31.5°	
Ave.			0.589 avg.				
	11-1	22.2	0.570				
8	15.5	30.0	0.612				
é	26.3	ú3.9	0.631	30	42.90	31.64	
1			A. LAT man	<b>.</b>	and a second second	And the second s	
r 48+			VOU/ EVE				

xp No	! t.	Initial Weight Crystal Mgm	Pinal Weight Crystal mgm	Cube Root Difference	Growth Time Minutes	Average Growth Temp.	Baume of Solution	Notes
		W,	W2	$\Delta(w^3)$	0	T2	Bez	
8	a 5 6	10.0 14.5 19.9	22.5 34.4 40.0	0.626 0.812 0.712	45	山, <b>0</b> °	31.7°	
A	<b>V</b> 6•			0.717 AVE.				
9 A	a d c	9 <b>•3</b> 18•3 26•2	19 <b>*1</b> 33*1 42*2	0.572 0.574 0.514 0.514	45	45 <b>. 3°</b>	32.0	
0	4 b 0	12.0 19.3 25.4	17.8 27.0 36.9	0,322 0,314 0,390	60	46 <b>+5</b> °	32,1°	
A	vg.			0.342 avg.				
1	X,	23.7	Lost	×				Crystal fell
<b>n</b> .	Y	28.4	Lost	*	30	45.60	31.00	H MITA DEBYA
e c	7 a. Z	29+3	13,8	-0, 683				Dissolution Reject Run
2	X	21.5	Lost	*				
	Y	29+9	52.1	0.632	30	42.20	31.00	
	Z	19.2	33.7	0,550		ι		
3	x	33+7	Lost	x				
	Y	15.5	Lost	x	20	40.3"	31.00	
	Z	14.9	27.9	0.570				
ŧ	x	15.5	Lost					
	Y	18.3	41.8	0.836	20	39.9*	31.00	
	Ż	20.0	39+4	0,689				

Car No	1 \$.	Initial Weight Crystal <u>Mam</u> ری,	Final Weight Crystal <u>mgm</u> W2	Cube Root <u>pifference</u> $\bigtriangleup(\omega^{1/3})$	Growth Time Minutes O	Average Growth Temp. Ta	Beams of Solution $B < 2^{\circ}$	Notes
25	X	20+6	58.0	1.130				
	X	16.4	45.8	1.038	20	40.90	32.00	
	Z	20,6	Lost	x				
26	x	13.9	43.0	1.099				
	Y	19.1	49.1	0.988	20	40.4°	32.04	
	2	28.9	56.0	0*758				
27	x	13.5	30.0	0.725				
	Y	15.1	27.2	0.535	20	43 <b>•3°</b>	32.00	
	7.	14+4	25.0	0*490				
28	x	15.1	23.1	0.376				
	X	16.2	25.2	0.401	20	46.50	32.20	
	Z	21.2	29.5	0.320				
9	x	16.0	36+7	0.803				
	Y	22.0	41.7	0.667	20	45.00	32.50	
	Z	21.7	39.2	0.609				
0	a b 0	14.8 21.7 32.2	16•7 23•4 34•8	0.101 0.070 0.085	20	46 <b>.</b> 4°	31.85*	
Å	¥g∗			0.085 avg.				
1	8 D C	16.7 23.4 34.8	21.2 28.2 42.2	0.212 0.184 0.220	20	45 <b>.2</b> °	32 <b>. 0</b> °	
A	vg.	-		0.205 avg.				

xp't. No.	Initial Weight Crystal mgm	Finel Weight Crystel	Cube Root Difference	Growth Time <u>Minutes</u>	Average Growth Temps	Beime of Solution	Notes
	5	W2	$\Delta(\omega^{\frac{1}{3}})$	Ð	Tz	Be260	Malika wasay dipanti sana ang kang kang sana ang kang kang sana ang kang kang sana sana sana sana sana sana sa
2 a td.b a.c Avg.	21.2 28.2 42.2	19.1 27.2 41.8	-0.094 -0.035 -0.009 -0.0h6 evs.	20	47 <b>•</b> 4°	32.0°	Dissolution Poor Growth Checks
3 a b o Avg.	19.1 27.2 41.8	23.3 31.3 47.1	0.182 0.142 0.139 0.154 evg.	20	45.80	32 <b>.</b> 1°	Velocity slightly higher than rest of series. By error.
∔ a b c Avg.	23.3 31.3 47.1	44.54.75	0.676 0.629 0.608 0.638 avg.	18	38 <b>.</b> 4°	32.1*	Slight moss on crystals- time cut short due to "breaking" of soln - High supersaturation
5 a td.b 1. c	18.6 19.5 22.8	15.7 17.5 20.0	-0.144 -0.093 -0.121 -0.119 avg.	20	48.20	32+2*	Dissolution
b b c	15.7 17.5 20.0	28.2 32.5 34.2	0.540 0.592 0.532	20	42.8*	32.2	
itd.	20+8 40+3	16+6 34+2	-0.199 -0.185 -0.192 avg.	10	49*4°	32.4*	Dissolution
8 6	10.0 16.3 24.4	13.6 21.1 31.1	0.233 0.229 0.215	30	35.5	28 <b>.</b> 45°	
Avg.	13.6 21.1 31.1	15.4 24.3 35.4	0.101 0.133 0.138 0.12h ave-	30	36 <b>.</b> 4°	28 <b>.</b> 55°	

