

Magnetosheath jets over solar cycle 24: an empirical model

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Key Points:

- Observed jet occurrence rates can be biased due to spacecraft orbits and uneven solar wind sampling
- We created a statistical model of jet occurrence using IMF cone angle, magnitude, SW speed, and density
- There is no strong solar cycle dependency in jet occurrence, but there may be a $\sim 10\text{--}20\%$ decrease around solar maximum

Abstract

Time History of Events and Macroscale Interactions during Substorms (THEMIS) spacecraft have been sampling the subsolar magnetosheath since the first dayside science phase in 2008, and we finally have observations over a solar cycle. However, we show that the solar wind coverage during these magnetosheath intervals is not always consistent with the solar wind conditions throughout the same year. This has implications for studying phenomena whose occurrence depends strongly on solar wind parameters. We demonstrate this with magnetosheath jets — flows of enhanced earthward dynamic pressure in the magnetosheath. Jets emerge from the bow shock, and some of them can go on and collide into the magnetopause. Their occurrence is highly linked to solar wind conditions, particularly the orientation of the interplanetary magnetic field (IMF), as jets are mostly observed downstream of the quasi-parallel shock. We study the yearly occurrence rates of jets recorded by THEMIS over solar cycle 24 (2008–2019) and find that they are biased due to differences in spacecraft orbits and uneven sampling of solar wind conditions during the different years. Thus, we instead use the THEMIS observations and their corresponding solar wind conditions to develop a model of how jet occurrence varies as a function of solar wind conditions. We then use OMNI data of the whole solar cycle to estimate the unbiased yearly jet occurrence rates. For comparison, we also estimate jet occurrence rates during solar cycle 23 (1996–2008). Our results suggest that there is no strong solar cycle dependency in jet formation.

1 Introduction

Magnetosheath jets are localized enhancements of dynamic pressure downstream of the Earth’s bow shock (see the review by Plaschke et al., 2018, and the references therein). These jets emerge from the shock and they propagate towards the Earth with some of them eventually impacting the magnetopause. The occurrence of jets is highly dependent on solar wind (SW) conditions, most importantly the orientation of the interplanetary magnetic field (IMF). When the angle between the Sun-Earth line and the IMF (the IMF cone angle) is small, the subsolar magnetosheath is downstream of a quasi-parallel shock, and jets occur most frequently (Archer & Horbury, 2013; Plaschke et al., 2013; Vuorinen et al., 2019). Therefore, suggested jet formation mechanisms are mostly related to the quasi-parallel shock and the foreshock region upstream of it: foreshock structures such as short large-amplitude magnetic structures (SLAMS; Schwartz, 1991) entering the magnetosheath (Karlsson et al., 2015; Palmroth et al., 2018; Suni et al., 2021), solar wind travelling through ripples on the bow shock (Hietala et al., 2009; Hietala & Plaschke, 2013), and solar wind being trapped into downstream during the shock reformation process (Raptis et al., 2022).

The growing number of Time History of Events and Macroscale Interactions during Substorms (THEMIS) spacecraft (Angelopoulos, 2008) observations in the subsolar magnetosheath have made possible extensive statistical studies, which have advanced our understanding of solar wind conditions affecting jet occurrence. Vuorinen et al. (2019) found that jet occurrence is 9 times higher downstream of the quasi-parallel shock than downstream of the quasi-perpendicular shock. LaMoury et al. (2021) studied separately jets observed close to the bow shock and those close to the magnetopause to disentangle the solar wind influence on jet formation and propagation to the magnetopause. They found that, in addition to the IMF cone angle, jet formation seems to be increased during low IMF magnitude B , low SW density n , high plasma β , and high Alfvén Mach number M_A . Koller et al. (2022) studied jets during large-scale solar wind structures, and found an increase in jet occurrence during stream-interaction regions/co-rotating interaction regions (SIRs/CIRs) and high-speed streams (HSSs), but a decrease during magnetic ejecta and sheath regions of coronal mass ejections (CMEs). Koller et al. (2023) continued this investigation and found that high IMF cone angle and high Alfvén Mach conditions are unfavorable for jet occurrence, which makes jet occurrence rates during

67 CMEs lower. Similarly, they found that conditions typical for HSSs (low IMF cone angle,
 68 low density, low IMF strength) are very favorable for jet generation. As the frequency
 69 of these structures and the characteristics of the solar wind vary across a solar cycle, a
 70 natural question arises: how does the formation of magnetosheath jets vary during the
 71 solar cycle? We now have THEMIS measurements from the subsolar magnetosheath from
 72 the years 2008–2020 that span over the solar cycle 24. In this paper we aim to answer
 73 this question by studying the yearly jet occurrence rates close to the bow shock.

74 Comparing yearly jet observation rates can be challenging. Jets are much more frequently
 75 observed close to the bow shock, so the number of observed jets varies depending
 76 on the spacecraft’s location in the magnetosheath. The apogees of THEMIS spacecraft
 77 change throughout the years. We can control for this bias by focusing only on jet
 78 observations close to the bow shock. However, when the spacecraft apogees are low, the
 79 spacecraft are close to the bow shock only during such solar wind conditions when the
 80 shock has moved substantially earthward. This leads to a bias in solar wind condition
 81 coverage and consequently in the jet occurrence rates. To obtain unbiased jet occurrence
 82 rates for each year, we build a statistical model of jet occurrence as a function of solar
 83 wind conditions using the THEMIS measurements from 2008–2020 and their corresponding
 84 OMNI measurements. To reconstruct unbiased yearly jet occurrence rates, we then
 85 input all OMNI solar wind observations throughout the solar cycle into the model. This
 86 reconstruction shows that there is no strong solar cycle variation in jet occurrence, in
 87 contrast to the biased THEMIS observations which show a large decrease in jet occurrence
 88 during the solar maximum. More generally, our results highlight the need for careful
 89 normalization when analyzing statistical data sets of phenomena that are dependent
 90 on location in the magnetosheath and on solar wind conditions.

91 This paper is organized as follows. First, we introduce the THEMIS data set used
 92 in this study. Second, we show how the solar wind conditions vary during solar cycle 24
 93 and during THEMIS dayside coverage and present the biased yearly jet occurrence rates
 94 observed by THEMIS spacecraft. We then describe how we build the statistical model
 95 to account for these biases. Following this, we create the model, show how it performs
 96 and finally present estimations of the unbiased jet occurrence rates across the solar cycle
 97 24. For comparison, we also show the estimations for the previous cycle 23.

98 2 Observations

99 2.1 Data Sets

100 We use a magnetosheath jet data set first presented by Koller et al. (2022) following
 101 the criteria introduced by Plaschke et al. (2013). It is based on THEMIS on-board
 102 moment data from the subsolar magnetosheath. THEMIS orbits undergo a yearly drift
 103 around the Earth due to the motion of the Earth around the Sun (Angelopoulos, 2008)
 104 such that their apogees will sometimes be at the flanks or in the tail so that they will
 105 not cross into the subsolar magnetosheath at all. This means that THEMIS spacecraft
 106 will inevitably be sampling that region only a fraction of the year or the solar cycle (around
 107 1/4 of the time as indicated by the red highlights in Figure 1). THEMIS spacecraft were
 108 required to be within a $7\text{--}18 R_E$ geocentric distance and inside a 30° Sun-facing cone with
 109 the Sun-Earth line as its axis. The solar wind and IMF conditions are from the 1-min
 110 high-resolution OMNI data set (King & Papitashvili, 2005), which we average over the
 111 five preceding minutes for a given magnetosheath observation. To ensure that the spacecraft
 112 were in fact in the magnetosheath, the THEMIS density measurements had to be
 113 over twice the density observed in the solar wind. Additionally, the energy flux of 1 keV
 114 ions had to be larger than that of 10 keV ions to exclude inner magnetospheric obser-
 115 vations. Only magnetosheath intervals longer than 2 min were included.

116 The main criterion of Plaschke et al. (2013) for magnetosheath jets is that the earth-
 117 ward ($-X_{\text{GSE}}$) dynamic pressure has to exceed 50 % of the corresponding solar wind dy-
 118 namic pressure. The whole jet interval around it is then defined as the period during which
 119 the earthward dynamic pressure stays above 25 % of the solar wind dynamic pressure.
 120 We follow the notation of Plaschke et al. (2013) and denote the time of the maximum
 121 dynamic pressure ratio between a jet and the upstream solar wind as t_0 . In this study,
 122 each jet is represented by the observation at its t_0 . At some point in the 1-min intervals
 123 before and after the jet interval, V_X also has to surpass $V_X(t_0)/2$. This velocity crite-
 124 rion excludes density enhancements in steady magnetosheath flow. We note that the con-
 125 clusions of this study remain while using a separate jet list introduced by Koller et al.
 126 (2022), which applies a local magnetosheath criterion for earthward dynamic pressure
 127 enhancements and does not include this velocity criterion. The list includes earthward
 128 dynamic pressure enhancements larger than three times the local 20-min running aver-
 129 age in the magnetosheath, and it can also be found online (Koller et al., 2021).

130 Recently, some concern has raised concerning the calibration of THEMIS E on-board
 131 moments during the later years of the mission, as these density and velocity measure-
 132 ments can deviate from ground moment measurements. THEMIS E observes more jets
 133 than THEMIS A and D (Koller et al., 2022). The results shown in this manuscript have
 134 been obtained using all data, but to ensure that this does not change our conclusions,
 135 we also reproduced the results while conservatively neglecting all THEMIS E data.

136 2.2 Solar Wind Observations During THEMIS Dayside Coverage

137 Figure 1 presents OMNI solar wind observations for the years 2008–2020 (panels
 138 a–g) and Earth’s heliographic latitude and heliocentric distance (panel h), spanning over
 139 the solar cycle 24 which lasted from December 2008 to December 2019. Many of the pa-
 140 rameters exhibit variations across the solar cycle: IMF magnitude is smaller during so-
 141 lar minimum and β and M_A are smaller during solar maximum. The sharp dynamic pres-
 142 sure increase observed here during 2014 (Figure 1g; close to solar maximum) is similar
 143 to a global phenomenon (across all heliolatitudes) observed during other solar cycles (J. Richard-
 144 son & Wang, 1999). We presume this may related to stream interaction regions being
 145 most prevalent during the declining phase of the solar cycle (I. G. Richardson & Cane,
 146 2012). We also see periodicity on a scale of around a year, perhaps influenced by the vary-
 147 ing heliographic latitude and heliocentric distance (Figure 1h). The time periods filled
 148 with red are the THEMIS observation intervals in the subsolar magnetosheath (as de-
 149 termined by the criteria of Plaschke et al., 2013). These intervals can coincide with the
 150 periodicity of the solar wind, which may lead to unrepresentative distributions of solar
 151 wind quantities for a given year. The most interesting parameter, from the perspective
 152 of magnetosheath jets, is the IMF cone angle. In Figure 1a, we can see that there are
 153 no substantial differences in its distribution throughout the solar cycle. This agrees with
 154 results reported by Samsonov et al. (2019), who investigated long-term variations in OMNI
 155 solar wind parameters relevant for solar wind-magnetosphere interactions over multiple
 156 solar cycles.

157 Jets are most frequently observed close to the bow shock, and their occurrence rates
 158 decrease substantially (by a factor of ~ 6) from the bow shock to the magnetopause (Plaschke
 159 et al., 2013; LaMoury et al., 2021). Thus, the spacecraft’s relative position in the mag-
 160 netosheath affects how many jets it observes. This relative position is determined by two
 161 factors: the orbit of the spacecraft and the locations of the bow shock and the magne-
 162 topause. The apogees, where the spacecraft spent most of their time, of THEMIS orbits
 163 vary throughout the years and solar wind conditions control the locations of the bound-
 164 aries. We can estimate the relative radial distance, or the fractional distance (e.g., Dim-
 165 mock & Nykyri, 2013), F ($F = 0$ at magnetopause and $F = 1$ at bow shock) in the
 166 magnetosheath by using the Shue et al. (1998) magnetopause model and the Merka et

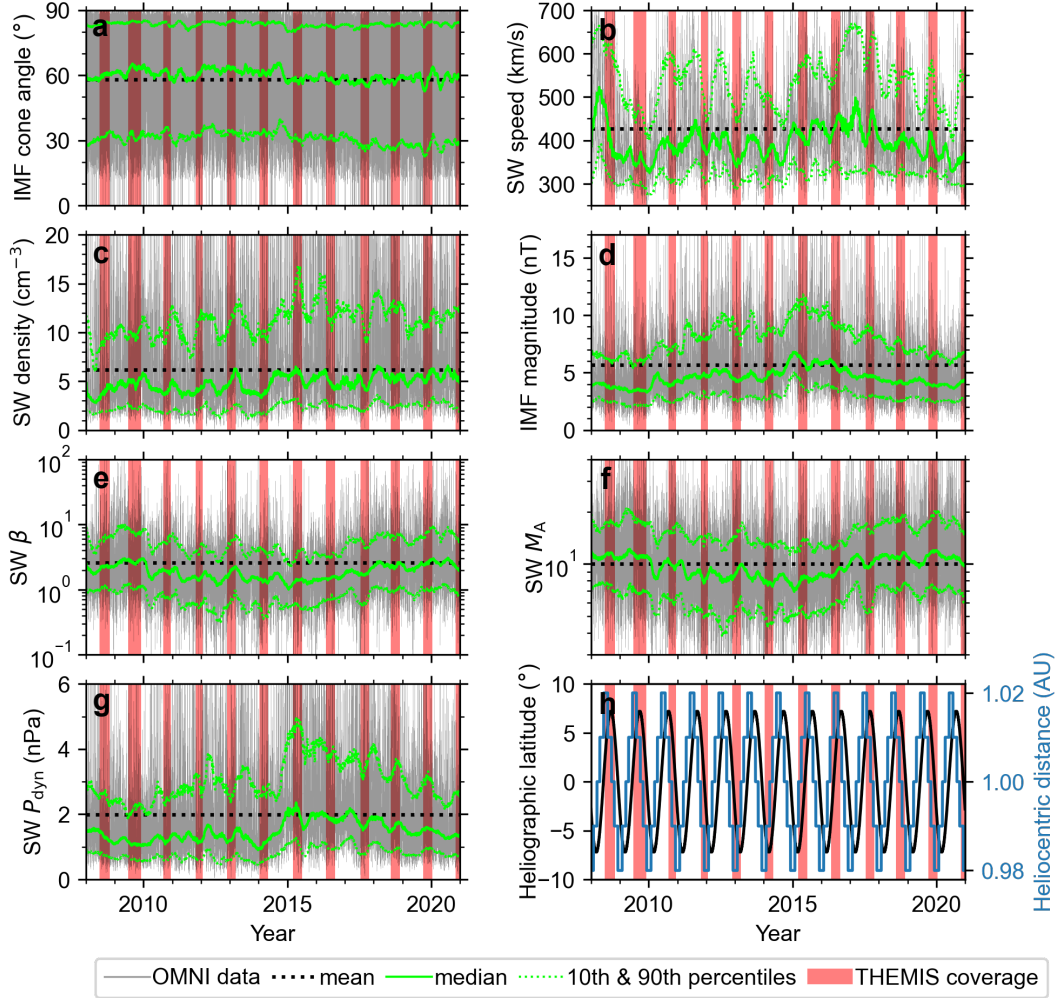


Figure 1. OMNI observations for the years 2008–2020 (solar cycle 24; from December 2008 until December 2019): (a) IMF cone angle, (b) solar wind speed, (c) density, (d) IMF magnitude, (e) β , (f) Alfvén Mach number, and (g) dynamic pressure. Gray lines show the hourly observations, red highlights the subsolar magnetosheath intervals of THEMIS, and the black dotted line shows the means of the quantities. The green solid line shows the running 90-day median, and the green dotted lines show the running 90-day 10th and 90th percentiles. Panel (h) shows Earth’s heliographic latitude (black) and heliocentric distance (blue).

