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# Formalizing Stack Safety as a Security Property

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Abstract—The term stack safety is used for a variety of compiler, run-time, and hardware mechanisms for protecting stack memory. Unlike "the heap," the ISA-level stack does not correspond to a single high-level language concept: different compilers use it in different ways to support procedural and functional abstraction mechanisms from a wide range of languages. This protean nature makes it difficult to nail down what it means to correctly enforce stack safety.

We propose a formal characterization of stack safety using concepts from language-based security. Rather than packaging all aspects of stack safety into a monolithic property, we decompose it into an integrity property and a confidentiality property for each of the caller and the callee, plus a control-flow property—five properties in all. This formulation is motivated by a particular class of enforcement mechanisms, the "lazy" stack safety micro-policies studied by Roessler and DeHon [1], which permit functions to write into one another's frames, but which taint the changed locations so that the frame's owner cannot access it. No existing characterization of stack safety captures this style of safety. We capture it here by stating our properties in terms of the observable behavior of the system.

Our properties go further than previous formal definitions of stack safety, supporting caller- and callee-saved registers, arguments passed on the stack, and tail-call elimination. We validate our properties by using them to distinguish between correct and incorrect implementations of Roessler and DeHon's micro-policies using property-based random testing. Our test harness successfully identifies several broken variants, including Roessler and DeHon's lazy policy; a repaired version of their policy does pass our tests.

## I. INTRODUCTION

Functions in high-level languages, and related abstractions such as procedures, methods, etc., are units of computation that call one another to modularly realize larger computations. At a low level, each function activation manages its own data—local variables, etc.—as well as information about the caller to which it must return. The call stack is the fundamental data structure used to implement functions, aided by an Application Binary Interface (ABI) that defines how registers are shared between activations.

From a security perspective, attacks on the call stack are attacks on the function abstraction itself. Indeed, the stack is an ancient [2] and perennial [3]–[8] target for low-level attacks, sometimes involving control-flow hijacking via corrupting the return address, sometimes memory corruption more generally. The variety in attacks on the stack is mirrored in the range of

software and hardware protections that aim to prevent them, including stack canaries [9], bounds checking [10]–[12], split stacks [13], shadow stacks [14], [15], capabilities [16]–[20], and hardware tagging [1], [21].

Enforcement mechanisms can be brittle, successfully eliminating one attack while leaving room for others. To avoid an endless game of whack-a-mole, we seek formal properties of safe behavior that can be proven or at least rigorously tested. Such properties can be used as the specification against which enforcement can be validated; even enforcement mechanisms that do not fulfill a property benefit from the ability to articulate why and when they may fail.

Of the mechanisms listed above, many are fundamentally ill suited for offering formal guarantees: may impede attackers, but do not provide universal protection. Shadow stacks, for instance, aim to "restrict the flexibility available in creating gadget chains" [15], not to categorically rule out attacks. Other mechanisms, such as SoftBound [10] and code-pointer integrity [13], do aim for stronger guarantees, but even these do not make formal promises. Indeed, to our knowledge, the sole line of work making a formal claim to protect stack safety is the secure calling conventions of Skorstengaard et al. [19] and Georges et al. [20].

Other mechanisms besides these should also be amenable to strong formal guarantees. In particular, Roessler and DeHon [1] have presented an array of tag-based micro-policies [22] for stack safety that offer strong guarantees. Their most realistic micro-policy, called Lazy Tagging and Clearing (LTC), makes an interesting performance trade-off: it allows function activations to improperly write into one another's stack frames, but ensures that the owner of the corrupted memory cannot access it afterward. Under this policy, one function activation can corrupt another's memory—just not in ways that affect observable behavior. Therefore, LTC would not fulfill Georges et al.'s property (adapted to the tagged setting). But LTC does arguably enforce stack safety. A looser, more observational definition of stack safety is needed to fit this situation.

We propose here a formal characterization of stack safety, based on the intuition of protecting function activations (both registers and stack frames) from each other. We use the tools of language-based security [23], treating function activations as security principals. We decompose stack safety into a family of properties describing the *integrity* and *confidentiality* of the caller's local state and the callee's behavior during the callee's execution, plus the *well-bracketed control flow* (WBCF) property articulated by Skorstengaard et al. [19]. While our properties are motivated by the desire to specify LTC precisely, they are stated abstractly in hopes of applying to other enforcement mechanisms.

We are not attempting to present a universal definition of stack safety for all systems. While many security properties can be described at the level of a high-level programming language and translated to a target machine by a secure compiler, stack safety cannot be defined in this way, since "the stack" is completely transparent in the definitions of most source languages. But neither is it satisfying as an entirely low-level property; indeed, at the lowest level, the specification of a "well-behaved stack" is almost vacuous. The ISA is not concerned with such questions as whether a caller's frame should be readable or writable to its callee. Those are the purview of high-level languages built atop the hardware stack.

Therefore, any low-level treatment of stack safety must begin by asking: which high-level features does our system support, and what are their security requirements? Different answers will beget different properties. We identify and define five security requirements that a system might try to enforce upon a function call: well-bracketed control flow, and the integrity and confidentiality of each of the caller and the callee. We apply these first to a simple system with very few features, then to a more realistic one supporting tail-call elimination, argument passing on the stack, and callee-save registers.

We show that our properties are useful for distinguishing correct enforcement from incorrect using QuickChick [25], [26], a property-based random testing tool for Coq. We find that LTC is flawed in a way that undermines both integrity and confidentiality; after correcting this flaw, the repaired LTC satisfies all our properties. Moreover, we modify LTC to protect the features of our more realistic system, and apply random testing to validate this extended protection mechanism against the extended properties.

In sum, we offer the following contributions:

- We give a novel characterization of stack safety as a collection of properties: confidentiality and integrity for callee and caller, plus well-bracketed control-flow. The properties are parameterized over a notion of external observation, allowing them to characterize lazy enforcement mechanisms.
- We extend these core definitions to describe a realistic setting with argument passing on the stack, callee-saves registers, and tail-call elimination. Our model is modular enough that handling these features is straightforward.
- We validate a tag-based enforcement mechanism, *Lazy Tagging and Clearing*, via property-based random testing, find that it falls short, and propose and validate a fix.

<sup>1</sup>Contrast Azevedo de Amorim et al.'s work on heap safety [24]: the concept of the heap figures directly in high-level language semantics and its security is therefore amenable to a high-level treatment.

In the next section, we give a brief overview of our framework and assumptions. In Section III, we walk through a function call in a simple example machine and discuss how each of our properties applies to it, informally. In the process we motivate the properties from a security perspective. In Section IV we formalize the machine model, its *security semantics*, and the stack safety properties built on these. Section V describes how to support an extended set of features. In Section VI we describe the micro-policies that we test, in Section VII the testing framework itself, and in Sections VIII and IX related and future work. Appendix A gives an (untested) proof-of-concept formalization of a more sophisticated, heap-like sharing model based on pointer provenance.

The accompanying artifact contains formal definitions (in Coq) of our properties, plus our testing framework. It does not include proofs: we use Coq primarily for the QuickChick testing library and for ensuring that our definitions are unambiguous. Formal proofs are left as future work.

## II. FRAMEWORK AND ASSUMPTIONS

Stack safety properties need to describe the behavior of machine code, but they naturally talk about function activations and stack contents—abstractions that are typically not visible at machine level. To bridge this gap, our properties are defined in terms of a security semantics layered on top of the standard execution semantics of the machine. The security semantics identifies certain state transitions of the machine as security-relevant operations, which update a notional security context. This context consists of an (abstract) stack of function activations, each associated with a view that maps each element of the machine state (memory location or register) to a security class (active, sealed, etc.) specifying how the activation can access the element. The action of a security-relevant operation on the context is defined by a set of rules that describe how the machine code makes use of the stack and registers to implement the function abstraction.

We define stack safety properties in terms of traces of *observable events* rather than internal machine states. This is particularly important for specifying lazy enforcement, which catches bad behaviors after they occur but before they can affect the trace. Observable events might include specific function calls (e.g., system calls that perform I/O), writes to special addresses representing memory-mapped regions, etc.

