

Exclusive J/ψ Detection and Physics with ECCE

X. Li¹, J. K. Adkins³⁸, Y. Akiba^{55,59}, A. Albataineh⁷³, M. Amaryan⁴⁹, I. C. Arsene⁷⁷, C. Ayerbe Gayoso⁴⁰, J. Bae⁶⁴, X. Bai⁸³, M.D. Baker^{6,30}, M. Bashkanov⁹³, R. Bellwied⁷¹, F. Benmokhtar¹⁶, V. Berdnikov¹⁴, J. C. Bernauer^{57,58,59}, F. Bock⁵¹, W. Boeglin¹⁸, M. Borysova⁸⁸, E. Brash¹², P. Brindza³⁰, W. J. Briscoe²², M. Brooks³⁴, S. Bueltmann⁴⁹, M. H. S. Bukhari²⁹, A. Bylinkin⁷³, R. Capobianco⁶⁹, W.-C. Chang³, Y. Cheon⁶², K. Chen⁹, K.-F. Chen⁴⁸, K.-Y. Cheng⁴², M. Chiu⁶, T. Chujo⁸⁰, Z. Citron⁵, E. Cline^{57,58}, E. Cohen⁴⁶, T. Cormier⁵¹, Y. Corrales Morales³⁴, C. Cotton⁸³, J. Crafts¹⁴, C. Crawford⁷⁴, S. Creekmore⁵¹, C. Cuevas³⁰, J. Cunningham⁵¹, G. David⁶, C. T. Dean³⁴, M. Demarteau⁵¹, S. Diehl⁶⁹, N. Doshita⁹⁰, R. Dupré²⁵, J. M. Durham³⁴, R. Dzhygadlo²¹, R. Ehlers⁵¹, L. El Fassi⁴⁰, A. Emmert⁸³, R. Ent³⁰, C. Fanelli³⁹, R. Fatemi⁷⁴, S. Fegan⁹³, M. Finger¹⁰, M. Finger Jr.¹⁰, J. Frantz⁵⁰, M. Friedman²⁴, I. Friscic^{39,30}, D. Gangadharan⁷¹, S. Gardner²⁰, K. Gates²⁰, F. Geurts⁵⁴, R. Gilman⁵⁶, D. Glazier²⁰, E. Glimos⁵¹, Y. Goto^{55,59}, N. Grau⁴, S. V. Greene⁸⁴, A. Q. Guo²⁷, L. Guo¹⁸, S. K. Ha⁹¹, J. Haggerty⁶, T. Hayward⁶⁹, X. He¹⁹, O. Hen³⁹, D. W. Higinbotham³⁰, M. Hoballah²⁵, T. Horn¹⁴, A. Hognmrtsyan², P.-h. J. Hsu⁴⁷, J. Huang⁶, G. Huber⁷⁸, A. Hutson⁷¹, K. Y. Hwang⁹², C. E. Hyde⁴⁹, M. Inaba⁶⁷, T. Iwata⁹⁰, H.S. Jo³³, K. Joo⁶⁹, N. Kalantarians⁸⁶, G. Kalicy¹⁴, K. Kawade⁶³, S. J. D. Kay⁷⁸, A. Kim⁶⁹, B. Kim⁶⁴, C. Kim⁵³, M. Kim⁵⁵, Y. Kim⁵³, Y. Kim⁶², E. Kistenev⁶, V. Klimenko⁶⁹, S. H. Ko⁶¹, I. Korover³⁹, W. Korsch⁷⁴, G. Krintiras⁷³, S. Kuhn⁴⁹, C.-M. Kuo⁴², T. Kutz³⁹, J. Lajoie²⁸, D. Lawrence³⁰, S. Lebedev²⁸, H. Lee⁶⁴, J. S. H. Lee⁷⁹, S. W. Lee³³, Y.-J. Lee³⁹, W. Li⁵⁴, W.B. Li^{57,58,89}, X. Li¹¹, X. Li³⁴, X. Li³⁹, Y. T. Liang²⁷, S. Lim⁵³, C.-H. Lin³, D. X. Lin²⁷, K. Liu³⁴, M. X. Liu³⁴, K. Livingston²⁰, N. Liyanage⁸³, W.J. Llope⁸⁷, C. Loizides⁵¹, E. Long⁷⁶, R.-S. Lu⁴⁸, Z. Lu¹¹, W. Lynch⁹³, S. Mantry⁷⁰, D. Marchand²⁵, M. Marcisovsky¹⁵, C. Markert⁸¹, P. Markowitz¹⁸, H. Marukyan², P. McGaughey³⁴, M. Mihovilovic⁷⁵, R. G. Milner³⁹, A. Milov⁸⁸, Y. Miyachi⁹⁰, A. Mkrtchyan², P. Monaghan¹², R. Montgomery²⁰, D. Morrison⁶, A. Movsisyan², H. Mkrtchyan², A. Mkrtchyan², C. Munoz Camacho²⁵, M. Murray⁷³, K. Nagai³⁴, J. Nagle⁶⁸, I. Nakagawa⁵⁵, C. Nattrass⁸², D. Nguyen³⁰, S. Niccolai²⁵, R. Nouicer⁶, G. Nukazuka⁵⁵, M. Nycz⁸³, V. A. Okorokov⁴⁵, S. Orešić⁷⁸, J.D. Osborn⁵¹, C. O'Shaughnessy³⁴, S. Paganis⁴⁸, Z. Papandreou⁷⁸, S. F. Pate⁴⁴, M. Patel²⁸, C. Paus³⁹, G. Penman²⁰, M. G. Perdekamp⁷², D. V. Perepelitsa⁶⁸, H. Periera da Costa³⁴, K. Peters²¹, W. Phelps¹², E. Piasetzky⁶⁵, C. Pinkenburg⁶, I. Prochazka¹⁰, T. Protzman³⁶, M. L. Purschke⁶, J. Putschke⁸⁷, J. R. Pybus³⁹, R. Rajput-Ghoshal³⁰, J. Rason⁵¹, B. Raue¹⁸, K.F. Read⁵¹, K. Røed⁷⁷, R. Reed³⁶, J. Reinhold¹⁸, E. L. Renner³⁴, J. Richards⁶⁹, C. Riedl⁷², T. Rinn⁶, J. Roche⁵⁰, G. M. Roland³⁹, G. Ron²⁴, M. Rosati²⁸, C. Royon⁷³, J. Ryu⁵³, S. Salur⁵⁶, N. Santiesteban³⁹, R. Santos⁶⁹, M. Sarsour¹⁹, J. Schambach⁵¹, A. Schmidt²², N. Schmidt⁵¹, C. Schwarz²¹, J. Schwiening²¹, R. Seidl^{55,59}, A. Sickles⁷², P. Simmerling⁶⁹, S. Sirca⁷⁵, D. Sharma¹⁹, Z. Shi³⁴, T.-A. Shibata⁴³, C.-W. Shih⁴², S. Shimizu⁵⁵, U. Shrestha⁶⁹, K. Slifer⁷⁶, K. Smith³⁴, D. Sokhan^{20,26}, R. Soltz³⁷, W. Sondheim³⁴, J. Song¹¹, J. Song⁵³, I. I. Strakovsky²², P. Steinberg⁶, P. Stepanov¹⁴, J. Stevens⁸⁹, J. Strube⁵², P. Sun¹¹, X. Sun⁹, K. Suresh⁷⁸, V. Tadevosyan², W.-C. Tang⁴², S. Tapia Araya²⁸, S. Tarafdar⁸⁴, L. Teodorescu⁷, D. Thomas⁸¹, A. Timmins⁷¹, L. Tomasek¹⁵, N. Trotta⁶⁹, R. Trotta¹⁴, T. S. Tveter⁷⁷, E. Umaka²⁸, A. Usman⁷⁸, H. W. van Hecke³⁴, C. Van Hulse²⁵, J. Velkovska⁸⁴, E. Voutier²⁵, P.K. Wang²⁵, Q. Wang⁷³, Y. Wang⁹, Y. Wang⁶⁶, D. P. Watts⁹³, N. Wickramaarachchi¹⁴, L. Weinstein⁴⁹, M. Williams³⁹, C.-P. Wong³⁴, L. Wood⁵², M. H. Wood⁸, C. Woody⁶, B. Wyslouch³⁹, Z. Xiao⁶⁶, Y. Yamazaki³², Y. Yang⁴¹, Z. Ye⁶⁶, H. D. Yoo⁹², M. Yurov³⁴, N. Zachariou⁹³, W.A. Zajc¹³, W. Zha^{1,*}, J.-L. Zhang⁶⁰, J.-X. Zhang⁸³, Y. Zhang⁶⁶, Y.-X. Zhao²⁷, X. Zheng⁸³, P. Zhuang⁶⁶

