Satellite edge computing for real-time and very-high resolution Earth observation

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Abstract—In high-resolution Earth observation imagery, Low Earth Orbit (LEO) satellites capture and transmit images to ground to create an updated map of an area of interest. Such maps provide valuable information for meteorology and environmental monitoring, but can also be employed for realtime disaster detection and management. However, the amount of data generated by these applications can easily exceed the communication capabilities of LEO satellites, leading to congestion and packet dropping. To avoid these problems, the Inter-Satellite Links (ISLs) can be used to distribute the data among multiple satellites and speed up processing. In this paper, we formulate a satellite mobile edge computing (SMEC) framework for real-time and very-high resolution Earth observation and optimize the image distribution and compression parameters to minimize energy consumption. Our results show that our approach increases the amount of images that the system can support by a factor of $12\times$ and $2\times$ when compared to directly downloading the data and to local SMEC, respectively. Furthermore, energy consumption was reduced by 11% in a real-life scenario of imaging a volcanic island, while a sensitivity analysis of the image acquisition process demonstrates that energy consumption can be reduced by up to

Index Terms—Earth observation, Low Earth Orbit (LEO) satellite communications, satellite imagery, satellite mobile edge computing (SMEC).

I. INTRODUCTION

Satellites in Low Earth Orbit (LEO) are widely used for Earth observation purposes as they can construct high-resolution maps of large areas by capturing images from space as they orbit the Earth. These maps can be used in in various applications, as in meteorology, agriculture, or environmental monitoring [1]. They are also very valuable in near-real time applications, such as disaster detection and

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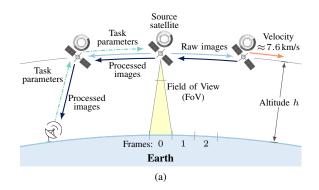
identification, supporting the coordination of the emergency response. Due to the limited storage in the individual LEO satellites, the images must be 1) captured, 2) processed for compression and/or optical correction, and 3) transmitted to ground for storage and/or distribution across the terrestrial infrastructure.

The area covered by each individual satellite image depends on numerous factors. Namely, the field of view (FoV) of the instrument/camera is the angle that determines the observable space of the camera sensor. The FoV together with the altitude of deployment of the satellite determine the *swath*, which is the width of the observable area on the surface of the Earth. Then, the swath and the resolution of the instrument/camera determine the ground sample distance (GSD), which is the distance covered by each single pixel. As an example, the European Space Agency (ESA) Sentinel-2 mission is located at an altitude of 748 km and captures images in the visible spectrum with a GSD of 1.5 m [2]. In total, the swath for Sentinel-2's visible spectrum instrument is only 60 km. Other common values for the GSD are in the range between 0.3 and 3 meters [3], [4].

To achieve a high image resolution, the GSD must be small and, in turn, so does the area covered by a single image. For example, the area covered by an image in high-definition (HD) format with a GSD of 3 m is around 18 km², which is smaller than several European airports. Therefore, high-resolution maps of large areas must be created by capturing and organizing a large number of images. These images must be captured with a sufficiently high frequency to avoid coverage holes in the map.

Traditionally, Earth observation satellites would communicate directly with a ground station (GS) to download the collected data. However, this greatly limits the amount of data that can be collected. In contrast, modern Earth observation missions possess numerous satellites with advanced communications and processing capabilities. For instance, recent advances in free-space optical (FSO) communications technology [5], in combination with the stable relative positions of satellites in the same orbital plane, make it possible to establish intra-plane Inter-Satellite Links (ISLs) to connect neighboring satellites in the same orbital plane using high-data rate FSO links. Such links can be used to distribute the images across the neighboring satellites, forming a satellite mobile edge computing (SMEC) cluster with distributed processing capabilities.

Fig. 1 illustrates an Earth observation mission relying on



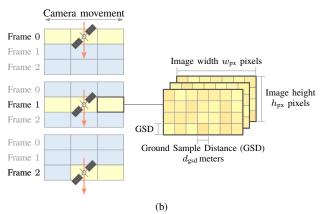


Fig. 1. Earth observation application where the source satellite scans the area of interest. (a) The FoV and the altitude of the satellites determine the area covered by each image. The raw images captured by the source satellite, in the middle of the figure, can be shared with the nearby satellites to process them in a distributed manner and, then, send them to the GS. (b) The source satellite captures a frame, consisting of W_k images, at slot k as indicated by the yellow area. The value of W_k may be different for each k depending on the dimensions of the area of interest.

a SMEC cluster to distribute the data to be processed and compressed by multiple satellites before being downloaded to the GS. As it can be seen, the orbital velocity of the satellite creates the need to capture images frequently to avoid coverage holes and the frequency is determined by the FoV and the altitude of the satellite. Specifically, the maximum period at which the images must be captured to avoid coverage holes is called the ground track frame period (GTFP), which imposes the timing constraints in the satellite processing and communication subsystems. In such setup, illustrated in Fig. 1b, the system operation can be divided into time slots. At each time slot, the satellite scans the area of interest by capturing a set of side-by-side images called a frame. Then, to maintain the stability in the processing and communication subsystems at the satellites, the time needed for processing and for communication at each link must be lower than that of the duration of a time slot. This is the scenario of interest for the present paper.

The generation of enormous amounts of data in Earth observation applications is a common concern, especially regarding the downlink capacity (i.e., satellite-to-ground link). Moreover, as satellites rely on solar panels and rechargeable batteries for energy supply, minimizing the energy consumption of

the communication and processing task at the satellites is of utmost importance. Nevertheless, the research on SMEC to reduce the amount of data transmission and energy consumption in Earth observation applications is still in its infancy. Specifically, most of the literature on SMEC, with a few clear exceptions [3], [4] that include our previous work [6], deals with tasks generated at the mobile users and, hence, mimics the traditional functionality of a terrestrial mobile edge computing (MEC) but substituting the terrestrial edge nodes with satellites [7]. Currently, SMEC approaches for Earth observation can be divided into: early discard [3], [4] and compression [6]. Early discard of images with relatively low information content (e.g., cloud coverage) effectively reduces the amount of data transmitted to ground [3], [4]. Note that the efficiency of early discard is mostly based on autonomous decisions at the satellites, which determine which images to transmit to ground and which ones to discard. Even though this inference process can be enhanced with techniques such as image-chain simulation (ICS) to evaluate the quality of the captured images [8], it may be problematic for missioncritical applications, for example, emergency scenarios, where partially obstructed images can still be valuable for the GS. To avoid these problems, the satellites might instead execute an algorithm to compress the collected data. For example, new video coding implementations for satellite Earth observation focus on achieving a sufficiently high encoding rate and compression ratio so the video frames can be compressed and transmitted to the GS based on the limitations of the downlink and processing modules [9]. The authors in [9] focus on the algorithmic implementations in a scenario with a single satellite and fixed downlink data rate and do not optimize the coding process for energy efficiency. Even though the proposed algorithm improved the execution time of the video coding process, it might still be restrictive for video applications requiring a high frame rate video. Thus, this scenario presents a good candidate for the distribution and parallel processing of the video frames at multiple satellites as proposed in the present paper.

While the literature on SMEC for Earth observation focuses on local processing of the data, there are numerous examples of terrestrial MEC and SMEC that consider the optimization of distributed processing, which is a generalization of local processing. For example, lossless compression was considered to occur both at the source mobile device and at the edge server in a terrestrial MEC to reach a combined compression ratio [10]. In a similar fashion, the benefits of offloading computation tasks from mobile users in remote areas to a SMEC network were studied in [11], which builds on recent literature on SMEC architectures [12]-[15]. In [11], authors propose a three-tier scheme where the tasks with low computational complexity are directly processed at the mobile users and the rest are distributed either to a ground cloud or to the satellite edge. The complex allocation problem is solved with the alternating direction method of multipliers (ADMM).

In our previous work [6], we focused on an Earth observation scenario with power allocation for communication and where the source satellite chooses between directly downloading the data or compressing it locally. The present paper

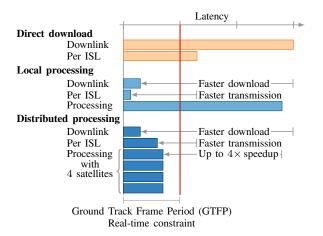


Fig. 2. Illustration of the different options for data delivery in high-resolution Earth observation: direct download, local processing, and distributed processing.

represents a major extension of our previous work and a major deviation with respect to the SMEC literature described above by considering real-time high-resolution Earth observation applications where the real-time requirements are defined by the dynamics of the system. In the considered scenario, we consider a general SMEC framework for real-time and very-high resolution Earth observation that involves five phases:

1) segmentation of the imaging data, 2) allocation of the processing tasks, 3) distribution of the image segments (i.e, scatter), 4) processing of the image segments, and 5) delivery of the processed images to the ground station (i.e., gather).

Fig. 2 illustrates the diverse options for executing a task with the GTFP as real-time constraint. The data can be directly downloaded to the GS. However, this might may cause backlog in the satellite-to-GS and ISL links due to their limited data rate for communication. On the other hand, the data can be processed locally at the source satellite. However, this might cause backlog at the CPU of the source satellite due to the limited processing power. Finally, the data can be distributed across 4 satellites, which alleviates the load in both the communication links and at the individual CPUs by reducing the amount of data to be transmitted at each individual link and to be processed at each CPU. By doing so, the real-time constraint defined by the GTFP is fulfilled, which guarantees the stability of the communication and processing subsystems.

The main contributions of this paper are described in the following.