167 al. (2005) bow shock model:

$$F = (r - r_{\text{MP}})/(r_{\text{BS}} - r_{\text{MP}}). \quad (1)$$

168 Here r is the geocentric distance of the spacecraft and r_{BS} and r_{MP} are the geocentric
 169 distances of the model bow shock and magnetopause along that same line. We consider
 170 observations with $F \in [0.5, 1.1]$ to be close to the bow shock. This selection yields 3400 h
 171 of magnetosheath observations and 9566 jets. Note that due to uncertainties in the model
 172 boundaries, while the spacecraft are truly in the magnetosheath, they can be outside of
 173 the model magnetosheath.

174 In Figure 2, we show the geocentric distances of the THEMIS spacecraft and the
 175 relative radial positions F during the subsolar magnetosheath observations. We can see

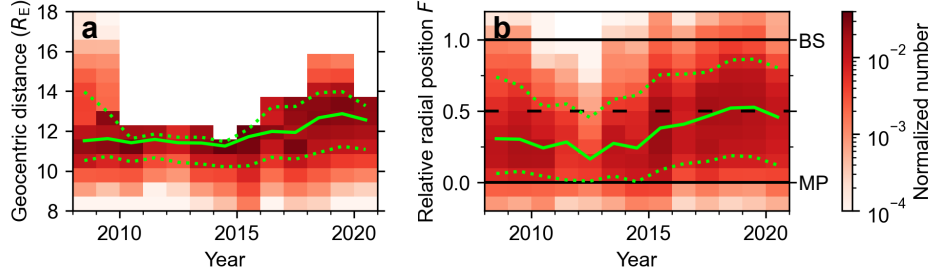


Figure 2. Distributions of (a) geocentric distances and (b) relative radial positions (between model bow shock at $F = 1$ and model magnetopause at $F = 0$) of THEMIS spacecraft during subsolar magnetosheath observations (i.e., the time spent at different locations) in years 2008–2020. The green solid line shows the yearly median, and the green dotted lines show the yearly 10th and 90th percentiles.

176 that the apogees of THEMIS spacecraft were lower in 2010–2014. THEMIS B and C or-
 177 bited the Earth with high apogees during 2008–2009, but they have been since then moved
 178 to orbit the Moon as the ARTEMIS probes (Angelopoulos, 2011). Due to the orbits, there
 179 are relatively fewer observations (only around 10% annually, see Figure 2b) close to the
 180 bow shock around 2010–2014. This may affect annual THEMIS observations of various
 181 bow shock related phenomena. The apogees were raised from 2015 onwards.

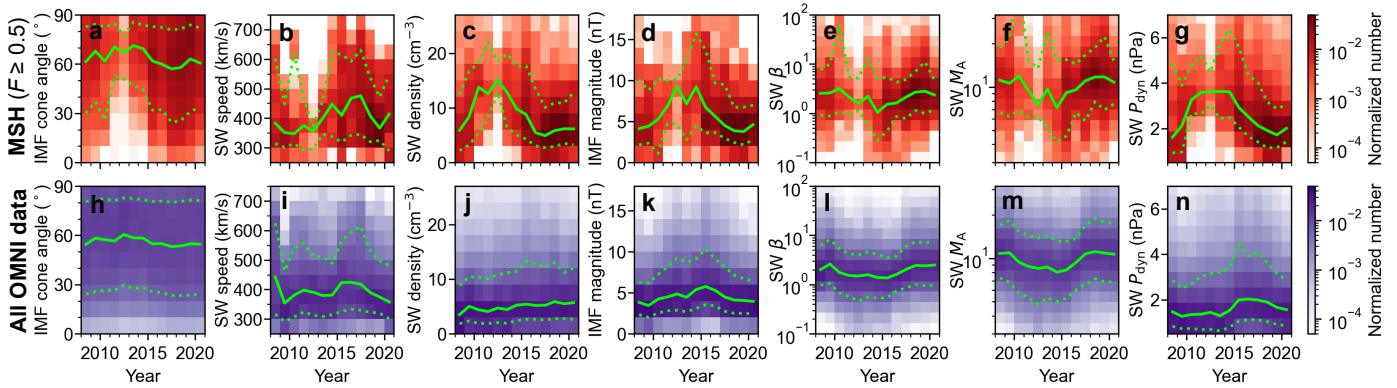


Figure 3. (a–g) OMNI solar wind observations linked to THEMIS subsolar magnetosheath observations close to the bow shock ($F \in [0.5, 1.1]$) from years 2008–2020 (solar cycle 24; from December 2008 until December 2019). (h–n) All OMNI observations from years 2008–2020. (a,h) IMF cone angle, (b,i) solar wind speed, (c,j) density, (d,k) IMF magnitude, (e,l) β , (f,m) Alfvén Mach number, and (g,n) dynamic pressure. The yearly medians are shown in solid green line and the 10th and 90th percentiles are shown in dotted green lines.

182 We focus on jets in the outer half of the magnetosheath ($F \in [0.5, 1.1]$). This al-
 183 lows us to control for the expected bias in jet occurrence due to the orbital variation.
 184 Importantly, LaMoury et al. (2021) showed that jet formation at the bow shock and the
 185 jet propagation to the magnetopause are influenced differently by the upstream solar wind
 186 conditions. Thus, focusing on the region close to the bow shock also allows us to con-
 187 centrate on jet formation. Figure 2b showed that this region was not evenly covered by
 188 the spacecraft orbits. In Figure 3, we show the distributions of OMNI measurements dur-

189 ing these THEMIS magnetosheath measurements (panels a–g, in red). For comparison,
 190 we also show all OMNI measurements during these years (panels h–n, in purple). We
 191 notice that OMNI measurements for the THEMIS magnetosheath intervals do not share
 192 the same distribution as all OMNI measurements during the period 2008–2020. In par-
 193 ticular, there are large differences between these two distributions during years 2011–
 194 2014. This is most visible for IMF cone angle, solar wind density, IMF magnitude, and
 195 dynamic pressure. The IMF cone angle being the most significant parameter controlling
 196 jet occurrence, THEMIS observed less favorable conditions for jet occurrence. This means
 197 that there will be a bias also in the annual jet occurrence rates during these years. There
 198 are several possible reasons for these less favorable conditions for jet occurrence. First,
 199 as the apogees were lower, the spacecraft were close to the bow shock only during condi-
 200 tions when the magnetosphere was compressed and the bow shock was pushed earth-
 201 ward. Thus, we see higher solar wind dynamic pressure during these years. Second, the
 202 lack of low IMF cone angles during these years is most likely due to the fact that dynamic
 203 pressure tends to be higher during high IMF cone angles than during low IMF cone an-
 204 gles (not shown). The numbers of magnetosheath intervals and jets closer to the model
 205 bow shock ultimately end up being small in those years, and these few intervals with a
 206 small number of jets have large weights in the yearly distributions.

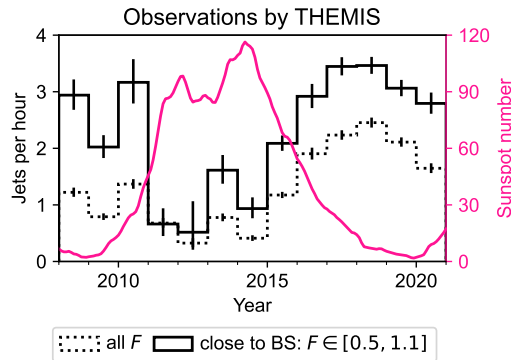


Figure 4. The yearly averages of observed jets per hour in the subsolar magnetosheath as observed by THEMIS spacecraft. The dotted histograms shows observations at all F values and the solid histogram shows the observations close to the bow shock ($F \in [0.5, 1.1]$). The error bars are 95 % binomial proportional confidence intervals. The pink line shows the smoothed sunspot number from NOAA.

207 In Figure 4 we present the observed jet occurrence rates for all F values (dotted
 208 histogram) and only close to the bow shock (solid histogram). We have also overplot-
 209 ted the number of sunspots from NOAA (SILSO World Data Center, 1996–2021) as a
 210 function of time (pink line) to act as a measure of solar activity. There is a significant
 211 decrease in the jet occurrence rates in years 2011–2014, which leads to an apparent anti-
 212 correlation: it seems as if jet occurrence is strongly decreased during the solar maximum.
 213 For all F , this decrease can be mostly attributed to the orbital differences. However, the
 214 jet occurrence close to the bow shock also seems to drop to ~ 1 jet per hour from ~ 3
 215 jets per hour observed during other years. However, as shown in Figure 3, there is a bias
 216 in solar wind conditions during these years: the IMF cone angles during these THEMIS
 217 observations (Figure 3a) were notably higher than those expected by the OMNI obser-
 218 vations (Figure 3h). Thus, these results in Figure 4 are not representative of the true
 219 jet occurrence rates.

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3 Statistical Model of Jet Occurrence as a Function of Solar Wind Conditions

3.1 Method

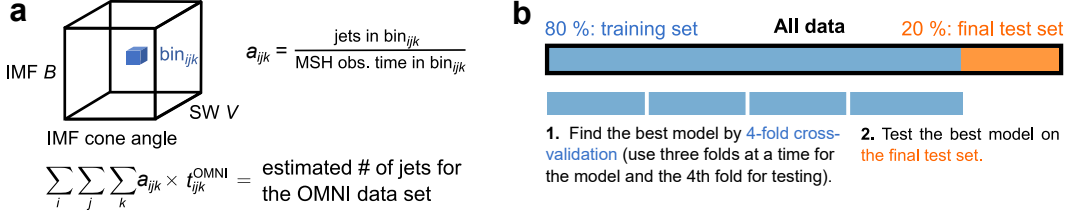


Figure 5. An illustration explaining (a) the “data cube” model, where we use existing data to estimate the occurrence rates of jets in each solar wind parameter space bin. New solar wind data can then be used as an input to the model (into the data cube) and the estimated number of jets for that data can be estimated; (b) the division of the THEMIS data set into a training set and a final test set, and how K -fold cross-validation (with $K = 4$) is used for model validation (i.e., for finding the best solar wind parameters for the model and the number of bins in the parameter space).

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To obtain more representative estimates of the jet occurrence rates close to the bow shock during different years across the solar cycle, we create an empirical statistical model by using the THEMIS jet and magnetosheath observations close to the bow shock available to us, together with their OMNI conditions. Over the whole period of 2008–2020, THEMIS spacecraft have made an extensive number of measurements in the subsolar magnetosheath during different solar wind conditions. This allows us to construct a statistical model of jet occurrence as a function of solar wind parameters. For the reconstructions we use OMNI 1-min resolution data, again averaged over the preceding five minutes. Using this extensive data set, we can calculate the number of jets seen per hour of magnetosheath observations during certain solar wind and IMF conditions (as illustrated in Figure 5a). For example, the statistical dependence of jet occurrence on the IMF cone angle is well known: jets occur mostly during low IMF cone angles, i.e., downstream of the quasi-parallel shock. We can use this statistical information to forecast/reconstruct how many jets per hour would we expect on average for given IMF cone angle conditions. We can also add other parameters to try to make the model better. We divide the parameter space into bins into which we project our jet and magnetosheath observations. We calculate the jets per hour occurrence rates a_{ijk} in all the bins (three indices i , j , and k would correspond to a model with three solar wind parameters). This “data cube” is our statistical model. To obtain an estimate from the model, we input OMNI solar wind data, again projecting it into the bins of the parameter space. Essentially the solar wind data set gives us a time t_{ijk}^{OMNI} spent in the conditions represented by bin_{ijk} . We estimate that $a_{ijk} \times t_{ijk}^{\text{OMNI}}$ jets were seen during that time. To get the estimated total number of jets for a given set of solar wind data obtained over a period of time (e.g., a year), we simply sum over the number of jets obtained for all the bins. This is the method we are going to use in this paper to estimate the unbiased yearly jet occurrence rates.

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This model is parametrized by the solar wind parameters used to create the data cube and by the number of bins in the parameter space. We select the model parameters from a pool of solar wind parameters which were found to influence jet occurrence based on the recent statistical results by LaMoury et al. (2021): IMF cone angle, IMF magnitude, flow speed, number density, plasma beta, and Alfvén Mach number. We divide each of the dimensions of the model parameter space into equal-width bins either

254 in linear or logarithmic space, depending on the parameter. This is done to best cap-
 255 ture the influence of the solar wind parameter to jet occurrence. For the binning of pa-
 256 rameters used in the models shown in this paper, we use (minimum, maximum, linear/logarithmic
 257 scale): IMF cone angle (0° , 90° , linear), IMF magnitude ($10^{0.06}$ nT, $10^{1.30}$ nT, logarithmic),
 258 SW speed (280 km/s, 700 km/s, linear), and SW density ($10^{0.1}$ cm $^{-3}$, $10^{1.4}$ cm $^{-3}$,
 259 logarithmic). We will search for the best model by using K -fold cross-validation (e.g.,
 260 Hastie et al., 2009). The search is executed by systematically going through models with
 261 different solar wind parameter combinations and systematically increasing the number
 262 of bins in each of the dimensions. The best model is selected quantitatively by minimiz-
 263 ing the maximum of our two error statistics, described below. Once the best model has
 264 been found during this *validation* step, we also test the final model's performance on new
 265 data quantitatively during the *final test* step.

266 To validate and test the model, we need to divide the data set into subsets. We do
 267 this by taking the individual intervals when THEMIS spacecraft were observing the sub-
 268 solar magnetosheath and randomly assign these measurement intervals into subsets. We
 269 perform this partition separately for intervals of each year to ensure that all subsets have
 270 similar coverage over all years. As illustrated in Figure 5b, we use 80 % of the data (the
 271 blue part) for validating and training the model and leave 20 % of the data for final test-
 272 ing (the orange part). During K -fold validation, we divide the training data into $K =$
 273 4 folds, and each of the subsets (folds) is used once as a test set while the other three
 274 are used for training the statistical model. We evaluate the model with two error esti-
 275 mates. First, we assess its performance on a test set by comparing the yearly jet occur-
 276 rence rates a_y (for year y) predicted by the model to the rates b_y actually measured in
 277 the test set for that year. We calculate the absolute error between these two values for
 278 each year and finally calculate a weighted mean of these yearly absolute errors (we weigh
 279 each of the yearly bins by the square root of the number of yearly magnetosheath ob-
 280 servations N_y in the test set):

$$E_1 = \frac{\sum_y \sqrt{N_y} |a_y - b_y|}{\sum_y \sqrt{N_y}}. \quad (2)$$

281 Each validation cycle provides an error estimate ($E_{1,n}$ for the n th cycle, $n \in [1, K] =$
 282 $[1, 4]$). We consider their average $\bar{E}_1 = \frac{1}{K} \sum_{n=1}^K E_{1,n}$ to be the error of the model in
 283 the validation process. This first error estimate evaluates the predictive performance of
 284 the model.

