Cosmological avatars of the landscape. I. Bracketing the supersymmetry breaking scale

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We investigate the effects of quantum entanglement between our horizon patch and others due to the tracing out of long wavelength modes in the wave function of the Universe as defined on a particular model of the landscape. In this, the first of two papers devoted to this topic, we find that the SUSY breaking scale is bounded both above *and* below: $10^{-10}M_P \le M_{SUSY} \le 10^{-8}M_P$ for grand unified theory (GUT) scale inflation. Bounds on the SUSY breaking parameter depend on the scale of inflation. If inflation occurred at GUT energies, the lower bound on *b* is at least 5 orders of magnitude larger than the expected value of this parameter, soon to be tested by LHC.

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I. INTRODUCTION

Is the string landscape predictive? This is one of the main points of contention in theoretical physics today. One camp [1] claims that the best we will be able to do is to ask anthropic questions and then hope that these are also the questions we want to have answered.

On the other hand, there are those, ourselves included, who believe that it is premature to give up the hope that some dynamical principle might be able to select out at least an interesting subclass of vacua out of the landscape. In particular, asking whether we can find the vacua that allow for consistent inflationary dynamics would be of great interest, especially in light of the WMAP3 data [2].

In previous work [3,4], we have advocated the use of the quantum dynamics of gravity to "thin out" the herd of vacua, as it were. To tie this into the landscape, we view the landscape as the natural configuration space for the wave function of the Universe. We showed that the inclusion of the backreaction of superhorizon matter modes onto the gravitational degrees of freedom generates a Wheeler-DeWitt master equation from which we could infer that the phase space of stable inflationary patches is dynamically reduced due to a Jeans instability. Furthermore, this analysis showed that treating the space of inflationary initial conditions as if it consisted of regions with field and gravitational configurations that were in thermodynamic equilibrium was, in fact, inconsistent [4] and that perturbative approaches cannot single out our vacua since a perturbed action results only on a rescaling of the vacuum energy Λ or some dark radiation contribution [5,6]. Thus,

the use of the nonperturbative dynamics of the gravitational and matter degrees of freedom, with the resulting mixed initial state due to nonlocal entanglement, seems a promising avenue as far as the vacuum selection problem is concerned.

While the analysis in Refs. [3,4] shows how the initial conditions for inflation in survivor universes are (super)-selected through gravitational quantum dynamics, one can ask whether there are more observationally distinctive signatures that might arise from this treatment. In fact, we find such signatures and we will elaborate on them in this series of papers.

In this, the first paper of the series, we show how traces of the combination of gravitational dynamics and quantum entanglement contained in the initial wave packet describing our universe, together with the requirement that the temperature anisotropies in the cosmic microwave background (CMB) were seeded by quantum fluctuations during an inflationary phase, allows us to place both upper and *lower* bounds on the scale of SUSY breaking. What makes this result particularly exciting is that our lower bound is 5 orders of magnitude larger than the TeV scale usually assumed; this allows for the possibility that our scenario could be falsified once the LHC starts taking data.

The companion article in this series deals with more detailed imprints that these gravitational effects leave on both the CMB as well as on large scale structure (LSS). In Sec. III we exhibit the details of the calculation of backreaction of long wavelength modes at the onset of inflation and derive the corresponding energy shift of the wave packet in its phase space trajectory. The energy shift results in a modification to the Friedmann equation and the generation of non-Gaussian inhomogeneities induced by the nonlocal entanglement left over from primordial times. The physical significance of these results is that our wave

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packet preserves unitarity, namely, the universe remains in a mixed state even at present, although the scale of the nonlocal entanglement is much larger than the present Hubble radius r_H . Observationally, the quantum entanglement between our patch and others and with the superhorizon wavelength modes leaves unique signatures on CMB temperature anisotropy power spectrum as well as on LSS.

Matching our results to the tight constraints coming from the requirement of flatness of the inflaton potential and the amount of inhomogeneities allowed by CMB data will allow us to bracket the scale of SUSY breaking for our universe.