To characterize situations in which values should be kept secret or prevented from influencing future execution, we borrow the idea of *variant* states from the theory of non-interference. For example, to show that certain locations are kept secret, it suffices to vary their contents and check that the observable output does not change.

Finally, we define high-level security properties—integrity, confidentiality, and well-bracketed control flow—in terms of the security classes of state elements. These take the form of predicates on states and contexts that use variants, assertions about future return states, and comparison of event traces to capture the desired behavior without reference to internal implementation details. We introduce these properties

by example in Section III and formally in Section IV. In the remainder of this section we describe the underlying framework in more detail.

Machine Model: We assume a conventional ISA (e.g. RISC-V, x86-64, etc.), with registers including a program counter and stack pointer. We make no particular assumptions about the provenance of the machine code; in particular, we do not assume the use of any particular compiler. The machine may possibly be enhanced with enforcement mechanisms such as hardware tags [21], [27] or capabilities [16]. If so, we assume that the behavior of these mechanisms is incorporated into the basic step semantics of the machine, but we keep the enforcement state unchanged when constructing variant states. Failstop behavior by enforcement mechanisms is modeled as stepping to the same state (and thus silently diverging.)

Security Semantics and Property Structure: A security semantics extends a machine with additional context about the identities of current and pending functions (which act as security principals) and about the registers and memory they require to be secure. This added context is purely notional; it does not affect the behavior of the real machine. The security context evolves dynamically through the execution of security-relevant operations, which include calls, returns, and frame manipulation. Our security properties are phrased in terms of this context, often as predicates on future states ("when control returns to the current function...") or as relations on traces of future execution (hyper-properties).

Security-relevant operations abstract over the implementation details of the actions they take. In this paper, each operation corresponds to a single underlying machine instruction. One instruction may perform multiple operations. We assume that a compiler or other trusted source has provided labels to disambiguate instructions that have multiple purposes. For instance, in the tagged RISC-V architecture that we use in our examples and tests, calls and returns are conventionally performed using the <code>jal</code> ("jump-and-link") and <code>jalr</code> ("jump-and-link-register") instructions, but these instructions might also be used for other things.

We end up with an annotated version of the machine transition function written  $m \xrightarrow{\bar{\psi},e} m'$ , where m and m are machine states, e is an event, and  $\bar{\psi}$  is a list of security-relevant operations. We then lift this into a transition between pairs of machine states and contexts, by applying a set of operation-specific rules to transform each state and context to a new context, in parallel with the ordinary transition on states. The most important rules describe call and return operations. A call pushes a new view onto the context stack and changes the class of the caller's data to protect it from the new callee; a return reverses these steps. Other operations can serve to signal how parts of the stack frame are being used to store or share data, and their corresponding rules alter the classes of different state elements accordingly.

Exactly which operations and rules are needed depends on what code features we wish to support. The set of security-relevant operations  $(\Psi)$  covered in this paper is given in

| Operation $\psi \in \Psi$ | Parameters                            | Sections |
|---------------------------|---------------------------------------|----------|
| call                      | target address, argument registers    | III,IV   |
|                           | stack arguments (base, offset & size) | V,VII    |
| return                    |                                       | III,IV   |
| alloc                     | offset & size                         | III,IV   |
|                           | public flag                           | V,VII    |
| dealloc                   | offset & size                         | III,IV   |
| tailcall                  | (same as for call)                    | V,VII    |
| promote                   | register, offset & size               | A        |
| propagate                 | source register/address               | A        |
|                           | destination register/address          | A        |
| clear                     | target register/address               | A        |

TABLE I: Security-relevant operations and their parameters, with the Sections in which they are first used in the paper.

Table I. A core set of operations covering calls, returns, and local memory is introduced in the example in Section III and formalized in Section IV. An extended set covering simple memory sharing and tail-call elimination is described in Section V and tested in Section VII. The remaining operations are needed for the capability-based model in Appendix A.

Views and Security Classes: The security context consists of a stack of views: functions that map each state element to a security class: public, free, active, or sealed.

State elements that are outside of the stack—general-purpose memory used for globals and the heap, as well as the code region and globally shared registers—are always labeled *public*. We place security requirements on some *public* elements for purposes of the WBCF property, and a given enforcement mechanism might restrict their access (e.g., by rendering code immutable), but for integrity and confidentiality purposes they are considered accessible at all times.

For a newly active function, every stack location that is available for use but not yet initialized is seen as *free*. From the perspective of the caller, the callee has no obligations regarding its use of free elements.

Arguments are marked *active*, meaning that their contents may be safely used. When a function allocates memory for its own stack frame, that memory will also be *active*. Then, on a call, *active* elements that are not being used to communicate with the new callee will become *sealed*—reserved for an inactive principal, and expected to be unchanged when it becomes active again.

Instantiating the Framework: Conceptually, the following steps are needed to instantiate the framework to a specific machine and code style: (i) define the base machine semantics, including any hardware security enforcement features; (ii) identify the set of security-relevant operations and rules required by the code style; (iii) determine how to label machine instructions with security-relevant operations as appropriate; (iv) specify the form of observable events.

Threat Model and Limitations: When our properties are used to evaluate a system, the threat model will depend on the details of that system. However, there are some constraints that our design puts on any system. In particular, we must trust that the security-relevant operations have been correctly labeled. If a compiled function call is not marked as such,

then the caller's data might not be protected from the callee; conversely, marking too many operations as calls will simply cause otherwise safe programs to be rejected.

We do not assume that low-level code adheres to any fixed calling convention or implements any particular source-language constructs. Indeed, if the source language is C, then high-level programs might contain undefined behavior, in which case they might be compiled to arbitrary machine code. A given enforcement mechanism or target architecture might place additional constraints, particularly on the behavior of call and return sequences. For instance, extant implementations tend to assume implicitly that callee-saved registers have their values maintained by whichever compiler generated their code. Our properties explicitly state this as a requirement, which could be enforced by a micro-policy, a well-behaved compiler, or other enforcement technique. Roessler and DeHon include the compiler in their trusted computing base, so our properties are stronger than necessary to characterize their micro-policies.

In general, it is impossible to distinguish buggy machine code from an attacker. In our examples we will identify one function or another as an attacker, but we do not require any static division between trusted and untrusted code, and we aim to protect even buggy code.

This is a strong threat model, but it does omit some important aspects of stack safety in real systems: in particular, it does not address concurrency. Hardware and timing attacks are also out of scope.

## III. PROPERTIES BY EXAMPLE

In this section we introduce our security property definitions by means of small code examples, using a simplified set of security-relevant operations for calls, returns, and private allocations. Figure 1 gives C code and possible corresponding compiled 64-bit RISC-V code for a function main, which takes an argument secret and initializes a local variable sensitive to contain potentially sensitive data. Then main calls another function f, and afterward performs a test on sensitive to decide whether to output secret. Since sensitive is initialized to 0, the test should fail, and main should instead output the return value of f. Output is performed by writing to the special global out, and we assume that such writes are the only observable events in the system.

The C code is compiled using the standard RISC-V calling conventions [28]. In particular, the first function argument and the function return value are both passed in a0. Memory is byte-addressed and the stack grows towards lower addresses. We assume that main begins at address 0 and its callee f at address 100.