285 Our second error estimate measures the stability of the model. Once we have cre-
 286 ated a model using training data, we have divided the parameter space into certain bins
 287 and calculated the jet occurrence rates a_{ijk} in each of those bins. We can also do the same
 288 thing using the test set — divide the test set data into the bins and calculate the jet oc-
 289 currence rates b_{ijk} in them. This way we can measure how much the model (the jet oc-
 290 currence rates in the bins of the parameter space) changes when the parameter space is
 291 filled by using different subsets of the data. We can again calculate the weighted mean
 292 of absolute errors between these rates (weighing by the number of all OMNI 2008–2020
 293 observations N_{ijk}^{OMNI} in each bin):

$$E_2 = \frac{\sum_i \sum_j \sum_k N_{ijk}^{\text{OMNI}} |a_{ijk} - b_{ijk}|}{\sum_i \sum_j \sum_k N_{ijk}^{\text{OMNI}}}. \quad (3)$$

294 There will again be $K = 4$ errors each corresponding to one validation cycle ($E_{2,n}$ for
 295 the n th cycle, $n \in [1, K] = [1, 4]$), and we average these errors to get an error estimate
 296 for the model that is used in the validation process: $\bar{E}_2 = \frac{1}{K} \sum_{n=1}^K E_{2,n}$. This second
 297 error estimate ensures that our parameter space is not divided into too many bins (or
 298 dimensions) unnecessarily. Rather than choosing a marginally better model (in terms
 299 of predictive power) which includes many more bins, we favor a model with fewer bins
 300 as there is more statistical confidence in the rates of the bins. Weighing by all OMNI

301 measurements from 2008–2020 ensures that the model performs the best during solar wind
 302 conditions that are the most prevalent (and have the most weight for the average yearly
 303 jet occurrence rates). We also tested weighing only by OMNI measurements from 2011–
 304 2015, that is around the time of the solar maximum where the jet occurrence rates ob-
 305 served by THEMIS were biased. The conclusions of this paper remained the same. We
 306 selected the largest feasible K , as we want to maximize the number of validation cycles.
 307 However, with increasing K , the sizes of the subsets become smaller and E_2 becomes higher
 308 due to sampling error. $K = 4$ was found to be the best choice. We tested using $K =$
 309 3 and $K = 5$, and the conclusions of this study remained.

310 During validation, we search for the type of model which minimizes the maximum
 311 of these two errors, $\max(\overline{E}_1, \overline{E}_2)$. Once we have chosen the best model (the best solar
 312 wind parameters and the best combination of the number of bins in the parameter space),
 313 we make the last test by using all the training data (80 % of the data; blue part in Fig-
 314 ure 5b) to train the model and test it on the final test set (the last 20 % of the data; or-
 315 ange part in Figure 5b) that was left aside. Performing this final test on data that has
 316 not been used in creating the model allows us to test its performance on new data. We
 317 again calculate the error estimates E_1 (Eq. 2) and E_2 (Eq. 3) and consider $\max(E_1, E_2)$
 318 as the final uncertainty of the model. After this we can start using the model: inputting
 319 OMNI data from the entire solar cycles 23 and 24 into the model.

320 3.2 Results of Validation and Testing

321 In Figure 6, we show the results of 4-fold cross-validation for the best 1D model
 322 using IMF cone angle (with 16 linear bins), for the best 2D model using IMF cone an-
 323 gle and IMF magnitude (with 2×3 bins; linear, log), the best 3D model using IMF cone
 324 angle, IMF magnitude, and solar wind density (with $2 \times 2 \times 2$ bins; linear, log, linear),
 325 and the best 4D model using IMF cone angle, IMF magnitude, solar wind speed, and
 326 solar wind density (with $2 \times 2 \times 2 \times 2$ bins; linear, log, linear, log). The black histograms
 327 show the occurrence rates in the four test sets of THEMIS data. The blue histograms
 328 show the model reconstructions for these test sets. We note that especially during 2012
 329 we can see large variations in the observed jet occurrence rates between the subsets due
 330 to the very low number of magnetosheath observations and jets during that year. The
 331 weighted mean absolute errors obtained for these models during the validation process
 332 are: 0.452 jets/h, 0.399 jets/h, 0.406 jets/h, and 0.419 jets/h, respectively. The 2D model
 333 with IMF cone angle and IMF magnitude is the best model. With $K = 4$, the param-
 334 eter space errors E_2 are more limiting than the yearly errors E_1 , because increasing the
 335 number of bins in the model often decreases E_1 but increases E_2 . Thus, while some of
 336 the 3D and 4D models have slightly better yearly predictions, the uncertainty in the 2D
 337 model is lower. Furthermore, as those predictions of 3D and 4D models are only marginally
 338 better, this suggests that the parameters complementing the IMF cone angle and IMF
 339 magnitude are not so important. All of these four models seem to capture the yearly jet
 340 occurrence rates well, although not perfectly. There is enough predictive power to re-
 341 produce the dip during years 2011–2014, but the 1D IMF cone angle model does not re-
 342 produce it as well as the others. We note that have reproduced the final results of this
 343 paper also with these models that have lower E_1 , and the conclusions remain.

344 Figure 7 shows the tests comparing the model predictions created using all train-
 345 ing data to the final test set (20 % of data that was reserved for this purpose). We again
 346 show the 1D (IMF cone angle), 2D (IMF cone angle & IMF magnitude), 3D (IMF cone
 347 angle, IMF magnitude & SW density), and 4D (IMF cone angle, IMF magnitude, SW
 348 speed & SW density) models. The final weighted mean absolute errors, i.e., the uncer-
 349 tainties of the models, are 0.438 jets/h, 0.386 jets/h, 0.389 jets/h, and 0.479 jets/h, re-
 350 spectively. Again, the 2D, 3D, and 4D models capture the dip better. While the uncer-
 351 tainties are not negligible, they are, for example, much smaller than the dip in jet oc-

352 currence rates observed by THEMIS. Thus, the models will be accurate enough to de-
 353 termine whether there are strong variations in jet occurrence across a solar cycle.

354 **3.3 Reconstructing Yearly Jet Occurrence Rates for Solar Cycles 23–** 355 **24**

356 Finally, we input the entire OMNI solar wind data of the solar cycle 24 and esti-
 357 mate the yearly jet occurrence rates. The OMNI data is in the same format as used in
 358 the statistical data set when building the model: 1-min resolution data averaged over
 359 the five preceding minutes. To understand the trends more generally, we also model the
 360 solar cycle 23. We show the reconstructed jet occurrence rates per year obtained from
 361 the four different models in Figure 8 (the purple histograms), using the model uncertain-
 362 ties as error bars. The models produce almost identical results, which indicates that the
 363 IMF cone angle is enough to capture the statistically most important solar wind vari-
 364 ations influencing jet occurrence. We have again overplotted the sunspot number as a
 365 function of time. The solar cycle 23 was a more active cycle than cycle 24, as clearly ev-
 366 idenced by the significantly higher number of sunspots. We can see that there is no strong
 367 decrease in jet occurrence during the solar maximum of solar cycle 24 that would cor-
 368 respond to the dip seen in the THEMIS observations in Figure 4 (see the solid black his-
 369 togram, which we concluded was not representative of the annual solar wind distribu-
 370 tions). The histograms show a shallow (around 10–20%) dip at the maxima of both so-
 371 lar cycles, but they are within the uncertainties of the model. Thus, our model results
 372 indicate that there is no strong solar cycle variation in jet occurrence.

373 **4 Discussion**

374 We have used THEMIS observations from the subsolar magnetosheath spanning
 375 years 2008–2020 to study how jet occurrence varies throughout the solar cycle 24. How-
 376 ever, we find that the average yearly occurrence rates are not directly comparable to each
 377 other, complicating this investigation. The THEMIS spacecraft apogees changed through-
 378 out the years, and the spacecraft spent relatively less time close to the bow shock when
 379 the apogees were lower, especially during the years 2010–2014. This affected the num-
 380 ber of observed jets during those years, because jets are more common near the bow shock.
 381 Therefore, such an effect should be accounted for when aiming for the unbiased jet oc-
 382 currence rates. We have considered this by only using data close to the model bow shock.
 383 However, when the spacecraft apogees are lower than usual, this selection favors solar
 384 wind conditions during which the magnetosphere is compressed and the bow shock moves
 385 earthward, i.e., times of high solar wind dynamic pressure. Therefore, we find that the
 386 distribution of solar wind conditions during the THEMIS measurement intervals close
 387 to the bow shock is not representative of the true distribution of solar wind conditions
 388 as observed by OMNI during those years. Additionally, THEMIS spacecraft traverse the
 389 subsolar magnetosheath for only a fraction of a year. The solar wind properties vary within
 390 a year, and thus the distribution of solar wind conditions during a THEMIS observation
 391 interval may differ from the distribution throughout the entire year.

392 To account for the orbital bias and bias due to uneven solar wind sampling in the
 393 measurements of different years, we have created a statistical model of jet occurrence close
 394 to the bow shock as a function of solar wind conditions. We have used the THEMIS ob-
 395 servations from 2008–2020 to create the model. This model allows us to input unbiased
 396 OMNI solar wind observations throughout the entire solar cycles 23 and 24, and to es-
 397 timate less biased average yearly jet occurrence rates. According to our model, jet oc-
 398 currence does not vary strongly within the solar cycle. There might be a slight (around
 399 10–20%) decrease in jet occurrence during solar maximum which is, however, within the
 400 uncertainty of the model. This decrease was observed in all the presented models in this
 401 paper and for both the solar cycle 23 and 24. The best model with the lowest error es-

402 timate used two parameters: IMF cone angle and IMF magnitude. . The predictions for
 403 higher-order models with solar wind speed and density are slightly better, but the sam-
 404 pling errors (Eq. 3) increase, making these models less reliable. The model that used only
 405 IMF cone angle also produced very similar predictions for the solar cycles 23 and 24. This
 406 suggests that variations in IMF cone angle are the dominating component in variations
 407 of the absolute number of jets. This is understandable because jet occurrence rates are
 408 9 times higher during low ($< 30^\circ$) IMF cone angles than during high ($\geq 60^\circ$) IMF cone
 409 angles (Vuorinen et al., 2019).

410 OMNI high-resolution data set contains data combined from multiple spacecraft.
 411 Over the years 1996–2020 investigated here, the data set contained observations from:
 412 ACE (1998–2020), Geotail (2001), IMP-8 (1996–2000), and WIND (1996–2020). While
 413 ACE measurements (Smith et al., 1998; McComas et al., 1998) comprised most of the
 414 OMNI data for solar cycle 23, WIND observations (Lepping et al., 1995; Ogilvie et al.,
 415 1995) dominate the data set for solar cycle 24. It is important to point out that the OMNI
 416 data set has a better coverage for magnetic field data than for plasma data. The yearly
 417 magnetic field data coverage varied between 85–96 % (mean 92 %) during the years 2008–
 418 2020. The yearly coverages for plasma data varied between 69–85,% (mean 78 %). There-
 419 fore, the model that only uses magnetic field data may be preferred. We note that these
 420 percentages of OMNI coverage also apply to the data that we have input to our model
 421 in this study. However, these two-parameter and the three/four-parameter models pro-
 422 duced very similar results, which indicates that this is not an issue. Overall the propor-
 423 tions of the year when OMNI data was not available at all varied between 4–15 % (mean
 424 8 %), with 2014 having clearly the worst coverage. All in all, because this was typically
 425 a small fraction of the data and our solar wind parameter bin size is coarse, we do not
 426 expect it to be significant for the results.

427 We note that the annual jet occurrence rates are not an estimate of the number
 428 of all jets that occurred in the magnetosheath close to the bow shock, but rather an es-
 429 timate of how many jets per hour a THEMIS spacecraft would have observed if it was
 430 observing jets close to the bow shock continuously. The THEMIS spacecraft cannot ob-
 431 serve all jets, but how their observed jet occurrence rates change allow us to estimate
 432 how the total jet occurrence rates vary. As mentioned in Section 2.1, we repeated the
 433 analysis neglecting THEMIS E data, to ensure that THEMIS E on-board moment cali-
 434 bration issues do not change the results. The reconstructed average yearly jet occur-
 435 rence rates decrease by 25 % (from rates ~ 3 –4 jets/hour to ~ 2 –3 jets/hour), but the
 436 trends and our main conclusion remain: there is no strong solar cycle variation in jet oc-
 437 currence.

438 Koller et al. (2022) studied the connection between jets and large-scale solar wind
 439 structures, and found that the occurrence of jets (defined by Plaschke et al., 2013, cri-
 440 teria) increases by ~ 20 –50 % during SIRs/CIRs and HSSs, but decreases by ~ 0 –30 %
 441 during sheath regions of CMEs and by ~ 20 –60 % during their magnetic ejecta. CMEs
 442 are most frequent during solar maximum when flows related to them can constitute up
 443 to ~ 40 –60 % of the solar wind at Earth (e.g., I. G. Richardson & Cane, 2012). SIRs
 444 or CIRs are more frequent during the declining phase of the cycle when they can make
 445 up around 60 % or more of the solar wind flow at Earth (e.g., I. G. Richardson & Cane,
 446 2012). While our results indicate that there are no strong statistical variations in the av-
 447 erage yearly jet occurrence rates, solar wind structures and periodic variations in the so-
 448 lar wind can still modulate jet occurrence. More studies are needed to understand the
 449 ranges of jet occurrence rates during different types of events. Here we have focused on
 450 jet formation, but jet propagation to the magnetopause is enhanced during high solar
 451 wind speed (LaMoury et al., 2021). This means that solar cycle periods with higher so-
 452 lar wind speeds may lead to more geoeffective jets.

5 Conclusions and Summary

Yearly THEMIS observations of jet occurrence rates are biased due to variations in spacecraft apogees in the subsolar magnetosheath and uneven coverage of the yearly solar wind conditions. Considering these biases in the data is crucial, because improper normalization can affect the conclusions drawn from the observations. This issue is not unique to jets, but also concerns other phenomena that are dependent on solar wind conditions and/or position in the magnetosheath.

Leveraging the information contained in the vast amount of THEMIS data, we have created an empirical statistical model of magnetosheath jet occurrence as a function of solar wind conditions and used it to reconstruct unbiased estimations of yearly jet occurrence rates across solar cycles 23 and 24. The best model (that minimizes the error estimates) has two parameters: IMF cone angle and IMF magnitude. 3D and 4D models with solar wind speed and density also included can provide slightly better yearly predictions, but the statistical errors become larger due to the finite size of the data set. Even a 1D model with just the IMF cone angle produces similar results and identical conclusions. Our model results show that the occurrence rate of earthward magnetosheath jets close to the bow shock does not vary significantly across the solar cycle. Both solar cycles exhibit a decrease of the order of 10–20% near the solar maximum, but this is within the uncertainties of the model. In the future, the statistical model can be further improved by including more data, either measurements from other spacecraft missions or future THEMIS observations.

Open Research

THEMIS and OMNI data can be accessed via, e.g., NASA’s Coordinated Data Analysis Web (<https://cdaweb.gsfc.nasa.gov/>). The magnetosheath and jet data set used in this study can be found at Koller et al. (2021).

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References

- Angelopoulos, V. (2008). The THEMIS Mission. *Space Science Reviews*, *141*(1), 5. doi: 10.1007/s11214-008-9336-1
- Angelopoulos, V. (2011). The ARTEMIS Mission. *Space Science Reviews*, *165*(1), 3–25. doi: 10.1007/s11214-010-9687-2
- Archer, M. O., & Horbury, T. S. (2013). Magnetosheath dynamic pressure enhancements: occurrence and typical properties. *Annales Geophysicae*, *31*(2), 319–331. doi: 10.5194/angeo-31-319-2013
- Dimmock, A. P., & Nykyri, K. (2013). The statistical mapping of magnetosheath plasma properties based on THEMIS measurements in the magnetosheath interplanetary medium reference frame. *Journal of Geophysical Research: Space Physics*, *118*(8), 4963–4976. doi: 10.1002/jgra.50465
- Hastie, T., Tibshirani, R., & Friedman, J. (2009). *The Elements of Statistical Learning* (2nd ed.). Springer.