II. A MODEL OF THE STRINGY LANDSCAPE

The string landscape [1] is a vast and complicated space of possible string vacua. A full analysis of the structure of the landscape is currently beyond our reach. It is expected that there are *at least* 10⁵⁰⁰ possible vacua present in the landscape. This suggests a statistical approach to the problem and such a program was begun by Douglas and Denef [7]. Their observation was that the matrix of fermion masses in SUSY theories is a complex symmetric matrix and so can be modeled by the so-called CI distribution of Altland and Zirnbauer [8], which leads to a distribution of mass eigenvalues that exhibits level repulsion and hence shows that degenerate eigenvalues are not the generic situation.

Starting from this observation, one of us (L. M-H [9,10]) constructed a model for the landscape that exhibits it as a lattice of vacua with a distribution of vacuum energies. A wave function can then be defined that uses this lattice as its configuration space. We found that some statistical aspects of the landscape can be understood via random matrix theory [9,10] and that the probability distribution on the landscape phase space with gravity included belongs to the type C universality class [3] rather than type CI of [8].

There are good reasons to believe that SUSY is broken in our world. In accord with the distribution of landscape vacua found in Refs. [3,7], we take this sector of the landscape to be modeled by a disordered lattice, where each of the N sites of this lattice is labeled by a mean value ϕ_i of the moduli fields, which serves as a collective coordinate for the landscape. In this context, disordering means that the energy density of the vacua has a stochastic distribution which we take to be drawn from the interval [-W, +W], where $W \sim M_{\text{Planck}}^4$. The disordering of the lattice is enforced by the Gaussian distribution we use to draw energy densities. The width Γ of this Gaussian is the disordering strength; we expect that this is related to the amount by which SUSY is broken and we take $M_{SUSY}^8 \leq$ $\Gamma \leq M_{\text{Planck}}^8$, where M_{SUSY} is the SUSY breaking scale. We also expect each lattice site to have some structure, corresponding to internal degrees of freedom that capture the distribution of the universality class for the landscape [3,7]; we take this to behave as closely spaced resonances which we label as $\{\phi_i^n\}$, where *n* tags the internal structure.

Quantum mechanically we expect tunneling between the vacua to take place. Given this and the disordered nature of the lattice, the interesting aspect of this lattice is that it allows Anderson localization [9–11] to take place around each one of the vacua (lattice sites). For large enough values of the disorder strength Γ , the majority of the levels are localized so that a semiclassical treatment of their classical trajectories in configuration space is justified.

If we consider a wave function that has as its configuration space the coordinates of the lattice of non-SUSY vacua, we can use the localization around each site to treat the ensemble of sites as the space of possible initial conditions for the Universe.

To tie this in to cosmology, we turn gravity on and first consider the minisuperspace determined by the coordinates on the landscape lattice together with the Friedmann-Robertson-Walker (FRW) scale factor *a* so that the wave function of the Universe Ψ is a function of *a*, $\{\phi_i^n\}$. The internal degrees of freedom can be used to construct wave packets in this minisuperspace following the approach of Ref. [12]. We take these Anderson localized wave packets to be Gaussian around each of these vacua with a width *b* which we expect to be of the order of the supersymmetry breaking scale M_{SUSY} in order to account for the splitting of the zero energy levels. The details of this construction can be found in Refs. [3,4].

The minisuperspace described above is not sufficient for our purposes. It has to be expanded to include fluctuations about the various mean values involved. Thus, we allow for metric perturbations about the background FRW geometry as well as perturbations about the scalar degrees of freedom, one of which will be the inflaton; these will be labeled as $\{d_n\}, \{f_n\}$ respectively. We follow Refs. [13,14].

We now have the setup needed to understand the new effects appearing from the landscape. In the next section, we explicitly trace out the long wavelength modes out of the wave function to construct a reduced density matrix $\rho_{red}(a, \phi; a', \phi')$ from which we compute the corrections to the energy density that appears in the modification to the Friedmann equation as well as other important quantities.

III. CALCULATION OF ENTANGLEMENT AND BACKREACTION EFFECTS

Our calculation of the entanglement and backreaction contribution to our wave function is carried out in the SUSY breaking sector of the landscape, where localization can occur. Each vacuum in this sector thus carries two parameters: the global (Planck) string scale M_P of the theory and the local SUSY breaking scale, M_{SUSY} , of the individual vacua under consideration. Both of these scales will appear in the width of the wave packets localized around each of the vacua in this sector of the landscape and will also show up in the width of the Gaussian suppression for the diagonal and off-diagonal terms of the reduced density matrix. These describe the entanglement of our inflationary patch with others [3,4] and M_P , M_{SUSY} will determine the interference and decoherence lengths of the wave function for our patch.

