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A neural network model for the evolution of learning in changing environments

Magdalena Kozielska[1*] and Franz J. Weissing[1†]

Affiliations:

[1] Groningen Institute for Evolutionary Life Sciences, University of Groningen, Groningen, The Netherlands

* m.a.kozielska@rug.nl

† f.j.weissing@rug.nl

Abstract

The ability to learn from past experience is an important adaptation, but how natural selection shapes learning is not well understood. Here, we present a novel way of modelling learning using small neural networks and a simple, biology-inspired learning algorithm. Learning affects only part of the network, and it is governed by the difference between expectations and reality. We used this model to study the evolution of learning under various environmental conditions and different scenarios for the trade-off between exploration (learning) and exploitation (foraging). Efficient learning regularly evolved in our individual-based simulations. However, in line with previous studies, the evolution of learning was less likely in relatively constant environments (where genetic adaptation alone can lead to efficient foraging) or in the case of short-lived organisms (that cannot afford to spend much of their lifetime on exploration). Once learning did evolve, the characteristics of the learning strategy (the duration of the learning period and the learning rate) and the average performance after learning were surprisingly little affected by the frequency and/or magnitude of environmental change. In contrast, an organism's lifespan and the distribution of resources in the environment had a strong effect on the evolved learning strategy. Interestingly, a longer learning period did not always lead to better performance, indicating that the evolved neural networks differ in the effectiveness of learning. Overall, however, we showed that a biologically inspired, yet relatively simple, learning mechanism can evolve to lead to an efficient adaptation in a changing environment.

Author Summary

The ability to learn from experience is an important adaptation. However, it is still unclear how learning is shaped by natural selection. Here, we present a novel way of modelling the evolution of learning using small neural networks and a simple, biology-inspired learning mechanism. Computer simulations reveal that efficient learning readily evolves in this model. However, the evolution of learning is less likely in relatively constant environments (where evolved inborn preferences can guide animal behaviour) and in short-lived organisms (that cannot afford to spend much of their lifetime on learning). If learning does

38 evolve, the evolved learning strategy is strongly affected by the lifespan and environmental richness but

39 surprisingly little by the rate and degree of environmental change. In summary, we show that a simple

40 and biologically plausible mechanism can help understand the evolution of learning and the structure of

41 the evolved learning strategies.

42

Introduction

44 Learning can be defined as a change in the nervous system manifested as altered behaviour due to

45 experience [1]. The ability to learn is widespread in the animal kingdom as it is an important adaptation

46 to life in complex environments [2–5]. Learning has been studied extensively in different fields, like

47 psychology, ethology, neurobiology, and more recently artificial intelligence. A number of theoretical

48 studies have been conducted in order to understand the evolution of learning but many questions still

49 remind unanswered [6].

50 The limited progress may be related to the fact that only a few evolution-oriented theoretical studies

51 considered that experience-based changes in behaviour are achieved via changes in neural networks.

52 Many studies take a behavioural-gambit approach [7], assuming that mechanisms do not matter and that

53 evolution will always shape learning in such a way that the outcome is optimal. Modelling studies that

54 do take mechanisms into consideration, typically focus on the evolution of simple learning rules that are

55 determined by a small number of parameters (e.g. [8–13] but see [14]). It is difficult to imagine how

56 such rules could emerge via the evolution of brain plasticity.

57 In contrast, machine learning and artificial intelligence deal with complex neural networks capable of

58 learning. However, the proposed learning mechanisms often rely on complicated algorithms, such as

59 backpropagation, which affect all connections in the network [15,16]. Such techniques are very efficient

60 in machine learning applications but are far removed from biological reality [17]. Additionally, when

61 evolutionary considerations are included, they are usually limited to network optimisation instead of

62 asking evolutionary questions (but see [18,19]). Mutation and selection are usually viewed as useful

63 tools that can be freely designed to achieve a computationally efficient outcome and often unrealistic

64 assumptions are made about the way how natural selection works [20–22].

65   Here, we take a first step toward filling the gap between these two approaches. We study the evolution

66   of neural networks that are capable of learning via a simple but plausible mechanism. In our model,

67   neural networks can change over the generations through evolution by natural selection, but also through

68   learning within the lifetime of an individual. Experience-induced changes in the network are localized

69   and affect only a small number of neural connections – an approach inspired by "reservoir computing"

70   [23,24]. The learning mechanism is based on prediction error, the difference between an animal's

71   expectation and observed reality. Such a mechanism is biologically plausible, as prediction errors are

72   signalled by the neurotransmitter dopamine, which is ascribed an important role in learning [25,26].

73   Learning algorithms based on error prediction have also been successfully implemented in machine

74   learning applications [23]. To our knowledge, this is the first time that such a biology-inspired local

75   learning mechanism is implemented in a study on the evolution of learning. Yet, we would like to stress

76   that it is not our goal to build a realistic model of a brain. Rather, we view our model as a conceptual

77   tool to explore how the addition of mechanistic detail affects the evolution of learning.

78   Learning theory predicts that the degree of environmental change affects the adaptive value of learning

79   and therefore the probability that learning evolves [6]. Generally speaking, learning is expected to be

80   most advantageous for moderate rates of environmental change [27]. If there is little or no change,

81   genetic control of behaviour should evolve. Learning is also not profitable if the change is too frequent

82   because information on the environment gets outdated too fast. We therefore study the evolution of

83   neural networks and their learning mechanisms in different regimes of frequency and magnitude of

84   environmental change, as it allows us to investigate whether a more mechanistic implementation of

85   learning is in line with the predictions of "mechanism-free" theory.

86   We also touch upon a rarely studied aspect of learning theory – the effect of lifespan on the evolution

87   of learning. As far as we know there are only two studies addressing this question [28,29]. These models

88   are vastly different from each other in assumptions and ecological context and lead to different

89   predictions on whether the investment in learning should be highest for shorter or longer lifespans. To

90   add to this limited body of knowledge, we also study how different lifespans affect the evolution of

91   learning and the evolved learning strategy.

92 Our simulation study addresses the following research questions: Under which environmental conditions

93 does learning evolve? What is the evolved learning strategy and how efficient is it? What is the effect

94 of lifespan on the evolved learning strategy?

95

Methods

96

Model overview

97

98 We used individual-based simulations to study the evolution of simple neural networks that are able to

99 adapt to changing environment by learning.

100 In our model, individuals harbour a neural network that guides their foraging decisions. Individuals have

101 a fixed lifetime of a given number of timesteps. At the start of their life, they can spend a number of

102 timesteps on learning. During this learning period, they gather information about the quality (energy

103 content) of food items in their environment, and they use this information to adjust their neural network.

104 After the learning period, individuals switch to foraging, when they use their network to assess the

105 available foraging options. They choose the food item their neural network finds the most profitable,

106 consume it and gain energy equal to its quality. The more energy their gather during the whole foraging

107 phase, the more offspring they have. There is a trade-off between exploration and exploitation: the

108 longer the learning ('exploration') period, the shorter the foraging ('exploitation') period, but potentially

109 the higher the efficacy with which the foraging period is used.

110 Offspring inherit their neural network and their learning strategy (the duration of the learning period and

111 the learning rate) from their parents, subject to rare mutations. Environmental conditions can change

112 between generations, making learning a potentially adaptive strategy.

113

Neural networks

114

115 Each individual possesses a neural network that is used to predict the quality of food items on the basis

116 of environment-specific cues.

5

117   We consider relatively simple neural networks consisting of 10 neuron-like nodes (Fig 1). In a pilot

118   study, we also considered more complex networks, but the network considered here performed almost

119   as well as more complex networks while being faster. Our network receives a cue C as input and it

120   produces an output $Q_p(C)$ that can be interpreted as the predicted quality of a food item emitting that

121   cue. The networks consist of nodes (the circles in Fig 1) that are organized in a sequence of layers. Each

122   node is connected to one or several nodes in the subsequent layer (the arrows in Fig 1), and it can

123   stimulate or inhibit the activities of these nodes.

124

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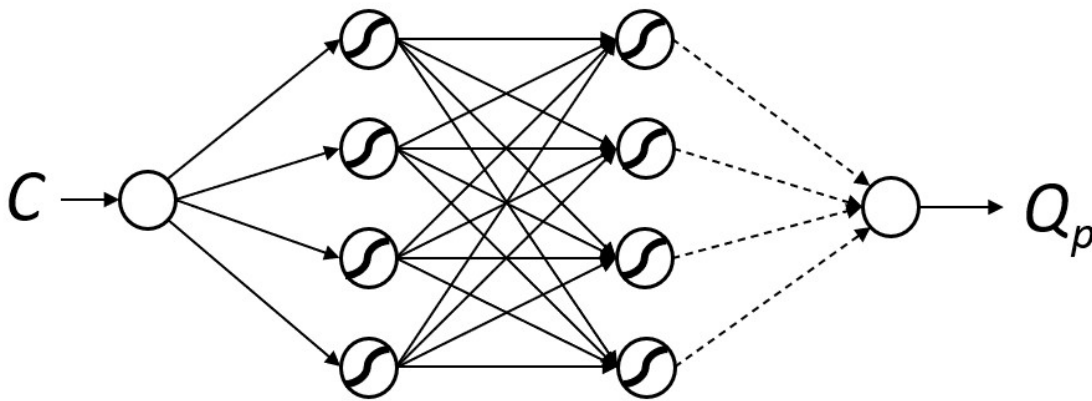
126   **Fig 1. The neural network used in this study.** Our network receives a cue C as input and it produces

127   an output Q_p that is the predicted quality of a food item emitting that cue. In this model we use a network

128   with one input and one output (C and Q_p, respectively) and two hidden layers, each with four nodes.

129   Arrows indicate the information flow in the network. Solid arrows represent genetically hardwired

130   connection that do not change during learning. Dashed arrows represent the weights that are genetically

131   determined but can also change during learning (see text for more details).