We now consider how f might misbehave and violate desirable stack safety properties associated with main. To put the violations in a security framework, suppose that f is actually an attacker seeking to leak secret. It might do so in a number of ways, shown as snippets of assembly code in Fig. 2. Leakage is most obviously viewed as a violation of main's confidentiality. In Fig. 2a, f takes an offset from the stack

```
volatile int out;
void main(int secret) {
    int sensitive = 0;
    int res = f();
    if (sensitive == 42)
         out = secret;
    else
         out = res;
       0:
           addi sp, sp, -20
                               alloc (-20, 20)
       4:
           sd ra, 12 (sp)
       8:
           sw a0,8(sp)
      12:
           sw zero, 4(sp)
     16:
            jal f, ra
                               call \varepsilon
      20:
           sw a0,0(sp)
           lw a4,4(sp)
      24:
           li a5,42
      28:
      32:
           bne a4,a5,L1
      36:
           lw a0,8(sp)
      40:
           sw a0, out
      44:
            j L2:
     48:
           lw a0,0(sp)
 L1,
      52:
           sw a0, out
 L2,
     56:
           ld ra, 12 (sp)
                               dealloc (0,20)
      60:
           addi sp, sp, 20
      64:
            jalr ra
                               return
                         8(SP) 12(SP)
                    4(SP)
               SP
              res
                    sens
                          sec
                                      raa
```

Fig. 1: Example: C and assembly code for main, and layout of its stack frame; the stack grows to the left.

pointer, accesses secret, and directly outputs it. But more subtly, even if somehow prevented from outputting secret directly, f can instead return that value so that main stores it to out, as in Fig. 2b. Beyond simply reading secret, the attacker might overwrite sensitive with 42, guaranteeing that main publishes its own secret unintentionally (Fig. 2c). Attacks of this kind do not violate main's confidentiality, but rather its *integrity*. In Fig. 2d, the attacker arranges to return to the wrong instruction, thereby bypassing the check and publishing secret regardless, violating the program's well-bracketed control flow (WBCF.) In Fig. 2e, a different attack violates WBCF, this time by returning to the correct program counter but with the wrong stack pointer.<sup>2</sup>

The security semantics for this program is based on the security-relevant events noted in the right columns of Figs. 1 and 2, namely execution of instructions that allocate or deal-locate space, make a call, or make a return.

Our security semantics attach a security context to the machine state, which consists of a view V and a stack  $\sigma$  of

<sup>&</sup>lt;sup>2</sup>We pad the last two variants with nops just so that all the snippets have the same length, which keeps the step numbering uniform in Fig. 3.

```
100:
       lw a4,8(sp)
104:
       sw a4, out
108:
       li a0,1
112:
       jalr ra
                        return
              (a) Leaking secret directly
100:
       lw a4,8(sp)
104:
       mov a4, a0
108:
       sw zero, -4 (sp)
112:
        jalr ra
                            return
             (b) Leaking secret indirectly
       li a5,42
100:
104:
       sw a5,4(sp)
108:
       li a0,1
112:
       jalr ra
                        return
              (c) Attacking sensitive
100:
       addi ra, ra, 16
104:
       nop
108:
       nop
112:
       jalr ra
                          return
               (d) Attacking control flow
100:
       addi sp, sp, 8
104:
       nop
108:
       nop
112:
       jalr ra
                         return
           (e) Attacking stack pointer integrity
```

Fig. 2: Example: assembly code alternatives for f as an attacker.

pending activations' views. Figure 3 shows how the security context evolves over the first few steps of the program. (The formal details of the security semantics are described in Section IV, and the context evolution rules are formalized in Fig. 7.) Execution begins at the start of main, where the program counter (PC) is zero, and with the stack pointer (SP) at address 1000. State transitions are numbered and labeled with a list of security operations, written  $\downarrow \overline{\psi}$  between steps.

The initial view  $V_0$  maps all stack addresses below SP to free and the remainder of memory to public. The sole used argument register, a0, is mapped to active; other caller-save registers are mapped to free and callee-save registers to sealed. Step 1 allocates a word each for secret, sensitive, and res, as well as two words for the return address. This has the effect of marking those bytes active. (We use  $V[\cdot]$  to denote updates to V.)

At step 5, the current principal's record is pushed onto the inactive list. Its return target is the return address of the call, and the stack pointer target is the stack pointer at the moment of call. The callee's view is updated from the caller's such that all *active* memory locations become *sealed*. (For now we assume no sharing of memory between activations; data is

passed only through argument registers, which remain active. In the presence of memory sharing, some memory would remain active, too.) Function f does not take any arguments; if it did, any registers containing them would be mapped to *active*, while any non-argument, caller-saved registers are mapped to *free*. In the current example, only register a0 has a change in security class. All callee-save registers remain *sealed* for all calls. Thus, if we varied the assembly code for the example slightly so that sensitive was stored in a callee-save register (e.g. s0) rather than in memory, its security class would still be *sealed* at the entry to f. At step 9, f returns, and the topmost inactive view, that of main, is restored.

We now show how this security semantics can be used to define notions of confidentiality, integrity, and correct control flow in such a way that many classes of bad behavior, including the attacks in Fig. 2, are detected as security violations.

Well-bracketed Control Flow: To begin with, what if f returns to an unexpected place (i.e.  $PC \neq 20$  or  $SP \neq 980$ )? We consider this to violate WBCF. WBCF is a relationship between call steps and their corresponding return steps: just after the return, the program counter should be at the next instruction following the call, and the stack pointer should be the same as it was before the call. Both of these are essential. In Fig. 2d, the attacker adds 16 to the return address and then returns, thus bypassing the if-test in the code and outputting secret. In Fig. 2e, the attacker returns with SP' = 988 instead of the correct SP = 980. In this scenario, given the layout of main's frame,

| SP ↓ |      | $SP' \downarrow$ |        |              |
|------|------|------------------|--------|--------------|
| res  | sens | sec              | $ra_1$ | ${\tt ra}_2$ |

main's attempt to read sensitive will instead read part of the return address, and its attempt to output res will instead output secret.

Before the call, the program counter is 16 and the stack pointer is 980. So we define a predicate on states that should hold just after the return:  $Ret \ m \triangleq m[PC] = 20 \land m[SP] = 980$ . We can identify the point just after the return (if a return occurs) as the first state in which the pending call stack is smaller than it was just after the call. WBCF requires that if m is the state at that point, then  $Ret \ m$  holds.

Stack Integrity: Like WBCF, stack integrity defines a condition at the call that must hold upon return. This time the condition applies to all of the memory in the function's frame. In Fig. 3 we see the lifecycle of an allocated frame: upon allocation, the view labels it active, and when a call is made, it instead becomes sealed. Intuitively, the integrity of main is preserved if, when control returns to it, any sealed elements are identical to when it made the call. Again, we need to know when a caller has been returned to, and we use the same mechanism of checking the depth of the call stack. In the case of the call from main to f, the sealed elements are the addresses 980 through 999 and callee-saved registers such as the stack pointer. Note that callee-saved registers often

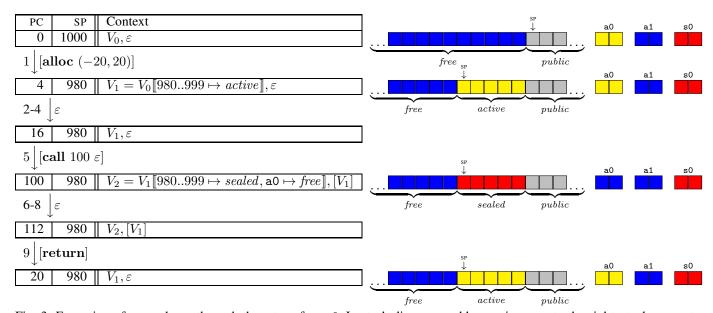


Fig. 3: Execution of example up through the return from f. In stack diagrams, addresses increase to the right, stack grows to the left, and boxes represent 4-byte words.

change during the call—but if the caller accesses them after the call, it should find them restored to their prior value.

While it would be simple to define integrity as "all sealed elements retain their values after the call," this would be stricter than necessary. Suppose that a callee overwrites some data of its caller, but the caller never accesses that data (or only does so after re-initializing it.) This would be harmless, with the callee essentially using the caller's memory as scratch space, but the caller never seeing any change.

For a set of elements K, a pair of states m and n are K-variants if their values an only disagree on elements in K. We say that the elements of K are irrelevant in m if they can be replaced by arbitrary other values without changing the observable behavior of the machine. All other elements are relevant.<sup>3</sup>

We define *caller integrity* (CLRI) as the property that every relevant element that is *sealed* under the callee's view is restored to its original value at the return point.