The calculation that follows uses the techniques described in Ref. [15] as well as Ref. [16], so we summarize below the main results from these works that we will use in the sequel. We are using the higher multipoles both of the scalar field driving inflation as well as (at least in principle) those of the metric to "measure" the wave function and induce decoherence between different states in a superposition. We treat these multipoles as perturbations on the zeroth order homogenous mode, and only keep their effects to quadratic order in the action. In this we follow Refs. [13,14].

An intrinsic time t can be defined for WKB wave functions [13,14,17] using

$$\frac{\partial}{\partial t} \equiv (\nabla S) \cdot \nabla_t$$

where *S*, defined via $\psi_0 \sim C \exp iS$, is the classical action and ∇ is the gradient vector defined on the minisuperspace variables [13,14].

The reduced density matrix of the system, obtained after tracing out the higher modes, in this approximation, can be written in terms of the density matrix in the absence of fluctuations $\rho_0(a, \phi; a', \phi')$ as

$$\rho(a, \phi; a', \phi') = \rho_0(a, \phi; a', \phi')$$

$$\times \prod_{n>0}^N \int df_n \psi_n^*((a', \phi', f_n)\psi_n(a, \phi, f_n),$$
(3.1)

where the wave functions ψ_n are solutions of $\hat{H}_n \psi_n = i \dot{\psi}_n$, where \hat{H}_n is given by

$$\hat{H}_n = -\frac{\partial^2}{\partial f_n^2} + e^{6\alpha} (m^2 + e^{-2\alpha} (n^2 - 1)) f_n^2, \qquad (3.2)$$

where $a = \exp \alpha$, *n* denotes the comoving momentum label in a closed Universe, and the -1 in the $n^2 - 1$ term comes from the curvature term. Note that we have not explicitly included here the effects of the tensor metric perturbations on the reduced density matrix, since the procedure is identical to that of tracing out the scalar modes. Besides, the former are simpler in some sense since they are gauge invariant, while the dominant contribution to the spectra and energy corrections comes from the scalar sector (see Ref. [13] for a more thorough discussion of this point).

If we make a Gaussian ansatz for ψ_n , i.e.

$$\psi_n = N(t) \exp(-\frac{1}{2}\Omega_n(t)f_n^2), \qquad (3.3)$$

we can insert this into the Schrödinger equation for ψ_n to arrive at equations for the normalization factor N(t) and the

frequency $\Omega_n(t)$. Taking the results from [15] we have for the survivor universes [3], i.e. in the limit that $m^2/H^2 \ll$ 9/4, where *m* is the mass of the inflaton field ϕ and *H* the Hubble parameter for this solution:

$$\Omega_n \simeq \frac{n^2 a^2 (n + iaH)}{n^2 + a^2 H^2} + i \frac{m^2 a^3}{3H} \equiv \Omega_{n,R} + i \Omega_{n,I}.$$
 (3.4)

The reduced density matrix can be written as [15]

$$\rho(\phi + \Delta, \phi) = \rho_0 \exp I \tag{3.5}$$

with $\Delta = (\phi - \phi')$ and

$$I = i \left(\operatorname{Tr} \frac{\Omega_I}{\Omega_R} \right) \Delta - \left(\operatorname{Tr} \frac{|\Omega'|^2}{\Omega_R} \right) \frac{\Delta^2}{2}.$$
 (3.6)

The real part of *I* corresponds to the cross term of the reduced density matrix which determines the degree of decoherence of our patch, that is, to what extent the phase relations of the entanglement with other patches ϕ' can be observed. The imaginary part corresponds to the diagonal term of ρ and describes the degree of coherence for the packet in ϕ that is the scale at which interference effects become significant.

From this result we can compute the corrections to the energy, as well as the effects of decoherence between different states present in the density matrix. The decoherence factor is given by [15]

$$D = \frac{1}{2} \sum_{n>0} n^2 \frac{\Omega_{n,I}^2}{\Omega_{n,R}^2}.$$
 (3.7)

This shows up in the reduced density matrix as $\exp(-Da^4(\phi - \phi')^2)$.

