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## Forecasting COVID-19 with Importance Sampling and Path-Integrals

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*Abstract-Background:* Forecasting nonlinear stochastic systems most often is quite difficult, without giving in to temptations to simply simplify models for the sake of permitting simple computations.

*Objective:* Here, two basic algorithms, Adaptive Simulated Annealing (ASA) and path-integral codes PATHINT/PATHTREE (and their quantum generalizations qPATHINT/ qPATHTREE) are suggested as being useful to fit COVID-19 data and to help predict spread or control of this pandemic. Multiple variables are considered, e.g., potentially including ethnicity, population density, obesity, deprivation, pollution, race, environmental temperature.

*Method:* ASA and PATHINT/PATHTREE have been demonstrated as being effective to forecast properties in three disparate disciplines in neuroscience, financial markets, and combat analysis.

*Results:* Not only can selected systems in these three disciplines be aptly modeled, but results of detailed calculations have led to new results and insights not previously obtained.

Keywords: path integral, importance sampling, financial options, combat analysis.

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# Forecasting COVID-19 with Importance Sampling and Path-Integrals

Lester Ingber

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*Results:* Not only can selected systems in these three disciplines be aptly modeled, but results of detailed calculations have led to new results and insights not previously obtained.

*Conclusion:* While optimization and path-integral algorithms are now quite well-known (at least to many scientists), these applications give strong support to a quite generic application of these tools to stochastic nonlinear systems.

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## I. INTRODUCTION

t is generally recognized that the spread of COVID-19 is affected by multiple variables, e.g., potentially including ethnicity, population density, obesity, deprivation, pollution, race, environmental temperature (Anastassopoulou *et al*, 2020; Bray *et al*, 2020; Li *et al*, 2020). Also, the Centre for Evidence-Based Medicine (CEBM) regularly cites papers on the dynamics of COVID-19 at https://www.cebm.net/evidence-synthesis/ transmission-dynamics-of-covid-19/.

This proposal offers the application of two basic multivariate algorithms to fairly generic issues in forecasting. As such, they may be useful to fit COVID-19 data and to help predict upcoming spread and control of this pandemic.

 (a) Adaptive Simulated Annealing (ASA) developed by the author (Ingber, 1993a) is an importancesampling optimization code usually used for nonlinear, nonequilibrium, non-stationary, multivariate systems.

Author: Physical Studies Institute LLC, Ashland, OR, USA. e-mail: ingber@caa.caltech.edu (b) PATHINT is a numerical path-integral PATHINT code developed by the author (Ingber, 1993b) used for propagation of nonlinear probability distributions, including discontinuities.

These codes were developed by the author and applied across multiple disciplines.

There is not "one size fits all" in forecasting different systems. This was demonstrated for three systems (Ingber, 2020b), where the author has addressed multiple projects across multiple disciplines using these tools: 72 papers/reports/lectures in neuroscience, e.g. (Ingber, 2018; Ingber, 2021), 31 papers/reports/lectures in finance, e.g. (Ingber & Mondescu, 2003; Ingber, 2020a), 24 papers/reports/ lectures in combat analyses, e.g. (Ingber, 1993b; Ingber, 2015), and 11 papers/reports/lectures in optimization, e.g. (Atiya *et al*, 2003; Ingber, 2012), It is reasonable to expect that this approach can be applied to many other projects.

For example, the path-integral representation of multivariate nonlinear stochastic differential equations permits derivation of canonical momenta indicators (CMI) which are faithful to intuitive concepts like Force, Momenta, Mass, etc (Ingber, 1996; Ingber, 2015; Ingber & Mondescu, 2001). Correlations among variables are explicitly included in the CMI.

## II. Data

A large and updated database for COVID-19 is maintained by the John Hopkins University (JHU) at https://github.com/CSSEGISandData/COVID-19/blob/m aster/archived\_data/archived\_daily\_case\_up-dates/01-21-2020\_2200.csv. This database was used for a pilot study.

### a) 50+ Locations

The data being used contains 3340 cities throughout the US and some territories. The locations have been broken into 57 States and Territories ready for production runs.

## III. TECHNICAL CONSIDERATIONS

If there is not time to process large data sets, then the data can be randomly sampled, e.g., as described in another paper, "Developing bid-ask probabilities for high-frequency trading" (Ingber, 2020a). If the required forecast is longer than the conditional distribution can sustain, PATHINT/ PATHTREE can be used to propagate the distribution.