Bxj	)*t.	Initial Weight Crystal 	Final Weight Crystal <u>Mga</u>	Cube Root Difference	Growth Time <u>Minutes</u>	Average Growth Texp.	Serve of Solution	Notes
-		رنئ	Wz	$\Delta(w^{k})$	θ	Tz	8260	
40	e D	15.4 24.3 35.4	19.4 28.9 41.5	0.199 0.170 0.182	20	34.6°	28.35*	
Av	<b>6</b> +			0.184 avg.	b i			
41 td. n)	a b ¢	19•4 28•9 41•5	19.4 29.0 41.3	Ro Growth	20	37.2°	28 <b>.</b> 45°	Result checks solubility data
42	a b c	19.4 29.0 41.3	26.0 36.8 51.9	0.276 0.255 0.272	20	32 <b>.2</b> *	23 <b>.35</b> *	
Av.	8*			0.268 avg.	•		•	
43	a b c	7.7 12.7 21.6	Lost 17.8 30.2	x 0,277 0,328	20	33•5°	28 <b>•45</b> •	
Av	8+	<b>2</b>	, ,	0.303 avg.	•			
44	8 D 6	17.8 30.2 36.8	30+3 46+2 54+0	0+506 0+475 0+454	20	30.1°	28 • 35°	
AV.	g•		,	0.478 avg.	•			
45	X	17.6	22.5	0.222				
	Y	16.9	18.4	0.074=	30	35.50	28 <b>.1</b> °	Reject 45Y
	Z	14.3	17.9	0,189				TOM LEBUTC
16	x	22.5	29.6	0.270				*Lon
	Y	18.4	27.2	0.367	60	35.5	28.1*	
	z	17.9	25.8	0,339				

Exp	*t.	Initial Weight Crystal	Pinal Weight Crystal	Cube Root Difference	Growth Time Minutes	Average Growth Temps	Saume of Solution	Notes
		121	12	$\Delta(W^{\prime}3)$	Θ	Tz	Be260	
47	X	23.0	39.8	0.570				
	Y	22.2	38+3	0.560	30	34 <b>•1°</b>	28 <b>.3°</b>	
	Z	27.6	43.4	0.512				
48	x	23.8	44.6	0+670				
	Y	32+5	55.8	0.630	20	32.20	28.5	
	2	20.4	35.6	0 <b>•558</b>				
49	X	19.1	41.4	0.786				
	Y	18.2	43.6	0.8904	21	<b>30.</b> 85°	28.5	*Figh
	Z	22.4	44.2	0.717				
50	8. D C	14.2 20.4 21.6	19.7 28.1 29.1	0.279 0.308 0.282		214+8+		U= 2.2 00
<b>A</b> V	'S*			0.290 avg	* >60	)	25.0	
	X	15.1	24.7	0-1110	( -	)		U= 20.6
	Y	13.5	20.1	0.338		25.00		U= 11.5
	Z	17.9	26.0	0.346	)			U= 7.0
51 A	8 D 0	19.7 28.1 29.1	26.5 35.9 38.1	0+280 0+259 0+289		-		
A۹	1 <b>8</b> +			0.276 ave	5 60	24.60	25.0	
	X	24.7	35.2	0.365			•	
	Y	20.1	30.3	0.399	)			
	2	26.0	36.8	0 <b>. 36</b> 4	/			

Ex]	oft.	Initial Weight Crystal Mgm	Final Weight Crystal	Cube Root Difference	Growth Time Minutes	Average Growth Temp.	Baume of Solution	Notes
	a in the state	Wi	Wr	$\Delta(w^{k_3})$	θ	Tz	Be260	-
52 A	8 D G	26.5 35.9 38.1	29.6 40.3 42.4	0.112 0.129 0.122				
A	″g•			0,121 avg	* (	01 <b>04</b>	A7 33	
	X	35.2	42.3	0+207	200	≪0 <b>.</b> ,V*	23+1-	
	Y	30-3	36*1	0.187				
	Z	36.8	42+7	0.169	)			
53 ▲	a. b	16.3 46.0	19*8 51*9	0+170 0+147	20	57.80	36 <b>*</b> 7°	
A٦	18•			0 <b>.159 a</b> vg	•			
54 A	8 b	19.8 36.2	22.0 39.5	0.097	20	58 <b>.</b> 3°	36+75°	
AV	8+			0.0975 avg	*			
55 A Av	8 b /8+	22.0 39.5	Lost 31.7	# -0,211 -0,211 avg	20	58 <b>•5</b> °	36+1*	Dissolution
ln)	a.	ø						
56 4 u	<b>b</b>	19*5 24*0	23.5 28.5	0.172 0.171 0.1715 av	20	56 <b>.</b> 8*	36.2*	
0.1 12 12	64	33 C	a). L	0 200	5*			
21 A4	a D Re	28,5	41.2	0.399 0.399 0.397 ave	20	55 <b>.</b> 1°	36.2	
ER	€2 <b>₽</b>	34.4	21. 1.		-			No month
<u>کر</u>	b 'g•	41.2	41.6	õ	15	57•4°	36.15	solubility Baume check.
59	8 D	34•4 41•6	62 73	0.706 0.714	20	5 <b>3.6</b> °	<b>36</b> +25°	
A۷	8+			0.710 avg	*			