In our example setting, the observation trace consists of the sequence of values written to out. The example in Fig. 2c modifies the value of sensitive, which is sealed. Figure 4 shows the state just after the call at step 5, assuming that sec is 5. Similar to WBCF, we define Int as a predicate on states that holds if all relevant sealed addresses in m are the same as after step 5. We require that Int hold on the state following the matching return, which is reached by step 9. Here sensitive has obviously changed, but is it relevant? Consider a variant state in which sensitive has any other value, say 43. As execution continues after the return from the original state, it passes the if-test on sensitive, whereas

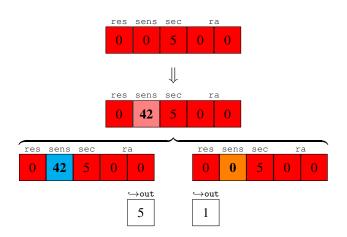


Fig. 4: Integrity Violation

the execution from the variant does not, resulting in differing outputs. Therefore sensitive *is* relevant, so *Int* does not hold, and integrity has indeed been violated.

Caller Confidentiality: We treat confidentiality as a form of non-interference as well: the confidentiality of a caller means that its callee's behavior is dependent only on publicly visible data, not the caller's private state. This also requires that the callee initialize memory before reading it. As we saw in the examples, we must consider both the observable events that the callee produces during the call and the changes that the callee makes to the state that might affect the caller after the callee returns.

Consider the state m after step 5, whose context is  $(V_2, \sigma)$ , with the attacker from Fig. 2a. We take a variant state over the set of elements that are *sealed* in  $V_2$  (see Fig. 5.) If we take a trace of execution from each state until it returns, the

<sup>&</sup>lt;sup>3</sup>This story is slightly over-simplified. If an enforcement mechanism maintains additional state associated with elements, such as tags, we don't want that state to vary. Formal definitions of variants and relevance that incorporate this wrinkle are given in Section IV-D.

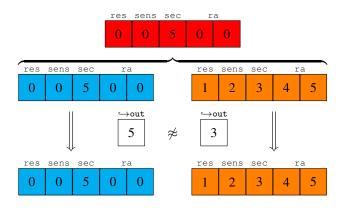


Fig. 5: Internal Confidentiality Violation

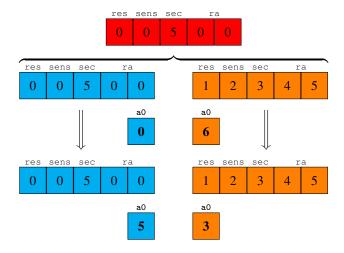


Fig. 6: Return-time Confidentiality Violation

traces may differ, in this case outputting 5 (the original value of secret) and 4 (its value in the variant) respectively. This is a violation of *internal confidentiality* (formalized in Table II, line 3a).

But, in Fig. 2b, we also saw an attacker that exfiltrated the secret by reading it and then returning it, in a context where the caller would output the returned value. Figure 6 shows the behavior of the same variants under this attacker, but in this case, there is no output during the call. Instead the value of secret is extracted and placed in a0, the return value register. We wish to identify this as a confidentiality violation, again by considering variants of the sealed elements in  $V_2$ , but capturing the required property is subtle. The return states do not agree on the value of a0, but then, the disagree on all of the other states, too. The difference is that a0 has changed during the call (in both the original and the variant, although only one of these would be necessary). The disagreement between the return states must therefore depend on a secret (in fact, the variable secret). Unless a0 happens to be irrelevant to the caller, this is a violation of what we term return-time confidentiality (formalized in Table II, line 3b).

Structurally, return-time confidentiality resembles integrity, but now dealing with variants. We begin with a state immediately following a call, m. We consider an arbitrary variant state, n, which may vary any element that is sealed or free, i.e., any element that is not used legitimately to pass arguments. Caller confidentiality therefore can be thought of as the callee's insensitivity to elements in its initial state that are not part of the caller-callee interface.

We define a binary relation Conf on pairs of states, which holds on eventual return states m' and n' if all relevant elements are uncorrupted relative to m and n. An element is corrupted if it differs between m' and n', and it either changed between m and m' or between n and n'.

Finally, we define *caller confidentiality* (CLRC) as the combination of internal and return-time confidentiality (Table II, line 3).

The Callee's Perspective: We presented our initial example from the perspective of the caller, but a callee may also have privilege that its caller lacks, and which must be protected from the caller. Consider a function that makes a privileged system call to obtain a secret key, and uses that key to perform a specific task. An untrustworthy or erroneous caller might attempt to read the key out of the callee's memory after return, or to influence the callee to cause it to misuse the key itself!

Where the caller's confidentiality and integrity are concerned with protecting specific, identifiable state—the caller's stack frame—their callee equivalents are concerned with enforcing the expected interface between caller and callee. Communication between the principals should occur only through the state elements that are designated for the purpose: those labeled *public* and *active*.

Applying this intuition using our framework, *callee confidentiality* (CLEC) turns out to resemble CLRI, extended to every element that is not marked *active* or *public* at call-time. The callee's internal behavior is represented by those elements that change over the course of its execution, and which are not part of the interface with the caller. At return, those elements should become irrelevant to the subsequent behavior of the caller

Similarly, in *callee integrity* (CLEI), only elements marked *active* or *public* at the call should influence the behavior of the callee. It may seem odd to call this integrity, as the callee does not have a private state. But an erroneous callee that performs a read-before-write within its stack frame, or which uses a non-argument register without initializing it, is vulnerable to its caller seeding those elements with values that will change its behavior. The fact that well-behaved callees have integrity by definition is probably why callee integrity is not typically discussed.

## IV. FORMALIZATION

We now give a formal description of our machine model, security semantics, and properties. Our definitions abstract over: (i) the details of the target machine architecture and ABI, (ii) the set of security-relevant operations and their effects on

the security context, (iii) the set of observable events, and (iv) a notion of value compatibility.

#### A. Machine

The building blocks of a machine are *words* and *registers*. Words are ranged over by w and, when used as addresses, a, and are drawn from the set  $\mathcal{W}$ . Registers in the set  $\mathcal{R}$  are ranged over by r, with the stack pointer given the special name SP; some registers may be classified as caller-saved or callee-saved. Along with the program counter, PC, these are referred to as *state elements* k in the set  $\mathcal{K} ::= PC|\mathcal{W}|\mathcal{R}$ .

A machine state  $m \in \mathcal{M}$  is a map from state elements to a set  $\mathcal{V}$  of values. Each value v contains a payload word, written |v|. We write m[k] to denote the value of m at k and m[v] as shorthand for m[|v|]. Depending on the specific machine being modeled, values may also contain other information relevant to hardware enforcement (such as a tag). When constructing variants (see below), this additional information should not be varied. To capture this idea, we assume a given compatibility equivalence relation  $\sim$  on values, and lift it element-wise to states. Two values should be compatible if their non-payload information (e.g. their tag) is identical.

The machine has a step function  $m \xrightarrow{\bar{\psi},e} m'$ . Except for the annotations over the arrow, this function just encodes the usual ISA description of the machine's instruction set. The annotations serve to connect the machine's operation to our security setting:  $\bar{\psi}$  is a list of security-relevant operations drawn from an assumed given set  $\Psi$ , and e is an (potentially silent) observable event; these are described further below.

## B. Security semantics

The security semantics operates in parallel with the machine. Each state element (memory word or register) is given a security class  $l \in \{public, active, sealed, free\}$ . A view  $V \in VIEW$  maps elements to security classes. For any security class l, we write l(V) to denote the set of elements k such that V = l. The initial view  $V_0$  maps all stack locations to free, all other locations to public, and registers based on which set they belong to: sealed for callee-saved, free for caller-saved except for those that contain arguments at the start of execution, which are active, and public otherwise.

A (security) *context* is a pair of the current activation's view and a list of views representing the call stack (pending inactive principals), ranged over by  $\sigma$ .

$$c \in C ::= VIEW \times list \ VIEW$$

The initial context is  $c_0 = (V_0, \varepsilon)$ .

