ACCEPTED MANUSCRIPT • OPEN ACCESS

Mechanical metamaterials for sports helmets: structural mechanics, design optimisation, and performance

To cite this article before publication: Daniel Haid et al 2023 Smart Mater. Struct. in press https://doi.org/10.1088/1361-665X/acfddf

Manuscript version: Accepted Manuscript

Accepted Manuscript is "the version of the article accepted for publication including all changes made as a result of the peer review process, and which may also include the addition to the article by IOP Publishing of a header, an article ID, a cover sheet and/or an 'Accepted Manuscript' watermark, but excluding any other editing, typesetting or other changes made by IOP Publishing and/or its licensors"

This Accepted Manuscript is © 2023 The Author(s). Published by IOP Publishing Ltd.



As the Version of Record of this article is going to be / has been published on a gold open access basis under a CC BY 4.0 licence, this Accepted Manuscript is available for reuse under a CC BY 4.0 licence immediately.

Everyone is permitted to use all or part of the original content in this article, provided that they adhere to all the terms of the licence https://creativecommons.org/licences/by/4.0

Although reasonable endeavours have been taken to obtain all necessary permissions from third parties to include their copyrighted content within this article, their full citation and copyright line may not be present in this Accepted Manuscript version. Before using any content from this article, please refer to the Version of Record on IOPscience once published for full citation and copyright details, as permissions may be required. All third party content is fully copyright protected and is not published on a gold open access basis under a CC BY licence, unless that is specifically stated in the figure caption in the Version of Record.

View the article online for updates and enhancements.

Mechanical metamaterials for sports helmets: structural mechanics, design optimisation, and performance

Daniel Haid¹, Leon Foster¹, John Hart¹, Richard Greenwald^{2,3}, Tom Allen⁴, Pooya Sareh^{5,6*}, Olly Duncan⁴

1) Advanced Wellbeing Research Centre, Sheffield Hallam University, Sheffield, UK

2) Simbex, Lebanon, New Hampshire, USA

3) Thayer School of Engineering, Dartmouth College, Hanover, New Hampshire, USA

4) Department of Engineering, Manchester Metropolitan University, Manchester, UK

5) School of Engineering, University of Liverpool, Liverpool, UK

6) School of Engineering, Newcastle University, Newcastle upon Tyne, UK

*Corresponding author: pooya.sareh@liverpool.ac.uk & pooya.sareh@newcastle.ac.uk

Abstract

Sports concussions are a public health concern. Improving helmet performance to reduce concussion risk, is a key part of the research and development community response. Direct and oblique head impacts with compliant surfaces that cause longduration moderate or high linear and rotational accelerations are associated with a high rate of clinical diagnoses of concussion. As engineered structures with unusual combinations of properties, mechanical metamaterials are being applied to sports helmets, with the goal of improving impact performance and reducing brain injury risk. Replacing established helmet material (i.e., foam) selection with a metamaterial design approach (structuring material to obtain desired properties) allows the development of near-optimal properties. Objective functions based on an up-to-date understanding of concussion, and helmet testing that is representative of actual sporting collisions and falls, could be applied to topology optimisation regimes, when designing mechanical metamaterials for helmets. Such regimes balance computational efficiency with predictive accuracy, both of which could be improved under high strains and strain rates to allow helmet modifications as knowledge of concussion develops. Researchers could also share mechanical metamaterial data, topologies, and computational models in open, homogenised repositories, to improve the efficiency of their development.

1. Introduction

Sporting concussions are prevalent and recognised as a public health concern [1–5]. Mechanical metamaterials are engineered structures with combinations of mechanical properties that are not possible in the individual materials they are made from [6–15]. They are suggested as options to improve helmet impact performance (e.g., [16–33]). In helmets, mechanical metamaterials can be tailored to reduce linear and rotational acceleration, thought to be associated with the clinical diagnosis of concussion [16–33].

Helmets are an established mechanical intervention for reducing head injury risk. They are considered effective at preventing severe head injury (e.g., skull fracture), but less so for concussion [34–42]. While there are many mechanical metamaterials reviews [14,43–49], including those on protective equipment [50,51], as well as some on general helmet materials (e.g., [52]), there is not a published review of mechanical metamaterials for sports helmets. Here, we formulate the current challenges relating to helmet development, and summarise the breadth of relevant mechanical metamaterials research. Finally, we include perspectives on opportunities and requirements for helmet development, focusing on reducing concussion risk.

Concussions can cause short-term functional impairments and long-term health problems [53,54]. They are typically considered a mild traumatic brain injury [55–57], but are part of the larger family of traumatic brain injury (TBI). Concussion injuries can be caused either by a direct blow to the head, or an impact to the body that causes head acceleration (e.g., via. whiplash) [2,58]. Symptoms of concussion, such as physical, cognitive, and emotional health, usually resolve within two weeks [2,3,53,59–61], but can last longer [62,63]. Concussions do not typically cause detectable

structural damage to the brain [2,62,64], so they are challenging to diagnose and manage.

A history of concussions [3,54,62,65] or repetitive sub-concussive head impacts [53,62,66] are associated with microstructural changes in the brain, and short or long-term functional, physiological, and neurological changes. Reported consequences include reduced quality of life [67], and increased risk of psychiatric disorders [4,53,60,66,68,69], neurodegenerative disorders [53,60,66,70], and suicide [71].

Rugby, American Football, and ice hockey have the highest concussion rates in mainstream sports [41,72]. Concussions are also of concern in other sports, including association football [73–76], lacrosse [72,77], snow-sports [34,78–82], cycling [27,83–85], water-sports [86], and rock climbing [87]. Strategies to reduce concussion risk, such as rule changes and helmet developments, have been introduced to various sports, with limited success [35,37,38,40,42,83,88,89]. There has also been notable investment by governmental agencies [90,91], and charitable organisations [92,93], in concussion research and related technology development over the past two decades.

Team sports are often played in environments that can be controlled and regulated [41,72], unlike outdoor sports such as cycling, snow-sports, water-sports, and climbing [27,34,86,87,78–85]. In many mainstream sports, strategies such as promoting helmet use have had limited effects on concussion rates [34,37,39–42,72,79,82,94]. Factors affecting reported concussion rates are multifaceted, so identifying the effect of interventions is challenging.

Risk factors for concussion include impact surface shape and stiffness, and impact speed, energy, direction, and location [35,37,38,40,42,83,88,89,95]. Ice hockey presents an interesting case for helmet development, as it includes various diverse impact types (e.g., high-speed puck, rigid ice and boards, and collisions between players and their equipment – which are considered compliant) [96,97]. The

introduction and regulation of ice hockey helmets have helped to nearly eliminate serious head injuries, particularly skull fractures [37,38]. Despite these developments, and as with other mainstream sports [37,39–42,72], concussion rates in ice hockey have been steadily increasing [37,39–42,72]. Most ice hockey concussions (93%) are caused by collisions between players (i.e., compliant surfaces) [37,63,88,96–99], while the remaining 7% are from falls onto ice [97]. About two-thirds of players indicate they would continue to play even if they thought they had sustained a concussion [100]. This attitude to concussion likely results in underreporting [37,39,41,101].

There is an ongoing debate over different possible concussion mechanisms [89,102–105]. It is generally agreed that the clinical condition resulting from an injury associated with diagnosed concussion is caused by excessive, or overly rapid, tissue deformation [102]. Such tissue deformation can be caused by skull deformation [89,106,107], movement of the brain within it [102,104,106,108], and by pressure gradients [106]. Most closed head injuries (non-fracture) follow head accelerations that damage brain tissue [104,109–112]. During linear (radial) impacts, injury can be caused by the brain being forced against the faster-moving skull [89,113,114]. During head rotation, loose coupling can damage connective blood vessels and neurons [102,104,106,114]. Linear and rotational head accelerations are likely to be present during head impacts [103,110,115,116], and helmets should aim to limit both.

2. Measures of concussion risk

Helmets are typically designed to decrease the various measures thought to contribute to head injury risk. Peak linear acceleration (PLA) is thought to contribute to severe injuries such as skull fractures, and concussions [109,115,117–121]. The Wayne State Tolerance Curve (WSTC), derived from animal and cadaver tests, combined linear acceleration and duration when assessing injury risk [122,123].

Further threshold curves (e.g., Gadd severity index [124] and head injury criterion (HIC) [125]) integrate acceleration over a portion of the impact duration, with a weighting factor for high accelerations [95,109,125–142].

Peak rotational acceleration (and velocity) are commonly considered as measures of concussion risk [109,120,127,137,143–156]. Various measures of head injury risk use rotational kinematics (e.g., the Rotational Injury Criterion [157] and Brain Injury Criterion (BrIC) [158,159]). The Generalized Acceleration Model for Brain Injury Tolerance (GAMBIT) [160] and Head Impact Power (HIP) [161–163] combine linear and rotational kinematics, while the weighted Principal Component Score (wPCS) also includes impact location [55,164].

Numerical brain trauma models have been developed (e.g., [114,165–168]). These models use measured kinematics as input variables to predict brain deformation metrics, such as principal strain, cumulative strain damage, or pressure [169–172]. Modelling the material properties of the brain is challenging, and care must be taken to ensure meaningful results [173].

In-field measurements with sensors, following validation (typically against video footage), can detect and characterise actual sporting head impacts [73,174]. These sensors can be attached to the skin [73,175–178] or helmet [73,176,179–184] or embedded within mouthguards [73,185–188]. Collected sensor data, along with subsequent clinical diagnosis, are helping to develop our understanding of concussion [73,174], as are mechanical tests [189,190], numerical simulations [173], and measurements from cadaver [191] and animal testing [192]. Findings form such work indicate benefits to (i) minimising peak linear and rotational accelerations; (ii) minimising the duration over which these values remain elevated; and (iii) shifting focus from PLA to also include rotational kinematics and duration. These measures, thought to increase concussion risk, are associated with impacts with compliant bodies, such

as collisions between ice hockey players [37,63,88,96–99]. Validated test methods, representative of conditions in the field of play, as well as brain models and biofidelic headforms [193,194], help further our understanding of concussion mechanisms.

3. Helmet Testing

There are many reviews on helmet testing, and Whyte et al's is particularly comprehensive [95]. As such, only key points related to helmet development are summarised here. Helmets are typically fitted to a headform when tested [95]. Most helmets certification tests within standards include a drop test onto a fixed anvil [126–130,132,195–217], with some exceptions [126–130,201]. None of these tests cover the full range of impact types a helmet may experience during use [95,143,190,218,219]. Certification tests within helmet standards are typically designed to ensure a minimum level of protection from a severe head impact (e.g., skull fracture, rather than concussion) [95].

Standards typically use centric impact vectors [126,127,196,198,200,214–216,220–222], and a rigid anvil [95,218,223]. Tests using non-centric impact vectors are more common in research publications than in standards, following growing recognition that few actual sporting collisions and falls cause centric impact vectors (e.g., [143–145,170,224–229]). Such non-centric impact vectors can be imparted using drop tests onto oblique anvils (e.g., [32,179,230,231]), pneumatic rams [151,190,225,232], pendulums and impulse hammers [77,153,227–229,233,234], or projectiles [235].

Energy is the typical metric used to classify impact tests and is usually between 18 and 150 J (depending on the sport [95]). Where rigid anvils are used for testing, energies may be lower than those expected during actual sporting collisions and falls, with a view to maintaining similar severities, and acceleration vs. time profiles, to actual

collisions and falls [190,228,230]. Wider ranges of impact velocities, energies, and anvil compliances are used in research studies than in standards [85,95,189,230,235]. Measures of magnitude, and sometimes duration, of linear and rotational acceleration, are used to define injury risk (to prevent varying helmet mass from affecting perceived performance). As covered in Section 2, there is ongoing discussion around the acceleration magnitudes and time profiles that are associated with clinical diagnosis of concussion, which should be resolved before updating standards [95]. As such, metrics are often compared to in-field measures for actual sporting collisions and falls, and those collected with an un-helmeted headform [190,227–230].

Various standardised headforms, with limited biofidelity [95,235–242], are used to test helmets [95,235–245]. Attempts have been made to use low friction covers to improve the biofidelity of the headform and helmet interface, with clear differences in rotational acceleration [32,136,246,247]. Attempts have also been made to develop more biofidelic headforms [193,194]. Neckforms [145,153,167,170,179,223,224,240,247–250], including biofidelic ones [95,143,146,156,219,239,251–255], are sometimes attached to headforms to achieve more realistic post-impact behaviour.

Sports concussions are typically caused by impacts with compliant surfaces [37,63,88,96–99], inducing long-duration impacts (noted as high risk in Section 2). These compliant surfaces may also increase friction, and rotational head acceleration, during oblique impacts [189,190] thought to cause concussion. Such oblique impacts with compliant surfaces are not tested for in certification tests within standards and are rarely used in peer-reviewed studies on new helmet technologies. Further, headforms with low biofidelity may cause unrealistic coupling with the helmet, potentially introducing errors while measuring rotational kinematics in the laboratory [32,136,246,247]. Mechanical metamaterials, offering greater control over effective

properties than conventional materials, could be used in helmet development efforts focused on reducing measures of concussion risk, while maintaining protection against skull fracture.

4. Helmet Design

4.1. Established Concepts

The idealised goal of impact protective equipment is to absorb induced impact energies without exceeding measures associated with injury risk. For a consistent impact scenario, like a certification test, the selection process for an energy-absorbing material is established. The challenge with helmets is the diverse variety of impact scenarios. There are various helmet designs available for different sports [35,36,218], with two main categories. The first category is single-impact helmets, which crush under impact and are designed to protect the head against one severe (high energy) impact. These include motorsports, cycling, and alpine sports helmets. After such an impact, these helmets should be replaced as they are damaged, and offer limited protection [35,218]. The other category is multi-impact helmets, which are designed to maintain their impact performance over a (typically) long service life, e.g., several years. These are used for American Football, ice hockey, and lacrosse [35,218], to name a few.

Helmets typically have at least three layers. A stiff (polymer or composite) outer shell (Figure 1 (A)) prevents penetration [35,36,84,218,256,257], absorbs the initial shock [84,258], and helps to hold the helmet together during or after an impact [84]. A compressible foam, or lattice, liner absorbs energy through deformation (Figure 1, [218,257]). Most single-impact helmets, particularly those for cycling, use crushable, expanded polystyrene (EPS) foam [36,259]. Vinyl nitrile (VN) (Figure 1 (A)) and expanded polypropylene (EPP) (Figure 1 (B)), are often used in multi-impact helmets

[35,151,260–262]. Many helmets also include a comfort liner, often a compliant foam [263], as shown in Figure 1 (A). New materials and components are also being added to helmets, generally intended to exceed minimum requirements in certification tests (e.g., [30,31,33,264–270]).



Figure 1: (**A**) VN foam, (**B**) EPP foam and slip plane, and (**C**) a shear-thickening polymer (STP) pad as parts of an ice hockey helmet liner. (authors' own image)

Inspecting example compressive stress (σ) vs. strain (ϵ) relationships (Figure 2), the area under the curve is the energy absorbed per unit volume (W, [271]). The compressive stress vs. strain relationships of cellular materials, such as foams, can often be divided into three sections: (i) linear elasticity, up to ~5% strain; (ii) plateau, elastic or plastic buckling of the cell walls; and (iii) densification, where cell walls self-contact and the constituent material is compressed [271].

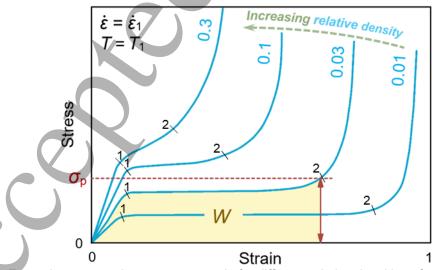


Figure 2: Example compression stress vs. strain for different relative densities of a foam at equal strain rates (arbitrarily using engineering strain values for simplicity). Area W under the curve illustrates the absorbed energy. The start (1) and end (2) of the stress plateau are marked for each foam.

Energy absorption efficiency (W/ σ) is highest during the plateau region [272], which can be tailored by modifying the constituent material or foam relative density [271]. An ideal foam for a given impact (e.g., curve 0.03 in Figure 2) absorbs the induced energy during the plateau region, without densifying [35,271]. Energy absorption before densification increases with liner thickness. However, overly large helmets are uncomfortable [35,271] and can increase rotational accelerations by increasing torque applied to the head [35]. As such, helmet liner thickness is generally limited. So, combining layers of foam of varying relative density, and hence stiffness, may broaden the range of manageable impacts, but will give lower maximal efficiency [36,273].

4.2. Emerging Developments

Various approaches have been taken to make helmets more effective over a wider range of impacts. Shear-thickening fluids (STFs) and polymers (STPs) are non-Newtonian (Figure 3). The viscosity of these materials increases with shear strain rate [274–277]. STFs include suspensions [274] and gels [278], while STPs (which are more commonly used in consumer products) are viscoelastic solids [276,277,279]. STPs adapt to impact severity [280,281]; they can be flexible and elastic during normal use and minor impacts, or stiffen and increase damping during severe impacts [274,282]. The viscosity change is reversible, providing an alternative to crushable foam over multiple impacts [283,284], with slow recovery potentially reducing rebound, impact duration, and various measures of injury risk [125,133–136]. So, foamed STPs are used in PPE [274,276,278,280], including helmets liners (Figure 1 (C)) [34], or without foaming as a structure to reduce rotational kinematics [18,25].

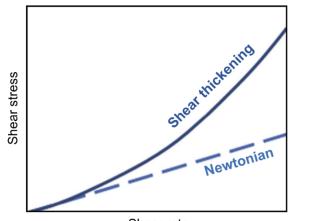




Figure 3: Behaviour of Newtonian and shear-thickening fluids (where gradient increase with shear rate).

A low-friction layer, placed between the helmet's liner and shell (Figure 2 (B), [21,285]), or between layers of foam [266], allows relative rotation between components. This relative rotation has been shown to reduce the rotational kinematics of headforms during oblique impact tests [32,231,246,285–289]. A well-known example of this technology is the multi-directional impact protection system (MIPS) [265]. The inclusion of anisotropic helmet liners has also been shown to reduce rotational acceleration during certain oblique impacts [19–21,290]. Such liners may have fibrous columns [21], or elongated cells [20], making them stiff through thickness but transversely compliant, lowering shear stiffness [291,292]. Salomon's EPS 4D helmet liner uses a similar principal, whereby columns of EPS foam appear to be designed to shear during oblique impacts [269]. These examples are relatively standard, using conventional materials and manufacturing methods.

Patents have been filed featuring concepts related to the application of mechanical metamaterials in helmets. These include helmets, or helmet liners, based on structured polymers such as lattices (e.g., [293–298]), sprung/suspended inserts (e.g., [299]), modular/custom fit structured components (e.g., [300,301]), foamed/structured shear thickening materials (e.g., [302,303]), bulk shear thickening

materials (e.g., [304]), and fluidic properties (e.g., [305,306]). Many of these innovations feature in commercially available helmets (e.g., [30,31,264,270]).