)†\$* 3*	Initial Weight Crystal <u>mgm</u> Wi	Pinal Weight Crystal <u>men</u> Wz	Cube Root <u>Difference</u> $\Delta(w'3)$	Growth Time <u>Minutes</u>	Average Growth Temp. Tz	$\frac{Baums}{of}$ <u>Solution</u> $\frac{Be_2^{40}}{Be_2^{40}}$	Notes
а Б .76+	17.2 30.3	27 <b>.</b> 2 45 <b>.</b> 7	0.426 0.457 0.442 avg	- 20	55 <b>•1°</b>	36*3°	
X	19.8	54.3	1.082	(			
Y	17.4	42.7	0.904				
2	Щ.6	33.6	0.783	ノ			

## CALCULATED DATA

	Run	Solution Saturation Temp. C.	Diameter Tube on	Solution Velocity <u>cm/sec.</u>	Solution Density 	Solution Viscosity 	Roac	[Ro] ~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	[RD] u=1
	******	Ts	D		5	<u>~</u>			Anticulture and interaction in the state
1	5678	29.6 29.2 29.2 28.1	4 <b>.</b> 77	3 04 #	1,23 "	2.19 2.18 2.16 2.12	1.93 1.50 2.44 2.82	2.80 1.96 2.41	1.47 1.15 1.85
2	12 13 14 15	47.2 47.2 47.4 47.4	4*77 "	3.04 "	1,29 ""	2.06 2.06 2.13 1.99	4.38 6.08 6.98 5.90	12.0 16.3 33.1 8.9	3.14 4.38 5.01 4.23
3	16 17 18 19	46-2 46-4 44-7 47+4	4.77 "	2,80 "	1.29 1.29 1.28 1.29	2+08 2+08 1+97 2+03	5.07 5.39 5.37 5.02	16.8 16.8 13.1 10.2	3•74 3•97 3•96 3•71
4	224 222 232 244 247 242	141 • 8 141 • 8 141 • 8 141 • 8	2.09 2.66 2.66 2.09 2.66	11.5 7.0 4.3 7.0 4.3	1,28 # # #	2.06 2.06 2.13 2.16 2.16	7.65 6.65 6.41 8.70 7.20	11.6 11.6 20.8 26.6 25.2	3•74 3•74 4•15 4•92 4•67
5	25x 26x 26x 26z 27x 27z 28x 28x 28x 28x 29x 29z	47.4 47.4 47.4 47.4 47.9 48.6	1.58 2.09 1.58 2.09 2.66 1.58 2.66 1.58 2.66 1.58 2.66 1.58 2.66 1.58 2.66	20.6 11.5 20.6 11.5 7.0 20.6 11.5 7.0 20.6 11.5 7.0 20.6 11.5 7.0		2.20 2.21 2.21 2.21 2.10 2.10 2.10 2.10	8.3 7.52 6.8 5.9 5.42 5.42 11.1 11.8 9.42 9.5 7.9 7.18	27.4 28.6 26.6 27.2 24.0 17.6 14.7 15.5 9.1 11.0 10.1 19.4 18.3 19.2	3.7442 3.7442 3.9358 3.9358 4.8847 7.7288 5.4 3.4 5.4 5.4 5.4 5.4 5.4 5.4 5.4 5.4 5.4 5
6	30 31 33 34 36	47.0 47.4 47.6 47.6 47.9	4 <sub>8</sub> 77	2+8 2*8 3*0 2*8 2*8	1.29 # # #	1.97 2.03 2.00 2.30 2.14	5.3 4.0 3.61 3.76 4.85	3.50 8.45 6.27 29.2 22.8	3.90 2.91 2.61 2.75 3.56
7	38 39 44 44	37.4 37.8 37.2 37.2 37.4 37.4	4, 77 n n n	2,8 ** ** **	1,26 " " "	2.08 2.05 2.10 2.20 2.17 2.30	4.65 3.57 4.34 3.28 4.47 4.20	6.69 3.51 7.90 11.4 12.9 20.4	3.52 2.70 3.29 2.48 3.40 3.19