132

133   Each connection has a certain strength - weight w, where a positive value of w represents stimulation,

134   while a negative value corresponds to inhibition. The input node receives the cue value C which is a real

135   number. This value is processed and determines the node activities at the subsequent level. More

136   precisely, the activity y_i of node i in each layer is given by an expression of the form

137
$$y_i = A\left(\sum_j w_{ij} x_j + b_i\right). \qquad (1)$$

138 Here j runs over all nodes of the previous layer that are connected to i, x_j is the activity of node j, and

139 w_{ij} is the strength of the connection between nodes j and i. b_i is the baseline activation of node i.

140 Function A is a so-called "activation function." Such functions can be useful, as they allow for more

141 versatile input-output relationships of neural networks and because they can ensure that the activity

142 levels y_i are restricted to a certain range (such as the interval [0,1]) [30]. A preliminary test showed that

143 the results are not strongly affected by the applied activation function. In this paper, we used the

144 "clamped ReLU" function that is fast and returns 0 if given values lower than 0, and 1 for the values

145 larger than 1. For values between 0 and 1, it returns these values without transformation. No activation

146 function was used for the output node.

147 We assumed that the network architecture does not change throughout the simulation and that all the

148 network parameters w_{ij} and b_i are heritable and transmitted from parents to offspring (subject to

149 mutation, see below). Therefore, the strength of connections between the nodes and the baseline node

150 activations can change in the process of evolution. Additionally, some weights can change during the

151 individual's lifetime via learning.

152

153 Learning

154 Four weights of the network connected to the output node (dashed arrows in Fig 1) can be modified via

155 learning during the individual's lifetime.

156 Different methods for network learning are used in artificial intelligence applications. Many of them

157 implement relatively complex algorithms that change all (or most) weights of the network based on

158 global information (e.g. error backpropagation) and are therefore unrealistic from the biological point

159 of view. As far as we know, there is no experimental data supporting such learning happening in the

160 brain. Additionally, at the initial stages of the evolution of learning a simple learning algorithm is more

161 likely to evolve from scratch.

162   Therefore, we decided to use a simple learning method, inspired by reservoir computing [23,24], that

163   assumes that learning is more localised in the brain and that it only leads to changes in weights of the

164   last layer, i.e. weights that directly influence the output of the network. These changes are governed by

165   the so-called "Delta Rule" that has proven to be effective in reservoir computing and other machine

166   learning applications [23]. It uses the difference between the current network output (prediction) and the

167   feedback received from the environment as a teaching signal. Interestingly, local dopamine

168   concentrations in the brain may signal such prediction error [25,26,31] and prediction-error-based

169   learning is a well-known phenomenon in animal psychology research [32].

170   Therefore, the changes in weights of the last layer (connected to the output node; dashed arrows in Fig

171   1) after one round of learning are given by the 'Delta Rule' [30]:

172 $$\Delta w_{ij} = L(Q - Q_p)x_j, \qquad (2)$$

173   where Δw_{ij} is the change in the weight connecting node j in the preceding layer to the output node i; Q

174   is the actual quality of the food item; Q_p is the quality predicted by the network before the weights are

175   updated; L is the learning rate (a heritable parameter), and x_j is the activation level of node j.

176   It should be noted that the values of the modified weights are not passed to the offspring, but only the

177   genes specifying the weights' values at the beginning of life.

178

Environment

180   Individuals live in an environment that contains food items of different quality. Food items can be

181   distinguished on the basis of their properties (like colour or smell) that we will call 'cues'. For simplicity,

182   we assume that the cues can be arranged on a circle or, equivalently, on the 'wrapped' interval [-1,1],

183   where -1 corresponds to +1. The energetic quality Q of a food item emitting cue C is given by a Gaussian

184   function (see Figure 2):

185 $$Q(C) = \exp\left(-\tfrac{1}{2} \cdot \left(\frac{C - P}{\sigma}\right)^2\right) \qquad (3)$$

186   where P is the location of the peak of the Gaussian while σ describes the width of the function. In our

187   simulations, the peak was initially located at zero. As a default, we used σ = 0.25, but other values were

188   also tested.

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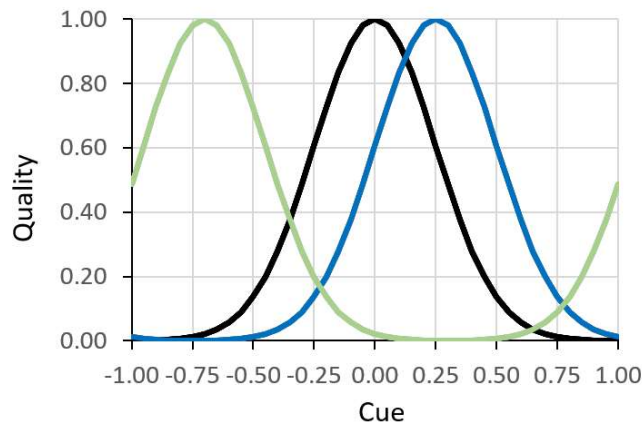
190   **Fig 2. Three Gaussian functions with σ = 0.25 illustrating the relationship between food cues and**

191   **food quality at three different points in time**. The peak of the quality function can shift, indicating a

192   change in the environment.

193

194   We assume that the environment can change over the generations, in the sense that the quality associated

195   with specific cues may change. We model this by shifting the whole quality function randomly to the

196   left or to the right. As mentioned above, we wrapped the quality function in order to assure that the total

197   amount of resources in every generation is the same (see Fig 2).

198   In order to study the effect of environmental change on the evolution of learning, we considered (a)

199   different frequencies of environmental change (f) – we present results for the values f = {1, 0.1, 0.01},

200   corresponding to a change every 1, 10 and 100 generations, respectively; and (b) different magnitudes

201   of environmental change (m) – how much the peak of the quality distribution shifts (left or right) when

202   the environment changes. Throughout the simulations we used values m = {0.1, 0.25, 0.4}. Each time

203   the peak moved, a small error term (with a coefficient of variation of 5%) was added to m to prevent

204   that only finitely many peak locations would be experienced in the course of evolution.

205

Life history

The lifespan of each individual is divided into a fixed number of discrete timesteps. We focus on a lifespan of 500 timesteps but later also briefly discuss the effect of shorter lifespan on the outcome of evolution. The first part of life is spent on learning; the duration of the learning period is either a fixed parameter or a heritable property. The second part of life is spent on foraging, where previous learning can potentially improve the ability to choose food items of better quality. At the end of their life, individuals reproduce and then die.

Learning period

In each timestep of the learning period, each individual explores one food item: it gets one randomly chosen cue, predicts the food quality associated with that cue (using its current neural network), is informed about the true food quality of the corresponding food item, and updates its network accordingly (see above). Once the learning period is finished, the network resulting from the succession of learning steps is used to guide the individual's decisions in the foraging phase. To reduce one source of randomness from our simulations, all individuals in the population were presented with the same sequence of random cues during the learning period.

Foraging period

In each timestep of the foraging period, each individual is presented with n food items (n was set to 5 in all simulations). Based on the food properties (cues) an individual has to decide which item to consume. To this end, the individual uses its neural network (that is partly inherited and partly adjusted by learning) to predict the quality of the food items presented. Subsequently, it consumes the item it predicted to be the best, gaining energy equal to the food item's true quality. In the next timestep, a new set of food items is presented, etc. Again, we reduced the randomness by presenting the same sets of food items to all individuals in the population.

Reproduction

Individuals reproduce after the foraging period. The expected reproductive success of an individual is proportional to the total amount of energy the individual gathered during its entire foraging period. For

232   each of the N individuals of the offspring generation, a parent is drawn at random (with replacement);

233   the probability that a given individual is drawn as a parent is proportional to the individual's total energy

234   gained. The offspring inherits all network parameters, learning rate and the number of learning episodes

235   from its parent. With per-locus mutation probability $\mu = 0.01$, a parental allele is affected by a mutation.

236   When for a given locus a mutation occurs, a small number ε is added to the parental value. For weights,

237   biases and learning rate the mutational step size ε is drawn from a normal distribution with mean 0 and

238   standard deviation 0.1. In case of the number of learning episodes (which is a non-negative whole

239   number), a mutation either leads to the increase or to the decrease by one unit, both with equal

240   probability. The offspring population replaces the parental population and the new generation starts.

241

Simulation setup

243   In our simulations, we consider a population of $N = 1000$ haploid individuals and discrete, non-

244   overlapping generations. Each individual harbours genes that encode the (initial) connection weights

245   and biases of its neural network (in total 33 values), the learning rate (L in equation 2) and the number

246   of learning episodes. Weights and biases can take any real value, the learning rate can be any non-

247   negative real number and the length of the learning period is an integer in the range [0, lifespan].

248   Each simulation started with a population consisting of individuals with random parameter values. Initial

249   weights and biases were drawn from a uniform distribution U(-1,1) and the learning rate from the

250   uniform distribution U(0,1). The number of initial learning episodes was set to a specific value

251   depending on the type of simulation (see Results).

252   Most simulations were run for 50 thousand generations, but evolutionary equilibrium (judged by the

253   population average of the amount of gathered energy) was usually reached in a much shorter time.

254

Results

256   We present our results in three sections. In the first section, the duration of the learning period is fixed.

257   This removes the exploration-exploitation trade-off and allows us to focus on the evolution of the

258   network and the learning mechanism. In the second section, we investigate the joint evolution of the

259   network and the duration of the learning period in order to study the trade-off between exploration and

260   exploitation. In the first two sections, we focus on organisms with a lifespan of 500 time units and an

261   intermediate width of the environmental quality distribution (σ=0.25). In the last section, we study how

262   the evolutionary outcome is affected by changes to these parameters.