5. Mechanical Metamaterials

Mechanical metamaterials can be made in various ways and have unique properties that could improve sport helmet performance. They can be fabricated from conventional materials such as foam [307,308] or textiles [51,309], or designed as periodical/graded cellular structures [12–14,310]. Mechanical metamaterials can also be made from sheets of material by folding (known as origami) [311–328], or by folding, cutting, and joining (known as kirigami) [17,329–345]. With high levels of control over end properties – given the additional degrees of design freedom afforded by controlling topology and base material – mechanical metamaterials are well suited to addressing complex engineering problems, like impact protection [17,50,263]. The common forms of unusual properties in mechanical properties are auxetic (negative Poisson's ratio) behaviour (covered extensively in various reviews [46,50,308,310,346,347] and textbooks [309,348,349]), negative stiffness [350–357], shape morphing [338,358–360], force/torque coupling [361–365], active/adaptive behaviour [352,366–368], or programmable properties that are tuned to a specific application [17,26,28,342,362].

5.1. Auxetic Metamaterials

Poisson's Ratio is the negative product of the ratio of lateral to axial strain. Auxetic materials undergo transverse expansion when stretched axially, and contract transversely in compression [11,286,307]. So, they form a dome shape under bending, and are used in a helmet liner for this reason (i.e., flat sheets can fit into domed helmets [32,264]).

Poisson's ratio (v) is one of the basic elastic constants, and (with Young's modulus/stiffness) affects shear modulus, bulk modulus, and indentation resistance

[369]. As detailed elsewhere [369], Poisson's ratio increases resistance to penetration by concentrated loads [370–374], and shear modulus [375–379]. The increased tendency of materials with a low or negative Poisson's ratio to deform volumetrically, rather than in shear (Figure 4), may also increase strength. With lower shear strain, the likelihood of failure close to a crack tip, or an ellipsoid, reduces, according to Von-Mises, Tresca, and crack propagation theories [380,381]. Without the presence of stress concentrations caused by a crack or ellipsoid, Von-Mises and Tresca criterion are unaffected [369]. So, auxetic helmet sections may fail less readily, reducing waste and severe head injury risk.

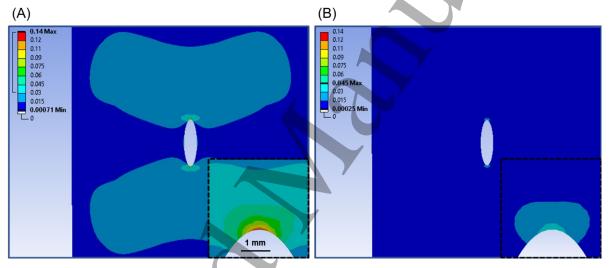


Figure 4: Contour plots of maximum shear (engineering) strain in 100 × 100 mm thin plates loaded parallel to the short axis of a 5 × 20 mm central ellipsoidal hole, with arbitrary, equal tensile loads and moduli, but Poisson's ratios of (**A**) 0.5 and (**B**) –0.5. Static structural simulations were undertaken in Ansys Mechanical.

The re-entrant-like cellular structure of auxetic foams is imparted by compressing conventional foam to buckle cell ribs [308,382,383]. So, while there is some uncertainty over whether these foams meet the requirement for the precisely defined topology of some metamaterial definitions [7–9], they are still a related medium. Readers interested in auxetic foam manufacturing are referred to Jiang et al.'s recent review [308]. Auxetic foams have been shown to increase vibration damping [384,385], and to exhibit peak impact forces up to ten times lower than their conventional counterparts [292,386–390]. It should be noted that peak force during the 13

typically stiff anvil and impactor impacts is not a scalar measure. Indeed, peak force increases exponentially as the foam densifies (see Figure 2) and "bottoms out" under impact. Further, auxetic foams made from expanded helmet foam have not been reported.

Auxetics may provide benefits in helmet liners: i) The ability to adapt to the shape of impacting bodies – remaining soft when impacting a relatively flat surface, but effectively stiffening under concentrated loads. ii) High vibration damping, redistributing vibrations transversely. iii) A tendency to bulk over shear deformation, reducing the likelihood of failure. Conversely, the early densification strain caused by the tendency to bulk deformation may shorten the stress vs. strain plateau in cellular solids – causing densification at lower strain ([292], Figure 2). With the ability to include a stiff shell, the benefit of the high indentation resistance possible for auxetics is unclear and has not been empirically demonstrated in helmets. Flexible shell helmets (e.g., [228,229]) may, however, benefit from the increased indentation resistance of auxetic materials. Further, the increase in shear modulus with negative Poisson's ratio goes against the broad strategy of reducing liner shear stiffness to reduce rotational acceleration [25,32,264,265,285,287–289]. So, the application of auxetic materials in helmet liners requires careful design based on justifiable benefits, such as increasing indentation resistance to facilitate lower stiffness liners.

An unstudied, potentially useful topic is auxetic helmet shells. Fibre-polymer composites can be auxetic, with the negative Poisson's ratio achieved by fibre alignment [391,392]. Due to the use of conventional fibres and pre-preg, auxetic fibre-polymer composites can be made with standard composite manufacturing methods [393]. These auxetic composites have been shown to resist back face damage under impacts [394]. Such increased resistance to back face damage could increase the

lifespan of multi-impact helmets featuring composite shells, particularly those with flat sections that are more susceptible to back face damage.

5.2. Periodic Structures

Advances in additive manufacturing, and moulding methods [25], have allowed mass production of lattice and honeycomb mechanical metamaterials (e.g., [31,33,264,395,396]). These methods allow precise manufacturing of complex geometries [16,397–399], expanding the range of available properties to meet complex requirements, such as those seen in helmets. 2D extruded cellular structures, such as honeycombs (Figure 5 (A)), repeat periodically in two directions [400]. Honeycomb and tubular structures are studied frequently as energy-absorbing elements in sports equipment and helmets [23,401–405], such as in Koroyd's helmet liner [31]. 3D periodic cellular structures, such as lattices, consist of unit cells repeating in three directions, increasing degrees of freedom during design, but also increasing manufacturing complexity and hence costs [397,399,400,406–411].

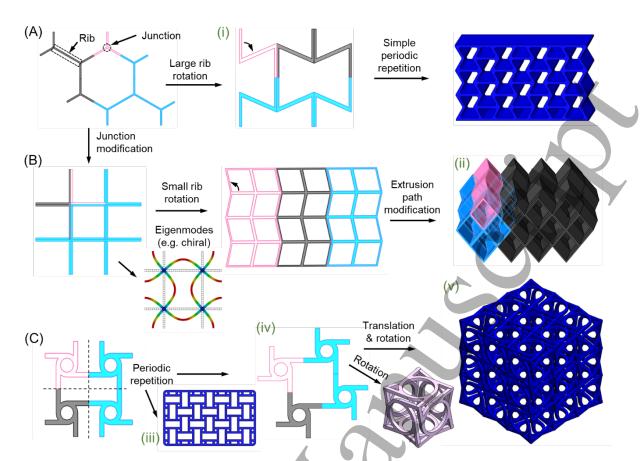


Figure 5: Some notable mechanical metamaterial design degrees of freedom: (**A**) Honeycombs, with large angle rib modifications, becoming (i) re-entrant. (**B**) Quadrilateral honeycomb, with Eigenmode rib tessellation to form an auxetic unit cell, or small rib rotations and extrusion path modification, forming a (ii) Miura-ori inspired metamaterial. (**C**) Various periodic rotational and translational repetitions of a chiral unit cell, forming iii) antitheoretical, iv) 2D chiral and v) 3D chiral metamaterials. Pink wireframe notes the simplest repeating unit cell, subsequent repetitions are shown in grey or blue.

Exemplary unit cell designs include hexagonal/re-entrant (Figure 5 (A)) [412,413]), square/cubic (Figure 5 (B)) [414]), or chiral/antichiral (Figure 5 (C)) [415–419]. Unit cell design degrees of freedom include; i) varying rib orientation (Figure 5 (A) & (B)), length, or thickness – slender ribs are often less stiff; varying rib form (Figure 5 (B) – Eigenmode example); varying the number of ribs (Figure 5 (A) & (B)), or adding and combining shapes and features (Figure 5 (C)). Unit cell patterning also affects topology, and so metamaterial properties; unit cells can be mirrored (Figure 5 (A - i) & (C)), linearly repeated (Figure 5 (A), (B) & (C - iii)), or rotated (Figure 5 (C - v)).

When creating honeycombs, some variation can be applied in the extruded direction, as is the case of Miura-ori-inspired structures (Figure 5 (B - ii)) [420,421]. Gradient metamaterials can also be developed by spatially varying unit cell parameters

and properties [404,405,422,423]. These variations can be continuous or discrete (i.e., gradual or abrupt change) [424–426]. 3D periodic cellular structures are being used in helmets (e.g., ice hockey [33] and American Football [395]). Such liners, or inserts, can also feature some through thickness variation, and can be made from STPs [30].

Concerning some common topologies, hexagonal honeycombs are relatively stiff, with low density, for compression parallel to their extruded dimension [404,427–430]. During impacts in the extruded direction, cell walls crumple and buckle [31,428], with densification occurring at ~75% compression [404]. When impacted or compressed perpendicular to their extruded dimensions, honeycomb stiffness is lower [28,404,429,431,432]. Re-entrant hexagonal honeycombs can be more compliant than equivalent density regular hexagonal ones (at low strains), due to the extra junction for rib hinging to occur around [425,431,433,434]. Buckling may not occur with these re-entrant unit cells, causing an almost linear compressive stress vs. strain response, i.e., a less pronounced plateau and densification region [370,425,431]. Such re-entrant unit cells may not be optimal within a target impact severity (e.g., as in Figure 2), but are less prone to stark peak force increases during severe impacts [29,292,387]. It is possible to design tall, slender stiff re-entrant cells that undergo buckling [272,424].

Structures made of solid rotating shapes are often stiff in compression, as the internal shapes undergo self-contact/densification at low strains, making them less studied for sporting impacts [435–438]. These rotating shapes have been made as lattices with hollow cells [439], or cut from foams, to tune out of plane properties while relying on foam characteristics through thickness [440,441]. High energy absorption, low initial crushing peak forces, large densification strain, and low strain rate sensitivity can be achieved with folded (kirigami or origami) structures [333,334,336,442,443]. By including such folds through the thickness of these structures, it is possible to tune buckling regions, and the length of the compressive stress plateau [17] (Figure 2).

Kirigami structures made from paper have been used in a recyclable cycling helmet [444].

For application in helmets, periodic structures must be patterned to fill an often complex/nearly spherical space. Such patterning, using conventional computer-aided design software, can be time-consuming and inefficient. Algorithmic-based design software, such as those marketed by nTopology [445], Hyperganic [446], or Rhino3d [447] can make the process of generating such geometries more efficient. Noting that impact vectors are usually non-centric, further challenges arise. Where there are enough unit cells, the response at various angles can be calculated based on orthotropic, strain-dependent properties, using standard elasticitv tensor transformation [425,448,449]. So, response to off-axis impacts can be designed by tuning the out-of-plane properties. Where there are too few unit cells to homogenise the material properties, as is often the case for periodic structures, the off-axis response must be obtained by higher order material approximations [450], microstructurally faithful simulations [25], or experimentally [25,32].

5.3. Force Torque Coupling

Advances in fabrication methods have allowed realisation of a wider range of unusual and potentially beneficial properties than auxetic behaviour. Mechanical metamaterials with force-torque coupling (known herein as twist) have seen increasing interest, since their rational design was shown in 2017 [364]. Like (negative) Poisson's ratio, twist translates axial deformation to transverse deformation – increasing resistance to indentation [361]. So, twisting mechanical metamaterials may resist penetration by concentrated loads, without shortening the stress plateau under compression (as seen for auxetics – see Section 5.1).

The development of these metamaterials could also facilitate more efficient analysis and design of lattices. The twisting response is not included in classical

(Cauchy) continuum mechanics, but it is in micro-morphic continuum mechanics (where a uniform load causes internal strain gradients [450]). Eringen presented some special cases in micro-morphic theories [450]. These include micropolar - where the gradients occur by rotation of rigid unit cells (sand provides an intuitive example), and micro-stretch - where the gradients occur by unit cell rotation and volume change, without shape change (picture the bronchi). Each of these allows some simplification (over the micro-morphic continuum) – reducing the amount of information required to approximate the response of a metamaterial – but may also cause some loss in precision.

Clearly, in the case of foams and lattices, which have relatively large internal features (when compared to the scale of external loads), micro-morphic continuum theories often apply [361,451,452]. Where classical continuum theories cannot be used, typical approaches to designing mechanical metamaterials for impact protection are experimental, or by using microstructurally faithful numerical models [17,26,28,29,417,418,421,453], which are less efficient. So, developing and applying these micro-morphic continuum theories, including their viscoelastic and visco-plastic formulations, could facilitate more efficient mechanical metamaterial analysis, design, and application in single or multi-impact helmets [450].

5.4. Negative Stiffness

Snap-through elements cause negative stiffness behaviour, corresponding to a drop in force as applied deformation increases [350–356]. Negative stiffness can be achieved by the buckling of an end constrained/preconditioned beam (Figure 6). The beam snaps from one state of equilibrium to the next following the application of a perpendicular load (often via a connecting rib) [350,351,356]. The negative stiffness region is present for a segment of the force vs. compression relationship,

corresponding to when the beam snaps through (Figure 6 (E)). Increasing the diagonal angle of the symmetric beam (φ , Figure 6 (B)) increases the onset, and length, of the region [354]. Decreasing the slenderness ratio of the beam increases the critical buckling load and hence the magnitude of both positive and negative stiffness [354]. Negative stiffness has been shown to improve protection during impacts [454], balancing the positive stiffness of neighbouring unit cells to flatten and elongate the stress plateau (Figure 2). Designing and manufacturing relatively unstable negative stiffness inclusions within helmets could bring added complexity, and further work applying these concepts to helmets is needed.

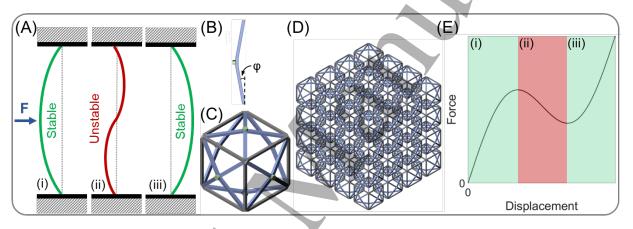


Figure 6 (**A**) Stages of snap through in a buckling beam, and direction of applied force. (**B**) Snap through element. (**C**) Inclusion in a cubic unit cell and (**D**) metamaterial, recreated from ref [354]. (**E**) Example force displacement (arbitrary values), including stages from (A).

5.5. Topology Optimisation

Precise control over topology allows the design of a desired response to various loading conditions. An efficient approach to topology optimisation is to optimise a unit cell, and homogenise (expand to an effective bulk material) using a set of boundary conditions (i.e., periodic symmetry [453,455–460]). Readers interested in homogenisation theory could refer to refs [461–463]. Such an approach is not widely applied during sporting impacts, causing high strains and strain rates, meaning degrees of freedom surrounding unit cell boundaries are influential and challenging to predict. For example, end loading for buckling beams, such as cell ribs, can vary with

neighbouring cell deformation, meaning a multi-cell optimisation is needed [464–466]. Instead, whole metamaterial samples are often optimised or iteratively improved [17,22,26,32]. Developing and applying micro-morphic theories [450] to lattices under impact may facilitate the prediction of rib constraints, and efficient (unit-cell) topology optimisation [467]. Open data approaches (such as the meta-genome [468]) could help develop these new homogenisation methods.

5.6. Adaptive Metamaterials

While shear thickening polymers can adapt their stiffness to various collision types, more degrees of design freedom, such as deformation mode switching, are possible. Deformation mode switching can be achieved by including an adaptive material, such as a viscoelastic one, that activates a topological instability [14]. For example, a beam's buckling mode (direction) can be designed to switch at a given strain rate. When two laterally connected beams of different stiffness (i.e., bi-beams) are compressed (Figure 7 (A)), the stiffer one drives the buckling direction while the other provides support, causing buckling towards the stiffer side. So, in Figure 7 (A), the deformation direction will switch at the strain rate when the viscoelastic beam becomes stiffer than the hyperplastic one. Bi-beams positioned like those in Figure 7 (A) will buckle away from each other at low compression rates, and towards each other, stiffening via self-contact, at higher compression rates. Negative causing viscoelasticity can also be achieved with such a system of bi-beams [366], if the order in Figure 7 (A) is reversed, so bi-beams effectively soften by buckling away from each other at high compression rates. Obtaining negative viscoelasticity with highly viscoelastic materials demonstrates the level of control available via topology that could be useful when designing helmets. The response, of these bi-beams, while previously shown to be retained for off-axis deformation angles of $\sim 10^{\circ}$ [366], is unknown during oblique impacts. Flexing of the beams may provide a desirable low shear modulus, as in similar tests of long-cell anisotropic foam liners [20,290], and should be studied further.

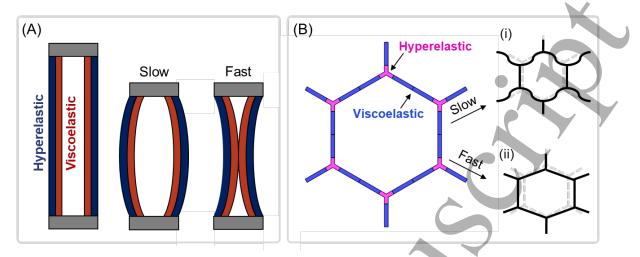


Figure 7 (**A**) Single bi-beam design and buckling direction for different axial compressive strain rates. (**B**) Multi-material hexagonal cell causing a switch in the dominant deformation mode.

Less dimensionally unstable adaptive metamaterial systems can also be designed. The dominant deformation mode in hexagonal honeycombs and lattices is cell rib flexure [431,449] (Figure 7 (B - i)). Such flexure reduces the distance to the neighbouring junction, reducing the magnitude of positive compressive Poisson's ratios, or increasing that of negative Poisson's ratio. Placing viscoelastic material in the cell ribs could switch the dominant mode, increasing the magnitude of positive Poisson's ratio, and hardness [369], during more severe impacts (Figure 7 (B - ii)). Conversely, placing viscoelastic material in the junction of auxetic, re-entrant honeycombs or lattices could have a similar effect, by amplifying the dominance of rib flexure to draw neighbouring junctions inward. These concepts have been demonstrated using dual materials of different stiffness, but not viscoelastic ones, and present notable options for future research, particularly related to applications in helmets [469,470]. Interestingly, such switching mechanisms and changes to Poisson's ratio can be achieved with one material, based on local changes in strain rate and stiffness; shifting the point of deformation [471–473].

The use of embedded electronics as adaptive mechanisms is emerging [14,474,475]. These include piezoelectric inclusions, which stiffen when an electrical field is applied [474], or embedded electromagnets [353]. Such systems allow a controlled response, with the potential for embedded electronics to environmental changes, like impact severity or strain rate, fall initiation, temperature or relative humidity, and micro-controllers to define a programmed response or adaption [14,474,475]. Challenges to application are associated with the manufacture of sufficiently small and robust components [14,353].