<b>Pium</b>	Solution Seturation Temp. <sup>o</sup> C.	Diameter Tube	Solution Velocity 	Solution Density	Solution Viscosity 	Ro AC	[Ro] (H=)	[R] N=1
	Tsi	P.	W.	<u>P</u>	<u>بر</u>		and the second s	
453	36 <b>.</b> 4	1.58	20.6	1.26	2.04	9.22	3.70	4.11
451	11	2.66	2-0	1.26	2.04	7.86	4.18	1.65
16x	36-4	1.58	20.6		2.01	5.6	44444	4
LGY	*	2.09	11.5	*	2.01	7.6	3.58	3-98
16Z	<b>11</b>	2.66	7.6	11	2.04	7.1	3.76	6.17
17X	37.0	1.58	20.6	<b>#</b>	2.13	7.83	9.5	3.50
477	<b>#</b>	2.09	11.5	11	2,13	7.70	10.9	4.01
472	**	2.66	7.0	教	2.13	7.05	11.4	4.19
48x	37.6	1.58	20.6	*	2.23	7.45	16.8	3.33
48Y	*	2.09	11.5	若	2.23	7.00	18.4	3.64
4.8z	<b>1</b>	2.66	7.0	<b>1</b>	2.23	6.20	18.5	3.66
498	37 <u>e</u> 6	1.58	20.6	Ħ	2.28	6.78	18.7	3.02
49 <b>Y</b>	¥1	2.09	11.5	<b>R</b>	2,28	7.68	24.8	4.00
492	**	2.05	7.0	-	2,28	6,18	22.7	3.66
50A	27.3	4.77	2.2	1.23	2,20	2.36	4.45	1.93
X	<b>R</b>	1.58	20.6	<b>1</b>	*	3.92	3.96	1.88
Y		2.09	11.5	Ħ	B	3.01	3.51	1.67
Z	<b>T</b>	2.66	7.0	77	<i>n</i>	3.08	4.01	1.91
51A	27:3	4.77	2.2	F3	2.17	2.34	4-23	1.92
X	97 44	1.58	20.6		74	3.11	3.20	1.48
X	*	2.09	11+5	20 20	** _	3.40	4+12	1.04
6	an L	200 L. 197	(*0	*	5 10	5410	4.62	1. YC
)CA	∠(•0 n	4+//	202	tt .	<*T0	4.01	1.05	+*21
∧ ₩	# .	2.00	2V+0 11 C	n	**	2.00	1 01	1430
1	· · · · · · · · · · · · · · · · · · ·	2.66	***7 7.0	**	ŧţ	5.27	1.94	1.44
<b>دی</b>	*	6.00	\$ • V			c • 34	1070	**42
534	58.8	4.77	2.2	1.33	1.96	5.95	6.50	4+33
54A	59.0	4.77	2.2	₩ 1	1.95	5.47	3.98	3.98
56	57.6	4.77	2.8	**	1.95	8.78	6.37	5.79
57	57.6	4.77	2.8	ti T	2,02	6.30	14.7	4.15
59	57-7	4.77	2.8	<b>7</b>	2.08	6.87	26.2	4.52
60A	57 <u>*</u> 8	4.77	2.2	ñ	2.02	6.36	18.05	4.63
60X	<b>罪</b>	1.58	20.6	蒹	<b>P</b>	15.5	17.75	4-55
60Y	47 #*	2.09	11.5	17 17	Ħ	13.0	18.8	4.82
60Z	ক	2.66	7.0	17	Ħ	11.3	20.0	5.13

	Saturation Temp. °C.	Growth Rate R <sub>D</sub> = //min	Supersetin $\Delta C = \frac{Sm}{100 \text{ gm}F}$	Veloáity N= cm/sec	$\left(\frac{R_{D}}{\Delta C}\right)$	$\left[ \begin{array}{c} \mathcal{R}_{0} \\ \mathcal{U}^{m} \end{array} \right]$
12745	19.5* "	4+05 3-84 4+80 *74 *77	3+54 2+86 2+40 0-70 0-70	2.39 3.17 6.0 33.6 33.6	1.15 1.34 2.00 1.06 1.10	
678901123456	41,*5° ** ** ** ** **	7.62 6.57 2.94 1.82 .94 2.22 1.50 3.30 2.72 4.89 2.93	2.32 1.78 1.61 .96 .65 1.30 .66 1.29 .625 2.49 .87	31.7 16.8 1.7 2.8 4.24 2.56 7.0 11.0 39.4 17.8 28.6	3.28 3.69 1.83 1.45 1.45 1.71 2.28 2.56 4.35 3.28 3.37	2.95 3.00 2.40 1.35 .61 1.62 .86 1.75 1.00 2.22 1.17
17 18 19 20 21 22 23 24	53.44° # # # #	7.05 4.86 9.81 3.30 8.91 14.79 12.0 5.37	1*93 1*11 3*87 *78 1*29 3*24 1*46 *69	4.24 7.62 2.45 11.0 31.0 9.75 18.0 102.0	3.65 3.44 2.54 4.23 6.90 4.57 8.21 7.77	4.4 2.45 7.2 1.48 2.8 6.9 3.4 1.10
2222223333345678	711° # # # # # # # # # #	18.66 49.26 27.24 24.09 12.81 17.76 14.61 7.65 12.54 4.20 9.00 8.10 6.09 6.60	1.13 2.63 1.58 1.90 1.09 1.59 2.35 .90 1.63 .82 2.84 2.57 1.11 1.85	112.0 56.0 95.0 61.0 110.0 44.2 17.6 36.6 20.8 11.7 6.8 7.5 7.05 9.02	16.5 18.7 17.2 12.7 12.3 11.2 6.22 8.50 7.70 5.12 3.17 3.15 5.49 3.57	1.01 4.07 1.61 1.88 .69 1.71 2.44 .82 1.91 2.73 2.32 1.85 1.69