Section III describes informally how the security context evolves as the system performs security-relevant operations. Formally, we combine each machine state with a context to create a *combined state* s=(m,c) and lift the transition to  $\Longrightarrow$  on combined states. At each step, the context updates based on an assumed given function  $Op: \mathcal{M} \to C \to \psi \to C$ . Since a single step might correspond to multiple operations, we apply Op as many times as needed, using foldl.

$$range \ r \ off \ sz \ m \triangleq \{m[r] + i| off \leq i < off + sz\}$$

$$K = range \ SP \ off \ sz \ m \cap \{a \mid V \ a = free\}$$

$$V' = V[a \mapsto sealed \mid a \in K]$$

$$Op \ m \ (alloc \ off, sz) \ (V, \sigma) = (V', \sigma)$$

$$b = m[SP] + off$$

$$V' = V[a \mapsto free \mid b \leq a < b + sz \land V \ a = active]$$

$$Op \ m \ (dealloc \ off, sz) \ (V, \sigma) = (V', \sigma)$$

$$V' = V[r \mapsto free \mid r \in CLR][r \mapsto public \mid r \in \overline{r_{args}}]$$

$$V'' = V'[a \mapsto sealed \mid V' \ a = active]$$

$$Op \ m \ (call \ a_{target} \ \overline{r_{args}}) \ (V, \sigma) = (V'', V :: \sigma)$$

$$\sigma = (V, a_{ret}, a_{sp}) :: \sigma'$$

$$Op \ m \ return \ (\_, \sigma) = (V, \sigma')$$

Fig. 7: Basic Operations

A definition of Op is most convenient to present decomposed into rules for each operation. We have already seen the intuition behind the rules for alloc, call, and ret. For the machine described in the example, the Op rules would be those found in Fig. 7. Note that Op takes as its first argument the state before the step.

## C. Events and Traces

We abstract over the events that can be observed in the system, assuming just oa given set EVENTS that contains at least the element  $\tau$ , the silent event. Other events might represent certain function calls (i.e., system calls) or writes to special addresses representing memory-mapped regions. A trace is a nonempty, finite or infinite sequence of events, ranged over by  $\mathcal{E}$ . We use "·" to represent "cons" for traces, reserving "::" for list-cons.

We are particularly interested in traces that end just after a function returns. We define these in terms of the depth d of the security context's call stack  $\sigma$ . We write  $d \hookrightarrow s$  for the trace of execution from a state s up to the first point where the stack depth is smaller than d, defined coinductively by these rules:

$$\frac{|\sigma| < d}{d \hookrightarrow (m, (V, \sigma)) = \tau}$$

$$\underline{(m, (V, \sigma)) \Longrightarrow (m', c', e) \quad |\sigma| \ge d \quad d \hookrightarrow (m', c') = \mathcal{E}}$$

$$d \hookrightarrow (m, (V, \sigma)) = e \cdot \mathcal{E}$$

When d=0, the trace will always be infinite; in this case we omit d and just write  $\hookrightarrow s$ .

Two event traces  $\mathcal{E}_1$  and  $\mathcal{E}_2$  are *similar*, written  $\mathcal{E}_1 \approx \mathcal{E}_2$ , if the sequence of non-silent events is the same. That is, we compare up to deletion of  $\tau$  events. Note that this results in an infinite silent trace being similar to any trace. So, a trace that silently diverges due to a failstop will fulfill this property vacuously.

$$\begin{array}{ccc} & & & & & \mathcal{E}_1 \eqsim \mathcal{E}_2 \\ \hline \mathcal{E} \eqsim \mathcal{E} & & & & e \cdot \mathcal{E}_2 \\ \hline \mathcal{E}_1 \eqsim \mathcal{E}_2 & & & & \mathcal{E}_1 \eqsim \mathcal{E}_2 \\ \hline \tau \cdot \mathcal{E}_1 \eqsim \mathcal{E}_2 & & & & \mathcal{E}_1 \eqsim \tau \cdot \mathcal{E}_2 \\ \hline \end{array}$$

## D. Variants, corrupted sets, and "on-return" assertions

Two (compatible) states are variants with respect to a set of elements K if they agree on the value of every element not in K. Our notion of non-interference involves comparing the traces of such K-variants. We use this to define sets of irrelevant elements.

**Definition 1.** The difference set of two machine states m and m', written  $\Delta(m, m')$ , is the set of elements k such that  $m[k] \neq m'[k]$ .

**Definition 2.** Machine states m and n are K-variants, written  $m \approx_K n$ , if  $m \sim n$  and  $\Delta(m, n) \subseteq K$ .

**Definition 3.** An element set K is *irrelevant* to state (m, c), written  $(m, c) \parallel K$ , if for all n such that  $m \approx_K n$ ,  $\hookrightarrow (m, c) \approx \hookrightarrow (n, c)$ .

When comparing the behavior of variant states, we need a notion of how their differences have influenced them.

**Definition 4.** The *corrupted set*  $\bar{\Diamond}(m,m',n,n')$  is the set  $(\Delta(m,m')\cup\Delta(n,n'))\cap\Delta(m',n')$ .

If we consider two execution sequences, one from m to m' and the other from n to n', then  $\bar{\Diamond}(m,m',n,n')$  is the set of elements that change in one or both executions and end up with different values. Intuitively, this captures the effect of any differences between m and n, i.e., the set of values that are "corrupted" by those differences.

Our "on-return" assertions are defined using a second-order logical operator  $d \uparrow P$ , pronounced "P holds on return from depth d," where P is a predicate on machine states. This is a coinductive relation similar to "weak until" in temporal logic—it also holds if the program never returns from depth d.

$$\frac{|\sigma| < d \quad P \ m}{(d \uparrow P) \ (m, (V, \sigma))} \text{RETURNED}$$

$$|\sigma| \ge d \quad (d \uparrow P) \ (m', c')$$

$$\frac{(m, (V, \sigma)) \stackrel{\overline{\psi}, e}{\Longrightarrow} (m', c')}{(d \uparrow P) \ (m, (V, \sigma))} \text{STEP}$$

Similarly, we give a binary equivalent for use in confidentiality. We define  $\uparrow$  so that (m,c)  $(d\uparrow R)$  (m',c') holds if R holds on the first states that return from depth d after (m,c) and (m',c'), respectively. Once again,  $\uparrow$  is coinductive.

$$\begin{aligned} & |\sigma_1| < d \quad |\sigma_2| < d \quad m_1 \ R \ m_2 \\ & \overline{(m_1,(V_1,\sigma_1)) \ (d \Uparrow R) \ (m_2,(V_2,\sigma_2))} \end{aligned} \text{RETURNED} \\ & |\sigma_1| \ge d \quad (m_1,(V_1,\sigma_1)) \xrightarrow{\overline{\psi},\, \xi} (m_1',\, c_1') \\ & \underline{(m_1',\, c_1') \ (d \Uparrow R) \ (m_2,(V_2,\sigma_2))} \quad \text{LEFT} \\ & \overline{(m_1,(V_1,\sigma_1)) \ (d \Uparrow R) \ (m_2,(V_2,\sigma_2))} \end{aligned} \\ & |\sigma_2| \ge d \quad (m_2,(V_2,\sigma_2)) \xrightarrow{\overline{\psi},\, \xi} (m_2',\, c_2') \\ & \underline{(m_1,(V_1,\sigma_1)) \ (d \Uparrow R) \ (m_2',\, c_2')} \quad \text{RIGHT} \\ & \overline{(m_1,(V_1,\sigma_1)) \ (d \Uparrow R) \ (m_2,(V_2,\sigma_2))} \end{aligned}$$

## E. Properties

Finally, the core property definitions are given in Table II, arranged to show their commonalities and distinctions. Each definition gives a criterion quantified over states s that immediately follow call steps. If an execution includes a transition  $s' \xrightarrow{\overline{\psi}} s$  where call  $a \ \overline{r} \in \overline{\psi}$ , then s is the target of a call. As a shorthand, we write that each property is defined by a criterion that must hold "for all call targets s," or, in the case of WBCF, "for all call steps  $s \Longrightarrow s'$ ."