6. Discussion

Some commercial, or mid- to high- technology readiness level mechanical metamaterials, show promise to reduce concussion risk when applied to helmets [18,21,25,30,32,264–266,395]. Separately, these metamaterials appear to have sufficient degrees of freedom to reduce shear and compressive response, and rotational and linear measures (e.g., [18,21,395,25,30,32,264–266,269,285]), reduce the duration of high accelerations via crushable or viscoelastic liners (e.g., [18,25,30–32,264,395]), and adapt to surface compliance, or impact severity, via rate dependency (e.g., [18,30,267]). For commercial helmets [30–33,264–267,269,285], independent, peer-reviewed, analysis of such functions is rarely published. These systems, along with ref [18], have demonstrated commercial viability of mechanical metamaterials (e.g., use of single material injection moulding or additive manufacturing). So, they reduce barriers to entry and raise awareness, facilitating continuous improvements and further application of mechanical metamaterials. Table 1 summarises the key mechanical metamaterial types covered in this review.

| 2 |
|----------|
| 3 |
| |
| 4 |
| 5 |
| 6 |
| 7 |
| , 8 |
| |
| 9 |
| 10 |
| 11 |
| |
| 12 |
| 13 |
| 14 |
| 15 |
| 16 |
| |
| 17 |
| 18 |
| 19 |
| 20 |
| |
| 21 |
| 22 |
| 23 |
| 24 |
| |
| 25 |
| 26 |
| 27 |
| 28 |
| 20 |
| |
| 30 |
| 31 |
| 32 |
| |
| |
| 34 |
| 35 |
| 36 |
| 37 |
| |
| 38 |
| 39 |
| 40 |
| |
| 41 |
| 42 |
| 43 |
| 44 |
| 45 |
| |
| 46 |
| 47 |
| 48 |
| 49 |
| |
| 50 |
| 51 |
| 52 |
| 53 |
| 55 |
| |
| 55 |
| 56 |
| 57 |
| 58 |
| 58 59 |
| 59 |

1

| Metamaterial | Potential Benefit | Potential Application | Challenges | |
|---------------------------|--|--|--|--|
| Periodic structures | Tuneable response | Compliant/crushable liners | Efficient design and manufacturing, particularly during non-centric impacts | |
| | Domed curvature | Helmet liner manufacturing solution | Already established | |
| Auxetics | High indentation resistance | Compliant/crushable liners, particularly of soft-shell helmets | Early densification, and increased shear modulus | |
| | High toughness | Compliant/crushable liners | Making crushable auxetic foam | |
| | | Helmet shells, particularly fibre-polymer composites | Demonstrating the requirement | |
| Force-torque coupling | High indentation resistance | Compliant/crushable liners, particularly of soft-shell helmets | Cannot be simulated as bulk solids using the Cauchy continua | |
| Negative stiffness | Extension of stress vs. strain plateau region | Compliant liners | Cost-effective design of such unstable mechanisms | |
| Adaptive metamaterials | Improved performance across various impact types | Compliant liners | Cost-effective manufacture and design – often featuring multiple materials deformation mechanisms | |

With the greater degrees of freedom afforded when designing mechanical metamaterials come some additional challenges. Firstly, metamaterials can be more expensive to manufacture than established helmet materials, so currently tend to only be used in high-end helmets [30,31,33,264,270]. Secondly, the effect of increasing, or changing, the pool of materials used in helmet design needs to be considered; particularly susceptibility to environmental considerations such as temperature, relative humidity, contaminants, and ultra-violet radiation [476]. Conversely, the greater design affordances associated with mechanical metamaterials could reduce susceptibility to environmental to achieve the required performance using only materials that resist degradation due to environmental conditions. The sports market may again be an important early adopter; providing long term, in-field (user) testing in variable environments before uptake by more conservative sectors such as aerospace.

Peer-reviewed publications noting tests of new helmet technologies rarely use biofidelic anthropomorphic test dummy heads or necks, nor impacts onto compliant anvils. Unrealistic coupling between helmet and head may affect rotational accelerations [32,136,246,247], while impacts with compliant surfaces are amongst the most common causes of sporting concussion [37,63,88,96–99]. Mechanical metamaterial design streams that reflect these high injury risk scenarios could be developed, to ensure they are designed and implemented in helmets based on up-to-date measures of concussion risk. An extensive range of mechanical metamaterial properties has been demonstrated (e.g., [18,21,25,32,285]), so such design steams appear feasible. Funding calls, challenges, and open data approaches that promote collaborations and knowledge exchange between groups with state-of-the-art test methods, and those developing helmets, could be beneficial. Such initiatives could be sport specific (e.g., [477]), or broader (e.g., [90–93,468]).

A metamaterials approach to helmet design: unit cell optimisation and patterning, based on an objective function of measures of concussion risk and manufacturing constraints, could be used to improve helmet impact performance [458,464]. Such an approach requires some form of rate dependency or adaption, justifying research developing ranges of viscoelastic materials for additive manufacturing. We note two forms of unusual property that are of prominent interest in helmet development: (1) negative stiffness inclusions, to extend or flatten the stress plateau (Figure 6), and (2) adaptive metamaterials (Figure 7). Switching of deformation mechanisms may provide options to increase rate dependence without the presence of extreme viscoelasticity. Efficient topology optimisation for such systems also requires some development, to apply periodic constraints that reflect rib buckling with single/minimal unit cells [458,464]. With such methods, helmet manufacturers could

adapt to developing knowledge of concussions, or design affordances offered by new manufacturing methods.

7. Conclusions

Mechanical metamaterial design affords degrees of freedom that could allow helmets with impact response that adapts between severe impacts that cause skull fracture and those that might lead to clinically diagnosed concussion. The objective functions that mechanical metamaterial helmet liners are designed or optimised for could be modified, by testing and refining the designed helmets on biofidelic headforms under representative test conditions. As such, efforts encouraging collaborations between those developing helmets, mechanical metamaterials, and test methods, could improve helmets. Epidemiological studies may help identify the effect of such interventions over time. Improving the efficiency and availability of topology optimisation tools at high strains and strain rates, would allow helmets to be updated as knowledge of concussion improves. Here, open data and opensource software initiatives will be beneficial. To increase options for mechanisms of adaption to impact severity, researchers could focus on increasing options to print or mould viscoelastic materials or developing topological approaches to tune effective viscoelasticity.

Conflict of interest statement

Dr Greenwald is the founder of Simbex, Lebanon, New Hampshire, USA, and is involved in the development of head impact exposure monitoring technology used commercially by Riddell, Inc. All other authors declare no conflict of interest.

Author contributions

Mr Haid drafted the review, while Drs Duncan, Allen, Sareh, and Greenwald edited it. Drs Hart and Foster provided feedback.

References

- 1. Concussion in sport inquiry. (**2021**) [accessed 2023 Apr 6]. https://committees.parliament.uk/work/977/concussion-in-sport/
- 2. McCrory P., Meeuwisse W., Dvořák J., Aubry M., Bailes J., Broglio S., et al. Consensus statement on concussion in sport—the 5th international conference on concussion in sport held in Berlin, October 2016. Br. J. Sports Med. **(2017)**.51(11). 838–47.
- 3. Harmon K.G., Clugston J.R., Dec K., Hainline B., Herring S.A., Kane S., et al. American Medical Society for Sports Medicine Position Statement on Concussion in Sport. Clin. J. Sport Med. (2019).29(2). 87–100.
- 4. Guskiewicz K.M., Marshall S.W., Bailes J., Mccrea M., Harding H.P., Matthews A., et al. Recurrent concussion and risk of depression in retired professional football players. Med. Sci. Sports Exerc. (2007).39(6). 903–9.
- 5. Moreland G., Barkley L.C. Concussion in Sport. Curr. Sports Med. Rep. (2021).20(4). 181–2.
- 6. Dancer C. What are metamaterials? (**2023**) [accessed 2023 Mar 27]. https://metamaterials.network/what-are-metamaterials/
- 7. Nature. Mechanical Metamaterials Collection. (2022) [accessed 2022 Aug 2]. https://www.nature.com/collections/iebdeffddc/
- 8. Boardman A. Pioneers in metamaterials: John Pendry and Victor Veselago. J. Opt. **(2011)**.13(2).
 - 9. Pendry J. Beyond metamaterials. Nat. Mater. (2006).5(10). 763-4.
 - 10. Ball P. Bending the laws of optics with metamaterials: an interview with John Pendry. Natl. Sci. Rev. (2018).5(2). 200–2.
 - 11. Pendry J.B. Negative refraction makes a perfect lens. Phys. Rev. Lett. **(2000)**.85(18). 3966–9.
 - 12. Barchiesi E., Spagnuolo M., Placidi L. Mechanical metamaterials: a state of the art. Math. Mech. Solids. (2019).24(1). 212–34.
 - 13. Surjadi J.U., Gao L., Du H., Li X., Xiong X., Fang N.X., et al. Mechanical Metamaterials and Their Engineering Applications. Adv. Eng. Mater. **(2019)**.21(3). 1–37.
- 14. Zadpoor A.A. Mechanical meta-materials. Mater. Horizons. (2016).3(5). 371–81.
- 15. Lee J.H., Singer J.P., Thomas E.L. Micro-/nanostructured mechanical metamaterials. Adv. Mater. (**2012**).24(36). 4782–810.
- 16. Soe S., Ryan M., McShane G., Theobald P. Energy absorption characteristics of additively manufactured TPE cellular structures. Second Int. Conf. Sustain. Des. Manuf. (2015). 145–58.
- 17. Townsend S., Adams R., Robinson M., Hanna B., Theobald P. 3D printed origami honeycombs with tailored out-of-plane energy absorption behavior. Mater. Des. (2020).195. 108930.
- La Fauci G., Parisi M., Nanni A., Crosetta L., Pugno N.M., Colonna M. Design and proofof-concept of an advanced protective system for the dissipation of tangential impact energy in helmets, based on non-Newtonian fluids. Smart Mater. Struct. (2023).32(4). 044004.
- 19. Mosleh Y., Cajka M., Depreitere B., Vander Sloten J., Ivens J. Designing safer composite helmets to reduce rotational accelerations during oblique impacts. Proc. Inst. Mech. Eng. Part H J. Eng. Med. (2018).232(5). 479–91.
- Vanden Bosche K., Mosleh Y., Depreitere B., Vander Sloten J., Verpoest I., Ivens J. Anisotropic polyethersulfone foam for bicycle helmet liners to reduce rotational acceleration during oblique impact. Proc. Inst. Mech. Eng. Part H J. Eng. Med. (2017).231(9). 1–11.
- 21. Mosleh Y., Cajka M., Depreitere B., Ivens J., Sloten J. Vander. Smart material and design solutions for protective headgears in linear and oblique impacts: column/matrix composite liner to mitigate rotational accelerations. Smart Mater. Struct. (2023).32(1).
- 22. Krishnan, B. R., Biswas, A. N., Kumar, K. A., & Sreekanth, P. R. Auxetic structure metamaterial for crash safety of sports helmet. Materials Today: Proceedings (**2022**). 56, 1043-1049.

- 23. Khosroshahi S.F., Tsampas S.A., Galvanetto U. Feasibility study on the use of a hierarchical lattice architecture for helmet liners. Mater. Today Commun. (2018).14(February). 312–23.
 - 24. Khosroshahi S.F., Yin X., Donat C.K., Mcgarry A., Lopez M.Y., Baxan N., et al. Multiscale modelling of cerebrovascular injury reveals the role of vascular anatomy and parenchymal shear stresses. Sci. Rep. (2021). 1–13. https://doi.org/10.1038/s41598-021-92371-0
 - 25. Siegkas P., Sharp D.J., Ghajari M. The traumatic brain injury mitigation effects of a new viscoelastic add-on liner. Sci. Rep. **(2019)**.9(1). 1–10.
 - 26. Hanna B., Adams R., Townsend S., Robinson M., Soe S., Stewart M., et al. Auxetic Metamaterial Optimisation for Head Impact Mitigation in American Football. Int. J. Impact Eng. (2021).157. 103991.
 - 27. Soe S.P., Martin P., Jones M., Robinson M., Theobald P. Feasibility of optimising bicycle helmet design safety through the use of additive manufactured TPE cellular structures. Int. J. Adv. Manuf. Technol. **(2015)**.79(9–12). 1975–82.
 - 28. Adams R., Townsend S., Soe S., Theobald P. Finite element-based optimisation of an elastomeric honeycomb for impact mitigation in helmet liners. Int. J. Mech. Sci. (2022).214(August 2021). 106920.
 - 29. Shepherd T., Allen T., Winwood K., Venkatraman P.D., Alderson A. Validation of a Finite Element Modelling Process for Auxetic Structures under Impact. Phys. Status Solidi B Basic Solid State Phys. (2020).1900197.
 - 30. Rheon, Xenith. Shadow XR. [accessed 2023 Apr 6]. https://rheonlabs.com/rheontechnology-products/shadow-xr/
 - 31. Koroyd. Koroyd Impact Protection. (2020).

- 32. Bliven E., Rouhier A., Tsai S., Willinger R., Bourdet N., Deck C., et al. Evaluation of a novel bicycle helmet concept in oblique impact testing. Accid. Anal. Prev. (2019).124(December 2018). 58–65.
- 33. 2020 Carbon I. Carbon3D CCM Super Tacks X. (**2020**) [accessed 2023 Mar 13]. https://www.carbon3d.com/resources/blog/ccm-super-tacks-x/
- 34. Bailly N., Laporte J.D., Afquir S., Masson C., Donnadieu T., Delay J.B., et al. Effect of Helmet Use on Traumatic Brain Injuries and Other Head Injuries in Alpine Sport. Wilderness Environ. Med. (2018).29(2). 151–8.
- 35. Hoshizaki T.B., Brien S.E., Bailes J.E., Maroon J.C., Kaye A.H., Cantu R.C. The science and design of head protection in sport. Neurosurgery. (2004).55(4). 956–67.
- 36. Piland S.G., Gould T.E., Jesunathadas M., Wiggins J.S., McNair O., Caswell S. V. Protective helmets in sports. Elsevier Ltd; (**2019**).pp.71–121p.
- 37. Pauelsen M., Nyberg G., Tegner C., Tegner Y. Concussion in ice hockey A cohort study across 29 seasons. Clin. J. Sport Med. (2017).27(3). 283–7.
- 38. Beaver W. Concussion in the NHL: A Case Study. J. Contemp. Athl. (2018).12(2). 123– 38.
- 39. Adams R., Li A.Y., Dai J.B., Haider S., Lau G.K., Cheung K.P., et al. Modifying Factors for Concussion Incidence and Severity in the 2013-2017 National Hockey League Seasons. Cureus. (2018).10(10).
- 40. Prien A., Grafe A., Rössler R., Junge A., Verhagen E. Epidemiology of Head Injuries Focusing on Concussions in Team Contact Sports: A Systematic Review. Sport. Med. (2018).48(4). 953–69.
- 41. Nezwek T.A., Lee C.S. Concussion in the NHL : Where Do We Stand ? J. Orthop. Res. Ther. (2016).2016(2). 3–5.
- 42. Kuhn A.W., Solomon G.S. Concussion in the National Hockey League: a systematic review of the literature. Concussion. **(2016)**.1(1).
- 43. Lakes R.S. Negative-Poisson's-Ratio Materials: Auxetic Solids. Annu. Rev. Mater. Res. (2017).47. 63–81.
- 44. Ren X., Das R., Tran P., Ngo T.D., Xie Y.M. Auxetic metamaterials and structures: a review. Smart Mater. Struct. **(2018)**.27. 023001.
 - 45. Wu Y., Lai Y., Zhang Z.Q. Elastic metamaterials with simultaneously negative effective

| 1 | | |
|----------|-----|--|
| 2 | | |
| 3 | | shear modulus and mass density. Phys. Rev. Lett. (2011) .107(10). 1–5. |
| 4 | 46. | Evans K.E., Alderson A. Auxetic materials: Functional materials and structures from |
| 5 | | lateral thinking! Adv. Mater. (2000) .12(9). 617–28. |
| 6 7 | 47. | Kelkar P.U., Kim H.S., Cho K.H., Kwak J.Y., Kang C.Y., Song H.C. Cellular auxetic |
| 7 | | structures for mechanical metamaterials: A review. Sensors. (2020).20(11). 1–26. |
| 8 9 | 48. | Lakes R.S. Composites and Metamaterials. World Scientific; (2020). |
| 9 10 | 49. | Lim TC. Mechanics of Metamaterials with Negative Parameters. Singapore: Springer |
| 11 | | Nature; (2020). |
| 12 | 50. | Duncan O., Shepherd T., Moroney C., Foster L., Venkatraman P.D., Winwood K., et al. |
| 13 | | Review of auxetic materials for sports applications: Expanding options in comfort and |
| 14 | | protection. Appl. Sci. (2018).8(6). |
| 15 | 51. | Tahir D., Zhang M., Hu H. Auxetic Materials for Personal Protection: A Review. Phys. |
| 16 | | Status Solidi Basic Res. (2022).259(12). 1–13. |
| 17 | 52. | Singh O., Kumar Behera B. Review: a developmental perspective on protective |
| 18 | | helmets. J. Mater. Sci. (2023). |
| 19 | 53. | McAllister T., McCrea M. Long-Term cognitive and neuropsychiatric consequences of |
| 20 | | repetitive concussion and head-impact exposure. J. Athl. Train. (2017).52(3). 309–17. |
| 21 | 54. | Bailes J.E., Petraglia A. I., Omalu B. i., Nauman E., Talavage T. Role of subconcussion |
| 22 | | in repetitve mild brain injury. J. Neurosurg. (2013).119(November). 1235–45. |
| 23 | 55. | Greenwald R.M., Gwin J.T., Chu J.J., Crisco J.J. Head Impact Severity Measures for |
| 24 | | Evaluating Mild Traumatic Brain Injury Risk Exposure. Neurosurgery. (2008).62(4). |
| 25 | | 789–98. |
| 26 | 56. | Rowson S., Duma S.M. Brain injury prediction: Assessing the combined probability of |
| 27 | | concussion using linear and rotational head acceleration. Ann. Biomed. Eng. |
| 28 | | (2013).41(5). 873–82. |
| 29 30 | 57. | Patton D.A., McIntosh A.S., Kleiven S. The biomechanical determinants of concussion: |
| 30 31 | | Finite element simulations to investigate brain tissue deformations during sporting |
| 32 | | impacts to the unprotected head. J. Appl. Biomech. (2015).31(4). 264-8. |
| 33 | 58. | Carroll L.J., Cassidy J.D., Holm L., Kraus J., Coronado V.G. Methodological issues and |
| 34 | | research recommendations for mild traumatic brain injury: The WHO Collaborating |
| 35 | | Centre Task Force on Mild Traumatic Brain Injury. J. Rehabil. Med. Suppl. (2004).(43). |
| 36 | | 113–25. |
| 37 | 59. | Ferry B., Alexei D. Concussion. (2022). pp. 1–8. |
| 38 | 60. | Jordan B.D. The clinical spectrum of sport-related traumatic brain injury. Nat. Rev. |
| 39 | | Neurol. (2013).9(4). 222–30. |
| 40 | 61. | Marshall C.M. Sports-related concussion: A narrative review of the literature. J. Can. |
| 41 | | Chiropr. Assoc. (2012).56(4). 299–310. |
| 42 | 62. | Choe M.C. The Pathophysiology of Concussion. Curr. Pain Headache Rep. |
| 43 | | (2016).20(6). |
| 44 | 63. | Tator C.H., Blanchet V., Ma J. Persisting Concussion Symptoms from Bodychecking: |
| 45 | | Unrecognized Toll in Boys' Ice Hockey. Can. J. Neurol. Sci. (2022). 1–9. |
| 46 | 64. | Signoretti S., Lazzarino G., Tavazzi B., Vagnozzi R. The pathophysiology of concussion. |
| 47 | | PM R. (2011).3(10 SUPPL. 2). 359–68. |
| 48 40 | 65. | Mainwaring L., Ferdinand Pennock K.M., Mylabathula S., Alavie B.Z. Subconcussive |
| 49 50 | | head impacts in sport: A systematic review of the evidence. Int. J. Psychophysiol. |
| 50 51 | | (2018).132(January). 39–54. |
| 52 | 66. | Manley G., Gardner A.J., Schneider K.J., Guskiewicz K.M., Bailes J., Cantu R.C., et al. |
| 53 | | A systematic review of potential long-term effects of sport-related concussion. Br. J. |
| 55 | | Sports Med. (2017).51(12). 969–77. |
| 55 | 67. | Gard A., Lehto N., Engström Å., Shahim P., Zetterberg H., Blennow K., et al. Quality of |
| 56 | (| life of ice hockey players after retirement due to concussions. Concussion. (2020).5(3). |
| 57 | 68. | Gouttebarge V., Kerkhoffs G.M.M.J. Sports career-related concussion and mental |
| 58 | | health symptoms in former elite athletes. Neurochirurgie. (2021).67(3). 280-2. |
| 59 | 69. | Chrisman S.P.D., Richardson L.P. Prevalence of diagnosed depression in adolescents |
| 60 | | with history of concussion. J. Adolesc. Heal. (2014).54(5). 582–6. |
| | | |
| | | |