## SUMMARY OF HIXSON DATA - (UNITS CONV RTED AND CALCULATED)

## SUMMARY OF MCCABE'S DATA (AC = 0.9)

Reciprocating Cage Experiments

RD=1.22 RL

Runs	Velocity cm/sec.	Growth Rate RL= Wmin	Growth Ro=Wmin	Rate Ro/be
180-183	*9	1.21	1.48	1.64
177-9	1.8	1.36	1.66	1.84
184-7	2.6	1.42	1.73	1.92
158-61	3•3	1.62	1.98	2.20
171-3	6.9	1.47	1.79	1.99
174-6	13.9	1.55	1.89	2.10

## Stationary Cage Experiments

Runs	Velocity on/see.	Growth Rate $R_{\perp} = M/min$ .	Growth   Ro	Roto Ro/ac
188-91	<b>e</b> 2	1.16	1.41	1.57
208-11	.6	1.41	1.72	1.91
192-5	1.0	1.53	1.87	2,08
211-15	2.4	1.61	1.96	2.18
196-9	1.9	1.71	2.08	2.31
216-19	2.3	1.80	2,20	2.44
200=3	2.7	1,92	2.34	2.60
<b>220-22</b> 2	2.7	1.85	2.26	2.51
204-7	3+6	1.92	2.34	2.60



FIGURE B







121. . . . <u>44</u> 臣 그그 17: ÷ ĩ.ĩ. ++-(2)ili 111) 171 村村 コン SATURATION TEMPERATURE °C