¹University of Science and Technology of China, Hefei, China

²A. Alikhanyan National Laboratory, Yerevan, Armenia

³Institute of Physics, Academia Sinica, Taipei, Taiwan

⁴Augustana University, Sioux Falls, SD, USA

⁵Ben-Gurion University of the Negev Beer-Sheva, Israel

⁶Brookhaven National Laboratory, Upton, NY, USA

⁷Brunel University London, Uxbridge, UK

⁸Canisius College, Buffalo, NY, USA

⁹Central China Normal University, Wuhan, China

¹⁰Charles University, Prague, Czech Republic

¹¹China Institute of Atomic Energy, Fangshan, Beijing, China

¹²Christopher Newport University, Newport News, VA, USA

¹³Columbia University, New York, NY, USA

¹⁴Catholic University of America, Washington DC, USA

¹⁵Czech Technical University, Prague, Czech Republic

¹⁶Duquesne University, Pittsburgh, PA, USA

¹⁷Duke University, Durham NC, USA

¹⁸Florida International University, Miami, FL, USA

¹⁹Georgia State University, Atlanta, GA, USA

²⁰University of Glasgow, Glasgow, UK

²¹GSI Helmholtzzentrum fuer Schwerionenforschung GmbH, Darmstadt, Germany

*first@ustc.edu.cn

- ²²The George Washington University, Washington, DC, USA
²³Hampton University, Hampton, VA, USA
²⁴Hebrew University, Jerusalem, Israel
²⁵Universite Paris-Saclay, CNRS/IN2P3, IJCLab, Orsay, France
²⁶IRFU, CEA, Universite Paris-Saclay, Gif-sur-Yvette France
²⁷Chinese Academy of Sciences, Lanzhou, China
²⁸Iowa State University, Iowa City, IA, USA
²⁹Jazan University, Jazan, Saudi Arabia
³⁰Thomas Jefferson National Accelerator Facility, Newport News, VA, USA
³¹James Madison University, Harrisonburg, VA, USA
³²Kobe University, Kobe, Japan
³³Kyungpook National University, Daegu, Republic of Korea
³⁴Los Alamos National Laboratory, Los Alamos, NM, USA
³⁵Lawrence Berkeley National Lab, Berkeley, CA, USA
³⁶Lehigh University, Bethlehem, PA, USA
³⁷Lawrence Livermore National Laboratory, Livermore, CA, USA
³⁸Morehead State University, Morehead, KY
³⁹Massachusetts Institute of Technology, Cambridge, MA, USA
⁴⁰Mississippi State University, Mississippi State, MS, USA
⁴¹National Cheng Kung University, Tainan, Taiwan
⁴²National Central University, Chungli, Taiwan
⁴³Nihon University, Tokyo, Japan
⁴⁴New Mexico State University, Las Cruces, NM, USA
⁴⁵National Research Nuclear University MEPhI, Moscow, Russian Federation
⁴⁶Nuclear Research Center - Negev, Beer-Sheva, Israel
⁴⁷National Tsing Hua University, Hsinchu, Taiwan
⁴⁸National Taiwan University, Taipei, Taiwan
⁴⁹Old Dominion University, Norfolk, VA, USA
⁵⁰Ohio University, Athens, OH, USA
⁵¹Oak Ridge National Laboratory, Oak Ridge, TN, USA
⁵²Pacific Northwest National Laboratory, Richland, WA, USA
⁵³Pusan National University, Busan, Republic of Korea
⁵⁴Rice University, Houston, TX, USA
⁵⁵RIKEN Nishina Center, Wako, Saitama, Japan
⁵⁶The State University of New Jersey, Piscataway, NJ, USA
⁵⁷Center for Frontiers in Nuclear Science, Stony Brook, NY, USA
⁵⁸Stony Brook University, Stony Brook, NY, USA
⁵⁹RIKEN BNL Research Center, Upton, NY, USA
⁶⁰Shandong University Qingdao, Shandong, China
⁶¹Seoul National University, Seoul, Republic of Korea
⁶²Sejong University, Seoul, Republic of Korea
⁶³Shinshu University, Matsumoto, Nagano, Japan
⁶⁴Sungkyunkwan University, Suwon, Republic of Korea
⁶⁵Tel Aviv University, Tel Aviv, Israel
⁶⁶Tsinghua University, Beijing, China
⁶⁷Tsukuba University of Technology, Tsukuba, Ibaraki, Japan
⁶⁸University of Colorado Boulder, Boulder, CO, USA
⁶⁹University of Connecticut, Storrs, CT, USA
⁷⁰University of North Georgia, Dahlonega GA, USA
⁷¹University of Houston, Houston, TX, USA
⁷²University of Illinois, Urbana, IL, USA
⁷³University of Kansas, Lawrence, KS, USA
⁷⁴University of Kentucky, Lexington, KY, USA
⁷⁵University of Ljubljana, Ljubljana, Slovenia, Ljubljana, Slovenia
⁷⁶University of New Hampshire, Durham, NH, USA
⁷⁷University of Oslo, Oslo, Norway
⁷⁸University of Regina, Regina, SK, Canada
⁷⁹University of Seoul, Seoul, Republic of Korea
⁸⁰University of Tsukuba, Tsukuba, Japan
⁸¹University of Texas, Austin, Texas, USA
⁸²University of Tennessee, Knoxville, TN, USA
⁸³University of Virginia, Charlottesville, VA, USA
⁸⁴Vanderbilt University, Nashville, TN, USA
⁸⁵Virginia Tech, Blacksburg, VA, USA
⁸⁶Virginia Union University, Richmond, VA, USA
⁸⁷Wayne State University, Detroit, MI, USA
⁸⁸Weizmann Institute of Science, Rehovot, Israel
⁸⁹The College of William and Mary, Williamsburg, VA, USA
⁹⁰Yamagata University, Yamagata, Japan
⁹¹Yarmouk University, Irbid, Jordan
⁹²Yonsei University, Seoul, Republic of Korea

Abstract

Exclusive heavy quarkonium photoproduction is one of the most popular processes in EIC, which has a large cross section and a simple final state. Due to the gluonic nature of the exchange Pomeron, this process can be related to the gluon distributions in the nucleus. The momentum transfer dependence of this process is sensitive to the interaction sites, which provides a powerful tool to probe the spatial distribution of gluons in the nucleus. Recently the problem of the origin of hadron mass has received lots of attention in determining the anomaly contribution M_a . The trace anomaly is sensitive to the gluon condensate, and exclusive production of quarkonia such as J/ψ and Υ can serve as a sensitive probe to constrain it. In this paper, we present the performance of the ECCE detector for exclusive J/ψ detection and the capability of this process to investigate the above physics opportunities with ECCE.