- We define a novel and general model for high-resolution Earth observation imagery, along with its real-time constraints imposed by the physical (i.e., orbital) parameters of LEO constellations and of the imaging instruments.
- 2) We formulate and solve a global optimization problem for the segmentation, allocation, and processing phases of our general SMEC framework. Given that the satellites have a limited battery supply, the objective of distributing the tasks across the satellites in the constellation is to minimize the overall energy consumption while fulfilling the limitations of the processing frequency at the satellites' CPU, and the rates at the

ISLs and satellite-to-ground link. The present work is a major extension of our previous study [6], where we only considered local edge computing and cloud computing, a single and homogeneous task at the satellites, a fixed CPU frequency, and a fixed compression ratio. In the present paper, we consider the optimization with distributed processing, where the set of satellites participating in the processing, the CPU frequency, and the compression ratio are optimization variables. Hence, the optimization problem considered in this paper is a generalization of the one considered in our previous work [6].

3) We consider a realistic imaging data size and perform both 1) a sensitivity analysis of the impact of the data generation process on the optimal solution of the problem and 2) a case study that validates our approach and illustrates of the potential gains of the global optimal solution in a real-life scenario.

In the baseline scenarios, our results show that the number of images that can be transmitted to the GS with our SMEC approach is up to $12 \times$ larger when compared to direct download without processing and up to $2 \times$ larger when compared to processing at the source satellite. Furthermore, the energy consumption of our SMEC approach is up to $10\times$ lower than with direct download. Finally, when compared to optimizing each frame independently, jointly optimizing the task parameters for the whole task with K frames leads to energy savings of up to 90% in the baseline scenarios with a relatively low number of images per frame. In the real-life scenario, where a satellite scans the island of La Palma, our results show that the energy consumption can be reduced at up to 11% by optimizing the task parameters for the K=82 frames when compared to optimizing for each frame independently This scenario is only feasible with distributed SMEC, as both direct download without processing and local processing approaches would lead to buffer overflows in the communication and/or processing buffers of the satellites.

The rest of the paper is organized as follows. Section II describes the system model. Next, the optimization problem is formulated in Section III, numerical results are presented in Section IV, and concluding remarks are given in Section V.

II. SYSTEM MODEL

A. Framing

We consider an orbital plane (i.e., ring) in a LEO satellite constellation and a GS g. The orbital ring is comprised of N satellites uniformly spaced along the orbit and deployed at an altitude h km above the Earth's surface. The satellites possess, among other subsystems, a camera, a processing payload, and communication modules to establish a radio frequency link towards the GS as well as high-data rate FSO ISLs with the two neighboring satellites. Hence, the satellites in the orbital plane form a ring topology.

The satellites in the orbital plane serve an Earth observation application with pre-planned tasks. Each task involves capturing images to scan a specific area of interest, which must be transmitted to the GS. The camera is used to capture images

TABLE I
PARAMETERS DEFINED IN THE SYSTEM MODEL

Symbol	Description
Scenario	
N	Number of satellites in the orbital plane
h	Altitude of deployment of the satellites [m]
h_{px}	Height of each image [pixels]
w_{px}	Width of each image [pixels]
q_{px}	Amount of bits per pixel
D_{img}	Size of each image [bits]
W_k	Number of side-by-side images in frame k
$d_{ m gsd}$	Average ground sampling distance [m]
$T_{\mathrm{GTF}}(h_{\mathrm{px}}, d_{\mathrm{gsd}}, h$) Ground track frame period (GTFP) [s]
Processing	
$f_{ m CPU}$	Highest CPU frequency [Hz]
$f_k^{(n)}$	CPU frequency [Hz] for processing at satellite n and frame k
$N_{ m CPU}$	Number of available processing cores per satellite
$ ho_k$	Compression ratio for frame k
ϵ	Parameter that determines the complexity of the compression algorithm
$C(\rho_k, \epsilon)$	Number of CPU cycles to compress one bit of data
Communication	
R_k	Data rate to transmit frame k to the GS [bps]
$P_{ m RF}^{ m tx}$	Transmission power for RF satellite-to-ground links [W]
$R_{ m ISL}$	Fixed data rate at the ISLs [bps]
$P_{ m ISL}$	Power consumption of the ISLs during transmission [W]
η	Fraction of $P_{\rm ISL}$ consumed due to data transmission
Segment allocation	
$X \in \mathbb{Z}^{K,N}$	Segment allocation matrix [bits]
$\mathbf{x}_k \in \{0, 1, \dots, n\}$	$\{D_k\}^N$ Segment allocation vector for frame k [bits]
$x_k^{(n)} \in \{0, 1, \dots$	$\{D_k\}$ Segment allocation for satellite n and frame k [bits]

of a fixed size

$$D_{\rm img} = w_{\rm px} \, h_{\rm px} \, q_{\rm px} \, {\rm bits}, \tag{1}$$

where $w_{\rm px}$ and $h_{\rm px}$ are the width and height in pixels and $q_{\rm px}$ is the number of bits to represent each pixel. Throughout this article, we assume that $h_{\rm px} < w_{\rm px}$ is aligned with the velocity vector of the satellite (i.e., the roll axis). The satellites capture images by pointing directly towards the Earth and by rotating the camera perpendicularly to the velocity vector as illustrated in Fig. 1b. Therefore, the satellite itself must enter the area of interest to start capturing the images.

The average distance between adjacent pixel centers $d_{\rm gsd}$ taken when pointing directly at the nadir point is called the GSD, which is a function of $w_{\rm px}$, the FoV, and the satellite altitude h [3]. The area covered by a single image is

$$A \approx w_{\rm px} h_{\rm px} d_{\rm osd}^2 \tag{2}$$

and the vertical distance-aligned with the roll axis of the satellite-covered is $h_{\rm px}d_{\rm gsd}$ m.

The task and, similarly, the operation of the system are divided into K time slots of duration equal to the GTFP.

At each time slot k, the source satellite v_0 captures a frame comprised of $W_k \in \mathbb{N}^+$ side-by-side images by rotating the camera perpendicularly to its velocity vector to cover the area of interest as it moves. The number of images W_k can be different for each frame in a task as exemplified in Fig. 1b, where frame $W_0 = W_1 = 3$ images and $W_2 = 2$.

We assume that the time to capture the W_k images in a frame and to make them available for the processing algorithm and the communication modules (i.e., to write the data in memory) does not impact the real-time constraints of the system. The resulting size of the k-th frame is $D_k = W_k D_{\rm img}$ bits and the frame is approximately $W_k w_{\rm px} d_{\rm gsd}$ meters wide.

Capturing frames at exactly the GTFP ensures that there are no coverage gaps, but also that there are no two pixels that cover the same area in two consecutive frames taken by the same satellite. To calculate the GTFP, let $T_o(h)$ be the orbital period of a satellite deployed at altitude h. Then, $T_o(h)$ can be closely approximated as

$$T_o(h) \approx \sqrt{\left(\frac{4\pi^2}{GM_E}\right) (R_E + h)^3},$$
 (3)

where G is the universal gravitational constant; M_E and R_E are the mass and radius of the Earth, respectively. The GTFP, denoted as $T_{\rm GTF}$, is given as

$$T_{\rm GTF}(h_{\rm px}, d_{\rm gsd}, h) = \frac{h_{\rm px} d_{\rm gsd} T_o(h)}{2\pi R_E}. \tag{4}$$

We define $t_k = kT_{\text{GTF}}$ as the time when frame k is captured by the satellite and, hence, $t_0 = 0$.

The frames may be processed before they are sent to ground, which involves, for example, correction of optical anomalies, compression, and encoding. Specifically, a frame captured by the source satellite v_0 , can be processed either locally or in a distributed manner to reduce its size by a compression factor $\rho > 1$, such that the resulting size of the frame is D_k/ρ .

B. SMEC framework

In the following, we describe a general SMEC framework for real-time and very-high resolution Earth observation where the task instructs a source satellite v_0 to capture K consecutive frames. The frameworks is based on classical communication models for distributed processing architectures, but considers the distinctive characteristics of LEO satellite communications, such as limited bandwidth and links with heterogeneous capacity.

- 1) Segmentation: At each time slot $k \in \{1, 2, ..., K\}$, where K is the total number of frames in the task, the source satellite v_0 captures a frame k with W_k images for a total size D_k bits and divides it into segments.
- 2) Allocation: Each of the satellites in the SMEC cluster for frame k, namely $n \in \mathcal{N}_k$, will receive a segment, which is a fraction $x_k^{(n)}$ of the total amount of data in the frame. The GS might also indicate a fraction of the frame $x_k^{(g)}$ that will not be processed by the satellites but downloaded directly without processing.

- 3) Scatter: The source satellite distributes the segments to all the satellites in the SMEC cluster $n \in \mathcal{N}_k$ using high-data rate ISLs. The rest of the data are routed directly to the GS without processing.
- 4) Distributed processing: The segments are processed at the satellites, with a consequent reduction in the size of the data by a factor ρ_k , called the compression ratio. Hence, the resulting size of the segment processed by satellite n is $x_k^{(n)}/\rho_k$. The CPU frequency selected to process the k-th frame at satellite n is denoted as $f_k^{(n)}$.
- 5) Gather: Once processing is completed, the satellites in the SMEC cluster \mathcal{N}_k send the processed segments to the GS through the destination satellite v_d .

C. Compression

Let $C(\rho_k,\epsilon)$ be the complexity of the compression algorithm, defined as the number of CPU cycles to compress one bit of data by a compression ratio ρ_k , being ϵ a positive constant that depends on the compression algorithm. In traditional and pure JPEG compression, the complexity can be considered as constant w.r.t. the compression ratio ρ_k since the latter is only determined by the entries of the quantization matrix, which does not affect the number of operations to be performed. Nevertheless, setting a constant compression complexity might only represent a small subset of possible compression algorithms.