- 501 Hietala, H., Laitinen, T. V., Andréevová, K., Vainio, R., Vaivads, A., Palmroth,
502 M., . . . Rème, H. (2009). Supermagnetosonic Jets behind a Collision-
503 less Quasiparallel Shock. *Physical Review Letters*, *103*(24), 245001. doi:
504 10.1103/PhysRevLett.103.245001
- 505 Hietala, H., & Plaschke, F. (2013). On the generation of magnetosheath high-speed
506 jets by bow shock ripples. *Journal of Geophysical Research: Space Physics*,
507 *118*(11), 7237–7245. doi: 10.1002/2013JA019172
- 508 Karlsson, T., Kullen, A., Liljeblad, E., Brenning, N., Nilsson, H., Gunell, H., &
509 Hamrin, M. (2015). On the origin of magnetosheath plasmoids and their rela-
510 tion to magnetosheath jets. *Journal of Geophysical Research: Space Physics*,
511 *120*, 7390–7403. doi: 10.1002/2015JA021487
- 512 King, J. H., & Papitashvili, N. E. (2005). Solar wind spatial scales in and com-
513 parisons of hourly Wind and ACE plasma and magnetic field data. *Jour-
514 nal of Geophysical Research: Space Physics (19782012)*, *110*(A2). doi:
515 10.1029/2004JA010649
- 516 Koller, F., Plaschke, F., Temmer, M., & Preisser, L. (2021). *THEMIS local and up-
517 stream magnetosheath jet data 2008-2020. [Dataset]*. <https://osf.io/6ywjz>.
- 518 Koller, F., Plaschke, F., Temmer, M., Preisser, L., Roberts, O. W., & Vrs, Z.
519 (2023). Magnetosheath jet formation influenced by parameters in solar
520 wind structures. *Journal of Geophysical Research: Space Physics*, *128*(4),
521 e2023JA031339. doi: 10.1029/2023JA031339
- 522 Koller, F., Temmer, M., Preisser, L., Plaschke, F., Geyer, P., Jian, L. K., . . . LaM-
523 oury, A. T. (2022). Magnetosheath Jet Occurrence Rate in Relation to
524 CMEs and SIRs. *Journal of Geophysical Research: Space Physics*, *127*(4),
525 e2021JA030124. doi: 10.1029/2021JA030124
- 526 LaMoury, A. T., Hietala, H., Plaschke, F., Vuorinen, L., & Eastwood, J. P. (2021).
527 Solar wind control of magnetosheath jet formation and propagation to the
528 magnetopause. *Journal of Geophysical Research: Space Physics*, *126*(9),
529 e2021JA029592. doi: 10.1029/2021JA029592
- 530 Lepping, R. P., Acuña, M. H., Burlaga, L. F., Farrell, W. M., Slavin, J. A., Schat-
531 ten, K. H., . . . Worley, E. M. (1995). The WIND magnetic field investigation.
532 *Space Science Reviews*, *71*(1), 207-229. doi: 10.1007/BF00751330
- 533 McComas, D. J., Bame, S. J., Barker, P., Feldman, W. C., Phillips, J. L., Riley,
534 P., & Griffee, J. W. (1998). Solar Wind Electron Proton Alpha Monitor
535 (SWEPAM) for the Advanced Composition Explorer. *Space Science Reviews*,
536 *86*(1), 563-612. doi: 10.1023/A:1005040232597
- 537 Merka, J., Szabo, A., Slavin, J. A., & Peredo, M. (2005). Three-dimensional position
538 and shape of the bow shock and their variation with upstream Mach numbers
539 and interplanetary magnetic field orientation. *Journal of Geophysical Research:
540 Space Physics*, *110*(A4), 1–13. doi: 10.1029/2004JA010944
- 541 Ogilvie, K. W., Chornay, D. J., Fritzenreiter, R. J., Hunsaker, F., Keller, J., Lo-
542 bell, J., . . . Gergin, E. (1995). SWE, a comprehensive plasma instru-
543 ment for the WIND spacecraft. *Space Science Reviews*, *71*(1), 55-77. doi:
544 10.1007/BF00751326
- 545 Palmroth, M., Hietala, H., Plaschke, F., Archer, M., Karlsson, T., Blanco-Cano, X.,
546 . . . Turc, L. (2018). Magnetosheath jet properties and evolution as determined
547 by a global hybrid-Vlasov simulation. *Annales Geophysicae*, *36*(5), 1171–1182.
548 doi: 10.5194/angeo-36-1171-2018
- 549 Plaschke, F., Hietala, H., & Angelopoulos, V. (2013). Anti-sunward high-speed jets
550 in the subsolar magnetosheath. *Annales Geophysicae*, *31*(10), 1877–1889. doi:
551 10.5194/angeo-31-1877-2013
- 552 Plaschke, F., Hietala, H., Archer, M., Blanco-Cano, X., Kajdič, P., Karlsson, T., . . .
553 Sibeck, D. (2018). Jets Downstream of Collisionless Shocks. *Space Science
554 Reviews*, *214*(5), 81. doi: 10.1007/s11214-018-0516-3
- 555 Raptis, S., Karlsson, T., Vaivads, A., Pollock, C., Plaschke, F., Johlander, A., . . .

- 556 Lindqvist, P.-A. (2022). Downstream high-speed plasma jet generation as a
 557 direct consequence of shock reformation. *Nature Communications*, *13*(1), 598.
 558 doi: 10.1038/s41467-022-28110-4
- 559 Richardson, I. G., & Cane, H. V. (2012). Near-earth solar wind flows and related
 560 geomagnetic activity during more than four solar cycles (1963-2011). *J. Space*
 561 *Weather Space Clim.*, *2*, A02. doi: 10.1051/swsc/2012003
- 562 Richardson, J., & Wang, C. (1999). The global nature of solar cycle variations of
 563 the solar wind dynamic pressure. *Geophysical Research Letters*, *26*(5), 561-564.
 564 doi: <https://doi.org/10.1029/1999GL900052>
- 565 Samsonov, A. A., Bogdanova, Y. V., Branduardi-Raymont, G., Safrankova, J.,
 566 Nemecek, Z., & Park, J.-S. (2019). Long-Term Variations in Solar Wind Pa-
 567 rameters, Magnetopause Location, and Geomagnetic Activity Over the Last
 568 Five Solar Cycles. *Journal of Geophysical Research: Space Physics*, *124*(6),
 569 4049-4063. doi: 10.1029/2018JA026355
- 570 Schwartz, S. J. (1991). Magnetic field structures and related phenomena at quasi-
 571 parallel shocks. *Advances in Space Research*, *11*(9), 231-240. doi: 10.1016/0273
 572 -1177(91)90039-M
- 573 Shue, J.-H., Song, P., Russell, C. T., Steinberg, J. T., Chao, J. K., Zastenker, G., ...
 574 Kawano, H. (1998). Magnetopause location under extreme solar wind condi-
 575 tions. *Journal of Geophysical Research: Space Physics*, *103*(A8), 17691-17700.
 576 doi: 10.1029/98JA01103
- 577 SILSO World Data Center. (1996-2021). The International Sunspot Number. *Inter-*
 578 *national Sunspot Number Monthly Bulletin and online catalogue*.
- 579 Smith, C. W., L'Heureux, J., Ness, N. F., Acuña, M. H., Burlaga, L. F., & Scheifele,
 580 J. (1998). The ace magnetic fields experiment. *Space Science Reviews*, *86*(1),
 581 613-632. doi: 10.1023/A:1005092216668
- 582 Suni, J., Palmroth, M., Turc, L., Battarbee, M., Johlander, A., Tarvus, V., ...
 583 Zhou, H. (2021). Connection Between Foreshock Structures and the Genera-
 584 tion of Magnetosheath Jets: Vlasiator Results. *Geophysical Research Letters*,
 585 *48*(20), e2021GL095655. doi: 10.1029/2021GL095655
- 586 Vuorinen, L., Hietala, H., & Plaschke, F. (2019). Jets in the magnetosheath: IMF
 587 control of where they occur. *Annales Geophysicae*, *37*(4), 689-697. doi: 10
 588 .5194/angeo-37-689-2019

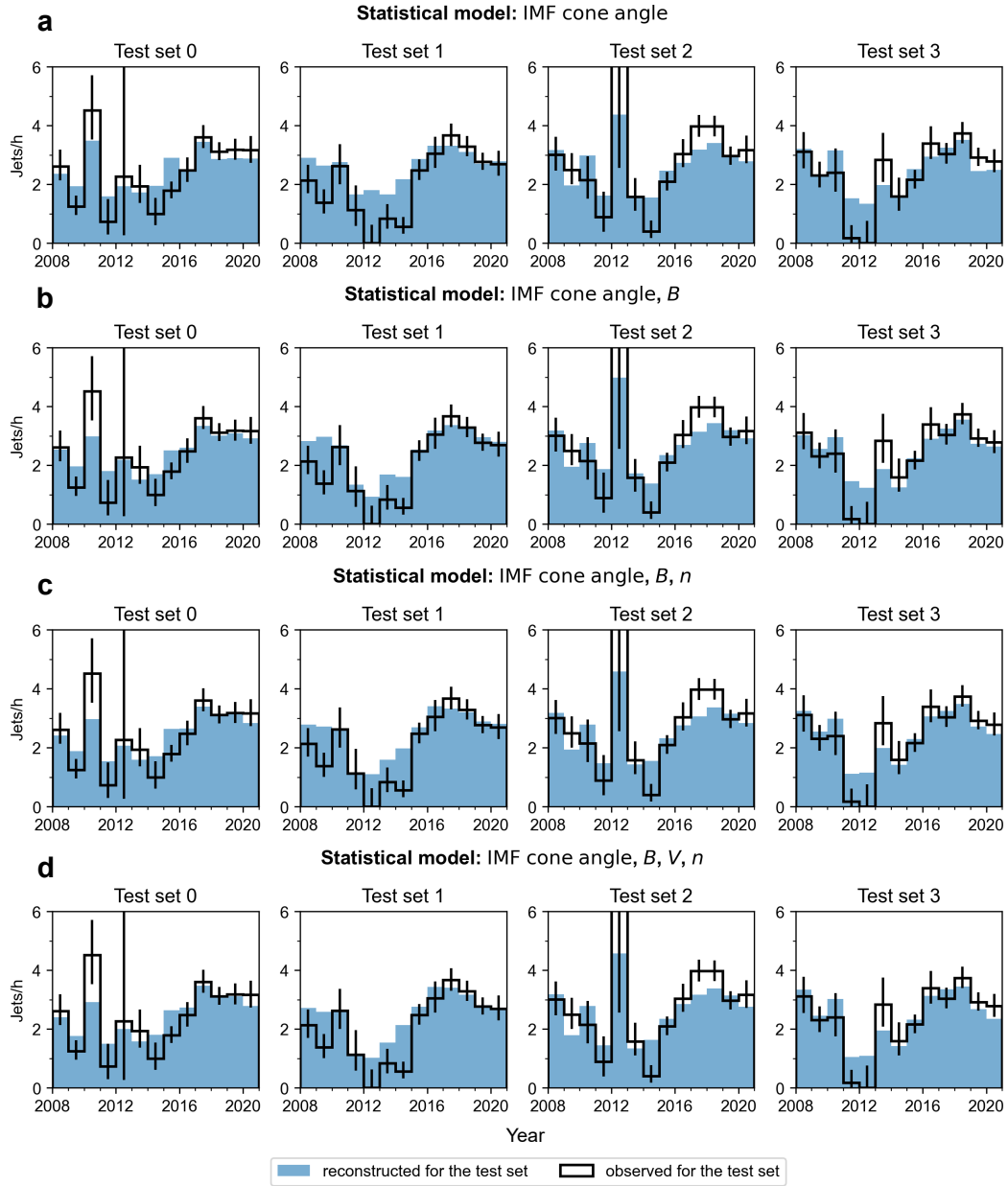


Figure 6. Results of the K-fold cross-validation, where the training data (80% of the THEMIS data set) has been divided into four folds. Each of the subsets is used once as a test set while the other four are used for creating the statistical models using (a) IMF cone angle, (b) IMF cone angle and magnitude, (c) IMF cone angle, IMF magnitude, and solar wind speed, and (d) IMF cone angle, IMF magnitude, solar wind speed, and density. The black histograms show the number of jets per observation time in the subsolar magnetosheath in the test sets. The error bars are 95 % proportional confidence intervals. The blue histograms show the model predictions for the test sets.

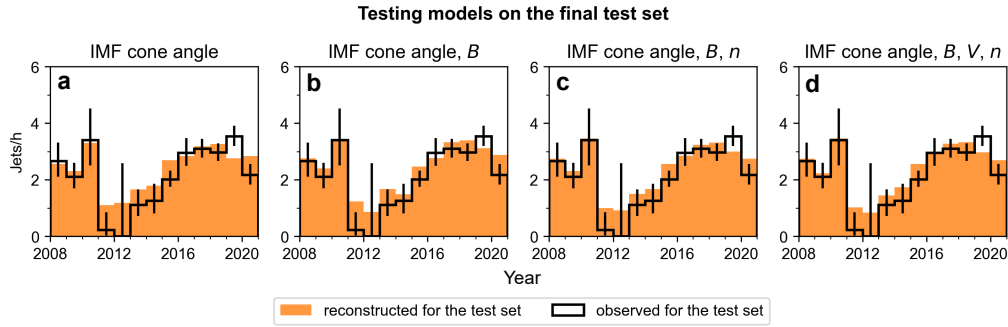


Figure 7. The results of testing the final models created using the whole training set (80 % of the THEMIS data set) on the final test set (20 % of the THEMIS data set). The orange histograms show the model predictions, and the black histogram shows the observed jet occurrence rates in the test set. The error bars are 95 % binomial proportional confidence intervals.