Keywords: ECCE, Electron Ion Collider, Exclusive, Near Threshold, Quarkonia

Contents

1 Introduction	3
2 Simulation Framework of ECCE Detector Setup for J/ψ Detection	4
3 Theoretical Setup for Projection	5
4 Physics Opportunities with Exclusive J/ψ Photoproduction at ECCE	6
5 Summary	9

1. Introduction

Nuclear parton distribution functions (nPDF) describe the behavior of bound partons in the nucleus. Most of the understanding of nPDF comes from fixed-target experiments. Determination of nPDF is through global fits to existing inclusive deep inelastic scattering (DIS) data. Constructing the ratio nPDF/PDF to quantified nuclear modifications is natural, which can cancel many of the theory uncertainties. A ratio below unity is called shadowing, while an enhancement is known as anti-shadowing. Recently a moderate gluon shadowing has been exhibited by J/ψ photoproduction data from LHC [1, 2, 3]. However, little is known about anti-shadowing at $x \sim 0.1$. The realization of the EIC with variable ion beam species will enable measurements of nPDF over a broad range of x and Q^2 . Photoproduction of vector meson via photon-Pomeron fusion is able to cleanly and clearly determine nuclear gluon PDFs at the EIC. With broad x coverage, J/ψ photoproduction can provide precise measurements to deepen our understanding of shadowing and anti-shadowing.

Exclusive photoproduction, which has a large cross section and a simple final state, is projected to play a prominent role in the heavy quarkonia production processes at the EIC. In the reaction, a virtual incident photon fluctuates into a

quark-antiquark pair, which scatters elastically off the target and emerges as a real quarkonium. The scattering process occurs via the exchange of a color neutral object, Pomeron, which can be viewed as two gluons with self interaction (gluon ladder) in the language of QCD. Due to the gluonic nature of Pomeron, the exclusive heavy quarkonia photoproduction at EIC can be related to the gluon distributions in the proton and nucleus using perturbative QCD. Furthermore, the distribution of momentum transfer from the target in the process is sensitive to the interaction sites, which provides a powerful tool to probe the spatial distribution of gluon in the nucleus.

Nucleons constitute about 99% of the mass of the visible universe. In the standard model, Higgs mechanism describes gauge bosons' "mass" generation. However it can only account for a small fraction of the nucleon mass. The major part comes from the strong interaction that binds quarks and gluons together. Understanding the hadron mass decomposition from strong interaction has become a topic of great interest in QCD. There are two key models [4, 5, 6, 7, 8, 9] for the mass decomposition. One contains a trace anomaly contribution which is quantified by the energy-momentum tensor (EMT), and the other one agrees with an energy decomposition in the rest frame of the system. Recently, there has been sustained interest [10, 11, 12] among the nucleon structure community in determining the anomaly contribution M_a as a key to understanding the origin of the proton mass. Specifically, it has been proposed, based on some theorists' suggestions [13, 14, 15], that M_a can be accessed through the forward ($t=0$) cross section via the exclusive production of heavy quarkonia states such as J/ψ and Υ . Heavy quarkonia are of particular interest here because they only couple to gluons, not to light quarks, and are thus sensitive to the gluonic structure of the proton. The trace anomaly is sensitive to the gluon condensate, with sensitivity greatest for production around the threshold.

In this paper, we simulate exclusive J/ψ production using Fun4All framework with the designed ECCE detector system.

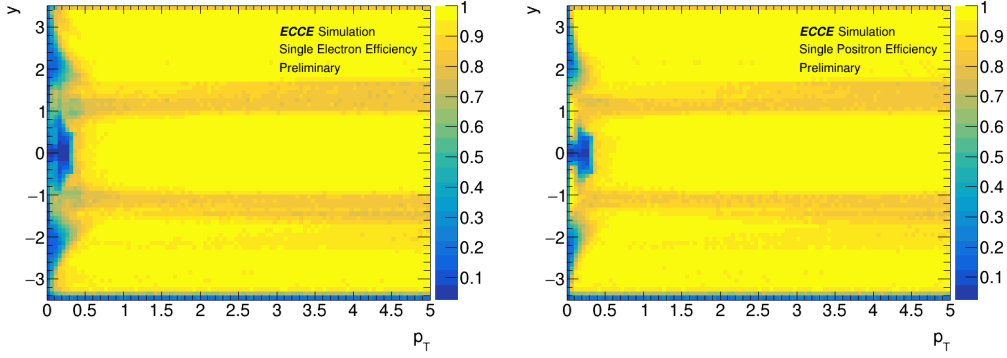


Figure 1: Single track efficiency. Left Panel: e^- efficiency. Right Panel: e^+ efficiency

In the simulation, we utilize eSTARLight model as the event generator for the exclusive photoproduction process. We make a projection of the exclusive J/ψ measurement at ECCE under the designed integrated luminosity of one year running for EIC to give an insight into related fruitful physics opportunities, such as probing the nuclear gluon PDF, spatial distribution and proton mass decomposition. The major goal of this research is to present the detection capability and the physics opportunities which could be achieved with the ECCE detector setup for the exclusive process of J/ψ photoproduction.

2. Simulation Framework of ECCE Detector Setup for J/ψ Detection

The ECCE detector is a cylindrical detector covering $|\eta| \leq 3.5$ and the full azimuth. ECCE's tracking and vertexing systems use semiconductor and gaseous tracking detector technologies: Monolithic Active Pixel Sensor (MAPS) based silicon vertex/tracking detector and μ Rwell based gas tracker derived from Gas Electron Multiplier (GEM) technology. According to the simulation of the designed tracking system, the momentum resolution of the central region and beam e-going direction is closed to or better than the requirement of Yellow Report (YR) [16].

For exclusive photoproduction of J/ψ , we adopt eSTARLight prediction of the cross section for $ep \rightarrow eJ/\psi p$ process with two minor improvements, detailed in Sec. 3. eSTARLight provides a photo-Pomeron interaction model parameterized by HERA data. In this study, two beam configurations, 5×41 GeV and 10×100 GeV, are used for e+p and e+Au collisions.

The detector response simulation is done by a GEANT4 based package called Fun4All. In this work, the "Prop.7" detector concept is employed in J/ψ reconstruction via dielectron channel. Single e^+/e^- Tracking simulation results are shown as Fig. 1. The difference in efficiency between e^+ and e^- at very low p_T is due to the initial assumption parameter in the Kalman filter. If the beginning parameter is set to "positron," negative charge particles will have a low match quality and will likely be rejected.

The kinematic distribution of J/ψ for exclusive photoproduction is initialized by the theoretical calculation from eSTARLight. With this as input, we can obtain J/ψ reconstruction

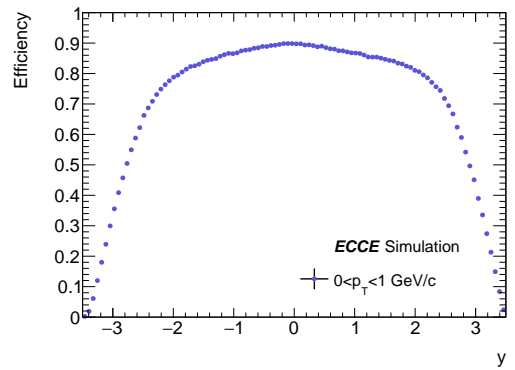


Figure 2: Tracking efficiency of J/ψ from exclusive J/ψ simulation.

efficiency from the Fun4All package with ECCE detector setup seen in Fig. 2. The efficiency of J/ψ is almost independent of the rapidity and transverse momentum except for the edge area at large forward and backward rapidity. We also study the effect of magnetic field strength and bremsstrahlung energy loss of electron on J/ψ detection, shown as Fig. 3. At very low p_T ($0.5 < p_T < 1.0$ GeV/c), the improvement of the acceptance of the lower magnetic field strength accounts for the higher efficiency. While at larger p_T ($1.0 < p_T < 2.0$ GeV/c), there is no significant difference between efficiencies of 0.7 Tesla and 1.4 Tesla. The bremsstrahlung energy loss has already been put in tracking performance in the "Prop.7" concept detector, which constitutes the tail in the reconstructed mass distribution depicted as the right panel in Fig. 3. We scale the mass distribution to unity for the convenience of comparison, and the efficiencies of several mass window cuts are detailed in Table. 1. As expected, the tail effect is more significant for the J/ψ at forward and backward rapidities (larger momentum of decayed electrons than that at central rapidity). With a proper mass cut window, the efficiency loss is minimal, implying that the effect of bremsstrahlung on J/ψ reconstruction with ECCE setup is not significant.