- 1. WBCF: Given a call step  $(m, (V, \sigma)) \implies (m', (V', \sigma'))$ , we define the predicate Ret to hold on states m'' whose stack pointer matches that of m and whose program counter is at the next instruction. A system enjoys WBCF if, for every call transition, Ret holds just after the callee returns (i.e., the call stack shrinks).
- 2. CLRI: When the call target is  $(m,(V,\sigma))$ , we define the predicate Int to hold on states m' if any elements that are both sealed in V and in the difference set between m and m' are irrelevant. A system enjoys CLRI if, for every call, Int holds just after the corresponding return.
- 3. CLRC: When the call target is  $(m,(V,\sigma))$ , we begin by taking an arbitrary n that is a K-variant of m, where K is the set of sealed elements in V. We require that two clauses hold. On line 3a, the behavior of a trace from  $(m,(V,\sigma))$  up to its return must match that of  $(n,(V,\sigma))$ . On line 3b, we define a relation Conf that relates states m' and n' if their corrupted set (relative to m and n) is irrelevant, and require that it hold just after the returns from the callees that start at  $(m,(V,\sigma))$  and  $(n,(V,\sigma))$ . A system enjoys CLRC if both clauses hold for every call.
- 4. CLEC: We consider the callee's private behavior to be any changes that it makes to the state outside of legitimate channels—elements marked active or public. The remainder should be kept secret, which is to say, irrelevant to future execution. Similar to CLRI, given a call target  $(m, (V, \sigma))$ , we define a predicate CConf to hold on states m' if the difference set between m and m', excluding active or public locations, is irrelevant. A system enjoys CLEC if, for every call, CConf holds just after the corresponding return.
- 5. CLEI: Callee integrity means that the caller does not influence it outside of legitimate channels. The caller's influence can be seen internally, or in corrupted data on return, just like the caller's secrets would be under CLRC. So, for a call target  $(m, (V, \sigma))$ , we take an arbitrary n that is a K-variant of m, where K is the set elements that are not active or public. The remainder of the property is identical to CLRC.

## V. EXTENDED CODE FEATURES

The system we model in Sections III and IV is very simple, but our framework is designed to make it easy to add support for additional code features. To support argument passing on the stack, we just add new parameters to the existing security-relevant operations, and refine how they update the security context. The remainder of the properties do not change at all. To add tail-calls, we add and define a new operation, and since it is a kind of call, we add it to the definition of call targets.

```
WBCF \triangleq (|\sigma'| \uparrow Ret) \ (m', (V', \sigma'))
                                                                                      where Ret \ m'' \triangleq m''[SP] = m[SP]
                                                                                                                                                                 for all calls (m, (V, \sigma)) \Longrightarrow (m', (V', \sigma'))
                                                                                      and m''[PC] = m[PC] + 4
2
       CLRI \triangleq (|\sigma| \uparrow Int) \ (m, (V, \sigma))
                                                                                      where Int m' \triangleq m' \parallel (sealed(V) \cap \Delta(m, m')) for all call targets (m, (V, \sigma))
3
      CLRC \triangleq \forall n \text{ s.t. } m \approx_K n,
                                                                                      where K = sealed(V)
                                                                                                                                                                 for all call targets (m, (V, \sigma))
3a
                    |\sigma| \hookrightarrow (m, (V, \sigma)) \simeq |\sigma| \hookrightarrow (n, (V, \sigma))
                     and (m, (V, \sigma)) (|\sigma| \uparrow Conf) (n, (V, \sigma)) where (m' Conf n') \triangleq m' || \bar{\Diamond}(m, n, m', n')
3b
      \mathsf{CLEC} \triangleq (|\sigma| \uparrow \mathit{CConf}) \ (m, (V, \sigma))
4
                                                                                      where CConf\ m' \triangleq m' \parallel (\Delta(m, m') - K)
                                                                                                                                                                 for all call targets (m, (V, \sigma))
                                                                                      where K = public(V) \cup active(V)
        CLEI \triangleq \forall n \text{ s.t. } m \approx_K n,
5
                                                                                      where K = \mathcal{K} - (public(V) \cup active(V))
                                                                                                                                                                 for all call targets (m, (V, \sigma))
5a
                    |\sigma| \hookrightarrow (m, (V, \sigma)) \simeq |\sigma| \hookrightarrow (n, (V, \sigma))
                                                                                     where (m' \ CInt \ n') \triangleq m' \parallel \bar{\Diamond}(m, n, m', n')
5b
                     and (m, (V, \sigma)) (|\sigma| \uparrow CInt) (n, (V, \sigma))
```

TABLE II: Properties

The rules for the extended security semantics are given in Fig. 8; the rules in Fig. 7 can be recaptured by instantiating call with  $\overline{sa}$  as the empty set, and alloc with flag f.

## A. Sharing Stack Memory

In our examples, we have presented a vision of stack safety in which the interface between caller and callee is in the registers that pass arguments and return values. This is frequently not the case in a realistic setting. Arguments may be passed on the stack because there are too many to pass in registers, as variadic arguments, or because they are composite types that inherently have pass-by-reference semantics. The caller may also pass an object by reference in the C++ style, or take its address and pass it as a pointer.

We refine our call operation to make use of the information that we have about which memory contain arguments,  $\overline{sa}$ .  $\overline{sa}$  is a set of triples of a register, an offset from the value of that register, and a size. We first define the helpful set  $passed \overline{sa} m$ , then extend the call operation to keep all objects in passed marked as active and seal everything else (Fig. 8b).

Using this mechanism, a call-by-value argument passed on the stack at an SP-relative offset is specified by the triple (SP, off, sz). In this case, only the immediate callee gains access to the argument location. A C++-style call-by-reference argument passed in r is instead specified by (r, 0, sz), which allows the reference to be passed further down the stack.

If the address of an object is taken directly and passed as a pointer, we simply classify the object as "public" and give it no protection against access by other functions. We extend the alloc operation with a boolean flag, where t indicates that the allocation is public, and f that it is private. If space for multiple objects is allocated in a single step, that step can make multiple allocation operations, each labeled appropriately. Public objects are labeled public rather than active, so they are never sealed at a call (Fig. 8a). Providing more fine-grained control over sharing is desirable, but seems to require a considerably more complex model; Appendix A describes one approach, based on capabilities.

## B. Tail Calls

The rule for a tail call is similar to that for a normal call. We do not push the caller's view onto the stack, but replace it outright. This means that a tail call does not increase the size of the call stack, and therefore for purposes of our properties,

all tail calls will be considered to return simultaneously when the eventual **return** operation pops the top of the stack.

Since the caller will not be returned to, it does not need integrity, but it should still enjoy confidentiality. We set its frame to *free* rather than *sealed* to express this. In terms of Table II, we replace "call" with "call or tail call" in CLRC, CLEC, and CLEI.

## VI. ENFORCEMENT

We implement and test two micro-policies from Roessler and DeHon [1]: Depth Isolation (DI) and Lazy Tagging and Clearing (LTC). They share a common structure: each function activation is assigned a "color" n representing its identity. Stack locations belonging to that activation are tagged STACK n, and while the activation is running, the tag on the program counter (PC tag) is PC n. Stack locations not part of any activation are tagged UNUSED.

In DI, n always corresponds to the depth of the stack when the function is called. A function must initialize its entire frame upon entry in order to tag it, and then clear the frame before returning. During normal execution, the micro-policy rules only permit load and store operations when the target memory is tagged with the same depth as the current PC tag, or, for store operations, if the target memory is tagged UNUSED.

In LTC, rather than initialize the entire frame at entry, a function initializes each location's tag when it writes to it. It does not check if those writes are legal! If the PC tag is PC n, then any stack location that recieves a store will be tagged STACK n. On a load, the micro-policy failstops if the source memory location is tagged UNUSED or STACK n for some n that doesn't match the PC tag.

Blessed Sequences: To implement this discipline, blessed instruction sequences appear at the entry and exit of each function, which manipulate tags as just described while performing the usual tasks of saving/restoring the return address to/from the stack and adjusting the stack pointer. A blessed sequence uses further tags to guarantee that the full sequence executes from the beginning—no jumping into the middle.