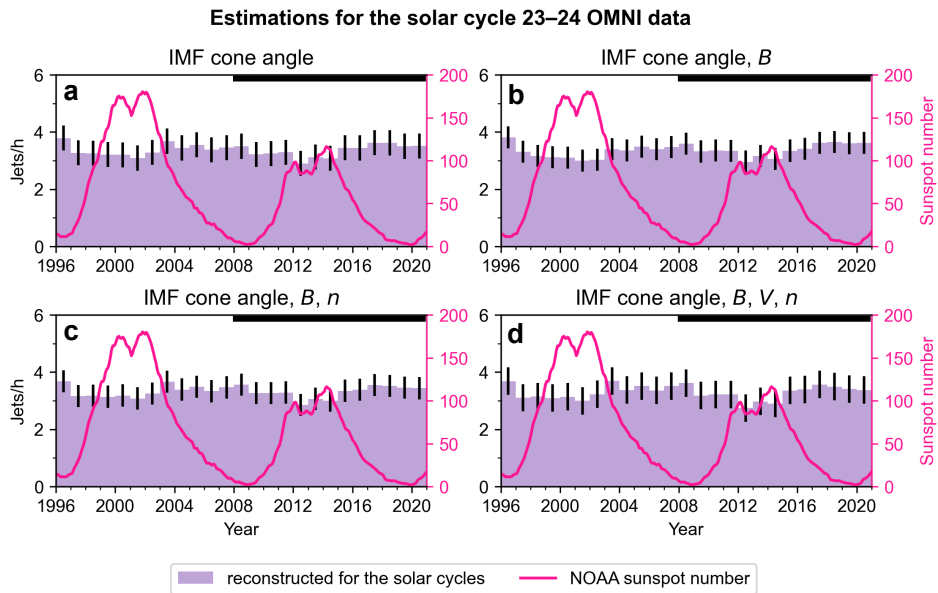
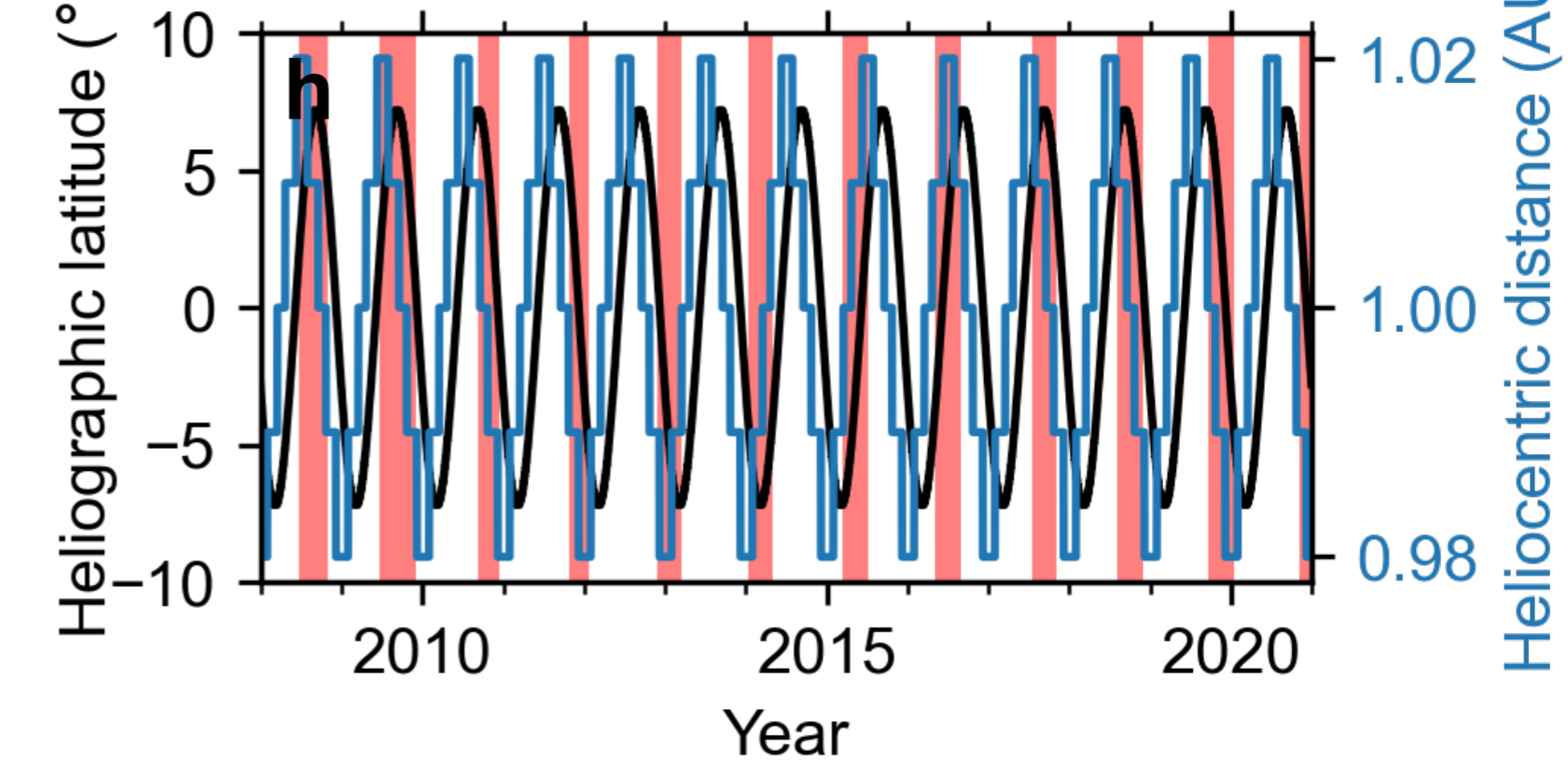
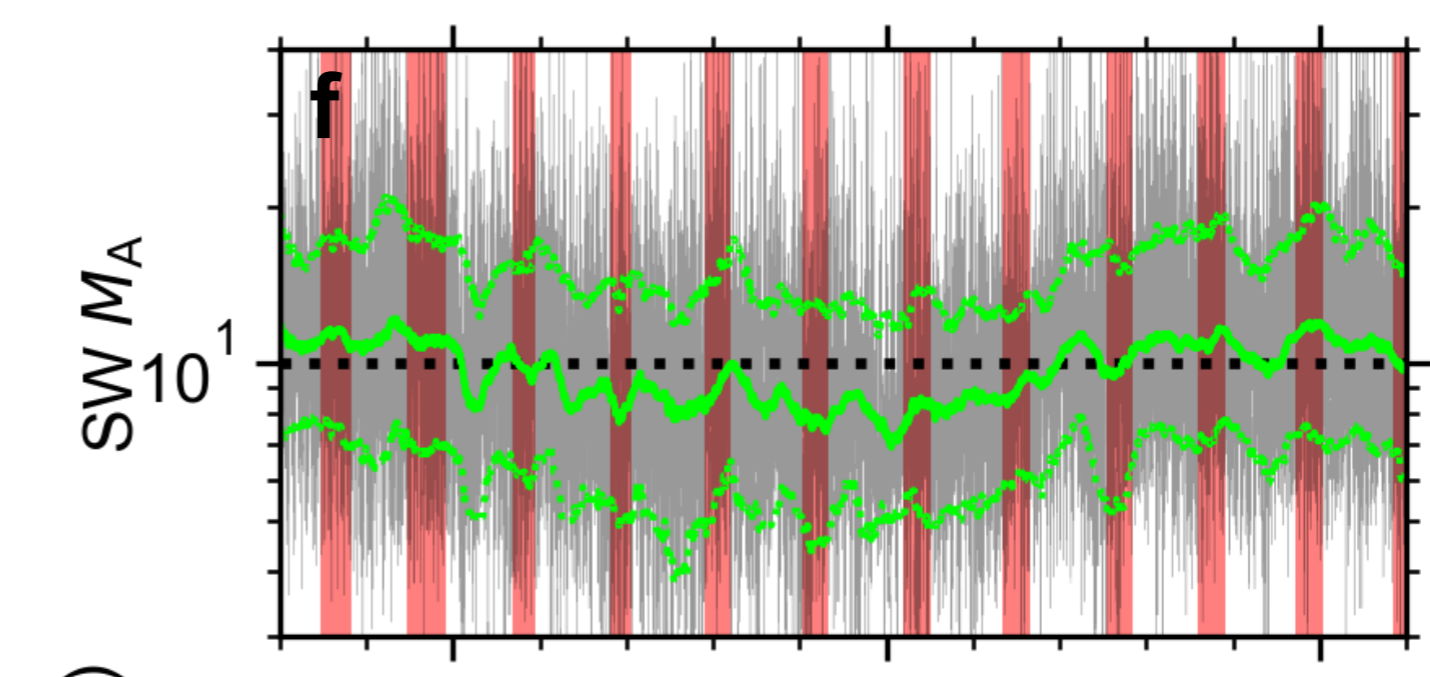
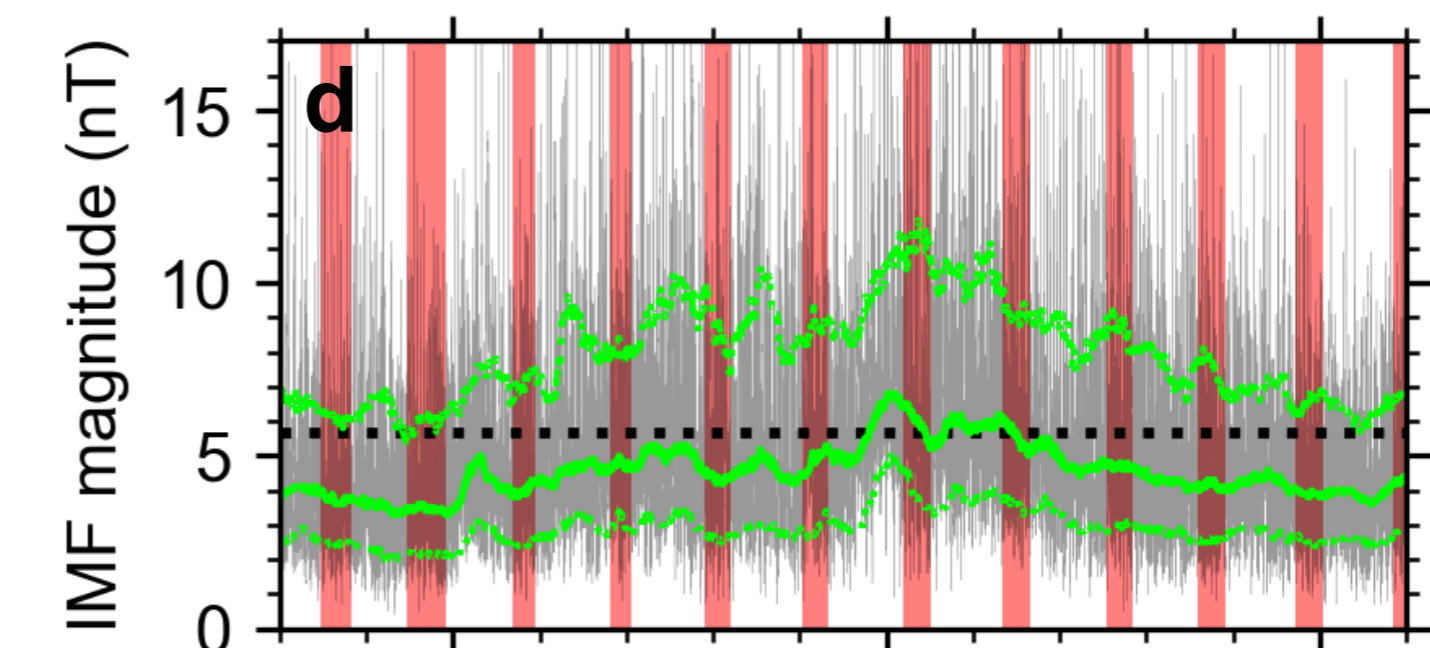
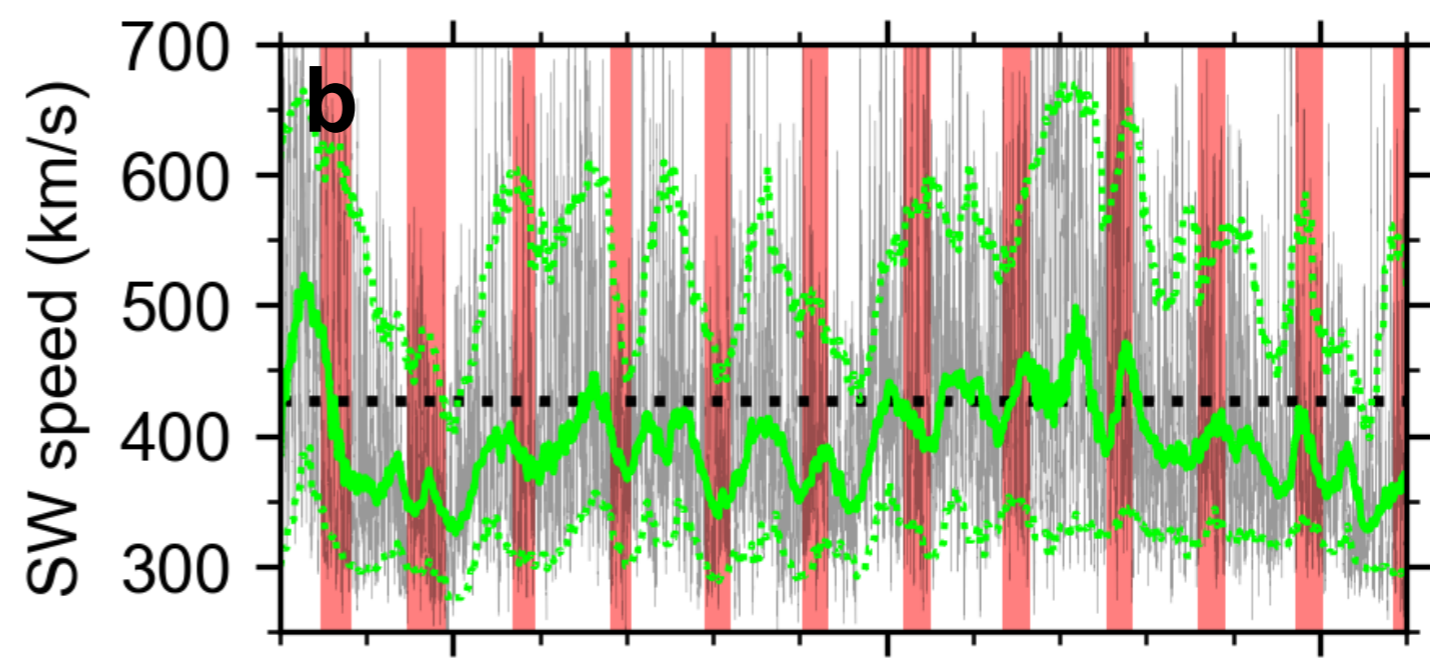
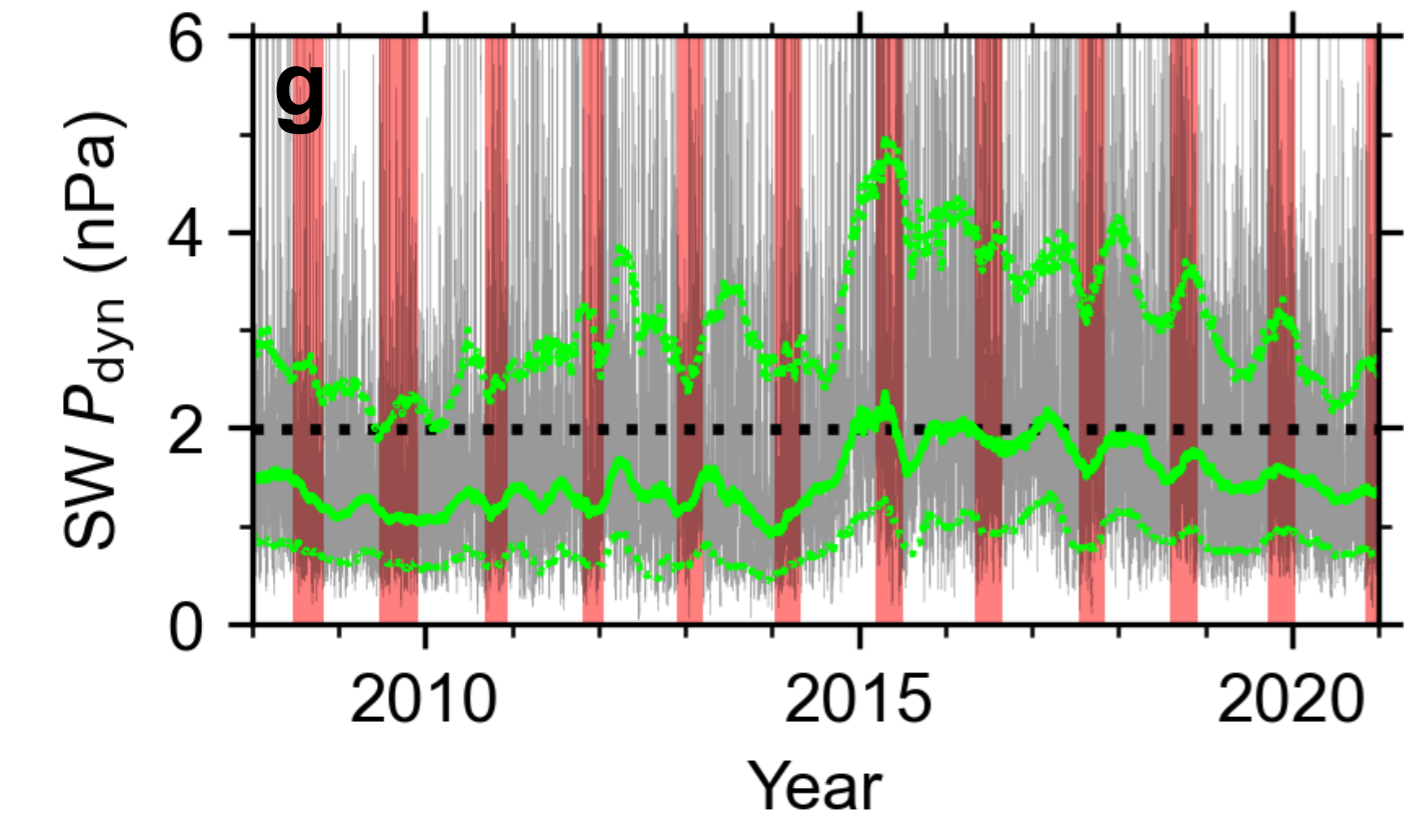
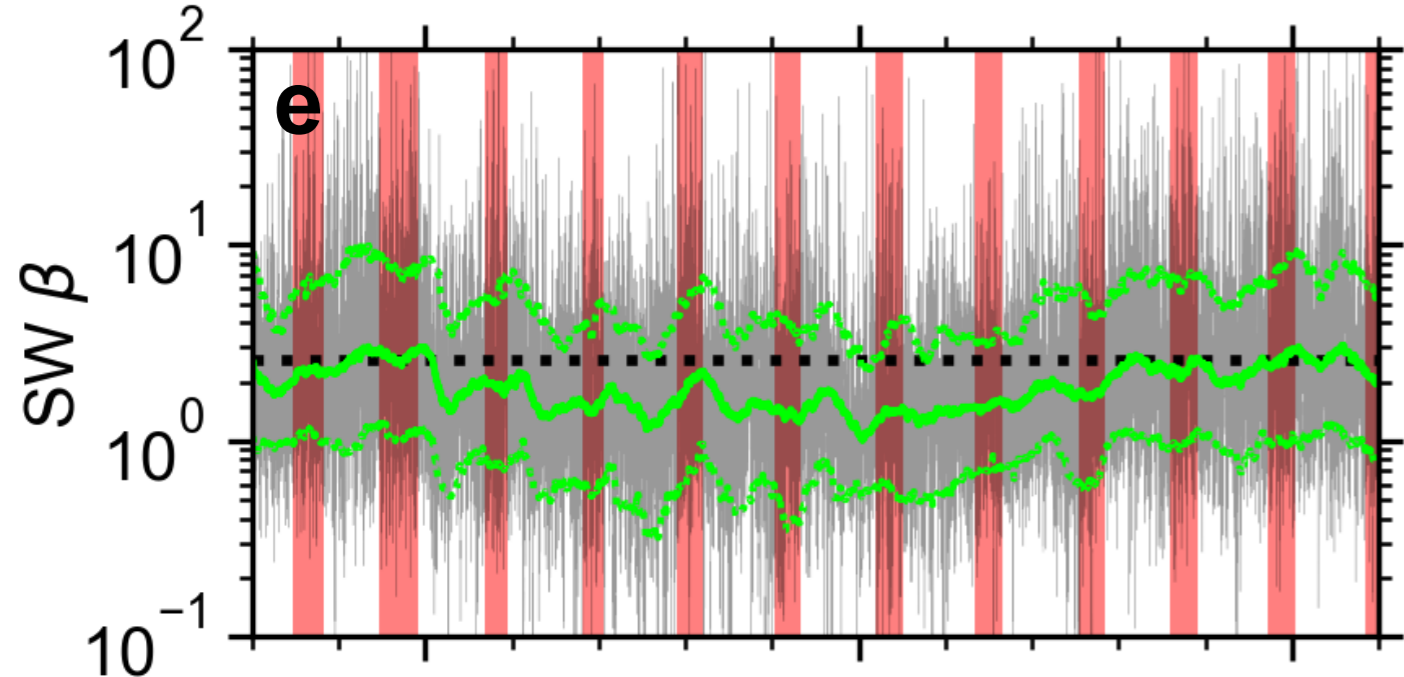
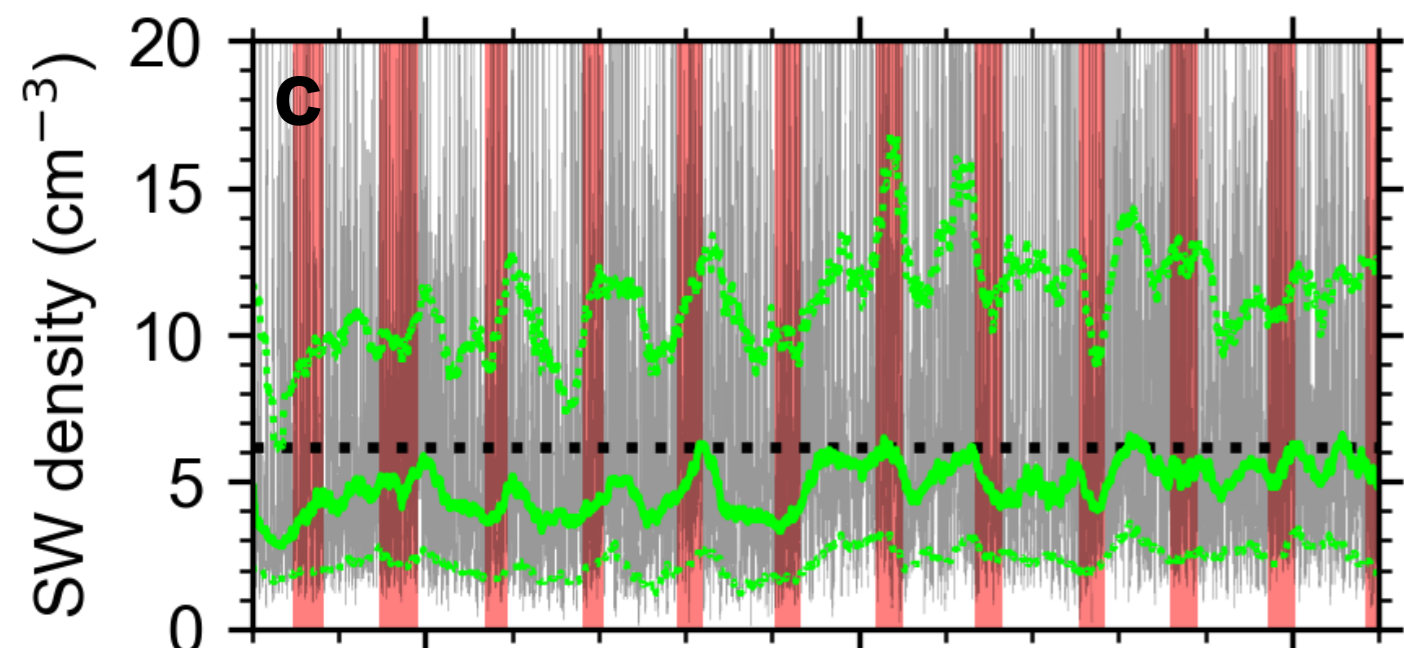
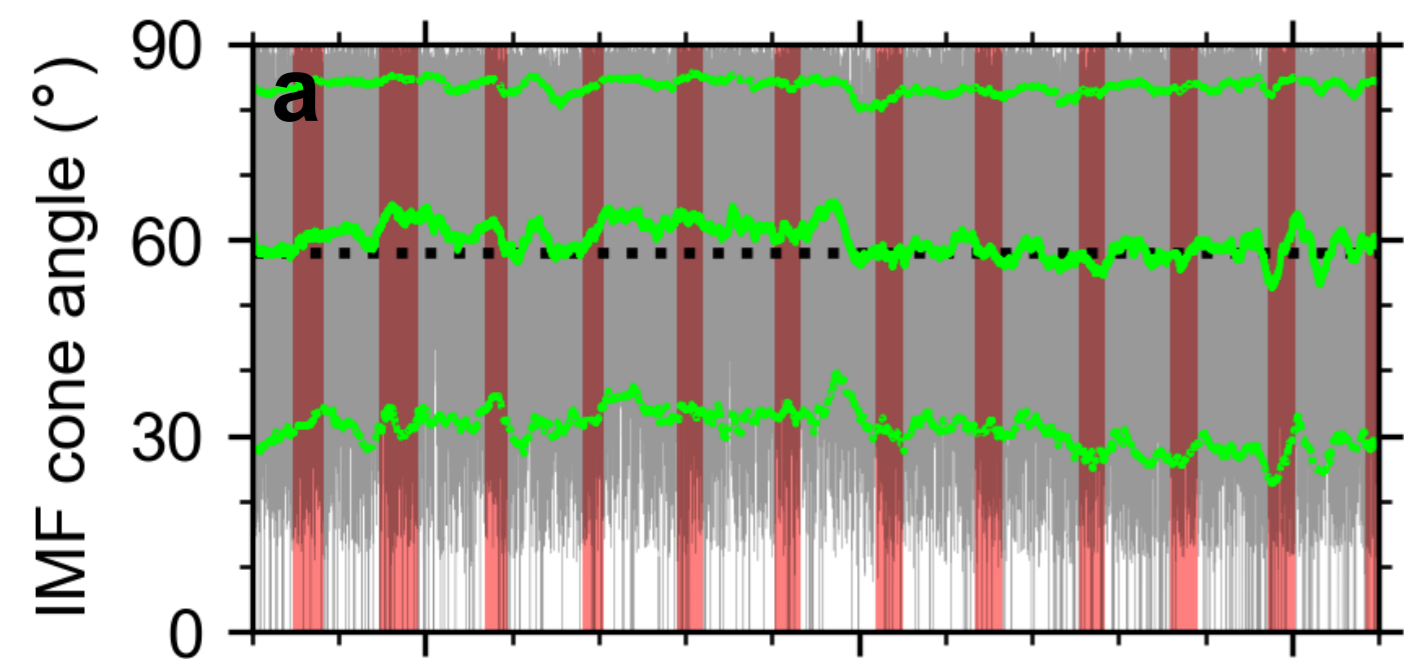