	.T		· · · · · ·	<sup>-</sup>						H.F.	, <u>1</u>			· · · · · · · · · · · · · · · · · · ·		.  -					1.1	:	1	 	11	Ī	+ - +   + - †	1 - 1	
	1 :	,	-			ļ			· - ·	LC:				+-  +		ļ.		+ 	1.11	:	F	Gi	IRE		T	-			- 1-4
					-  : -		1.	· _ 3					<u>:</u>	1	ΞF	· .	:.;,	- - 	11:	* <u>-</u> :			·		••••••	+		: -  :	1.5
-	- <del>  .</del> .			7			<u>;</u> ;;;		1		1.2	1.4-		· .		ļ. ·.		- L - L 1		· ·	;-; ;	 	-					; ;	
	1		000						  -	: .	i -	11-1					1	9	ļ-	<u> </u>	ļ	.  .	<u> </u>		1	<u> </u>		·]	1.17
		· · · · ·	+	<b> </b>	+			 	;  ;			-	+				1				<u> </u>		1		<u> </u>	<u> </u>			
-	<del>     </del>	- I		[				<u> </u>							<u>  -, -</u>   -, -	1	<u></u>	· · · ·	i i L		+				:  - †	<u></u>		+ +	
	+	+		. ·	-	<u> </u>										1										-+-			
	 		\$00		- + -	<u> </u>	+	<u>.</u>							1				<u>· · ·</u>	1 			, -		. 1 .				
	1.7 <u>1</u> 1:			<u> </u>							 				<u> </u>			1 <u>.</u>		<u>{</u>				:	<u>+ · ·</u>			+++++++++++++++++++++++++++++++++++++++	
	†:			<b>.</b>					1 ± - '				- 4	1					X	<u> </u>				- <u>-</u> ;	<u> .'</u>		<u>p.</u>		
			+-+			ļ ļ	1 . 				: 		S/			<u> </u>			Y	1 [ 	1	· · ·				. ·			
	1		106	, <u>,</u> 10				: <u>-</u>		<u> </u>	+- +- + ++ - ++	107	<u> </u>		1		·	1	<u>; ; ; ;</u>		1.	1. 1	{		<u>.</u>			E	
,	Ë					:*::= 	+- : 	÷		+ +++	-	1					7	z, -	-' _ † 	i	}++		· ·						
	11.2			1			[; ; <u>;</u>	1-	-		Ę	5	1	: . : .			1	Ē		,	ir.;	+	· · ·			  ,-	;	=::	↓ ↓
	102					.  +1	ļ‡ Ţ		<u>.</u>	· · ·	1				• † † † , , † † †	17	1		1. I. 1.	:	+	, î ;			111 111	11			
						· · · ·		1 + - +	• •	j.				.T	5		<u>/</u>			-1	; ; ; ;	_ <u>t</u> _	; <u>1</u> -:		·++	·			11.
	â	1	icu		.:				- 6	5		-		-10	1	Z	· · · · ·		- •				1		╞╌┯┯┿			· · · ·	
	ţ,	7	+	+	• • • •	1:	***	   ;	1	 	ᇿ	+ +	·	57	1	4	- !	• •				• •	, È ; •	1-1			 	1	
		<u>.</u>		. <u>.</u>	111	 	1.11			+-'.			R	/	14			+				····		T.					
									<u></u>				f	1		 	·	L + L - L L	+ +	1.71. . • . •						· · · · · · · · · · · · · · · · · · ·	+++++ ++++-	'-	
		+ 1	00	4 1 4	1 • 1 • 1	+1+				1 1		×		/₹		+++							• • • •	11-1					
 t				 		-112   + - <u>-</u> -		· · ·	,			1		2				[	2	<u>A</u> T		<b>C1</b> .7	NNT.			~0			
· · · · ·	- <b></b>					· · · · · · · · · · · · · · · · · · ·		:		1;,,,; 1,,;,	T f	٥.,	5			1-1-1		<u>-</u>		CH			EN T	10	N	<b>· + + ·</b>		† <u>†</u>	
-1	-7	11;;;; 1,:;;	iFi	[++  -  -		'1': 744+		; 4 ;	- <u>-</u> ["† -		Ζi	X			15T			- 1											
			990					'; ;  !+-	1	Z		2	-+ +	****** 		; + :. 		F.	-1 ; -; -; 	<u> </u> +						172		-	11
	<u>t</u>	117		, ·		1		<u>, i</u> , i	·::'		4	ti i.				· · · · · · · ·	Ţ		<u>i</u> ti i			u.11		, i i i	<u>.</u>				1,11
+ ; + ; - ; . ;	.   .	· · ·	1	•	.) . t t t	.,	111	11.54	$\mathcal{I}$	$\angle$	47	-+ +					t∔:,		H.,	1	†'†]	- , i			į1. į				
			-   ' - '		+				ίH-	3	1, j. j.	1;-	- : - ::	1 <sup>+</sup> +;		++ '+ + +		1	- 14	;-+- ; _;		ī †., .+				12." 		田片	ł
	r+++	5	LITE TAR	- 1 - 1	+			<b>A</b> E		1 - 1 1 1 1 1 1 1				- 	141 141	· · · · · · · · · · · · · · · · · · ·				. : I				11.		++-+			
		<u>1</u>	11 1 4 51		-	+- ‡	- 1	1	-++1		 →+	;		· .	t+i‡	Τ.		+L :		;;; <u></u>					ļ† ]				1
	. ;;	:	, , ,					<b>Z</b> ==	F' ; 1		• • •		+++++++++++++++++++++++++++++++++++++++	::::	- <u>+</u> i ;	t :t						+++++++++++++++++++++++++++++++++++++++		:::;			詽甘		:+-
			1		1-	: : :			ri 14			+! +										1		· · · · · · · · · · · · · · · · · · ·					
	, , ,	· · · · ·				:					<u> </u> 		ΗĘ			· <u>·</u> · <u>·</u> · <u>·</u>			н ЦН					++++ + +++ +++++++++++++++++++++++					‡ +[
	1 m		<b>,00</b>				4	<u>0</u>		+ - + - + - + - + - + - + - + - +	1	<u>c</u>			<u>ا</u> اکر آر			±1 -=    -   -	±++ 	$\overline{0}$	11: 11:11			1			+++=	· · · ·	+ +
				-51	· · '				+++++ +-++++++++++++++++++++++++++++++	R	нг	0				F1	·	NZA	;;;;;1		*****			. <u></u> 	+++++++++++++++++++++++++++++++++++++++		<u>}</u>	<u>I</u>	 
	111 111		+ - • -+ - •			: 	Т <u>Г</u>							7 <u>77</u> 7		•••.• 			. :: '  	··		+ + + + + + + + + + + + + + + + + + + +	!⊥  !1_1		1.1		<u>.</u>		<u>1, †</u>
	· + ' · + · · ·			+ + i   -+ - i   -i		+1 -1 -1 -1		+, ,						+++-' 		• • •	+	L							+'	+ <u>+</u> ;T  ====	<u>. † , 1</u> - <u>1 - 1</u>		+1+
	-i-i-i-i-i-i-i-i-i-i-i-i-i-i-i-i-i-i-i	L., 			<u></u>			1, .1 F				,	111			· · · · · · · · · · · · · · · · · · ·			121						빏	•];-;-]	╪╪ <sub>╞</sub> ┇ <mark>╷</mark>	.T_+ + + + + + + + + + + + + + + + + + +	, 1 ' <del>, 1 '</del>
	117	{- <u>-</u> -	11 1 1 1	1. N. S. M. M.	1 1 4 8	I		1 1 1 1 1				1	A 4-1 1.	1				1	1	با بد بسند	1.1.1.1	1						· · · · ·	1
									+-  , +-  ,	,   	<u>}</u>							+ +-  	· ] []		нĒ								• L. • <del>-</del> - <del>-</del> - <del>-</del> - <del>-</del> - <del>-</del> - <del>-</del>
							+ + ' + + - + - + + - + + - +		+							· · ·	i= , , , , , , , , , , , , , , , , , , ,										11 ", 1 - 15,	1	
						+ + + + + + + + + + + + + + + + + + +																							

١

10 X 10 THE 12 INCH 359-11L

1

.