Instead, we adopt a model where the complexity of the compression algorithm increases exponentially with the compression ratio as $C(\rho_k,\epsilon)=e^{\epsilon\rho_k}-e^{\epsilon}$ [16]. This latter model covers several popular compression techniques, such as Zlib, Zstandard, and XZ compression and makes our optimization framework more general. Consequently, by selecting the exponential model for the complexity of the compression algorithm, our framework is applicable to a much wider range of compression algorithms than the constant complexity model for JPEG. Furthermore, as it will be seen in Section III, adoption of the exponential model creates a trade-off between the energy used for processing and for communication. In contrast, selecting the optimal compression ratio under a constant complexity model for the formulated optimization problem would be trivial.

To process and compress the images, the processing payload of the satellites consists of a CPU with N_{CPU} cores and a maximum clock frequency f_{CPU} . The satellites are able to adapt the CPU clock frequency for each frame $k \in \mathcal{K}$ in the task through Dynamic Voltage and Frequency Scaling (DVFS), which allows to reduce the energy consumption of tasks with relaxed latency requirements. Therefore, we define $f_k^{(n)}$ as the CPU clock frequency selected by satellite $n \in \mathcal{N}$ to process the data belonging to frame k.

Let T_k^{proc} be the execution time of the image processing algorithm for a frame in task k, which is given, for satellite n, as

$$T_k^{\text{proc}}(n, D_k, \rho, f_k; \epsilon, N_{\text{CPU}}) = \frac{D_k C(\rho, \epsilon)}{N_{\text{CPU}} f_k^{(n)}}.$$
 (5)

The processing of the data received by the satellites is managed by a scheduler that operates in a first-in first-out fashion. Hence, it may need to queue the processing of a segment until the processing of the previous one is completed and the CPU is available. Specifically, we denote the queueing time to process the data received at time t at satellite n as $Q_t^{\rm proc}(n) \in \mathbb{R}^+$ seconds. In other words, the data received at time t must wait in the queue of satellite n until time $t+Q_t^{\rm proc}(n)$ before it can be processed. Throughout this paper, we focus on maintaining the stability of the processing queues rather than on their impact on the overall latency.

D. Communication

After processing, the resulting data must be transmitted to the GS g. The communication modules are used to establish communication with the satellites in the same orbital plane via the intra-plane ISLs, and with g. Specifically, intra-plane ISLs are established with the two neighboring satellites in the same orbital plane and a downlink satellite-to-ground link is established between g and the closest satellite. Let $\mathcal{G}_k = (\mathcal{V}, \mathcal{E}_k)$ be the directed graph that represents the system at time t_k , where $\mathcal{V} = \mathcal{N} \cup \{g\}$ is the vertex set and \mathcal{E}_k is the edge set at time t_k . As mentioned above, we consider a time-slotted system and, hence, update graph \mathcal{G}_k along with its parameters by taking a snapshot at the beginning of each time slot.

Without loss of generality, we denote the source satellite as v_0 and the destination satellite, which has a direct connection to the GS, as v_d . The directed edges $(u,v) \in \mathcal{E}_k$ represent the full-duplex communication links, which are assumed to remain fixed within the interval $[t_k,t_{k+1}]$. A path from vertex v_0 to vertex v_d is called a v_0-v_d path and denoted as $\mathcal{P}_k(v_0,v_d)=(v_0,v_1,\ldots,v_d)$, where $v_0,v_1,\ldots,v_d \in \mathcal{V}$ and $\ell\left(\mathcal{P}_k(u,v)\right)$ is the length of the path.

High-data rate FSO links are considered for the intra-plane ISLs since the relative distances and positions among these satellites are maintained, which minimizes pointing errors [5]. As a consequence, the intra-plane ISLs are fixed throughout the operation of the network and also possess a fixed data rate $R_{\rm ISL}$ and consume a fixed amount of power during transmission $P_{\rm ISL}$.

Point-to-point satellite-to-ground links are established dynamically between the GS and the closest available satellite. Therefore, we define the edge set at time k as

$$\mathcal{E}_k = \left\{ (u, v) \cup (v_d, g) : u, v \in \mathcal{N}, v_d = \operatorname*{arg\,min}_{v \in \mathcal{N}} d_{t_k}(v, g) \right\},\$$
(6)

where $d_{t_k}(v,g)$ is the Euclidean distance between satellite v and g at time t_k . The latter can be accurately calculated based on the ephemeris of the satellites for any $t_k \in \mathbb{R}$ and, hence, our model operates with snapshots of the edge set taken at each t_k .

Differently from the intra-plane ISLs, the beams and data rate must be adapted continuously at the downlink due to the rapid movement of the satellites. Traditional RF technology is less prone to outages due to pointing errors and atmospheric conditions than FSO and, hence, it is used to achieve reliable communication to the GS.

We consider an interference-free additive-white Gaussian noise (AWGN) channel with free-space path loss and with noise power σ^2 . Hence, the signal-to-noise ratio (SNR) for the satellite-to-ground link (i.e., downlink) at time t is given as

$$\gamma_t = G_{tx} G_{rx} P_{RF}^{tx} \left(\frac{c}{4\pi d_t(v_d, g) f_c \sigma} \right)^2,$$
where $v_d = \arg \min_{v} d_t(v, g)$ (7)

where f_c is the carrier frequency, $c=2.998\cdot 10^8$ m/s is the speed of light, G_d and G_g are the transmitter and receiver antenna gains, and $P_{\rm RF}^{\rm tx}$ is the transmission power.

Once the SNR is known, a proper modulation and coding scheme can be selected as follows. Let $\mathcal{R}_{\text{DVB}}=\{R'\}$ be the set of available rates R' in b/s/Hz defined in the DVB-S2X system. Next, let $\gamma_{\min}(R') \geq 2^{R'}-1$ be the minimum required SNR to achieve a block error rate $<10^{-5}$ with rate R'. Then, the modulation and coding scheme for downlink communication is selected to achieve the data rate

$$R_k = B \max \{ R' \in \mathcal{R}_{\text{DVB-S2}} : \min \{ \gamma_t \} \ge \gamma_{\min}(R'),$$

$$t \in [t_k, t_k + \Delta t] \}. \quad (8)$$

That is, the rate is selected using the thresholds defined in the DVB-S2X system [17] and R' is a valid rate for downlink communication at time slot k if and only if the SNR for this link is greater than $\gamma_{\min}(R')$ throughout the whole time slot.

Similarly as for processing, we denote the queueing time at the communication module to transmit the data from u to v as $Q_t^{\text{trans}}(u,v) \in \mathbb{R}^+$ seconds, where t is the time at which the data is received by u. Furthermore, we define the transmission time for a packet of size D_k as

$$L_k^{\text{trans}}(D_k, u, v) = \frac{D_k}{R_k(u, v)},\tag{9}$$

where $R_k(u, v) = R_{ISL}$ for all the ISLs and $R_k(v_d, g) = R_k$ for the downlink.

E. Energy consumption

In the considered problem, there are two contributors of interest to the energy consumption at the satellite: the processing and compression of the images, and the communications.

We consider a model for the energy consumption of the satellites due to the processing of the task that captures the most relevant CPU parameters [18]–[20]. In this model, the energy consumption of the CPU per clock cycle is proportional to the square of its clock frequency $f_k^{(n)}$ times a constant ν , which is the effective capacitance coefficient [19], [20]. Specifically,

$$E_{\rm cycle}^{\rm proc}\left(f_k^{(n)}\right) = \nu \, \left(f_k^{(n)}\right)^2 = \frac{P_{\rm proc}(f_{\rm CPU})}{f_{\rm CPU}^3} \, \left(f_k^{(n)}\right)^2, \quad (10)$$

where $P_{\text{proc}}(f_{\text{CPU}})$ is the power consumption during processing at the maximum CPU frequency. Building on this, and assuming that the supplied power is linear with the number of

processor cores N_{CPU} , the energy consumption to process an image of size D_k bits is modeled as

$$E_k^{\text{proc}}\left(\rho_k, f_k^{(n)}; D_k, \epsilon\right) = D_k C(\rho_k, \epsilon) E_{\text{cycle}}^{\text{proc}}\left(f_k^{(n)}\right). \tag{11}$$

Regarding the energy consumption during communication, we consider a model that includes the energy due to data transmission, the inefficiency of the power amplifiers, and the static power consumption of the communication modules [21]. Consequently, the power consumption for the RF downlink during communication $P_{\rm RF}$ is modeled as a function of the power consumption due to data transmission $P_{\rm RF}^{\rm tx}$, inefficiency of the power amplifier $\mu_{\rm RF}^{\rm amp}$, and the static power consumption $P_{\rm RF}^{\rm static}$, as

$$P_{\rm RF} = \mu_{\rm RF}^{\rm amp} P_{\rm RF}^{\rm tx} + P_{\rm RF}^{\rm static}. \tag{12}$$

We assume that the RF link of the destination satellite v_d consumes $P_{\rm RF}^{\rm static}$ at all times and, hence, is not considered to evaluate the energy consumption of the SMEC framework. Then, during data transmission, the v_d consumes an extra $\mu_{\rm RF}^{\rm amp} P_{\rm RF}^{\rm tx}$ W and the energy consumption due to transmit D_k bits of data in the downlink is

$$E_{RF}^{trans}(D_k) = \frac{\mu_{RF}^{amp} P_{RF}^{tx} D_k}{R_k}$$
 (13)

Similarly, the power consumption for the FSO ISLs during communication can be divided into the power consumption due to data transmission $P_{\rm ISL}^{\rm tx}$, the inefficiency of the power amplifier $\mu_{\rm amp}$, and the static power consumption $P_{\rm ISL}^{\rm static}$, and is given as [21]

$$P_{\rm ISL} = \mu_{\rm ISL}^{\rm amp} P_{\rm ISL}^{\rm tx} + P_{\rm ISL}^{\rm static}.$$
 (14)

In our model for the FSO links, we consider that P_{ISL} is fixed and define the parameter

$$\eta = \frac{\mu_{\text{ISL}}^{\text{amp}} P_{\text{ISL}}^{\text{tx}}}{\mu_{\text{ISL}}^{\text{amp}} P_{\text{ISL}}^{\text{tx}} + P_{\text{ISL}}^{\text{static}}} \in [0, 1].$$
 (15)