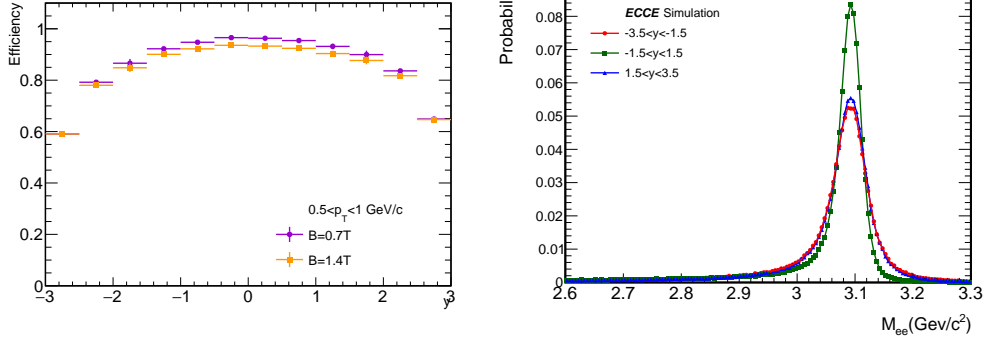


Figure 3: Magnetic strength effect on efficiency and bremsstrahlung energy loss effect on J/ψ reconstruction.

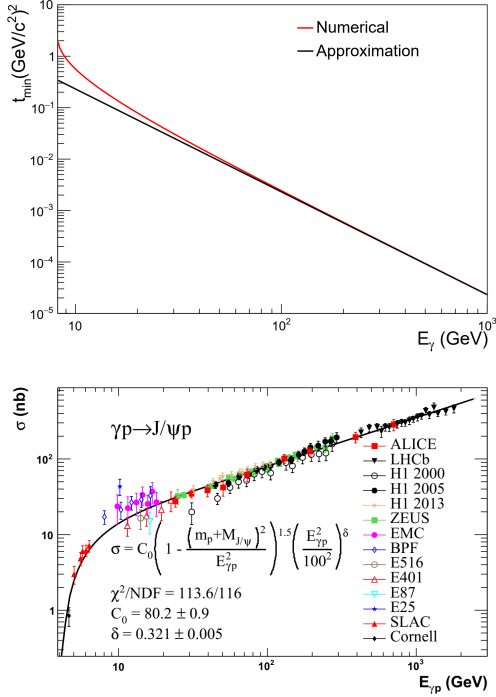


Figure 4: Upper Panel: The minimum momentum transfer as a function of incident photon energy in the rest frame of the nuclear beam (target frame). Lower Panel: The world-wide measurements of $\sigma(\gamma p \rightarrow V p)$.

Table 1: Efficiency of mass window cut for J/ψ reconstruction

mass window (GeV/c ²)	-3.5 < y < -1.5	-1.5 < y < 1.5	1.5 < y < 3.5
2.8-3.2	0.931	0.943	0.934
2.9-3.2	0.903	0.917	0.907
3.0-3.2	0.835	0.866	0.843

3. Theoretical Setup for Projection

This section presents the theoretical framework of exclusive J/ψ photoproduction in $e+p$ and $e+A$ collisions, which is employed in the simulation. The cross section of exclusive vector meson photoproduction $\sigma(eA \rightarrow eAV)$ is calculated as an integration of photon flux induced by the electron beam and the collision of the virtual photon on the target nucleus. The cross section of exclusive vector meson photoproduction $\sigma(eA \rightarrow eAV)$ is derived by integrating the photon flux caused by the electron beam and the virtual photon collision on the target nucleus, as illustrated in Eq.(1):

$$\sigma(eA \rightarrow eAV) = \int \frac{dW}{W} \int dk \int dQ^2 \frac{d^2 N_\gamma}{dkdQ^2} \sigma_{\gamma^* A \rightarrow VA}(W, Q^2), \quad (1)$$

where the photon flux can be written as:

$$\frac{d^2 N_\gamma}{dkdQ^2} = \frac{\alpha}{\pi k Q^2} \left[1 - \frac{k}{Ee} + \frac{k^2}{2Ee^2} - \left(1 - \frac{k}{Ee} \right) \left| \frac{Q_{\min}^2}{Q^2} \right| \right]. \quad (2)$$

The cross section of virtual photon collision on the nucleus can be related to the production cross section with real photon:

$$\sigma_{\gamma^* A \rightarrow VA}(W, Q^2) = f(M_V) \sigma(W, Q^2 = 0) \left(\frac{M_V^2}{M_V^2 + Q^2} \right)^n \quad (3)$$

$$n = c_1 + c_2 (Q^2 + M_V^2),$$

where c_1 and c_2 are parameters determined by the HERA measurements. $f(M_V)$ is the Breit-Wigner distribution of the vector meson. And the cross section at $Q^2 = 0$ can be calculated by the integration of the forward scattering cross section and the square of the nucleus form factor, revealed as Eq.(4):

$$\sigma(W, Q^2 = 0) = \int_{t_{\min}}^{\infty} dt \frac{d\sigma(\gamma A \rightarrow VA)}{dt} \Big|_{t=0} |F(t)|^2, \quad (4)$$

where $\frac{d\sigma(\gamma A \rightarrow VA)}{dt} \Big|_{t=0}$ can be determined by $\frac{d\sigma(\gamma p \rightarrow Vp)}{dt} \Big|_{t=0}$ via Glauber approach. The cross section of $\gamma p \rightarrow Vp$ can be

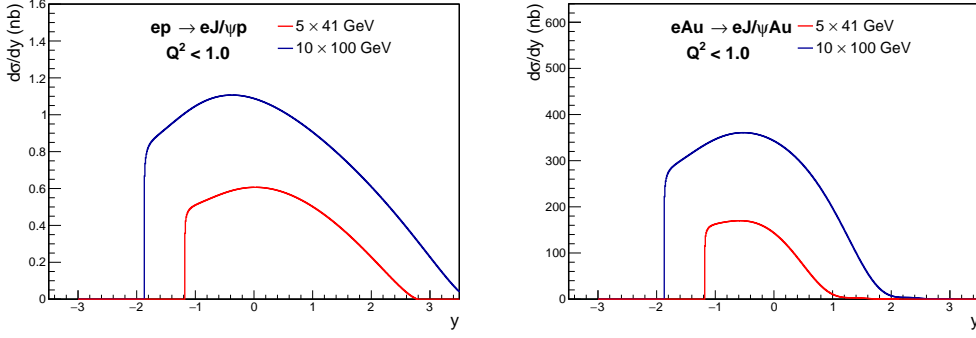


Figure 5: Rapidity dependence of differential cross section of exclusive J/ψ photoproduction for $Q^2 < 1 \text{ GeV}^2$.

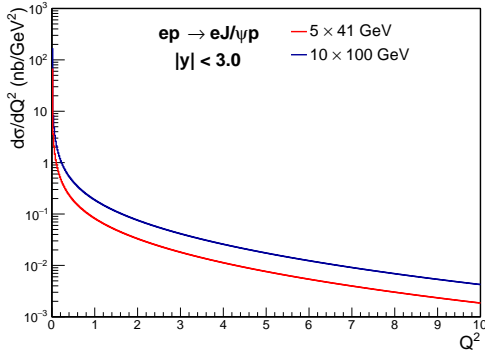


Figure 6: The Q^2 dependence of differential cross section of exclusive J/ψ photoproduction in e+p collision.

parameterized using the world-wide measurements [17]. The framework is almost the same as eSTARLight [18][19], except for two minor improvements. In eSTARLight, the minimum momentum transfer t_{min} is approximated as $t_{min} = ((M_v)^2/2k)^2$. One can get the minimum of t when the transverse momentum of the produced vector meson is equal to zero. Then true t_{min} can be obtained from energy-momentum conservation of the $\gamma p \rightarrow Vp$ process in the target frame as Eq.(5):

$$E_\gamma + m_p = \sqrt{M_v^2 + (E_\gamma - P_z'^2)} + \sqrt{m_p^2 + P_z'^2}, \quad (5)$$

$$t = (P' - P)^2 = \left(\sqrt{m_p^2 + P_z'^2} - m_p \right)^2 - P_z'^2, \quad (6)$$

where $P_z'^2$ is the longitudinal momentum of the final state proton. The photon energy dependence of t_{min} can be found in the upper panel of Fig. 4. The approximation in eSTARLight is proper at high photon energy. However, it would underestimate the magnitude at low values of photon energy, as is the case for our projection at ECCE. Furthermore, in eSTARLight, the parametrization of the $\gamma p \rightarrow Vp$ cross section is only based on high-energy HERA data. The behavior of energy dependency is notably different between the high and low energy ranges, as demonstrated in the lower panel of Fig. 4, which would skew the computations at EIC. With these two improvements, the calculated results of rapidity distribution for

exclusive J/ψ photoproduction in e+p and e+A collisions for 5×41 and 10×100 GeV collision energies are shown in Fig. 5. Q^2 dependence of e+p collision for 5×41 and 10×100 GeV with a rapidity range from -3 to 3 is illustrated in Fig. 6.