Figure 8. Results of the statistical model (using IMF cone angle, IMF magnitude, solar wind speed, and density) applied to the OMNI data of years 1996–2020 (spanning over solar cycles 23 & 24). The error bars denote the estimated uncertainties of the models. The pink line shows the smoothed sunspot number from NOAA. The thick black horizontal lines at the top of the panels highlight the years 2008–2020, to which we can compare the results of Figure 4.

Figure 1.



— OMNI data mean — median 10th & 90th percentiles ■ THEMIS coverage

Figure 2.

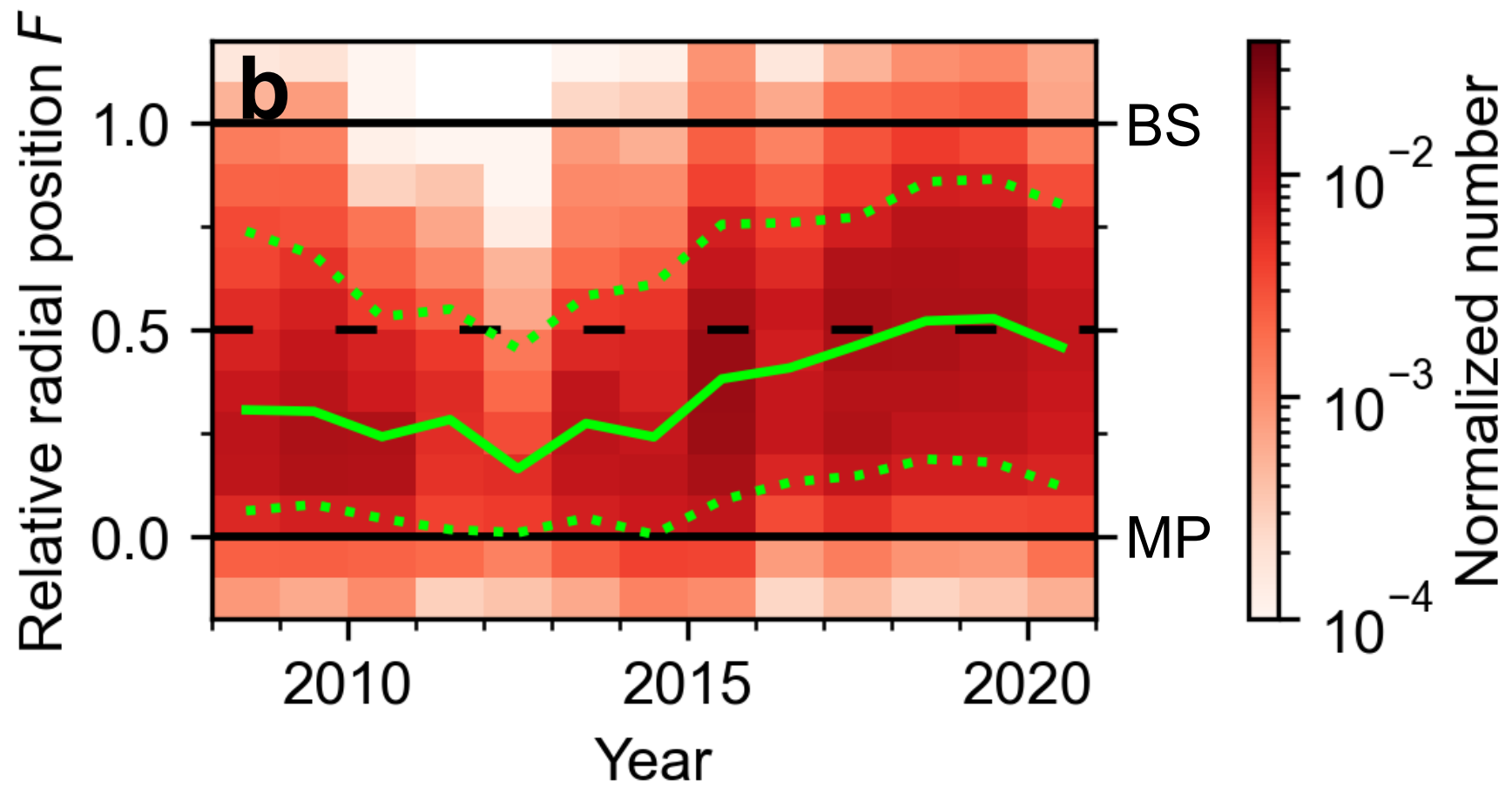
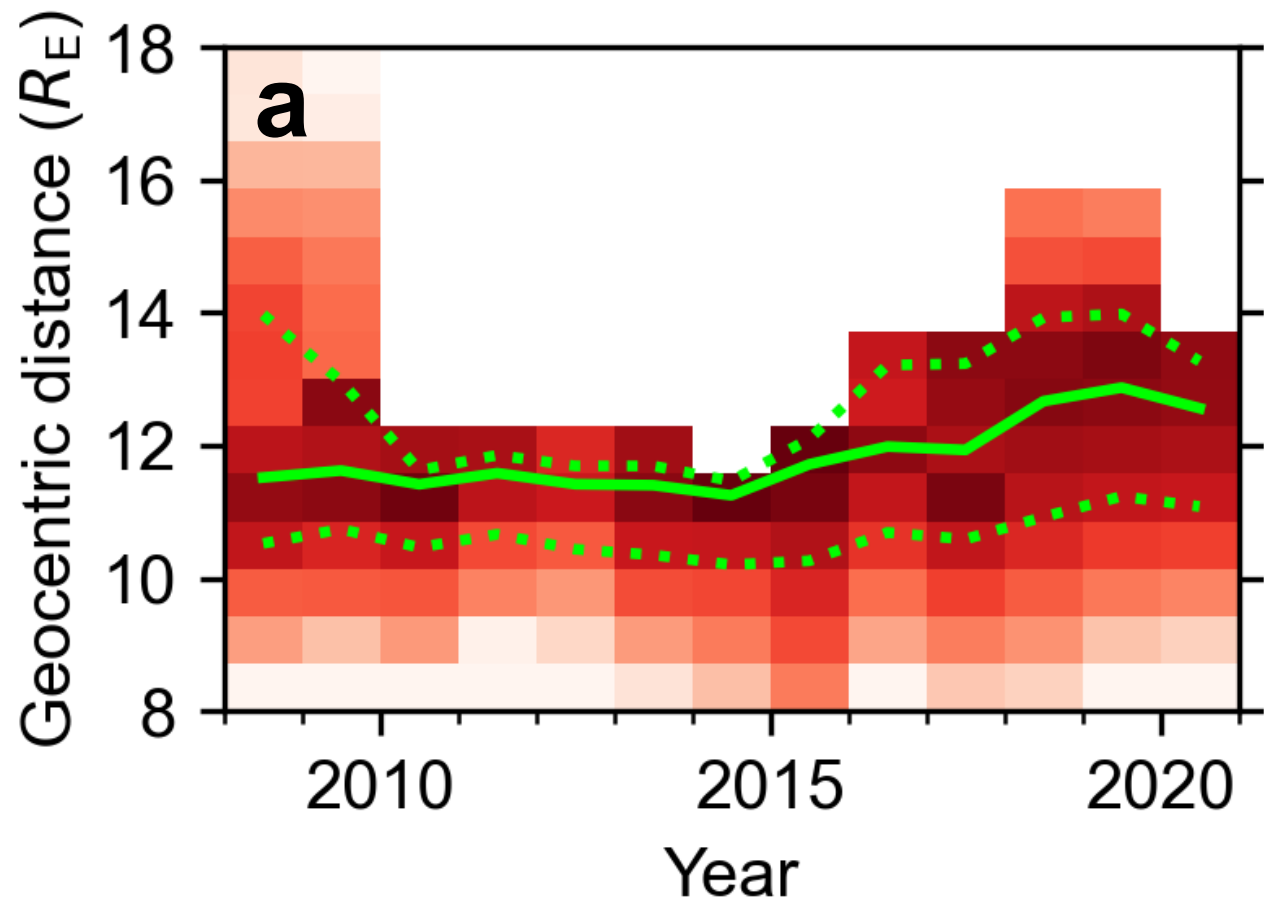


Figure 3.