Therefore, we consider that $\eta P_{\rm ISL} = \mu_{\rm ISL}^{\rm amp} P_{\rm ISL}^{\rm tx}$ is consumed during data transmission [21]. The remaining $(1-\eta)P_{\rm ISL} = P_{\rm ISL}^{\rm static}$ is the static power consumption of the FSO ISLs. Hence, the energy consumption to transmit D_k bits of data through an FSO ISL is

$$E_{\rm ISL}^{\rm trans}(D_k) = \frac{\eta P_{\rm ISL} D_k}{R_{\rm ISL}}.$$
 (16)

III. PROBLEM FORMULATION

A task might consist of one or multiple frames, namely K, that are captured continuously by a source satellite v_0 . Each of the k frames contains $W_k \in \{0,1,\ldots,\}$ images. The GS schedules the segmentation, processing, and transmission of the segments in a task jointly using its knowledge about the communication and processing capabilities of the satellites, along with the value of W_k for all $k \in \mathcal{K}$. For this, the GS builds an allocation matrix $\mathbf{X} \in \mathbb{N}^{K \times N+1}$, whose (k,n)-th element is $x_k^{(n)}$, indicating the amount of data from frame k that satellite k must process. Moreover, we denote the k-th row of \mathbf{X} as

$$\mathbf{x}_k = \left[x_k^{(1)}, x_k^{(2)}, \dots, x_k^{(N)}, x_k^{(g)} \right], \tag{17}$$

which is the allocation vector for frame k. Naturally,

$$\mathbf{x}_{k}\mathbf{1} = \sum_{n=1}^{N} x_{k}^{(n)} + x_{k}^{(g)} = D_{k}$$
 (18)

and the number of segments for frame k is the number of non-zero elements in vector \mathbf{x}_k .

The segment allocation is accompanied by matrix $\mathbf{F} \in \mathbb{R}_+^{K \times N}$, whose (k,n)-th element is $f_k^{(n)}$ and defines the CPU frequency that must be selected by the satellite n for processing the segment from frame k. Finally, the GS must define the compression factor for each frame, defined by the vector $\boldsymbol{\rho} = [\rho_1, \rho_2, \dots, \rho_K]$.

We follow a resource slicing approach to ensure the stability of the processing and communication queues in the orbital plane. In such approach, the task is allocated an amount of processing and communication resources that is proportional to its duration $KT_{\rm GTF}$. Therefore, the processing and communication parameters for the task values must be selected to ensure that the average processing and transmission time of each segment, at each satellite and each link does not exceed the GTFP. Building on this, we formulate the following constraints.

Processing constraint: To ensure the stability of the processing queues at the satellite CPUs, the average time to process all the segments allocated to a given satellite $n \in \mathcal{N}$, of size $\sum_{k=0}^K x_k^{(n)}$, must be shorter than the duration of the task. Therefore, a proper CPU frequency must be selected for the processing of each segment at each satellite, denoted as $f_k^{(n)}$. From (5) we derive the processing constraint:

$$\sum_{k=1}^{K} \frac{x_k^{(n)} C(\rho_k, \epsilon)}{N_{\text{CPU}} f_k^{(n)}} \le K T_{\text{GTF}}, \quad \forall n \in \mathcal{N}.$$
 (19)

Downlink and ISL rate constraints: The average data rate for the satellite-to-ground link and the ISLs must be sufficiently high to transmit the generated data within the considered period of time of $KT_{\rm GTF}$ seconds. Hence, we formulate the downlink constraint as follows.

$$\sum_{k=1}^{K} \left(x_k^{(g)} + \frac{1}{\rho_k} \sum_{n=1}^{N} x_k^{(n)} \right) \le T_{\text{GTF}}(h_{\text{px}}, d_{\text{gsd}}, h) \sum_{k=1}^{K} R_k$$
 (20)

For the ISLs, the total amount of traffic depends on the scatter algorithm and the location of the processing satellites $n \in \mathcal{N}_k$ w.r.t. the source satellite v_0 and g for all the K frames. Specifically, to calculate the amount of traffic assigned to each ISL $(u,v) \in \mathcal{E}_k$, let $\mathcal{P}_k(u,v)$ be the shortest path between u and v at time slot k. Next, we define the indicator variable $y_k^{(e)}(u,v)$, which takes the value of 1 if the edge $e \in \mathcal{E}_k$ is in the path $\mathcal{P}_k(u,v)$ and 0 otherwise. That is,

$$y_k^{(e)}(u,v) \triangleq \begin{cases} 1, & \text{if } e \in \mathcal{P}_k(u,v) \\ 0 & \text{otherwise.} \end{cases}$$
 (21)

Based on the latter, we define the constraint for the data rate at the ISIs as

$$\sum_{k=1}^{K} x_{k}^{(g)} y_{k}^{(e)}(v_{0}, g) + \sum_{n=1}^{N} x_{k}^{(n)} \left(y_{k}^{(e)}(v_{0}, n) + \frac{y_{k}^{(e)}(n, g)}{\rho_{k}} \right) \\
\leq KT_{\text{GTF}}R_{\text{ISL}}, \quad \forall e \in \mathcal{E}_{k}. \quad (22)$$

Nevertheless, in most practical scatter algorithms, the ISLs that communicate the source satellite v_0 with its neighbors will be subject to the heaviest traffic. Therefore, the latter constraint can be simplified by limiting it to the ISLs $\mathcal{E}_0 = \{(v_0, n) \in \mathcal{E} : n \in \mathcal{N}_k^{(n)}\}$

Further, recall that $\ell(\mathcal{P}_k(u,v))$ is defined as the length of the u-v path. Then, we define the energy devoted for the *scatter* phase as

$$E_{k}^{\text{scatter}}(v_{0}, \mathbf{x}_{k}; \eta) = \frac{\mu_{\text{RF}}^{\text{amp}} P_{\text{RF}}^{\text{tx}} x_{k}^{(g)}}{R_{k}} + \frac{\eta P_{\text{ISL}}}{R_{\text{ISL}}} \times \left(\sum_{n=1}^{N} \ell \left(\mathcal{P}_{k}(v_{0}, n) \right) x_{k}^{(n)} + \left(\ell \left(\mathcal{P}_{k}(v_{0}, g) \right) - 1 \right) x_{k}^{(g)} \right), (23)$$

where the first addend corresponds to energy needed to reach the GS and the second one for the distribution among satellites. The parenthesis accounts for the amount of data that reaches each node, weighted by the number of steps (i.e., links). Likewise, the consumed energy for the *gather* phase is defined as

$$E_k^{\text{gather}}(\rho_k, \mathbf{x}_k; \eta) = \frac{1}{\rho_k} \sum_{n=1}^{N} x_k^{(n)} \left(\frac{\mu_{\text{RF}}^{\text{amp}} P_{\text{RF}}^{\text{tx}}}{R_k} + \frac{\eta P_{\text{ISL}}}{R_{\text{ISL}}} \left(\ell \left(\mathcal{P}_k(n, g) \right) - 1 \right) \right), (24)$$

where each compressed segment, i.e., $x_k^{(n)}/\rho_k$, is weighted by the energy per bit it takes to reach the GS from each satellite n through ISL and RF links. The overall energy consumption, due to distribution and processing of the data, is defined as the sum of the energy at the scatter, processing, and gather phases. Hence, we formulate the energy minimization problem as

$$\begin{split} \mathbf{P}_{1}: & \underset{\mathbf{X}, \mathbf{F}, \boldsymbol{\rho}}{\operatorname{minimize}} & \sum_{k=1}^{K} E_{k}^{\operatorname{scatter}}(v_{0}, \mathbf{x}_{k}; \boldsymbol{\eta}) + E_{k}^{\operatorname{gather}}(\boldsymbol{\rho}_{k}, \mathbf{x}_{k}; \boldsymbol{\eta}) \\ & + \sum_{n=1}^{N} E_{k}^{\operatorname{proc}}\left(x_{k}^{(n)}, \boldsymbol{\rho}_{k}, f_{k}^{(n)}; \boldsymbol{\epsilon}\right) & (25) \\ & \text{subject to} & (19), \ (20), \ (22) \\ & 0 \leq x_{k}^{(n)} \leq D_{k}, & \forall n \in \mathcal{N}, k \in \mathcal{K} & (25a) \\ & \mathbf{x}_{k} \mathbf{1} = D_{k}, & \forall k \in \mathcal{K} & (25b) \\ & 1 < \boldsymbol{\rho}_{k} \leq \boldsymbol{\rho}_{\max}, & \forall k \in \mathcal{K} & (25c) \\ & 0 < f_{k}^{(n)} \leq f_{\mathrm{CPU}}, & \forall k \in \mathcal{K}, n \in \mathcal{N}. \ (25d) \end{split}$$

where the parameter $\rho_{\rm max}$ is a pre-defined maximum acceptable compression ratio.

That is, for each frame $k \in \mathcal{K}$, the GS must determine the compression ratio ρ_k , the allocation vector \mathbf{x}_k , and the CPU frequency $f_k^{(n)}$ to minimize energy while fulfilling the processing and communication constraints. Note that constraint (25c) is defined to avoid the value of $\rho_k = 1$, as this represents no processing at the satellites and is an equivalent solution to setting $x_k^{(g)} = 1$.

Naturally, the routing algorithm, which determines the paths to be followed by the segments, has an impact on the links used during the scatter and gather phases by determining the variables $\ell\left(\mathcal{P}_k(v_0,n)\right),\ \ell\left(\mathcal{P}_k(n,g)\right)$, and $y_k^{(e)}(v_0,n)$ and $y_k^{(e)}(n,g)$. Consequently, the routing algorithm has an impact

(28c)

on the ISL constraint and on the energy consumption. Nevertheless, investigating the optimal routing algorithm for each phase is out of the scope of the paper and, hence, we consider a typical hop-count shortest-path routing algorithm and treat these variables as parameters in (25).