The dataset should be broken into independent Training and Testing subsets, to test the trained distribution. If this is not possible, e.g., because of data or time limitations, at the least experts can be used to judge if the model is ready for realtime applications, e.g., the Delphi method (Okoli & Pawlowski, 2004).

If an algorithm like ASA is to be used across a large class of problems, then it must be tunable to different classes. Over the 30+ years of ASA development, the author has worked with many volunteers who have contributed valuable ideas, modifications and corrections to this code. This has resulted in over 150 ASA options that can be used for additional timing additional tuning making it useful across many classes of problems.

The path integral algorithm includes its mathematical equivalents, a large class of stochastic differential equations and a large class of partial

$$L_{eff} = [(x_{t+1} - x_t - g_x dt)g_{xx'}(x'_{t+1} - x'_t - g_{x'} dt) + 1/2 \log(2\pi dt g^2)$$

$$g_x = a \exp(x^b)$$

$$g_{xx'} = c \exp(x^d)$$

$$g = \det(g_{xx'})$$

with parameters to be fit to data  $\{a, b, c, d\}$ . This is a simple one-factor model. In more than one dimension,  $g_{xx}$  is the metric of this space, the inverse of the covariance matrix.

For the full data set, 100,000 generated-state iteration-s of this cost/objective function's states over the JHU data gave

$$a = 0.077, b = 0.874, c = 2.79, d = 0.845$$
 (2)

#### a) Comet Profile

These codes were run on XSEDE Comet, for 100000 generated states.

"Comet is a dedicated XSEDE cluster designed by Dell and SDSC delivering 2.0 petaflops, featuring Intel next-gen processors with AVX2, Mellanox FDR InfiniBand interconnects and Aeon storage. The standard compute nodes consist of Intel Xeon E5-2680v3 (formerly codenamed Haswell) processors, 128

GB DDR4 DRAM (64 GB per socket), and 320 GB of SSD local scratch memory. The GPU nodes contain four NVIDIA GPUs each. The large memory nodes contain 1.5 TB of DRAM and four Haswell processors each. The network topology is 56 Gbps FDR InfiniBand with rack-level full bisection bandwidth and 4:1 oversubscription cross-rack bandwidth. Comet has 7 petabytes of 200 GB/second performance storage and 6 petabytes of 100 GB/second durable storage. It also has dedicated gateway hosting

differential equations. The advantages of the path integral algorithm are:

- (a) Intuitive description in terms of classical forces, inertia, momentum, etc., leading to new indicators.
- (b) Delivering a cost function derived from a Lagrangian, or its Action (Lagrangian x dt). Sometimes constraints need to be added as Lagrange multipliers, as was required for normalization requirements in financial risk projects (Ingber, 2010).

## IV. PILOT STUDY

The shape of the spread of this virus is clearly nonlinear. A simple model was used for a pilot study to at least capture some nonlinearity. For example, just using the daily number of total cases reported, *C*, the short-time conditional Probability P(t + 1|t) is given in terms of its effective Lagrangian L, P =exp ( $L_{eff}dt$ ) (including the logarithm of the prefactor normalization as it may contain nonlinearities as modeled here):

nodes and a Virtual Machine repository. External

Comet is being phased out and users will soon be using the new Expanse platform.

connectivity to Internet2 and ESNet is 100 Gbps."

#### b) Parallel Processing

"Parallel Processing for this project basically is similar to many projects developed by the author as Principal Investigator at the Extreme Science and Engineering Discovery Environment (XSEDE.org) since February 2013. That is "trivial MPI" is used, wherein many simultaneous runs are achieved by simply reading in different data files to ASA, using the "array" feature offered by some XSEDE platforms. As offered in a previous XSEDE Extended Collaborative Support Service (ECSS) ticket:

Parallelization efficiency is 1 for jobs running on a single core that is max one could get. For multi-threaded apps one can get some to decent bump in speed using multiple cores up to some point before plateauing. However, speed bump with multiple cores often leads drop in parallelization efficiency.

Drawback of using single core is too long run time. Though in this case, you are running array jobs with single core and getting maximum efficiency. This is the ideal situation on 'Comet' because nodes on this machine can be shared. You should explain on Scaling and parallelization efficiency section that your application is not multi-threaded and you use single core on comet to run your jobs. This gives efficiency of 1, which is maximum value achievable. However, you run array of jobs in one submission and each job uses a single core. This is most efficient use of resources because node sharing is allowed on Comet. It won't hurt to write that you have consulted XSEDE staff on this matter."

