

## Erratum: Searching for dark radiation at the LHC

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Elias Bernreuther,<sup>a</sup> Felix Kahlhoefer,<sup>b,c</sup> Michele Lucente<sup>b</sup> and Alessandro Morandini<sup>b</sup>

<sup>a</sup>*Fermi National Accelerator Laboratory,  
Batavia, IL 60510, U.S.A.*

<sup>b</sup>*Institute for Theoretical Particle Physics and Cosmology (TTK), RWTH Aachen University,  
D-52056 Aachen, Germany*

<sup>c</sup>*Institut für Theoretische Teilchenphysik, Karlsruhe Institute of Technology (KIT),  
76128 Karlsruhe, Germany*

*E-mail:* [ebernreu@fnal.gov](mailto:ebernreu@fnal.gov), [kahlhoefer@kit.edu](mailto:kahlhoefer@kit.edu),  
[michele.lucente@unibo.it](mailto:michele.lucente@unibo.it), [alessandro.morandini@kit.edu](mailto:alessandro.morandini@kit.edu)

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In the published version there was a small mistake in eq. (2.15), leading to errors also in eqs. (2.16) and (2.18). The corrected expression should read

$$I = 8\pi^2 \int dE E^3 \int d\eta \sinh^2 \eta \int d\cos\theta \frac{2E(\cosh\eta + \sinh\eta \cos\theta)}{m_B} f_B(2E \cosh\eta) \delta(E - m_B/2) \times \left[ 1 - \frac{f_\chi(E(\cosh\eta + \sinh\eta \cos\theta))}{f_\chi^{\text{eq}}(E(\cosh\eta + \sinh\eta \cos\theta))} \right], \quad (1)$$

which directly implies

$$I = \pi^2 m_B^3 \int d\eta \sinh^2 \eta \int d\cos\theta (\cosh\eta + \sinh\eta \cos\theta) f_B(m_B \cosh\eta) \times \left[ 1 - \frac{f_\chi\left(\frac{m_B}{2}(\cosh\eta + \sinh\eta \cos\theta)\right)}{f_\chi^{\text{eq}}\left(\frac{m_B}{2}(\cosh\eta + \sinh\eta \cos\theta)\right)} \right]. \quad (2)$$

This then leads to

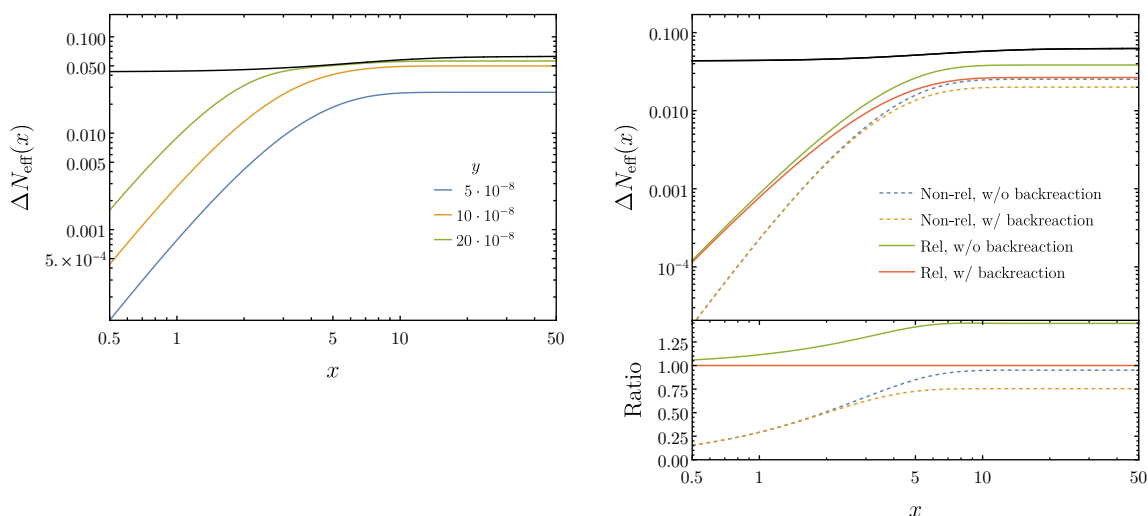
$$\tilde{H}x s^{4/3}(x) \frac{dZ_\chi}{dx} = \frac{m_B^4 \Gamma_B}{8\pi^2} \int_{-1}^1 d\cos\theta \int_1^\infty dw \sqrt{w^2 - 1} f_B^{\text{eq}}(w; T) (w + \sqrt{w^2 - 1} \cos\theta) \times \left[ 1 - r_\chi(w + \sqrt{w^2 - 1} \cos\theta; T, \epsilon) \right]. \quad (3)$$

We note that in the absence of backreaction (setting  $r_\chi = 0$ ) the integral over  $\cos\theta$  can be performed analytically, giving