- 70. Mez J., Daneshvar D.H., Kiernan P.T., Abdolmohammadi B., Alvarez V.E., Huber B.R., et al. Clinicopathological evaluation of chronic traumatic encephalopathy in players of American football. JAMA J. Am. Med. Assoc. **(2017)**.318(4). 360–70.
- 71. Fralick M., Thiruchelvam D., Tien H., Redelmeier D. Risk of suicide after a concussion. C. 2016. **(2016)**.188(7). 497–504.
- Van Pelt K.L., Puetz T., Swallow J., Lapointe A.P., Broglio S.P. Data-Driven Risk Classification of Concussion Rates: A Systematic Review and Meta-Analysis. Sport. Med. (2021).51(6). 1227–44.
- 73. O'Connor K.L., Rowson S., Duma S.M., Broglio S.P. Head-impact-measurement devices: A systematic review. J. Athl. Train. (2017).52(3). 206–27.
- 74. Kawata K., Tierney R., Phillips J., Jeka J.J. Effect of Repetitive Sub-concussive Head Impacts on Ocular Near Point of Convergence. Int. J. Sports Med. **(2016)**.37(5). 405– 10.
- 75. Dunn M., Davies D., Hart J. Effect of Football Size and Mass in Youth Football Head Impacts. Proc. 13th Conf. Int. Sport. Eng. Assoc. **(2020)**.49(29).
- Parr J.V. V, Uiga L., Marshall B., Wood G. Soccer heading immediately alters brain function and brain-muscle communication. Front. Hum. Neurosci. (2023).17(1145700). 1–10.
- 77. Oeur R.A., Zanetti K., Hoshizaki T.B. Angular acceleration responses of American football, lacrosse and ice hockey helmets subject to low-energy impacts. 2014 IRCOBI Conf. Proc. Int. Res. Counc. Biomech. Inj. **(2014)**. 81–92.
- 78. Dickson T.J., Trathen S., Waddington G., Terwiel F.A., Baltis D. A human factors approach to snowsport safety: Novel research on pediatric participants' behaviors and head injury risk. Appl. Ergon. (2016).53. 79–86. http://dx.doi.org/10.1016/j.apergo.2015.08.006
- 79. Dickson T.J., Trathen S., Terwiel F.A., Waddington G., Adams R. Head injury trends and helmet use in skiers and snowboarders in Western Canada , 2008 2009 to 2012 2013 : an ecological study. **(2017)**. 236–44.
- 80. Dickson T.J., Waddington G., Terwiel F.A. Snowsport experience, expertise, lower limb injury and somatosensory ability. J. Sci. Med. Sport. (2018). 6–10.
- 81. Dickson T.J., Forsdyke S., James S. Terrain park participants ' perceptions of contributing factors in injury events and risk management suggestions. J. Outdoor Recreat. Tour. (2021).35(July). 100416.
- 82. Dickson T.J., Terwiel F.A. Head injury and helmet usage trends for alpine skiers and snowboard in western Canada during the decade 2008-9 to 2017-18. J. Sci. Med. Sport. (2020).
- 83. A. Shaw J. A Review of the Incidence of Head Injuries in Football, Baseball, Ice Hockey, and Cycling. Am. J. Sport. Sci. (2019).7(1). 1.
- 84. Leng B., Ruan D., Tse K.M. Recent bicycle helmet designs and directions for future research: A comprehensive review from material and structural mechanics aspects. Int. J. Impact Eng. **(2022)**.168(July). 104317.
- 85. Bland M.L., McNally C., Rowson S. Differences in Impact Performance of Bicycle Helmets during Oblique Impacts. J. Biomech. Eng. **(2018)**.140(9). 20–3.
- 86. Scher I.S., Stepan L.L., Hoover R.W. Head and neck injury potential during water sports falls: examining the effects of helmets. Sport. Eng. **(2020)**.23(1). 1–10.
- 87. Begonia M., Rowson B., Scicli B., Goff J.E. Laboratory evaluation of climbing helmets: assessment of linear acceleration. Smart Mater. Struct. **(2023)**.32(3).
- 88. Anderson G.R., Melugin H.P., Stuart M.J. Epidemiology of Injuries in Ice Hockey. Sports Health. **(2019)**.11(6). 514–9.
- 89. Hardy W.N., Mason M.J., Foster C.D., Shah C.S., Kopacz J.M., Yang K.H., et al. A study of the response of the human cadaver head to impact. Stapp Car Crash J. (2007).51. 17–80.
- 90. Mott M., Koroshetz W. Concussion research at the National Institutes of Health: An update from the National Institute of Neurological Disorders and Stroke. Concussion. **(2016)**.1(2). 8–11.

| 1 | |
|----------|--|
| 2 3 | |
| 4 | |
| 5 | |
| 6 | |
| 7 | |
| 8 | |
| 9 10 | |
| 11 | |
| 12 | |
| 13 | |
| 14 | |
| 15 16 | |
| 17 | |
| 18 | |
| 19 | |
| 20 | |
| 21 22 | |
| 23 | |
| 24 | |
| 25 | |
| 26 27 | |
| 27 28 | |
| 29 | |
| 30 | |
| 31 22 | |
| 32 33 | |
| 34 | |
| 35 | |
| 36 | |
| 37 38 | |
| 39 | |
| 40 | |
| 41 | |
| 42 | |
| 43 44 | |
| 45 | |
| 46 | |
| 47 | |
| 48 49 | |
| 49 50 | |
| 51 | |
| 52 | |
| 53 | |
| 54 55 | |
| 55 56 | |
| 57 | |
| 58 | |
| 59 | |
| 60 | |

- 91. Hicks K. Department of Defense Warfighter Brain Health Initiative. (**2022**) [accessed 2023 May 5]. https://media.defense.gov/2022/Aug/24/2003063181/-1/-1/0/DOD-WARFIGHTER-BRAIN-HEALTH-INITIATIVE-STRATEGY-AND-ACTION-PLAN.PDF
 - 92. The Concussion Foundation. (**2022**) [accessed 2023 Apr 19]. https://theconcussionfoundation.org/
 - 93. Brain Research UK. (**2023**) [accessed 2023 Apr 20]. https://www.brainresearchuk.org.uk/research/apply
 - 94. O'Reilly M., Mahon S., Reid D., Hume P., Hardaker N., Theadom A. Knowledge, attitudes, and behavior toward concussion in adult cyclists. Brain Inj. (2020).34(9). 1175–82. https://doi.org/10.1080/02699052.2020.1793386
- 95. Whyte T., Stuart C.A., Mallory A., Ghajari M., Plant D.J., Siegmund G.P., et al. A review of impact testing methods for headgear in sports: Considerations for improved prevention of head injury through research and standards. J. Biomech. Eng. (2019).141(7).
- 96. Hutchison M.G., Comper P., Meeuwisse W.H., Echemendia R.J. A systematic video analysis of National Hockey League (NHL) concussions, part I: Who, when, where and what? Br. J. Sports Med. (2015).49(8). 547–51.
- 97. Hutchison M.G., Comper P., Meeuwisse W.H., Echemendia R.J. A systematic video analysis of National Hockey League (NHL) concussions, part II: How concussions occur in the NHL. Br. J. Sports Med. **(2015)**.49(8). 552–5.
- 98. Robidoux M.A., Kendall M., Laflamme Y., Post A., Karton C., Hoshizaki T.B. Comparing concussion rates as reported by hockey Canada with head contact events as observed across minor ice-hockey age categories. J. Concussion. (2020).4. 205970022091128.
- Van Pelt K.L., Caccese J.B., Eckner J.T., Putukian M., Brooks M.A., Cameron K.L., et al. Detailed description of Division I ice hockey concussions: Findings from the NCAA and Department of Defense CARE Consortium. J. Sport Heal. Sci. (2021).10(2). 162– 71.
- 100. Hutchinson S., Ellison P., Levy A., Marchant D. Knowledge and attitudes towards concussion in UK-based male ice hockey players: A need for attitude change? Int. J. Sport. Sci. Coach. (2019).14(2). 153–61.
- 101. Williamson I.J.S., Goodman D. Converging evidence for the under-reporting of concussions in youth ice hockey. Br. J. Sports Med. (2006).40(2). 128–32.
- 102. Post A., Hoshizaki T.B. Mechanisms of brain impact injuries and their prediction: A review. Trauma. **(2012)**.14(4). 327–49.
- 103. King A.I., Yang K.H., Zhang L., Hardy W. Is head injury caused by linear or angular acceleration? Proc. Int. Res. Conf. Biomech. Impacts. (2003).(September). 1–12.
- 104. Bayly P. V., Cohen T.S., Leister E.P., Ajo D., Leuthardt E.C., Genin G.M. Deformation of the human brain induced by mild acceleration. J. Neurotrauma. (2005).22(8). 845–56.
- Zhang L., Yang K.H., King A.I. Biomechanics of neurotrauma. Neurol. Res. (2001).23(2– 3). 144–56.
- 106. Hardy W.N., Khalil T.B., King A.I. Literature review of head injury biomechanics. Int. J. Impact Eng. (1994).15(4). 561–86.
- 107. Thomas L.M., Roberts V.L., Gurdjian E.S. Impact-induced pressure gradients along three orthogonal axes in the human skull. J. Neurosurg. (1967).26(3). 316–21.
- 108. Kleiven S. Influence of impact direction on the human head in prediction of subdural hematoma. J. Neurotrauma. (2003).20(4). 365–79.
- 109. Pellman E.J., Viano D.C., Withnall C., Shewchenko N., Bir C.A., Halstead P.D. Concussion in professional football: Helmet testing to assess impact performance Part 11. Neurosurgery. **(2006)**.58(1). 78–95.
- 110. Zhang J., Yoganandan N., Pintar F.A., Gennarelli T.A. Role of translational and rotational accelerations on brain strain in lateral head impact. Tech. Pap. ISA. **(2006)**.464(May 2014). 501–6.
- 111. Thomas L.M., Roberts V.L., Gurdjian E.S. Experimental intracranial pressure gradients in the human skull. J. Neurol. Neurosurg. Psychiatry. **(1966)**.29(5). 404–11.

- 112. Post A., Hoshizaki T.B., Karton C., Clark J.M., Dawson L., Cournoyer J., et al. The biomechanics of concussion for ice hockey head impact events. Comput. Methods Biomech. Biomed. Engin. **(2019)**.22(6). 631–43.
- Hardy W.N., Foster C.D., Mason M.J., Yang K.H., King A., Tashman S. Investigation of Head Injury Mechanisms Using Neutral Density Technology and. Stapp Car Crash J. (2001).45(November).
- 114. Gilchrist M.D., O'Donoghue D. Simulation of the development of frontal head impact injury. Comput. Mech. (2000).26(3). 229–35.
- Zhang L., Yang K.H., King A.I. A Proposed Injury Threshold for Mild Traumatic Brain Injury. J. Biomech. Eng. (2004).126(2). 226–36.
- 116. Bandak F.A., Eppinger R.H. A three-dimensional finite element analysis of the human brain under combined rotational and translational accelerations. SAE Tech. Pap. (1994).103. 1708–26.
- 117. Funk J.R., Duma S.M., Manoogian S.J., Rowson S. Biomechanical Risk Estimates for Mild Traumatic Brain Injury. 51st Annu. Proc. Assoc. Adv. Automot. Med. **(2007)**.1(1). 343–61.
- 118. Denny-Brown D., R. R.W. Experimental Cerebral Concussion. Brain. (1941).64(2). 93– 164.
- 119. Gurdjian E.S., Roberts V.L., Thomas M. Tolerance Curves of Acceleration and Intracranial Pressure and Protective Index in Experimental Head Injury. J. Trauma. (1966).6(5). 600–4.
- 120. Ono K., Kikuchi A., Nakamura M., Kobayashi H., Nakamura N. Human head tolerance to sagittal impact reliable estimation deduced from experimental head injury using subhuman primates and human cadaver skulls. SAE Tech. Pap. (1980). 101–60.
- 121. Ommaya A.K., Hirsch A.E., Flamm E.S., Mahone R.H. Cerebral Concussion in the Monkey: An Experimental Model. Science (80-.). (1966).153(3732). 211–3.
- 122. Lissner H.R., Lebow M., Evans F.G. Experimental studies on the relation between acceleration and intracranial pressure changes in man. Surgery, Gynecol. Obstet. (1960).111. 329–38.
- 123. Gurdjian E.S., Lissner H.R., Latimer F.R., Haddad B.F., Webster J.E. Quantitative determination of acceleration and intracranial pressure in experimental head injury; preliminary report. Neurology. (1953).3(6), 417–23.
- 124. Gadd C.W. Use of a weighted-impulse criterion for estimating injury hazard. SAE Tech. Pap. (1966).No. 660793. 95–100.
- 125. Hutchinson J., Kaiser M.J., Lankarani H.M. The Head Injury Criterion (HIC) functional. Appl. Math. Comput. (1998).96(1), 1–16.
- 126. NOCSAE DOC (ND) 030 11m16, 2016, "Standard Performance Specification for Newly Manufactured Ice Hockey Helmets", National Operating Committee on Standards for Athletic Equipment.
- 127. NOCSAE DOC (ND) 002-17m19a, 2019, "Standard Performance Specification for Newly Manufactured Football Helmets", National Operating Committee on Standards for Athletic Equipment.
- 128. NOCSAE DOC (ND) 022-21,2021, "Standard Performance Specification for Newly Manufactured Baseball/Softball Batter's Helmets", National Operating Committee on Standards for Athletic Equipment.
- 129. NOCSAE DOC (ND) 024-21, "Standard Performance Specification for Newly Manufactured Baseball/Softball Catcher's Helmets with Faceguard", National Operating Committee on Standards for Athletic Equipmen.
- 130. NOCSAE DOC (ND) 029-21, 2021, "Standard Performance Specification for Newly Manufactured Baseball/Softball Fielder's Headgear", National Operating Committee on Standards for Athletic Equipment.
- 131. NOCSAE DOC (ND) 050-11m19, 2019, "Standard Performance Specification for Newly Manufactured Polo Helmets", National Operating Committee on Standards for Atletic Equipment.
- 132. NOCSAE DOC (ND) 041- 15m18, 2018, "Standard Performance Specification for Newly

| 1 | |
|----------|--|
| 2 | |
| 3 | |
| 4 | |
| 5 | |
| 6 | |
| 7 | |
| 8 | |
| 9 | |
| 10 | |
| 11 | |
| 12 | |
| 13 | |
| 14 | |
| 15 | |
| 16 | |
| 17 | |
| 18 | |
| 18 19 | |
| | |
| 20 | |
| 21 | |
| 22 | |
| 23 | |
| 24 | |
| 25 | |
| 26 | |
| 27 | |
| 28 | |
| 29 | |
| 30 | |
| 31 | |
| 32 | |
| 33 | |
| 34 | |
| 35 | |
| 36 | |
| 37 | |
| 38 | |
| 39 | |
| | |
| 40 | |
| 41 | |
| 42 | |
| 43 | |
| 44 | |
| 45 | |
| 46 | |
| 47 | |
| 48 | |
| 49 | |
| 50 | |
| 51 | |
| 52 | |
| 53 | |
| 54 | |
| 55 | |
| 56 | |
| 57 | |
| 57 58 | |
| 10 | |

60

Manufactures Lacrosse Helmets With Faceguard", National Operating Committee on Standards for Athletic Equipment.