For the case with $C(\rho_k,\epsilon) = e^{\rho_k\epsilon} - e^{\epsilon}$, neither the energy consumption for processing $E_k^{\mathrm{proc}}\left(\rho_k, f_k^{(n)}; D_k, \epsilon\right)$, defined in (11), nor for communication in the gather phase $E_k^{\text{gather}}(\rho_k, \mathbf{X}_k; \eta)$, defined in (24), are jointly convex in \mathbf{X} and ρ . Consequently, the objective function (25) is not jointly convex in \mathbf{X} , $\boldsymbol{\rho}$, and \mathbf{F} . Furthermore, constraints (19), (20), (22) are not jointly convex in X and ρ . Thus, P₁ is a nonconvex optimization problem. Nevertheless, we exploit the fact that the problem is convex when only considering one optimization variable at a time. In particular, a closed-form expression can be obtained for the CPU frequency of the satellites **F**. Furthermore, $E_k^{\text{scatter}}(v_0, \mathbf{x}_k; \eta)$ is linear in **X**. Therefore, we follow a variable decomposition approach and decompose the general optimization problem (25) into three sub-problems, which are solved iteratively following the Block Coordinate Descent (BCD) algorithm to reach a near-optimal solution [22]. Specifically, we begin by obtaining the closedform solution for the optimal CPU frequency F^* . The optimal CPU frequency is then used to optimize X and ρ iteratively.

Conversely, for the case with the JPEG compression algorithm $C(\rho_k,\epsilon)=\epsilon$, the optimal solution for the compression ratio is $\rho_k=\rho_{\rm max}$, which is treated as a parameter and the optimization problem (25) simplifies to only optimizing ${\bf X}$ and ${\bf F}$ jointly.

A. Optimizing the CPU frequency

As starting point, we consider the problem of optimizing the CPU frequency F for a given ρ and X in P_1 . We formulate the optimization problem for this case as

$$P_{F}: \text{minimize} \quad \sum_{n=1}^{N} \sum_{k=1}^{K} E_{k}^{\text{proc}} \left(x_{k}^{(n)}, \rho_{k}, f_{k}^{(n)}; \epsilon \right)$$

$$\text{subject to} \quad \sum_{k=1}^{K} \frac{x_{k}^{(n)} C(\rho_{k}, \epsilon)}{K N_{\text{CPU}} f_{k}^{(n)}} \leq T_{\text{GTF}} \ \forall n \in \mathcal{N}$$

$$0 \leq f_{k}^{(n)} \leq f_{\text{CPU}}, \qquad \forall k \in \mathcal{K}, n \in \mathcal{N}.$$

Theorem 1 (Optimal CPU frequency). If the problem is feasible for the given \mathbf{X} and ρ , the optimal CPU frequency is constant and equals the minimum required to satisfy the processing constraint (19). Therefore, the optimal CPU frequency for satellite n given \mathbf{X} and $\boldsymbol{\rho}$ is given by

$$f_k^{(n)*} = f^{(n)} = \frac{\sum_{k=1}^K x_k^{(n)} C(\rho_k, \epsilon)}{K N_{\text{CPU}} T_{\text{GTF}}},$$

$$\forall n \in \mathcal{N} : \sum_{k=1}^K x_k^{(n)} C(\rho_k, \epsilon) - T_{\text{GTF}} K N_{\text{CPU}} f_{\text{CPU}} \le 0.$$
(27)

The proof is based on the complementary slackness condition and is presented in the Appendix A.

In all the cases where the processing constraint cannot be fulfilled, the CPU frequency is set momentarily to $f^{(n)} = f_{CPU}$ to proceed with the iterative optimization.

B. Optimizing the task allocation

Next, we define problem P_X : optimizing X for a given F^* and ρ . Based on the previous result for F^* , we transform the constraint (19) and define the problem as

$$\begin{aligned} \mathbf{P_{X}}: & \underset{\mathbf{X}}{\text{minimize}} & \sum_{k=1}^{K} \left(E_{k}^{\text{scatter}}(v_{0}, \mathbf{x}_{k}; \eta) + E_{k}^{\text{gather}}(\rho_{k}, \mathbf{x}_{k}; \eta) \right) \\ & + \sum_{n=1}^{N} E_{k}^{\text{proc}} \left(x_{k}^{(n)}, \rho_{k}, f^{(n)}; \epsilon \right) & (28) \\ & \text{subject to} & \sum_{k=1}^{K} x_{k}^{(n)} C(\rho_{k}, \epsilon) - K T_{\text{GTF}} N_{\text{CPU}} f^{(n)} \leq 0, \\ & \forall n \in \mathcal{N}, & (28a) \\ & (20), & (22) \\ & 0 \leq x_{k}^{(n)} \leq D_{k}, & \forall n \in \mathcal{N}, k \in \mathcal{K} & (28b) \end{aligned}$$

Note that $P_{\mathbf{X}}$ is linear in \mathbf{X} with affine constraints and, since \mathbf{F}^* can be calculated in closed-form, we solve the problem using an iterative convex optimization approach with the augmented Lagrangian of (28), where constraint (28a) is moved to the objective and used as penalty [23]. Specifically,

$$\begin{aligned} & \text{P}_{\mathcal{L}(\mathbf{X},\mathbf{F}^*;\alpha)} \colon \\ & \text{minimize} \quad \sum_{k=1}^{K} \left(E_k^{\text{scatter}}(v_0,\mathbf{x}_k;\eta) + E_k^{\text{gather}}(\rho_k,\mathbf{x}_k;\eta) \right) \\ & \quad + \sum_{n=1}^{N} \left[E_k^{\text{proc}} \left(x_k^{(n)}, \rho_k, f^{(n)}; \epsilon \right) \right. \\ & \quad + \lambda^{(n)} \left(\sum_{k=1}^{K} \frac{x_k^{(n)} C(\rho_k, \epsilon)}{K T_{\text{GTF}} N_{\text{CPU}}} - f^{(n)} + s^{(n)} \right) \\ & \quad + \frac{\alpha}{2} \left(\sum_{k=1}^{K} \frac{x_k^{(n)} C(\rho_k, \epsilon)}{K T_{\text{GTF}} N_{\text{CPU}}} - f^{(n)} + s^{(n)} \right)^2 \right] (29) \\ & \text{subject to} \quad (20), \quad (22) \\ & \quad 0 \leq x_k^{(n)} \leq D_k, \quad \forall n \in \mathcal{N}, k \in \mathcal{K} \\ & \quad \mathbf{x}_k \mathbf{1} = D_k, \qquad \forall k \in \mathcal{K}. \end{aligned} \tag{29a}$$

We solve problem (29) following the Increasing Penalty Dual Decomposition (IPDD) method [24] by first solving for \mathbf{X} for a given \mathbf{F} . Then, the values of \mathbf{F}^* are updated after each iteration with the update rule in (27). Finally, as \mathbf{F}^* has been already updated, the slack variables $s^{(n)}$ become 0. Then, following the IPDD method, the Lagrange multipliers $\lambda^{(n)}$ and the penalty terms $\alpha^{(n)}$ are updated according to a pre-defined threshold τ_{proc} and increase factor $\beta \in (0,1)$. Namely, if the

processing constraint is below a pre-defined threshold au_{proc} , the update rule for $\lambda^{(n)}$ with inequality constraints becomes

$$\lambda^{(n)} = \max\left(0, \lambda^{(n)} + \alpha^{(n)}\right)$$

$$\times \left(\sum_{k=1}^{K} x_k^{(n)} C(\rho_k, \epsilon) - T_{\text{GTF}} K N_{\text{CPU}} f^{(n)}\right). \tag{30}$$

Otherwise, if the processing constraint is above τ_{proc} , the penalty parameter is increased as $\alpha^{(n)} \leftarrow \alpha^{(n)}/\beta$.

C. Optimizing the compression ratio

Finally, we proceed to optimize the compression factor ρ for a given \mathbf{X} and \mathbf{F}^* for the case where $C(\rho_k, \epsilon)$ increases with ρ_k . The optimization problem for ρ is formulated from (25) by removing the constant term $E_k^{\text{scatter}}(v_0, \mathbf{x}_k; \eta)$ and the constraints on \mathbf{X} , which give

$$\begin{split} \mathbf{P}_{\rho}: & \underset{\rho}{\text{minimize}} & \sum_{k=1}^{K} E_{k}^{\text{gather}}(\rho_{k}, \mathbf{x}_{k}; \eta) \\ & + \sum_{n=1}^{N} E_{k}^{\text{proc}}\left(x_{k}^{(n)}, \rho_{k}, f^{(n)}; \epsilon\right) \\ & \text{subject to} & \sum_{k=1}^{K} x_{k}^{(n)} C(\rho_{k}, \epsilon) - K T_{\text{GTF}} N_{\text{CPU}} f^{(n)} \leq 0, \\ & \forall n \in \mathcal{N}, \\ & (20), \ (22) \\ & 1 < \rho_{k} \leq \rho_{\text{max}} \quad \text{for all } k \in \mathcal{K} \end{aligned} \tag{31b}$$