The entanglement in the initial mixed state induces a shift in the energy of the wave packet in its trajectory in phase space¹ given by the total Hamiltonian which contains the backreaction corrections in our Master equation [3], $\mathcal{H} = \mathcal{H}_0 + \sum_n \mathcal{H}_n$. Therefore, this correction term to the energy density of the universe, which originates from the nonlocal entanglement of our wave packet with other patches and the backreaction of the higher multipoles, modifies the right-hand side of the Friedmann equation as follows $\Delta E_{\phi} = \mathcal{H}_{n,\phi}V$, which in a first order WKB approximation becomes [15]:

$$-\Delta E_{\phi} = \frac{1}{V} \operatorname{Tr}(\Omega_R) + \frac{aH}{V} \operatorname{Tr}\left(\frac{\Omega_I'}{2\Omega_R}\right). \quad (3.8)$$

This energy shift induces a nonlocal correction to the Friedmann equation of our universe, given by $V_{\text{eff}} = V(\phi) + \Delta E_{\phi}$. We have to unwrap some notation in the above equation. The volume of 3-space is denoted by V (it is just a^3). The traces are sums over the modes, $\Omega_{R,I} =$

¹This effect is well known in particle physics: when a charge interacts with a field there is an energy shift in its trajectory.

 $\Omega_{n,R,I}$ and the prime denotes a derivative with respect to the scale factor *a*.

The interference or coherence length can also be calculated and it is given by $l_{coh}^2 = A_1$, where

$$HA_1 = \operatorname{Tr}\left(\frac{\Omega_I}{\Omega_R}\right). \tag{3.9}$$

Below we approximate the sums over mode numbers by integrals when integrating out the long superhorizon wavelength modes and in computing the relevant traces of Eqs. (3.6), (3.7), and (3.8). The only question is what to take as the UV and IR cutoffs on these integrals. Since we are tracing out superhorizon modes, the *upper* limit on n should be aH.

The lower limit is a somewhat more subtle question to deal with since it is related to the well-known IR divergence problem in quantum gravity and the interference length, estimated below, depends crucially on it. Let us recall that our system (the relevant degrees of freedom) corresponds to wavelengths shorter than horizon radius and the environment (irrelevant degrees of freedom) to the longer wavelength multipoles. Now, we argue here that a physically well motivated choice for the IR cutoff is given by the SUSY breaking scale b which determines the vacuum energy. The main point is that we are constructing wave packets localized on a landscape vacuum with vacuum energy given by b, and width b^{-1} determined by the uncertainty principle. If we probe this wave packet on scales much shorter than b^{-1} , this would destroy its quantum coherence and localization by exciting the system in such a manner that the wave packet would spread over many vacua and disintegrate into its many components. On larger scales, the wave packet can be approximated by a classical particle so that a classical trajectory in phase space and decoherence for our universe are assured. But if the characteristic scale of disturbance is shorter than the characteristic size of the system, then the interference effects among its many components become significant, a process which destroys decoherence. Hence, translation to distances much larger than b^{-1} in the landscape would take us away from the vacuum in which our wave packet is centered and onto other vacua solution of the landscape. Since we are interested in the classical solution corresponding to our vacuum, within our WKB approximation (nearest neighbor interaction) then we are limited between two scales H and b, as it becomes clear below by the expression for the interference and decoherence lengths A_1 , D. For this reason we take k = ab as the IR cutoff for the scale of entanglement of our inflaton patch. We should note that there are other possible regularization methods [18], but we use this one as it reflects the nature of our model of the landscape. To conclude there are two scales in the problem, a global one, the Planck scale, which applies to all vacua, and a local one which is the SUSY breaking scale b. Both of these should appear in the description of the effective physics described by the reduced density matrix. Doing this gives us

$$HA_1 = ia \int_{ab}^{aH} dn \frac{m^2(n^2 + a^2H^2) + 3n^2H^2}{3n^3H}.$$
 (3.10)

The integral yields

$$HA_{1} = -ia\left\{\left(\frac{m^{2}}{3H} + H\right)\ln\frac{b}{H} - \frac{m^{2}H}{6}\left(\frac{1}{b^{2}} - \frac{1}{H^{2}}\right)\right]\right\}.$$
(3.11)