- 133. Versace J. A Review of the Severity Index. SAE Tech. Pap. 15th Stapp Car Crash Conf. (1971).
- 134. Jorgensen J.K., Thoreson A.R., Stuart M.B., Loyd A., Smith A.M., Twardowski C., et al. Interpreting oblique impact data from an accelerometer-instrumented ice hockey helmet. Proc. Inst. Mech. Eng. Part P J. Sport. Eng. Technol. (2017).231(4). 307–16.
- 135. Richards D., Ivarsson B.J., Scher I., Hoover R., Rodowicz K., Cripton P. Ice hockey shoulder pad design and the effect on head response during shoulder-to-head impacts. Sport. Biomech. (2016).15(4). 385–96.
- Pellman E.J., Viano D.C., Tucker A.M., Casson I.R., Waeckerle J.F. Concussion in Professional Football: Reconstruction of Game Impacts and Injuries. Neurosurgery. (2003).53(4). 799–814.
- 137. Rousseau P., Hoshizaki T.B. The influence of deflection and neck compliance on the impact dynamics of a Hybrid III headform. Proc. Inst. Mech. Eng. Part P J. Sport. Eng. Technol. (2009).223(3). 89–97.
- Carlson S., Zerpa C., Pryzsucha E., Liu M., Sanzo P., Bay T. Energy Measures Across Hockey Helmet Impact Locations. In: ISBS Proceedings Archive 371. (2019). pp. 443– 6.
- 139. Johnson G.I. A comparison of results on helmet impact testing. J. Test. Eval. (2003).31(1). 79–90.
- 140. Pennock B., Kivi D., Zerpa C. Effect of Neck Strength on Simulated Head Impacts During Falls in Female Ice Hockey Players. Int. J. Exerc. Sci. (2021).14(1). 446–61.
- Zerpa C., Carlson S., Przysucha E., Liu M., Sanzo P. Evaluating the Performance of a Hockey Helmet in Mitigating Concussion Risk Using Measures of Acceleration and Energy During Simulated Free Fall. Int. J. Extrem. Autom. Connect. Healthc. (2021).3(2). 33–50.
- 142. NOCSAE DOC (ND) 022-20, 2020, "Standard Performance Specification for Newly Manufactured Baseball/Softball Batter's Helmets", National Operating Committee on Standards for Athletic Equipment.
- 143. Clark J.M., Post A., Hoshizaki T.B., Gilchrist M.D. Protective Capacity of Ice Hockey Helmets against Different Impact Events. Ann. Biomed. Eng. (2016).44(12). 3693–704.
- 144. de Grau S., Post A., Hoshizaki T.B., Gilchrist M.D. Effects of surface compliance on the dynamic response and strains sustained by a player's helmeted head during ice hockey impacts. Proc. Inst. Mech. Eng. Part P J. Sport. Eng. Technol. (2019).
- 145. Kendall M., Post A., Gilchrist M.D. A Comparison of dynamic impact response and brain deformation metrics within the cerebrum of head impact reconstructions representing three mechanisms of head injury in ice hockey. IRCOBI Conf. 2012. (2012). 12–4.
- Michio Clark J., Post A., Blaine Hoshizaki T., Gilchrist M.D. Distribution of brain strain in the cerebrum for laboratory impacts to ice hockey goaltender masks. J. Biomech. Eng. (2018).140(12). 1–10.
- 147. Ommaya A.K., Hirsch A.E., Martinez J.L. The Role of Whiplash in Cerebral Concussion. SAE Tech. Pap. (1966).
- 148. Gennarelli T.A., Thibault L.E. Biomechanics of acute subdural hematoma. J. Trauma. (1982).22(8). 680–6.
- 149. Unterharnscheidt F.J. Translational versus Rotational Acceleration-Animal Experiments with Measured Input. Scand. J. Rehabil. Med. (1971).4. 24–6.
- 150. Pincemaille Y., Trosseille X., MacK P., Tarrière C., Breton F., Renault B. Some new data related to human tolerance obtained from volunteer boxers. SAE Tech. Pap. (1989).98. 1752–65.
- 151. Rousseau P., Post A., Hoshizaki T.B. The effects of impact management materials in ice hockey helmets on head injury criteria. Proc. Inst. Mech. Eng. Part P J. Sport. Eng. Technol. **(2009)**.223(4). 159–65.
- 152. Rousseau P., Hoshizaki T.B., Gilchrist M.D. For ASTM F-08: Protective capacity of ice hockey player helmets against puck impacts. Mech. Concussion Sport. (2014). 196–

207.

- 153. Giacomazzi A., Smith T., Kersey R. Analysis of the impact performance of ICE hockey helmets using two different test methodologies. J. ASTM Int. (2009).6(4). 1–7.
- 154. Kendall M., Post A., Rousseau P., Hoshizaki T.B. The effect of shoulder pad design on reducing peak resultant linear and rotational acceleration in shoulder-to-head impacts. Mech. Concussion Sport. **(2014)**. 142–52.
- 155. Post A., Karton C., Hoshizaki T.B., Gilchrist M.D. Analysis of the protective capacity of ice hockey helmets in a concussion injury reconstruction. 2014 IRCOBI Conf. Proc. Int. Res. Counc. Biomech. Inj. (2014). 72–80.
- 156. Clark J.M., Post A., Hoshizaki T.B., Gilchrist M.D. Determining the relationship between linear and rotational acceleration and MPS for different magnitudes of classified brain injury risk in ice hockey. In: 2015 IRCOBI Conference Proceedings. (**2015**).
- 157. Kimpara H., Iwamoto M. Mild traumatic brain injury predictors based on angular accelerations during impacts. Ann. Biomed. Eng. **(2012)**.40(1). 114–26.
- 158. Takhounts E.G., Hasija V., Ridella S.A., Rowson S., Duma S.M. Kinematic Rotational Brain Injury Criterion (BRIC). In: Proceedings of the 22nd enhanced safety of vehicles conference Paper no 11-0263. (**2011**).
- 159. Takhounts E.G., Craig M.J., Moorhouse K., McFadden J., Hasija V. Development of Brain Injury Criteria (BrIC). SAE Tech. Pap. **(2013)**.2013-Novem(November). 243–66.
- 160. Newman J.A. A generalized acceleration model for brain injury threshold (GAMBIT). Proc. Int. IRCOBI Conf. (1986).
- Newman J., Barr C., Beusenberg M., Fournier E., Shewchenko N., Welbourne E., et al. a New Biomechanical Assessment of Mild Traumatic Brain Injury. Proc. 2000 Int. Conf. Biomech. Impact. (1995).108(2). 223–33.
- 162. Newman J.A., Shewchenko N. A Proposed New Biomechanical Head Injury Assessment Function - The Maximum Power Index. In: 44th Stapp Car Crash Conference (SAE Technical Papers). (**2000**).
- 163. Fréchède B., McIntosh A.S. Numerical reconstruction of real-life concussive football impacts. Med. Sci. Sports Exerc. (2009).41(2), 390–8.
- 164. Beckwith J., Chu J., Crisco J., Mcallister T.W., Duma S., Brolinson P., et al. Severity of head impacts resulting in mild traumatic brain injury. Am. Soc. (2009).(January). 4–5. http://www.asbweb.org/conferences/2009/pdf/1144.pdf
- 165. Gilchrist M.D., O'Donoghue D., Horgan T.J. A two-dimensional analysis of the biomechanics of frontal and occipital head impact injuries. Int. J. Crashworthiness. (2001).6(2). 253–62.
- 166. Gilchrist M.D. Modelling and accident reconstruction of head impact injuries. Key Eng. Mater. (2003).245–246. 417–30.
- 167. Knowles B.M., Dennison C.R. Predicting Cumulative and Maximum Brain Strain Measures From HybridIII Head Kinematics: A Combined Laboratory Study and Post-Hoc Regression Analysis. Ann. Biomed. Eng. (2017).45(9). 2146–58.
- 168. Ouckama R., Pearsall D.J. Projectile impact testing of ice hockey helmets: Headform kinematics and dynamic measurement of localized pressure distribution. 2014 IRCOBI Conf. Proc. Int. Res. Counc. Biomech. Inj. (2014).(September). 62–71.
- 169. Willinger R., Deck C., Halldin P., Otte D. Towards advanced bicycle helmet test methods. Int. Cycl. Saf. Conf. (2014).(November). 1–11.
- 170. Post A., Oeur A., Hoshizaki B., Gilchrist M.D. Examination of the relationship between peak linear and angular accelerations to brain deformation metrics in hockey helmet impacts. Comput. Methods Biomech. Biomed. Engin. **(2013)**.16(5). 511–9.
- 171. Post A., Dawson L., Hoshizaki T.B., Gilchrist M.D., Cusimano M.D. The influence of impact source on variables associated with strain for impacts in ice hockey. Comput. Methods Biomech. Biomed. Engin. **(2019)**.22(7). 713–26.
- 172. Gabler L.F., Crandall J.R., Panzer M.B. Development of a Second-Order System for Rapid Estimation of Maximum Brain Strain. Ann. Biomed. Eng. **(2019)**.47(9). 1971–81.
- 173. Ji S., Ghajari M., Mao H., Kraft, Reuben H., Hajiaghamemar M., Panzer M.B., et al. Use of brain biomechanical models for monitoring impact exposure in contact sports. Ann.

| 1 2 | |
|----------------------|-----------------|
| 3 4 5 | 174 |
| 6 7 8 | 175 |
| 9 10 | 176 |
| 11 12 13 | 177 |
| 14 15 16 | 178 |
| 17 18 19 20 | 179 |
| 21 22 | 180 |
| 23 24 25 | 18 ⁻ |
| 26 27 | |
| 28 29 20 | 182 |
| 30 31 32 | 183 |
| 33 34 35 | 184 |
| 36 37 38 | 185 |
| 39 40 41 | 186 |
| 42 43 44 45 | 187 |
| 45 46 47 48 | 188 |
| 49 50 | 189 |
| 51 52 53 | 190 |
| 54 55 56 | 19 ⁻ |
| 57 58 59 60 | 192 |
| | |

Biomed. Eng. (2022).50. 1389–1408.

- 174. Patton D.A., Huber C.M., Jain D., Myers R.K., McDonald C.C., Margulies S.S., et al. Head Impact Sensor Studies In Sports: A Systematic Review Of Exposure Confirmation Methods. Ann. Biomed. Eng. (2020).48(11). 2497–507.
- 175. Wu L.C., Nangia V., Bui K., Hammoor B., Kurt M., Hernandez F., et al. In Vivo Evaluation of Wearable Head Impact Sensors. Ann. Biomed. Eng. (2016).44(4). 1234–45.
- 176. Miyashita T., Diakogeorgiou E., Marrie K., Danaher R. Frequency and Location of Head Impacts in Division I Men's Lacrosse Players. Athl. Train. Sport. Heal. Care. **(2016)**.8(5). 202–8.
- 177. Press J.N., Rowson S. Quantifying head impact exposure in collegiate women's soccer. Clin. J. Sport Med. **(2017)**.27(2). 104–10.
- 178. McIntosh A.S., Willmott C., Patton D.A., Mitra B., Brennan J.H., Dimech-Betancourt B., et al. An assessment of the utility and functionality of wearable head impact sensors in Australian Football. J. Sci. Med. Sport. **(2019)**.22(7). 784–9. https://doi.org/10.1016/j.jsams.2019.02.004
- 179. Allison M.A., Kang Y.S., Bolte IV J.H., Maltese M.R., Arbogast K.B. Validation of a Helmet-based system to measure head impact biomechanics in ice hockey. Med. Sci. Sports Exerc. (2014).46(1). 115–23.
- 180. Simbex. A helmet that detects hard hits. [accessed 2020 Apr 6]. https://simbex.com/helmet-detects-hard-hits/
- Cummiskey B., Schiffmiller D., Talavage T.M., Leverenz L., Meyer J.J., Adams D., et al. Reliability and accuracy of helmet-mounted and head-mounted devices used to measure head accelerations. Proc. Inst. Mech. Eng. Part P J. Sport. Eng. Technol. (2017).231(2). 144–53.
- 182. Caswell S. V., Kelshaw P., Lincoln A.E., Hepburn L., Dunn R., Cortes N. Game-Related Impacts in High School Boys' Lacrosse. Orthop. J. Sport. Med. (2019).7(4). 1–8.
- Cortes N., Lincoln A.E., Myer G.D., Hepburn L., Higgins M., Putukian M., et al. Video Analysis Verification of Head Impact Events Measured by Wearable Sensors. Am. J. Sports Med. (2017).45(10). 2379–87.
- 184. Duma S.M., Manoogian S.J., Bussone W.R., Brolinson P.G., Goforth M.W., Donnenwerth J.J., et al. Analysis of real-time head accelerations in collegiate football players. Clin. J. Sport Med. (2005).15(1). 3–8.
- 185. Bartsch A.J., Hedin D.S., Gibson P.L., Miele V.J., Benzel E.C., Alberts J.L., et al. Laboratory and On-field Data Collected by a Head Impact Monitoring Mouthguard. Proc. Annu. Int. Conf. IEEE Eng. Med. Biol. Soc. EMBS. (2019).(Imm). 2068–72.
- 186. Greybe D.G., Jones C.M., Brown, M R., Williams, È, M P. Comparison of head impact measurements via an instrumented mouthguard and an anthropometric testing device. Sport. Eng. (2020). https://doi.org/10.1007/s12283-020-00324-z
- 187. Wu L.C., Kuo C., Loza J., Kurt M., Laksari K., Yanez L.Z., et al. Detection of American Football Head Impacts Using Biomechanical Features and Support Vector Machine Classification. Sci. Rep. (2018).8(1). 1–14. http://dx.doi.org/10.1038/s41598-017-17864-3
- 188. Kuo C., Wu L., Loza J., Senif D., Anderson S.C., Camarillo D.B. Comparison of videobased and sensor-based head impact exposure. PLoS One. **(2018)**.13(6). 1–19.
- Michio Clark J., Connor T.A., Post A., Blaine Hoshizaki T., Ní Annaidh A., Gilchrist M.D. Could a Compliant Foam Anvil Characterize the Biofidelic Impact Response of Equestrian Helmets? J. Biomech. Eng. (2020).142(6). 1–9.
- 190. Meehan A., Post A., Hoshizaki T.B., Gilchrist M.D. Investigation of an Ice Hockey Helmet Test Protocol Representing Three Concussion Event Types. J. Test. Eval. (2022).50(1).
- 191. Mez J., Daneshvar D.H., Kiernan P.T., Abdolmohammadi B., Alvarez V.E., Huber B.R., et al. Clinicopathological Evaluation of Chronic Traumatic Encephalopathy in Players of American Football. J. Am. Med. Assoc. **(2017)**.02118(4). 360–70.
- 192. Wojnarowicz M.W., Fisher A.M., Minaeva O., Goldstein L.E. Considerations for experimental animal models of concussion, traumatic brain injury, and chronic traumatic

encephalopathy-these matters matter. Front. Neurol. (2017).8(JUN). 1–14.

- 193. Petrone N., Carraro G., Dal Castello S., Broggio L., Koptyug A., Backstrom M. A novel instrumented human head surrogate for the impact evaluation of helmets. Proc. 12th Conf. Eng. Sport. ISEA. (2018). 1–7.
- Stone B., Mitchell S., Miyazaki Y., Peirce N., Harland A. A destructible headform for the assessment of sports impacts. Proc. Inst. Mech. Eng. Part P J. Sport. Eng. Technol. (2021).237(1). 7–18.
- 195. ASTM Standard F1447, 2018, "Standard Specification for Helmets Used in Recreational Bicycling or Roller Skating", ASTM International, West Conshohocken, PA, 2018, DOI:10.1520/F1447-18, www.astm.org.
- 196. ASTM Standard F1952 22, "Standard Specification for Helmets Used for Downhill Mountain Bicycle Racing", ASTM International, West Conshohocken, PA, 2015, DOI:10.1520/F1952-22, www.astm.org.
- 197. 16 CFR Part 1203, 1998, "Safety Standard for Bicycle Helmets; Final Rule", Consumer Product Safety Commission.
- 198. EN 1078:2012+A1:2012, 2014, "Helmets for pedal cyclists and for users of skateboards and roller skates", DIN Deutsches Institut für Normung e. V.
- 199. Snell B-95A, 1998, "1995 Standard for Protectice Headgear For Use In Bicycling", Snell Memorial Foundation Inc.
- 200. ASTM Standard F1446 20, "Standard Test Methods for Equipment and Procedures Used in Evaluating the Performance Characteristics of Protective Headgear", ASTM International, West Conshohocken, PA, 2020, DOI:10.1520/F1446-20, www.astm.org.
- 201. BS 7928:2013+A1:2019, "Specification for head protectors for cricketers", BSI Standards Publication.
- 202. Snell E2016, 2016, "Standard for Protectice Headgear For Use in Horseback Riding", Snell Memorial Foundation Inc.
- 203. ASTM Standard F1163-15, 2015, "Standard Specification for Protective Headgear Used in Horse Sports and Horseback Riding", ASTM International, West Conshohocken, PA, 2018, DOI:10.1520/F1163-15, www.astm.org.
- 204. EN 1384:2017, 2017, "Helmets for equestrian activities", DIN Deutsches Institut für Normung e. V.
- 205. Snell foundation S.P.F.H. Snell SA2015, "Standard for Protectice Headgear For Use in Competitive Automotive Sports", Snell Memorial Foundation Inc. 2020.
- 206. Snell SA20, 2019, "2020 Special Applications Standard for Protective Headgear", Snell Memorial Foundation Inc.
- 207. Snell EA2016, 2016, "Standard for Protective Headgear For Use in Elite Automotive Sports", Snell Memorial Foundation Inc.
- 208. Federation Internationale de l'Automobile. Norme Fia 8860-2018 Et 8860-2018-Abp Fia Standard 8860-2018 and 8860-2018-Abp Casque Haute Performance. **(2018)**.
- 209. Used P. ASTM Standard F1492 22, "Standard Specification for Helmets Used in Skateboarding and Trick Roller Skating", ASTM International, West Conshohocken, PA, 2022, DOI:10.1520/F1492-22, www.astm.org. (2001).i. 2–4.
- 210. ASTM Standard F2040, 2018, "Standard Specification for Helmets Used for Recreational Snow Sports", ASTM International, West Conshohocken, PA, 2003, DOI:10.1520/F2040-18, www.astm.org.
- 211. Snell RS-98, 1998, "1998 Standard for Protectice Headgear For Use In Recreational Skiing and Snowboarding", Snell Memorial Foundation Inc.
- 212. Snell S-98, 1998, "1998 Standard for Protectice Headgear For Skiing and Other Winter Activities", Snell Memorial Foundation Inc.
- 213. Deutsche Norm. EN 1077:2007, 2007, "Helmets for alpine skiers and snowboarders", Deutsches Institut für Normung.
- 214. ASTM Standard F1045 22, "Standard Performance Specification for Ice Hockey Helmets", ASTM International, West Conshohocken, PA, 2022, DOI:10.1520/F1045-22, www.astm.org.
- 215. EN ISO 10256 2:2018, 2018, "Protective equipment for use in ice hockey Part 2:

| י ר | |
|--|--|
| 2 | |
| 3 | |
| 4 | |
| 5 | |
| 6 | |
| 7 | |
| 8 | |
| 9 | |
| 10 | |
| 11 | |
| 11 | |
| 12 | |
| 13 | |
| 14 | |
| 15 | |
| 16 | |
| 17 | |
| 18 | |
| 10 11 12 13 14 15 16 17 18 19 20 | |
| 70 | |
| 21 | |
| 21 | |
| 22 23 24 25 26 | |
| 23 | |
| 24 | |
| 25 | |
| 26 | |
| 27 | |
| 28 | |
| 29 | |
| 30 | |
| 31 | |
| 32 | |
| 5Z | |
| 33 34 35 36 | |
| 34 | |
| 35 | |
| 36 | |
| 37 | |
| 38 | |
| 39 | |
| 40 | |
| 41 | |
| 41 | |
| | |
| 43 | |
| 44 | |
| 45 | |
| 46 | |
| 47 | |
| 48 | |
| 49 | |
| 50 | |
| 51 | |
| 52 | |
| | |
| 53 | |
| 54 | |
| 55 | |
| 56 | |
| 57 | |
| 58 | |
| 59 | |

Head protection for skaters", BSI Standards Publication.