Let s be the vector of slack variables, which includes those for the downlink constraint $s^{(g)}$, for the ISL constraints $s^{(e)}$, and for the values of ρ_k , namely $s_k^{(\rho)}$. Further, we define the Lagrange multiplier and penalty terms for these constraints as $\lambda^{(g)}$ and $\alpha^{(g)}$, $\lambda^{(e)}$ and $\alpha^{(e)}$, and $\lambda^{(\rho)}_k$ and $\alpha^{(\rho)}_k$, respectively. Building on these, the augmented Lagrangian for P_{ρ} is given by (32) on top of Page 10. Note that neither the slack variables for the downlink constraint nor for the ISL constraints depend on k as the limiting factors are the average rates throughout the execution of the task. Therefore, the problem becomes

$$\underset{\boldsymbol{\rho} \geq 1, \, \boldsymbol{s} \geq 0}{\text{minimize}} \quad \underset{\boldsymbol{\lambda} \geq 0, \, \lambda^{(n)}, \, \lambda_k}{\text{maximize}} \, \mathcal{L}(\mathbf{X}, \boldsymbol{\rho}, \boldsymbol{\lambda}, \boldsymbol{s}; \boldsymbol{\alpha}), \tag{33}$$

which we solve using the method of projected gradient descent by applying the following update rules for λ after updating \mathbf{F} according to (27) and $\lambda^{(n)}$ according to (30).

$$\lambda^{(g)} = \max \left(0, \lambda^{(g)} + \alpha^{(g)} \right) \times \left[s^{(g)} + \sum_{k=1}^{K} \frac{1}{T_{\text{GTF}}} \left(x_k^{(g)} + \sum_{n=1}^{N} \frac{x_k^{(n)}}{\rho_k} \right) - R_k \right]$$
(34)

$$\lambda_k^{(\rho)} = \max\left(0, \lambda_k^{(\rho)} + \alpha_k^{(\rho)} \left(\rho_k - \rho_{\text{max}} - s_k^{(\rho)}\right)\right) \tag{35}$$

$$\lambda^{(e)} = \max \left(0, \lambda^{(e)} + \alpha^{(e)} \left[s^{(e)} + \sum_{k=1}^{K} \frac{x_k^{(g)} y_k^{(e)}(v_0, g)}{K T_{\text{GTF}} R_{\text{ISL}}} + \sum_{n=1}^{N} \frac{x_k^{(n)}}{K T_{\text{GTF}} R_{\text{ISL}}} \left(y_k^{(e)}(v_0, n) + \frac{y_k^{(e)}(n, g)}{\rho_k} \right) \right] \right) (36)$$

D. Global optimization algorithm and practical considerations

Algorithm 1 illustrates the iterative procedure for global optimization for the case where $C(\rho_k, \epsilon) = e^{\rho_k \epsilon} - e^{\epsilon}$. Note that a feasible value for each ρ_k must be selected during initialization. For instance, we initialize each ρ_k with the value

$$\rho_k^{\text{init}} = \min \left\{ \max \left(1, \frac{D_k}{T_{\text{GTF}} R_k} \right), \rho_{\text{max}} \right\}. \tag{37}$$

As with traditional penalty methods, the convergence of the IPDD method and of projected gradient descent depend on the initial value of the penalty terms and the termination condition. While these methods can achieve convergence with finite penalty terms and finite number of iterations, the number of iterations to fulfill the termination conditions vary widely depending on the characteristics of the objective function and the problem constraints. In our study, the termination condition for the optimization of the task allocation **X** is $\|\mathbf{X} - \mathbf{X}'\|_2 \le \delta$ and of the compression ratio ρ is $\|\rho - \rho'\|_2 \le \delta$. These termination conditions are defined in lines 5 and 10 of Algorithm 1. If Algorithm 1 were to be implemented in a real system where the solution must be obtained within a specific deadline, the termination conditions can be modified to limit the number of iterations so the deadline can be met. This will result in a sub-optimal solution, but the execution time can be easily characterized for the specific computing platform.

IV. RESULTS

We consider an orbital plane with N=20 satellites capturing images in an HD format with 1920×1080 pixels under the following two scenarios.

- Per-frame optimization: Optimizing one frame independently is optimal if the task is relatively long (i.e., $K \to \infty$) and the frame size is constant $W_k = W_{k'}$ for all $k, k' \in \mathcal{K}$ and, naturally, if K = 1.
- Multi-frame optimization: In all cases, optimizing across
 the K frames of the task is the optimal approach. We
 illustrate the gains of this approach with respect to perframe optimization in a synthetic scenario that leads to the
 upper bound in energy savings and in a realistic scenario
 that leads to the lower bound in energy savings.

Without loss of generality, the source satellite is denoted as v_0 . The destination satellite v_d is assumed to be located at the edge of coverage at the first frame of the task and moves towards the center of coverage. The default parameters for the performance analysis are listed in Table II. With these parameters, the downlink data rate at the edge of coverage area is $2.16\,\mathrm{Gbps}$. The GSD is set to $d_\mathrm{gsd}=0.5\,\mathrm{m}$, which results in a GTFP of $78\,\mathrm{ms}$.

$$\mathcal{L}(\boldsymbol{\rho}, \boldsymbol{\lambda}, s; \mathbf{X}, \boldsymbol{\alpha}) = \sum_{k=1}^{K} E_{k}^{\text{gather}}(\rho_{k}, \mathbf{x}_{k}; \eta) + \sum_{n=1}^{N} E_{k}^{\text{proc}} \left(x_{k}^{(n)}, \rho_{k}, f^{(n)}; \epsilon \right) \\
+ \sum_{n=1}^{N} \left[\lambda^{(n)} \left(\sum_{k=1}^{K} \frac{x_{k}^{(n)} C(\rho_{k}, \epsilon)}{K N_{\text{CPU}} T_{\text{GTF}}} - f^{(n)} + s^{(n)} \right) + \frac{\alpha^{(n)}}{2} \left(\sum_{k=1}^{K} \frac{x_{k}^{(n)} C(\rho_{k}, \epsilon)}{K N_{\text{CPU}} T_{\text{GTF}}} - f^{(n)} + s^{(n)} \right)^{2} \right] \\
+ \lambda^{(g)} \left[s^{(g)} + \sum_{k=1}^{K} \frac{x_{k}^{(g)} + \sum_{n=1}^{N} \frac{x_{k}^{(n)}}{\rho_{k}}}{T_{\text{GTF}}} - R_{k} \right] + \frac{\alpha^{(g)}}{2} \left[s^{(g)} + \sum_{k=1}^{K} \frac{x_{k}^{(g)} + \sum_{n=1}^{N} \frac{x_{k}^{(n)}}{\rho_{k}}}{T_{\text{GTF}}} - R_{k} \right]^{2} \\
+ \sum_{e \in \mathcal{E}_{s}} \lambda^{(e)} \left[s^{(e)} + \sum_{k=1}^{K} \frac{x_{k}^{(g)} y_{k}^{(e)}(v_{0}, g)}{K T_{\text{GTF}} R_{\text{ISL}}} + \sum_{n=1}^{N} \frac{x_{k}^{(n)} \left(y_{k}^{(e)}(v_{0}, n) + \frac{y_{k}^{(e)}(n, g)}{\rho_{k}} \right)}{K T_{\text{GTF}} R_{\text{ISL}}} \right]^{2} \\
+ \sum_{e \in \mathcal{E}_{s}} \frac{\alpha^{(e)}}{2} \left[s^{(e)} + \sum_{k=1}^{K} \frac{x_{k}^{(g)} y_{k}^{(e)}(v_{0}, g)}{K T_{\text{GTF}} R_{\text{ISL}}} + \sum_{n=1}^{N} \frac{x_{k}^{(n)} \left(y_{k}^{(e)}(v_{0}, n) + \frac{y_{k}^{(e)}(n, g)}{\rho_{k}} \right)}{K T_{\text{GTF}} R_{\text{ISL}}} \right]^{2} \\
+ \sum_{k=1}^{K} \lambda_{k}^{(\rho)} \left(\rho_{k} - \rho_{\text{max}} + s_{k}^{(\rho)} \right) + \sum_{k=1}^{K} \frac{\alpha_{k}^{(\rho)}}{2} \left(\rho_{k} - \rho_{\text{max}} + s_{k}^{(\rho)} \right)^{2}$$
(32)

Algorithm 1 BCD algorithm for iterative non-convex optimization.

```
Input: K, R_{\text{ISL}} W_k, \mathcal{G}_k, R_k for all k \in \mathcal{K} and tolerance \delta

1: Calculate \mathcal{P}_k(v_0, n), y_k^{(e)}(v_0, n), \mathcal{P}_k(n, g) and y_k^{(e)}(n, g) for all n \in \mathcal{N} and k \in \mathcal{K}

2: Initialize x_k^{(v_0)} \leftarrow D_k, x_k^{(n)} = x_k^{(g)} \leftarrow 0 for all n \neq v_0, and \rho_k \leftarrow \rho_{nk}^{\text{init}} for all k \in \mathcal{K}, and f^{(n)} \leftarrow f_{\text{CPU}} for all n \neq v_0,
    3: \mathbf{X}' \leftarrow \mathbf{0} and \boldsymbol{\rho}' \leftarrow \mathbf{0}
            \begin{aligned} & \text{while } & \|\mathbf{X} - \mathbf{X}'\|_2 + \|\boldsymbol{\rho} - \boldsymbol{\rho}'\|_2 > \delta \text{ do} \\ & \text{while } & \|\mathbf{X} - \mathbf{X}'\|_2 > \delta \text{ do} \end{aligned} 
    5:
    6:
                           Optimize X given \mathbf{F}^* and \boldsymbol{\rho} with IPDD (29)
    7:
                           Update \mathbf{F}^* given \mathbf{X} and \boldsymbol{\rho} as in (27)
    8:
                    end while
     9:
                    while \|\boldsymbol{\rho} - \boldsymbol{\rho}'\|_2 > \delta do
  10:
  11:
                           Optimize \rho given \mathbf{F}^* and \mathbf{X} with projected gradient
  12:
                           descent as in (32)
                           Update \mathbf{F}^* given \mathbf{X} and \boldsymbol{\rho} as in (27)
  13:
                    end while
  15: end while
  16: return \mathbf{X}^* \leftarrow \mathbf{X}, \rho^* \leftarrow \boldsymbol{\rho}, and \mathbf{F}^*
```

The results were obtained using a simulator coded in Python to replicate the orbital dynamics of the satellites and to calculate the data rates at each time slot. The optimization problems were solved using the CVXPY package [25] using MOSEK ApS as solver.