The raw counts per unit rapidity are shown in Fig. 7 for e+p and e+Au collisions for 10×100 GeV. For the projection results in the following section, we assume the integrated luminosity collected by ECCE is 100 fb^{-1} for e+p collisions and $10 \text{ fb}^{-1}/A$ for e+Au collisions, where A is the mass number of Au. The figure shows that millions of J/ψ s would be observed with the designed ECCE setup, which provides us with plenty of physics opportunities. And Q^2 dependence of the statistics of e+p collision in 5×41 and 10×100 GeV are shown in Fig. 8. As we can see, most events locate in the low Q^2 region, especially for $Q^2 < 1 \text{ GeV}^2$.

4. Physics Opportunities with Exclusive J/ψ Photoproduction at ECCE

4.1. Probe the nuclear gluon PDF

The gluon parton distribution functions (PDFs) in the proton and nucleus have large uncertainties because gluons do not carry any electric charge and can not be directly determined by the DIS measurements. As mentioned in the introduction, the exclusive J/ψ photoproduction occurs via Pomeron exchange. Due to the gluonic nature of Pomeron, this process is directly sensitive to the gluon PDF. According to the calculation of perturbative QCD, the forward scattering cross section is proportional to the square of the gluon density distribution, shown in the following [20][21]:

$$\frac{d\sigma(\gamma A \rightarrow VA)}{dt} \Big|_{t=0} = \frac{\alpha_s^2 \Gamma_{ee}}{3\alpha M_V^\epsilon} 16\pi^3 [xg_A(x, \mu^2)]^2, \quad (7)$$

where Γ_{ee} is the width of the electronic decay of J/ψ , $g_A(x, \mu^2)$ is the gluon density and the momentum fraction x can be determined by the rapidity of J/ψ :

$$x = \frac{M_V e^y}{2E_N}, \quad (8)$$

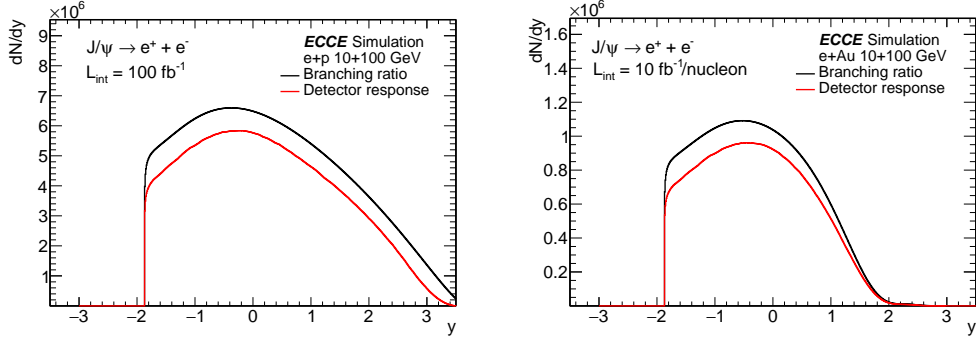


Figure 7: Rapidity dependence statistics of coherent exclusive production of J/ψ in e+p and e+Au collisions for 10×100 GeV. Left Panel: e+p collision. Right Panel: e+Au collision

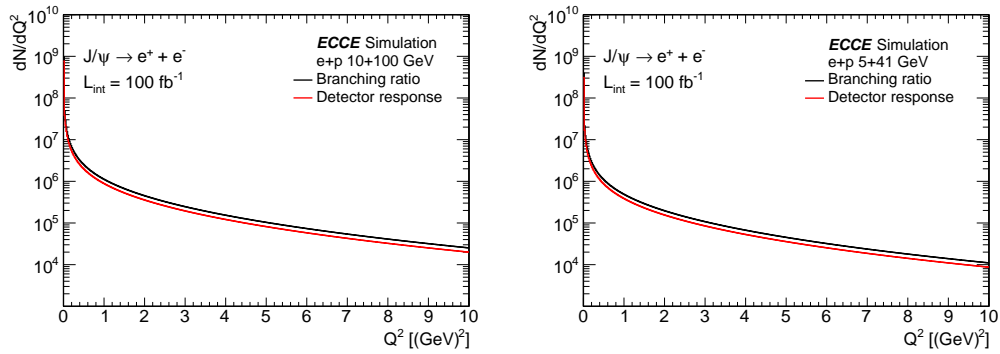


Figure 8: The Q^2 dependence of J/ψ photoproduction in e+p. Left Panel: 10×100 GeV. Right Panel: 5×41 GeV.

where E_N is the energy of nuclear beam per nucleon. Eq.(7) is derived from leading order (LO) pQCD calculation in the non-relativistic approximation [20], which indicates that the transverse momenta of c quarks in J/ψ are negligible. In that case, it is prescribed that $\mu^2 = M_V^2/4$.

The nuclear gluon shadowing can be model-independently quantified by R_g :

$$R_g = \sqrt{\frac{\left. \frac{d\sigma(\gamma A \rightarrow VA)}{dt} \right|_{t=0}}{\left. \frac{d\sigma(\gamma p \rightarrow Vp)}{dt} \right|_{t=0}}}. \quad (9)$$

As shown in Eq.(7), if we make the forward scattering amplitude ratio between e+p and e+Au collisions, the shadowing factor R_g of gluon can be directly extracted. So measurements of J/ψ photoproduction can provide direct access to $g_A(x, \mu^2)$.

Elastic J/ψ photoproduction processes are simulated in 10×100 (GeV) e+p and e+Au collisions with the framework described in the above sections. From the simulation, we extracted the $d^2\sigma/dtdy$ of J/ψ at $t=0$ for both e+p and e+Au collisions to make projection on R_g . The uncertainty of the projection only includes the statistical error. At a given x , we can transfer it to the corresponding y value via Eq.(8) and get the statistics with the detector response. Then we fit the simulated t distribution with the predicted statistics and get the fit error of $d\sigma/dt$ for e+p and e+Au collisions at $t=0$. The statisti-

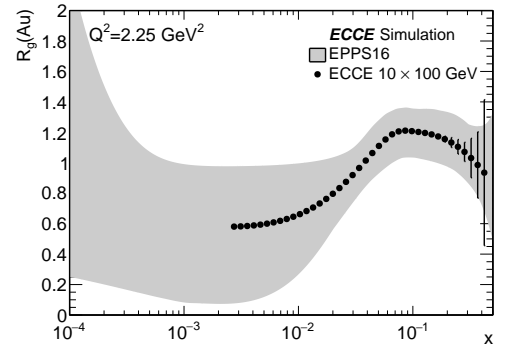


Figure 9: Gluon nuclear shadowing factor as function of momentum fraction x .

cal error of projection can be extracted by the error propagation approach via R_g equation in Eq.(8). As shown in Fig.9, the measurement of exclusive J/ψ production has a wide x coverage down to 2×10^{-3} for beam configuration 10×100 GeV. In the low x region, the EPPS16 [22] PDF set has a large uncertainty band, while the projected statistical error for ECCE is negligible. This shows that the precision exclusive J/ψ measurements at the EIC will significantly reduce the uncertainty of the nuclear gluon PDF at low values of x ($x < 10^{-2}$).