We also find

$$D \sim a^{2} \int_{ab}^{aH} dnn \left(\frac{m^{2}(n^{2} + a^{2}H^{2}) + 3n^{2}H^{2}}{3n^{3}H} \right)^{2}$$

= $-a^{2}H^{2} \left[\left(1 + \frac{m^{2}}{3H^{2}} \right)^{2} \ln \frac{b}{H} - \frac{a^{4}}{36} \left(\frac{1}{b^{4}} - \frac{1}{H^{4}} \right) - \frac{1}{3} \left(1 + \frac{m^{2}}{3H^{2}} \right) \left(\frac{1}{b^{2}} - \frac{1}{H^{2}} \right) \right].$ (3.12)

Just to reemphasize the point, *D* measures the width of the Gaussian suppression of the off-diagonal terms in the density matrix. This in turn describes the suppression of interference between different branches (degrees of freedom) and thus the rate of separation of the degrees of freedom ϕ , a(t) in our wave packet from the others ϕ' , a'(t). In short, the emergence of our classical world from a fundamentally quantum world.

Finally, we compute ΔE_{ϕ} . This requires us to compute two traces: $A_3 \equiv \text{Tr}(\Omega_R)$ and $A_4 \equiv \text{Tr}(\Omega'_I/2\Omega_R)$. We do these in turn:

$$A_{3} = \int_{ab}^{aH} dnn \frac{n^{2}a^{2}}{n^{2} + a^{2}H^{2}}$$
$$= -\frac{a^{4}H^{2}}{2} \left[\left(\frac{b^{2}}{H^{2}} - 1 \right) - \ln \frac{b}{H} \right].$$
(3.13)

A similar calculation yields

$$A_4 = \frac{3H}{2}A_1 + \frac{aH^2}{2}\ln\left[\frac{2b^2}{b^2 + H^2}\right].$$
 (3.14)

IV. LANDSCAPE CONSTRAINTS ON THE SUSY BREAKING SCALE

The fact that backreaction effects can help solve the problem of inflationary initial conditions is fascinating in and of itself. However, this will be academic unless we can argue that there are falsifiable consequences arising from these effects. In this section, we show that our knowledge of the CMB power spectrum can bound some of the parameters which are a part of our description of the landscape. One such parameter is b. As described above, it describes the width of the wave packets constructed around each vacuum in the landscape using the internal excitations around each vacuum and is related to the SUSY

breaking scale. What we will find is that b can be related to the value of the quadrupole of CMB [19]. On the other hand, it is also related to the amount of quantum interference, as determined by the reduced density matrix, between our horizon patch and others.

For definiteness we will follow Ref. [20] and use the following inflaton potential with its slope chosen such as to satisfy the slow-roll conditions,

$$V(\phi) = V_0 \exp\left(-\lambda \frac{\phi}{M_{\rm P}}\right). \tag{4.1}$$

This inflationary potential can arise in SUGRA models, which is the reason we chose this particular example for illustration. However, our results will be valid for generic slow-roll potentials that allow for an inflationary phase.

When the backreaction effects are included, due to the energy shift in the WKB trajectory of our wave packet in phase space the relevant Friedmann equation of Eq. (3.8) becomes modified as follows, when replacing Ω_I , Ω_R computed in Eqs. (3.9), (3.10), (3.11), (3.12), (3.13), and (3.14):

$$H^{2} = \frac{1}{3M_{\rm P}^{2}} \left[V(\phi) + \frac{1}{2} \left(\frac{V(\phi)}{3M_{\rm P}^{2}} \right)^{2} F(b, V) \right] \equiv \frac{V_{\rm eff}}{3M_{\rm P}^{2}}, \quad (4.2)$$

where

$$F(b, V) = \frac{3}{2} \left(2 + \frac{m^2 M_{\rm P}^2}{V} \right) \log \left(\frac{b^2 M_{\rm P}^2}{V} \right) -\frac{1}{2} \left(1 + \frac{m^2}{b^2} \right) \exp \left(-3 \frac{b^2 M_{\rm P}^2}{V} \right).$$
(4.3)

Note that here, we have approximated the dependence on the Hubble parameter *H* contained in Eq. (3.8) by the inflaton potential $H^2 \approx V(\phi)$. Because of the slow-roll conditions *H* is nearly a constant during inflation, however the slight change in the potential during the slow roll is taken into account in the next section, Eq. (4.8).