Protecting Registers: Roessler and DeHon do not protect registers, since the compiler is in the trusted computing base, but we support threat models that do not. In particular, CLRI requires callee-saved registers to be saved and restored properly. We extend DI and LTC so that callee-saved registers, too, are tagged with the color of the function that is using

range 
$$r$$
 off  $sz$   $m riangleq \{m[r]+i|off \leq i < off + sz\}$ 

$$K = range ext{ SP off } sz ext{ } m \cap \{a \mid V \text{ } a = free\}$$

$$V' = V \llbracket a \mapsto sealed \mid a \in K \rrbracket$$

$$Op m ext{ } (alloc ext{ } f \text{ } off, sz) \text{ } (V, \sigma) = (V', \sigma)$$

$$K = range ext{ SP off } sz ext{ } m \cap \{a \mid V \text{ } a = free\}$$

$$V' = V \llbracket a \mapsto public \mid a \in K \rrbracket$$

$$Op m ext{ } (alloc ext{ } t \text{ } off, sz) \text{ } (V, \sigma) = (V', \sigma)$$

$$b = m[sP] + off$$

$$V' = V \llbracket a \mapsto free \mid b \leq a < b + sz \wedge V \text{ } a = active} \rrbracket$$

$$Op m ext{ } (dealloc ext{ } off, sz) \text{ } (V, \sigma) = (V', \sigma)$$

$$b = m[sP] + off$$

$$V' = V \llbracket a \mapsto free \mid V' \text{ } a = active \wedge a \notin (passed \overline{sa} \text{ } m) \rrbracket$$

$$Op m ext{ } (tailcall \text{ } a_{target} \overline{r_{args}} \overline{sa}) \text{ } (V, \sigma) = (V', \sigma)$$

$$Op m ext{ } (tailcall \text{ } a_{target} \overline{r_{args}} \overline{sa}) \text{ } (V, \sigma) = (V', \sigma)$$

$$Op m ext{ } (tailcall \text{ } a_{target} \overline{r_{args}} \overline{sa}) \text{ } (V, \sigma) = (V', \sigma)$$

$$Op m ext{ } (tailcall \text{ } a_{target} \overline{r_{args}} \overline{sa}) \text{ } (V, \sigma) = (V', \sigma)$$

$$Op m ext{ } (tailcall \text{ } a_{target} \overline{r_{args}} \overline{sa}) \text{ } (V, \sigma) = (V', \sigma)$$

$$Op m ext{ } (tailcall \text{ } a_{target} \overline{r_{args}} \overline{sa}) \text{ } (V, \sigma) = (V', \sigma)$$

$$Op m ext{ } (tailcall \text{ } a_{target} \overline{r_{args}} \overline{sa}) \text{ } (V, \sigma) = (V', \sigma)$$

$$Op m ext{ } (tailcall \text{ } a_{target} \overline{r_{args}} \overline{sa}) \text{ } (V, \sigma) = (V', \sigma)$$

$$Op m ext{ } (tailcall \text{ } a_{target} \overline{r_{args}} \overline{sa}) \text{ } (V, \sigma) = (V', \sigma)$$

$$Op m ext{ } (tailcall \text{ } a_{target} \overline{r_{args}} \overline{sa}) \text{ } (V, \sigma) = (V', \sigma)$$

$$Op m ext{ } (tailcall \text{ } a_{target} \overline{r_{args}} \overline{sa}) \text{ } (V, \sigma) = (V', \sigma)$$

$$Op m ext{ } (tailcall \text{ } a_{target} \overline{r_{args}} \overline{sa}) \text{ } (V, \sigma) = (V', \sigma)$$

$$Op m ext{ } (tailcall \text{ } a_{target} \overline{r_{args}} \overline{sa}) \text{ } (V, \sigma) = (V', \sigma)$$

$$Op m ext{ } (tailcall \text{ } a_{target} \overline{r_{args}} \overline{sa}) \text{ } (V, \sigma) = (V', \sigma)$$

$$Op m ext{ } (tailcall \text{ } a_{target} \overline{r_{args}} \overline{sa}) \text{ } (V, \sigma) = (V', \sigma)$$

$$Op m ext{ } (tailcall \text{ } a_{target} \overline{r_{args}} \overline{sa}) \text{ } (V, \sigma) = (V', \sigma)$$

Fig. 8: Operations supporting tail calls and argument passing on stack.

them. In DI they are tagged as part of the entry sequence, while in LTC they are tagged when a value is placed in them.

## VII. VALIDATION THROUGH RANDOM TESTING

There are several ways to evaluate whether an enforcement mechanism enforces the above stack safety properties. Ideally such validation would be done through formal proof over the semantics of the enforcement-augmented machine. However, while there are no fundamental barriers to producing such a proof, it would be considerable work to carry out for a full ISA like RISC-V and complex enforcement mechanisms like Roessler and DeHon's micro-policies. We therefore choose to systematically *test* their micro-policies. Our primary testing targets are the eager *Depth Isolation* and the *Lazy Per-Activation Tagging and Clearing* micro-policies.

We use a Coq specification of the RISC-V architecture [29], and extend it with a runtime monitor implementing a stack safety micro-policy. We choose Coq for our implementation to ensure that our definitions are well-formed and to leverage the power of the QuickChick testing framework [26].

## A. Test Generation

To use QuickChick, we developed random test-case generators that produce (1) an initial RISC-V machine state, including the program to be executed; (2) an initial policy state, tagging instructions and the stack regions appropriately for the micro-policy (see Section VI) (3) a map from instructions to lists of their operations in the security semantics.

To write such generators we build on the work of Hriţcu et al. [30], [31], which introduced generation by execution, a technique that produces programs that lead to longer executions—and hopefully towards more interesting behaviors as a result. We extend their technique with an additional degree of statefulness: when complex calling conventions need to be observed to avoid early failstops, extra care must be taken to ensure that calls are well behaved. For example, immediately after a call we need to initialize any stack-allocated variables with an increased probability. However, at the same time, we

need to allow for the possibility of *not* performing such an initialization to allow for potential attack vectors to manifest.

Moreover, we need to further extend typical hyperproperty testing schemes to handle the nested nature of confidentiality: rather than just generating two variant initial machines and letting them execute to test for noninterference, we generate a new variant *every time a call is made* and check confidentiality for the subtrace produced from that variant state until its corresponding return. As a result, a "single" confidentiality test compactly checks multiple nested calls.

## B. Mutation Testing

To ensure the effectiveness of testing against our formal properties, we use *mutation testing* [32] to inject errors (mutations) in a program that should cause the property of interest (here, stack safety) to fail, and ensure that the testing framework can find them. The bugs we use for our evaluation are either artificially generated by us (deliberately weakening the micro-policy in ways that we expect should break its guarantees), or actual bugs that we discovered through testing our implementation. We elaborate on some such bugs below.

For example, when loading from a stack location, Depth Isolation needs to enforce that the tag on the location being read is STACK n for some number n and that the tag of the current PC is PC n for the same depth n. We can relax that restriction by omitting the check (row  $LOAD\_NO\_CHECK\_DI$ ). Similarly, when storing to a stack location, the correct micropolicy needs to ensure that the tag on the memory location is either UNUSED or has again the same depth as the current PC tag. Relaxing that constraint causes violations to the integrity property (row  $STORE\_NO\_CHECK$ ).

## C. Results

The mean-time-to-failure (MTTF) and average number of tests for various bugs can be found in Table III, along with the average number of tests it took to find the failure. Experiments were run in a desktop machine equipped with i7-4790K CPU @ 4.0GHz with 32GB RAM.

| Bug              | Property Violated | MTTF (s) | Tests  |
|------------------|-------------------|----------|--------|
| LOAD_NO_CHECK_DI | Confidentiality   | 24.2     | 13.3   |
| STORE_NO_CHECK   | Integrity         | 26.9     | 26     |
| HEADER_NO_INIT   | Integrity         | 69.5     | 76.3   |
| PER_DEPTH_TAG    | Integrity         | 189.7    | 8342.5 |
| LOAD_NO_CHECK_LT | Integrity         | 23.5     | 12.0   |
| LOAD_NO_CHECK_LT | Confidentiality   | 19.2     | 695.5  |
| STORE_NO_UPDATE  | Integrity         | 70       | 80.6   |
| STORE_NO_UPDATE  | Confidentiality   | 4.9      | 88.5   |

TABLE III: MTTF for finding bugs in erroneous policy enforcement mechanisms

For *LTC*, the original micro-policy, implemented as *PER\_DEPTH\_TAG*, fails in testing, in cases where data is leaked between sequential calls. To round out our mutation testing we also check *LOAD\_NO\_CHECK\_LT*, equivalent to its counterpart in depth isolation, and a version where stores succeed but fails to propagate the PC tag, *STORE\_NO\_UPDATE*. It turns out that *PER\_DEPTH\_TAG* is a comparatively subtle bug, taking longer to catch.