#### c) Xeon Processor

The full US run was done on the author's P1 Gen 3 Thinkpad with a Xeon processor. Previous runs show full agreement between the Comet and the Thinkpad runs when "-ffloat-store" is added to the compile parameters. A full US run of 100,000 generated states with 3239 non-zero locations took 1 hr 47 min 17 sec. (All runs including subsets of the full US therefore took about twice that long.)

#### ALL RESULTS V.

All locations were processed to exclude those with all "0" for all days, 99 of them.

Note that a few locations, those with just sublocation as it turned out, gave parameter values that hit boundaries of assigned parameter maximums or minimums. Since these were few exceptions, the decision was made to keep the default ranges given in Table 1.

#### Table 1

Par	Min	Max
0	-2	2
1	-2	2
2	0.1	2
3	-2	2

Final Results for all 58 Locations are given in Table 2.

## Table 2

RUNS COVID/asa usr out 01-Alabama final cost value = 0.0006165903Parameter Value

- 0 0.07526909
- 1 0.7867917
- 2 0.1
- 1.036661 3

RUNS COVID/asa usr out 02-Alaska final cost value = 0.0008660421Parameter Value

- 0 0.03041555
- 1 0.9221085
- 2 0.1
- 3 0.9276368

RUNS COVID/asa usr out 03-Arizona final cost value = 0.003912767Parameter Value

- 0 0.08377208
- 1 0.818453
- 2 0.1
- 3 1.287453

RUNS COVID/asa usr out 04-Arkansas final cost value = 0.0004816542Ρ

Parameter	Value	

0	0.07941101
1	0.7750893

0.7	10	003
	-	

2	0.1	

3 1.183597

RUNS COVID/asa usr out 05-California final cost value = 0.0009490655

Parameter Value

0	0.06696538
1	0 8527078

-	
2	0.1

3 1.292374

RUNS COVID/asa usr out 06-Colorado final cost value = 0.000503892Parameter Value

0	0.02576714

1	0.875757
1	0.8/5/5/

- 0.1076587 2
- 3 1.033743

RUNS COVID/asa usr out 07-Connecticut final cost value = 0.006819112Parameter Value

0	0.03883795

- 2 0.1499112
- 3 1.133882

RUNS COVID/asa usr out 08-Delaware final cost value = 0.004949477Parameter Value

liametei	value
0	0.1227538

-	
1	0.6899159

2	0.261152

3 0.9695861

RUNS COVID/asa usr out 09-Diamond Princess final cost value = -0.05391078

Parameter Value

0	-4.98784e-07
1	-1.992295
2	0.1

2	0.1
3	-2

RUNS COVID/asa usr out 10-District of Columbia final cost value = 0.06929941Parameter Value 0 2 1 0.4060976 2 2 3 0.7794162 RUNS COVID/asa usr out 11-Florida final cost value = 0.0008101027Parameter Value 0 0.0844608 1 0.8210241 2 0.1 1.270596 3 RUNS COVID/asa usr out 12-Georgia final cost value = 0.0002643592Parameter Value 0 0.04424673 0.8548552 1 2 0.1 3 1.162738 RUNS\_COVID/asa\_usr\_out\_13-Grand\_Princess final cost value = -0.063622Parameter Value -6.538724e-08 0 -1.806268 1 2 0.1 3 -2 RUNS COVID/asa usr out 14-Guam final cost value = 0.0465182Parameter Value

0	0.008877227
1	1,154289

- 2 0.1
- 3 1.147461

RUNS COVID/asa usr out 15-Hawaii final cost value = 0.006862005Parameter Value

- 0 0.01611866
- 1 1.050401
- 2 0.1
- 3 1.102763

RUNS COVID/asa usr out 16-Idaho final cost value = 0.0007488098Parameter Value

- 0 0.05115676
- 1 0.8504985
- 2 0.1
- 3 1.084733

RUNS COVID/asa usr out 17-Illinois final  $\overline{cost}$  value =  $\overline{0.0004481785}$ Parameter Value