FIGURE IIA



FIGURE 28





![](_page_53_Figure_0.jpeg)

FIGURE Y

![](_page_54_Figure_1.jpeg)

FIGURE YI

![](_page_55_Figure_1.jpeg)

r

FIGURE VI

![](_page_56_Figure_1.jpeg)

U Sec

LIGURE VIII

![](_page_57_Figure_1.jpeg)

### FIGURE IX

![](_page_58_Figure_1.jpeg)

![](_page_59_Figure_0.jpeg)

![](_page_60_Figure_0.jpeg)

#### DISCUSSION - EXPERIMENTAL METHOD

Several weeks work were required to become familiar with the apparatus. Difficulties encountered and problems to be worked out were as follows:

- 1. Obtaining close control of cooling water temperature.
- 2. Obtaining close control of heater input.
- 3. Handling of crystals and sampling from a fluidised bed.
- 4. Avoidance of nucleii formation and freeze-up of the apparatus.
- 5. Find a sufficiently accurate method for measurement of solution concentration.
- 6. Obtain accurate data on solubility of copper sulphate.
- 7. Use of the rheostat for varying the solution velocity gave only a narrow range of velocities.
- 8. Obtaining a wide range of  $\triangle 0$ .
- 9. Measurement of crystal growth.

For the first fifteen runs, difficulty was encountered in keeping the cooling water constant  $(\pm 1/2^{\circ}C_{*})_{*}$ . This was remedied by using a large bucket as a reservoir. Good temperature control was obtained by adding a quantity of cold water about every ten minutes.

To obtain better heat control, the electric heater was graduated with ten divisions. This enabled the writer to reach and duplicate desired operating conditions in a short amount of time.

Because of the multiplicity of variables in crystal growth fluid bads and due to experimental difficulties, the writer decided to concentrate on single crystals rather than a large quantity of crystals. Although the apparatus was designed by a local equipment company for fluid-bed crystal experiments, the writer found it adaptable for single crystal work. This simplified the operation of the apparatus and enabled the writer to collect considerable data in a relatively short amount of time. Single crystals could be grown under steady state conditions, for several hours if necessary. With only 3 or 4 crystals in the system, nucleation was inhibited. For the same reason, no filter or porous plate was needed.

Any nucleii formed in the sub-cooled portion of the apparatus were swept into the dissolver, wherein they dissolved under controlled unsaturation conditions. It was found that a retention time of two minutes, moderate agitation, and a solution kept one or two degrees above the saturation point would rapidly redissolve the invisible nucleii formed during the course of a run.

Solution concentration was measured by a standardized hydrometer. Feriodic readings throughout a run checked consistently to the nearest 0.1° Be.

Using the solubility data from the International Critical Tables (stated to be only accurate to ± 2%) the writer found that dissolution or shrinkage of the crystals occurred under supposedly supersaturated conditions. Solubility data from Seidell "Solubilities of Inorganic Compounds" when plotted, gave a curve which did not coincide with ICT. The writer then decided to obtain solubility data using the apparatus in figure #%.

The data obtained was found to lie on a smooth curve. The validity of the curve was then checked by placing crystals under saturation conditions in the crystallizer for a length of time (1 % 30 minutes). No change in weight resulted.

Variation of the speed of the recycle solution pump (220 volts D.C.) permitted a limited range of solution velocities (see Fig. II). In addition, the pump would stall at low speeds. To obtain a velocity spread, the writer hooked up several tubes in series. This had the additional advantage in that several orystals could be grown simultaneously without a source of AC error, since the temperature drop across the series of tubes was found to be negligible when the system was in equilibrium.

The writer feels that Hixson's range of AC was limited because of the presence of a bed of crystals and a filter in his apparatus. A filter capable of removing microscopic crystal nucleii would have a very large pressure drop. Function of the dissolver has been previously described.

The writer felt that the simplest and most rapid way to measure crystal growth was with the use of an analytical balance. Linear growth could most easily be expressed as the difference between the cube roots of the final and initial weights ( $W_2^{\nu_3} - W_1^{\nu_3}$ ). This form of expression cannot be visualized, however, nor compared with the work of others.

The writer chose McCabe's units because they were simple. In order to compare with Hixson, the writer converted growth units first to  $\frac{W_2-W_1}{A\Theta} = G$  and then to  $R_D$ .