We have taken $8\pi G_N = M_P^{-2}$, $b = M_{SUSY}$ is the SUSY breaking scale and $m^2 = V''(\phi)$. There are two types of corrections appearing in our modification to the Friedmann equation. The term involving the exponential arises from the nonlocal entanglement of our horizon patch with others. While the calculation in Sec. III only obtains the first two terms of an expansion of the exponential in terms of b^2/H^2 , we exponentiated it, anticipating that it corresponds to a tunneling type of correction. This is based on the fact that for our ansatz of the wave function we can formally write the energy corrections to be of the familiar form coming from particle creation: $\mathcal{H}_{\phi} \approx \text{Tr}(\omega +$ $2\omega|\beta|^2$ with $\Omega \approx \omega + i\dot{\omega}/2\omega$ and β^2 the exponential term here, which formally corresponds to particle creation [15]. Since b^2/H^2 will be small as shown in [4], doing this will not cause any inaccuracies.

The term involving the logarithm incorporates the effects of superhorizon massive fluctuations. Note that both of these corrections involve a nontrivial time dependent function of the coupling between the effects due to the inflaton potential $V(\phi)$ and superhorizon fluctuations represented by *b*. This will give rise to subtle effects on large scale structure, as we discuss in the second paper in this series [21].

The primordial power spectrum is given by

$$P_{\mathcal{R}} = \frac{1}{75\pi^2 M_{\rm P}^2} \frac{V_{\rm eff}^3}{V_{\rm eff}^{\prime 2}}.$$
 (4.4)

For the potential given by Eq. (4.1), we have

$$P_{\mathcal{R}}^{0} = \frac{1}{75\pi^{2}M_{\rm P}^{2}} \frac{V_{0}}{\lambda^{2}M_{\rm P}^{4}}.$$
(4.5)

The scalar spectral index is given by $n_s - 1 = -\lambda^2$. Modifications in the Friedmann equation result in a running of the spectral index $n_s = n_s^0 + \delta n_s$, as we describe below.

In our case, i.e., with the effective potential V_{eff} , the situation becomes more complicated. Now the solution for the inflaton field becomes

$$\phi = \lambda M_{\rm pl} \bigg[1 + \frac{1}{2} \frac{1}{3M_{\rm pl}^2} \bigg(\frac{V_0}{3M_{\rm pl}^2} \bigg) \bigg\{ 3 \bigg(2 + \frac{m^2 M_{\rm pl}^2}{V_0} \bigg) \\ \times \log \bigg(b \sqrt{\frac{3M_{\rm pl}}{V_0}} \bigg) - \frac{1}{2} \bigg(1 + \frac{m^2}{b^2} \bigg) e^{-3M_{\rm pl}^2 b^2 / V_0} \bigg\} \bigg]^{-1} \\ \times \log \bigg(\frac{k}{k_{\rm ref}} \bigg), \tag{4.6}$$

where $k_{ref} \simeq (4000 \text{ Mpc})^{-1}$.

Define $3M_p^2/F(b, V) \equiv \sigma(b, \phi)$ and denote the energy correction $V^2/\sigma = f(b, V)$. The modified Friedmann equation can then be written as

$$3M_p^2 H^2 = V + f(b, V). (4.7)$$

Notice that f(b, V) is a negative function, so that we are restricted to the regime for which the right-hand side of this equation is positive.

We are now ready to derive the cosmological bounds for the local SUSY breaking scale in our patch.

A. Flatness of the inflaton potential

As is well known, for a successful stage of inflation to occur, inflationary potentials have to be "fine-tuned" such that they satisfy the flatness condition [22]

$$\Delta V / (\Delta \phi)^4 \le O(10^{-7}).$$
 (4.8)

For grand unified theory (GUT) scale inflation with $\Delta \phi \simeq \mathcal{O}(M_P)$, the exponential potential type considered here would satisfy this condition, if we choose parameters such that, for example, $V_0 \simeq 10^{-9} M_P^4$, $\lambda \simeq 0.1$.