- 0 0.06157631
- 1 0.8171975
- 2 0.8193241
- 3 1.021197

RUNS COVID/asa usr out\_18-Indiana final cost value = 0.0003787652Parameter Value

- 0 0.0412226
- 1 0.8332504
- 2 0.1
- 3 0.9823153

RUNS COVID/asa usr\_out\_19-lowa final cost value = 0.0003525547

Parameter Value

- 0 0.07068677
- 1 0.7683947
- 2 0.1387974
- 3 1.049687

RUNS COVID/asa\_usr\_out\_20-Kansas final cost value = 0.0002747757Parameter Value

0 1	0.0456688 0.8592813
2	0.1
3	1.161988

RUNS COVID/asa usr out 21-Kentucky final cost value = 0.0002246308Parameter Value

- 0 0.03505446
- 1 0.8823249
- 2 0.1
- 3 0.9808715

RUNS COVID/asa usr out 22-Louisiana final cost value = 0.0008015797Parameter Value

- 0 0.1070208
- 0.7072564 1
- 2 2
- 3 0.7402889

RUNS COVID/asa\_usr\_out\_23-Maine final cost value = 0.001441506Parameter Value

> 0 0.03198315

- 1 0.7940144
- 2 0.1823495
- 3 0.6823531

RUNS COVID/asa usr out 24-Maryland final cost value = 0.002061062Parameter Value

- 0 0.0638636
- 1 0.7898237
- 2 0.1
- 1.089192 3

RUNS COVID/asa usr out 25-Massachusetts final cost value = 0.004352416

Parameter Value

- 0 0.06403747
- 1 0.7364045
- 2 0.1
- 1.128749 3

RUNS COVID/asa usr out 26-Michigan final cost value = 0.0004323011Parameter Value

- 0 0.04372185
- 1 0.7974153
- 2 0.311704
- З 0.8720471

RUNS COVID/asa usr out 27-Minnesota final cost value = 0.0004295167Value

Parameter

- 0 0.06178572
- 1 0.8006544
- 2 0.1
- З 1.253828

RUNS COVID/asa usr out 28-Mississippi final cost value = 0.000463057Parameter Value

- 0 0.1097083
- 1 0.6931913
- 2 0.1054405
- 3 0.9913985

RUNS COVID/asa usr out 29-Missouri final cost value = 0.000257466Parameter Value

- 0 0.05215969
- 1 0.8596338
- 2 0.1
- 3 1.055173

RUNS COVID/asa\_usr\_out\_30-Montana final cost value = 0.0004428111Parameter Value

- 0 0.03814208
- 1 0.899361
- 2 0.1
- З 0.9560651

RUNS COVID/asa usr out 31-Nebraska final cost value = 0.0003267622Parameter Value

- 0 0.04517647
- 1 0.8218373
- 2 0.1
- 3 1.145402

RUNS COVID/asa usr out 32-Nevada final cost value = 0.001893444Parameter Value

- 0 0.03241173
- 1 0.9219539
- 2 0.1
- 3 1.156847

RUNS\_COVID/asa\_usr\_out\_33-New\_Hampshire final cost value = 0.003540204Parameter Value

- 0 0.05990541 1
- 0.713824
- 2 1.999386
- 3 0.5164278

RUNS COVID/asa usr out 34-New Jersey final cost value = 0.003764219Parameter Value

- 0 2
- 1 0.3257865
- 2 2
- 3 1.048204

RUNS COVID/asa usr out\_35-New\_Mexico final cost value =  $0.00115\overline{2}665$ Parameter Value

- 0 0.1004785
- 1 0.695894
- 2 0.6817652
- 3 0.7827343

RUNS COVID/asa usr out 36-New York final cost value = 0.0007147068Parameter Value

- 0 0.04110297
- 1 0.7541359
- 2 0.1
- 3 1.054681

RUNS COVID/asa usr out 37-North Carolina final cost value = 0.0003851502

Parameter Value

- 0 0.08513204
- 1 0.7664615
- 2 0.1
- 3 1.003618

RUNS COVID/asa usr out 38-North Dakota final cost value =  $\overline{0.0003929314}$ Parameter Value