#### DISCUSSION - GENERAL

According to the International Critical Tables, the presence of a "beta" form of copper sulphate occurs at about 60°C. This temperature is above the range (27°-58°C) studied in this work. The data of Hixson-Knox show a wider scatter above this temperature (see Figure VII).

Growth rates obtained agree with that of McCabe's cage experiments, but are about twice as high as Hixson's. This may be due partly to a difference in assumed crystal geometry, and also to an edge-effect. Hixson used crystals about one half inch in size as compared with one-eighth inch used by the writer. The quantitative effects of solution velocity were found to agree with both McCabe's and Hixson's findings.

This writer is unable to agree with Hixson's complex correlation for several reasons:

- 1. Growth rate was found to be independent of particle size - this would not be true in a fluidized bed of crystals where settling velocity comes into play. In any case, this writer feels that the D term in B<sub>2</sub> should be the tube diameter. A modified Ro would be needed to correlate fluid=bed studies - rather than modify the D term, this writer would attempt to modify the D term, this writer would attempt to modify the D term, this writer would attempt to modify the D term, this writer would attempt some relation involving Stokes Law, settling velocity etc.
- 2. A plot of growth rate vs. Reynolds number cannot give parallel curves on legelog paper because the effect of velocity varies with solution concentration (or temperature).
- 3. Diffusivity data is questionable.
- 4. Hixson assumed the viscosity to be constant regardless of the effect of sub-cooling for a given saturation temperature. Application of the log µ vs log Absolute temperature rule for obtaining viscosities, indicates a 10% increase in the viscosity value for five degrees of sub cooling.

Factors to be considered for future work on the study of crystal growth should include:

- Correlation with activities or degree of ionisation - compare with use of concentration values.
- 2. The significance of a "Critical" crystal size above which perfect crystals cannot or are difficult to grow.
- 3. The effect and mechanism of pH on growth.

The writer feels that discrepancies and the scatter of data in crystal growth work are not due to the errors involved in measurement, but due to the crystal itself. The cause may lie in a film of dehydrated material or dust on the crystal service, the presence of imperfections on the surface, etc.

A possible means of overcoming this is by preparing the crystal - perhaps a short submersion in slightly undersaturation solution. The time of growth may be a factor. A time-growth curve would clarify this.

The data from this work, though greater in quantity, is probably inferior to Hixsons from the standpoint of scatter, particularly in the early runs.

Data on the low concentration ( $T_S = 27^\circ$ ) runs is insufficient to confirm the linear effect of  $\Delta C$ , or to disprove McCabe's equation (using an agitator, tank, large quantity of seed)

$$R_L = f (\Delta C 1.8)$$

## NOMENCLATURE

C <sub>B</sub>		solution concentration gm CuSO <sub>L</sub> .5H20 per 100 gm. free water
W	12	weight crystal - mgm
V	*	volume orystal - mm <sup>3</sup>
A	糯	area crystal - mm <sup>2</sup>
θ	<b>4</b> 2	time - minutes
R <sub>D</sub>	縱	$\frac{\Delta D}{\Theta} = \frac{R_{\rm L}}{R_{\rm L}} = \frac{\Delta L}{\Theta}$
D	**	diameter of sphere having same area as crystal - p
L	*	square root of long x short sides of crystal - M
T2	*	crystal growth temperature °C
Ts	*	saturation temp. of solution "C.
T	*	absolute temperature "K.

W = velocity cm./sec.

#### BIBLIOGRAPHY

### Reference

(1)	"Unit Operation Reviews", Ind. Eng. Chem., Jan. 153
(2)	"Rate of Solution of Crystals", Wilhelm, Conklin, and Sauer, Ind. Eng. Chem. 33, p. 453-7 (1941)
(3)	"Unit Operation Review", Ind. Eng. Chem. 40 (1948)
(4)	"Kinetics of Sucrose Crystallization", A. Van Hook, Ind. Eng. Chem. 36, p. 1042-8 (1944)
(5)	"Kinetics of Sucrose Grystallization", A. Van Hook, Ind. Eng. Chem. 37, p. 782-5 (1945)
(6)	"Effect of Agitation on Growth of Single Crystals", A.W. Hixson and K.L. Knox, Ind. Eng. Chem. 43, p. 2144-51 (1951)
(7)	"Rate of Growth of Crystals in Aqueous Solutions", W.L. McCabe and R.P. Stevens, Chem. Eng. Prog. <u>47</u> , p. 168-74 (1951)
(8)	"Nature and Measure of Agitation", A.W. Hixson, Ind. Eng. Chem. <u>36</u> , p. 488-96 (1944)
(9)	Crystal Growth, H.E. Buckley, Wiley & Sons, N.Y. 1951
(10)	"Velocity of Crystellization from Aqueous Solutions", N.P. Campbell, Chem. Soc. Journal (London) 107, p. 475-8 (1915)

- (11) International Critical Tables, IV, p. 222.
- (12) Solubilities of Inorganic and Metal Organic Compounds, A. Seidell, Vol. I. 1940, Van Nostrand Co., N.Y.