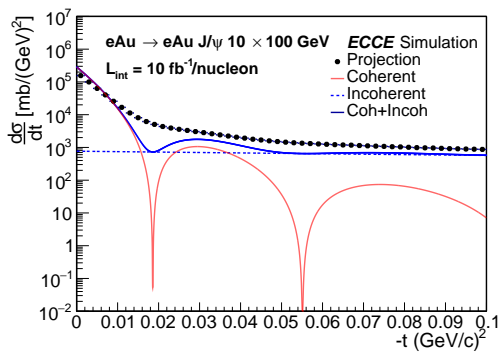


Figure 10: t dependence of exclusive J/ψ production in $e+Au$ collision. Woods-Saxon distribution is used as input.

4.2. Probe the Gluon Spatial Distribution

The Pomeron is the exchange object for the diffractive process, and diffraction is generally sensitive to spatial distribution. The momentum transfer from the target in the exclusive J/ψ photoproduction is sensitive to the production site, which provides us with a powerful tool to infer the spatial distribution of gluon in both proton and nucleus.

In the simulation, the Woods-Saxon distribution is used as input of the gluon source distribution $F(b)$. We made a projection of t distribution for the processes in 10×100 (GeV) $e+Au$ collisions with both coherent and incoherent J/ψ photoproduction. The results are shown in Fig.10, the red and blue curves are the coherent and incoherent contributions from calculations, respectively. The solid data points are the projected results from simulation, in which the statistical uncertainty is negligible. However, it should be noticed that according to the state of the art theoretical calculation of elastic scattering, we will not get this minimum at these dips [23][24]. So the model here is a simplified and ideal one, and the purpose is to show the momentum resolution impact on this t dependence. Due to the momentum smearing from tracking system, the slope of the distribution is slightly different from that of theoretical calculations, and the diffraction dips are fold out. This suggests that the detector response should be precisely determined to extract the gluon spatial distribution.

The projected t distributions in 5×41 and 10×100 (GeV) $e+p$ collisions are illustrated in Fig. 11 with the systematical and the statistical errors for different Q^2 regions (0-1, 1-3 and 3-10 GeV^2). The statistical error is determined with a similar approach given in Sec.4.1. The systematical uncertainty is determined by the maximum deviation between the input and reconstructed t distribution. The statistical and systematical uncertainties are added in quadrature.

4.3. The Near-Threshold Production Mechanism

The elastic near-threshold J/ψ production can provide new insight into multi-quark, gluonic, hidden-color correlations of hadronic and nuclear wave-functions in QCD. Moreover, the measurements of this process probe the $x \sim 1$ configuration in

the target, and the spectator partons carry a vanishing fraction $x \sim 0$ of the target momentum. This implies that the production rate behaves near $x \rightarrow 1$ as $(1-x)^{2n_s}$, where n_s is the number of spectators. Then two gluon and three gluon exchange contributions can be written as [25]:

$$\frac{d\sigma}{dt} = \mathcal{N}_{2g} v \frac{(1-x)^2}{R^2 M^2} F_{2g}^2(t) (W_{\gamma p}^2 - m_p^2)^2, \quad (10)$$

$$\frac{d\sigma}{dt} = \mathcal{N}_{3g} v \frac{(1-x)^0}{R^4 M^4} F_{3g}^2(t) (W_{\gamma p}^2 - m_p^2)^2, \quad (11)$$

where R is the radius of proton, M is the mass of J/ψ , and $W_{\gamma p}$ is the center of mass energy of γp .

The projected results for near-threshold production for 10×100 GeV and 5×41 GeV $e+p$ collisions are shown in Fig. 12. The GlueX results, two and three gluon exchange contributions are also shown for comparison. All the theoretical curves and projection results are normalized with the GlueX measurements. The error bars on GlueX measurements represent only statistical uncertainties. At low $W_{\gamma p} < 4.5$ GeV region, the cross section is dominated by three gluon exchange process. At $W_{\gamma p} > 4.5$ GeV, two gluon exchange process comes to take control. For 10×100 GeV $e+p$ collisions, the center-of-mass energy can only reach as low as 4.5 GeV due to the limited detector coverage. But for 5×41 GeV $e+p$ collisions, they cover the whole near-threshold range. The GlueX experiment at JLab has already shed light on the near-threshold production mechanism as a sum of two-gluon and three-gluon exchange and set limits on pentaquark production [26]. Measurements of near-threshold with larger statistics and broader $W_{\gamma p}$ range at the EIC has the potential to impose more powerful constraints on the production mechanism, like charmed pentaquark P_c production [27, 28].

4.4. Trace Anomaly and Proton Mass Decomposition

According to QCD theory, there are four terms of decomposition in nucleon mass as Eq.(12) [29]: quark energy M_q , gluon energy M_g , quark mass M_m and the trace anomaly contribution M_a , and these terms are sensitive to the momentum fraction a carried by all quarks and the trace anomaly parameter b .

$$\begin{aligned} M_q &= \frac{3}{4} \left(a - \frac{b}{1 + \gamma_m} \right) M_N, \\ M_g &= \frac{3}{4} (1 - a) M_N, \\ M_m &= \frac{4 + \gamma_m}{4(1 + \gamma_m)} b M_N, \\ M_a &= \frac{1}{4} (1 - b) M_N, \end{aligned} \quad (12)$$

Recent theoretical efforts from VMD model and Holographic model [30][31][32] suggest that the trace anomaly parameter can be extracted by the near-threshold exclusive heavy quarkonia process via their production at $(d\sigma/dt)|_{t=t_{min}}$. In the simulation, we made the projection of the trace anomaly parameter restriction capability at ECCE. The results are shown in Fig. 13

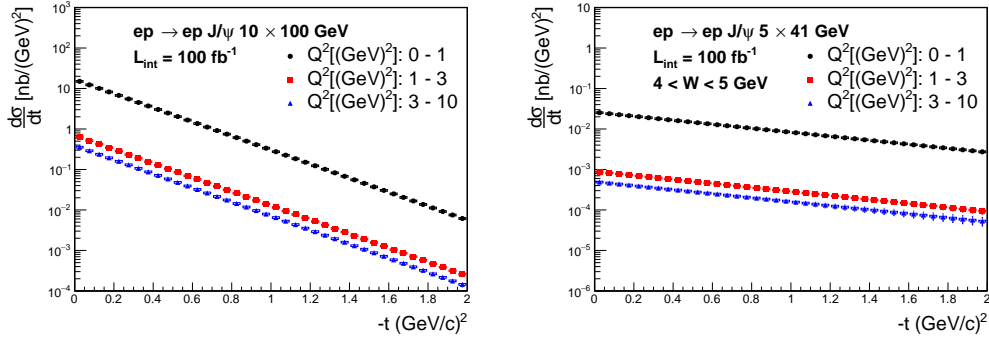


Figure 11: t dependence of exclusive J/ψ production in $e+p$ collision in several Q^2 intervals. Left Panel: 10×100 . Right Panel: 5×41

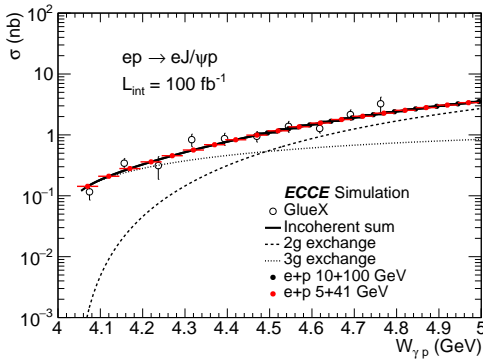


Figure 12: Projection of J/ψ photoproduction cross section near threshold in 10×100 GeV and 5×41 GeV $e+p$ collisions.