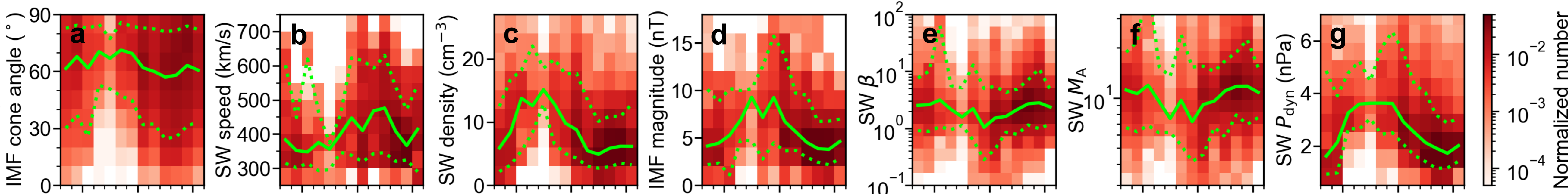
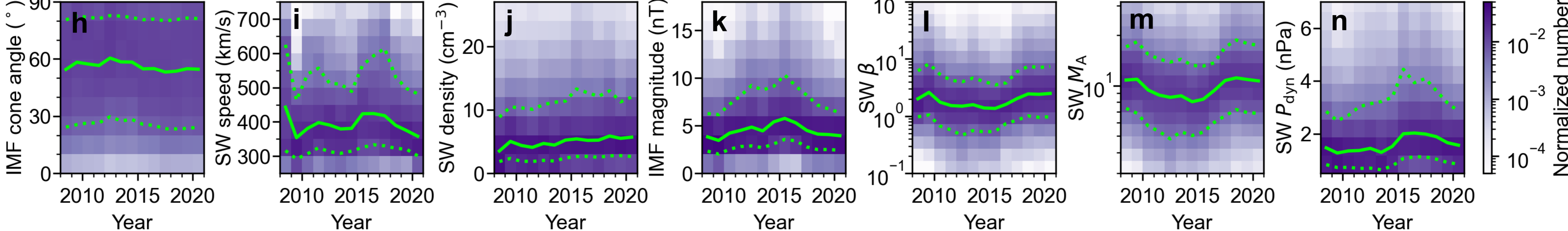
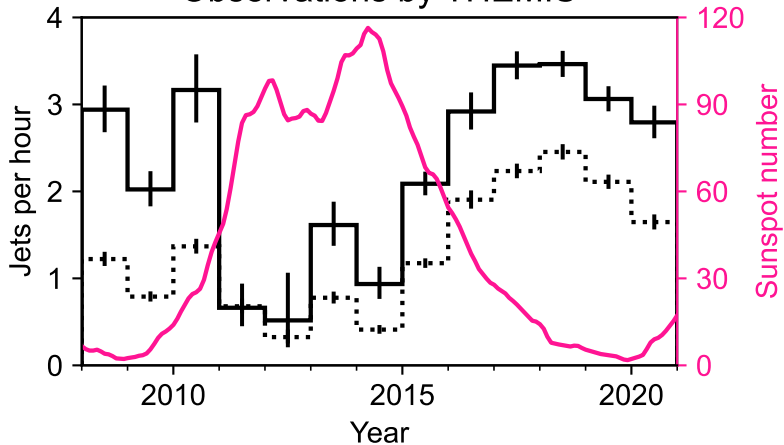
MSH ($F \geq 0.5$)**ALL OMNI data**

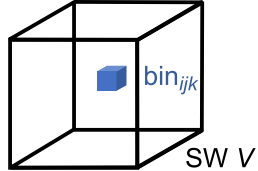
Figure 4.

Observations by THEMIS



..... all F **▬** close to BS: $F \in [0.5, 1.1]$

Figure 5.

aIMF B 

$$a_{ijk} = \frac{\text{jets in bin}_{ijk}}{\text{MSH obs. time in bin}_{ijk}}$$

IMF cone angle

$$\sum_i \sum_j \sum_k a_{ijk} \times t_{ijk}^{\text{OMNI}} = \text{estimated \# of jets for the OMNI data set}$$

b

80 %: training set

All data

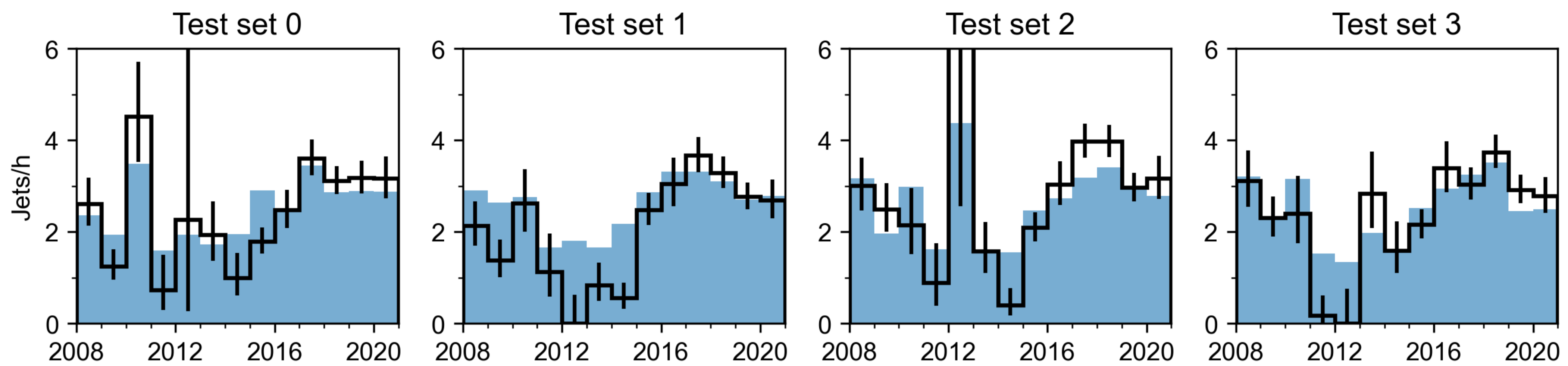
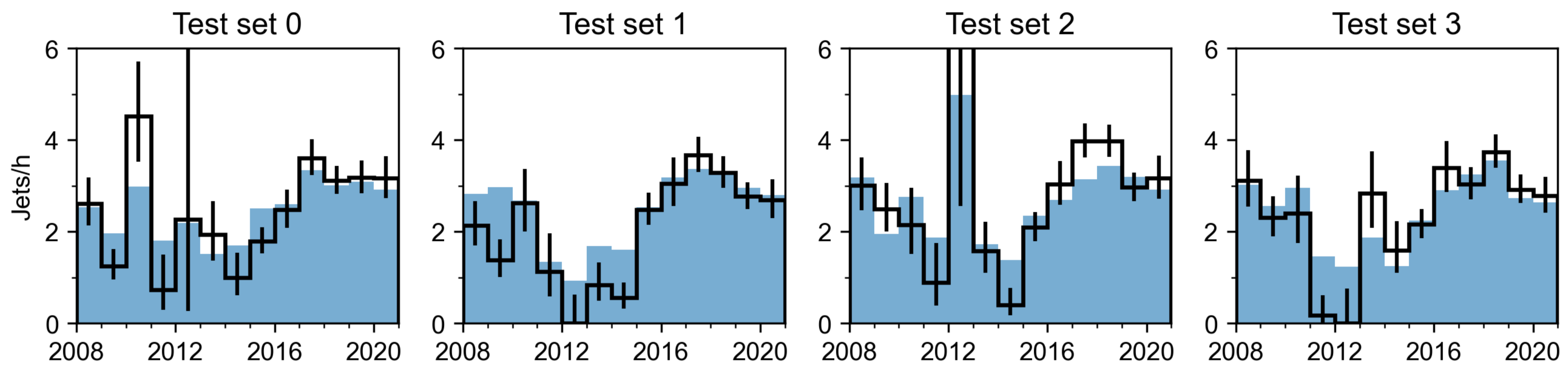
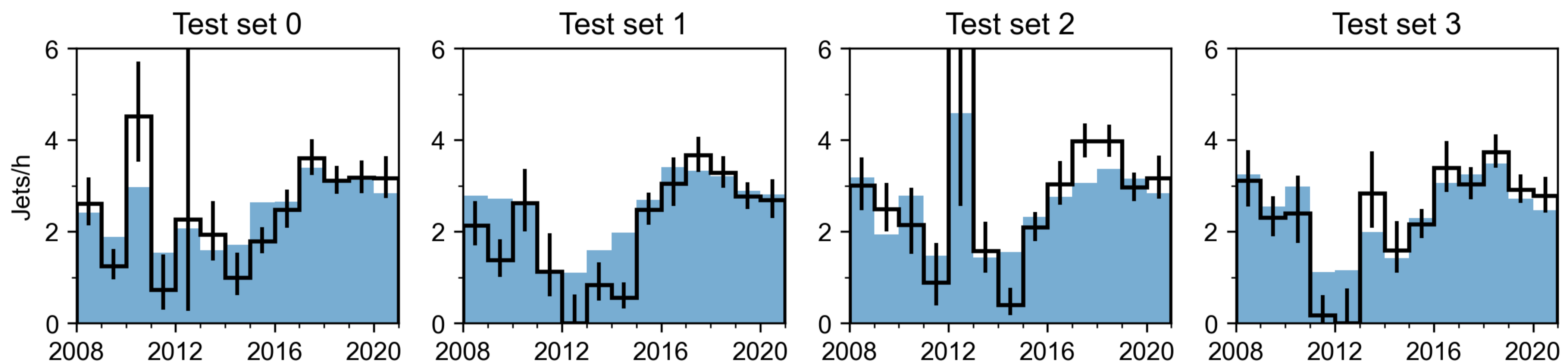
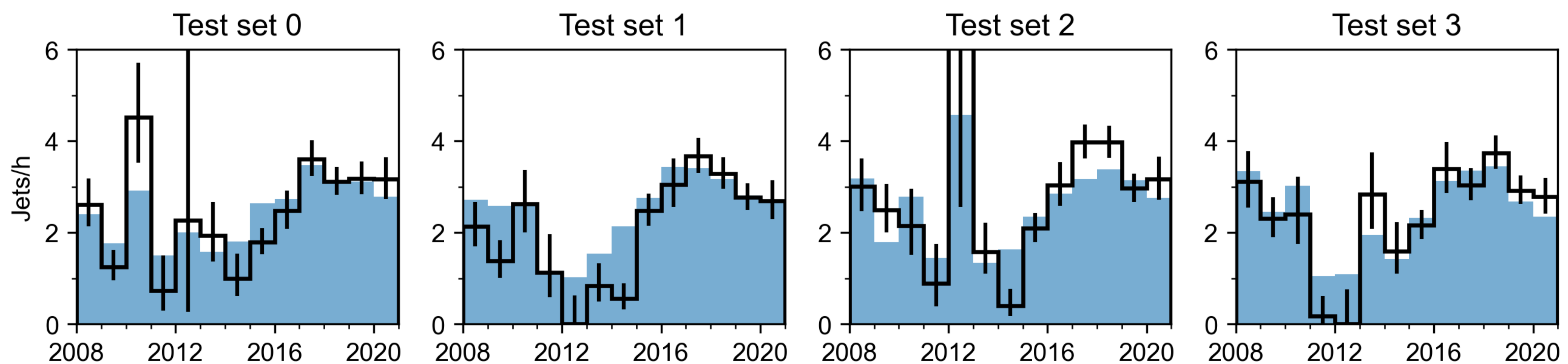
20 %: final test set



1. Find the best model by **4-fold cross-validation** (use three folds at a time for the model and the 4th fold for testing).

2. Test the best model on **the final test set**.

Figure 6.

a Statistical model: IMF cone angle**b** Statistical model: IMF cone angle, B **c** Statistical model: IMF cone angle, B, n **d** Statistical model: IMF cone angle, B, V, n 

Year

reconstructed for the test set observed for the test set

Figure 7.