263

## Fixed duration of the learning period

265   As a first step, we fixed the number of learning episodes (LE) to different values. For simplicity, we

266   present the results for a lifespan of 500, but the same pattern is seen for other lifespans, as long as the

267   absolute number of learning episodes is the same.

268   One of the most important measures for the performance of a network is its ability to choose a high-

269   quality food item among the available options. We calculated the relative performance ("performance"

270   in brief) of a network within a given choice situation by dividing the energy content of the food item

271   chosen by the energy content of the highest-quality food item on offer. Therefore, performance equals

272   one if during the foraging period an individual always chooses optimally, and it is smaller than one

273   otherwise. All other things being equal, a higher performance leads to higher fitness, which in our model

274   is proportional to the "lifetime energy gain", that is, to the sum of the energy of all food items collected

275   throughout the lifetime. When, however, the learning periods differ, a higher performance does not

276   necessarily result in a higher lifetime energy gain. If the higher performance is associated with a longer

277   learning period and, hence, a shorter foraging time it may not offset the time "lost".

278   Fig 3 shows how, for a given duration of the learning period, the performance and the lifetime energy

279   gain of the evolved learning networks are affected by the frequency and magnitude of environmental

280   change. As a benchmark, consider first the absence of learning (LE = 0; red dots and lines). For the

281   environmental quality distribution considered here (σ=0.25), a randomly choosing individual would

282   achieve a performance of about 0.41. Even without learning, the networks typically perform better than

283   this, because they adapt genetically to the pattern of environmental change. Such "adaptive tracking"

284   [33] can lead to a high network performance if the environmental change is rare and/or if the magnitude

12

285 of environmental change is small. In the case of f=0.01 (change once every 100 generations) and m=0.1

286 (small magnitude of change), the non-learning networks achieve practically the same high performance

287 as the networks that were allowed to learn. In this case, the non-learning networks even have a fitness

288 advantage (a higher lifetime energy gain), as they do not lose foraging time. On the other hand, if f=1

289 (change every generation) and m=0.4 (large magnitude of change), the genetic mechanism cannot

290 adaptively track the environmental changes, and the networks do not perform better than 0.41, the

291 performance of a random-choice mechanism.

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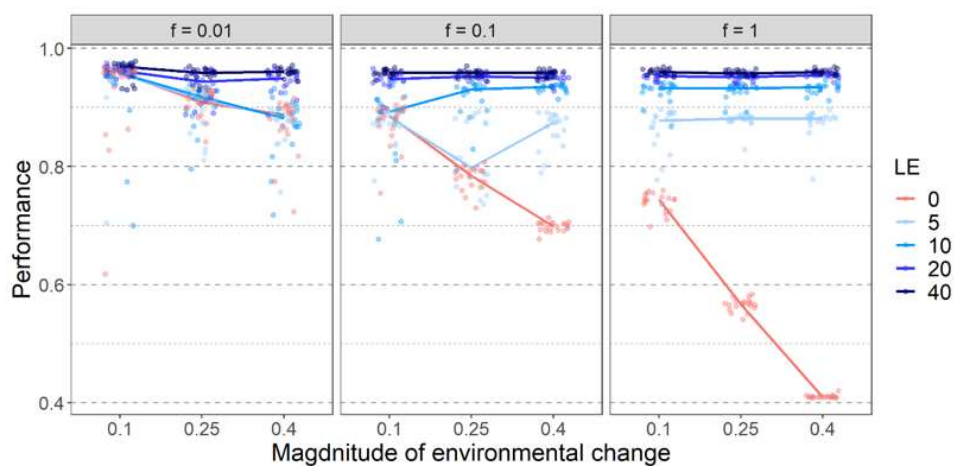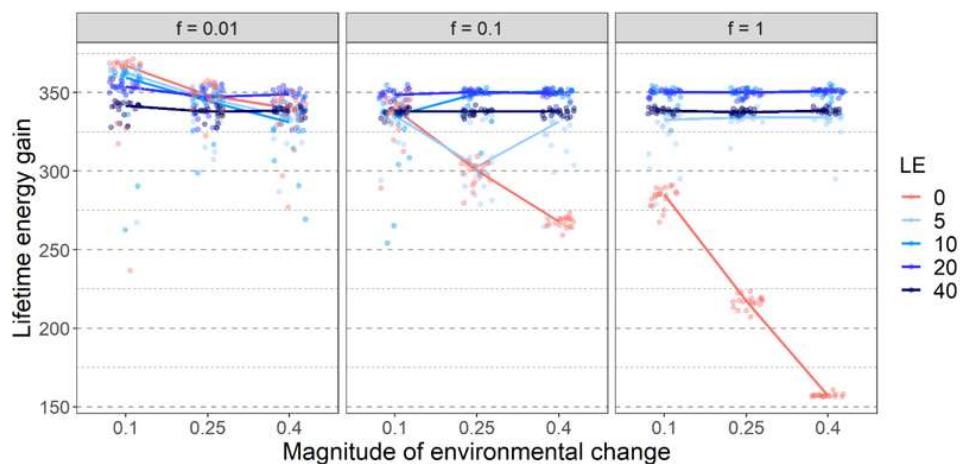
Fig 3. Effect of a fixed number of learning episodes (LE) on (A) evolved network performance and (B) lifetime energy gain in different environmental regimes. Panels in different columns corresponds to a different frequency of environmental change f, ranging from 0.01 (a change once every 100

296   generations) to 1.0 (a change every generation). The *x*-axis of each panel represents the magnitude of

297   environmental change: the distance that the environmental quality peak moves when change occurs. 20

298   replicate simulations were run for each parameter combination (in all cases, lifespan = 500). Each

299   replicate is represented by a coloured point, which corresponds to the population mean of this replicate,

300   averaged over the last 2000 generations. The lines connect the median values of 20 replicates for

301   different parameter settings. As expected, performance tends to increase with the number of learning

302   episodes. However, the total amount of resources gained tends to be highest for an intermediate number

303   of learning episodes, because a longer learning period reduces the time left for foraging.

304

305   As expected, when learning is present, a longer learning period has a positive effect on network

306   performance (Fig 3A). In general, performance increases with the number of learning episodes, but

307   levels off from a certain point onward. In other words, the returns from adding more learning episodes

308   diminish and eventually they become negligible. Therefore, the foraging time lost to longer learning can

309   to some extent be compensated by improved performance, but there is a limit to that. Accordingly,

310   fitness (lifetime energy gain) is typically maximized for an intermediate number of learning periods (Fig

311   3B).

312   Fig 4 shows the temporal dynamics in more detail, for a scenario where the environment changes every

313   ten generations. Without learning (LE=0), performance drops every time when environmental change

314   happens and subsequently recovers (due to the genetic evolution of the network) to its former value.

315   Learning reduces the drop in performance considerably, especially if the learning period is long

316   (LE=20).

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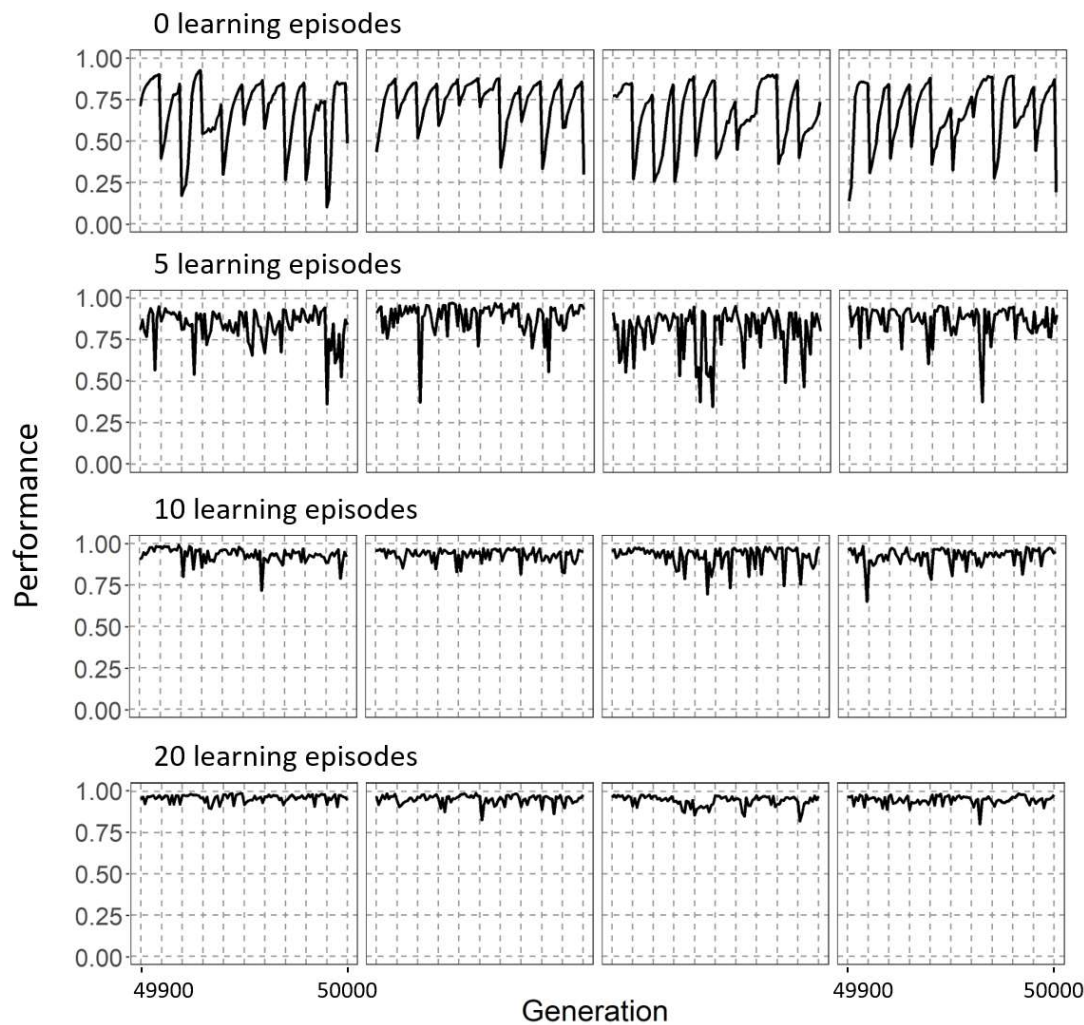
Fig 4. The time course of network performance in a changing environment. The panels show the time course of average population performance over the last 100 generations of simulations with an environmental change rate f=0.1 (change once every 10 generations) and magnitude m=0.4. For four values of the number of learning episodes (LE = 0, 5, 10, 20) four randomly chosen replicate simulations are shown. In the absence of learning (LE = 0), the population performance clearly drops to low levels every time the environment changes (indicated by vertical dashed lines). With an increasing number of learning episodes, the drops in performance are smaller, and performance is better throughout the simulation.