When the primordial effects of entanglement and backreaction of superhorizon matter perturbations on the inflaton potential are taken into account, it is the effective potential $V_{\rm eff} = V + V^2/\sigma(b, V)$ that must satisfy this condition. Now note that we can approximate $\sigma(b, V) = M_P^4/(\Delta N_b - m^2/b^2)$, with $\ln(3M_P^2b^2/V) \simeq 2\ln(k_b/k) \simeq \Delta N_b$, where ΔN_b is the number of e-folds before the end of inflation at which the scale *b* leaves the horizon and we take $e^{-3M_P^2b^2/V} \simeq 1$. Using this, the flatness condition gives $\sigma > 10^{-9}M_P^4$ that places a lower bound on the SUSY breaking scale

$$b \ge 10^{-10} M_P.$$
 (4.9)

B. Constraints from CMB experiments

The second condition on the SUSY breaking scale comes from the temperature-temperature power spectrum of the CMB. Corrections disturb slow-roll inflation. Inhomogeneities on scales larger than the horizon induce gradients and shear across our horizon [19] that affect the Newtonian background potential. The contribution from these corrections to the quadropole is constrained to be [2,19]

$$(\nabla T/T)_{\text{quad}} \approx r_H^2 \nabla^2 \delta \phi = (ck_1/H_0)^2 \delta \phi$$

$$\approx 0.5 (r_H/L_1)^2 (\delta \rho/\rho)_1. \tag{4.10}$$

The subscript 1 denotes the wave number/scale where inhomogeneities arising from the entanglement σ dominate, 0 denotes present-day values, and $\delta\phi$ is the σ -induced quadrupole Newtonian potential. Notice that the quadrupole contribution from entanglement to the amplitude of anisotropies turns out to be the interference length of the wave packet obtained from the width of the diagonal terms of the density matrix, as derived in the previous section: $(A_1/aH) = (L_1/r_H)^{-2}$.

Taking into account the possibility that other fluctuations from such as curvaton [23] and modulated reheating [24] can contribute to the primordial fluctuation, we take $\delta \rho / \rho \leq 10^{-5}$ then the bound from Eq. (4.10) reads: $(L_1/H_0)^2 = (A_1/aH) > 10^5$ thus $b^2/6m^2 \leq 10^{-5}$ or

$$b \le 10^{-8} M_P. \tag{4.11}$$

We have thus derived cosmological upper and lower bounds on the SUSY breaking scale $b = M_{SUSY}$:

$$10^{-10}M_P < b < 10^{-8}M_P. \tag{4.12}$$

The cosmological bounds derived here are relevant for the GUT scale inflation. However, as it can be seen from Eqs. (4.9) and (4.11), it is straightforward to derive the lower and upper bound for the SUSY breaking scale as a function of V by our approach here for any scale of inflation, namely,

$$\frac{V}{M_p^4} < \frac{b^2}{m^2} < 10^{-5},\tag{4.13}$$

where V, $m^2 = V''$ are the inflaton potential and mass squared, respectively, at any scale. The scale of inflation is bound by the reheating temperature to be at least of order TeV. In this case the lowest possible bound on the SUSY breaking scale becomes $b > 10^{-15}M_p$, a value which might be within the reach of LHC. Hence, if *b* is observed at LHC scales, we would learn valuable information not only about SUSY and Higgs physics but also information about the inflation scale itself. For example, if the LHC disproves the above bound then we have to choose between either our model being incorrect, or that inflation did not occur at the GUT scale. For the general case, our predicted cosmological bounds on SUSY breaking scale as a function of the energy scale at which inflation occurred, are given by the contour plots of Fig. 1.

Two comments are in order. First, it is very interesting that the induced quadrupole anisotropy scale is given by the interference length of the wave packet. This provides a natural physical explanation behind the channel of the induced inhomogeneities on the LSS. It also sheds light on the reason why *b* is the IR cutoff for our patch. The underlying significance of this result is that our inflaton bubble is a classical world roughly up to the scales given by the interference length $L_1 > 10^{2.5}H_0$. Beyond this scale, we can expect to see strong quantum interference effects associated with the nonlocal entanglement in the mixed state of our universe and with the fundamentally quantum nature of the fluctuations.