A. Per-frame optimization

Fig. 3 shows the energy consumption per image for the feasible values of W_k for direct download, local processing, and the global optimal solution. Two topologies are considered: 1)

TABLE II
PARAMETER SETTINGS FOR PERFORMANCE EVALUATION

Parameter	Symbol	Setting
Altitude of deployment [km]	h	600
Number of satellites	N	20
Processor frequency [GHz]	$f_{ m CPU}$	1.8
Number of processor cores	$N_{ m cores}$	4
Power consumption for processing [W]	$P_{\rm proc}(f_{ m CPU})$	10
Data rate of the ISLs [Gbps]	$R_{ m ISL}$	10
Transmission power of the ISLs [W]	P_{ISL}	60
Downlink transmission power [W]	$P^{ ext{tx}}_{ ext{RF}} u_{ ext{RF}}^{ ext{tx}}$	10
Inefficiency of the downlink RF power am-	$\mu_{ ext{p}_{ ext{D}}}^{ ext{alth}p}$	1
plifier	· KI	
Downlink carrier frequency [GHz]	f_c	20
Downlink bandwidth [MHz]	B	500
Downlink antenna gain [dBi]	G_d	32.13
Antenna gain of the GS [dBi]	$G_g \ \sigma_{ ext{dB}}^2$	34.20
Noise power [dBW]	$\sigma_{\scriptscriptstyle ext{dP}}^{ ilde{ ilde{2}}}$	-119.32
Width of the k-th frame [images]	W_k	$\{0, 1, 2, \dots\}$
Size of HD image [MB]	$D_{ m img}$	5.93
Ground sample distance (GSD) [m/pixel]	$d_{ m gsd}$	0.5
Maximum compression factor	ρ_{max}	20
Complexity of the image processing algo-	ϵ	0.1
rithm		
Fraction of $P_{\rm ISL}$ consumed during data transmission	η	{0.1, 1}

in Fig. 3b the destination satellite is the same as the source satellite $v_d = v_0$ and 2) in Fig. 3d the destination satellite is $v_d = v_5$, namely, it's five hops away from the source satellite. Besides, two values are considered for parameter $\eta = \{0.1, 1\}$.

As it can be seen in Fig. 3, the energy consumption with direct download is much higher when compared to local processing and to the global optimal. Furthermore, direct download is only feasible with $W_k \leq 3$ images. In contrast, local processing achieves a similar energy consumption as the global optimal for most of the cases within its feasible region $W_k \leq 18$ images. This behavior means that local processing

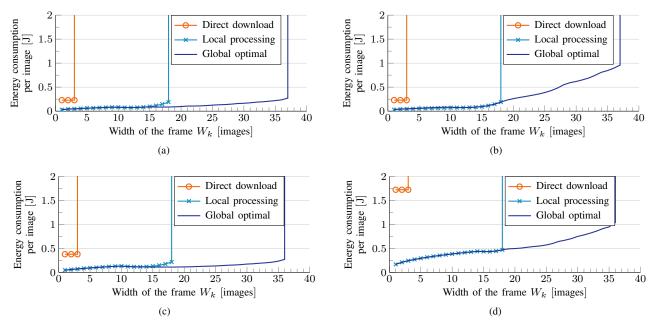


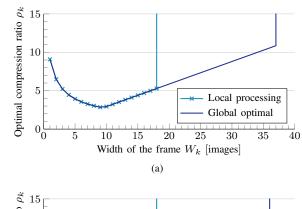
Fig. 3. Energy consumption per image for $d_{\rm gsd}=0.5\,{\rm m}$ with per-frame optimization for the cases where the destination satellite is $v_d=v_0$ (a) with $\eta=0.1$ and (b) with $\eta=1$ and where the destination satellite is $v_d=v_5$ (c) with $\eta=0.1$ and (d) with $\eta=1$ considering the three approaches: direct download, local processing, and global optimal. The energy consumption is set to ∞ outside the feasible region.

is the optimal solution with relatively small frames sizes W_k . Finally, the global optimal solution leads to the minimum energy consumption in all cases and also increases the feasible region to $W_k \leq 37$ for $v_d = v_0$ (see Fig. 3a and Fig. 3b) and to $W_k \leq 36$ for $v_d = v_5$ (see Fig. 3c and Fig. 3d). Thus, the global optimal solution increases the number of images per frame that are supported by the system by a factor of $12\times$ when compared to direct download and by a factor of $2\times$ when compared to local processing.

In addition, the energy consumption per image is considerably lower for $v_d=v_0$ in Fig. 3b than for $v_d=v_5$ in Fig. 3d due to the increased distance between the source satellite and the destination, which increases the energy consumption at the gather phase. Naturally, the energy consumption with $\eta=0.1$ (see Fig. 3a and Fig. 3c) is considerably lower than that with $\eta=1$ (see Fig. 3b and Fig. 3d).

Next, Fig. 4 shows the selected value of ρ as a function of W_k . Clearly, the same value of $\rho_k = \rho_k^*$ is selected by both the global optimal and the local processing approaches. Specifically, ρ_k^* decreases as W_k increases up to $W_k = 9$ for $v_d = v_0$ and up to $W_k = 14$ for $v_d = v_5$. As W_k increases beyond these values, the optimal compression ratio is $\rho_k^* = D_k/R_k$, which is the lowest value that ensures that the downlink constraint is fulfilled, which can be easily calculated in closed form.

We conclude the analyses of the per-frame optimization scenario by illustrating the values of $x_k^{(n)*}$ in Fig. 5 for $v_d=v_0$ and $v_d=v_5$ with $\eta=\{0.1,1\}$ and the source satellite being n=5. Clearly, Fig. 5 shows that the data to process at satellites close to the source n=5 increases as W_k increases. Specifically, as shown in Fig. 5a and Fig. 5b, the data is distributed symmetrically across neighbouring satellites in the SMEC cluster when $v_d=v_0$ as the source satellite has



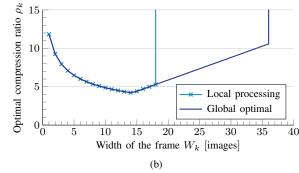
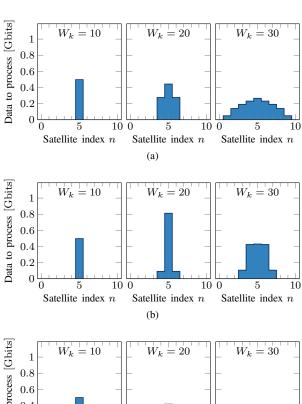
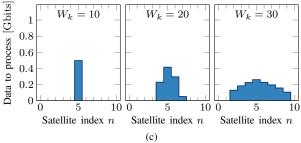


Fig. 4. Optimal compression ratio with per-frame optimization considering local processing and global optimal for (a) $v_d = v_0$ and (b) $v_d = v_5$.

direct connection to the GS. Conversely, for the case with $v_d=v_5$ shown in Fig. 5c and Fig. 5d, a larger amount of the data is distributed to satellites in the SMEC cluster that are in the shortest path towards the destination n=10. Furthermore, more satellites are used for processing for the case with $\eta=0.1$ (see Fig. 5a and Fig. 5c) when compared to the case with $\eta=1$ (see Fig. 5b and Fig. 5d). This is because





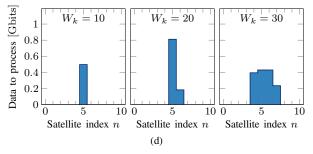
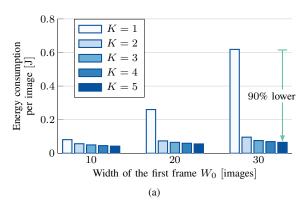


Fig. 5. Amount of data processed at the SMEC cluster for each satellite n for $W_k = \{10, 20, 30\}$ with the source satellite v_0 being n=5. The destination satellite v_d is also n=5 in (a) $\eta=0.1$ and (b) $\eta=1$ and the destination satellite v_d is n=10 in (c) $\eta=0.1$ and (d) $\eta=1$.

the case with $\eta=1$ results in a higher transmission power in the FSO links, which serves as a penalty for inter-satellite communication. In all the illustrated cases, the amount of data downloaded without processing is zero.

B. Multi-frame optimization

Next, we evaluate the energy consumption that can be achieved by performing multi-frame optimization. First, we consider a scenario where the amount of tasks per GTFP is relatively low and the scheduler can dedicate an extended duration per task to reduce energy consumption. This is modeled by defining an initial frame of width W_0 images followed by K-1 empty frames (i.e., with $W_k=0$ for k>0).



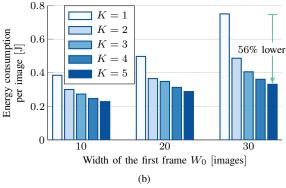


Fig. 6. Global optimal energy consumption for a task with K frames for $\eta=1$, where the first frame contains $W_0\in\{5,10,15,20\}$ images and the remaining K-1 frames are empty, i.e., $W_k=0$ for k>0. (a) $v_d=v_0$ and (b) $v_d=v_5$.

The energy consumption for $W_0=\{10,20,30\}$ with $K=\{1,2,3,4,5\}$ is shown in Fig. 6 considering $v_d=v_0$ in Fig. 6a and $v_d=v_5$ in Fig. 6b. As it can be seen, the energy consumption increases drastically with the width of the frame W_0 for the case with K=1, which has zero empty frames. On the other hand, it is clear that the energy consumption per image decreases as K increases. Specifically, the energy consumption with K=5, which contains 4 empty frames, is 90% lower than with K=1 for the case with $v_d=v_0$ and 56% lower than with K=1 for the case with $v_d=v_0$.