Quite generally, learning strongly improves the match between the real environmental quality and the one predicted by individuals if the environment changes frequently and/or if the magnitude of change is large. This is exemplified in Fig 5 which shows prediction profiles for networks evolved for different

15

330   durations of the learning period. When there is no learning and the environment changed, the prediction

331   profile does not match the real quality associated with different cues. With learning, the innate quality

332   prediction can be relatively poor, as it is considerably improved by learning. Even though the predicted

333   quality after learning does not perfectly match the real environmental quality for all cues, individuals

334   perform quite well, as they only need to assess the relative quality associated with the five cues available

335   during one foraging episode and to find the one that is linked with the highest energy level.

336   Conversely, if environmental change happens less frequently or is smaller in magnitude, even though

337   individuals spent time learning they are not necessarily efficient at it and a considerable number of

338   learning episodes is needed to reach an improvement in performance (Fig 3A and Fig A in S1 Appendix).

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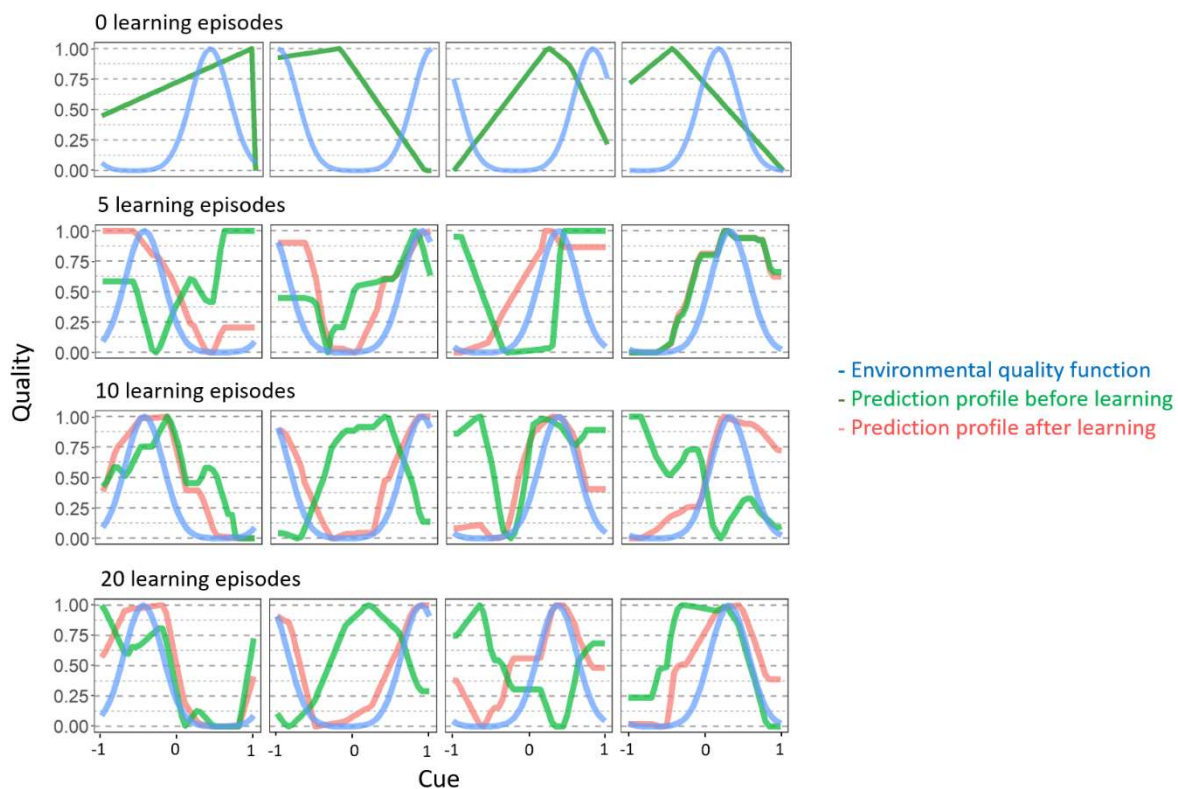
340   **Figure 5. Prediction profiles of networks evolved for different durations of the learning period.**

341   For each of the 16 populations presented in Fig 4, one network was chosen at random at the end of the

342   simulation (when the environment had just changed) and was investigated in more detail. The plots show

343   the environmental quality function (blue), the prediction profile (i.e., the quality predicted for each

344   possible cue) of the network before learning had started (green) and at the end of the learning period

345   (red). For longer learning periods, the "learned" prediction profiles (red curve) match the "true"

346   environment quality profile (blue curve) reasonably well, even though the "innate" prediction profile

347   (green curve) is way off target. Parameter settings as in Fig. 4 (*f*=0.1, *m*=0.4).
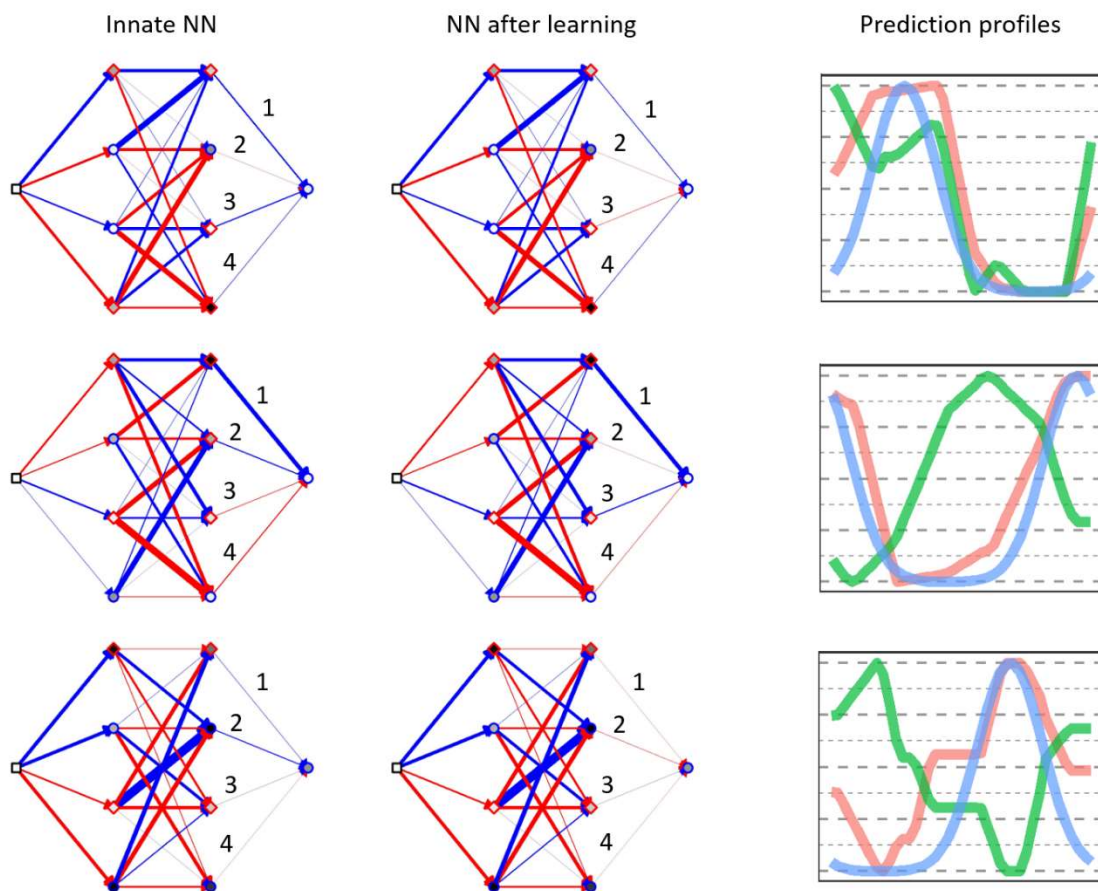
348

349   Examples of the evolved neural networks and the effect of learning on the weights can be seen in Fig 6.

350   In different replicates, different networks evolved, but within a replicate variability between individuals

351   was low.

352

353   **Fig 6. Examples of evolved neural networks and their prediction profiles before and after learning.**

354   Networks from three different replicates from simulations with LE = 20 are shown (three of the four

355   individuals shown in Fig 5). Blue arrows correspond to excitatory connections (positive weights) and

356   red to inhibitory connections (negative weights) The thickness of the lines is proportional to the strength

357   of the connection. The baseline activation of each node is represented by circles with a blue edge for

358   positive values and by diamonds with a red edge for negative values. The absolute strength of the

359   baseline activation is given by the inner shading of the symbol, the darker the colour the larger the value.