Our properties allow us to identify an enforcement mechanism as not really stack safe, and to validate a possible fix.

## VIII. RELATED WORK

The centrality of the functional abstraction and its security are behind the many software and hardware mechanisms proposed for its protection [1], [9]–[21]. Many enforcement techniques focus purely on WBCF; others combine this with some degree of memory protection, chiefly focusing on integrity. Roessler and DeHon's *Depth Isolation* and *Lazy Tagging and Clearing* [1] both offer protections corresponding to WBCF, CLRI, and CLRC, though they do not give a formal description of this. They are generally not concerned with protecting callees.

To our knowledge, the only other line of work that aims to rigorously characterize the security of the stack is the StkTokens-Cerise family of CHERI-enforced secure calling conventions [18]-[20]. These works define stack safety as overlay semantics and related stack safety properties, phrased in terms of logical relations instead of trace properties. Originally, they describe "local state encapsulation" [19] in terms of integrity only (but it has confidentiality, equivalent to CLRI and CLRC). Their latest paper [20] was inspired by the properties presented in this paper to extend their formalism to include confidentiality. When checking if our properties applied to their old calling convention, they noted that it did not enforce CLEC, and made sure that their new version would in addition to building it into their formalism [33]. This demonstrates the benefit of our choice to explicitly state properties in security terms: specifying security is hard, and when the spec takes the form of a "correct by construction" machine, it is easy to neglect a non-obvious security requirement.

In terms of direct feature comparison with Georges et al. (being the most recent work in the line), with the addition of confidentiality to their formalism, we are roughly at parity in terms of the expressiveness of our properties. We have additionally proposed callee-integrity, but it is probably the

least practical of our properties. We extend our model to tailcalls, which they do not, and to the passing of pointers to stack objects. They discuss stack objects and the interaction between stack and heap, but their calling convention does not guarantee safety in the presence of pointer passing without additional checks. We test a limited degree of pointer passing, which does not guarantee memory safety for the passed pointer but which does not undermine the security of its frame, and we offer an untested formalism for memory-safe passing of pointers. On the other hand, their properties are validated by proof, while ours are only tested.

## IX. FUTURE WORK

We plan to test our properties against multiple enforcement mechanisms. The top priority is capability machines, namely CHERI [34], a modern architecture designed to provide efficient fine-grained memory protection and compartmentalization. We want to test the most recent work by Georges et al. [20], which is designed to enforce analogues of all of our properties except for CLEI.

It would also be interesting to test a software approach. Under a bounds checking discipline [10], all the pointers in a program are extended with some disjoint metadata used to gate memory accesses. These approaches enforce a form of *memory safety*, and we would therefore expect them to enforce CLRI and CLRC. They aim to enforce WBCF by cutting off attacks that involve memory-safety violations, but that may not be sufficient. Bounds checking approaches require substantial compiler cooperation. This is not a problem for our properties in general, but it is not very compatible with generation-by-execution of low-level code. A better choice might be to generate high-level code using a tool like CSmith [35], or prove the properties instead.

Several popular enforcement mechanisms are not designed to provide absolute guarantees of security. For example, stack canaries [9] and shadow stacks [14], [15] are chiefly hardening techniques: they increase the difficulty of some control-flow attacks on the stack, but cannot provide absolute guarantees on WBCF under a normal attacker model. Interestingly, these are lazy enforcement mechanisms, in that the attack may occur and be detected some time later, as long as it is detected before it can become dangerous. That would make our observation-based formalism a good fit for defining their security, if we could find a formal characterization of what they do acheive (perhaps in terms of a base machine with restricted addressing power).

We have preliminary work on extending our model to handle C++-style exceptions, which, like tailcalls, obey only a weakened version of WBCF. We are also exploring extensions to concurrency, starting with a model of statically allocated coroutines. These extensions will also require non-trivial testing effort. We also plan to test the model in Appendix A for arbitrary memory-safe pointer sharing.

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## **APPENDIX**

## A. Provenance, Capabilities, and Protecting Objects

What if we want to express a finer-grained notion of safety, in which stack objects are protected unless the function that owns them intentionally passes a pointer to them? This can be thought of as a *capability*-based notion of security. Capabilities are unforgeable tokens that grant access to a region of memory, typically corresponding to valid pointers to that region. So, in order to express such a property, we need our machine to carry some notion of *pointer provenance*—a distinction between a pointer that is intended to point to a given object, and non-pointer integers as well as pointers to other objects. This constitutes a substantial addition to the security context.

One such provenance model is Memarian et al.'s PVI [36], in which pointers are annotated with the identity of the object they first pointed to. This annotation is propagated when the pointer is copied and when operations are performed on it—even integer-only operations.

We can model this as a trio of additional security-relevant operations: one which declares a register to contain a valid pointer, one which transmits the provenance of a pointer from one element to another, and one which clears the provenance (for instance, when a pointer is modified in place in a way that makes it invalid.)

In addition to the normal call stack, our security context will carry a map  $\rho$  from elements to memory regions, represented as a base and a bound  $c=(V,\sigma,\rho)$ . Existing operations are extended to keep the value of  $\rho$  the same, and the new operations work as follows:

$$\psi = \mathbf{promote} \ r_{dst} \ (r_{base}, off, sz)$$

$$\rho' = \rho[r_{dst} \mapsto range \ r_{base} \ off \ sz] \quad \text{PROMOTE}$$

$$Op \ m \ \psi \ (V, \sigma, \rho) = (V, \sigma, \rho')$$

$$\psi = \mathbf{propagate} \ k_{src} \ k_{dst}$$

$$\rho' = \rho[k_{dst} \mapsto \rho[k_{src}]] \quad \text{PROPAGATE}$$

$$Op \ m \ \psi \ (V, \sigma, \rho) = (V, \sigma, \rho')$$

$$\psi = \mathbf{clear} \ k$$

$$Op \ m \ \psi \ (V, \sigma, \rho) = (V, \sigma, \rho[k \mapsto \emptyset]) \quad \text{CLEAR}$$

We now have a notion of provenance, and must integrate it into the definition of stack safety. We essentially generalize the above notion of passing: we will consider a caller to have intentionally passed an object if that object is reachable by a capability that has been passed to the callee. This includes capabilities passed indirectly, by being stored in an object that is in turn passed. Formally, we call this set *capped*, and define it recursively:

$$\begin{array}{l} capped \ K \ \rho \triangleq \bigcup_{k \in K} \{k\} \cup capped \ K' \ \rho \ \text{where} \\ K' = \{k' | \rho[k] = (base, bound) \land base \leq k' < bound\} \end{array}$$

We then tweak the call operation to seal only objects that are in *capped*, or the previously defined *passed*.

$$\psi = \mathbf{call} \ a_{target} \ \overline{r_{args}} \ \overline{sa}$$

$$V' = V \llbracket r \mapsto free | r \in CLR \rrbracket \llbracket r \mapsto public | r \in \overline{r_{args}} \rrbracket$$

$$K = \{ a | V' \ a = active \land a \not\in (passed \ \overline{sa} \ m) \cup (capped \ \overline{r_{args}} \ \rho) \}$$

$$V'' = V' \llbracket K \mapsto sealed \rrbracket$$

$$Op \ m \ \psi \ (V, \sigma, \rho) = (V'', V :: \sigma, \rho)$$

In the resulting property, once an object is sealed (because its capability has not been passed to a callee), subsequent nested calls can never unseal it. On the other hand, an object that is passed via a pointer may be passed on indefinitely.