Perhaps more surprising, the cosmological bounds obtained above place tight constraints on the SUSY breaking scale; they appear to force it to be about 5 orders of magnitude larger than the normal TeV expectation. These bounds soon will be complemented by ones from the LHC. If our approach is correct and that it is indeed true that cosmology requires that SUSY be broken at very high energy scales then scenarios such as split supersymmetry [25] may be the only way to make use of supersymmetry to

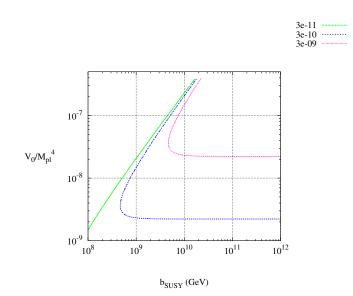


FIG. 1 (color online). Contours of P_k at k = 0.002 Mpc are shown. The value of λ is fixed as $\lambda = 0.1$ in this figure.

deal with the hierarchy problem. We checked these bounds by performing a numerical analysis which confirmed are analytical findings and the fact that the cosmological bounds found here are very stringent indeed. The results of the numerical analysis are shown in Fig. 1 where we have plotted the contours of SUSY breaking versus GUT scale inflaton potential V.

The fact that cosmology rather than particle physics can place such tight bounds on the SUSY breaking scale and require it to be so much higher than expected coupled with the fact the LHC will soon be able to test our SUSY breaking bounds directly is an exciting possibility indeed.

V. CONCLUSIONS

No scientific theory can be considered to be on firm grounds unless it makes predictions that can be tested. What can be said about the quantum gravity string landscape as a candidate for the underlying theory for the early universe? We took up these issues in a series of papers [3,4,9,10] by proposing that the landscape provides the phase space for the ensemble of initial patches known as the multiverse. We then allowed the wave function of the universe to propagate through this structure in order to find out which one of the vacua would be selected as our initial patch, i.e. to address the issue of the selection of the initial conditions from the point of view of a superselection rule emerging from the quantum dynamics of gravity [3].

Our picture of the landscape and how the wave function of the Universe is affected by quantum gravity effects such as nonlocal entanglement with other patches gives rise to observational consequences, shown here and its companion paper [21], that may in fact explain some of the strange features found in studies of the CMB as well as LSS. There is no way one could phenomenologically guess the nonlocal entanglement between b and $V(\phi)$ in the highly nontrivial corrections to the Friedmann equations (4.2)and (4.3), and its subsequent unique signatures on CMB and LSS, derived in Sec. III. Our proposal has thus not just provided a good working model for deriving the quantum gravity effects, left from the early times, in the multiverse phase space of the landscape, thereby leading the way for a dynamic rather than anthropic approach to the selection of our universe. But, as we showed here and in the next paper in this series [21], it also makes predictions that can be tested by observations. By probing into the underlying structure of the initial state and confronting the issues of the origin of our universe from the physics of quantum gravity, we have shed some light into the interrelation between the SUSY breaking scale and the size of nonlocality of quantum entanglement.

To summarize our results, we have seen that the requirement of having a sufficiently flat inflationary potential after the modifications to the Friedmann equation are taken into account, coupled with the known value of the COBE quadrupole put stringent bounds on the energy scale related to the structure of vacua in the non-SUSY part of the landscape. In our picture, this is the actual SUSY scale, and we find that it has to be significantly larger (five to 8 orders of magnitude larger) than studies of the hierarchy problem would have required. The LHC will soon be able to test this statement, once again showing the tight interconnectivity between particle physics and cosmology. It is amazing how a coherent cosmological picture of the early universe can predict such tight bounds on a particle physics parameter by relating it to imprints of the nonlocal entanglement of our universe with other horizon patches on astrophysical observables. More interestingly, we make predictions which are within the observational limits of current experiments such SDSS, WMAP, HST, as well as within those of the upcoming Planck, LISA, and lensing experiments and will soon be compared against the LHC results.

In the second paper in this series [21], we will show how the effects of entanglement and backreaction due to the superhorizon modes has very interesting, and more importantly, testable effects on the CMB and large scale structure.

Our feeling in this enterprise is that our model of the landscape contains enough of the coarse features of the true stringy landscape to be a reliable model of it. What we find rather startling is the plethora of cosmological manifestations of the physics of the landscape and how amenable to observation they are. We expect that, even if our model does not yet capture the finer details of the landscape, the strategy of using the landscape as the space of initial states for the wave function of the universe and following its evolution in the manner described both here and in our previous work promises to be a fruitful approach.

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