17

360   During learning only the four numbered weights can change. For example, for the network in the centre,

361   two weights changed the strength and the type of connection (from excitatory to inhibitory - weight 2;

362   and the other way round – weight 3) and weight 4 weakened in strength. Such relatively small changes

363   to the network lead to a drastic change in the prediction profile (right column, plotting convention as in

364   Fig 5). Note that the four "learning weights" of the networks tend to have smaller absolute weight values

365   (thinner lines) than other weights. This was a common pattern for networks that evolved efficient

366   learning (Fig C in S1 Appendix).

367

368   We also looked at the evolved learning rate. In environmental settings in which learning increases

369   performance (i.e., when environmental change is frequent and/or of large magnitude), the learning rate

370   tends to slightly decrease with the increasing learning period (Fig B in S1 Appendix). In other words,

371   when the learning period is brief, learning tends to take place in larger strides, while it tends to take

372   place in smaller steps when there is much time for learning.

373

Evolution of the duration of the learning period

375   From now on, we assume that the duration of the learning period coevolves with the learning rate and

376   the properties of the network. Accordingly, the evolutionary outcome reflects the exploration-

377   exploitation trade-off: the system should evolve to a state in which the time spent learning (and lost for

378   foraging) is compensated by the better choices made during foraging. There is, however, a start-up

379   problem. When a simulation starts with a random network, the learning period may evolve toward zero

380   (as learning does not provide any benefit at the early stage of network evolution). Once the learning

381   period is around zero, and the selection for learning is weak, the evolution of the optimal number of

382   learning episodes is hampered. To overcome this problem, we started each simulation with a fixed

383   number of learning episodes (LE = 20) and let the network and the learning rate evolve for 10K

384   generations. After this initial period, the number of learning episodes became subject to mutations and

385   could therefore start to evolve as well for further 50K generations.

386   Fig 7 shows that learning persists in the population under a broad range of environmental conditions,

387   leading to greatly increased performance and fitness (compared to a population with no learning; Fig

388   7A). This shows again that the time spent learning can be compensated by the better choices made in

389   the foraging phase. In other words, the benefits of learning often outweigh the costs in terms of a

390   shortened foraging time.
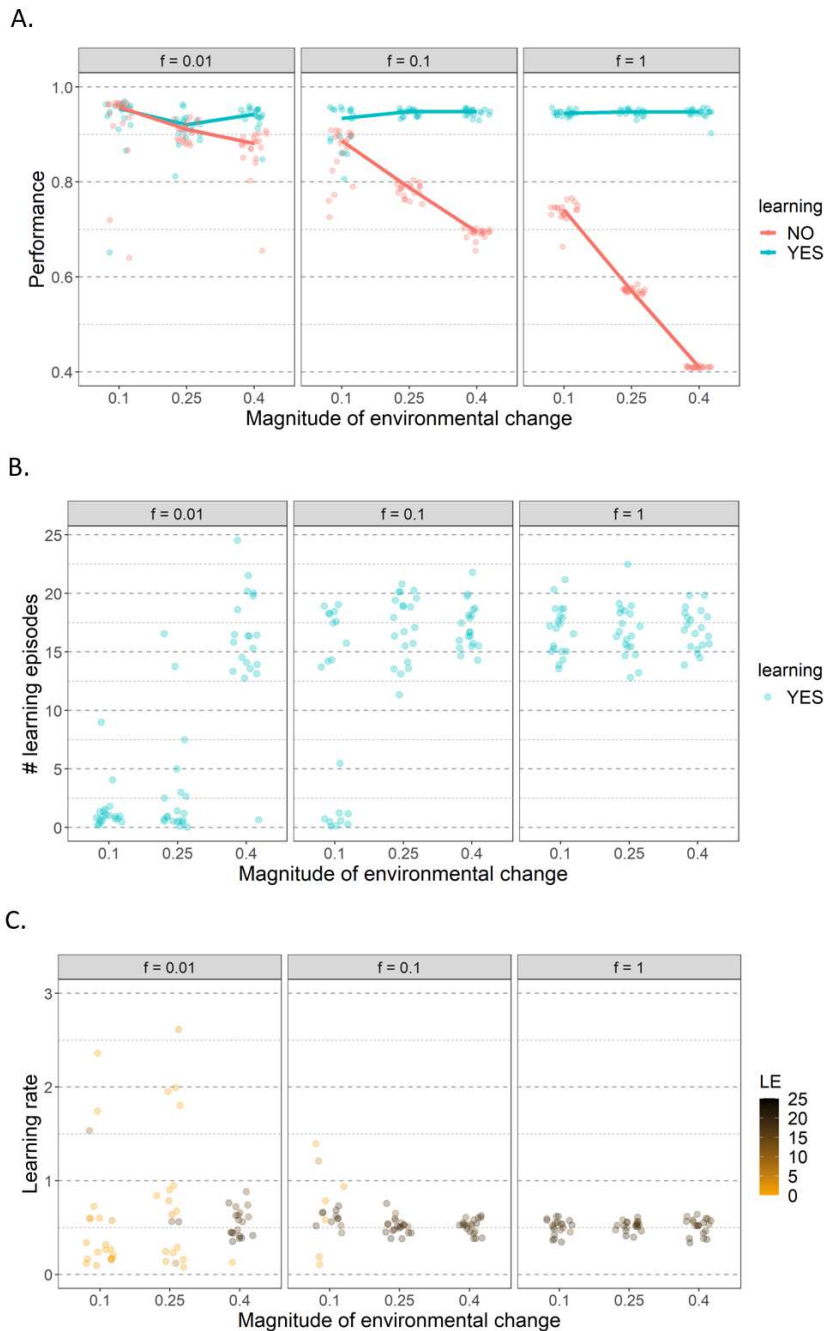
391   **Fig 7. The joint evolution of (A) network performance, (B) duration of the learning period, and**

392   **(C) learning rate for various environmental scenarios.** Parameter settings and graphical conventions

19

393   are as in Fig. 3. In (A), the performance of the evolved networks in the simulations in which learning

394   was allowed to evolve is shown in turquoise. For comparison, the simulations in Fig. 3A where learning

395   was not allowed to evolve (LE=0) are also shown (in red). (B) shows the evolved number of learning

396   episodes. Notice that LE often evolves toward zero (i.e., learning disappears in the course of evolution)

397   when the magnitude of change is small and environmental change is infrequent. (C) shows the evolved

398   learning rates – different colours indicate the association between the evolved learning rate and the

399   evolved duration of the learning period in the replicate simulations. Notice that the evolved learning rate

400   is close to 0.5 in all simulations where learning evolved (LE > 10). When learning disappeared in the

401   course of evolution (LE < 5), the learning rate is no longer under strong selection and can take on many

402   different values (three data points with LE < 5 are not visible, as the learning rate exceeds 3).

403

404   Whether learning evolves can be to a large extent predicted from the results of the previous section. Fig

405   3 shows what number of learning episodes (among the ones tested) lead to the highest gain in resources,

406   and, hence fitness. For example, when the environment changes every generation the simulations with

407   learning episodes of 10 and 20 obtained the highest energy. When we let the number of learning episodes

408   evolve it reaches a median value of around 17 (Fig 7B). On the other hand, when a small change of 0.1

409   happens every 100 generations, then the highest energy gain was obtained in simulations with no

410   learning. In line with this, the number of learning episodes converges to zero, corresponding to the loss

411   of learning from the population.

412   Smaller and less frequent environmental changes reduce the likelihood that learning is maintained.

413   Interestingly, when learning evolves, the number of learning episodes, network performance, and

414   network fitness are practically independent of the magnitude or frequency of environmental change (Fig

415   7). This seems to be due to the fact that when effective learning evolves, the networks do not track

416   environmental change genetically but fully rely on learning. In other words, the "innate prediction

417   profile" is relatively stable over time, while the "learned prediction profile" is adjusted to the current

418   environmental quality function (see Fig D in S1 Appendix).

20

419 In addition to the duration of the learning period (the number of learning episodes), the learning rate is

420 also an important aspect of the learning strategy. This parameter is also practically independent of the

421 environmental conditions in the replicates in which the efficient learning evolved (Fig 7C).

422 Fig 8 illustrates that the relationship between the number of learning episodes and performance is not

423 straightforward. First of all, in some environmental conditions, the outcome of evolution differs

424 considerably across replicates. If that is the case, networks that do not learn have worse performance

425 (their ability to choose the best environment is lower) than networks that learn (Fig 8). This is often

426 linked with lower fitness, i.e., more time spent foraging does not compensate for lower performance.

427 However, similarly to what we observed in the previous section, when learning evolves, a longer

428 learning period does not always lead to better performance. In some environmental regimes, a wide

429 range of learning episodes leads to practically the same performance (Fig 8). We hypothesize that the

430 variability between replicates might be partly explained by the properties of the coevolved networks.

431 Each replicate evolves a unique network that likely affects the effectiveness of learning. Loss of learning

432 in some replicates even if retention of learning could potentially lead to higher fitness could be linked

433 to the learning ability of a specific network. However, due to the complexity of the system, we were not

434 able to prove this hypothesis. It is also worth noting that in environmental regimes that lead to either

435 loss or maintenance of learning, in some replicates in which learning was lost at some point, it revolved

436 again.