Testing models on the final test set

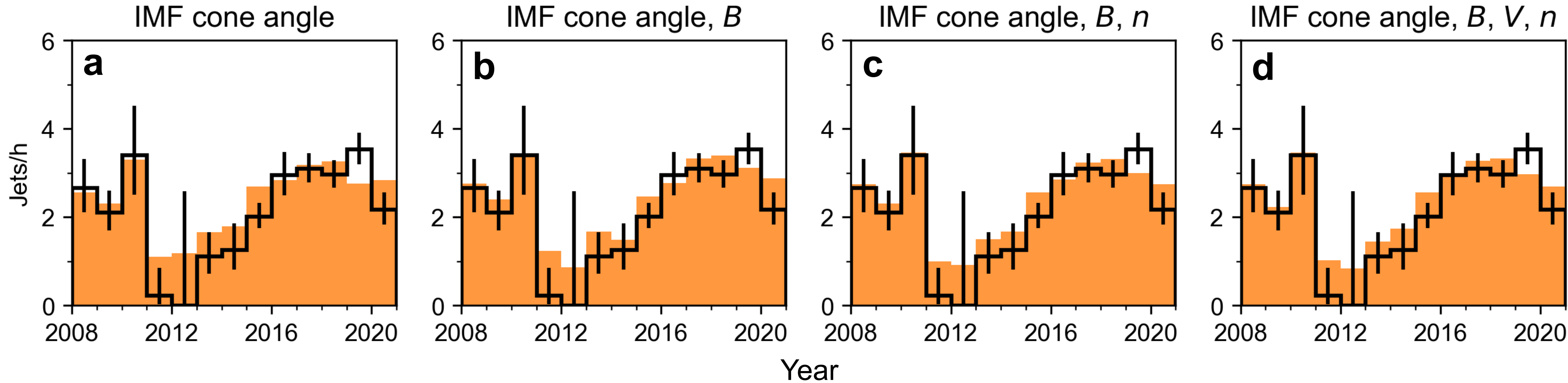
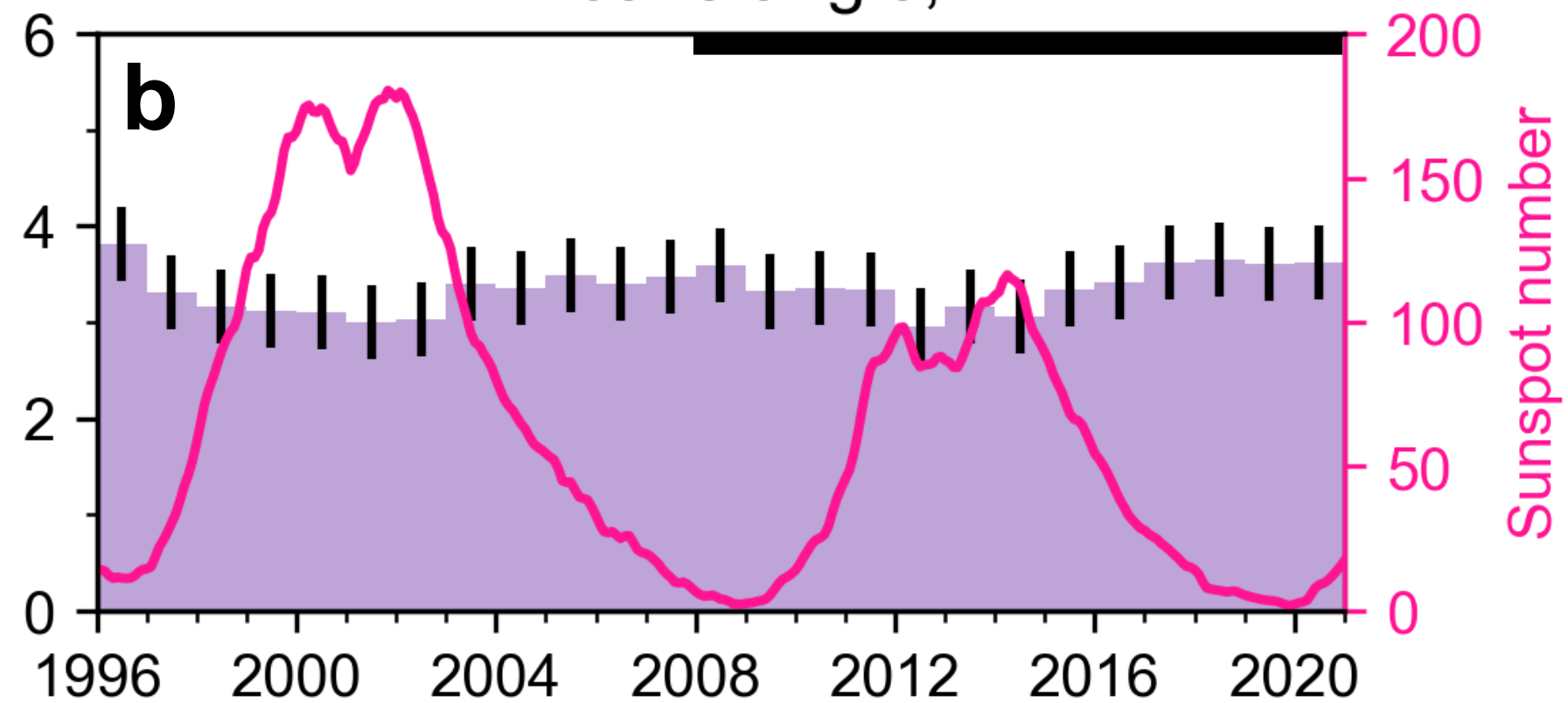
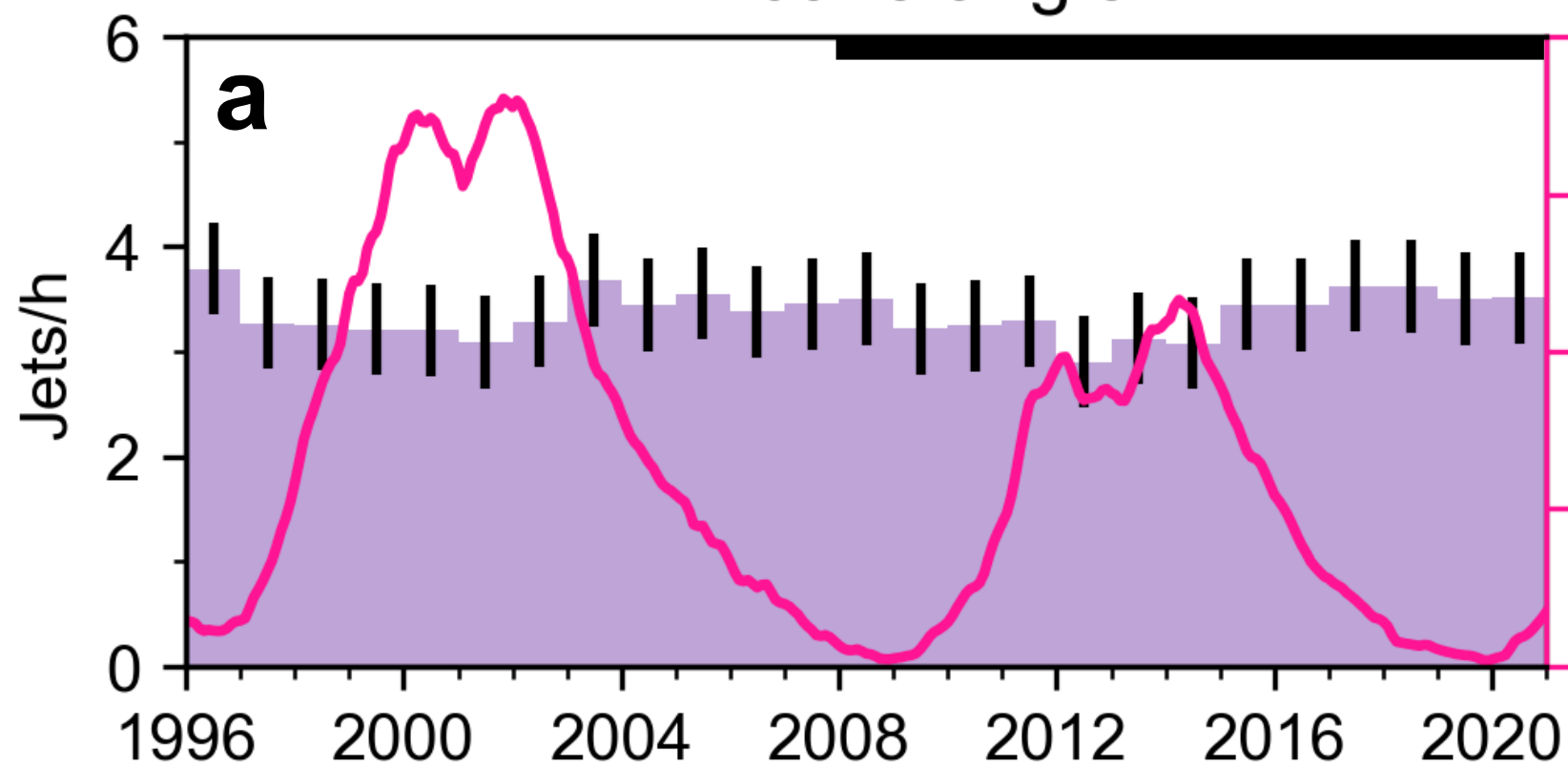


Figure 8.

Estimations for the solar cycle 23–24 OMNI data

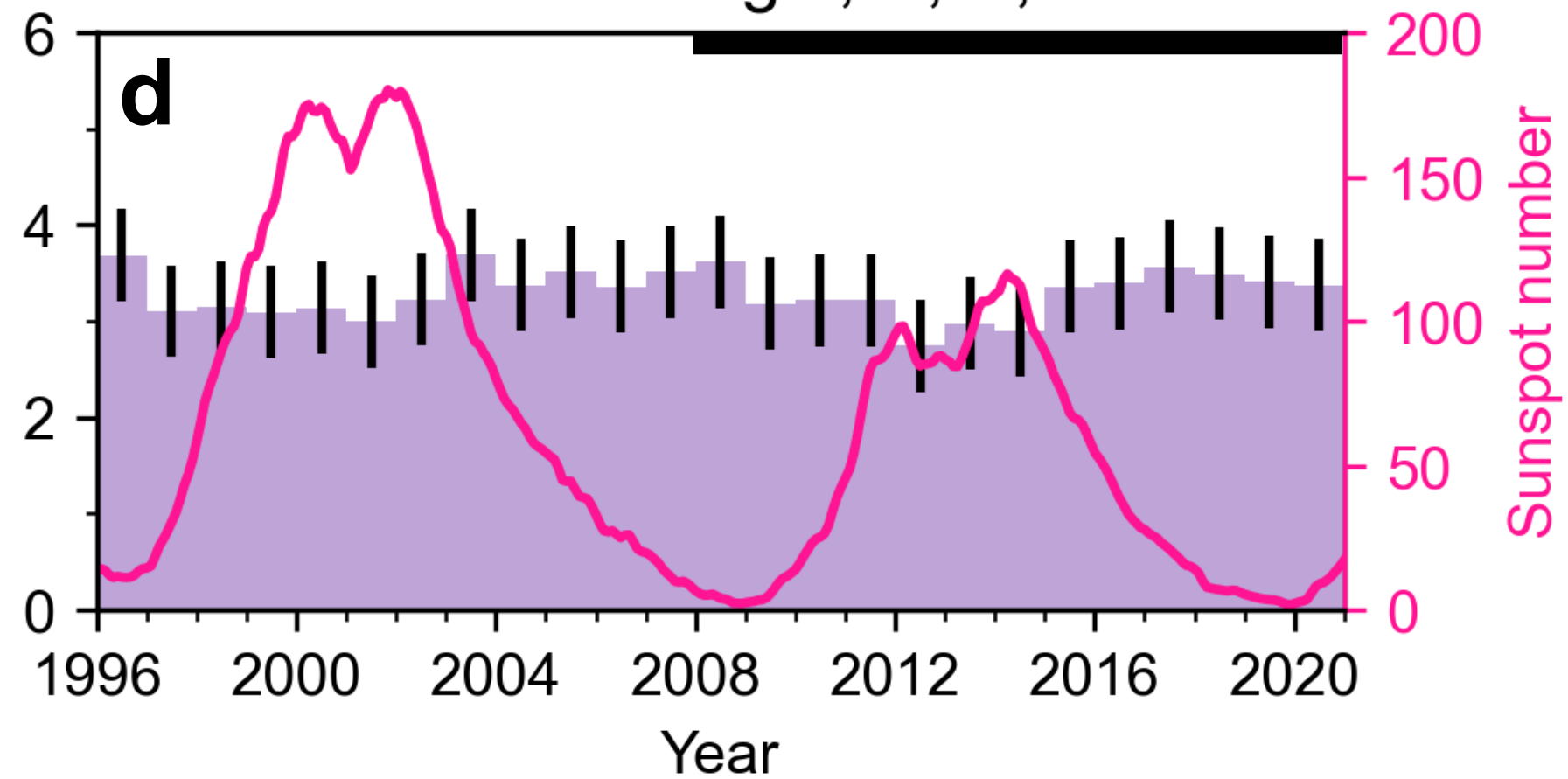
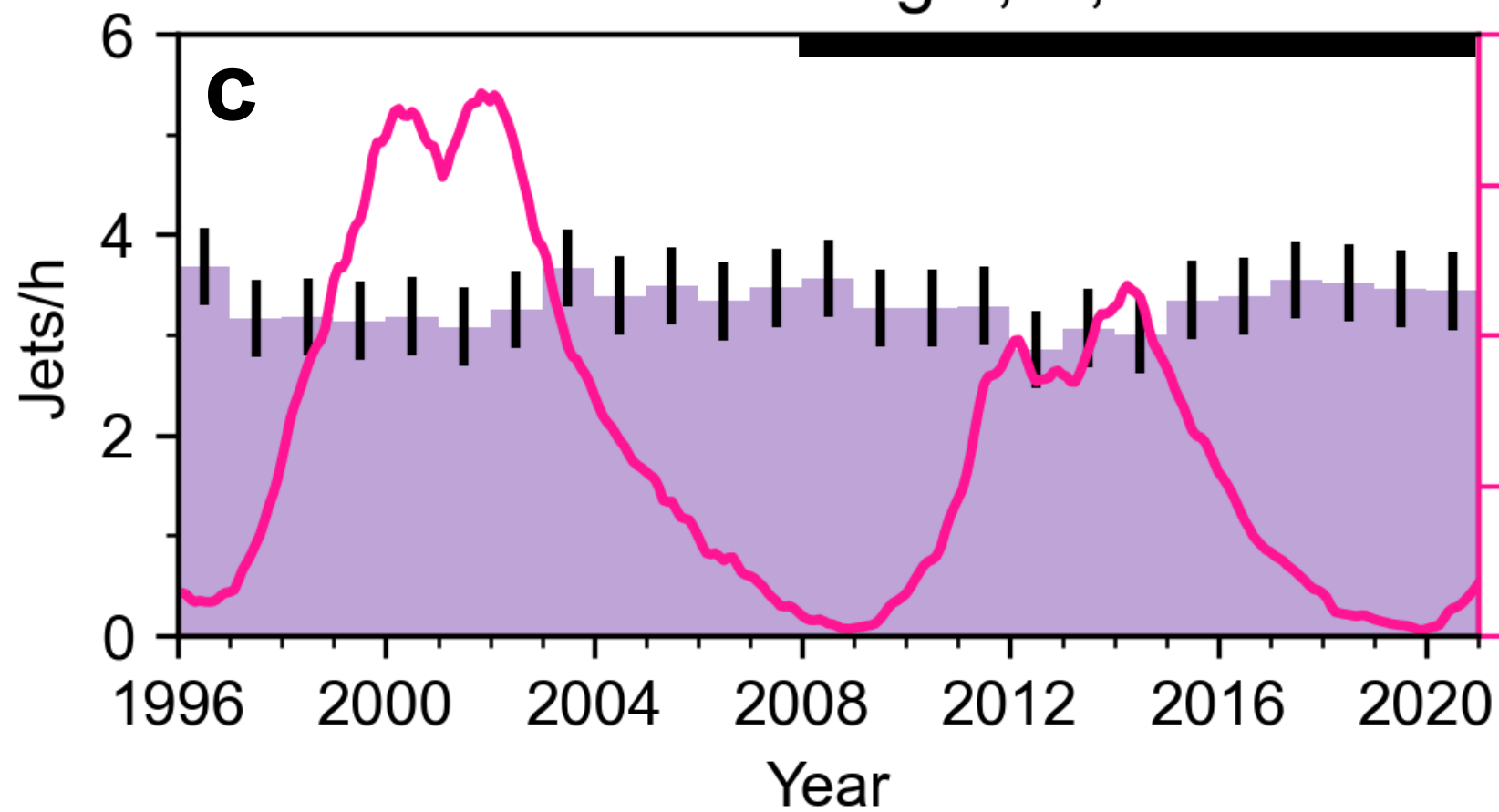
IMF cone angle

IMF cone angle, B



IMF cone angle, B, n

IMF cone angle, B, V, n



reconstructed for the solar cycles

NOAA sunspot number