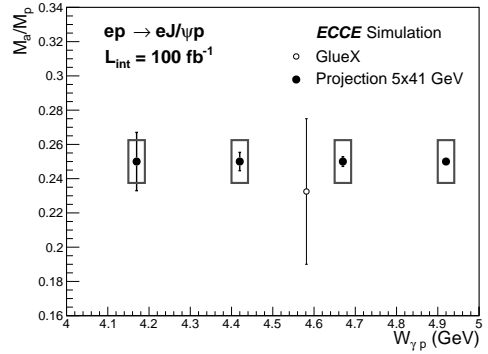


Figure 13: Trace anomaly contribution as a function of γp center of mass energy

and Fig. 14, which can provide precise information on the nucleon mass decomposition. The GlueX result [29] of the trace anomaly is also shown for comparison. The projection uncertainty consists of two parts, the statistical error using similar method as Sec. 4.1 and systematical error defined in Sec. 4.2. The $d\sigma/dt|_{t=0}$ can be related to the trace anomaly parameter with Eq.(13,14,15) [29],

$$\left. \frac{d\sigma_{\gamma N \rightarrow J/\psi N}}{dt} \right|_{t=0} = \frac{3\Gamma(J/\psi \rightarrow e^+e^-)}{\alpha m_{J/\psi}} \left(\frac{k_{J/\psi N}}{k_{\gamma N}} \right)^2 \left. \frac{d\sigma_{J/\psi N \rightarrow J/\psi N}}{dt} \right|_{t=0}, \quad (13)$$

$$\left. \frac{d\sigma_{J/\psi N \rightarrow J/\psi N}}{dt} \right|_{t=0} = \frac{1}{64\pi} \frac{1}{m_{J/\psi}^2 (\lambda^2 - m_N^2)} |F_{J/\psi N}|^2, \quad (14)$$

where $k_{ab}^2 = [s - (m_a + m_b)^2][s - (m_a - m_b)^2]/4s$ denotes the squared momentum of center-of-mass of the corresponding two-body system, Γ is the decay width of specific channel, α is the fine structure constant. $\lambda = (p_N p_{J/\psi}/m_{J/\psi})$ is the energy of nucleon in the J/ψ rest frame. At low energy, the forward amplitude $F_{J/\psi N}$ can be approximately written as a function of $(1-b)$ in Eq.(15), and the relative uncertainty of $d\sigma/dt|_{t=0}$ can be used to get the uncertainty of M_a/M_p ($\propto (1-b)$) via the error

propagation formula.

$$\begin{aligned} F_{J/\psi N} &\simeq r_0^3 d_2 \frac{2\pi^2}{27} \left(2M_N^2 - \left\langle N \left| \sum_{i=u,d,s} m_i \bar{q}_i q_i \right| N \right\rangle \right) \\ &\simeq r_0^3 d_2 \frac{2\pi^2}{27} (2M_N^2 - 2bM_N^2) \\ &\simeq r_0^3 d_2 \frac{2\pi^2}{27} 2M_N^2 (1-b), \end{aligned} \quad (15)$$

where r_0 is the "Bohr" radius of J/ψ , and d_2 is the Wilson coefficient. These two parameters can be treated as constant in the relationship between $d\sigma/dt|_{t=0}$ and $(1-b)$ at low energy, thus could be neglected in the uncertainty determination.

5. Summary

In this paper, we simulate exclusive J/ψ production using Fun4All framework with the designed ECCE detector system at the future EIC. For J/ψ detection, ECCE has good reconstruction efficiency and broad coverage, with large statistics for the designed EIC luminosity. We also demonstrate the capability of ECCE to probe the related physics opportunities for the exclusive J/ψ photoproduction process. For gluon distribution in the proton and nucleus, the projection of the gluon nuclear shadowing effect shows an excellent capability of constraining the nuclear gluon PDF with the exclusive J/ψ forward

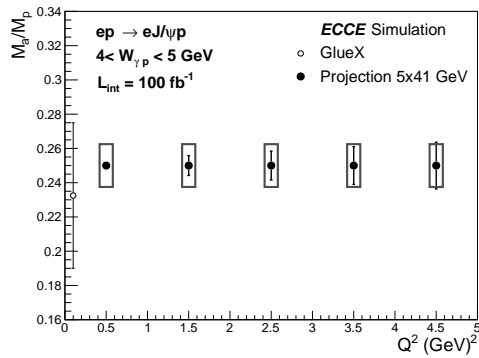


Figure 14: Trace anomaly contribution as a function of Q^2

scattering measurements at ECCE. Benefited from the unprecedented coverage and excellent reconstruction capability, ECCE can provide a strong constraint to the near-threshold production mechanism of the exclusive J/ψ photoproduction process. Furthermore, the projection results of the near-threshold exclusive heavy quarkonia production also show an excellent capability to extract the trace anomaly parameter to precisely determine the nucleon mass decomposition.

Acknowledgement

X. Li and W. Zha are supported by the National Natural Science Foundation of China (12005220, 12175223) and MOST(2018YFE0104900). The authors would like to thank the ECCE Consortium for performing a full simulation of their detector design, for providing up-to-date information on EIC run conditions, and for suggestions and comments on the manuscript. X. Li and W. Zha would like to thank Y. Zhou for useful suggestions and discussions related to this analysis.