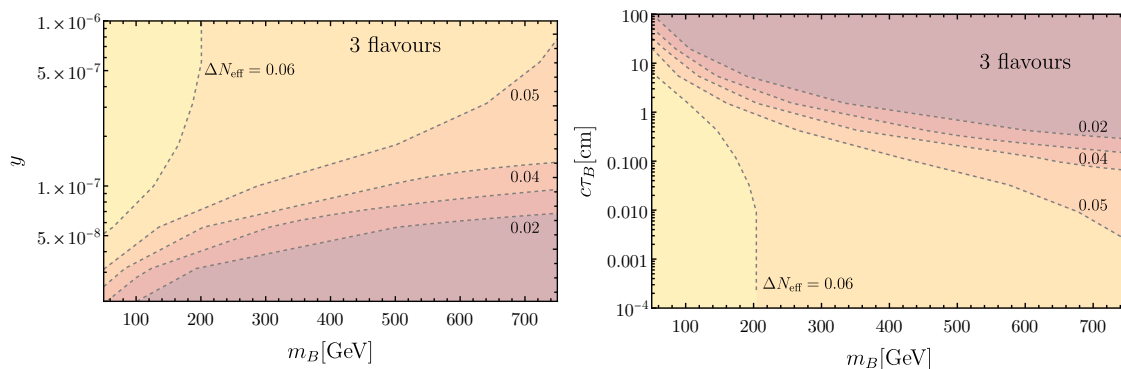
$$I = 2\pi^2 m_B^3 \int dw \sqrt{w^2 - 1} w f_B(m_B w) = \frac{\pi}{2} \int d^3 p_B f_B(E_B) = 4\pi^4 n_B, \quad (4)$$

where we have introduced  $E_B = m_B w$  in the second line. In other words, the relativistic corrections for freeze-in from decays cancel out, and the integrated collision operator is simply given by  $m_B \Gamma_B n_B / 2$ .

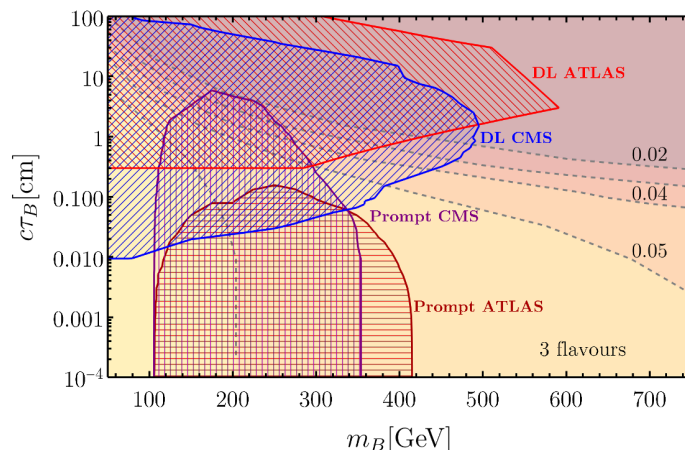
The correction leads to a slightly enhanced production of dark radiation at high temperatures, leading to a slight increase in the predicted value of  $\Delta N_{\text{eff}}$  for a given model parameter point. The mistake therefore affects all figures shown in the published version. We include the corrected versions below.



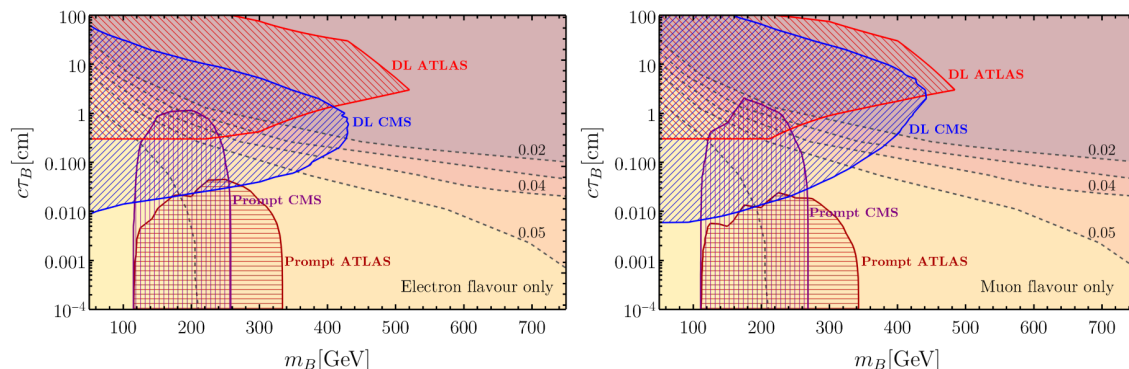
**Figure 1.** Shift in the effective number of relativistic species as defined in eq. (2.5) as a function of time for a benchmark mass value of  $m_B = 300$  GeV. The left panel shows how increasing the coupling increases  $\Delta N_{\text{eff}}$ , but the increase becomes milder for large couplings due to the backreaction effect. The right panel illustrates the importance of the various effects included in our analysis compared to simpler approximations (non-relativistic decays, no backreaction).



**Figure 2.** Shift in the effective degrees of freedom as a function of the mass and coupling (*left*) or proper decay length (*right*). Shorter lifetimes correspond to larger coupling and for short enough lifetimes we reach the equilibrium densities and the upper bound on  $\Delta N_{\text{eff}}$ .



**Figure 3.** LHC constraints on the parameter space of interest for the 3-flavour case ( $y_e = y_\mu = y_\tau = y$ ). Note that for short lifetimes and  $m_B \lesssim 100$  GeV the parameter space is at least partially excluded by LEP searches [1].



**Figure 4.** LHC constraints on the parameter space of interest in the case of  $B$  only coupling to a single flavour. On the left for coupling to electrons only ( $y_e = y, y_\mu = y_\tau = 0$ ), on the right for coupling to muons only ( $y_\mu = y, y_e = y_\tau = 0$ ). Also in this case LEP excludes partner masses  $m_B \leq 104$  GeV.

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## References

- [1] DELPHI collaboration, *Searches for supersymmetric particles in  $e^+e^-$  collisions up to 208-GeV and interpretation of the results within the MSSM*, *Eur. Phys. J. C* **31** (2003) 421 [[hep-ex/0311019](https://arxiv.org/abs/hep-ex/0311019)] [[INSPIRE](https://inspirehep.net/literature/1000000)].