- 216. Canadian Standards Association. (2009). Casques de hockey sur glace (CAN/CSA Standard No. Z262.1-09).
- 217. Snell B-90A B-90C, 1998, "Standard for Protectice Headgear For Use In Bicycling", Snell Memorial Foundation Inc.
- 218. Hoshizaki T.B., Post A., Oeur R.A., Brien S.E. Current and future concepts in helmet and sports injury prevention. Neurosurgery. **(2014)**.75(4). s136–48.
- 219. Post A., Dawson L., Hoshizaki T.B., Gilchrist M.D., Cusimano M.D. Development of a test method for adult ice hockey helmet evaluation. Comput. Methods Biomech. Biomed. Engin. (2020).23(11). 690–702.
- 220. NOCSAE DOC (ND) 001-17m19, 2019, "Standard Test Method and Equipment Used in Evaluating the Performance Characteristics of Headgear/Equipment", National Operating Committee on Standards for Atletic Equipment.
- 221. EN 966:2012+A1:2012, 2013, "Helmets for airborne sports", DIN Deutsches Institut für Normung e. V.
- 222. NOCSAE DOC (ND) 081-18am19a, 2019, "Standard Pneumatic Ram Test Method and Equipment Used in Evaluating the Performance Characteristics of Protective Headgear and Face Guards, National Operating Committee on Standards for Athletic Equipment.
- 223. Oeur R.A., Hoshizaki T.B. The effect of impact compliance, velocity, and location in predicting brain trauma for falls in sport. 2016 IRCOBI Conf. Proc. Int. Res. Counc. Biomech. Inj. **(2016)**. 228–38.
- Walsh E.S., Post A., Rousseau P., Kendall M., Karton C., Oeur A., et al. Dynamic impact response characteristics of a helmeted Hybrid III headform using a centric and noncentric impact protocol. Proc. Inst. Mech. Eng. Part P J. Sport. Eng. Technol. (2012).226(3–4). 220–5.
- 225. Rousseau P., Post A., Hoshizaki T.B. A comparison of peak linear and angular headform accelerations using ice hockey helmets. J. ASTM Int. (2009).6(1).
- 226. Levy Y., Gallone M.B., Bian K., McDougall K., Ouckama R., Mao H. Using a Strain-Based Computational Approach for Ice Hockey Helmet Performance Evaluation. **(2020)**. 569–80.
- 227. Cummiskey B., Sankaran G.N., McIver K.G., Shyu D., Markel J., Talavage T.M., et al. Quantitative evaluation of impact attenuation by football helmets using a modal impulse hammer. Proc. Inst. Mech. Eng. Part P J. Sport. Eng. Technol. **(2019)**.233(2). 301–11.
- 228. McIver K.G., Lee P., Bucherl S., Talavage T.M., Myer G.D., Nauman E.A. Design Considerations for the Attenuation of Translational and Rotational Accelerations in American Football Helmets. J. Biomech. Eng. **(2023)**.145(6). 1–9.
- 229. McIver K.G., Sankaran G.N., Lee P., Bucherl S., Leiva N., Talavage T.M., et al. Impact attenuation of male and female lacrosse helmets using a modal impulse hammer. J. Biomech. (2019).95. 109313.
- 230. Haid D., Duncan O., Foster L., Hart J. Free-fall drop test with interchangeable surfaces to recreate concussive ice hockey head impacts. Sport. Eng. **(2023)**.26(25).
- 231. Halldin P., Gilchrist A., Mills N.J. A new oblique impacttest for motorcycle helmets. Int. J. Crashworthiness. **(2001)**.6(1). 53–64.
- 232. Jeffries L., Zerpa C., Przysucha E., Sanzo P., Carlson S. The Use of a Pneumatic Horizontal Impact System for Helmet Testing. J. Saf. Eng. **(2017)**.6(1). 8–13.
- 233. Schmitt K.U., Muser M.H., Thueler H., Bruegger O. Crash-test dummy and pendulum impact tests of ice hockey boards: Greater displacement does not reduce impact. Br. J. Sports Med. (2018).52(1). 41–6.
- 234. Tyson A.M., Rowson S. Adult Football STAR Methodology. Virginia Tech Helmet Lab. **(2018)**.(540). 3–6.
- 235. McIntosh A.S., Janda D. Evaluation of cricket helmet performance and comparison with baseball and ice hockey helmets. Br. J. Sports Med. **(2003)**.37(4). 325–30.
- 236. Cobb B.R., Macalister A., Young T.J., Kemper A.R., Rowson S., Duma S.M. Quantitative comparison of Hybrid III and National Operating Committee on Standards for Athletic Equipment headform shape characteristics and implications on football

helmet fit. Proc. Inst. Mech. Eng. Part P J. Sport. Eng. Technol. (2015).229(1). 39-46.

- 237. Post A., Oeur A., Hoshizaki B., Gilchrist M.D. An examination of American football helmets using brain deformation metrics associated with concussion. Mater. Des. (2013).45. 653–62.
- 238. MacAlister A. Surrogate Head Forms for the Evaluation of Head Injury Risk. Brain Inj. Biomech. Symp. (2013).
- 239. Chen W., Post A., Karton C., Gilchrist M.D., Robidoux M., Hoshizaki T.B. A comparison of frequency and magnitude of head impacts between Pee Wee And Bantam youth ice hockey. Sport. Biomech. (2020).00(00). 1–24.
- 240. Post A., Karton C., Robidoux M., Gilchrist M.D., Hoshizaki T.B. An examination of the brain trauma in Novice and Midget ice hockey: Implications for helmet innovation. (2019). 1–4.
- 241. Post A., De Grau S., Ignacy T., Meehan A., Zemek R., Hoshizaki B., et al. Comparison of helmeted head impact in youth and adult ice hockey. 2016 IRCOBI Conf. Proc. Int. Res. Counc. Biomech. Inj. (2016). 194–204.
- 242. Kendall M., Walsh E.S., Hoshizaki T.B. Comparison between Hybrid III and Hodgson-WSU headforms by linear and angular dynamic impact response. Proc. Inst. Mech. Eng. Part P J. Sport. Eng. Technol. **(2012)**.226(3–4). 260–5.
- 243. ASTM Standard F2220-2015, 2015, "Standard Specification for Headforms", ASTM International, West Conshohocken, PA, 2015, DOI:10.1520/F2220-15, www.astm.org.
- 244. Solutions H.I. Hybrid III 50th Male. (2020).
- 245. British Standards Institution (2006), BS EN 960:2006, Headforms for use in the testing of protective helmets.
- 246. Bottlang M., Rouhier A., Tsai S., Gregoire J., Madey S.M. Impact Performance Comparison of Advanced Bicycle Helmets with Dedicated Rotation-Damping Systems. Ann. Biomed. Eng. **(2020)**.48(1). 68–78.
- 247. Allison M.A., Kang Y.S., Maltese M.R., Bolte J.H., Arbogast K.B. Measurement of Hybrid III Head Impact Kinematics Using an Accelerometer and Gyroscope System in Ice Hockey Helmets. Ann. Biomed. Eng. **(2015)**.43(8). 1896–906.
- 248. Walsh E.S., Hoshizaki T.B. Poster Session III, July 15th 2010 Abstracts Sensitivity analysis of a Hybrid III head- and neckform to impact angle variations. Procedia Eng. (2010).2(2). 3487.
- 249. Rousseau P., Hoshizaki T.B. Defining the effective impact mass of elbow and shoulder strikes in ice hockey. Sport. Biomech. (2015).14(1). 57–67.
- 250. McIntosh A.S., Lai A., Schilter E. Bicycle Helmets: Head Impact Dynamics in Helmeted and Unhelmeted Oblique Impact Tests. Traffic Inj. Prev. (2013).14(5). 501–8.
- 251. Farmer J., Mitchell S., Sherratt P., Miyazaki Y. A human surrogate neck for traumatic brain injury research. Front. Bioeng. Biotechnol. (2022).10(December). 1–19.
- 252. Clark J.M., Connor T.A., Post A., Hoshizaki T.B., Gilchrist M.D. The influence of impact surface on head kinematics and brain tissue response during impacts with equestrian helmets. Sport. Biomech. (2019).00(00). 1–14.
- 253. Clark J.M., Taylor K., Post A., Hoshizaki T.B., Gilchrist M.D. Comparison of Ice Hockey Goaltender Helmets for Concussion Type Impacts. Ann. Biomed. Eng. **(2018)**.46(7). 986–1000.
- 254. Clark J.M., Hoshizaki T.B., Gilchrist M.D. Protective capacity of an ice hockey goaltender helmet for three events associated with concussion. Comput. Methods Biomech. Biomed. Engin. (2017).20(12). 1299–311.
- 255. Post A., Clark J.M., Robertson D.G.E., Hoshizaki T.B., Gilchrist M.D. The effect of acceleration signal processing for head impact numeric simulations. Sport. Eng. (2017).20(2). 111–9.
- 256. Bhudolia S.K., Gohel G., Subramanyam E.S.B., Leong K.F., Gerard P. Enhanced impact energy absorption and failure characteristics of novel fully thermoplastic and hybrid composite bicycle helmet shells. Mater. Des. **(2021)**.209. 110003.
- 257. Di Landro L., Sala G., Olivieri D. Deformation mechanisms and energy absorption of polystyrene foams for protective helmets. Polym. Test. **(2002)**.21(2). 217–28.

| 1 | |
|----------|--------------|
| 2 3 | 258. |
| 3 4 | 200. |
| 5 6 | |
| 0 7 | 259. |
| 8 | 260. |
| 9 | 200. |
| 10 | |
| 11 12 | 261. |
| 13 | |
| 14 | 000 |
| 15 | 262. |
| 16 17 | 263. |
| 18 | 200. |
| 19 | 264. |
| 20 | 265. |
| 21 | 266. |
| 22 23 | 0.07 |
| 24 | 267. 268. |
| 25 | 200. |
| 26 | 269. |
| 27 | |
| 28 29 | 270. |
| 30 | 0=4 |
| 31 | 271. |
| 32 | 272. |
| 33 34 | 273. |
| 34 35 | |
| 36 | 274. |
| 37 | |
| 38 | 275. |
| 39 40 | |
| 40 | 276. |
| 42 | 210. |
| 43 | 277. |
| 44 45 | |
| 45 46 | 278. |
| 47 | |
| 48 | 279. |
| 49 | 215. |
| 50 51 | 280. |
| 52 | |
| 53 | 281. |
| 54 | 000 |
| 55 | 282. |
| 56 57 | (|
| 57 | 283. |
| 59 | |
| 60 | |

- 258. Pinnoji P.K., Mahajan P. Analysis of impact-induced damage and delamination in the composite shell of a helmet. Mater. Des. **(2010)**.31(8). 3716–23. http://dx.doi.org/10.1016/j.matdes.2010.03.011
 - 259. Coelho R.M., Alves de Sousa R.J., Fernandes F.A.O., Teixeira-Dias F. New composite liners for energy absorption purposes. Mater. Des. (2013).43. 384–92.
 - Andena L., Caimmi F., Leonardi L., Ghisi A., Mariani S., Braghin F. Towards Safer Helmets: Characterisation, Modelling and Monitoring. Procedia Eng. (2016).147. 478– 83.
 - 261. Mcgillivray K., Przysucha E., Sanzo P., Liu M., Zerpa C. Comparison of Hockey Helmet Lining Technologies in Mitigating Concussion Risk During Simulated Horizontal Head Collisions. Int. J. Extrem. Autom. Connect. Healthc. **(2022)**.4(1). 1–17.
- 262. Gimbel G., Hoshizaki T. Compressive properties of helmet materials subjected to dynamic impact loading of various energies. Eur. J. Sport Sci. (2008) 8(6). 341–9.
- 263. Foster L., Peketi P., Allen T., Senior T., Duncan O., Alderson A. Application of auxetic foam in sports helmets. Appl. Sci. **(2018)**.8(3). 1–12.
- 264. Wavecel. WaveCel Technology. (2023).
- 265. MIPS. mipsprotection. [accessed 2023 Apr 5]. https://mipsprotection.com/
- 266. MIPS. Mips Integra. (**2023**) [accessed 2023 Apr 5]. https://mipsprotection.com/productrange/mips-integra/
 - 267. D3O 2020. D3O Protection. (2023).
 - 268. POC. POC SPIN Pad Kit. (2023) [accessed 2023 May 5]. https://www.pocsports.com/products/omne-air-spin-pad-kit?variant=36219708604568
 - 269. Salomon. Salomon EPS 4D. (**2016**) [accessed 2023 Apr 13]. https://youtu.be/YcmUFMUyjsE
 - 270. Vicis. Vicis Matrix Technology. (2023) [accessed 2023 Aug 14]. https://vicis.com/pages/zero2-matrix
 - 271. Gibson L.J., Ashby M.F. Energy absorption in cellular materials. (**2014**).pp.309–344p.
 - 272. Duncan O., Bailly N., Allen T., Petit Y., Wagnac E., Alderson A. Effect of compressive strain rate on the Poisson's ratio of auxetic foam. Appl. Sci. **(2021)**.11(3).
 - 273. Mustafa H., Pang T.Y., Ellena T., Nasir S.H. Impact attenuation of user-centred bicycle helmet design with different foam densities. J. Phys. Conf. Ser. **(2019)**.1150(1).
 - 274. Wei M., Lin K., Sun L. Shear thickening fluids and their applications. Mater. Des. (2022).216. 110570.
 - 275. Li S., Wang J., Zhao S., Cai W., Wang Z., Wang S. Giant Rheological Effect of Shear Thickening Suspension Comprising Silica Nanoparticles with No Aggregation. J. Mater. Sci. Technol. **(2017)**.33(3). 261–5. http://dx.doi.org/10.1016/j.jmst.2016.06.008
 - 276. Cossa K.N. Basic concepts on rheology and application of shear-thickening fluids in protective gear. SN Appl. Sci. (2019).1(10). 1–6.
 - 277. LeMaitre J. Introduction to Elasticity and Viscoelasticity. Academic Press; (**2001**).pp.71– 74p. http://dx.doi.org/10.1016/B978-0-12-443341-0.50006-5
 - 278. Zhao C., Gong X., Wang S., Jiang W., Xuan S. Shear Stiffening Gels for Intelligent Antiimpact Applications. Cell Reports Phys. Sci. **(2020)**.1(12). 100266. https://doi.org/10.1016/j.xcrp.2020.100266
 - 279. Coussot P. Introduction to the rheology of complex fluids. Underst. Rheol. Concr. (2012). 3–22.
 - 280. Fowler J.N., Pallanta A.A., Swanik C.B., Wagner N.J. The Use of Shear Thickening Nanocomposites in Impact Resistant Materials. J. Biomech. Eng. **(2015)**.137(5).
 - 281. Soutrenon M., Michaud V. Impact properties of shear thickening fluid impregnated foams. Smart Mater. Struct. **(2014)**.23(3).
 - 282. Nakonieczna P., Wierzbicki Ł., Śladowska B., Leonowicz M., Lisiecki J., Nowakowski D. Composites With Impact Absorption Ability Based on Shear Thickening Fluids and Auxetic Foams. Compos. Theory Pract. (2017).17(2). 67–72.
 - 283. Jachowicz M., Owczarek G. Analysis of selected mechanical parameters for foamed materials with non-Newtonian liquid characteristics in terms of their use in aspects of protective helmets. Int. J. Occup. Saf. Ergon. (2020).26(3). 617–23.

- 284. Waitukaitis S.R., Jaeger H.M. Impact-activated solidification of dense suspensions via dynamic jamming fronts. Nature. **(2012)**.487(7406). 205–9.
 - 285. Halldin P., Aare M., Kleiven S., von Holst H. Improved helmet design and test methods to reduce rotational induced brain injuries. RTO Spec. Meet. NATO's Res. Technol. Organ. (2003).
 - Evans K.E. Auxetic polymers: a new range of materials. Endeavour. (1991).15(4). 170–4.
- 287. Aare M., Halldin P. A new laboratory rig for evaluating helmets subject to oblique impacts. Traffic Inj. Prev. (2003).4(3). 240–8.
- 288. Holst V. United States Patent: US 6,658,671. (2004).2(12). 0–5.

- 289. Jacques Durocher S.-J. United States Patent US 9,961,952 B2. Vol. 2. 2018.
- 290. Mosleh Y., Vanden Bosche K., Depreitere B., Vander Sloten J., Verpoest I., Ivens J. Effect of polymer foam anisotropy on energy absorption during combined shear-compression loading. J. Cell. Plast. (2018).54(3). 597–613.
- 291. Huber M.T. The theory of crosswise reinforced ferroconcrete slabs and its application to various important constructional problems involving rectangular slabs. Der Bauingenieur. (1923).4(12). 354–60.
- 292. Parisi M.F., Allen T., Cologna M., Pugno N., Duncan O. Indentation and impact response of conventional, auxetic, and shear gel thickening infused auxetic closed cell foam. Under Rev. Int. J. Impact Eng.
- 293. STONE A., ALFERNESS A.P., CZERSKI M., NEUBAUER J., FRANK A. LATERALLY SUPPORTED FILAMENTS. US Patent; US 2018 / 0184745 A1, 2018.
- 294. Bologna V., Gillogly M., Ide T.M. FOOTBALL HELMET WITH COMPONENTS ADDITIVELY MANUFACTURED TO MANAGE IMPACT FORCES. Vol. 2. U.S. PATENT; US 11,167,198 B2, 2021.
- 295. Posner J.D., Dardis J.T., Leonard P.C., Reinhall P.G. PROTECTIVE HELMETS INCLUDING NON - LINEARLY DEFORMING ELEMENTS. US Patent; US 10,813,402 B2, 2020.
- 296. Bottlang M., Bennett J. ENERGY ABSORBING STRUCTURE WITH DEFINED MULTI - PHASIC CRUSH PROPERTIES. US Patent; US 2022/0324194 A1, 2022.
- 297. Chilson J.A., Lloyd J., Rogers J., Storey P. HELMET WITH SHOCK ABSORBING INSERTS. US Patent; US 10,736,373 B2, 2020.
- 298. Baracco S., Marino F. PROTECTIVE HELMET. EUROPEAN PATENT; EP003130243B1, 2020.
- 299. Loubert S . Suddaby. HELMET WITH MULTIPLE PROTECTIVE ZONES. US Patent; US 9,795 ,178 B2, 2017.
- 300. Vanhoutin L.A., Long V.R., Loucks N., Groff R. SPORTS HELMET WITH CUSTOM -FIT LINER. US Patent; US 11,026,466 B2, 2021.
- 301. Fischer K., Fukuda K., Czerski M., Frank A., Santiago C. MODULAR LINER SYSTEM FOR PROTECTIVE HELMETS. US Patent; US 10,342 ,281 B2, 2019.
- 302. Plant D.J. ENERGY ABSORBING SYSTEM. US Patent; US 2020/0040958 A1, 2020.
- 303. Plant D.J. FLEXIBLE ENERGY ABSORBING MATERAL AND METHODS OF MANUFACTURE THEREOF. US Patent; US 7.608,314 B2, 2009.
- 304. Morgan J.T., Morgan G.E. HELMET WITH NON NEWTONIAN FLUID LINER SYSTEM. US Patent; US 11,219,263 B2, 2022.
- 305. Warmouth C., VanHoutin L.A., Long V.R. SPORTS HELMET WITH LINER SYSTEM. US Patent; US 2017/0056750 A1, 2017.
- 306. Jason E. Kirshon. IMPACT DISSIPATING LINERS AND METHODS OF FABRICATING IMPACT DISSIPATING LINERS. US Patent; US 2020/0205502 A1, 2020.
- 307. Lakes Roderic. Foam Structures with a Negative Poisson's Ratio. Science (80-.). (1987).235(4792). 1038–40.
- 308. Jiang W., Ren X., Wang S.L., Zhang X.G., Zhang X.Y., Luo C., et al. Manufacturing, characteristics and applications of auxetic foams: A state-of-the-art review. Compos. Part B Eng. (2022).235. 109733.