We conclude our analyses by evaluating the energy savings for the case of a realistic task of scanning the island of La Palma with $v_d = v_5$. Such task comprises K = 82 frames with different widths $W_k \in [1,29]$ as shown in Fig. 7a. The total duration of the task is equal to the duration of the pass of the satellite over La Palma takes $6.4 \, \mathrm{s}$, occurs from top to bottom of the area shown in Fig. 7a. Due to the large number of images per frame, neither direct download nor local processing are feasible in this scenario.

Fig. 7b shows the energy consumption per image with perframe optimization and with global optimization for $\eta=\{0.1,1\}$ for scanning the island of La Palma. Naturally, the energy consumption with $\eta=0.1$ is much lower than with $\eta=1$ as the energy consumption for transmission at the ISLs is $10\times$ greater for the latter case. Most importantly, Fig. 7b shows that the global optimization across all the K=82 frames results in saving 9% and 11% of the energy when compared to per-frame optimization for $\eta=0.1$ and $\eta=1$,

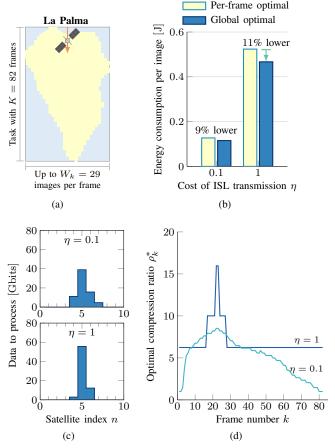


Fig. 7. (a) Task characteristics, (b) energy consumption, (c) task allocation where the source satellite v_0 is n=5, and (d) optimal value of ρ_k for scanning La Palma island with a GSD of $d_{\rm gsd}=0.5\,\rm m$.

respectively. Even though these energy savings are lesser than for the case with K-1 empty frames, they still represent an important reduction in energy consumption.

Next, Fig. 7c shows the amount of data allocated to each satellite throughout the K=82 frames $\sum_{k=1}^K x_k^{(n)}$ given that the source satellite is n=5. Clearly, the data is more evenly distributed across 4 satellites with $\eta=0.1$ than with $\eta=1$, where the source satellite n=5 processes more than 78% of the total amount of data.

Finally, Fig. 7d shows that the optimal compression ratio for each frame ρ_k^* is not uniform across the task and, in general, increases with the number of images in the frame. Furthermore, the values of ρ_k^* are widely different for the two considered values of η , which illustrates the need for the careful selection of ρ_k^* based on the task allocation and the transmission power.

V. CONCLUSIONS

In this paper, we considered a scenario where the physical characteristics of the system, dictated by the orbital parameters of the satellites and the area covered by their camera, determine the real-time requirements, which are necessary to maintain stability in the communication links and in the CPUs of the satellites. Moreover, we presented a general framework

and an iterative optimization method for distributed SMEC. Our results show that distributed SMEC allows to capture, process, and download up to $6\times$ more images than with direct download and up to $2\times$ more images than with local SMEC. Furthermore, up to 90% of the energy can be saved by carefully selecting the allocation of data, the compression ratio, and the processing frequency at the satellites. Finally, we considered a real-life task and observed that 1) it is only feasible to complete the task with distributed SMEC and 2) optimizing the task parameters jointly leads to additional energy savings when compared to optimizing each frame independently. These benefits set the basis for achieving veryhigh resolution Earth observation missions.

APPENDIX

To obtain the closed-form expression for the optimal CPU frequency, observe that the energy for processing increases monotonically with $f_k^{(n)}$. Furthermore, the problem is feasible with a given \mathbf{X} and $\boldsymbol{\rho}$ if and only if $\exists F: 0 \leq f_k^{(n)} \leq f_{\text{CPU}}$ for all n and k that satisfies (19).

To find the closed-form expression for the optimal CPU frequency, we define the Lagrangian of P_F , defined in (26) as

$$\mathcal{L}(\mathbf{F}, \lambda) = \sum_{n=1}^{N} \left[\sum_{k=1}^{K} \nu C(\rho_{k}, \epsilon) x_{k}^{(n)} \left(f_{k}^{(n)} \right)^{2} + \lambda^{(n)} \left(\sum_{k=1}^{K} \frac{x_{k}^{(n)} C(\rho_{k}, \epsilon)}{K N_{\text{CPU}} f_{k}^{(n)}} - T_{\text{GTF}} \right) + \sum_{k=1}^{K} \lambda_{k}^{(n)} \left(f_{k}^{(n)} - f_{\text{CPU}} \right) \right]$$
(38)

From complementary slackness [26], we have that an optimal solution to the primal and dual problem satisfies the following two conditions.

$$\lambda^{(n)} \left(\sum_{k=1}^{K} \frac{x_k^{(n)} C(\rho_k, \epsilon)}{K N_{\text{CPU}} f_k^{(n)}} - T_{\text{GTF}} \right) = 0, \tag{39}$$

$$\sum_{n=1}^{N} \sum_{k=1}^{K} \lambda_k^{(n)*} \left(f_k^{(n)*} - f_{\text{CPU}} \right) = 0.$$
 (40)

Thus, we express the first complementary slackness condition (39) as

$$\sum_{k=1}^{K} \frac{x_k^{(n)} C(\rho_k, \epsilon)}{f_k^{(n)}} < T_{\text{GTF}} K N_{\text{CPU}} \quad \Longrightarrow \quad \lambda^{(n)} = 0, \quad (41)$$

otherwise

$$\lambda^{(n)} > 0 \quad \Longrightarrow \quad \sum_{k=1}^{K} \frac{x_k^{(n)} C(\rho_k, \epsilon)}{f_k^{(n)}} = T_{\text{GTF}} K N_{\text{CPU}}. \quad (42)$$

For condition (40) we have that

$$f_k^{(n)*} < f_{\text{CPU}} \implies \lambda_k^{(n)*} = 0.$$
 (43)

Otherwise,

$$\lambda_k^{(n)*} > 0 \implies f_k^{(n)*} = f_{\text{CPU}}.$$
 (44)

Next, by taking the gradient of the Lagrangian $\mathcal{L}(\mathbf{F}, \lambda)$ w.r.t. $f_h^{(n)}$ we have

$$\nabla_{f_k^{(n)}} \mathcal{L}(\mathbf{F}, \boldsymbol{\lambda}) = 2\nu C(\rho_k, \epsilon) x_k^{(n)} f_k^{(n)}$$

$$-\frac{\lambda^{(n)} x_k^{(n)} C(\rho_k, \epsilon)}{K N_{\text{CPU}} \left(f_k^{(n)}\right)^2} + \lambda_k^{(n)}$$

$$= 0. \tag{45}$$

In the following, we consider the solution of problem P_F for the cases where $C(\rho_k, \epsilon)x_k^{(n)} > 0$.

Case 1: To fulfill condition (43), the optimal value of the multiplier obtained from (45) is

$$\begin{split} \lambda^{(n)*} &= 2\nu K N_{\text{CPU}} \left(f_k^{(n)*} \right)^3, \\ \text{s.t. } f_k^{(n)*} &< f_{\text{CPU}} \text{ and } \lambda_k^{(n)*} = 0 \text{ for all } k \in \mathcal{K}, \end{split} \tag{46}$$

Therefore, we conclude that an equal solution $f^{(n)} = f_{i}^{(n)*}$ f_{CPU} is obtained for all $k \in \mathcal{K}$. That is, for any given satellite $n \in \mathcal{N}$, the optimal CPU frequency is equal for all the frames in a task. Furthermore, this implies that, if $\exists \lambda_k^{(n)} = 0$ for $k\in\mathcal{K}$, then $\lambda_k^{(n)}=0$ for all $k\in\mathcal{K}$. Specifically, by substituting $f_k^{(n)*}$ with $f^{(n)}$ in (42), we

obtain

$$f^{(n)} = \frac{1}{K N_{\text{CPU}} T_{\text{GTF}}} \sum_{k=1}^{K} x_k^{(n)} C(\rho_k, \epsilon)$$
 (47)

Furthermore, note that from (42) and (46), the following condition must hold

$$f^{(n)} \in (0, f_{\text{CPU}}) \implies \lambda^{(n)*} > 0. \tag{48}$$

Nevertheless, the latter does not prevent the case where $f^{(n)} =$ f_{CPU} and $\lambda^{(n)*} = 0$ and, therefore (47) is the optimal solution for all cases where $\lambda_k^{(n)} = 0$.

Case 2: To fulfill condition (41), the optimal value of the multiplier obtained from (45) is

$$\lambda_k^{(n)*} = -2\nu C(\rho_k, \epsilon) x_k^{(n)} f_k^{(n)*}$$
(49)

Since all the terms on the right-hand side of (49) are either positive or zero and it is required that $\lambda^{(n)*} \geq 0$, then the only solutions to fulfill (49) lead to $\lambda^{(n)*} = \lambda^{(n)*}_k = 0$ and are as

If there is no data to process at satellite n, any CPU frequency can be selected, namely,

$$C(\rho_k, \epsilon) x_k^{(n)} = 0 \implies f_k^{(n)*} \in [0, f_{\text{CPU}}], \quad (50)$$

which means that the value of $f_k^{(n)}$ is irrelevant. The other option is when the satellite n has data to process

$$C(\rho_k, \epsilon) x_k^{(n)} > 0 \implies f_k^{(n)*} = 0,$$
 (51)

but the latter option makes the processing time to be infinite, so it should be excluded from the set of possible solutions. Consequently, conditions (41) and (43) can only be fulfilled jointly if the satellite has no data to process. In other words, there is no optimal solution where $f_k^{(n)*} < f_{\mathrm{CPU}}$ and that leads to a processing time lesser than T_{GTF} .

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