437 Within each environmental regime, a range of learning episodes evolve. One might expect that in

438 replicates in which the learning period is shorter, the learning rate is higher to allow for faster adjustment

439 of weights and *vice versa* (similarly to the situation with fixed LE). When efficient learning evolves, in

440 some environmental regimes there is indeed a negative relation between the learning rates and the

441 number of learning episodes, but this is not a general trend (Fig 9). For example, for a small (0.1)

442 environmental change every 10 generations, in replicates in which learning evolved the learning rate

443 value seems to be even slightly positively correlated with the number of learning episodes (Fig 9). If the

444 number of learning episodes is very small (below 5), learning is not effective (Fig 8) and the learning

445 rate is very variable between replicates, consistent with random drift (Fig 9).
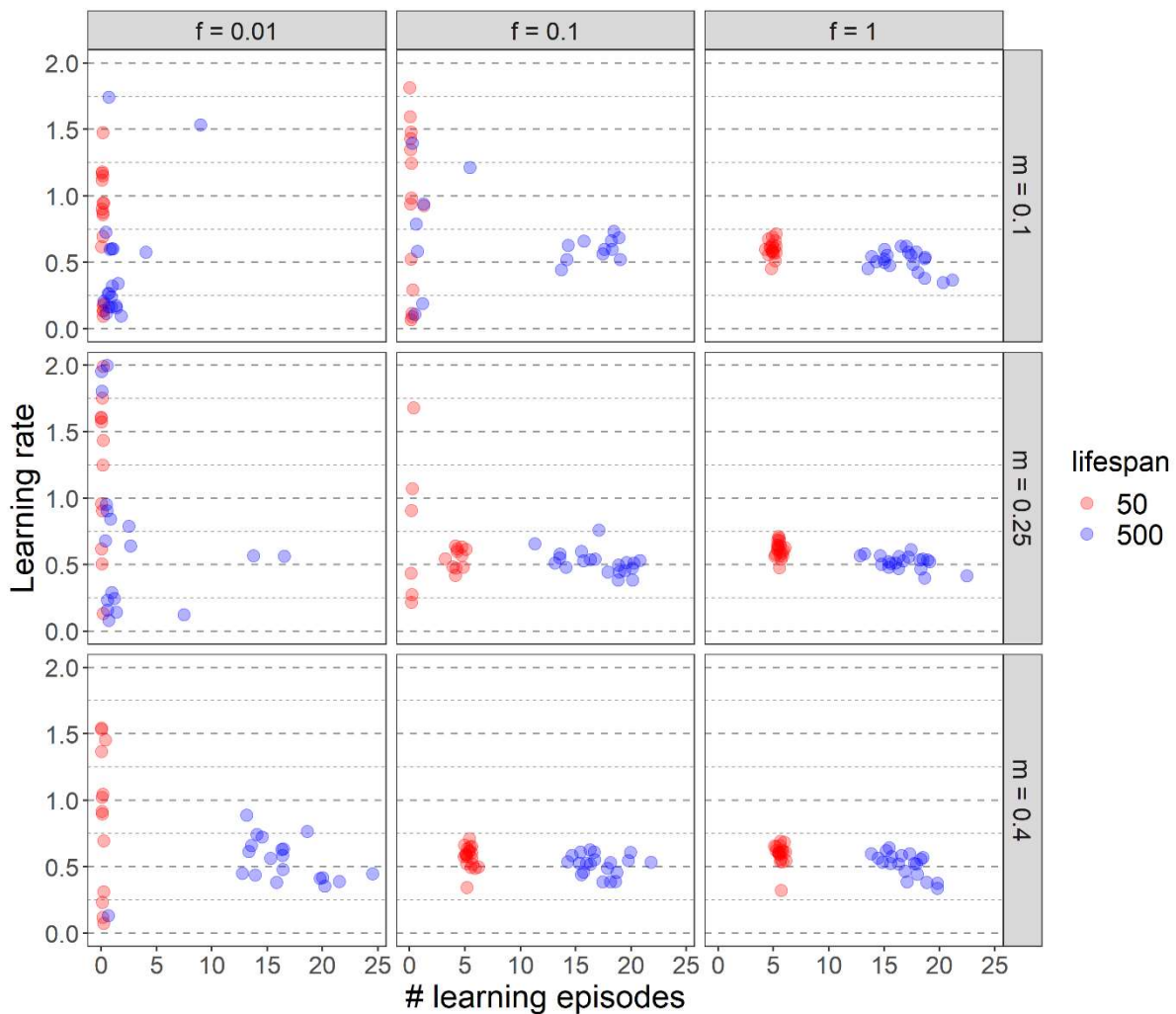
446

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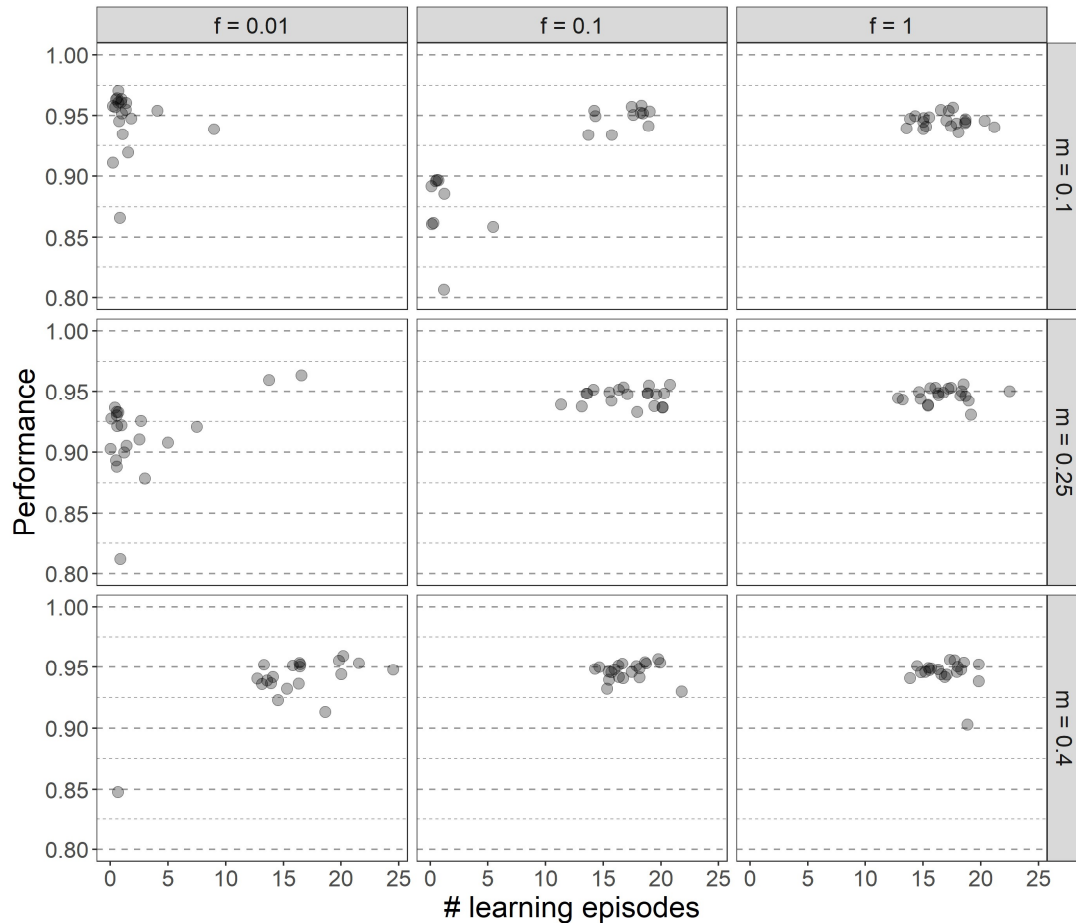
Fig 8. The relationship between performance and the number of learning episodes in different environmental regimes. Different columns correspond to different frequencies of environmental change (*f*) and different rows to different magnitudes of environmental change (*m*). Each point represents the average of the population mean over the last 2000 generations of a single replicate. One simulation (*f*=0.1, *m*=0.1) with low average LE (=0.93) is not visible, as the average performance (=0.65) was too low.

The last, but crucial part of the evolved learning mechanism is the neural network itself, and specifically the value of its weights. Neural networks are notoriously difficult to analyse but we decided to look at some of the properties of evolved neural networks. The only pattern we could see is that the average strength of connections that can be adjusted through learning was clearly lower for networks that evolved learning compared to networks that did not evolve learning (Fig C in S1 Appendix). This suggests that efficient learning cannot be achieved when weights are too high.

Effect of lifespan and environment on the evolution of learning

Until now, we considered an organism with a lifetime of 500 timesteps where the exploration-exploitation trade-off is relatively weak because efficient learning can be accomplished within a period of 20 timesteps. In this section, we consider an organism with a lifespan of only 50 timesteps, where the cost of learning is much larger, as each timestep spent learning corresponds to 2% of the organism's lifetime and hence reduces the foraging time considerably.

Figure 9. Effect of lifespan on the evolution of learning. For two lifespans (50 timesteps: red; 500 timesteps: blue) each panel shows the evolved relationship between the learning rate and the number of learning episodes in 20 replicate simulations. The panels correspond to different environmental regimes: the columns show three frequencies of environmental change (*f*) and the rows three magnitudes of change (*m*). Each point represents the average of the population mean over the last 2000 generations of

23

471   a single replicate. For clarity, only learning rates up to 2.0 are shown; 34 data points with a learning rate

472   above 2.0, all with a very low number of learning episodes (= no learning), are not visible.

473

474   For various environmental regimes, Fig 9 compares the evolutionary outcome for the two lifespans

475   considered. Not surprisingly, learning is less likely to evolve in the case of a shorter lifespan, especially

476   in those environmental regimes where adaptive tracking is, at least to a certain extent, efficient (a low

477   rate of change and/or a small magnitude of change). When learning evolves despite the short lifespan,

478   the evolved learning period is shorter in absolute terms (smaller number of learning episodes) but longer

479   in relative terms (a larger percentage of the lifespan is spent on learning). As in the case of a long lifespan

480   (Fig 7BC), both the number of learning episodes and the learning rate is practically independent of the

481   magnitude and rate of environmental change. However, the number of learning episodes is less variable,

482   reflecting a stronger selection on the efficient use of every single timestep.