References

- [1] B. Abelev, et al., Coherent J/ψ photoproduction in ultra-peripheral Pb–Pb collisions at $s_{NN} = 2.76\text{TeV}$, *Physics Letters B* 718 (4) (2013) 1273–1283. doi:<https://doi.org/10.1016/j.physletb.2012.11.059>. URL <https://www.sciencedirect.com/science/article/pii/S0370269312012257>
- [2] V. Khachatryan, et al., Coherent J/ψ photoproduction in ultra-peripheral PbPb collisions at $s_{NN} = 2.76\text{TeV}$ with the CMS experiment, *Physics Letters B* 772 (2017) 489–511. doi:<https://doi.org/10.1016/j.physletb.2017.07.001>. URL <https://www.sciencedirect.com/science/article/pii/S0370269317305488>
- [3] E. Abbas, et al., Charmonium and e^+e^- pair photoproduction at mid-rapidity in ultra-peripheral Pb–Pb collisions at $s_{NN} = 2.76\text{TeV}$, *The European Physical Journal C* 73 (11) (2013). doi:10.1140/epjc/s10052-013-2617-1. URL <https://link.springer.com/article/10.1140/epjc/s10052-013-2617-1>
- [4] X. Ji, QCD analysis of the mass structure of the nucleon, *Physical Review Letters* 74 (7) (1995) 1071–1074. doi:10.1103/physrevlett.74.1071. URL <http://dx.doi.org/10.1103/PhysRevLett.74.1071>
- [5] C. Lorcé, On the hadron mass decomposition, *The European Physical Journal C* 78 (120) (Feb 2018). doi:10.1140/epjc/s10052-018-5561-2. URL <http://dx.doi.org/10.1140/epjc/s10052-018-5561-2>
- [6] A. Metz, B. Pasquini, S. Rodini, Revisiting the proton mass decomposition, *Physical Review D* 102 (11) (Dec 2020). doi:10.1103/physrevd.102.114042. URL <http://dx.doi.org/10.1103/PhysRevD.102.114042>
- [7] C. Roberts, Empirical consequences of emergent mass, *Symmetry* 12 (9) (2020) 1468. doi:10.3390/sym12091468. URL <http://dx.doi.org/10.3390/sym12091468>
- [8] K. Tanaka, Three-loop formula for quark and gluon contributions to the QCD trace anomaly, *Journal of High Energy Physics* 2019 (1) (Jan 2019). doi:10.1007/jhep01(2019)120. URL [http://dx.doi.org/10.1007/JHEP01\(2019\)120](http://dx.doi.org/10.1007/JHEP01(2019)120)
- [9] M. Shifman, A. Vainshtein, V. Zakharov, Remarks on higgs-boson interactions with nucleons, *Physics Letters B* 78 (4) (1978) 443–446. doi:10.1016/0370-2693(78)90481-1. URL <https://www.sciencedirect.com/science/article/pii/0370269378904811>
- [10] X. Ji, Breakup of hadron masses and energy-momentum tensor of QCD, *Phys. Rev. D* 52 (1995) 271–281. arXiv:hep-ph/9502213, doi:10.1103/PhysRevD.52.271.
- [11] X. Ji, Proton mass decomposition: naturalness and interpretations, *Front. Phys. (Beijing)* 16 (6) (2021) 64601. arXiv:2102.07830, doi:10.1007/s11467-021-1065-x.
- [12] Y. Guo, X. Ji, Y. Liu, QCD Analysis of Near-Threshold Photon-Proton Production of Heavy Quarkonium, *Phys. Rev. D* 103 (9) (2021) 096010. arXiv:2103.11506, doi:10.1103/PhysRevD.103.096010.
- [13] S. Brodsky, E. Chudakov, P. Hoyer, J. Laget, Photoproduction of charm near threshold, *Physics Letters B* 498 (1-2) (2001) 23–28. doi:10.1016/S0370-2693(00)01373-3. URL [http://dx.doi.org/10.1016/S0370-2693\(00\)01373-3](http://dx.doi.org/10.1016/S0370-2693(00)01373-3)
- [14] O. Gryniuk, M. Vanderhaeghen, Accessing the real part of the forward J/ψ -p scattering amplitude from J/ψ Photoproduction on protons around threshold, *Physical Review D* 94 (7) (Oct 2016). doi:10.1103/physrevd.94.074001. URL <http://dx.doi.org/10.1103/PhysRevD.94.074001>
- [15] M. Du, V. Baru, F. Guo, C. Hanhart, U.-G. Meißner, A. Nefediev, I. Strakovsky, Deciphering the mechanism of Near-Threshold J/ψ Photoproduction, *The European Physical Journal C* 80 (11) (Nov 2020). doi:10.1140/epjc/s10052-020-08620-5. URL <http://dx.doi.org/10.1140/epjc/s10052-020-08620-5>
- [16] R. Abdul Khalek, et al., Science Requirements and Detector Concepts for the Electron-Ion Collider: EIC Yellow Report (Mar 2021). arXiv:2103.05419.
- [17] Z. Cao, L. Ruan, Z. Tang, Z. Xu, C. Yang, S. Yang, W. Zha, Photoproduction of J/ψ in non-single-diffractive p+p collisions, *Chinese Physics C* 43 (6) (2019) 064103. doi:10.1088/1674-1137/43/6/064103. URL <https://doi.org/10.1088/1674-1137/43/6/064103>
- [18] M. Lomnitz, S. Klein, Exclusive vector meson production at an electron-ion collider, *Phys. Rev. C* 99 (2019) 015203. doi:10.1103/PhysRevC.99.015203. URL <https://link.aps.org/doi/10.1103/PhysRevC.99.015203>
- [19] W. Zha, S. R. Klein, R. Ma, L. Ruan, T. Todoroki, Z. Tang, Z. Xu, C. Yang, Q. Yang, S. Yang, Coherent J/ψ Photoproduction in hadronic heavy-ion collisions, *Phys. Rev. C* 97 (2018) 044910. doi:10.1103/PhysRevC.97.044910. URL <https://link.aps.org/doi/10.1103/PhysRevC.97.044910>
- [20] V. Guzey, M. Zhalov, Exclusive J/ψ production in ultraperipheral collisions at the LHC: constraints on the gluon distributions in the proton and nuclei, *Journal of High Energy Physics* 2013 (10) (Oct 2013). doi:10.1007/jhep10(2013)207. URL [http://dx.doi.org/10.1007/JHEP10\(2013\)207](http://dx.doi.org/10.1007/JHEP10(2013)207)
- [21] V. Guzey, M. Zhalov, Rapidity and momentum transfer distributions of coherent J/ψ Photoproduction in ultraperipheral ppb collisions at the LHC, *Journal of High Energy Physics* 2014 (2) (Feb 2014). doi:10.1007/jhep02(2014)046. URL [http://dx.doi.org/10.1007/JHEP02\(2014\)046](http://dx.doi.org/10.1007/JHEP02(2014)046)

- [22] K. J. Eskola, P. Paakkinen, H. Paukkunen, C. A. Salgado, Eps16: nuclear parton distributions with LHC data, *The European Physical Journal C* 77 (3) (Mar 2017). doi:10.1140/epjc/s10052-017-4725-9. URL <http://dx.doi.org/10.1140/epjc/s10052-017-4725-9>
- [23] X. Roca-Maza, M. Centelles, F. Salvat, X. Viñas, Theoretical study of elastic electron scattering off stable and exotic nuclei, *Phys. Rev. C* 78 (2008) 044332. doi:10.1103/PhysRevC.78.044332. URL <https://link.aps.org/doi/10.1103/PhysRevC.78.044332>
- [24] J. Liu, R. Xu, J. Zhang, C. Xu, Z. Ren, Elastic electron scattering off nuclei with shape coexistence, *Journal of Physics G: Nuclear and Particle Physics* 46 (5) (2019) 055105. doi:10.1088/1361-6471/ab029a. URL <https://doi.org/10.1088/1361-6471/ab029a>
- [25] S. Brodsky, E. Chudakov, P. Hoyer, J. Laget, Photoproduction of charm near threshold, *Physics Letters B* 498 (1-2) (2001) 23–28. doi:10.1016/S0370-2693(00)01373-3. URL [http://dx.doi.org/10.1016/S0370-2693\(00\)01373-3](http://dx.doi.org/10.1016/S0370-2693(00)01373-3)
- [26] A. Ali, et al., First Measurement of Near-Threshold J/ψ Exclusive Photoproduction off the Proton, *Phys. Rev. Lett.* 123 (2019) 072001. doi:10.1103/PhysRevLett.123.072001. URL <https://link.aps.org/doi/10.1103/PhysRevLett.123.072001>
- [27] Q. Wang, X. Liu, Q. Zhao, Photoproduction of hidden charm pentaquark states $P_c^+(4380)$ and $P_c^+(4450)$, *Phys. Rev. D* 92 (2015) 034022. doi:10.1103/PhysRevD.92.034022. URL <https://link.aps.org/doi/10.1103/PhysRevD.92.034022>
- [28] A. N. H. Blin, C. Fernández-Ramírez, A. Jackura, V. Mathieu, V. I. Mokeev, A. Pilloni, A. P. Szczepaniak, Studying the $P_c(4450)$ resonance in J/ψ photoproduction off protons, *Phys. Rev. D* 94 (2016) 034002. doi:10.1103/PhysRevD.94.034002. URL <https://link.aps.org/doi/10.1103/PhysRevD.94.034002>
- [29] R. Wang, X. Chen, J. Evslin, The origin of proton mass from J/ψ photoproduction data, *Eur. Phys. J. C* 80 (6) (2020) 507. doi:10.1140/epjc/s10052-020-8057-9. URL <https://doi.org/10.1140/epjc/s10052-020-8057-9>
- [30] K. A. Mamo, I. Zahed, Diffractive Photoproduction of J/ψ and Υ using holographic QCD: Gravitational form factors and GPD of gluons in the proton, *Phys. Rev. D* 101 (2020) 086003. doi:10.1103/PhysRevD.101.086003. URL <https://link.aps.org/doi/10.1103/PhysRevD.101.086003>
- [31] Y. Hatta, D. Yang, Holographic J/ψ production near threshold and the proton mass problem, *Phys. Rev. D* 98 (2018) 074003. doi:10.1103/PhysRevD.98.074003. URL <https://link.aps.org/doi/10.1103/PhysRevD.98.074003>
- [32] R. Boussarie, Y. Hatta, QCD analysis of Near-Threshold quarkonium lepton production at large photon virtualities, *Physical Review D* 101 (11) (Jun 2020). doi:10.1103/physrevd.101.114004. URL <http://dx.doi.org/10.1103/PhysRevD.101.114004>