| 2 | |
|----------------|---|
| 3 | |
| 4 5 | |
| 5 | |
| 6 7 | |
| 7 | |
| 8 | |
| 9 10 | |
| 11 | |
| 12 | |
| 13 | |
| 14 | |
| 15 | |
| 15 16 17 | |
| 17 | |
| 18 | |
| 19 | |
| 20 | |
| 20 21 22 | |
| 22 | |
| 24 | |
| 25 | |
| 26 | |
| 27 | |
| 28 | |
| 29 | |
| 30 | |
| 31 | |
| 32 33 | |
| 34 | |
| 35 | |
| 36 | |
| 37 | |
| 38 | |
| 39 | |
| 40 | |
| 41 42 | |
| 42 | |
| 44 | |
| 45 | |
| 46 | |
| 47 | |
| 48 | |
| 49 | |
| 50 51 | |
| 51 | |
| 53 | |
| 54 | |
| 55 | |
| 56 | |
| 57 | |
| 58 | 4 |
| 59 | |
| 60 | |

- 309. Hu H., Zhang M., Yanping L. Auxetic Textiles. Woodhead Publishing Ltd.; (2019).
- 310. Novak N., Vesenjak M., Ren Z. Auxetic cellular materials A review. Stroj. Vestnik/Journal Mech. Eng. (2016).62(9). 485–93.
- Miura K. Map Fold a La Miura Style, Its Physical Characteristics and Application to the Space Science. In: Takaki R, editor. Research of Pattern Formation. KTK Scientific Publishers; (1994). pp. 77–90.
- 312. Miura K. Method of packaging and deployment of large membranes in space. In: Congress of International Astronautical Federation. (**1980**).
 - Sareh P., Guest S.D. Design of non-isomorphic symmetric descendants of the Miuraori. Smart Mater. Struct. (2015).24(8). 85002. http://dx.doi.org/10.1088/0964-1726/24/8/085002
- 314. Sareh P. The least symmetric crystallographic derivative of the developable double corrugation surface: Computational design using underlying conic and cubic curves. Mater. Des. **(2019)**.183. 108128. https://doi.org/10.1016/j.matdes.2019.108128
- 315. Chen Y., Lu C., Fan W., Feng J., Sareh P. Data-driven design and morphological analysis of conical six-fold origami structures. Thin-Walled Struct. (2023).185(December 2022). 110626. https://doi.org/10.1016/j.tws.2023.110626
- 316. Chen Y., Xu R., Lu C., Liu K., Feng J., Sareh P. Multi-stability of the hexagonal origami hypar based on group theory and symmetry breaking. Int. J. Mech. Sci. (2023).247(January). 108196. https://doi.org/10.1016/j.ijmecsci.2023.108196
- 317. Hunt G.W., Ario I. Twist buckling and the foldable cylinder: An exercise in origami. Int. J. Non. Linear. Mech. **(2005)**.40(6). 833–43.
- 318. Chen Y., Shi P., Bai Y., Li J., Feng J., Sareh P. Engineered origami crease perforations for optimal mechanical performance and fatigue life. Thin-Walled Struct. (2023).185(January). 110572. https://doi.org/10.1016/j.tws.2023.110572
- 319. Zhang Z., Ma W., Wu H., Wu H., Jiang S., Chai G. A rigid thick Miura-Ori structure driven by bistable carbon fibre-reinforced polymer cylindrical shell. Compos. Sci. Technol. (2018).167(August). 411–20. https://doi.org/10.1016/j.compscitech.2018.08.033
- 320. Chen Y., Lu C., Yan J., Feng J., Sareh P. Intelligent computational design of scalenefaceted flat-foldable tessellations. J. Comput. Des. Eng. **(2022)**.9(5). 1765–74.
- 321. Miura K. The Science of Miura-Ori: A Review. In: Origami 4. 1st ed. New York: A K Peters/CRC Press; (**2009**). pp. 14.
- 322. Miura K. Triangles and quadrangles in space," In Symposium of the International Association for Shell and Spatial Structures. In: In Symposium of the International Association for Shell and Spatial Structures. (**2009**).
- 323. Nojima T. Modelling of Folding Patterns in Flat Membranes and Cylinders by Origami. Japan Soc. Mech. Eng. Int. J. **(2002)**.45(1). 364–70.
- 324. Chen, Y., Yan, J., Feng, J., Sareh, P. Particle swarm optimization-based metaheuristic design generation of non-trivial flat-foldable origami tessellations with degree-4 vertices. Journal of Mechanical Design, (**2021**).143(1), 011703.
- 325. Chen, Y., Ye, W., Shi, P., He, R., Liang, J., Feng, J., Sareh, P. Computational parametric analysis of cellular solids with the Miura-ori metamaterial geometry under quasi-static compressive loads. Advanced Engineering Materials. (**2023**) 2201762.
- 326. Sareh, P., Chen, Y. Intrinsic non-flat-foldability of two-tile DDC surfaces composed of glide-reflected irregular quadrilaterals. International Journal of Mechanical Sciences. (2020).185, 105881.
- 327. Lu, C., Chen, Y., Yan, J., Feng, J., Sareh, P. Algorithmic spatial form-finding of four-fold origami structures based on mountain-valley assignments. Journal of Mechanisms and Robotics. (**2024**). 16(3), 031001.
- 328. Sareh P., Guest S.D. Design of isomorphic symmetric descendants of the Miura-ori. Smart Mater. Struct. **(2015)**.24(8). 85001. http://dx.doi.org/10.1088/0964-1726/24/8/085001
- 329. Tang Y., Lin G., Yang S., Yi Y.K., Kamien R.D., Yin J. Programmable Kiri-Kirigami Metamaterials. Adv. Mater. **(2017)**.29(10).
 - 330. Castle T., Cho Y., Gong X., Jung E., Sussman D.M., Yang S., et al. Making the cut:

Lattice kirigami rules. Phys. Rev. Lett. (2014).113(24). 1-5.

- 331. Heimbs S., Cichosz J., Klaus M., Kilchert S., Johnson A.F. Sandwich structures with Struct. textile-reinforced composite foldcores under impact loads. Compos. (2010).92(6). 1485-97.
- Heimbs S., Middendorf P., Kilchert S., Johnson A.F., Maier M. Experimental and 332. numerical analysis of composite folded sandwich core structures under compression. Appl. Compos. Mater. (2007).14(5-6). 363-77.
- Li Z., Chen W., Hao H. Crushing behaviours of folded kirigami structure with square 333. dome shape. Int. J. Impact Eng. (2018).115(February). 94–105.
- 334. Li Z., Chen W., Hao H. Numerical study of folded dome shape aluminium structure against flatwise crushing. In: 12th International Converence on Shock & Impact Loads on Structures. (2017).
- 335. Teng T.L., Liang C.C., Nguyen V.H. Innovative design of bicycle helmet liners. Proc. Inst. Mech. Eng. Part L J. Mater. Des. Appl. (2014).228(4). 341-51.
- 336. Li Z., Chen W., Hao H., Cui J., Shi Y. Experimental study of multi-layer folded truncated structures under dynamic crushing. Int. J. Impact Eng. (2019).131(May). 111-22.
- Defense 2020 Viconic. Viconic Defense. (2020). 337.
- 338. Neville R.M., Scarpa F., Pirrera A. Shape morphing Kirigami mechanical metamaterials. Sci. Rep. (2016).6(July). 1-12.
- Tang Y., Yin J. Design of cut unit geometry in hierarchical kirigami-based auxetic 339. metamaterials for high stretchability and compressibility. Extrem. Mech. Lett. (2017).12. 77–85.
- Alderete N.A., Medina L., Lamberti L., Sciammarella C., Espinosa H.D. Programmable 340. 3D structures via Kirigami engineering and controlled stretching. Extrem. Mech. Lett. (2021).43. 101146. https://doi.org/10.1016/j.eml.2020.101146
- 341. Hou Y., Neville R., Scarpa F., Remillat C., Gu B., Ruzzene M. Graded conventionalauxetic Kirigami sandwich structures: Flatwise compression and edgewise loading. Compos. Part B Eng. (2014).59. 33–42. Chen Y., Ye W., Xu R., Sun Y., Feng J., Sareh P. A programmable auxetic metamaterial
- 342. with tunable crystal symmetry. Int. J. Mech. Sci. (2023).249. 108249.
- Jalali E., Soltanizadeh H., Chen Y., Xie Y.M., Sareh P. Selective hinge removal strategy 343. for architecting hierarchical auxetic metamaterials. Commun. Mater. (2022).3(1).
- Hwang D.G., Trent K., Bartlett M.D. Kirigami-Inspired Structures for Smart Adhesion. 344. ACS Appl. Mater. Interfaces. (2018).10(7). 6747-54.
- Sun Y., Ye W., Chen Y., Fan W., Feng J., Sareh P. Geometric design classification of 345. kirigami-inspired metastructures and metamaterials. Structures. (2021).33(December 2020). 3633-43.
- 346. Saxena K.K., Das R., Calius E.P. Three Decades of Auxetics Research - Materials with Negative Poisson's Ratio: A Review. Adv. Eng. Mater. (2016).18(11). 1847-70.
- Prawoto Y. Seeing auxetic materials from the mechanics point of view: A structural 347. review on the negative Poisson's ratio. Comput. Mater. Sci. (2012).58. 140-53.
- 348. Lim T.C. Micromechanical Models for Auxetic Materials. In: Auxetic Materials and Structures, Singapore: (2014), pp. 45–105.
- Lim T.C. Auxetic Materials and Structures. Springer Singapore; (2015). 349.
- Platus D.L., Technology M.K. Negative Stiffness Mechanism. (1999).3786(July). 98-350. 105.
- 351. Lakes R.S., Drugan W.J. Dramatically stiffer elastic composite materials due to a negative stiffness phase? J. Mech. Phys. Solids. (2002).50(5). 979-1009.
- Churchill C.B., Shahan D.W., Smith S.P., Keefe A.C., McKnight G.P. Dynamically 352. variable negative stiffness structures. Sci. Adv. (2016).2(2). 1-7.
- Hewage T.A.M., Alderson K.L., Alderson A., Scarpa F. Double-Negative Mechanical 353. Metamaterials Displaying Simultaneous Negative Stiffness and Negative Poisson's Ratio Properties. Adv. Mater. (2016).28(46). 10323–32.
- 354. Ha C.S., Lakes R.S., Plesha M.E. Cubic negative stiffness lattice structure for energy absorption: Numerical and experimental studies. Int. J. Solids Struct. (2019).178–179.

1 2 3

4

5

6

7

8

9

10

| 1 |
|--|
| 2 |
| 3 |
| 4 |
| |
| 5 |
| 6 |
| 6 7 |
| , 8 |
| |
| 9 |
| 10 |
| 11 |
| 11 12 |
| 12 |
| 13 |
| 14 |
| 15 |
| 10 |
| 16 17 |
| 17 |
| 18 |
| 19 |
| |
| 20 |
| 21 |
| 20 21 22 23 |
| 23 |
| 23 |
| 24 |
| 25 |
| 25 26 27 |
| 27 |
| 27 |
| 28 |
| 29 |
| 30 |
| 31 |
| 22 |
| 32 |
| 33 |
| 34 |
| 35 |
| 22 |
| 36 |
| 30 31 32 33 34 35 36 37 |
| 38 |
| 39 |
| |
| 40 |
| 41 |
| 42 |
| 43 |
| |
| 44 |
| 45 |
| 46 |
| 47 |
| |
| 48 |
| 49 |
| 50 |
| 51 |
| |
| 52 |
| 53 |
| 54 |
| 55 |
| |
| 56 |
| 57 |

60

127–35.

- 355. Zhang K., Qi L., Zhao P., Zhao C., Deng Z. Buckling induced negative stiffness mechanical metamaterial for bandgap tuning. Compos. Struct. (2023).304. 116421.
- 356. Goldsberry B.M., Haberman M.R. Negative stiffness honeycombs as tunable elastic metamaterials. J. Appl. Phys. **(2018)**.123(9).
- 357. Mehreganian N., Fallah A.S., Sareh P. Structural mechanics of negative stiffness honeycomb metamaterials. J. Appl. Mech. (2021).88(5). 051006.
- 358. Zhang Z., Krushynska A.O. Programmable shape-morphing of rose-shaped mechanical metamaterials. APL Mater. (2022).10(080701).
- 359. Dudek K.K., Iglesias Martinez J.A., Ulliac G., Kadic M. Micro-scale Auxetic Hierarchical Mechanical Metamaterials for Shape Morphing. Adv. Mater. (2022).
- 360. de Jong P., Schwab A., Mirzaali M.J., Zadpoor A.A. A multibody kinematic system approach for the design of shape-morphing mechanism-based metamaterials. Res. Sq. Pre-Print. (2003).
- 361. Duncan O., Chester M., Wang W., Alderson A., Allen T. Effect of twist on indentation resistance. Mater. Today Commun. (2023).35(105616).
- 362. Goswami D., Zhang Y., Liu S., Abdalla O.A., Zavattieri P.D., Martinez R. V. Mechanical metamaterials with programmable compression-twist coupling. Smart Mater. Struct. (2021).30(1). 015005.
- 363. Frenzel T., Kadic M., Wegener M. Three-dimensional mechanical metamaterials with a twist. Science (80-.). (2017).358(6366). 1072–4.
- 364. Fernandez-Corbaton I., Rockstuhl C., Ziemke P., Gumbsch P., Albiez A., Schwaiger R., et al. New Twists of 3D Chiral Metamaterials. Adv. Mater. (2019).31(26). 1–7.
- 365. Canejo J.P., Borges J.P., Godinho M.H., Brogueira P., Teixeira P.I.C., Terentjev E.M. Helical twisting of electrospun liquid crystalline cellulose micro- and nanofibers. Adv. Mater. (2008).20(24). 4821–5.
- 366. Janbaz S., Narooei K., Van Manen T., Zadpoor A.A. Strain rate-dependent mechanical metamaterials. Sci. Adv. **(2020)**.6(25).
- Wu R., Roberts P.C.E., Lyu S., Zheng F., Soutis C., Diver C., et al. Lightweight Self-Forming Super-Elastic Mechanical Metamaterials with Adaptive Stiffness. Adv. Funct. Mater. (2020). 2008252.
- 368. Zhu R., Chen Y.Y., Barnhart M. V., Hu G.K., Sun C.T., Huang G.L. Experimental study of an adaptive elastic metamaterial controlled by electric circuits. Appl. Phys. Lett. (2016).108(1).
- 369. Timoshenko S.P., Goodier J.N. Theory of Elasticity. 3rd ed. New York: McGraw-Hill, USA; (**1970**).
- 370. Duncan O., Allen T., Foster L., Alderson A. Effect of Poisson's ratio on the indentation of open cell foam. Eur. J. Mech. A/Solids. (2023).99(104922). 1–9.
- 371. Lakes R.S., Elms K. Indentability of conventional and negative Poisson's ratio foams. J. Compos. Mater. (1993).27(12). 1193–202.
- 372. Chan N., Evans K.E. Indentation Resilience of Conventional and Auxetic Foams. J. Cell. Plast. (1998).34. 231–60.
- Allen T., Duncan O., Foster L., Senior T., Zampieri D., Edeh V., et al. Auxetic foam for snow-sport safety devices. In: Snow Sports Trauma and Safety. 1st ed. Cham, Switzerland: Springer; (2016). pp. 145–59.
- 374. Alderson K.L., Pickles A.P., Neale P.J., Evans K.E. Auxetic polyethylene: The effect of a negative poisson's ratio on hardness. Acta Metall. Mater. (1994).42(7). 2261–6.
- 375. Novak N., Duncan O., Allen T., Alderson A., Vesenjak M., Ren Z. Shear modulus of conventional and auxetic open-cell foam. Mech. Mater. (2021).257. 104743.
- 376. Novak N., Krstulovid-Opara L., Ren Z., Vesenjak M. Compression and shear behaviour of graded chiral auxetic structures Nejc. Mech. Mater. **(2020)**.
- 377. Scarpa F., Tomlinson G. Theoretical characteristics of the vibration of sandwich plates with in-plane negative Poisson's ratio values. J. Sound Vib. **(2000)**.230(1). 45–67.
- 378. Scarpa F., Tomlin P.J. On the transverse shear modulus of negative Poisson's ratio honeycomb structures. Fatigue Fract. Eng. Mater. Struct. (**2000**).23(8). 717–20.

- 379. Chun Checn H., Scarpa F., Hallak Panzera T., Farrow I., Peng H.-X. Shear stiffness and energy absorption of auxetic open cell foams as sandwich cores. Phys. Status Solidi. **(2018)**.256(1). 1–9.
 - Kwon K., Phan A. V. Symmetric-Galerkin boundary element analysis of the dynamic Tstress for the interaction of a crack with an auxetic inclusion. Mech. Res. Commun. (2015).69. 91–6.
 - 381. Adam M.M., Berger J.R., Martin P.A. Singularities in auxetic elastic bimaterials. Mech. Res. Commun. (2013).47. 102–5.
 - 382. Lakes R.S. Foam Structures with a Negative Poisson's Ratio. Science (80-.). (1987).235(4792). 1038–40.
 - 383. Chan N., Evans K.E. Fabrication methods for auxetic foams. J. Mater. Sci. (1997).32. 5945–53.
 - 384. Scarpa F., Giacomin J., Zhang Y., Pastorino P. Mechanical performance of auxetic polyurethane foam for antivibration glove applications. Cell. Polym. **(2005)**.24(5). 253–68.
 - 385. Bianchi M., Scarpa F. Vibration transmissibility and damping behaviour for auxetic and conventional foams under linear and nonlinear regimes. Smart Mater. Struct. **(2013)**.22(8).
 - 386. Duncan O., Foster L., Senior T., Alderson A., Allen T. Quasi-static characterisation and impact testing of auxetic foam for sports safety applications. Smart Mater. Struct. (2016).25(5). 054014.
- 387. Allen T., Shepherd J., Hewage T.A.M., Senior T., Foster L., Alderson A. Low-kinetic energy impact response of auxetic and conventional open-cell polyurethane foams. Phys. Status Solidi Basic Res. (2015).252(7). 1631–9.
- 388. Ge C. A comparative study between felted and triaxial compressed polymer foams on cushion performance. J. Cell. Plast. **(2013)**.49(6). 521–33.
- Lisiecki J., Błazejewicz T., Kłysz S., Gmurczyk G., Reymer P., Mikułowski G. Tests of polyurethane foams with negative Poisson's ratio. Phys. Status Solidi Basic Res. (2013).250(10). 1988–95.
- 390. Żhang Q., Ścarpa F., Barton D., Zhu Y., Lang Z., Zhang D., et al. Impact properties of uniaxially thermoformed auxetic foams. Int. J. Impact Eng. (2022). 104176.
- 391. Evans K.E., Donoghue J., Alderson K.. The design, matching and manufacture of auxetic carbon fibre laminates. J. Compos. Mater. **(2004)**.38(2). 95–106.
- Alderson K.L., Simkins V.R., Coenen V.L., Davies P.J., Alderson A., Evans K.E. How to make auxetic fibre reinforced composites. Phys. Status Solidi Basic Res. (2005).242(3). 509–18.
- 393. HEAD. Auxetic The Science Behind the Sensational Feel. (2021) [accessed 2022 May 12]. https://www.head.com/de_CH/tennis/all-about-tennis/auxetic-the-science-behind-the-sensational-feel
- 394. Alderson K.L., Coenen V.L. The low velocity impact response of auxetic carbon fibre laminates. Phys. Status Solidi. **(2008)**.496(3). 489–96.
- 395. 2020 Carbon I. Carbon3D Riddell. (2020).
- 396. Adidas. 4D Shoes. https://www.adidas.co.uk/4d-shoes
- 397. Tancogne-Dejean T., Spierings A.B., Mohr D. Additively-manufactured metallic microlattice materials for high specific energy absorption under static and dynamic loading. Acta Mater. **(2016)**.116. 14–28.
- Qiu W., Lu F., Wang G., Huang G., Zhang H., Zhang Z., et al. Evaluation of mechanical performance and optimization design for lattice girders. Tunn. Undergr. Sp. Technol. (2019).87(February). 100–11.
- 399. Zheng X., Lee H., Weisgraber T.H., Shusteff M., DeOtte J., Duoss E.B., et al. Ultralight, ultrastiff mechanical metamaterials. Science (80-.). (2014).344(6190). 1373–7.
- 400. Gümrük R., Mines R.A.W. Compressive behaviour of stainless steel micro-lattice structures. Int. J. Mech. Sci. (2013).68. 125–39.
- 401. Fernandes F.A.O., de Sousa R.J.A., Ptak M., Migueis G. Helmet design based on the optimization of biocomposite energy-absorbing liners under multi-impact loading. Appl.

| 1 2 | | |
|----------------------|---|---|
| 3 4 5 | | 4 |
| 6 7 8 | | 4 |
| 9 10 | | 4 |
| 11 12 13 14 | | 4 |
| 15 16 17 | | 4 |
| 18 19 | | 4 |
| 20 21 22 | | 4 |
| 23 24 25 26 | | 4 |
| 27 28 | | 4 |
| 29 30 | | 4 |
| 31 32 | | 4 |
| 33 34 35 36 | | 4 |
| 37 38 | | 4 |
| 39 40 | | 4 |
| 41 42 43 | | 4 |
| 44 45 | | 4 |
| 46 47 | | 4 |
| 48 49 | | 4 |
| 50 51 52 | | 4 |
| 52 53 54 | | 4 |
| 55 56 | | 4 |
| 57 58 | _ | 4 |
| 59 60 | | |

Sci. **(2019)**.9(4). 1–26.