483   Fig 10 shows that, whenever learning evolves at all, the resulting performance is smaller in case of a

484   short lifespan. In view of the fact that short-lived organisms spend less time learning, this is not too

485   surprising. Interestingly, when learning evolves in both lifespan conditions, even though the number of

486   learning episodes is clearly different, the evolved learning rate is only slightly higher for lower lifespan

487   for some environmental conditions (e.g. for the very frequent environmental change) but is independent

488   of the lifespan for other conditions (see Fig 9 and Fig E in S1 Appendix).
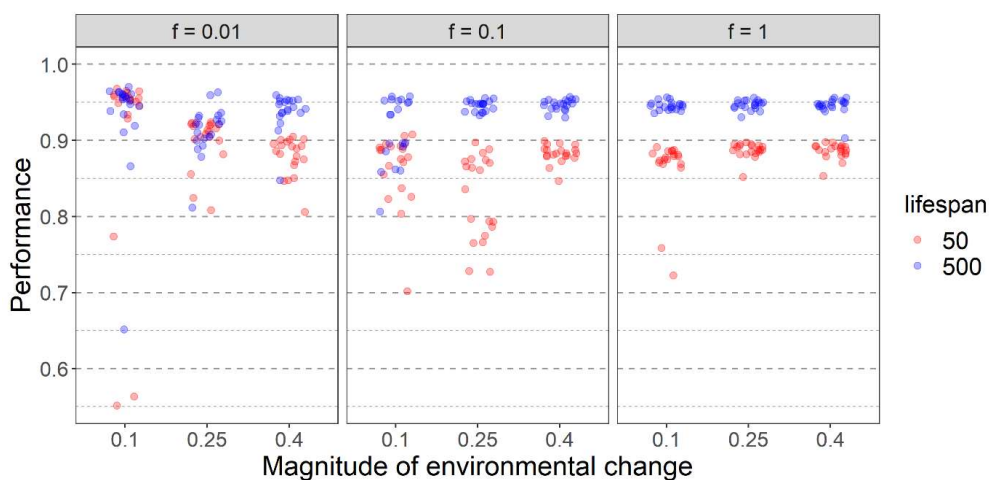
489   **Fig 10. Effect of lifespan on performance.** Results for two lifespans (50 timesteps: red; 500 timesteps:

490   blue) and nine environmental regimes (defined by the rate f and the magnitude m of change) are shown.

491   The average population performance in the last 2000 generations of 20 replicate simulations for each

492   parameter set is indicated by coloured dots.

493

494   All results presented thus far were based on an environmental quality function with σ = 0.25 (Fig 2).

495   Here, we consider the implications of a narrower (σ = 0.1) or a wider (σ = 0.4) Gaussian function. If the

496   function is narrow, only a small fraction of the available food is of high quality. Therefore, mistakes in

497   choosing among food items potentially lead to a severe loss of fitness. On top of this, environmental

498   change has a more drastic effect. If, for example, the magnitude of environmental change is large (e.g.,

499    $m = 0.4$), all high-quality food items in the previous generation become low-quality, while a small range

500   of the previously low-quality items become high-quality after the shift. One would therefore expect a

501   much stronger selection for learning in case of σ = 0.1. Conversely, selection for learning is expected to

502   be weaker in case of σ = 0.4.

503   Fig 11 shows how the evolution of learning (= the evolved duration of the learning period) depends on

504   lifespan and the width of the environmental quality function. Figs E and F in S1 Appendix show the

505   corresponding learning rates and performance levels, respectively. Consider first the case of a narrow

506   quality function (σ = 0.1). As argued above, one would expect that learning is more important in this

507   case. It is therefore somewhat surprising that learning less easily off the ground than in our standard

508   scenario (σ = 0.25). This may be explained by the fact that efficient learning is difficult to achieve in the

509   case of a narrow quality function. The reason can be that most of the cues sampled during the learning

510   period are of very low (practically zero) quality (cues are sampled randomly); accordingly, these cues

511   provide little information on where the peak of the function is located.

512   When the quality function is broad (σ = 0.4) the environmental conditions (frequency and magnitude of

513   change) in which learning evolves are very similar to the ones with σ = 0.25 (Fig 11). One clear

514   exception is an environmental change of m=0.25 every 10 generations (f=0.1) for the lifespan of 50. In

515   this case for σ = 0.4 learning never evolves, while it does for roughly half of the replicates for σ = 0.25.

516   It seems that for a relatively small and rare change spending time learning doesn't compensate enough

517   for lost foraging opportunities if food quality changes only slightly around the peak and choosing less

518   optimally does not reduce fitness considerably (for σ = 0.4).

25

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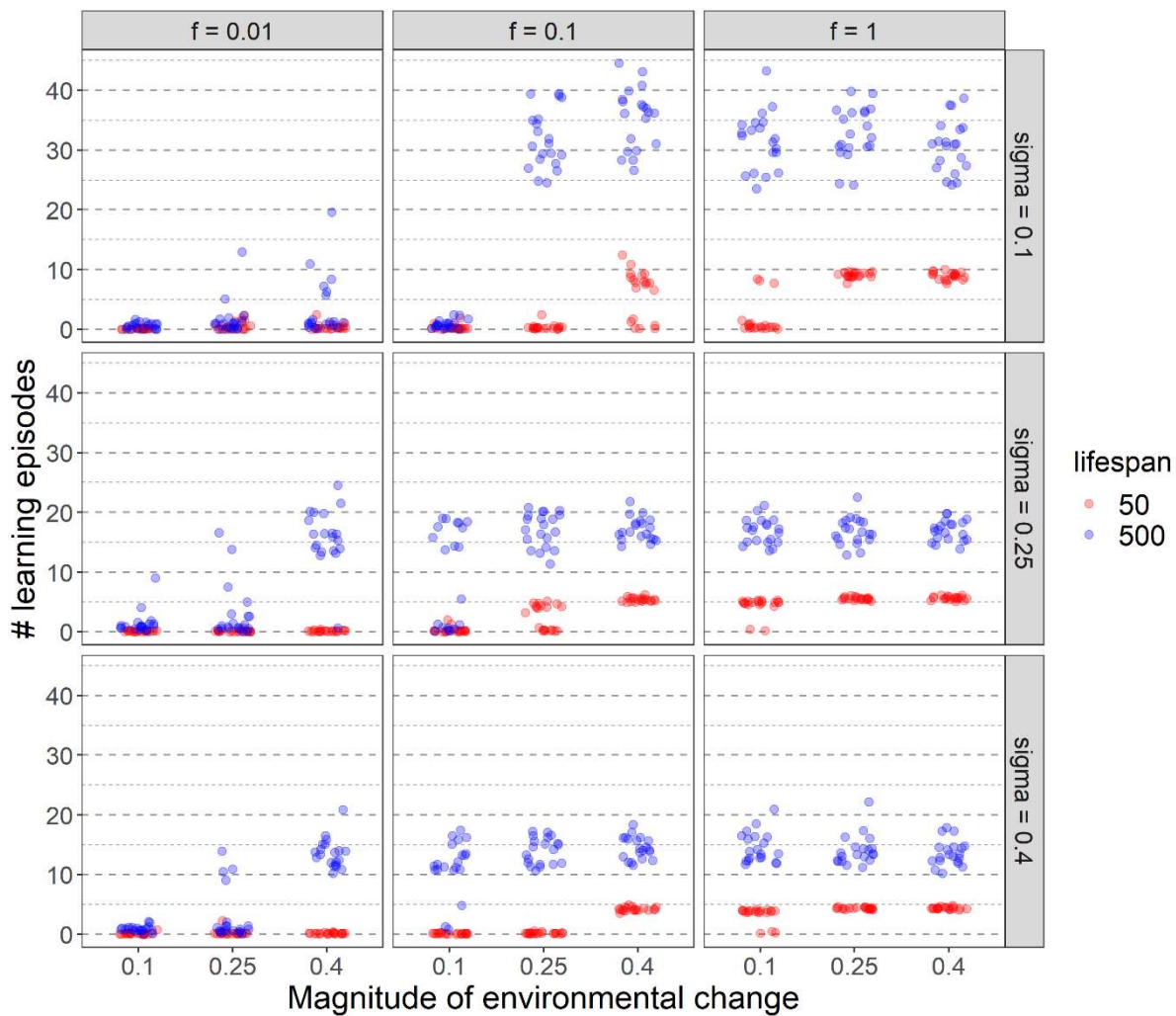
Fig 11. Effect of lifespan and the width of the quality distribution on the evolution of learning.

Rows correspond to different values of σ (sigma), that is, to different widths of the quality function.

Graphical conventions as in the previous figures.

When learning is maintained, the number of learning episodes increases with decreasing σ, while at the same time, performance decreases (Fig F in S1 Appendix) as every mistake is more costly. Similarly, the learning rate decreases with decreasing σ, supporting the general expectation that with a lower number of learning episodes, the learning rate should be larger to allow for faster learning in a shorter time (Fig E in S1 Appendix). However, as noted earlier, within one environmental regime learning rate might not correlate with the number of learning episodes.

530 As observed earlier, for a given width of quality distribution, if learning evolves the number of learning

531 episodes and learning rate do not depend on the magnitude and frequency of environmental change (Fig

532 11 and Fig E in S1 Appendix).

533

534 Discussion

535 We presented a novel way of modelling the evolution of learning, using small neural networks and a

536 simple, biology-inspired learning algorithm. We used this model as a tool to answer evolutionary

537 questions that are usually tackled by simple analytical models. Contrary to analytical methods, even a

538 relatively simple network, as studied here, allows for more complex phenotypes and learning strategies

539 and at the same time can lead to efficient adaptation and novel insights into the evolution of learning.

540 In line with the literature (e.g [6,10,27,34]), the frequency of environmental change had a large effect

541 on the probability that learning will be maintained in the population. The same holds for the magnitude

542 of environmental change, although this aspect of environmental variation has rarely been studied.