- 0 0.04932907
- 1 0.8614704
- 2 0.1
- 3 0.9475553

RUNS COVID/asa usr out 39-Northern Mariana Islands final cost value = 0.0110592

Parameter Value

- 0 0.03284899
- 1 0.6745235
- 2 0.1
- З 0.3440228

RUNS COVID/asa usr out 40-Ohio final cost value = 0.0004090411

Parameter Value

- 0 0.04184926
- 0.8463094 1
- 2 0.1
- 1.049081 3

RUNS COVID/asa\_usr\_out\_41-Oklahoma final cost value = 0.0004630219Parameter Value

- 0 0.04501715
- 1 0.8799497
- 2 0.3494903
- 3 0.9048175

RUNS COVID/asa usr out 42-Oregon final cost value = 0.0009208029

Parameter Value

- 0 0.05225226
- 1 0.816799
- 2 0.2053155
- 3 0.9100787

RUNS COVID/asa usr out 43-Pennsylvania final cost value = 0.0005589026Parameter Value

- - 0 0.04241694
  - 1 0.8052484
  - 2 0.1
  - З 1.015383

RUNS\_COVID/asa\_usr\_out\_44-Puerto\_Rico final cost value = 0.000312391Parameter Value

0 0.03449601

- 1 0.9045291
- 2 0.1
- З 1.088644

RUNS\_COVID/asa\_usr\_out\_45-Rhode\_Island final cost value = 0.0111474Parameter Value

- 0 0.04708741
- 1 0.7901072
- 2 0.1
- 3 1.442058

RUNS COVID/asa usr out 46-South Carolina final cost value = 0.0009722008Parameter Value

- 0 0.09290075
- 1 0.7718165
- 2 0.1
- 3 1.095007

RUNS COVID/asa usr out 47-South Dakota final cost value = 0.0003353859

Parameter Value

- 0 0.05975135
- 1 0.7782754
- 2 0.1
- 0.9210539 3

RUNS COVID/asa usr out 48-Tennessee final cost value = 0.0005178384 Parameter Value

- 0 0.09073933
- 1 0.7754924
- 2 2
- 3 0.8461525

RUNS COVID/asa usr out 49-Texas final cost value = 0.0001681769Parameter Value

- 0 0.05172033
- 1 0.8703259
- 2 0.1
- 3 1.330712

RUNS COVID/asa usr out 50-US final cost value = 1.27974e-05Parameter Value

- 0 0.05285717
- 1 0.8271716
- 2 0.1090954
- 3 1.204249

RUNS COVID/asa usr out 51-Utah final cost value = 0.003623466Parameter Value

- 0 0.04933961
- 1 0.8573352
- 2 0.1
- 3 1.086935

2021

RUNS\_COVID/asa\_usr\_out\_52-Vermont final cost value = 0.0008160128 Parameter Value

- 0 0.006796208
- 1 0.9282152
- 2 0.1
- 3 0.4539584

RUNS\_COVID/asa\_usr\_out\_53-Virgin\_Islands final cost value = 0.03999473 Parameter Value

- 0 0.06337426
  - 1 0.8251611
  - 2 0.1
  - 2 0.1
  - 3 1.064258

RUNS\_COVID/asa\_usr\_out\_54-Virginia final cost value = 0.0001637778 Parameter Value

- 0 0.05090517
- 1 0.8072254
- 2 0.1
- 3 0.9941458

RUNS\_COVID/asa\_usr\_out\_55-Washington final cost value = 0.0005114633 Parameter Value

- 0 0.05293824
- 1 0.8114288
- 2 0.1
- 3 1.026359

RUNS\_COVID/asa\_usr\_out\_56-West\_Virginia final cost value = 0.0004020269 Parameter Value

- 0 0.02179989
- 1 0.9542683
- 2 0.1
- 3 0.8805843

RUNS\_COVID/asa\_usr\_out\_57-Wisconsin final cost value = 0.0005233912 Parameter Value

0 0.05836374

- 1 0.8373115
- 2 0.1
- 2 0.1
- 3 1.251952

RUNS\_COVID/asa\_usr\_out\_58-Wyoming final cost value = 0.0008048018 Parameter Value

- 0 0.05755666
- 1 0.7254984
- 3 0.8178418

## VI. CONCLUSION

Two algorithms are suggested for fitting data and forecasting COVID-19, ASA for importancesampling and fitting parameters to models, and PATHINT/PATHTREE. These algorithms have been applied to several disciplines — neuroscience, financial markets, combat analysis. While optimization and pathintegral algorithms are now quite well-known (at least to many scientists), these previous applications give strong support to application of these tools to COVID-19 data.

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