- 402. Hansen K., Dau N., Feist F., Deck C., Willinger R., Madey S.M., et al. Angular Impact Mitigation system for bicycle helmets to reduce head acceleration and risk of traumatic brain injury. Accid. Anal. Prev. **(2013)**.59. 109–17.
- 403. Caserta G.D., Iannucci L., Galvanetto U. Shock absorption performance of a motorbike helmet with honeycomb reinforced liner. Compos. Struct. (2011).93(11). 2748–59.
- 404. Kholoosi F., Galehdari S.A. Design, optimisation and analysis of a helmet made with graded honeycomb structure under impact load. Int. J. Crashworthiness. **(2019)**.24(6). 645–55.
- 405. Kholoosi F., Galehdari S.A. Design and Analysis of a Helmet Equipped with Graded Honeycomb Structure under Impact of Flat and Hemi-spherical Anvils. Procedia Eng. (2017).173. 1299–306.
- 406. Ozdemir Z., Hernandez-Nava E., Tyas A., Warren J.A., Fay S.D., Goodall R., et al. Energy absorption in lattice structures in dynamics: Experiments. Int. J. Impact Eng. (2016).89. 49–61.
- 407. Fleck N.A., Deshpande V.S., Ashby M.F. Micro-architectured materials: Past, present and future. Proc. R. Soc. A Math. Phys. Eng. Sci. (2010).466(2121). 2495–516.
- 408. Song J., Wang Y., Zhou W., Fan R., Yu B., Lu Y., et al. Topology optimization-guided lattice composites and their mechanical characterizations. Compos. Part B Eng. (2019).160(November 2018). 402–11.
- 409. Schaedler T.A., Ro C.J., Sorensen A.E., Eckel Z., Yang S.S., Carter W.B., et al. Designing metallic microlattices for energy absorber applications. Adv. Eng. Mater. (2014).16(3). 276–83.
- 410. Du Y., Li H., Luo Z., Tian Q. Topological design optimization of lattice structures to maximize shear stiffness. Adv. Eng. Softw. (2017).112, 211–21.
- 411. Ashby M.F. The properties of foams and lattices. Philos. Trans. R. Soc. A Math. Phys. Eng. Sci. (2006).364(1838). 15–30.
- 412. Liu Z., Liu J., Liu J., Zeng W., Huang W. The impact responses and failure mechanism of composite gradient reentrant honeycomb structure. Thin-Walled Struct. (2023).182(October 2022). 110228.
- 413. Özen İ., Çava K., Gedikli H., Alver Ü., Aslan M. Low-energy impact response of composite sandwich panels with thermoplastic honeycomb and reentrant cores. Thin-Walled Struct. (2020).156(August).
- 414. Wang S., Xu Y., Zhang W. Low-velocity impact response of 3D-printed lattice sandwich panels. IOP Conf. Ser. Mater. Sci. Eng. (2019).531(1).
- 415. Gao D., Wang S., Zhang M., Zhang C. Experimental and numerical investigation on inplane impact behaviour of chiral auxetic structure. Compos. Struct. (2021).267(December 2020). 113922.
- 416. Lu Q., Qi D., Li Y., Xiao D., Wu W. Impact energy absorption performances of ordinary and hierarchical chiral structures. Thin-Walled Struct. **(2019)**.140(March). 495–505.
- 417. Wu W., Hu W., Qian G., Liao H., Xu X., Berto F. Mechanical design and multifunctional applications of chiral mechanical metamaterials: A review. Mater. Des. (2019).180(June). 107950.
- 418. Ye M., Gao L., Wang F., Li H. A novel design method for energy absorption property of chiral mechanical metamaterials. Materials (Basel). **(2021)**.14(18). 1–21.
- 419. Kai L., Xiaofei C., Peng Z., WenWang W., Ying L. Dynamic mechanical performances of enhanced anti-tetra-chiral structure with rolled cross-section ligaments under impact loading. Int. J. Impact Eng. (2022).166(July 2021). 104204.
- 420. Xiang X., Qiang W., Hou B., Tran P., Lu G. Quasi-static and dynamic mechanical properties of Miura-ori metamaterials. Thin-Walled Struct. **(2020)**.157(May). 106993.
- 421. Xiang X., Fu Z., Zhang S., Lu G., Ha N.S., Liang Y., et al. The mechanical characteristics of graded Miura-ori metamaterials. Mater. Des. **(2021)**.211. 110173.
- 422. Galehdari S.A., Khodarahmi H., Atrian A. Design and analysis of graded honeycomb shock absorber for increasing the safety of passengers in armored vehicles exposed to mine explosion. J. Solid Mech. (**2017**).9(2). 370–83.

423. Sun G., Jiang H., Fang J., Li G., Li Q. Crashworthiness of vertex based hierarchical honeycombs in out-of-plane impact. Mater. Des. **(2016)**.110. 705–19.

- 424. Duncan O., Alderson A., Allen T. Fabrication, characterization and analytical modeling of gradient auxetic closed cell foams. Smart Mater. Struct. **(2021)**.30(3).
- 425. Duncan O., Allen T., Foster L., Senior T., Alderson A. Fabrication, characterisation and modelling of uniform and gradient auxetic foam sheets. Acta Mater. **(2017)**.126. 426–37.
- 426. Sanami M., Alderson A., Alderson K.L., McDonald S. a., Mottershead B., Withers P.J. The production and characterization of topologically and mechanically gradient opencell thermoplastic foams. Smart Mater. Struct. **(2014)**.23(5). 055016.
- 427. Evans A.G., Hutchinson J.W., Fleck N.A., Ashby M.F., Wadley H.N.G. The topological design of multifunctional cellular metals. Prog. Mater. Sci. (2001).46(3–4). 309–27.
- 428. Caccese V., Ferguson J.R., Edgecomb M.A. Optimal design of honeycomb material used to mitigate head impact. Compos. Struct. (2013).100. 404–12.
- 429. Zhang Y., Lu M., Wang C.H., Sun G., Li G. Out-of-plane crashworthiness of bio-inspired self-similar regular hierarchical honeycombs. Compos. Struct. (2016).144. 1–13.
- 430. Liu Y., Schaedler T.A., Chen X. Dynamic energy absorption characteristics of hollow microlattice structures. Mech. Mater. (2014).77. 1–13.
- 431. Gibson L.J., Ashby M.F. Cellular solids. Structure and properties. Cambridge: Press Syndicate of the University of Cambridge; (**1997**).pp.4, 67, 103, 106, 167–169, 176– 183, 259–264, 286, 3p.
- 432. Robinson M., Soe S., Johnston R., Adams R., Hanna B., Burek R., et al. Mechanical characterisation of additively manufactured elastomeric structures for variable strain rate applications. Addit. Manuf. **(2019)**.27(March). 398–407.
- 433. Wan H., Ohtaki H., Kotosaka S., Hu G. A study of negative Poisson's ratios in auxetic honeycombs based on a large deflection model. Eur. J. Mech. A/Solids. (2004).23(1). 95–106.
- 434. Yang, S., Qi C., Guo D.M., Wang D. Energy absorption of an re-entrant honeycombs with negative Poisson's ratio. Appl. Mech. Mater. **(2012)**.148. 992–5.
- 435. Dobnik Dubrovski P., Novak N., Borovinšek M., Vesenjak M., Ren Z. In-Plane Behavior of Auxetic Nonwoven Fabrics based on Rotating Square Unit Geometry under Tensile Load. Polymers (Basel). (2019).11(6). 1–13.
- 436. Grima J.N., Evans K.E. Auxetic behavior from rotating squares. J. Mater. Sci. Lett. (2000).19(17). 1563–5.
- 437. Grima J.N., Évans K.E. Auxetic behavior from rotating triangles. J. Mater. Sci. (2006).41. 3193–6.
- 438. Dudek K.K., Drzewiński A., Kadic M. Self-rotating 3D mechanical metamaterials. Proc.R.Soc.A. (2021).447(20200825).
- 439. Gao Y., Wei X., Han X., Zhou Z., Xiong J. Novel 3D auxetic lattice structures developed based on the rotating rigid mechanism. Int. J. Solids Struct. (2021).233(August). 111232.
- 440. Cross T.M., Hoffer K.W., Jones D.P., Kirschner P.B., Meschter J.C. Auxetic Structures And Footwear With Soles Having Auxetic Structures (US 2015/0075034 A1). Vol. 1. 2015.
- 441. Moroney C. The Application of Auxetic Structures for Rugby Shoulder Padding (PhD Thesis, Manchester Metropolitan University). (**2021**).
- 442. Li Z., Chen W., Hao H. Numerical study of open-top truncated pyramid folded structures with interconnected side walls against flatwise crushing. Thin-Walled Struct. (2018).132(September). 537–48.
- 443. Li Z., Chen W., Hao H. Blast mitigation performance of cladding using square domeshape kirigami folded structure as core. Int. J. Mech. Sci. (2018).145(July). 83–95.
- 444. Shiffer I., Hertz K., Tu D., Heller L. Ecohelmet. (**2017**) [accessed 2023 Apr 14]. https://www.ecohelmet.com/
- 445. nTopology. (2023). https://www.ntop.com/
- 446. Hyperganic. (2023) [accessed 2023 Aug 14]. https://www.hyperganic.com/

| 1 | |
|----------------------------|--|
| 2 | |
| 3 | |
| 4 | |
| 5 | |
| 6 | |
| 7 | |
| 8 | |
| 9 | |
| 10 | |
| 11 | |
| 12 | |
| 13 | |
| 12 13 14 15 16 | |
| 15 | |
| 16 | |
| 17 | |
| 18 | |
| 19 | |
| 20 | |
| 21 | |
| 22 | |
| 22 23 | |
| 24 | |
| 25 | |
| 26 | |
| 27 | |
| 28 | |
| 29 | |
| 30 | |
| 31 | |
| 32 | |
| 33 | |
| 34 | |
| 35 | |
| 36 | |
| 37 | |
| 38 | |
| 39 | |
| 40 | |
| 40 41 | |
| 41 | |
| 43 | |
| 44 | |
| 44 | |
| 45 46 | |
| 40 47 | |
| 47 48 | |
| 40 49 | |
| 49 50 | |
| 50 51 | |
| 51 52 | |
| 52 53 | |
| | |
| 54 | |
| 55 | |
| 56 | |
| 57 | |
| 58 | |
| 59 | |

- 447. Rhino. (2023) [accessed 2023 Aug 14]. https://www.rhino3d.com/6/new/grasshopper/
- 448. Hearmon R.F. An Introduction to Applied Aniso-tropic Elasticity. London, UK: Oxford University Press; (**1962**).pp.12p.
 - 449. Masters I.G., Evans K.E. Models for the elastic deformation of honeycombs. Compos. Struct. (1996).35(4). 403–22.
 - 450. Eringen A.C. Microcontinuum Field Theories. 1st ed. New York: Springer Science+Business Media; (1999).
 - 451. Lakes R. Experimental micro mechanics methods for conventional and negative poisson's ratio cellular solids as cosserat continua. J. Eng. Mater. Technol. Trans. ASME. (1991).113(1). 148–55.
- 452. Lakes R., Drugan W.J. Bending of a Cosserat Elastic Bar of Square Cross Section: Theory and Experiment. J. Appl. Mech. Trans. ASME. **(2015)**.82(9). 1–16.
- 453. Nightingale M., Hewson R., Santer M. Multiscale optimisation of resonant frequencies for lattice-based additive manufactured structures. Struct. Multidiscip. Optim. (2021).63(3). 1187–201.
- 454. Pan F., Li Y., Li Z., Yang J., Liu B., Chen Y. 3D Pixel Mechanical Metamaterials. Adv. Mater. (2019).31(25). 1–8.
- 455. Wang Y., Groen J.P., Sigmund O. Simple optimal lattice structures for arbitrary loadings. Extrem. Mech. Lett. (2019).29. 100447.
- 456. Andreassen E., Clausen A., Schevenels M., Lazarov B.S., Sigmund O. Efficient topology optimization in MATLAB using 88 lines of code. Struct. Multidiscip. Optim. (2011).43(1). 1–16.
- 457. Sigmund O. A 99 line topology optimization code written in Matlab. Struct. Multidiscip. Optim. **(2001)**.21(1999). 120–7.
- 458. Murphy R., Imediegwu C., Hewson R., Santer M. Multiscale structural optimization with concurrent coupling between scales. Struct. Multidiscip. Optim. (2021).63(4). 1721–41.
- 459. Mehreganian, N., Fallah, A. S., Sareh, P. Impact response of negative stiffness curvedbeam-architected metastructures. International Journal of Solids and Structures. (**2023**).179, 112389.
- 460. Chen, Y., Shi, J., He, R., Lu, C., Shi, P., Feng, J., Sareh, P. A unified inverse design and optimization workflow for the Miura-oRing metastructure. Journal of Mechanical Design. (**2023**).145(9).
- 461. Pinho-da-Cruz J., Oliveira J.A., Teixeira-Dias F. Asymptotic homogenisation in linear elasticity. Part I: Mathematical formulation and finite element modelling. Comput. Mater. Sci. (2009).45(4). 1073–80.
- 462. Oliveira J.A., Pinho-da-Cruz J., Teixeira-Dias F. Asymptotic homogenisation in linear elasticity. Part II: Finite element procedures and multiscale applications. Comput. Mater. Sci. (2009).45(4). 1081–96.
- 463. Cioranescu D., Donato P. Introduction to homogenization. Oxford University Press; (1999).
- 464. Carstensen J. V., Lotfi R., Chen W., Szyniszewski S., Gaitanaros S., Schroers J., et al. Topology-optimized bulk metallic glass cellular materials for energy absorption. Scr. Mater. **(2022)**.208. 114361. https://doi.org/10.1016/j.scriptamat.2021.114361
- 465. Carstensen J. V, Lotfi R., Guest J.K. Topology Optimization of Cellular Materials for Properties Governed by Nonlinear Mechanics. In: 11th World Congress on Structural and Multidisciplinary Optimization. (**2015**). pp. 1–6.
- Carstensen J. V., Guest J.K., Lotfi R. Topology optimization of nonlinear cellular materials. In: 17th AIAA/ISSMO Multidisciplinary Analysis and Optimization Conference. (2016). pp. 1–10.
- 467. Wu L., Mustafa M., Segurado J., Noels L. Second-order computational homogenisation enhanced with non-uniform body forces for non-linear cellular materials and metamaterials. Comput. Methods Appl. Mech. Eng. **(2023)**.407. 115931.
- 468. Earnshaw J., Duncan O., Kaczmarczyk L., Syrotiuk N., Byres J., Scarpa F., et al. Meta-Genome. (**2023**) [accessed 2023 Mar 27]. https://meta-genome.org/
- 469. Johnston R., Kazancı Z. Analysis of additively manufactured (3D printed) dual-material

auxetic structures under compression. Addit. Manuf. (2021).38(November 2020). 101783. https://doi.org/10.1016/j.addma.2020.101783

- 470. Wang K., Chang Y.H., Chen Y., Zhang C., Wang B. Designable dual-material auxetic metamaterials using three-dimensional printing. Mater. Des. (2015).67. 159–64.
- 471. Gao D., Wang B., Gao H., Ren F., Guo C., Ma S., et al. Strain Rate Effect on Mechanical Properties of the 3D-Printed Metamaterial Foams With Tunable Negative Poisson's Ratio. Front. Mater. **(2021)**.8(August). 1–12.
- Cervinek O., Pettermann H., Todt M., Koutny D., Vaverka O. Non-linear dynamic finite element analysis of micro-strut lattice structures made by laser powder bed fusion. J. Mater. Res. Technol. (2022).18. 3684–99.
- 473. Mauko A., Fíla T., Falta J., Koudelka P., Rada V., Neuhäuserová M., et al. Dynamic deformation behaviour of chiral auxetic lattices at low and high strain-rates. Metals (Basel). (2021).11(1). 1–15.
- 474. Qi J., Chen Z., Jiang P., Hu W., Wang Y., Zhao Z., et al. Recent Progress in Active Mechanical Metamaterials and Construction Principles. Adv. Sci. (2022).9(1). 1–27.
- 475. Levine D.J., Turner K.T., Pikul J.H. Materials with Electroprogrammable Stiffness. Adv. Mater. (2021).33(35). 1–26.
- 476. Mills N.J. Polymer Foams Handbook: engineering and biomechanics applications and design guide. Elsevier; (2007).
- 477. HeadHealthTECH Helmet Challenge Grants. (**2020**) [accessed 2023 Apr 6]. https://www.nfl.com/playerhealthandsafety/equipment-andinnovation/headhealthtech/headhealthtech-challenges