543 Usually, environmental change is assumed to be random and there is no correlation between subsequent

544 environmental states (e.g., [10,35] and references therein), even though it is likely not the case in the

545 real world [36]. In our model, when environmental change is infrequent and/or small, genetic tracking

546 evolved. In less stable environments, learning (a "plastic" response) was selected for, but if the change

547 was very frequent and large, individuals made random choices – a strategy resembling bet-hedging.

548 Similar results for the evolution of adaptive tracking, plastic responses, and bet-hedging were observed

549 by Botero *et al.* [33], although they modelled the predictability of the future environment based on the

550 current cues, while in our model different magnitudes and frequencies of environmental change can say

551 something about how much the current environment predicts a future state.

552 Whenever learning evolves one might expect that the learning strategy (the length of the learning period

553 and the learning rate) is fine-tuned to the environmental change regime. However, surprisingly, we

554 found that the learning strategy was independent of the environmental change regime. To the best of our

555 knowledge, our study is the first to report such a finding. The few studies that investigated such effects

556 reported a relationship between the frequency of environmental change and the evolved or optimal

557   learning parameters [28,29,34,37,38]. We are not aware of any neural network models studying the

558   effect of environmental change regimes on the learning strategy.

559   The discrepancy between our results and those of previous studies may reflect the higher number of

560   degrees of freedom in our model or the peculiarities of the task itself. In earlier models, learning

561   (governed by a single parameter) affects only one variable., which is sometimes identical to the

562   "phenotype". Under this restriction, different learning parameter values seem necessary to deal with

563   different frequencies of environmental change. In our model, the "phenotype" is more complex (the

564   function ascribing a predicted quality to a range of cues) and learning affects more than one parameter

565   (four network weights). When the environment changes, the relationship between cues and their quality

566   changes. In this case, when efficient learning evolves it lets organisms predict the current location of the

567   environmental peak, independent of when and how much it changed in the past. In the future, it would

568   be interesting to study the evolved learning strategy of networks challenged by a different task, e.g.

569   having to know the quality of all environmental cues, rather than just identifying the ones that are the

570   best in a set of options.

571   For learning to be efficient, not only a learning strategy must be fine-tuned, but also the underlying

572   neural network. While many networks can perform the task, not all are suitable to learn. For example,

573   our initial networks with random weights did not support efficient learning and the performance of our

574   simulated organisms was initially poor. Randomly initialised neural networks can show a good

575   performance if the learning algorithm is very efficient (e.g. backpropagation) and if the learning consists

576   of many learning steps [39]. However, different studies consistently indicate that networks that evolved

577   initial weights can be trained significantly faster and better than networks with random initial weights

578   [20,40] (but see the discussion on reservoir computing below). This seems to apply also to our less

579   sophisticated learning mechanism and supports the view that learning and evolution together are more

580   successful than either alone [40,41]. As noted by Mery and Burn "evolution of a combination of learning

581   and innate behavioural responses is probably a common process" [42] but it has very rarely been

582   included in models of the evolution of learning. Neural networks provide an intuitive way of studying

583   the intertwined evolution of innate and learned responses to the environment.

28

584 Another interesting finding of our study is that the distribution of resources in the environment strongly

585 affects the probability of learning evolving and the evolved learning strategy. To our knowledge, this

586 has never been observed (or even investigated) before. When only a small fraction of available resources

587 provides nutrients (small σ in our model) then one could expect that learning would be more likely to

588 evolve to allow individuals to find the cues that are linked with profitable food. However, this is not the

589 case and learning is actually less likely to evolve then. It seems that learning is less likely to evolve

590 whenever sampling the environment can lead to frequent encounters with items that do not provide

591 resources and therefore information – "clueless environments" [43]. In this case, spending time learning

592 is relatively more costly, which seems to shift the cost-benefits balance against learning. More studies

593 looking at this aspect of the environment would be welcome.

594 Not only environmental but also organismal properties can affect the evolution of learning. One obvious

595 one is an organism's lifespan. While it is generally assumed that shorter-lived organisms should invest

596 less in cognitive functions, as the cost of learning is relatively larger while the time to profit from

597 learning is shorter (see the discussion on this topic in [29,44]), there are, to the best of our knowledge,

598 only two modelling studies that investigated the effect of lifespan on learning. Eliassen *et al*. [28] studied

599 learning in the context of the exploration-exploitation trade-off and showed that learners should invest

600 less in learning for shorter expected lifespans (higher external mortality). But the optimal speed of

601 learning depended not only on the expected lifespan but also on the temporal change in the environment.

602 Liedtke & Fromhage [29] built a vastly different and simpler model in which learning reduced the

603 handling time of food items. They showed that the learning speed and the investment in learning (in

604 their model the higher the learning speed the higher costs paid) should be highest for short and

605 intermediate lifespans. Our results are to some extent in line with those of Eliassen *et al*. and the common

606 wisdom that short-lived organisms should invest less in learning. However, in our model, lifespan and

607 the pattern of environmental change have a surprisingly small (or even negligible) effect on the learning

608 speed when learning evolves. Clearly, details of the model assumptions can have a profound effect on

609 the model outcomes. Therefore, additional studies, both theoretical and empirical, on the effect of

610 lifespan on learning are needed.

611   It is generally accepted that learning is costly. The costs can be manifold, for example, energetic costs

612   of growth and maintenance of the brain tissue, resource allocation trade-offs, or increased mortality due

613   to suboptimal behaviour during the learning phase (see e.g. [6,45–47]). In many studies, the cost of

614   learning is just one of the parameters included *a priori* in the model (see e.g. [10] and references therein).

615   To avoid extra assumptions, the only cost of learning in our model stems from the limited lifespan and

616   the trade-off between exploration (learning) and exploitation (foraging). To this end, our model assumes

617   that an individual's life is divided into two separate stages: learning and foraging. This is clearly a

618   simplification, as animals can learn during their whole life. However, this simplification was used in

619   models before (e.g. [48]) and it is to some extent justified by the observation that in many animals

620   (including humans), early life (childhood) is characterised by much more intense learning than later life

621   [49]. Separation of the learning and foraging phases allows for a better understanding of the evolved

622   strategies under a time constraint. However, since learning also incurs other costs (see above) our model

623   is a starting point for studying the minimal requirements for learning to evolve [50]. It would also be

624   interesting to consider scenarios where the environment changes during an individual's lifetime. In that

625   case, it is not the best strategy to learn only at the beginning of life. Future models could implement life-

626   long learning and allow for learning while foraging.

627   In our model, learning induces a change in the nervous system that usually leads to an improvement in

628   performance. But this is not always the case, e.g. if the learning period is very short. This finding

629   undermines the common assumption that, as long as the learning cues are reliable, learning will always

630   improve performance or even lead to perfect behaviour (e.g. [10,35,51]). Mechanistic approaches like

631   ours are required to elucidate whether and when such an assumption is justified.

632   Neural network models are especially suited to answer evolutionary questions concerning behaviour as

633   they explicitly incorporate the proximate stimulus-response aspect of behaviour. Optimisation

634   approaches (tend to) neglect the proximate underpinning of adaptations. Neural networks are also suited

635   for more complex problems than the ones that can be tackled with analytical methods [52]. Also, as

636   mentioned earlier, they provide a great opportunity to study the coevolution of innate behaviours

637   together with the evolution of learning mechanisms. In our model, learning affected only part of the

638   network – this approach was inspired by reservoir computing in which also only the weights linked to

30

639 the output node change, yet the network can still learn complex tasks [23,24,53]. Such a learning

640 mechanism seems very suitable for evolutionary studies as it is unlikely that in early animals a single

641 learning event could affect all connections in the network as is usually assumed in AI applications.

642 We draw inspiration from reservoir computing in the sense that learning affects only a small subset of

643 network weights. However, our network and the task it needs to perform is much simpler than what is

644 potentially possible with a reservoir computing approach and what biological brains can do [23,24,53].

645 Promising future projects could incorporate larger networks that not only pass information in one

646 direction (feed-forward) but also include backward connections and feedback loops (allowing for

647 longer-term memory). Such "reservoir" networks could dynamically store various types of inputs,

648 making them available for a diversity of decision-making processes, such as making decisions in the

649 context of foraging, predator avoidance, mating, and social behaviour. Each type of decision (which we

650 henceforth will call a "domain") would be governed by domain-specific output nodes, which are

651 connected to the reservoir. Domain-specific learning could happen as in our model: based on simple

652 mechanisms only affecting the connections to the domain-specific output nodes. Each output node may

653 have its own domain-specific connections with the reservoir, allowing output nodes governing foraging

654 behaviour to tap into different parts of the reservoir than output nodes linked with predator avoidance.

655 By considering mutations that break or create connections from the output nodes to reservoir nodes, this

656 part of the network architecture could evolve by domain-specific selection. Such partial restructuring of

657 the network would likely make behaviour and learning more efficient [24,54], even though learning

658 would affect only a small fraction of the connections. The domain-general reservoir could also be shaped

659 by natural selection. Interestingly, the demands on the reservoir may not be stringent, provided that it is

660 sufficiently complex: as shown in the literature on reservoir computing [23,24,53]. Reservoir-based

661 learning can be very efficient even if the connections between the nodes of the reservoir are quite

662 arbitrary (i.e., if the connection strengths are drawn at random). A network model as sketched above

663 would allow using the same environmental information and network structure to perform different tasks,

664 as is also seen in the animal brains [24] without making a priori assumptions on what environmental

665 cues are important in different contexts.

666 In conclusion, we showed that a biologically inspired, yet relatively simple, learning mechanism can

667 evolve to lead to an efficient adaptation in a changing environment. We hope that our model will serve

668 as an inspiration for future work on more challenging research projects and ultimately to a better

669 understanding of the evolution of learning.

670

Acknowledgements

675

Supporting information

677 S1 Appendix. **Supplementary figures A-F.**

678 The source code (in C + +) for the simulation program is available at

679 https://github.com/marmgroup/evolution_of_learning.

680

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