

Robust Optimization using a new Volume-Based Clustering approach

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Robust Optimization using a new Volume-Based Clustering approach

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We introduce an uncertainty set construction method based on a newly developed **volume-based clustering** approach.

Robust optimization

In robust optimization, We consider the following constraint:

$$(\bar{a} + Pu)^T x \leq b \quad \forall u \in \mathcal{U}$$

Uncertainty set (\mathcal{U})

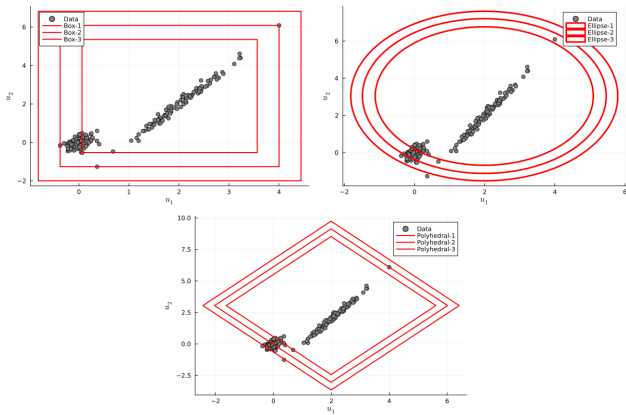


Figure 1: Fundamental uncertainty sets

<i>Box</i>	$\mathcal{U} = \{u : \ u\ _\infty \leq \rho\}$
<i>Ellipsoidal</i>	$\mathcal{U} = \{u : \ u\ _2 \leq \rho\}$
<i>Polyhedral</i>	$\mathcal{U} = \{u : \ u\ _1 \leq \rho\}$

The proposed uncertainty set construction method resulting in **less-conservative** solutions with minimizing volume of the uncertainty set and clustering.

Minimum volume ellipsoid Clustering (MVEC)

For an ellipsoid

$$\{x : \|Ax + b\| \leq 1\}$$

which is represented by (A, b) , the volume is proportional to $\frac{1}{\det A}$.

Hence, MVEC can be represented in the following mathematical optimization:

$$\max_{A_j, b_j} \sum_{j=1}^K \log \det(A_j)$$

$$\text{subject to} \quad \|A_j x^i + b_j\| \leq 1 \quad \forall x^i \in C_j, j = 1, \dots, K$$

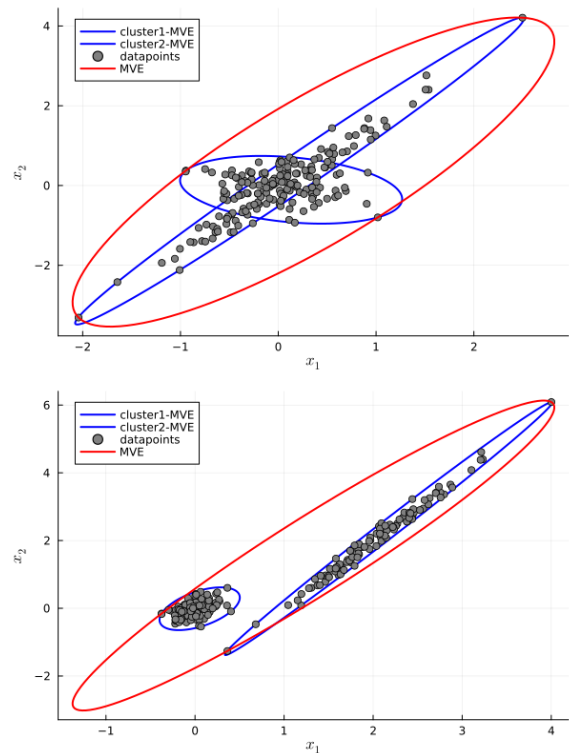


Figure 2: Uncertainty set based on MVEC

Then the proposed uncertainty set is:

$$\mathcal{U} = \bigcup_{j=1}^k U_j,$$

where

$$U_j = x : A_j x + b_j \leq 1$$